

# Jets at Hadron Colliders (2)

Gavin Salam

CERN, Princeton and LPTHE/Paris (CNRS)

CERN Academic Training Lectures  
30 March - 1 April 2011

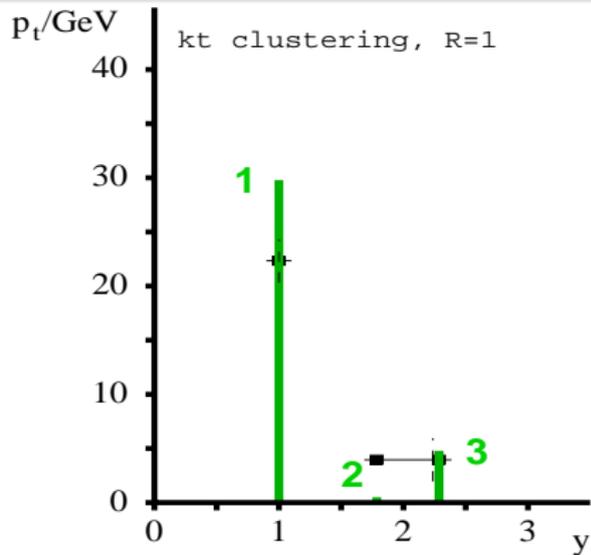
# A full set of IRC-safe jet algorithms

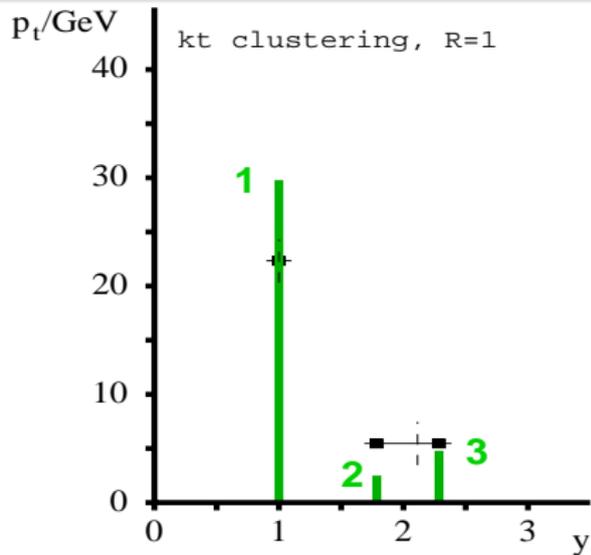
Generalise inclusive-type sequential recombination with

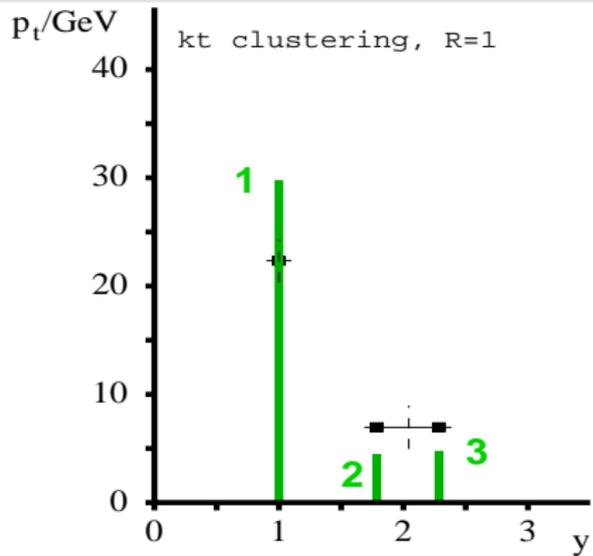
$$d_{ij} = \min(k_{ti}^{2p}, k_{tj}^{2p}) \Delta R_{ij}^2 / R^2 \quad d_{iB} = k_{ti}^{2p}$$

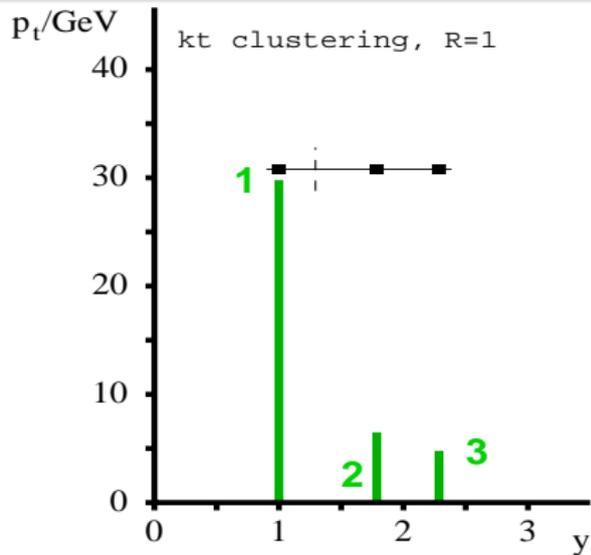
	Alg. name	Comment	time
$p = 1$	$k_t$ CDOSTW '91-93; ES '93	Hierarchical in rel. $k_t$	$N \ln N$ exp.
$p = 0$	Cambridge/Aachen Dok, Leder, Moretti, Webber '97 Wengler, Wobisch '98	Hierarchical in angle Scan multiple $R$ at once $\leftrightarrow$ QCD angular ordering	$N \ln N$
$p = -1$	anti- $k_t$ Cacciari, GPS, Soyez '08 $\sim$ reverse- $k_t$ Delsart	Hierarchy meaningless, jets like CMS cone (IC-PR)	$N^{3/2}$
SC-SM	SISCone GPS Soyez '07 + Tevatron run II '00	Replaces JetClu, ATLAS MidPoint (xC-SM) cones	$N^2 \ln N$ exp.

