## **INGREDIENTS FOR ACCURATE COLLIDER PHYSICS (2/2)**

Gavin Salam, CERN

PSI Summer School Exothiggs, Zuoz, August 2016

► We discussed the "Master" formula

$$\sigma \left(h_1 h_2 \to W + X\right) = \sum_{n=0}^{\infty} \alpha_s^n \left(\mu_R^2\right) \sum_{i,j} \int dx_1 dx_2 f_{i/h_1}\left(x_1, \mu_F^2\right) f_{j/h_2}\left(x_2, \mu_F^2\right)$$
$$\times \hat{\sigma}_{ij \to W + X}^{(n)} \left(x_1 x_2 s, \mu_R^2, \mu_F^2\right) + \mathcal{O}\left(\frac{\Lambda^2}{M_W^4}\right),$$

- ► and its main inputs
  - $\blacktriangleright$  the strong coupling  $a_s$
  - Parton Distribution Functions (PDFs)
- ► Today: we discuss the actual scattering cross section

► We discussed the "Master" formula

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## the hard cross section

$$\sigma \sim \sigma_2 \alpha_s^2 + \sigma_3 \alpha_s^3 + \sigma_4 \alpha_s^4 + \sigma_5 \alpha_s^5 + \cdots$$
  
LO NLO NNLO N3LO

#### **INGREDIENTS FOR A CALCULATION (generic 2→2 process)**

Tree 2→2

LO



to illustrate the concepts, we don't care what the particles are — just draw lines

#### **INGREDIENTS FOR A CALCULATION (generic 2→2 process)**



#### **INGREDIENTS FOR A CALCULATION (generic 2→2 process)**



$$\frac{\sigma(e^+e^- \to \text{hadrons})}{\sigma(e^+e^- \to \mu^+\mu^-)} = [\alpha_s \equiv \alpha_s(\sqrt{s_{e^+e^-}})]$$
$$= R_0 \left(1 + 0.32\alpha_s + 0.14\alpha_s^2 - 0.47\alpha_s^3 - 0.59316\alpha_s^4 + \cdots\right)$$
Baikov et al., 1206.1288 (numbers for  $\gamma$ -exchange only)

This is one of the few quantities calculated to N4LO Good convergence of the series at every order (at least for  $\alpha_s(M_z) = 0.118$ )  $\sigma(pp \to H) = (961 \,\mathrm{pb}) \times (\alpha_s^2 + 10.4\alpha_s^3 + 38\alpha_s^4 + 48\alpha_s^5 + \cdots)$  $\alpha_s \equiv \alpha_s(M_H/2)$  $\sqrt{s_{pp}} = 13 \,\mathrm{TeV}$ 

Anastasiou et al., 1602.00695 (ggF, hEFT)

pp→H (via gluon fusion) is one of only two hadron-collider processes known at N3LO (the other is pp→H via weak-boson fusion)

The series does not converge well (explanations for why are only moderately convincing)

- On previous page, we wrote the series in terms of powers of a<sub>s</sub>(M<sub>H</sub>/2)
- But we are free to rewrite it in terms of a<sub>s</sub>(μ) for any choice of "renormalisation scale" μ.
   Higgs cross section





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scale dependence (an intrinsic uncertainty) gets reduced as you go to higher order

Scale dependence as the "THEORY UNCERTAINTY"



Convention: "theory uncertainty" (i.e. from missing higher orders) is estimated by change of cross section when varying µ in range 1/2 → 2 around central value Scale dependence as the "THEORY UNCERTAINTY"



Here, only the renorm. scale µ has been varied. In real life you need to change renorm. and factorisation scales.

Convention: "theory uncertainty" (i.e. from missing higher orders) is estimated by change of cross section when varying  $\mu$  in range 1/2  $\rightarrow$  2 around central value 14

► LO: almost any process

(with MadGraph, ALPGEN, etc.)

