

# REACHING BEYOND THE ELECTROWEAK SCALE:

Giant  $K$ -factors, **FAT** jets and 

Gavin Salam

CERN, Princeton & LPTHE/CNRS (Paris)

based on work with Matteo Cacciari, Mathieu Rubin, Sebastian Sapeta & Gregory Soyez

CMS Week  
CERN, 30 March 2011

# REACHING BEYOND THE ELECTROWEAK SCALE:

Giant *K*-factors, **FAT** jets and pileup  
pileup  
pileup  
pileup  
pileup  
pileup

Gavin Salam

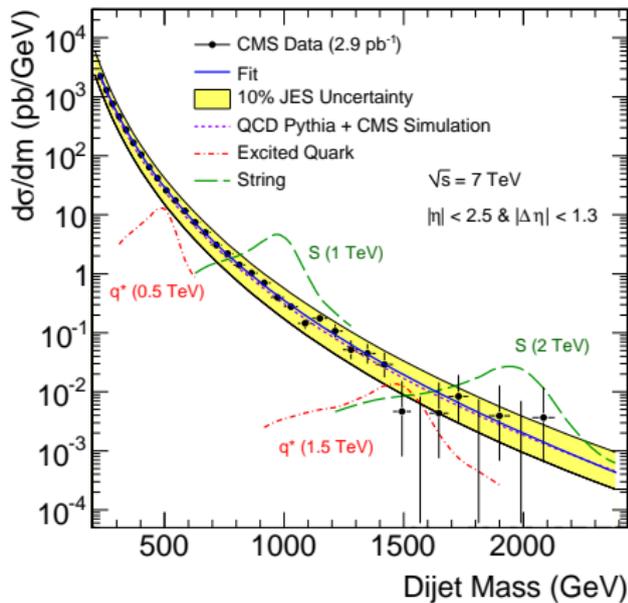
CERN, Princeton & LPTHE/CNRS (Paris)

based on work with Matteo Cacciari, Mathieu Rubin, Sebastian Sapeta & Gregory Soyez

CMS Week  
CERN, 30 March 2011

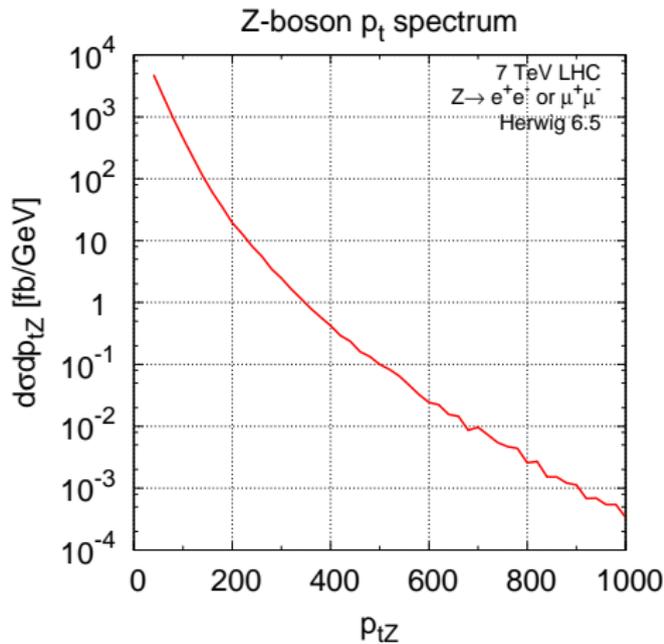
CMS has so far probed strongly-interacting physics far beyond the electroweak scale. For example di-jet resonance and supersymmetry searches.

With the forthcoming few  $\text{fb}^{-1}$ , strongly interacting physics will be taken to the multi-TeV scale and electroweak physics close to the TeV scale.



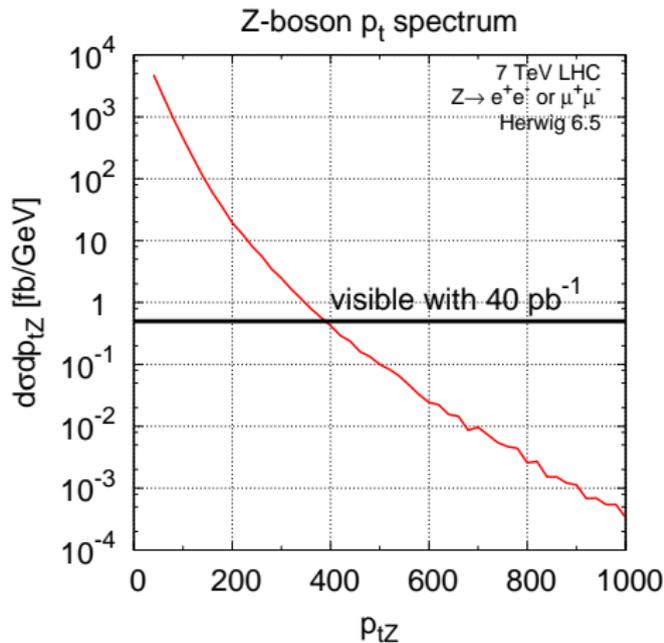
CMS has so far probed strongly-interacting physics far beyond the electroweak scale. For example di-jet resonance and supersymmetry searches.

With the forthcoming few  $\text{fb}^{-1}$ , strongly interacting physics will be taken to the multi-TeV scale and electroweak physics close to the TeV scale.



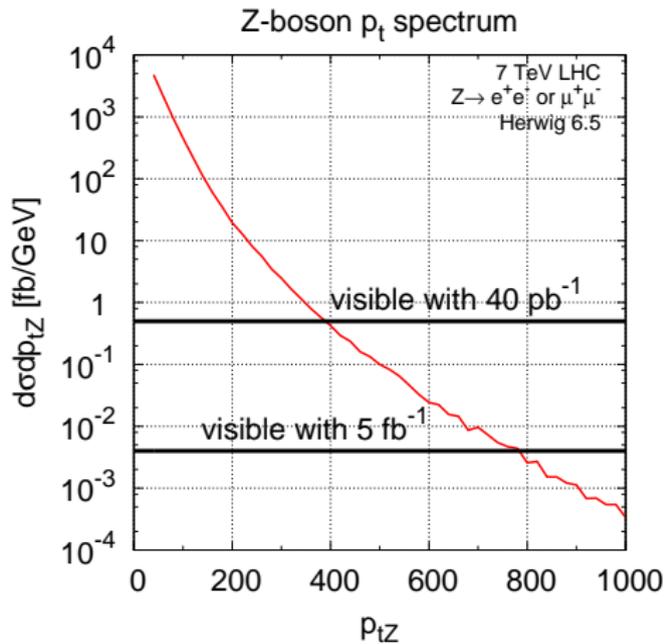
CMS has so far probed strongly-interacting physics far beyond the electroweak scale. For example di-jet resonance and supersymmetry searches.

With the forthcoming few  $\text{fb}^{-1}$ , strongly interacting physics will be taken to the multi-TeV scale and electroweak physics close to the TeV scale.



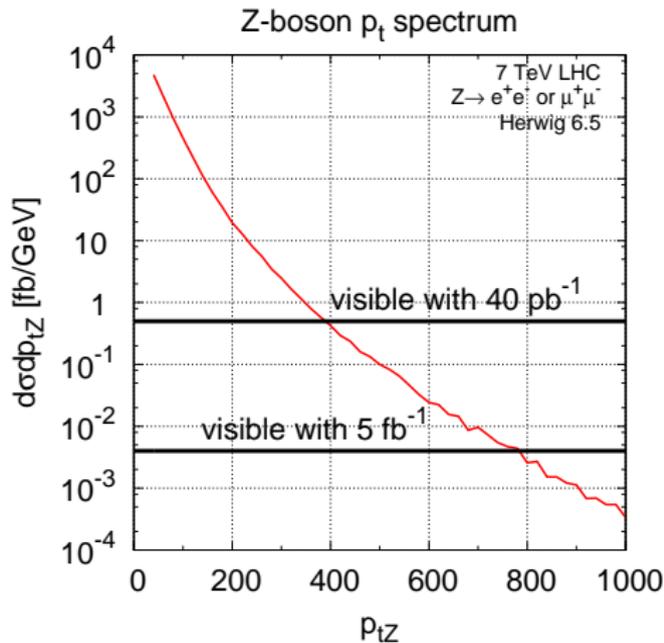
CMS has so far probed strongly-interacting physics far beyond the electroweak scale. For example di-jet resonance and supersymmetry searches.

With the forthcoming few  $\text{fb}^{-1}$ , strongly interacting physics will be taken to the multi-TeV scale and electroweak physics close to the TeV scale.



CMS has so far probed strongly-interacting physics far beyond the electroweak scale. For example di-jet resonance and supersymmetry searches.

With the forthcoming few  $\text{fb}^{-1}$ , strongly interacting physics will be taken to the multi-TeV scale and electroweak physics close to the TeV scale.



What's characteristically new as we approach the TeV scale with EW-scale objects?

W's, Z's, Higgses and even top-quarks all become **light**

Giving  $p_t \sim 1$  TeV to a Z-boson is analogous to giving  $p_t \sim 50$  GeV to a B-hadron.

**This can have implications for:**

1. the convergence of perturbative QCD
2. the methods used for reconstruction

And as a side effect of the high luminosities, you need to deal with large amounts of pileup

# Giant $K$ factors

# How accurate is perturbative QCD?

$$\sigma = c_0 + c_1\alpha_s + c_2\alpha_s^2 + \dots$$

$$\alpha_s \simeq 0.1$$

That implies LO QCD (just  $c_0$ )  
should be accurate to within 10%

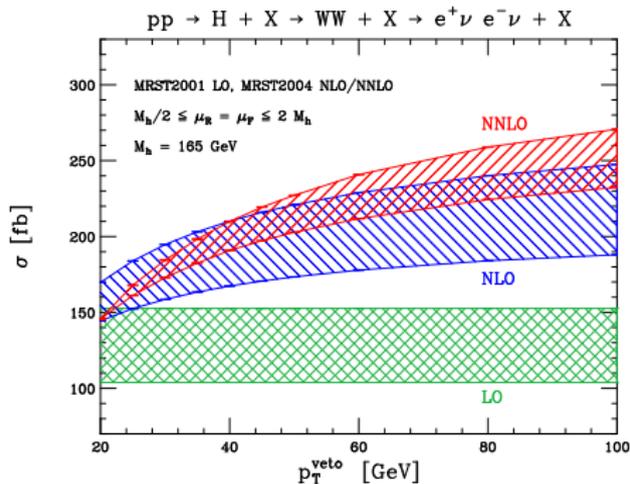
It isn't

Rules of thumb:

LO good to within factor of 2

NLO good to within scale  
uncertainty

This drives our understanding of accuracy of QCD predictions;  
e.g. when combining QCD with data-driven background estimates



$$\sigma = c_0 + c_1 \alpha_s + c_2 \alpha_s^2 + \dots$$

$$\alpha_s \simeq 0.1$$

That implies LO QCD (just  $c_0$ ) should be accurate to within 10%

**It isn't**

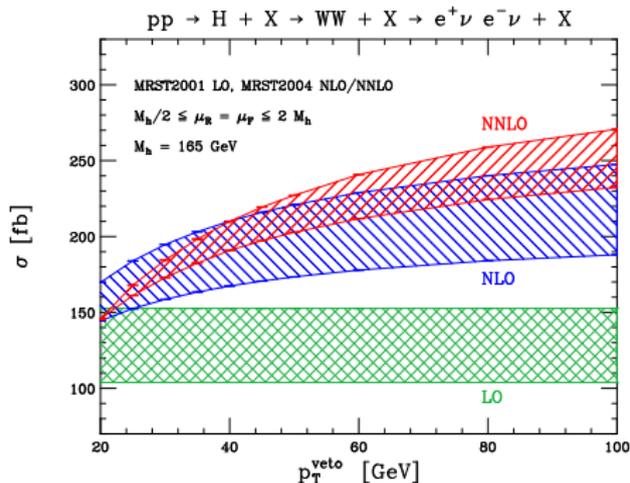
Rules of thumb:

LO good to within factor of 2

NLO good to within scale uncertainty

Anastasiou, Melnikov & Petriello '04  
 Anastasiou, Dissertori & Stöckli '07

This drives our understanding of accuracy of QCD predictions;  
 e.g. when combining QCD with data-driven background estimates



$$\sigma = c_0 + c_1 \alpha_s + c_2 \alpha_s^2 + \dots$$

$$\alpha_s \simeq 0.1$$

That implies LO QCD (just  $c_0$ ) should be accurate to within 10%

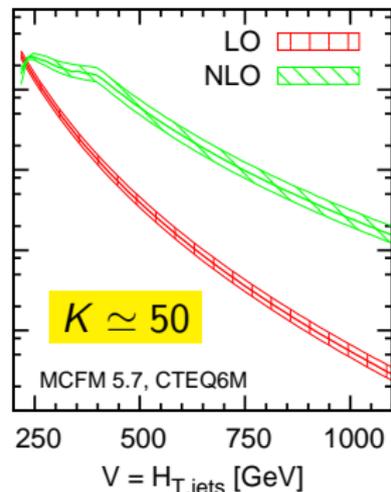
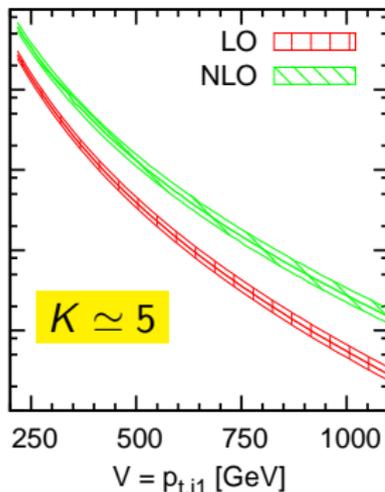
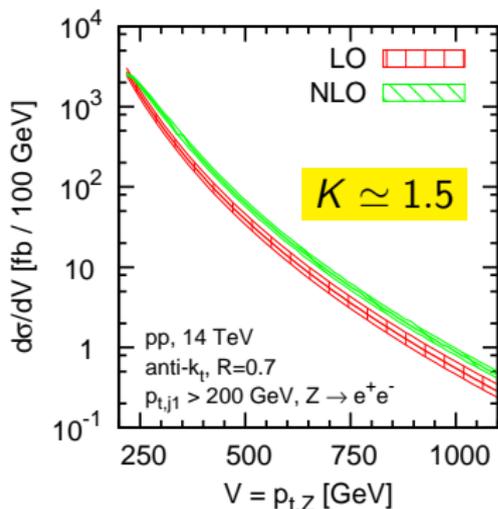
**It isn't**

Rules of thumb:

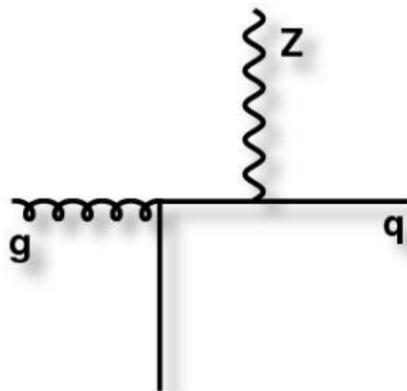
LO good to within factor of 2

NLO good to within scale uncertainty

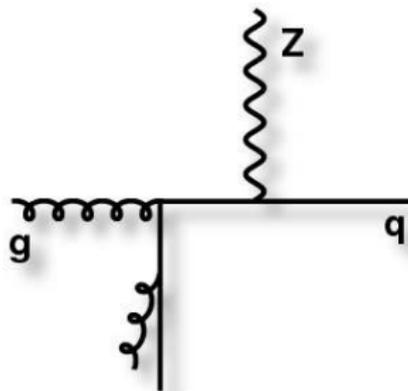
**This drives our understanding of accuracy of QCD predictions; e.g. when combining QCD with data-driven background estimates**