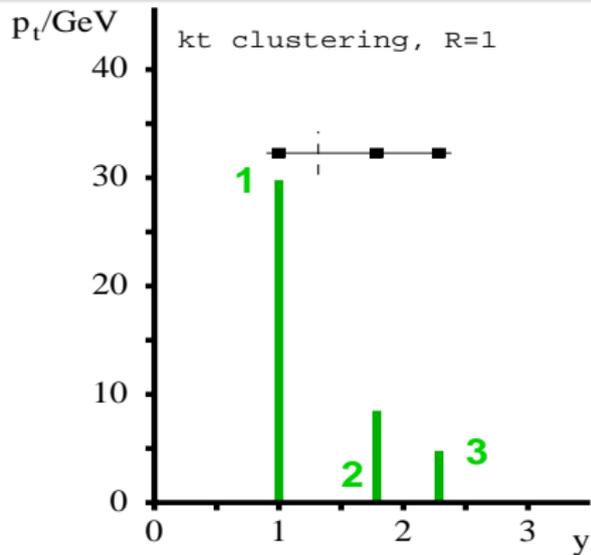
**All these algorithms [& much more] coded in (efficient) C++ at**  
<http://fastjet.fr/> (Cacciari, GPS & Soyez '05-'11)

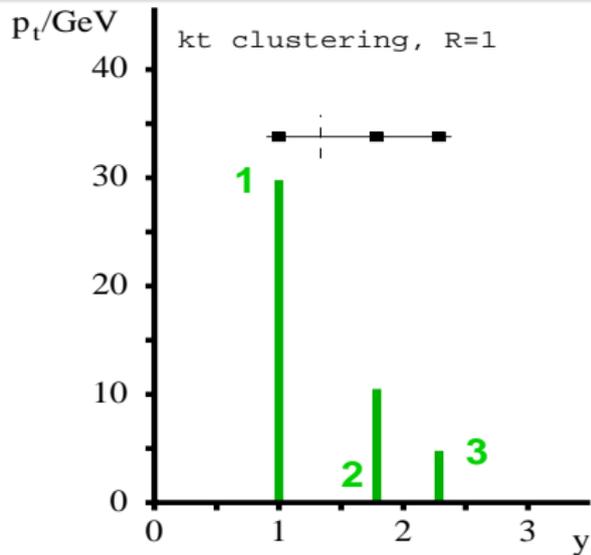


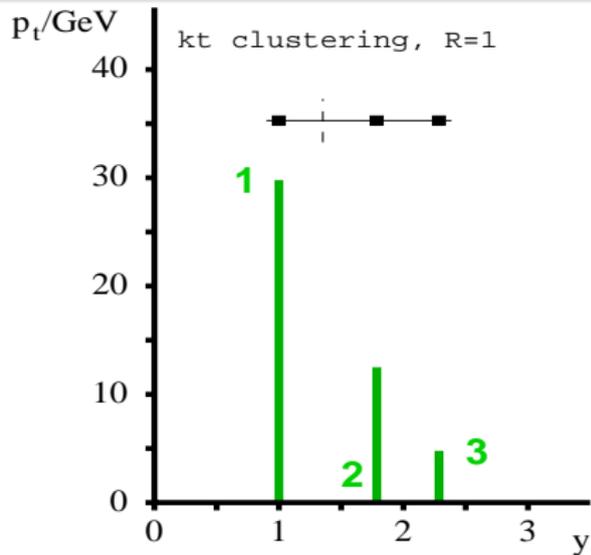