- NLO: most processes (with MCFM, NLOJet + +, MG5\_aMC@NLO, Blackhat/NJet/Gosam/etc. + Sherpa)
- ► NNLO: all 2→1 and many 2→2 (but not dijets) (DY/HNNLO, FEWZ, MATRIX, MCFM & private codes)
- ► N3LO: pp → Higgs via gluon fusion and weak-boson fusion both in approximations (EFT,  $QCD_1 \times QCD_2$ )
- ► NLO EW corrections, i.e. relative a<sub>EW</sub> rather than a<sub>s</sub>: most 2→1 and many 2→2

## the real world?



#### **GLUON EMISSION FROM A QUARK**



Consider an emission with

- ► energy  $\mathbf{E} \ll \sqrt{\mathbf{s}}$  ("soft")
- angle θ < 1</li>
   ("collinear" wrt quark)

Examine correction to some hard process with cross section  $\sigma_0$ 

$$d\sigma \simeq \sigma_0 \times \frac{2\alpha_s C_F}{\pi} \frac{dE}{E} \frac{d\theta}{\theta}$$

This has a divergence when  $E \rightarrow 0$  or  $\theta \rightarrow 0$ [in some sense because of quark propagator going on-shell]

#### How come we get finite cross sections?



Divergences are present in both real and virtual diagrams.

If you are "inclusive", i.e. your measurement doesn't care whether a soft/collinear gluon has been emitted then the real and virtual divergences cancel. Probability  $P_g$  of emitting gluon from a quark with energy Q:

$$P_g \simeq \frac{2\alpha_s C_F}{\pi} \int^Q \frac{dE}{E} \int^1 \frac{d\theta}{\theta} \Theta(E\theta > Q_0)$$

This diverges unless we cut off the integral for transverse momenta ( $p_T \approx E \theta$ ) below some non-perturbative threshold  $Q_0$ .

> On the grounds that perturbation theory doesn't apply for  $p_T \sim \Lambda_{QCD}$ language of quarks and gluons becomes meaningless

With this cutoff, the result is

$$P_g \simeq \frac{\alpha_s C_F}{\pi} \ln^2 \frac{Q}{Q_0} + \mathcal{O}\left(\alpha_s \ln Q\right)$$

this is called a "double logarithm" [it crops up all over the place in QCD] Suppose we're not inclusive — e.g. calculate probability of emitting a gluon

Suppose we take  $Q_0 \sim \Lambda_{QCD}$ , what do we get?

Let's use  $a_s = a_s(Q) = 1/(2b \ln Q/\Lambda)$ [Actually over most of integration range this is optimistically small]

$$P_g \simeq \frac{\alpha_s C_F}{\pi} \ln^2 \frac{Q}{Q_0} \to \frac{C_F}{2b\pi} \ln \frac{Q}{\Lambda_{QCD}} \to \frac{C_F}{4b^2 \pi \alpha_s}$$

Put in some numbers: Q = 100 GeV,  $\Lambda_{QCD} \approx 0.2$  GeV,  $C_F = 4/3$ , b  $\approx 0.6$ 

$$P_g \simeq 2.2$$

This is supposed to be an  $O(\alpha_s)$  correction. But the final result ~  $1/\alpha_s$ QCD hates to not emit gluons!



## Start off with a qqbar system



## a gluon gets emitted at small angles



## it radiates a further gluon



## and so forth



## meanwhile the same happened on the other side





## then a non-perturbative transition occurs



**giving a pattern of hadrons that "remembers" the gluon branching** (hadrons mostly produced at small angles wrt qqbar directions — two "jets")

# resummation and parton showers

the previous slides applied in practice

- It's common to ask questions like "what is the probability that a Higgs boson is produced with transverse momentum < p<sub>T</sub>"
- Answer is given (~) by a "Sudakov form factor", i.e. the probability of not emitting any gluons with transverse momentum > p<sub>T</sub>.

$$P(\text{Higgs trans.mom.} < p_T) \simeq \exp\left[-\frac{2\alpha_s C_A}{\pi} \ln^2 \frac{M_H}{p_T}\right]$$

➤ when p<sub>T</sub> is small, the logarithm is large and compensates for the smallness of a<sub>s</sub> — so you need to resum log-enhanced terms to all orders in a<sub>s</sub>.