QCD convergence can fail badly — eg.  $Z$ +jet $p_t$  of Z-boson $p_t$  of jet 1 $H_{T,jets} = \sum_{jets} p_{t,j}$ **“Giant  $K$ -factors”**

They're not just large; they often depend on  $p_t$ ;  
and they can even have kinks

Leading Order

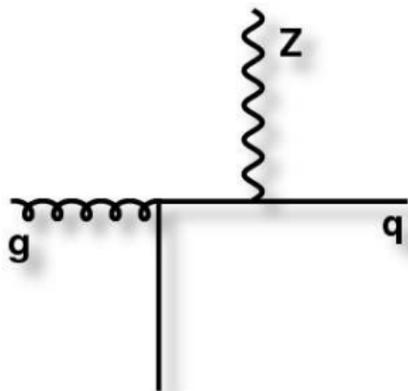
$$\alpha_s \alpha_{EW}$$

Next-to-Leading Order

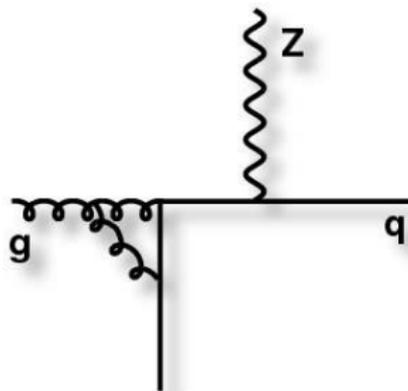
$$\alpha_s^2 \alpha_{EW}$$

New logarithmically enhanced topologies appear because EW bosons are light;  $M_Z \ll \sqrt{s}$

Also: new partonic channels at NLO,  $qq$  scattering with large PDF lumi

Leading Order

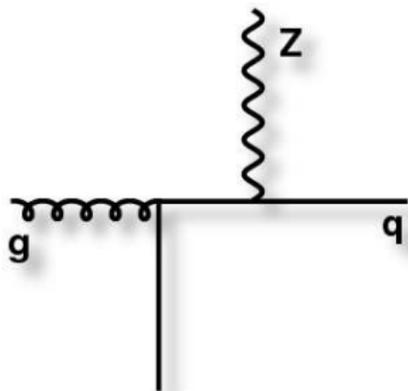
$$\alpha_s \alpha_{EW}$$

Next-to-Leading Order

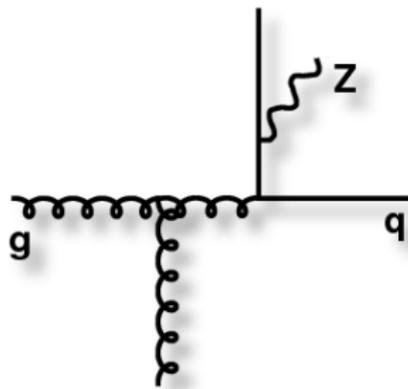
$$\alpha_s^2 \alpha_{EW}$$

New logarithmically enhanced topologies appear because EW bosons are light;  $M_Z \ll \sqrt{s}$

Also: new partonic channels at NLO,  $q\bar{q}$  scattering with large PDF lumi

Leading Order

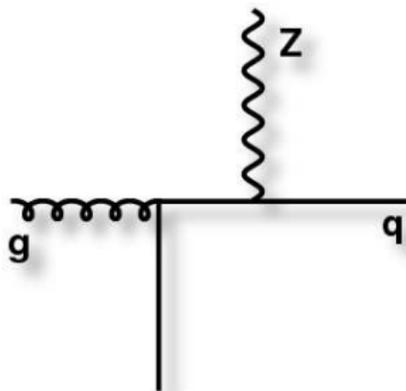
$$\alpha_s \alpha_{EW}$$

Next-to-Leading Order

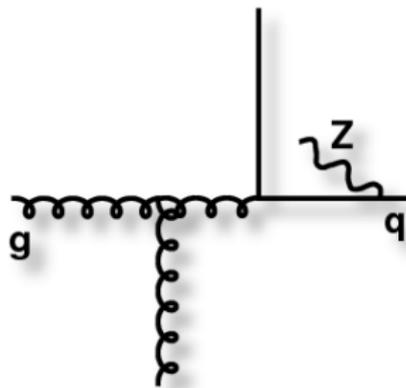
$$\alpha_s^2 \alpha_{EW} \ln^2 \frac{p_t}{M_Z}$$

**New logarithmically enhanced topologies appear because EW bosons are light;  $M_Z \ll \sqrt{s}$**

Also: new partonic channels at NLO,  $qq$  scattering with large PDF lumi

Leading Order

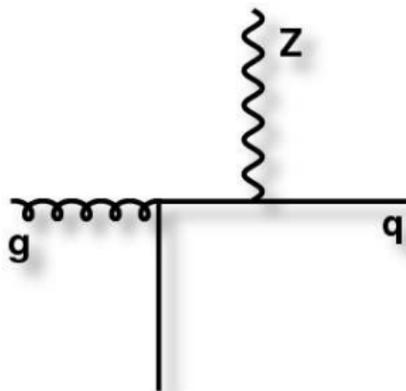
$$\alpha_s \alpha_{EW}$$

Next-to-Leading Order

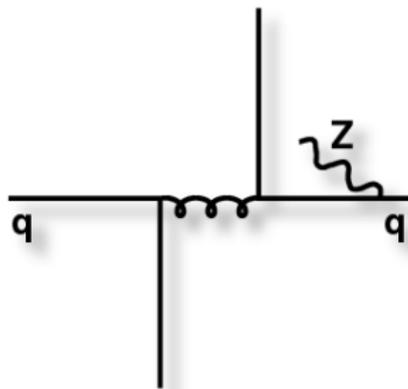
$$\alpha_s^2 \alpha_{EW} \ln^2 \frac{p_t}{M_Z}$$

**New logarithmically enhanced topologies appear because EW bosons are light;  $M_Z \ll \sqrt{s}$**

Also: new partonic channels at NLO,  $qq$  scattering with large PDF lumi

Leading Order

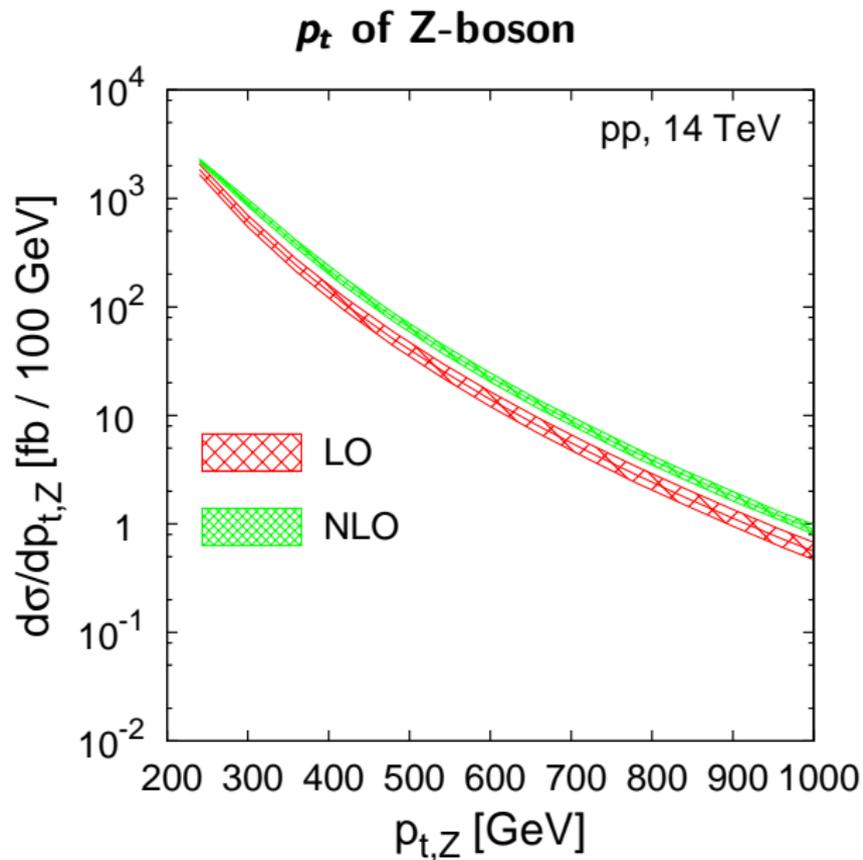
$$\alpha_s \alpha_{EW}$$

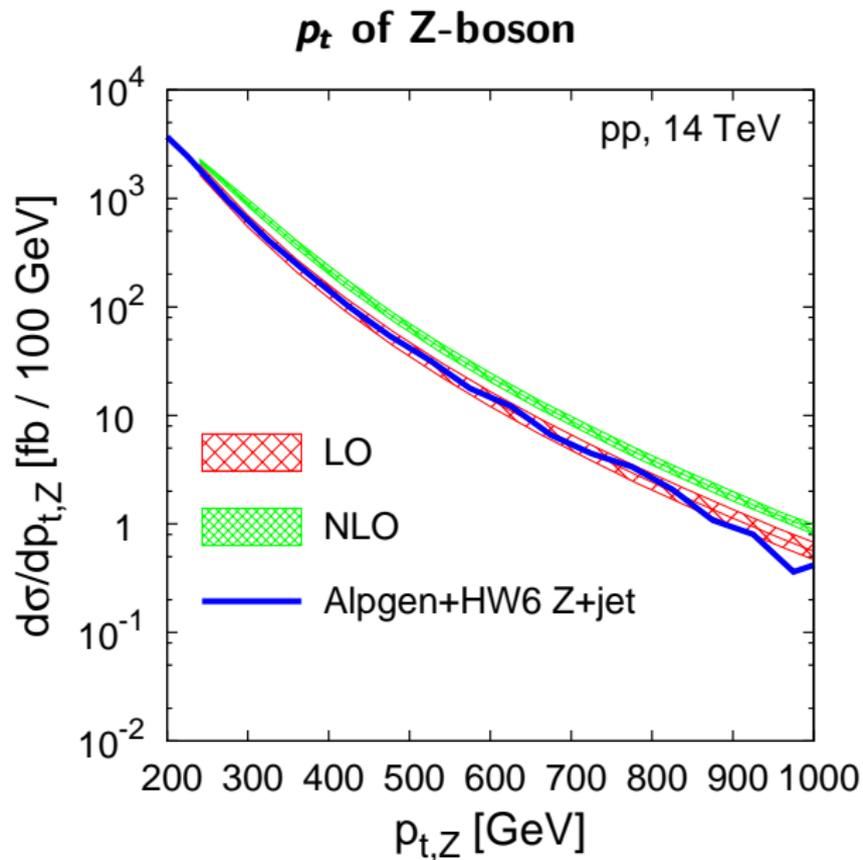
Next-to-Leading Order

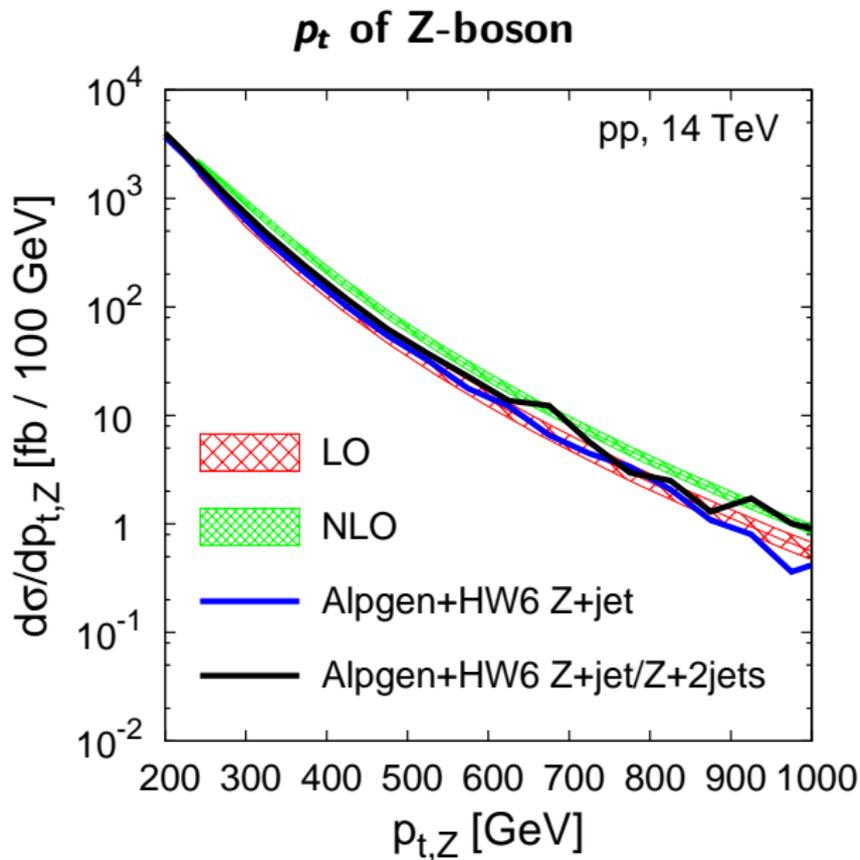
$$\alpha_s^2 \alpha_{EW} \ln^2 \frac{p_t}{M_Z}$$

**New logarithmically enhanced topologies appear because EW bosons are light;  $M_Z \ll \sqrt{s}$**

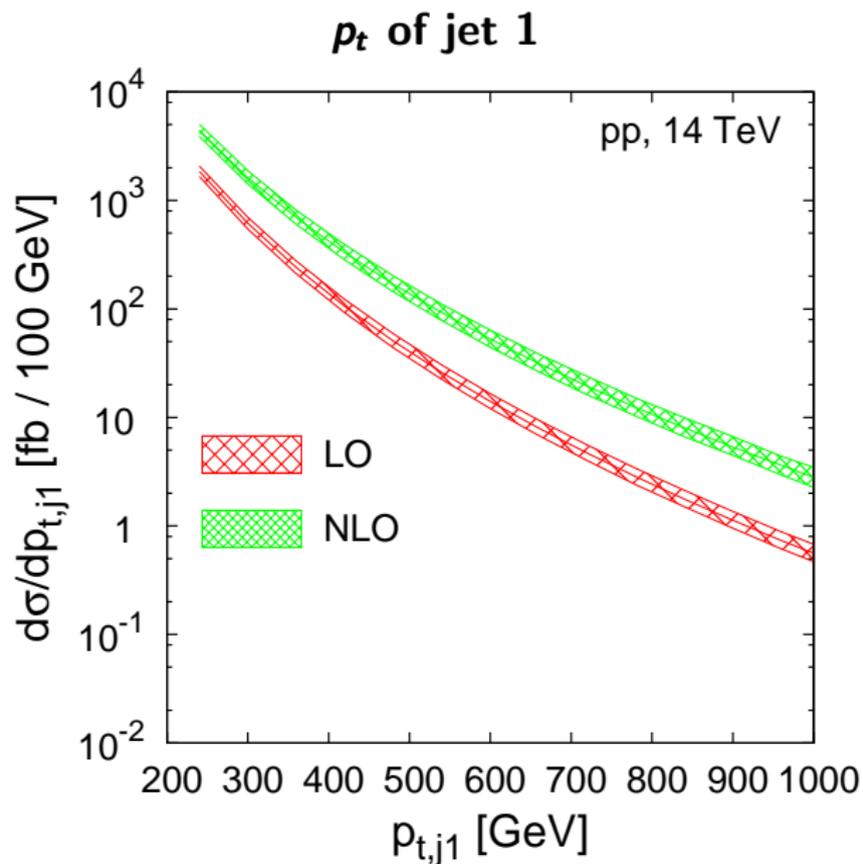
Also: new partonic channels at NLO,  $qq$  scattering with large PDF lumi

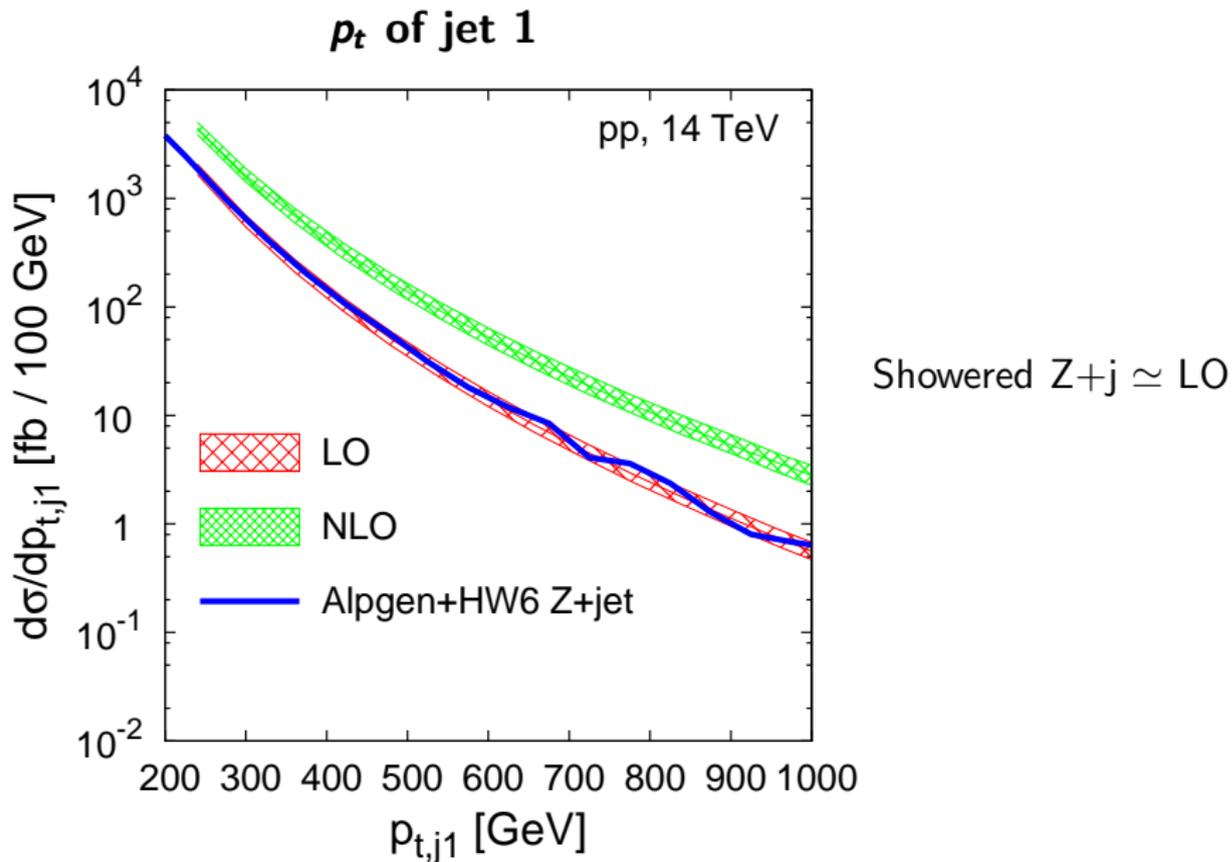


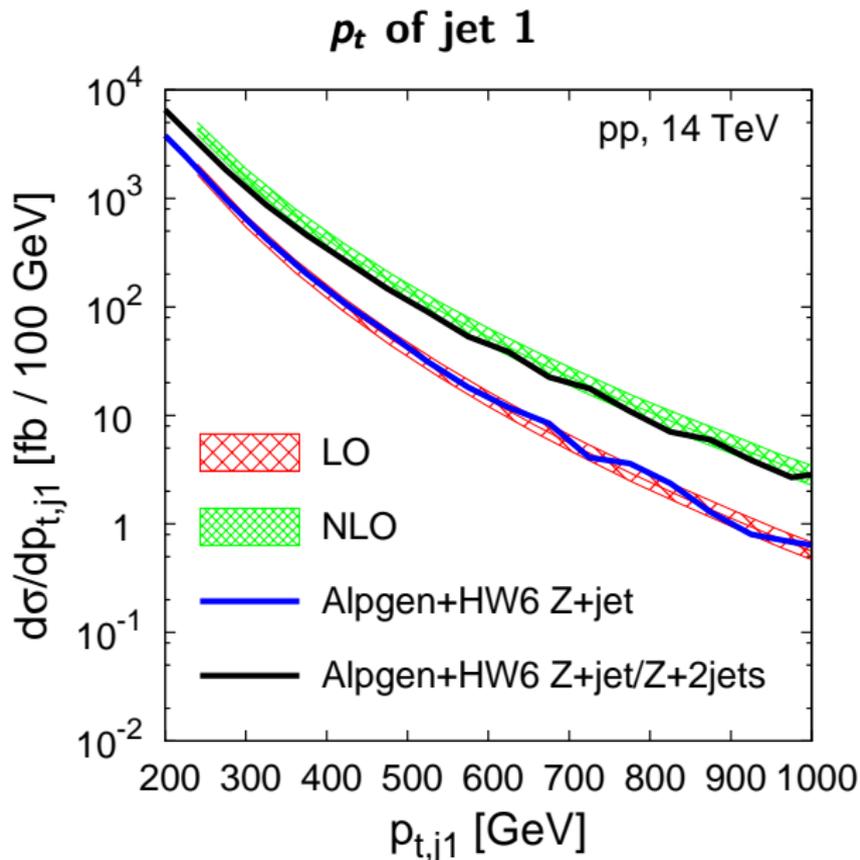




All predictions similar  
and stable

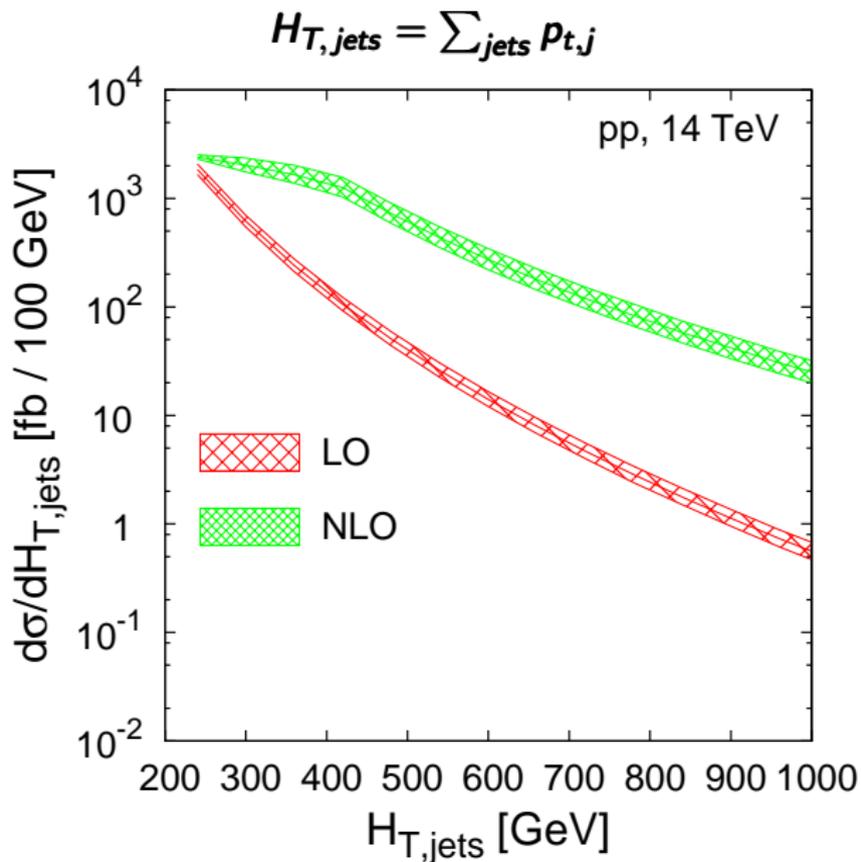


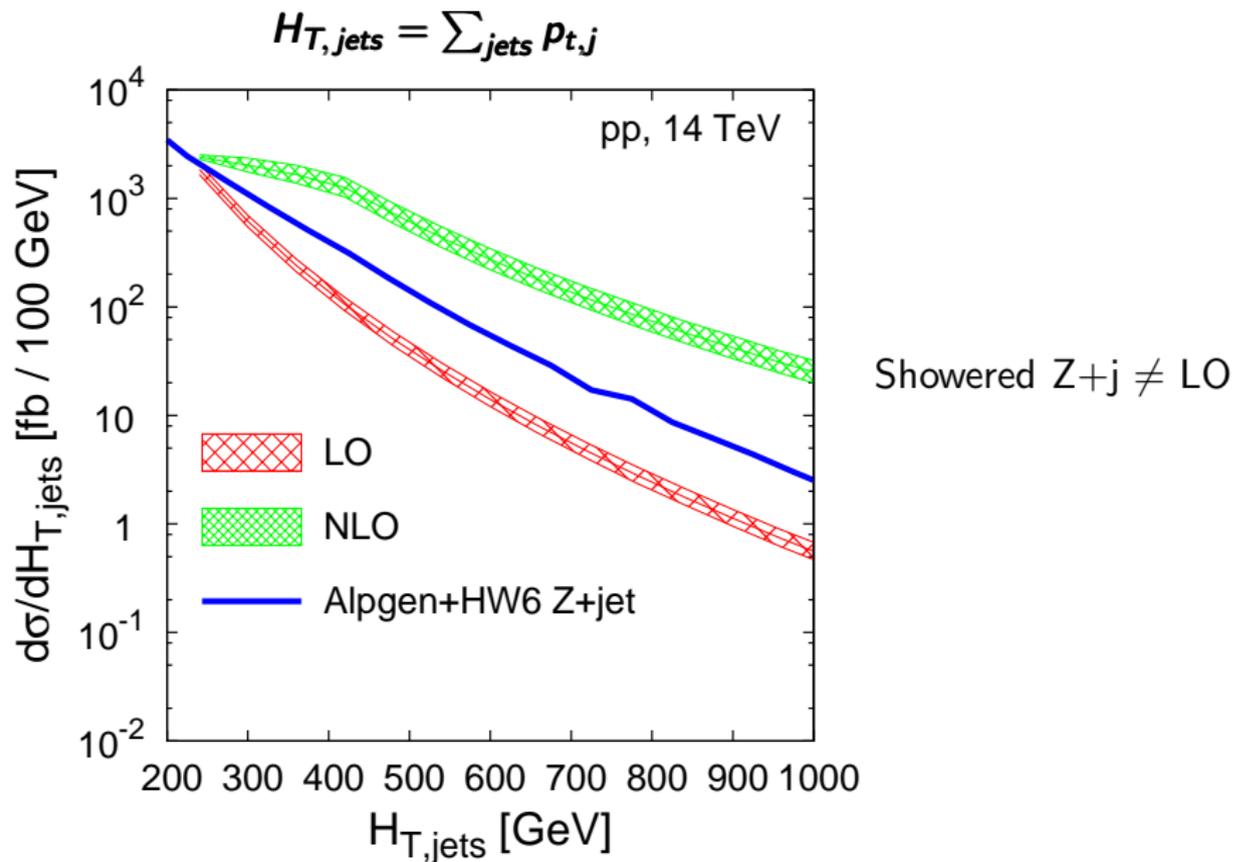


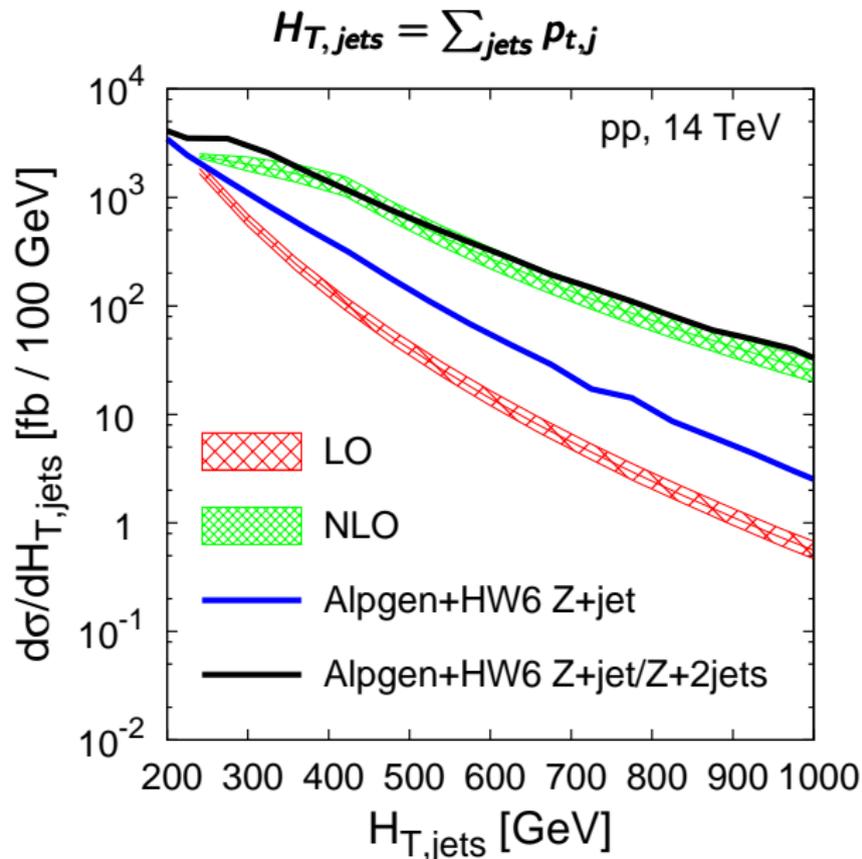


Showered Z+j  $\simeq$  LO

Showered Z+j/Z+2j  
 $\simeq$  NLO







Showered Z+j  $\neq$  LO

Showered Z+j/Z+2j  
 $\simeq$  NLO

# 1st lesson:

If you figure out the “leading” process

[Z + jet @ LO]

and add in process with one extra jet through  
MLM/CKKW matching.

[i.e. include Z + 2 jets @ LO]

impact of new large topologies will often show up

**This might be called “Pauper’s NLO”**

It’s reassuring that **suitable** use of Alpgen/Madgraph/... catches this.

[cf. also de Aquino et al ’11]

Is it always being used “suitably” (i.e. with extra jets)?

How do you get NLO normalisation for these samples?

# 1st lesson:

If you figure out the “leading” process

[Z + jet @ LO]

and add in process with one extra jet through  
MLM/CKKW matching.

[i.e. include Z + 2 jets @ LO]

impact of new large topologies will often show up

This might be called “Pauper’s NLO”

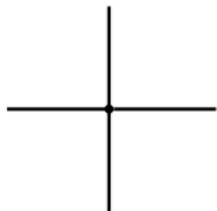
It’s reassuring that **suitable use** of Alpgen/Madgraph/... catches this.