- ➤ You'll sometimes see mention of "NNLL" or similar
- This means next-next-to-leading logarithmic
- ► Leading logarithmic (LL) means you sum all terms with p=n+1 (for n=1...∞) in

$$\exp\left[-\sum_{n,p} \alpha_s^n \ln^p \frac{M_H}{p_T}\right]$$

- ► NLL: all terms with p=n (for  $n=1...\infty$ )
- ► NNLL: all terms with p=n-1 (for  $n=1...\infty$ )

In real life, the function that appears in the resummation is sometimes instead a Fourier or Mellin transform of an exponential

### Resummation of Higgs $p_T$ spectrum

**Resummation is essential to** predict small-p<sub>T</sub> region (where you have most of the events) 1.000 0.500 HqT2.0 Т **HRes** dσ/dp<sub>T</sub> (fb/GeV) 0.100 0.050 This kind of resummation is an input to nearly all LHC Higgs studies  $pp \rightarrow H + X \rightarrow \gamma \gamma + X$ 0.020 de Florian et al  $\sqrt{s}=8$  TeV, MSTW2008 1203.6321  $0.010 \vdash \mu_{\rm F} = \mu_{\rm R} = 2Q = m_{\rm H} = 125 \text{ GeV}$ 0.005 50 100 150 200  $\cap$  $p_{T}$  (GeV)

#### Resummation of Higgs $p_T$ spectrum



This is resummation of a kinematic variable — can usually be made robust by examining region with  $p_T \ll m_H$ 

Another kind of resummation is **threshold resummation**, of logs of  $\tau = (1 - M^2/s)$ . For many applications (ttbar, Higgs) it's debated whether  $\tau$  is small enough for resummation to bring genuine information
#### resummation v. parton showers (the basic idea)

- ► a resummation predicts **one observable** to high accuracy
- a parton shower takes the same idea of a Sudakov form factor and uses it to generate emissions
- From probability of not emitting gluons above a certain p<sub>T</sub>, you can deduce p<sub>T</sub> distribution of first emission
- 1. use a random number generator (r) to sample that  $p_{\rm T}$  distribution

deduce 
$$p_T$$
 by solving  $r = \exp\left[-\frac{2\alpha_s C_A}{\pi}\ln^2\frac{p_{T,\max}^2}{p_T^2}\right]$ 

2. repeat for next emission, etc., until  $p_T$  falls below some non-perturbative cutoff

#### very similar to radioactive decay, with time ~ 1/p<sub>T</sub> and a decay rate ~ p<sub>T</sub> log 1/p<sub>T</sub>

#### A toy shower <u>https://github.com/gavinsalam/zuoz2016-toy-shower</u>

(fixed coupling, primary branching only, only p<sub>T</sub>, no energy conservation, no PDFs, etc.)

```
#!/usr/bin/env python
# an oversimplified (QED-like) parton shower
# for Zuoz lectures (2016) by Gavin P. Salam
from random import random
from math import pi, exp, log, sqrt
ptHigh = 100.0
ptCut = 1.0
alphas = 0.12
CA=3
def main():
    for iev in range(0,10):
        print "\nEvent", iev
        event()
def event():
    # start with maximum possible value of Sudakov
    sudakov = 1
    while (True):
        # scale it by a random number
        sudakov *= random()
        # deduce the corresponding pt
        pt = ptFromSudakov(sudakov)
        # if pt falls below the cutoff, event is finished
        if (pt < ptCut): break</pre>
        print " primary emission with pt = ", pt
def ptFromSudakov(sudakovValue):
    """Returns the pt value that solves the relation
       Sudakov = sudakovValue (for 0 < sudakovValue < 1)
    .....
    norm = (2*CA/pi)
    \# r = Sudakov = exp(-alphas * norm * L<sup>2</sup>)
    \# \rightarrow \log(r) = -alphas * norm * L^2
    \# \longrightarrow L^2 = \log(r)/(-alphas*norm)
    L2 = log(sudakovValue)/(-alphas * norm)
    pt = ptHigh * exp(-sqrt(L2))
    return pt
```