[cf. also de Aquino et al ’11]

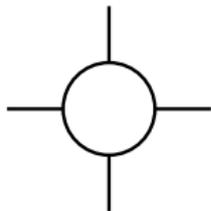
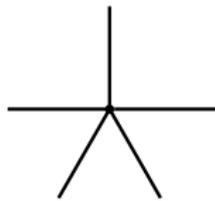
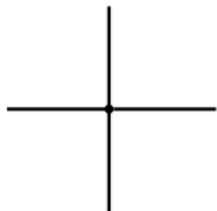
Is it always being used “suitably” (i.e. with extra jets)?

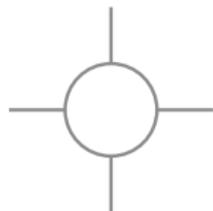
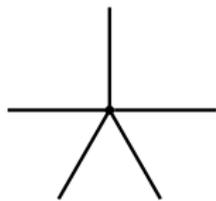
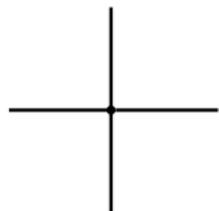
How do you get NLO normalisation for these samples?

LO



NLO



$\bar{n}LO$ 

MLM matching keeps the tree-level parts of NLO, but approximates the loops.

We denote this  $\bar{n}LO$

Can be a good approx. to NLO

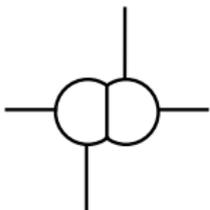
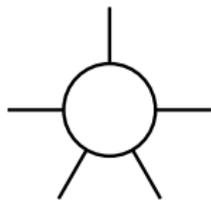
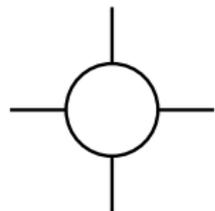
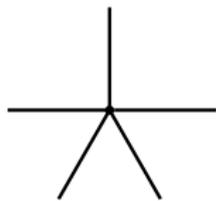
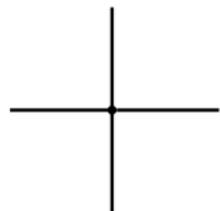


Exact



Approximate

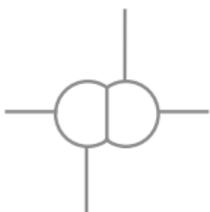
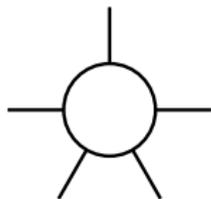
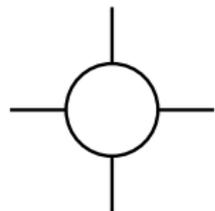
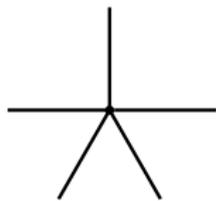
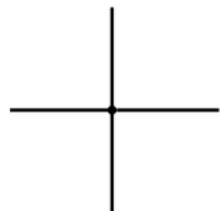
## NNLO



MLM matching keeps the tree-level parts of NLO, but approximates the loops.

We denote this  $\bar{n}\text{LO}$

Can be a good approx. to NLO

$\bar{n}$ NLO

Exact



Approximate

MLM matching keeps the tree-level parts of NLO, but approximates the loops.

We denote this  $\bar{n}$ LO

Can be a good approx. to NLO

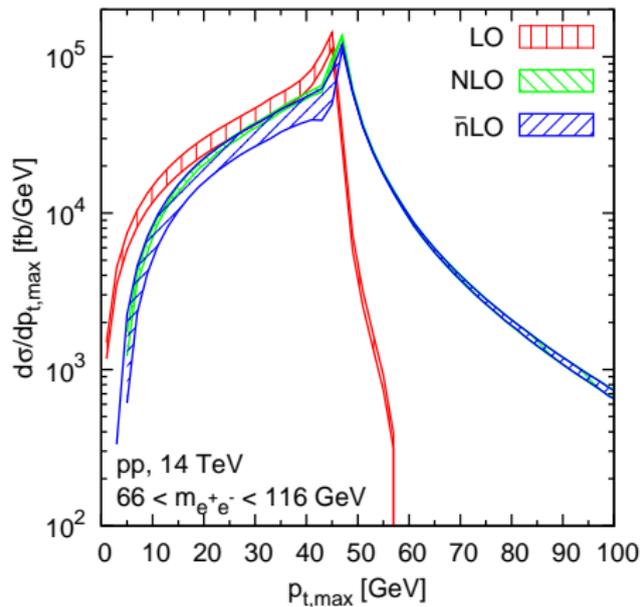
To approximate NNLO, take tree-level and 1-loop pieces (from NLO  $Z+j$  &  $Z+2j$ ) and approximate 2-loop part.

$\bar{n}$ LO, using “LoopSim”

NB: pure partonic; no shower MC

Rubin, GPS & Sapeta '10

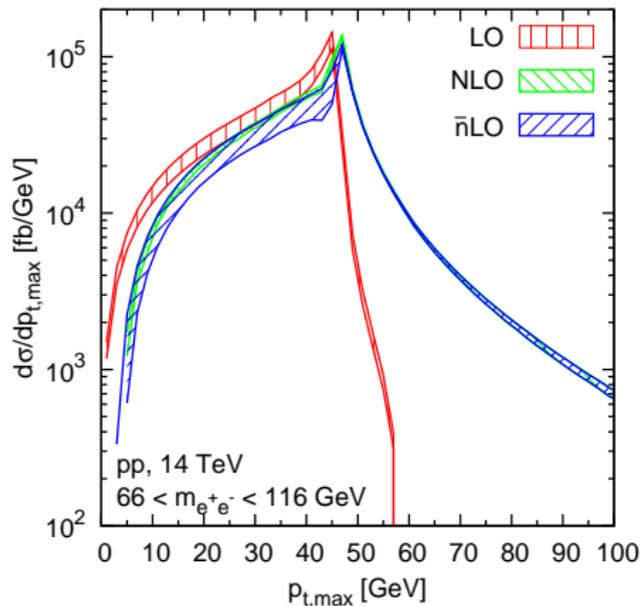
## $\bar{n}$ LO v. NLO



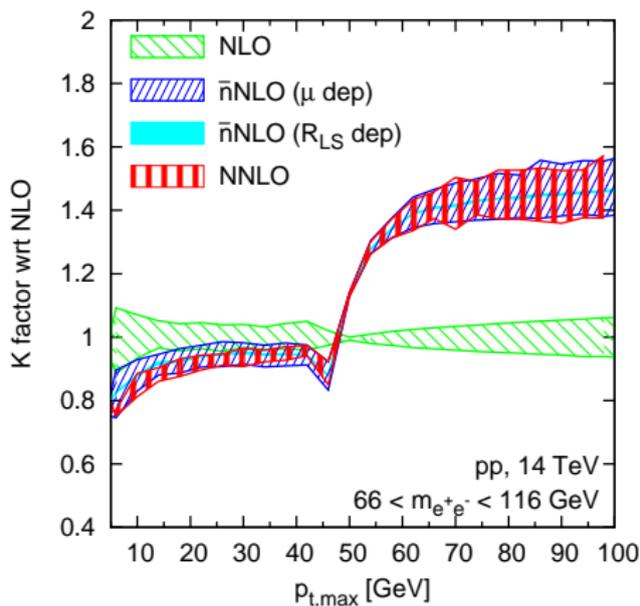
Z (i.e. DY) with Z+j from MCFM & LoopSim

For  $p_{t,l} \gtrsim \frac{1}{2}M_Z + \Gamma_Z$  (giant  $K$ -factor!) it had to work  
For  $p_{t,l} \lesssim \frac{1}{2}M_Z + \Gamma_Z$  it's remarkable that it still works

## $\bar{n}$ LO v. NLO



## $\bar{n}$ NLO v. NNLO

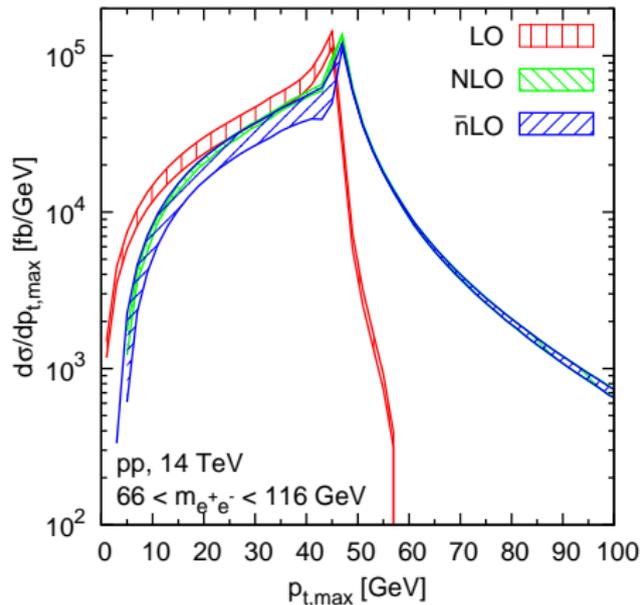


NNLO from DYNNOLO, Z (i.e. DY) with Z+j from MCFM & LoopSim

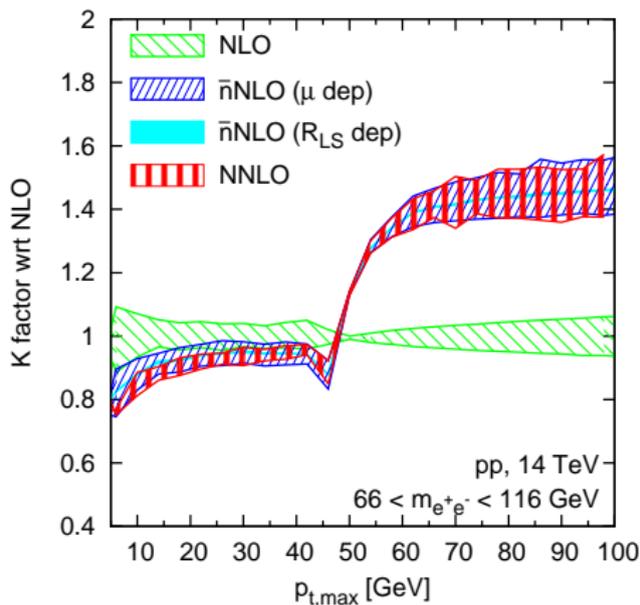
For  $p_{t,l} \gtrsim \frac{1}{2}M_Z + \Gamma_Z$  (giant  $K$ -factor!) it had to work  
 For  $p_{t,l} \lesssim \frac{1}{2}M_Z + \Gamma_Z$  it's remarkable that it still works

# Validation: Drell-Yan lepton $p_t$ , $\bar{n}$ NLO v. NNLO

## $\bar{n}$ LO v. NLO



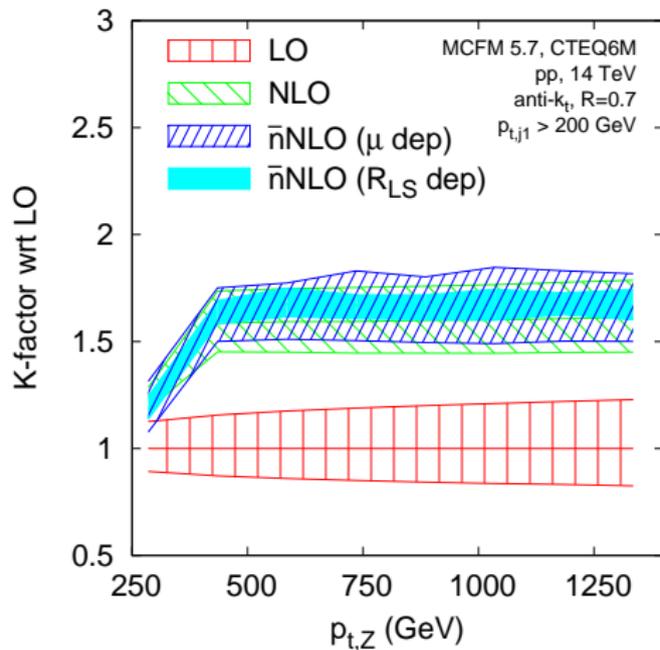
## $\bar{n}$ NLO v. NNLO



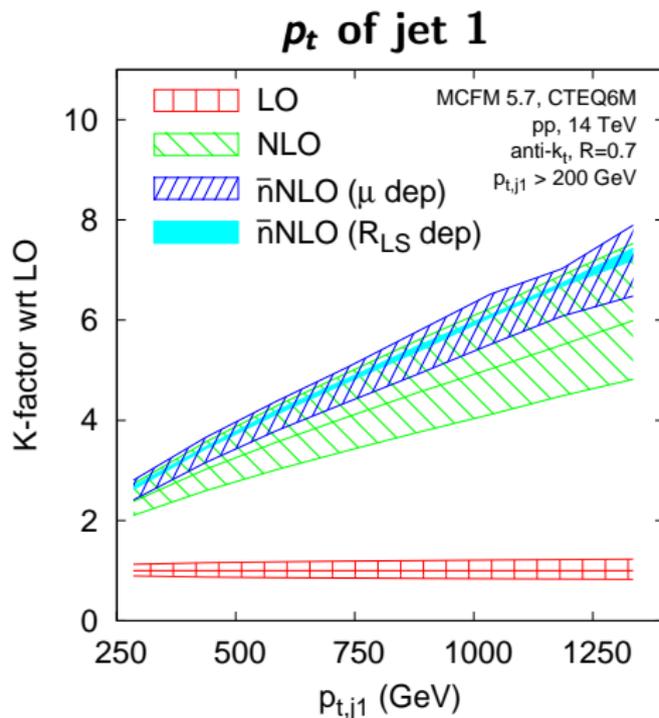
NNLO from DYNNOLO, Z (i.e. DY) with Z+j from MCFM & LoopSim

For  $p_{t,l} \gtrsim \frac{1}{2}M_Z + \Gamma_Z$  (giant  $K$ -factor!) it had to work  
 For  $p_{t,l} \lesssim \frac{1}{2}M_Z + \Gamma_Z$  it's remarkable that it still works

## $p_t$ of Z-boson

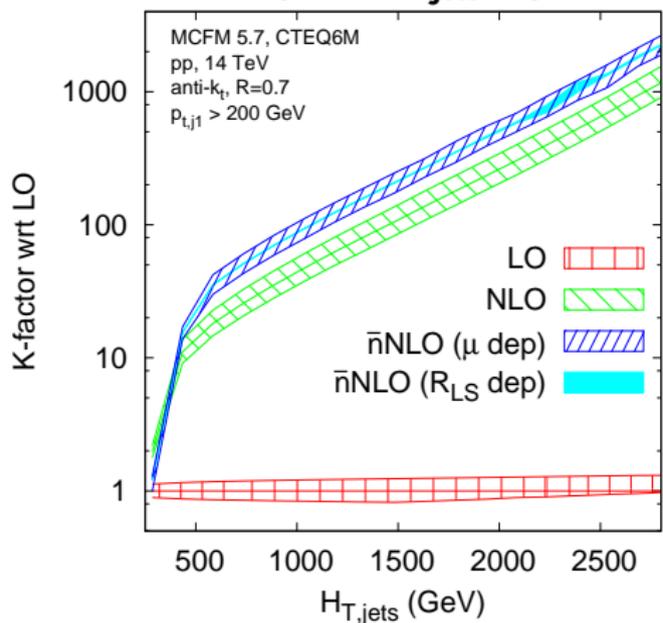


- ▶  $p_{tZ}$  distribution didn't have giant  $K$ -factors.
- ▶  $\bar{n}$ NLO brings no benefit
  - To get improvement you would need exact 2-loop terms



- ▶  $p_{tj}$  distribution seems to converge at  $\bar{n}$ NLO
- ▶ scale uncertainties reduced by  $\sim$  factor 2

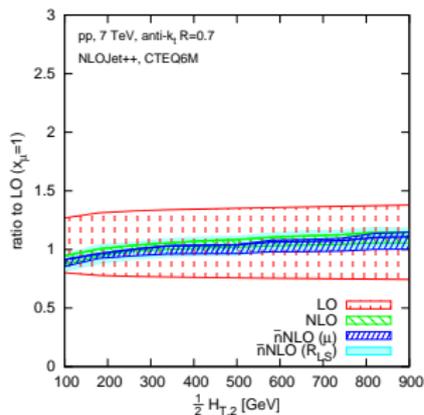
$$H_{T,jets} = \sum_{jets} p_{t,j}$$



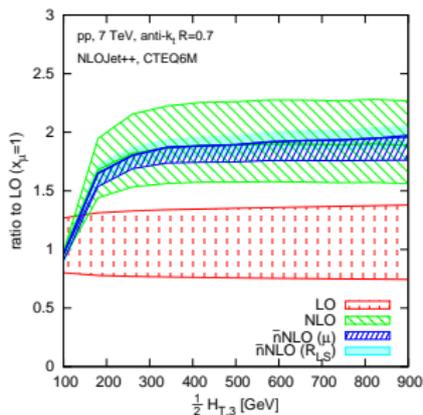
- ▶ Significant further enhancement for  $H_{T,jets}$
- ▶  $\bar{n}$ NLO brings clear message:

**$H_{T,jets}$  is not a good observable!**

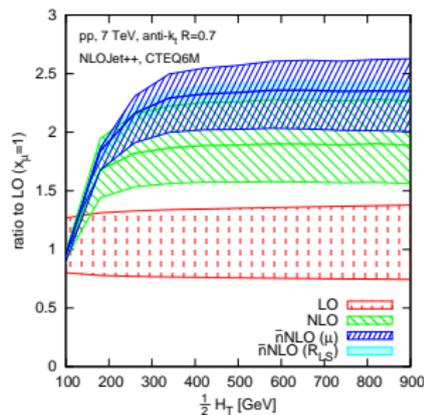
## $H_{T,2}$



## $H_{T,3}$



## $H_{T,\infty}$



**A clear message:**

for a process with  $n$  objects at lowest order, use  $H_{T,n}$

Do you know what gets used in your experiment's searches?

Many writers of LHC SUSY proceedings didn't...

**LoopSim, as it stands, should work for processes with zero or one vector bosons and any number of jets. Not yet public:**

- ▶ Interfaces to MCFM and NLOJet++ required more (or less) hacking  
and then very long run times
- ▶ Let us (Sebastian Sapeta, GPS) know if you need predictions

**Giant  $K$  factors are present in many contexts beyond those shown here, and may be directly relevant in searches**

e.g. with  $V\gamma$  backgrounds

- ▶ You can check for giant  $K$  factors, by comparing LO & NLO
- ▶ Watch out for how  $H_T$  is defined in searches:

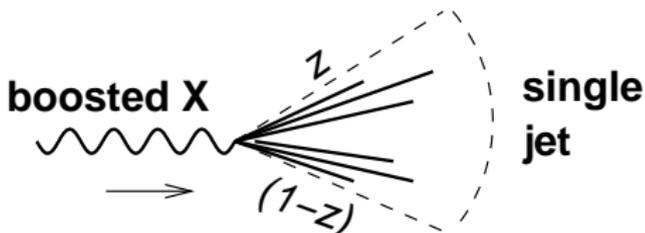
**Rule of thumb(?):**  $H_T$  should sum over all non-jet objects and at most as many jets as are present in the signal

Another “side-effect” of having  $\sqrt{s} \gg M_{EW}$ :  
Hadronically decaying boosted Z/W/H/tops  
a.k.a. Fat Jets

What’s new?

a number of recent papers — more than can be reviewed here

## Hadronically decaying EW boson at high $p_t \neq$ two jets



$$R \gtrsim \frac{m}{p_t} \frac{1}{\sqrt{z(1-z)}}$$

### Rules of thumb:

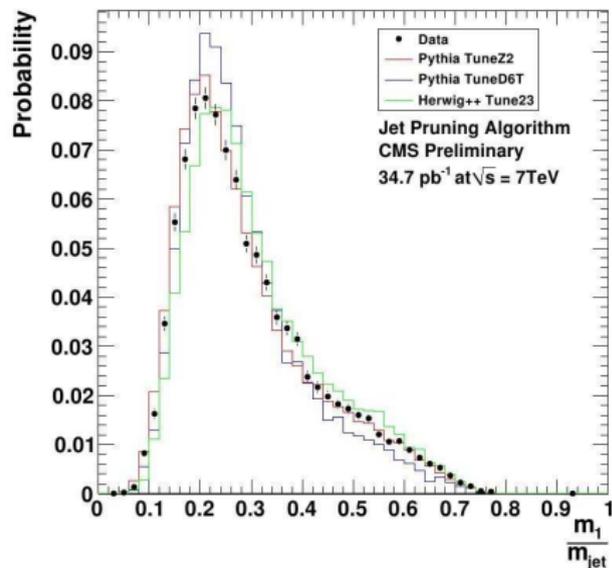
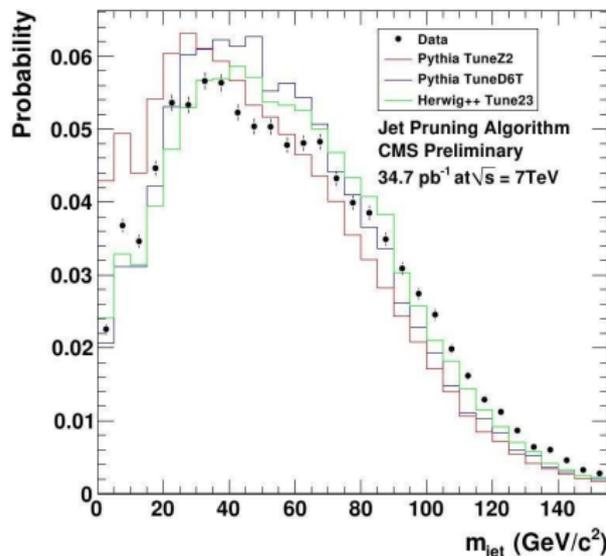
$$m = 100 \text{ GeV}, p_t = 500 \text{ GeV}$$

▶  $R < \frac{2m}{p_t}$ : always resolve **two** jets

$$R < 0.4$$

▶  $R \gtrsim \frac{3m}{p_t}$ : resolve **one** jet in 75% of cases ( $\frac{1}{8} < z < \frac{7}{8}$ )

$$R \gtrsim 0.6$$



Important: confirms general MC reliability for background predictions in this hitherto relatively untested region.

Interesting Herwig++ does remarkably well

Looking for 2 “top” jets:

- ▶ each with  $130 < m < 210$  GeV
- ▶ leading one with  $p_t > 400$  GeV

---

Expected $t\bar{t}$	$3 \pm 0.8$
---------------------	-------------

---

Expected background	$11 \pm 4.6$
---------------------	--------------

---

Observed	30
----------	----

---

CDF also sees an excess  
in tri-jet mass for 6-jet events

Looking for 2 “top” jets:

- ▶ each with  $130 < m < 210$  GeV
- ▶ leading one with  $p_t > 400$  GeV

Expected $t\bar{t}$	$3 \pm 0.8$
---------------------	-------------

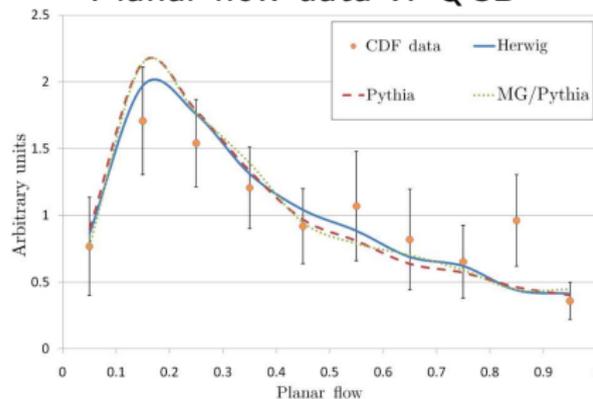
Expected background	$11 \pm 4.6$
---------------------	--------------

Observed	30
----------	----

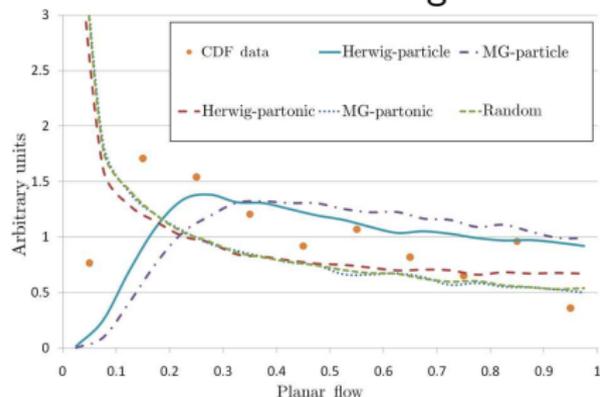
CDF also sees an excess  
in tri-jet mass for 6-jet events

Diagnostic: a jet shape variable,  
**planar flow**

Planar flow data v. QCD



Planar flow data v. gluino



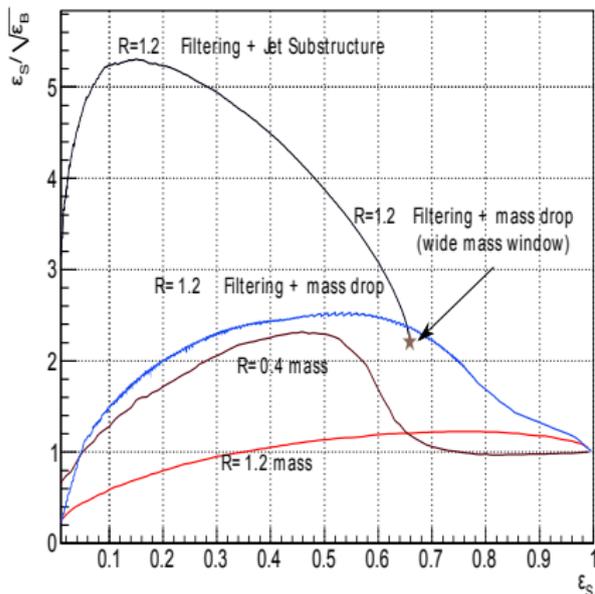
- ▶ Using matrix-element methods for the substructure Done analytically  
Soper & Spannowsky '11  
Most "physically interesting"
- ▶ Using jet shapes. E.g. subjettness: break a jet into subjets 1, 2, ... N

$$S_N = \frac{1}{p_t} \sum_i p_{ti} \min(\delta R_{i1}, \dots, \delta R_{iN})$$

J-H Kim '10; Thaler & Van Tilburg '10

- ▶ Using boosted decision trees  
Cui, Han & Schwartz '10; seems powerful

Cui et al BDT v. BRDS



Biggest improvements are to be had at moderate signal efficiencies

Conclusion from Boost 2010 comparison study of top taggers  
The method to be adopted depends on the signal efficiency you want

# Pileup

high  $p_t \rightarrow$  requires high lumi  $\rightarrow$  high pileup

28/03/2011

LHC 8:30 meeting

## 2011 Records



3.5 TeV

Items in red are records set in the past week

Peak Stable Luminosity Delivered	2.49x10 <sup>32</sup>	Fill 1645	11/03/22, 17:12
Maximum Peak Events per Bunch Crossing	13.08	Fill 1644	11/03/22, 02:20
Maximum Average Events per Bunch Crossing	8.93	Fill 1644	11/03/22, 02:20

$\gtrsim 10$  events per bunch crossing  
 $\mathcal{O}(10 \text{ GeV})$  of extra  $p_t$  per jet, with large fluctuations

$$p_{t,jet}^{\text{subtracted}} = p_{t,jet} - \rho \times A_{jet}$$

Cacciari, GPS & Soyez '08

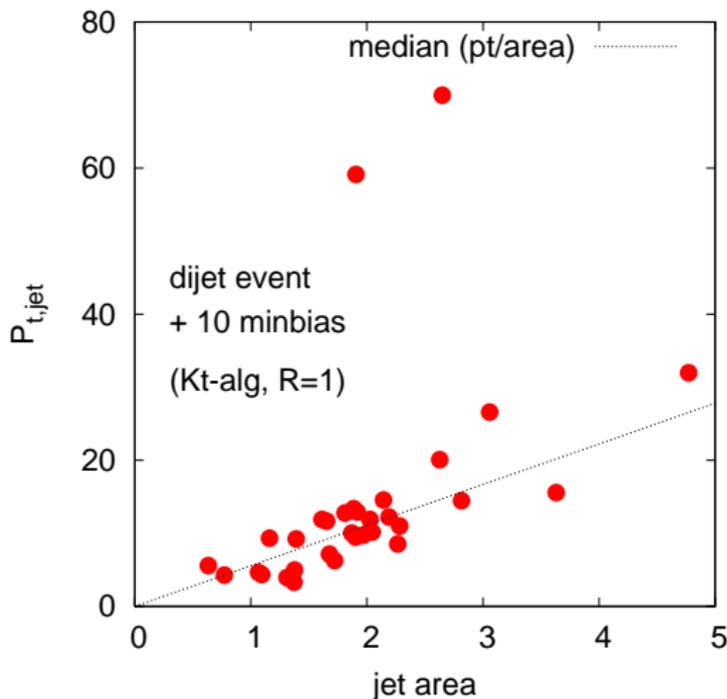
$A_{jet}$  = jet area

$\rho$  =  $p_t$  per unit area from pileup  
(or “background”)

This procedure is intended to be common to pp ( $\rho \sim 1-2$  GeV), pp with pileup ( $\rho \sim 2-15$  GeV) and Heavy-Ion collisions ( $\rho \sim 100-300$  GeV)

**As proposed so far: jet-by-jet area determination,  
event-by-event  $\rho$  determination**

## IN A SINGLE EVENT



Most jets in event are “background”

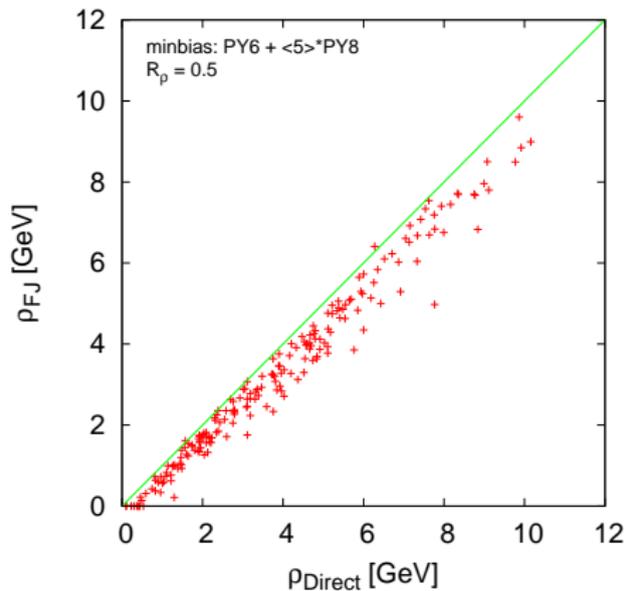
Their  $p_t$  is correlated with their area.