#### A toy shower

(fixed coupling, primary branching only, only  $p_T$ , no energy conservation, no PDFs, etc.)

```
#!/usr/bin/env python
                                                                % python ./toy-shower.py
# an oversimplified (QED-like) parton shower
# for Zuoz lectures (2016) by Gavin P. Salam
                                                                 Event 0
from random import random
                                                                   primary emission with pt = 58.4041962726
from math import pi, exp, log, sqrt
                                                                   primary emission with pt = 3.61999582015
ptHigh = 100.0
                                                                   primary emission with pt = 2.31198814996
ptCut = 1.0
alphas = 0.12
                                                                 Event 1
CA=3
                                                                   primary emission with pt = 32.1881228375
                                                                   primary emission with pt = 10.1818306204
def main():
   for iev in range(0,10):
                                                                   primary emission with pt = 10.1383134201
       print "\nEvent", iev
                                                                   primary emission with pt = 7.24482350383
       event()
                                                                   primary emission with pt = 2.35709074796
                                                                   primary emission with pt = 1.0829758034
def event():
   # start with maximum possible value of Sudakov
   sudakov = 1
                                                                Event 2
   while (True):
                                                                   primary emission with pt = 64.934992001
       # scale it by a random number
                                                                   primary emission with pt = 16.4122436094
       sudakov *= random()
                                                                   primary emission with pt = 2.53473253194
       # deduce the corresponding pt
       pt = ptFromSudakov(sudakov)
       # if pt falls below the cutoff, event is finished
                                                                Event 3
       if (pt < ptCut): break</pre>
                                                                   primary emission with pt = 37.6281171491
       print " primary emission with pt = ", pt
                                                                   primary emission with pt = 22.7262873764
                                                                   primary emission with pt = 12.0255817868
def ptFromSudakov(sudakovValue):
                                                                   primary emission with pt = 4.73678636215
   """Returns the pt value that solves the relation
      Sudakov = sudakovValue (for 0 < sudakovValue < 1)
                                                                   primary emission with pt = 3.92257832288
   .....
   norm = (2*CA/pi)
                                                                Event 4
   \# r = Sudakov = exp(-alphas * norm * L<sup>2</sup>)
                                                                   primary emission with pt = 21.5359449851
   \# \rightarrow \log(r) = -alphas * norm * L^2
                                                                   primary emission with pt = 4.01438733798
   \# --> L^2 = log(r)/(-alphas*norm)
   L2 = log(sudakovValue)/(-alphas * norm)
                                                                   primary emission with pt = 3.33902663941
   pt = ptHigh * exp(-sqrt(L2))
                                                                   primary emission with pt = 2.02771620824
   return pt
                                                                   primary emission with pt = 1.05944759028
```

. .

#### A toy shower

(fixed coupling, primary branching only, only  $p_T$ , no energy conservation, no PDFs, etc.)