**Estimate  $\rho$ :**

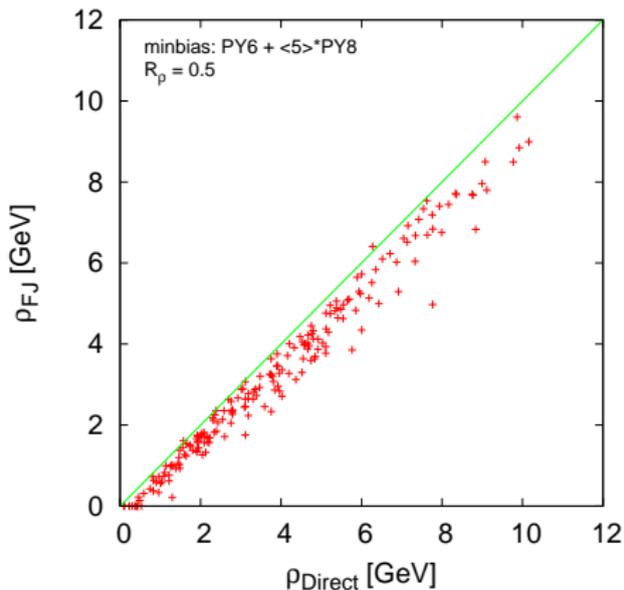
$$\rho \simeq \text{median}_{\{jets\}} \left[ \frac{p_{t,jet}}{A_{jet}} \right]$$

Median limits bias  
from hard jets  
Cacciari & GPS '07

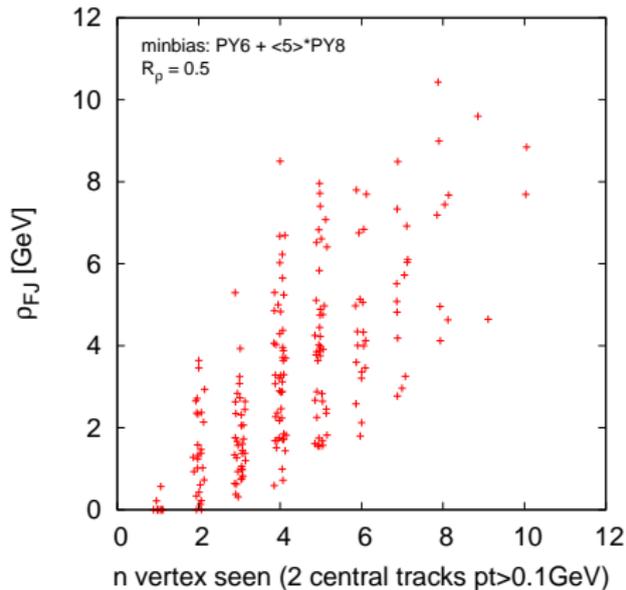
Compare FastJet median  $\rho$  to Monte Carlo truth ( $\rho_{Direct}$ )



Compare FastJet median  $\rho$  to Monte Carlo truth ( $\rho_{Direct}$ )



Works much better than counting primary vertices



# A non-trivial issue: rapidity dependence

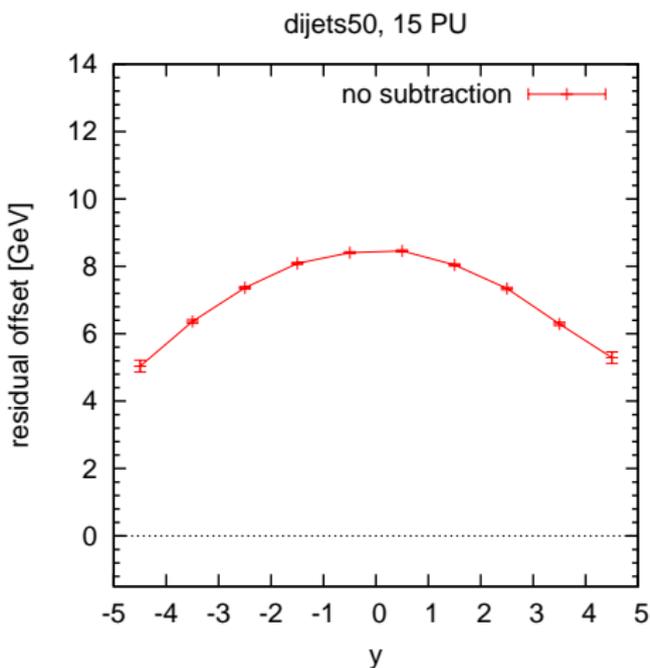
The original method assumed rapidity dependence was small

- ▶ In some sense it is,  $\lesssim 1.5$  GeV
- ▶ Measure  $\rho$  globally, and include a rapidity-dependent rescaling

$$p_t^{sub} = p_t - f(y)\rho A$$

determine  $f(y)$  from min-bias

- ▶ Measure  $\rho$  "locally" in strips of  $|\Delta y| < 1.5$



Conclusion: global  $\rho$  determination with fixed rapidity-dependent rescaling is probably the most effective choice

# A non-trivial issue: rapidity dependence

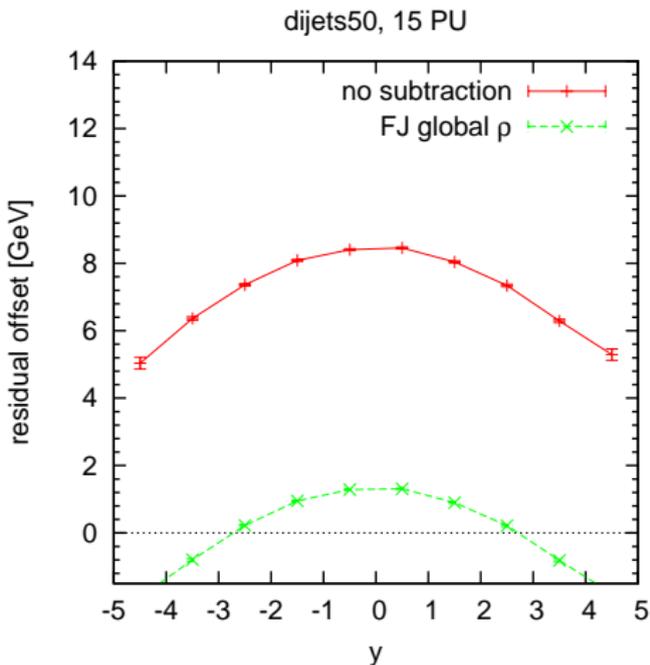
The original method assumed rapidity dependence was small

- ▶ In some sense it is,  $\lesssim 1.5$  GeV
- ▶ Measure  $\rho$  globally, and include a rapidity-dependent rescaling

$$p_t^{sub} = p_t - f(y)\rho A$$

determine  $f(y)$  from min-bias

- ▶ Measure  $\rho$  "locally" in strips of  $|\Delta y| < 1.5$



Conclusion: global  $\rho$  determination with fixed rapidity-dependent rescaling is probably the most effective choice

# A non-trivial issue: rapidity dependence

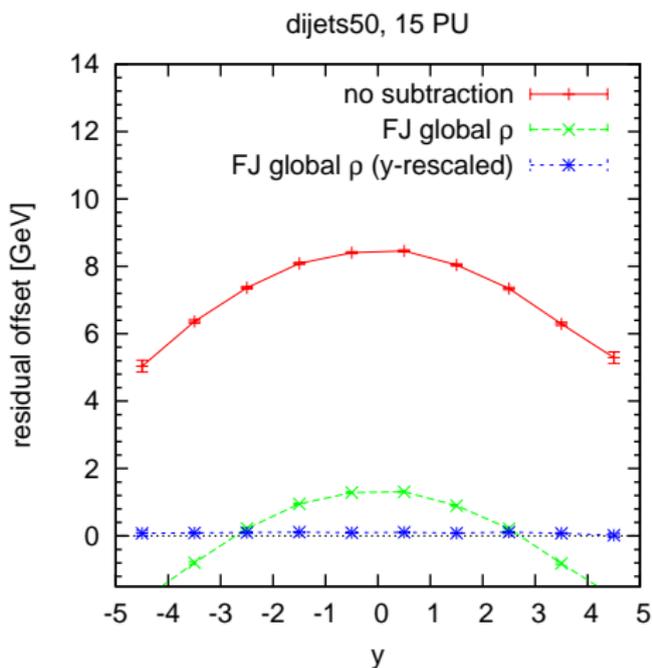
The original method assumed rapidity dependence was small

- ▶ In some sense it is,  $\lesssim 1.5$  GeV
- ▶ Measure  $\rho$  globally, and include a rapidity-dependent rescaling

$$p_t^{sub} = p_t - f(y)\rho A$$

determine  $f(y)$  from min-bias

- ▶ Measure  $\rho$  "locally" in strips of  $|\Delta y| < 1.5$



Conclusion: global  $\rho$  determination with fixed rapidity-dependent rescaling is probably the most effective choice

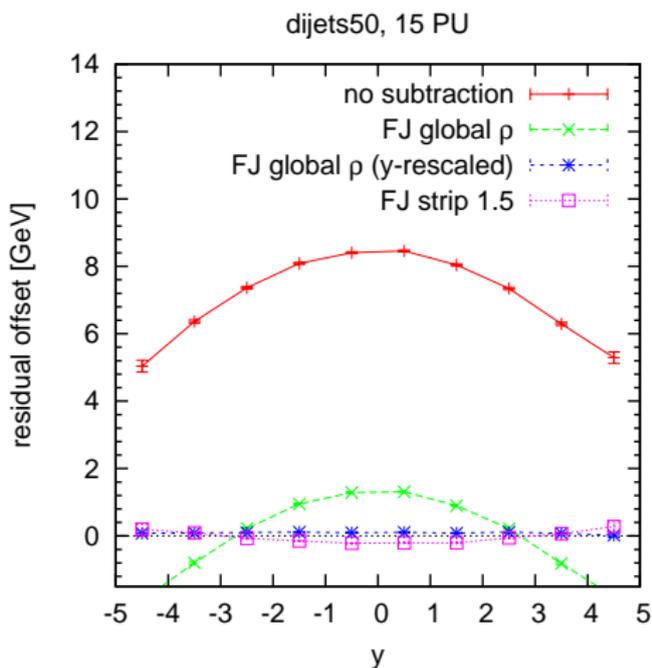
The original method assumed rapidity dependence was small

- ▶ In some sense it is,  $\lesssim 1.5$  GeV
- ▶ Measure  $\rho$  globally, and include a rapidity-dependent rescaling

$$p_t^{sub} = p_t - f(y)\rho A$$

determine  $f(y)$  from min-bias

- ▶ Measure  $\rho$  "locally" in strips of  $|\Delta y| < 1.5$



Conclusion: global  $\rho$  determination with fixed rapidity-dependent rescaling is probably the most effective choice

# A non-trivial issue: rapidity dependence

The original method assumed rapidity dependence was small

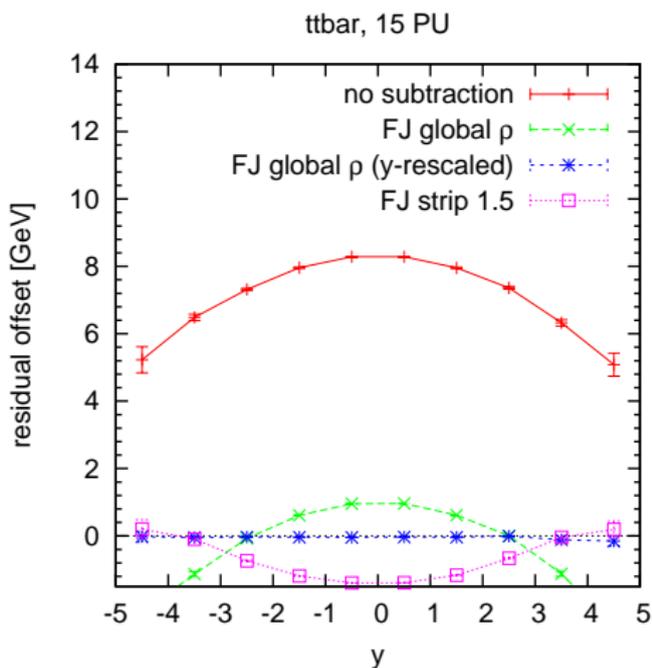
- ▶ In some sense it is,  $\lesssim 1.5$  GeV
- ▶ Measure  $\rho$  globally, and include a rapidity-dependent rescaling

$$p_t^{sub} = p_t - f(y)\rho A$$

determine  $f(y)$  from min-bias

- ▶ Measure  $\rho$  "locally" in strips of  $|\Delta y| < 1.5$

But lower number of total jets more biased by hard jets (e.g.  $t\bar{t}$ )



Conclusion: global  $\rho$  determination with fixed rapidity-dependent rescaling is probably the most effective choice

The original method assumed rapidity dependence was small

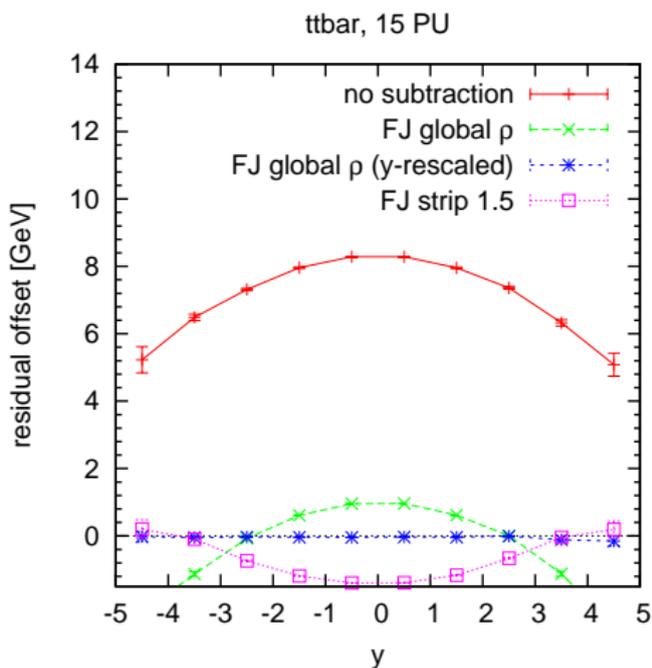
- ▶ In some sense it is,  $\lesssim 1.5$  GeV
- ▶ Measure  $\rho$  globally, and include a rapidity-dependent rescaling

$$p_t^{sub} = p_t - f(y)\rho A$$

determine  $f(y)$  from min-bias

- ▶ Measure  $\rho$  "locally" in strips of  $|\Delta y| < 1.5$

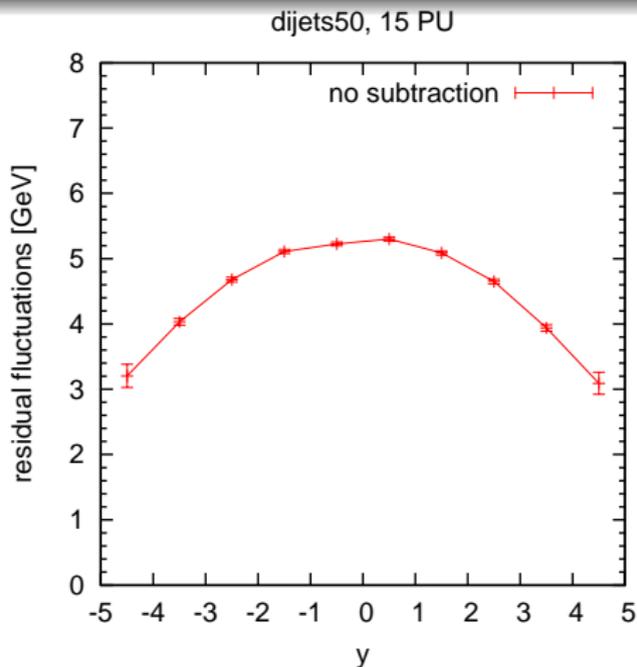
But lower number of total jets more biased by hard jets (e.g.  $t\bar{t}$ )



Conclusion: global  $\rho$  determination with fixed rapidity-dependent rescaling is probably the most effective choice

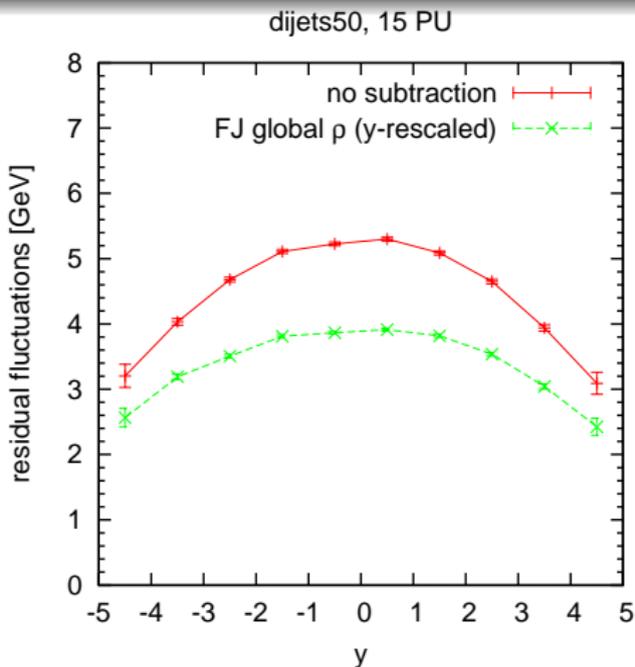
Dispersion of offset gives another measure of the subtraction “quality”

- ▶ several GeV without subtraction
- ▶ only partially reduced with FJ subtraction
- ▶ alternative: use PF to remove PU charged tracks in each jet if PU is in-time
- ▶ scaling PU charged track in the jet to correct also for neutrals



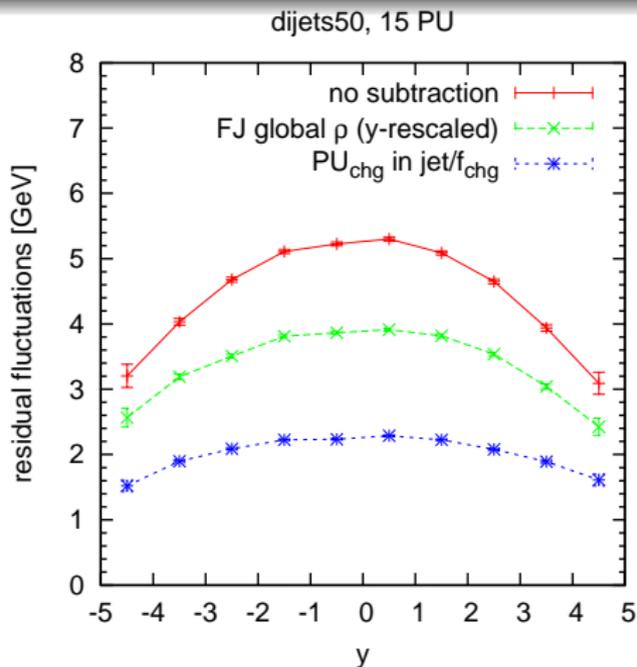
Dispersion of offset gives another measure of the subtraction “quality”

- ▶ several GeV without subtraction
- ▶ only partially reduced with FJ subtraction
- ▶ alternative: use PF to remove PU charged tracks in each jet if PU is in-time
- ▶ scaling PU charged track in the jet to correct also for neutrals
- ▶ or supplementing with FJ subtraction for the neutrals better still



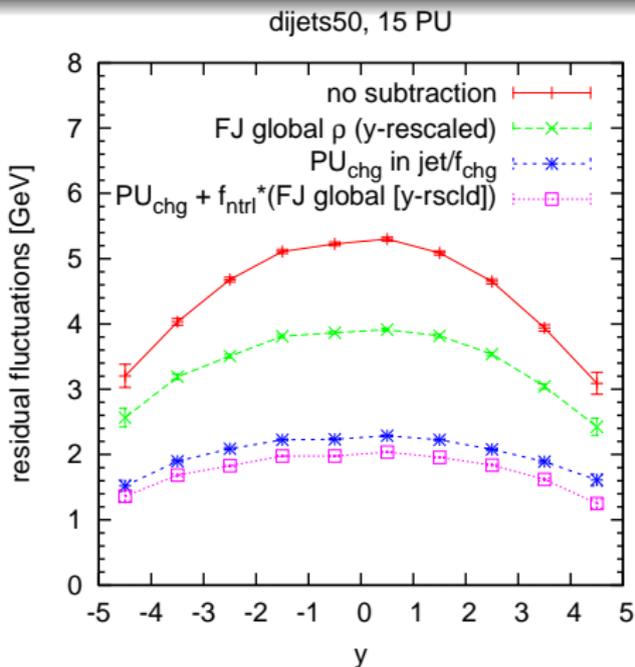
Dispersion of offset gives another measure of the subtraction “quality”

- ▶ several GeV without subtraction
- ▶ only partially reduced with FJ subtraction
- ▶ alternative: use PF to remove PU charged tracks in each jet  
if PU is in-time
- ▶ scaling PU charged track in the jet to correct also for neutrals
- ▶ or supplementing with FJ subtraction for the neutrals  
better still



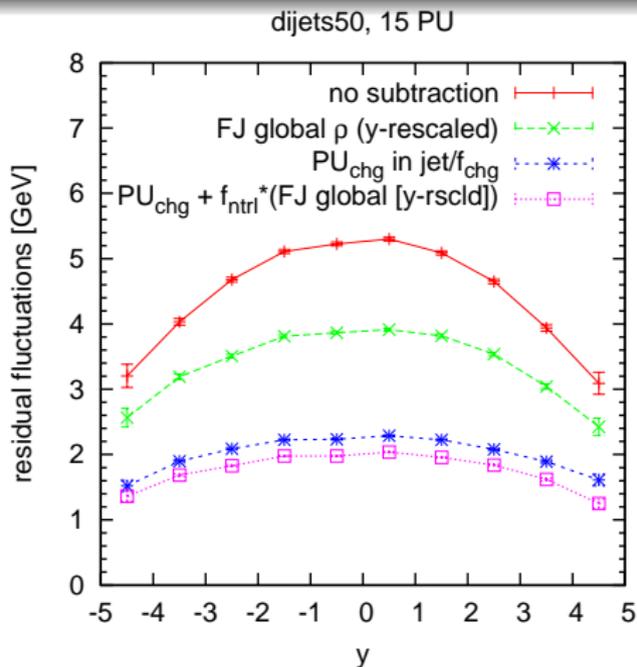
Dispersion of offset gives another measure of the subtraction “quality”

- ▶ several GeV without subtraction
- ▶ only partially reduced with FJ subtraction
- ▶ alternative: use PF to remove PU charged tracks in each jet  
if PU is in-time
- ▶ scaling PU charged track in the jet to correct also for neutrals
- ▶ or supplementing with FJ subtraction for the neutrals  
better still



Dispersion of offset gives another measure of the subtraction “quality”

- ▶ several GeV without subtraction
- ▶ only partially reduced with FJ subtraction
- ▶ alternative: use PF to remove PU charged tracks in each jet  
if PU is in-time
- ▶ scaling PU charged track in the jet to correct also for neutrals
- ▶ or supplementing with FJ subtraction for the neutrals  
better still



Direct knowledge of PU from tracks  
can be beneficial

Detector impact harder to judge

Fat-jet studies need more than just the jet  $p_t$ . E.g. **jet mass**

There are methods to limit PU sensitivity of jet masses.

Filtering: Butterworth et al '08

Pruning: Ellis et al '09

Trimming: Thaler et al '09

4-vector subtraction can also help

$$p_\mu^{(sub)} = p_\mu - f(y)\rho A_\mu$$

“Automatically” corrects mass

as long as hadron masses set to zero

Many more things can be corrected for PU beyond jet  $p_t$   
Tests are still in v. early stages / drawing board

Fat-jet studies need more than just the jet  $p_t$ . E.g. **jet mass**

There are methods to limit PU sensitivity of jet masses.

Filtering: Butterworth et al '08

Pruning: Ellis et al '09

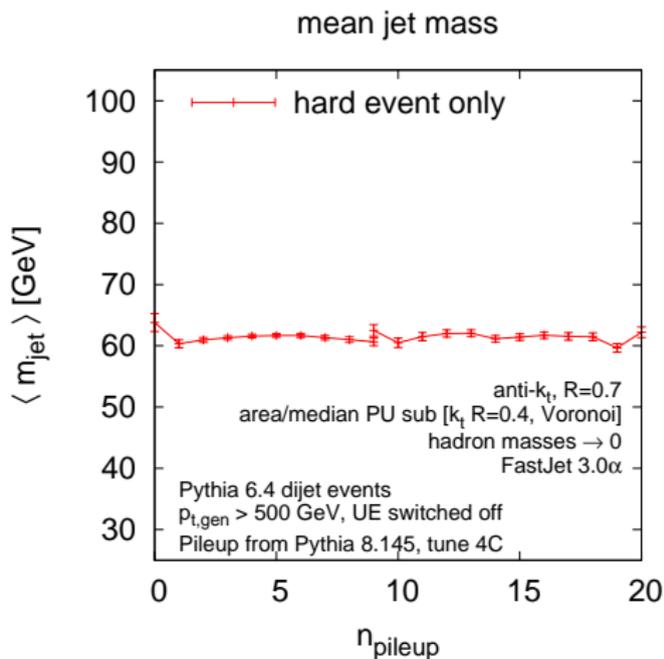
Trimming: Thaler et al '09

4-vector subtraction can also help

$$p_{\mu}^{(sub)} = p_{\mu} - f(y)\rho A_{\mu}$$

“Automatically” corrects mass

as long as hadron masses set to zero



Many more things can be corrected for PU beyond jet  $p_t$   
Tests are still in v. early stages / drawing board

Fat-jet studies need more than just the jet  $p_t$ . E.g. **jet mass**

There are methods to limit PU sensitivity of jet masses.

Filtering: Butterworth et al '08

Pruning: Ellis et al '09

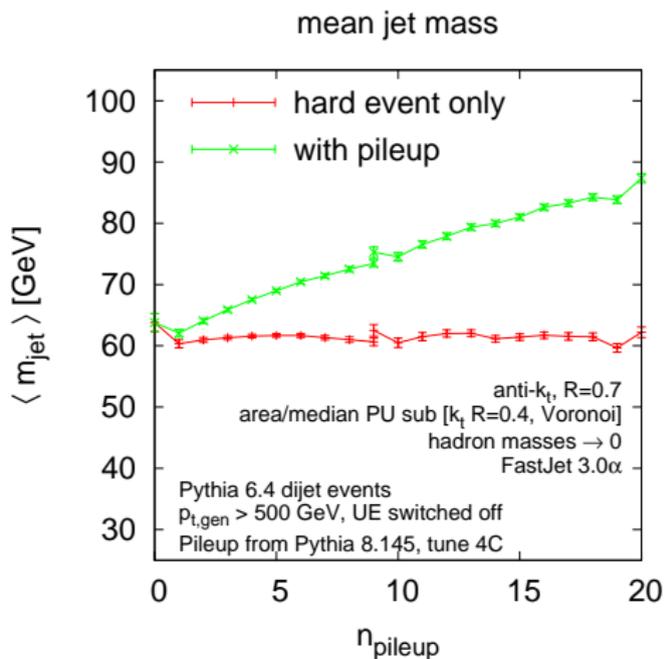
Trimming: Thaler et al '09

4-vector subtraction can also help

$$p_{\mu}^{(sub)} = p_{\mu} - f(y)\rho A_{\mu}$$

“Automatically” corrects mass

as long as hadron masses set to zero



Many more things can be corrected for PU beyond jet  $p_t$   
 Tests are still in v. early stages / drawing board

Fat-jet studies need more than just the jet  $p_t$ . E.g. **jet mass**

There are methods to limit PU sensitivity of jet masses.

Filtering: Butterworth et al '08

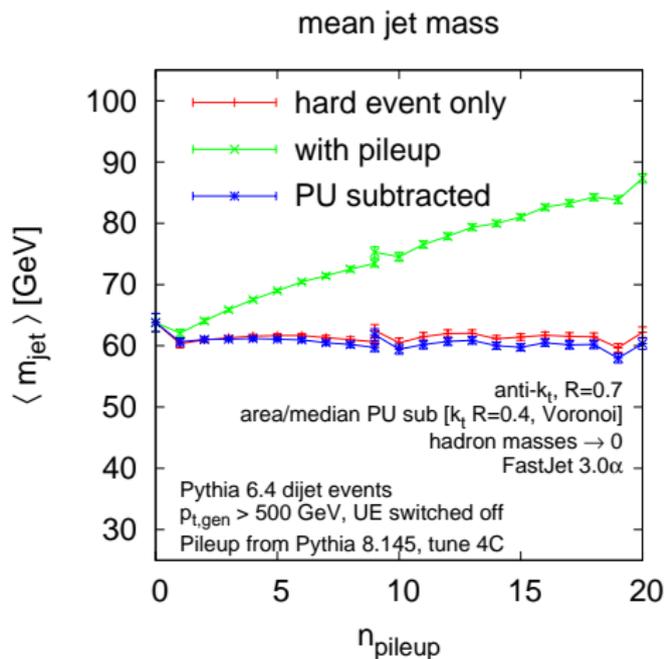
Pruning: Ellis et al '09

Trimming: Thaler et al '09

4-vector subtraction can also help

$$p_{\mu}^{(sub)} = p_{\mu} - f(y)\rho A_{\mu}$$

“Automatically” corrects mass  
as long as hadron masses set to zero



Many more things can be corrected for PU beyond jet  $p_t$   
Tests are still in v. early stages / drawing board

Fat-jet studies need more than just the jet  $p_t$ . E.g. **jet mass**

There are methods to limit PU sensitivity of jet masses.