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   """Returns the pt value that solves the relation
```

Exercise: replace  $C_A=3$  (emission from gluons) with  $C_F=4/3$  (emission from quarks) and see how pattern of emissions changes (multiplicity,  $p_T$  of hardest emission, etc.)

---PARTON SHOWERS---

IHEP	ID	IDPDG	IST	M01	M02	DA1	DA2	P-X	P-Y	P-Z	ENERGY	MASS		
9	UQRK	94	141	4	6	11	16	2,64	-9,83	592,2	590,2	-49.07		
10	CONE	0	100	4	5	0	0	-0,27	0.96	0.1	1.0	0,00		
11	GLUON	21	2	9	12	32	33	-1,02	3,59	5.6	6.7	0.75-		
12	GLUON	21	2	9	13	34	35	0,25	1,46	3.6	4.0	0.75-		AL
13	GLUON	21	2	9	14	36	37	-0,87	1.62	4.7	5.1	0.75-		'E
14	GLUON	21	2	9	15	38	39	-0,81	4.17	3611.7	3611.7	0.75-	SIAI	•
15	GLUON	21	2	9	16	40	41	-0,19	-1,01	1727.7	1727.7	0,75-	SHO	WER
16	UD	2101	2	9	25	42	41	0,00	0,00	1054.6	1054.6	0.32-		
17	GLUON	94	142	5	6	19	21	-2,23	0,44	-233.5	232,8	-18,36		
18	CONE	0	100	5	8	0	0	0,77	0.64	0.2	1.0	0,00		
19	GLUON	21	2	17	20	43	44	1,60	0,58	-2,1	2,8	0.75		
20	UD	2101	2	17	21	45	44	0,00	0,00	-2687.6	2687.6	0,32		
21	UQRK	_2	2	17	- 32	46	45	0,63	-1,02	-4076.9	4076.9	0.32		
22	ZO/GAMA*	23	195	7	- 22	251	252	-257,66	-219,68	324.8	477.5	88,56	-	
23	UQRK	94	144	8	6	25	- 31	258,06	210,29	33.9	345.5	86,10		
- 24	CONE	0	100	8	5	0	0	0,21	0,17	-1.0	1.0	0,00		
25	UQRK	2	2	23	26	47	42	26,82	24,33	23.7	43.3	0,32		
26	GLUON	21	2	23	27	48	49	8.50	8,18	6.0	13.3	0.75	STAT	· E
27	GLUON	21	2	23	28	50	51	73,27	61,24	12.0	96.2	0.75	SIAI	
- 28	GLUON	21	2	23	29	52	53	73,66	58,54	-6,3	94.3	0,75	SHO	WFR
29	GLUON	21	2	23	30	54	55	67,58	52,13	-7,3	85.7	0,75		
30	GLUON	21	2	23	31	56	57	6,98	4.60	2.3	8.7	0.75		
31	GLUON	21	2	23	43	58	59	1,24	1,26	3.6	4.1	0.75		

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#### > Pythia, Herwig, Sherpa

(each has one or more formulations of a parton shower)

- Sudakov approximation is not accurate for high-p<sub>T</sub> emissions, and intrinsic accuracy of cross sections is LO
  - showers combined with NLO through tools like MC@NLO or POWHEG
     (NNLO matching is a research topic with first tools

available)

Full matrix elements for hard emissions included through methods like MLM, CKKW, FxFx, Sherpa "merging" or through Vincia or MiNLO techniques

# hadronisation & MPI

essential models for realistic events

#### two main models for the parton-hadron transition ("hadronisation")



String Fragmentation (Pythia and friends)

б  $\mathcal{S}\mathcal{S}$ γ ð

> **Cluster Fragmentation** (Herwig) (& Sherpa) Pictures from ESW book<sub>37</sub>

#### multi-parton interactions (MPI, a.k.a. underlying event)



taken from 1206.2205

Allow 2→2 scatterings of multiple other partons in the incoming protons







While you can see jets with your eyes, to do quantitative physics, you need an algorithmic procedure that defines what exactly a jet is

#### make a choice, specify a Jet Definition



- Which particles do you put together into a same jet?
- How do you recombine their momenta (4-momentum sum is the obvious choice, right?)

"Jet [definitions] are legal contracts between theorists and experimentalists" -- MJ Tannenbaum

They're also a way of organising the information in an event 1000's of particles per events, up to 20.000,000 events per second



#### projection to jets should be resilient to QCD effects

**Two parameters,** *R* and  $p_{t,min}$ (These are the two parameters in essentially every widely used hadron-collider jet algorithm)

$$d_{ij} = \frac{1}{\max(p_{ti}^2, p_{tj}^2)} \frac{\Delta R_{ij}^2}{R^2}, \qquad d_{iB} = \frac{1}{p_{ti}^2}$$