Filtering: Butterworth et al '08

Pruning: Ellis et al '09

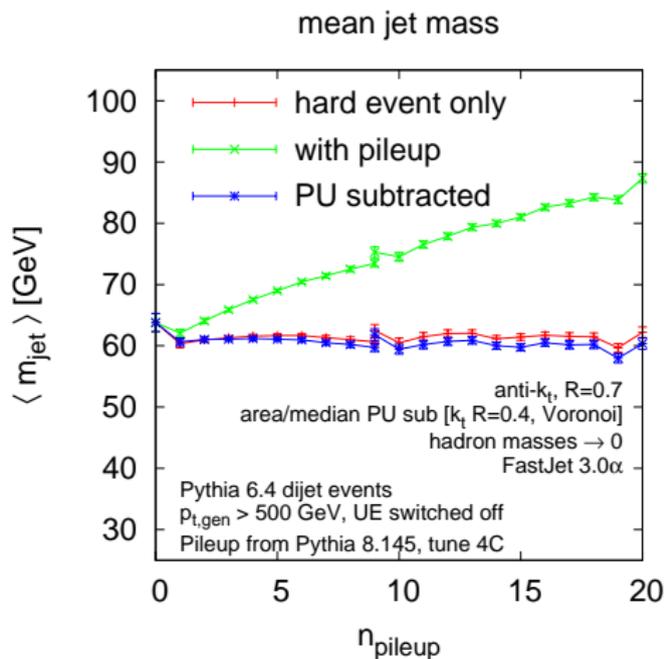
Trimming: Thaler et al '09

4-vector subtraction can also help

$$p_{\mu}^{(sub)} = p_{\mu} - f(y)\rho A_{\mu}$$

“Automatically” corrects mass

as long as hadron masses set to zero



Many more things can be corrected for PU beyond jet  $p_t$   
 Tests are still in v. early stages / drawing board

# Conclusions

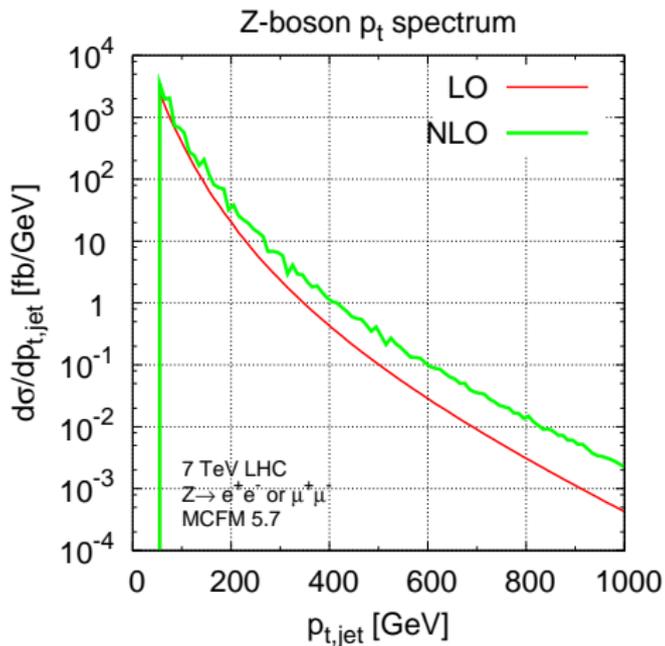
As we (you!) explore beyond the electroweak scale, our way of thinking about  $W/Z/H/top$  needs to evolve

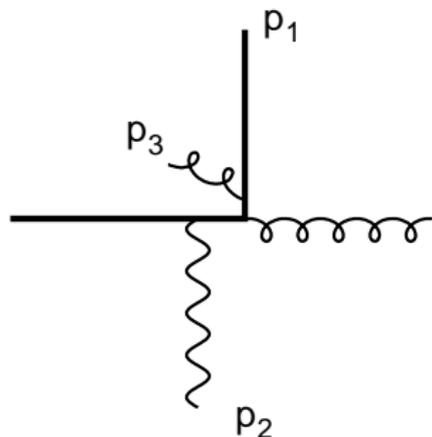
Particles that used to be heavy suddenly become light — EW symmetry is almost restored

As a result  $W/Z/H/top$  are easier to produce  
And their decays look almost like QCD jets

Yet even at the TeV scale, GeV-scale pileup physics matters, but can be corrected for

# EXTRAS

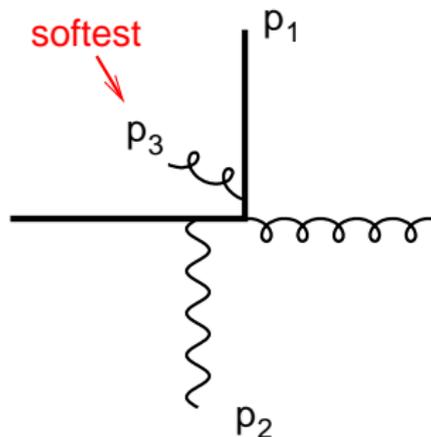




**Z + 2 partons**

$$|M^2(p_1, p_2, p_3)|$$

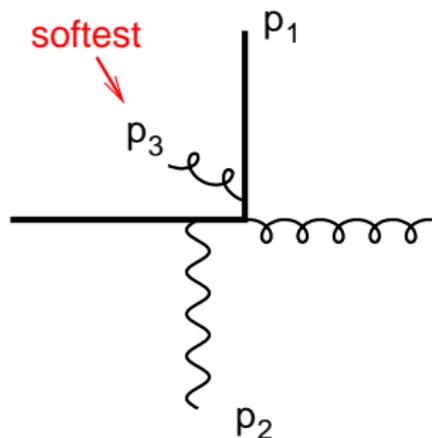
- ▶ Identify softest or most collinear parton [with help of a jet algorithm]
- ▶ “Loop” it  $\equiv$  remove it from event, reshuffle other momenta; weight of looped event is  $(-1) \times$  weight of tree-level event



**Z + 2 partons**

$$|M^2(p_1, p_2, p_3)|$$

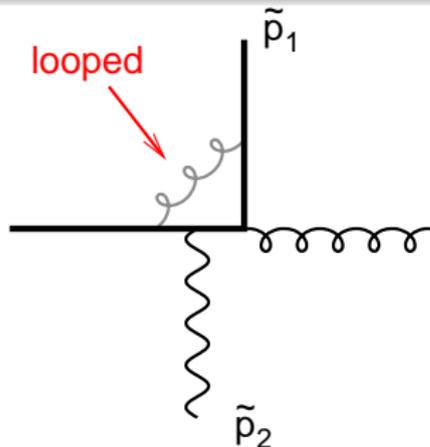
- ▶ Identify softest or most collinear parton [with help of a jet algorithm]
- ▶ “Loop” it  $\equiv$  remove it from event, reshuffle other momenta; weight of looped event is  $(-1) \times$  weight of tree-level event



**Z + 2 partons**

$$|M^2(p_1, p_2, p_3)|$$

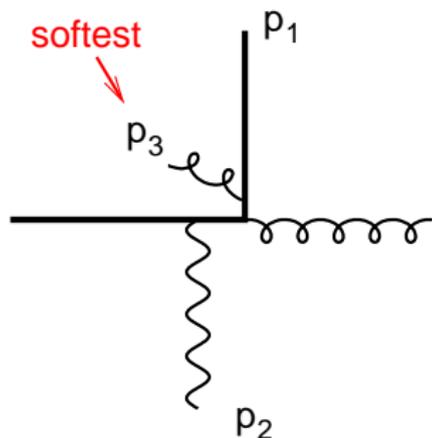
+



**Z + 1 parton + 1 sim. loop**

$$-|M^2(p_1, p_2, p_3)|$$

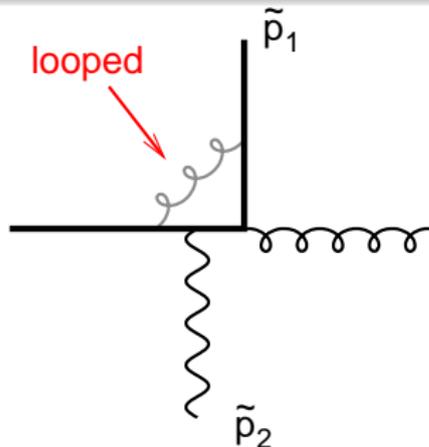
- ▶ Identify softest or most collinear parton [with help of a jet algorithm]
- ▶ “Loop” it  $\equiv$  remove it from event, reshuffle other momenta; weight of looped event is  $(-1) \times$  weight of tree-level event



**Z + 2 partons**

$$|M^2(p_1, p_2, p_3)|$$

+

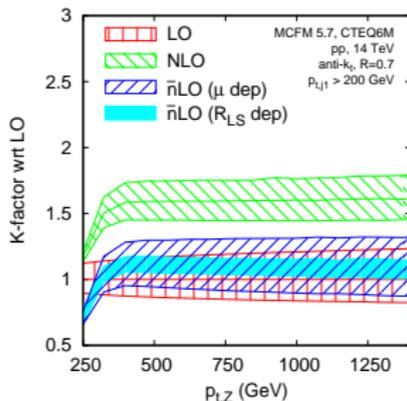
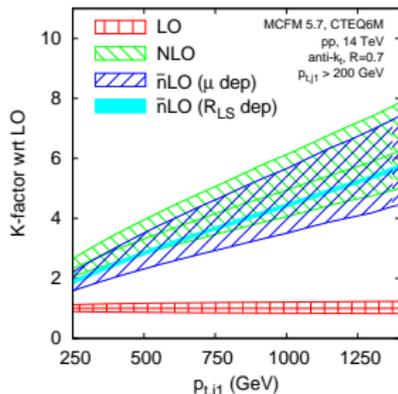
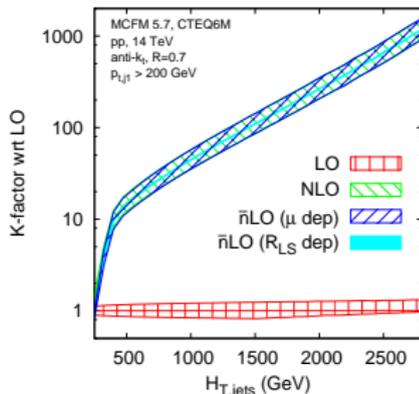


**Z + 1 parton + 1 sim. loop**

$$-|M^2(p_1, p_2, p_3)|$$

- ▶ Identify softest or most collinear parton [with help of a jet algorithm]
- ▶ “Loop” it  $\equiv$  remove it from event, reshuffle other momenta; weight of looped event is  $(-1) \times$  weight of tree-level event

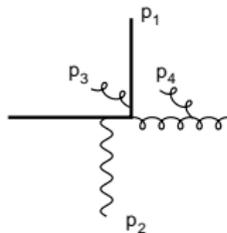
This cancels all the “single-unresolved” divergences in the Z+2 events

$\bar{n}$ LO results ( $K$ -factors, normalised to LO) $p_t$  of Z-boson $p_t$  of jet 1 $H_{T,jets} = \sum_{jets} p_{t,j}$ 

When the  $K$ -factors are large,  $\bar{n}$ LO agrees well with NLO

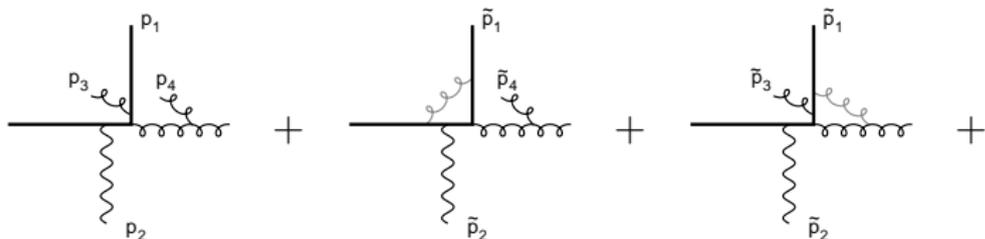
MLM matching also does a similar job  
cf. de Aquino, Hagiwara, Li & Maltoni '11

add tree-level Z+3,  
cancel divergences in single + doubly unresolved limits:  $\bar{n}\bar{n}$ LO



$$|M^2(p_1, p_2, p_3, p_4)|$$

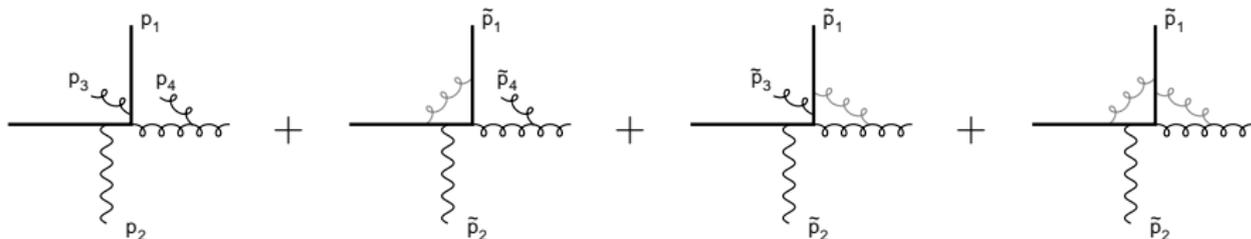
add tree-level Z+3,  
cancel divergences in single + doubly unresolved limits:  $\bar{n}\bar{n}$ LO



$$|M^2(p_1, p_2, p_3, p_4)| \quad - |M^2(p_1, p_2, p_3, p_4)| \quad - |M^2(p_1, p_2, p_3, p_4)|$$

Separately loop either of the 2 softest emissions: provides approx of 1-loop

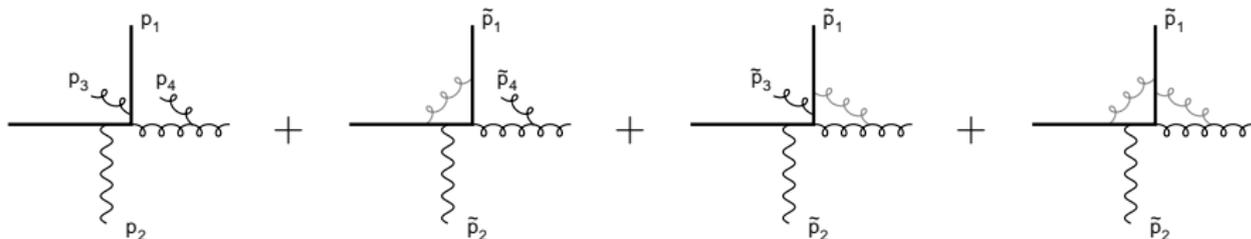
add tree-level Z+3,  
cancel divergences in single + doubly unresolved limits:  $\bar{n}\bar{n}$ LO



$$|M^2(p_1, p_2, p_3, p_4)| - |M^2(p_1, p_2, p_3, p_4)| - |M^2(p_1, p_2, p_3, p_4)| + |M^2(p_1, p_2, p_3, p_4)|$$

Simultaneously loop each of the 2 softest emissions: provides approx of 2-loop  
Total of tree plus approx 1- and 2-loop pieces gives zero

add tree-level Z+3,  
cancel divergences in single + doubly unresolved limits:  $\bar{n}\bar{n}$ LO



$$|M^2(p_1, p_2, p_3, p_4)| - |M^2(p_1, p_2, p_3, p_4)| - |M^2(p_1, p_2, p_3, p_4)| + |M^2(p_1, p_2, p_3, p_4)|$$

Simultaneously loop each of the 2 softest emissions: provides approx of 2-loop  
Total of tree plus approx 1- and 2-loop pieces gives zero

add in (exact Z+2 @ 1-loop) – (approximate Z+2 @ 1-loop)  
+ extra simulated 2-loop piece to cancel new Z+2@1-loop divergences

**This is  $\bar{n}$ NLO**

The 2-loop piece has the topology of the LO diagram.

The “mistake” we make in approximating it should therefore be a “pure”  $\mathcal{O}(\alpha_s^2)$  correction, without any large enhancements from new NLO type topologies.

$$\begin{aligned}\sigma_{\bar{n}\text{NLO}} &= \sigma_{\text{NNLO}} + \mathcal{O}(\alpha_s^2 \sigma_{\text{LO}}) \\ &= \sigma_{\text{NNLO}} \left( 1 + \mathcal{O}\left(\frac{\alpha_s^2}{K_{\text{NNLO}}}\right) \right)\end{aligned}$$

$$K_{\text{NNLO}} = \frac{\sigma_{\text{NNLO}}}{\sigma_{\text{LO}}} \sim K_{\text{NLO}} \gg 1$$

The *relative* contribution of the neglected piece is suppressed by the large  $K$ -factor.

$\bar{n}$ NLO should be a good approximation to NNLO when the  $K$ -factor is large and due to new higher-order topologies.