 $\Delta R_{ij}^2 = (y_i - y_j)^2 + (\phi_i - \phi_j)^2$ 

# Sequential recombination algorithm

- 1. Find smallest of  $d_{ij}$ ,  $d_{iB}$
- 2. If *ij*, recombine them
- 3. If *iB*, call i a jet and remove from list of particles
- 4. repeat from step 1 until no particles left Only use jets with  $p_t > p_{t,min}$

*anti-k<sub>t</sub> algorithm Cacciari, GPS & Soyez, 0802.1189* 

# anti-k<sub>t</sub> in action

$$d_{ij} = \frac{1}{\max(p_{ti}^2, p_{tj}^2)} \frac{\Delta R_{ij}^2}{R^2}, \quad d_{iB} = \frac{1}{p_{ti}^2}$$

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Clustering grows around hard cores

$$d_{ij} = \frac{1}{\max(p_{ti}^2, p_{tj}^2)} \frac{\Delta R_{ij}^2}{R^2}, \quad d_{iB} = \frac{1}{p_{ti}^2}$$



Anti-kt gives circular jets ("cone-like") in a way that's infrared safe

# conclusions

#### ATLAS H $\rightarrow$ WW\* ANALYSIS [1604.02997]

# **3 Signal and background models**

The ggF and VBF production modes for  $H \rightarrow WW^*$  are modelled at next-to-leading order (NLO) in the strong coupling  $\alpha_S$  with the Powneg MC generator [22–25], interfaced with PYTHIA8 [26] (version 8.165) for the parton shower, hadronisation, and underlying event. The CT10 [27] PDF set is used and the parameters of the Pythia8 generator controlling the modelling of the parton shower and the underlying event are those corresponding to the AU2 set [28]. The Higgs boson mass set in the generation is 125.0 GeV, which is close to the measured value. The Powheg ggF model takes into account finite quark masses and a running-width Breit–Wigner distribution that includes electroweak corrections at NLO [29]. To improve the modelling of the Higgs boson  $p_{\rm T}$  distribution, a reweighting scheme is applied to reproduce the prediction of the next-to-next-to-leading-order (NNLO) and next-to-next-to-leading-logarithm (NNLL) dynamic-scale calculation given by the HREs 2.1 program [30] Events with  $\geq 2$  jets are further reweighted to reproduce the  $p_T^H$  spectrum predicted by the NLO Powheg simulation of Higgs boson production in association with two jets (H + 2 jets) [31]. Interference with continuum WW production [32, 33] has a negligible impact on this analysis due to the transverse-mass selection criteria described in Section 4 and is not included in the signal model.

Jets are reconstructed from topological clusters of calorimeter cells [50–52] using the anti- $k_t$  algorithm with a radius parameter of R = 0.4 [53]. Jet energies are corrected for the effects of calorimeter non-





#### CONCLUSIONS

- A huge number of ingredients goes into hadron-collider predictions and studies (a<sub>s</sub>, PDFs, matrix elements, resummation, parton showers, non-perturbative models, jet algorithms, etc.)
- ► a key idea is the separation of time scales ("factorisation")
  - short timescales: the hard process
  - Iong timescales: hadronic physics
  - ► in between: parton showers, resummation, DGLAP
- as long as you ask the right questions (e.g. look at jets, not individual hadrons), you can exploit this separation for quantitative, accurate, collider physics
# EXTRA SLIDES

## **GLUON V. HADRON MULTIPLICITY**

It turns out you can calculate the gluon multiplicity analytically, by summing all orders (n) of perturbation theory:

$$\langle N_g \rangle \sim \sum_n \frac{1}{(n!)^2} \left( \frac{C_A}{\pi b} \ln \frac{Q}{\Lambda} \right)^n$$
  
 $\sim \exp \sqrt{\frac{4C_A}{\pi b} \ln \frac{Q}{\Lambda}}$ 

Compare to data for hadron multiplicity ( $Q \equiv \sqrt{s}$ ) Including some other higher-order terms and fitting overall normalisation

**Agreement is amazing!** 



# nnlo

### NNLO hadron-collider calculations v. time



f(z) is some function with finite limit for  $z \to 0$ 

# **"SLICING"**

$$\sigma = \left(c - \ln \frac{1}{\text{cut}}\right) \cdot f(0) + \int_{\text{cut}}^{1} dz \frac{f(z)}{z}$$

virtual & counterterm: get from soft-collinear resummation

real part: use MC integration (cut has to be small, but not too small)

qT-subtraction: Catani, Grazzini

N-jettiness subtraction: Boughezal, Focke, Liu, Petriello; Gaunt, Stahlhofen, Tackmann, Walsh

f(z) is some function with finite limit for  $z \to 0$ 

# **LOCAL SUBTRACTION**

$$\sigma = c \cdot f(0) + \int_0^1 dz \left[ \frac{f(z)}{z} - \frac{f(0)}{z} \right]$$

virtual & counterterm: may need (tough) analytic calc<sup>n</sup> *real part: MC integration is finite even without cut* 

Sector decomposition: Anastasiou, Melnikov, Petriello; Binoth, Heinrich Antennae subtraction: Kosower; Gehrmann, Gehrmann-de Ridder, Glover Sector-improved residue subtraction: Czakon; Boughezal, Melnikov, Petriello CoLorFul subtraction: Del Duca, Somogyi, Trocsanyi Projection-to-Born: Cacciari, Dreyer, Karlberg, GPS, Zanderighi

### WHAT PRECISION AT NNLO?



For many processes NNLO scale band is  ${\sim}\pm2\%$  But only in 3/17 cases is NNLO (central) within NLO scale band...

# WHAT PRECISION AT NNLO?



For many processes NNLO scale band is  $\sim \pm 2\%$ But only in 3/17 cases is NNLO (central) within NLO scale band...

#### Processes currently known through NNLO

dijets	O(3%)	gluon-gluon, gluon-quark	PDFs, strong couplings, BSM
H+0 jet	O(3-5 %)	fully inclusive (N3LO )	Higgs couplings
H+1 jet	O(7%)	fully exclusive; Higgs decays, infinite mass tops	Higgs couplings, Higgs p <sub>t</sub> , structure for the ggH vertex.
tT pair	O(4%)	fully exclusive, stable tops	top cross section, mass, p <sub>t</sub> , FB asymmetry, PDFs, BSM
single top	O(1%)	fully exclusive, stable tops, t-channel	V <sub>tb</sub> , width, PDFs
WBF	O(1%)	exclusive, VBF cuts	Higgs couplings
W+j	O(1%)	fully exclusive, decays	PDFs
Z+j	O(1-3%)	decays, off-shell effects	PDFs
ZH	O(3-5 %)	decays to bb at NLO	Higgs couplings (H-> bb)
ZZ	O(4%)	fully exclusive	Trilinear gauge couplings, BSM
WW	O(3%)	fully inclusive	Trilinear gauge couplings, BSM
top decay	O(1-2 %)	exclusive	Top couplings
H -> bb	O(1-2 %)	exclusive, massless	Higgs couplings, boosted

y, February 27, 16

done ~ in past year

K. Melnikov @ KITP

# **n3lo**

Higgs via gluon fusion Higgs via weak-boson fusion



# N3L0 CONVERGENCE?



VBF converges much faster than ggF

But both calc<sup>ns</sup> share feature that NNLO fell outside NLO scale band, while N3LO (with good central scale choice) is very close to NNLO N3L0 splitting functions not known. But N3L0 DIS coefficient functions are known and their impact for quarks is >> NNL0 splitting-function scale variation (~0.1%)

Dreyer & Karlberg, 1606.00840



First results on N3L0 splitting-fn moments e-Print: arXiv:1605.08408 First Forcer results on deep-inelastic scattering and related quantities

B. Ruijl, T. Ueda, J.A.M. Vermaseren (NIKHEF, Amsterdam), J. Davies, A. Vogt (Liverpool U., Dept. Math.).

# Zpt

## Z $p_T$ : Data v. two theory calculations

#### NNLO ~ ±1.5 %



### X-sections normalised to Z are great, if we understand Z production



Up to 5% discrepancy?

Are NNLO scale errors (~0.5%) a reliable indicator of uncertainties?

Does it matter, given the large luminosity uncertainty?