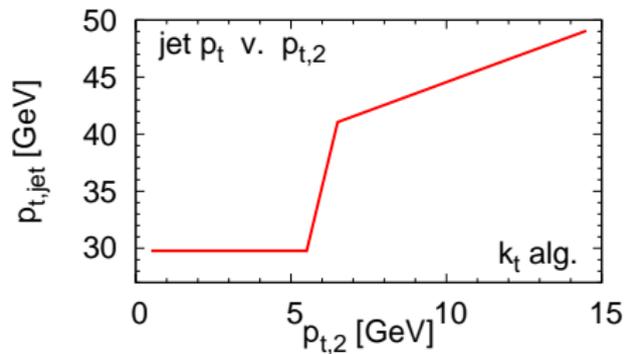
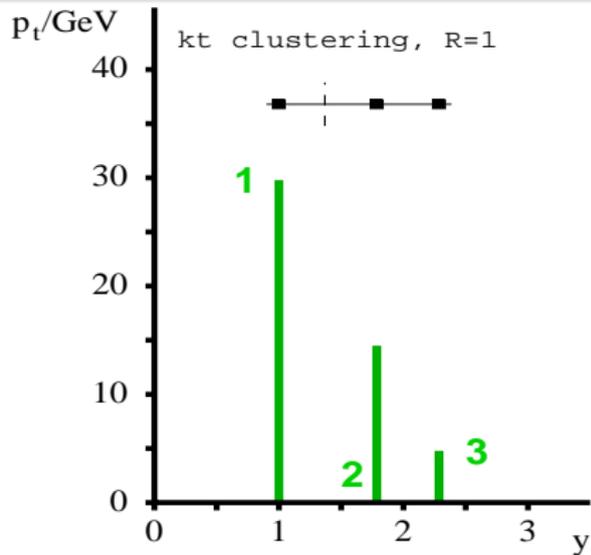


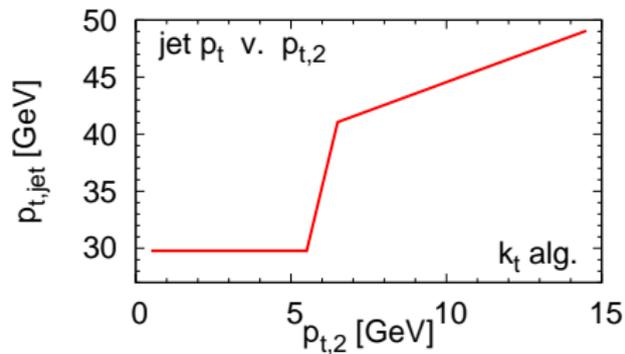
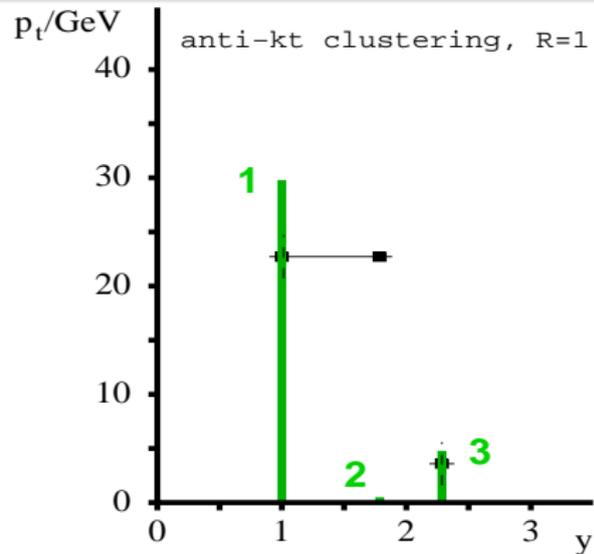
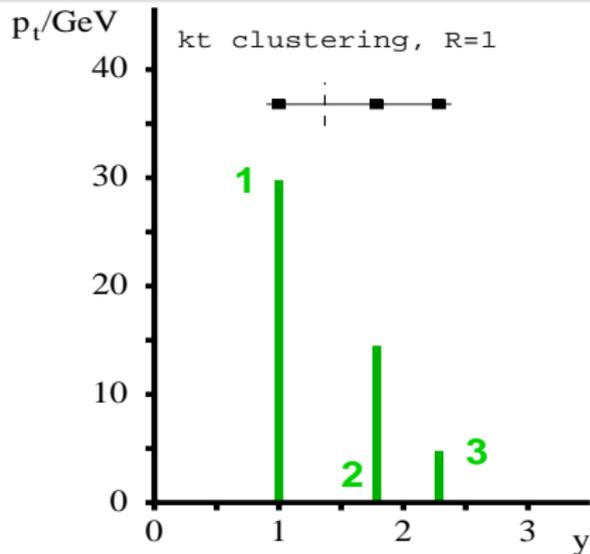


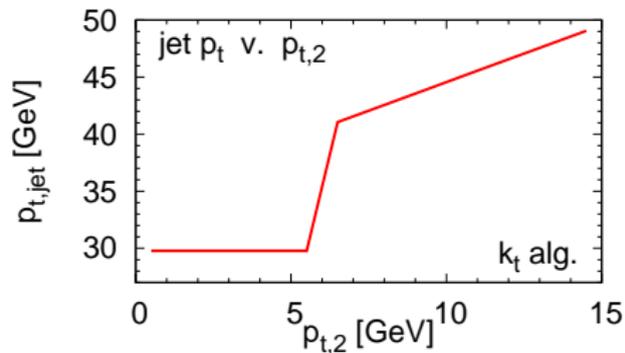
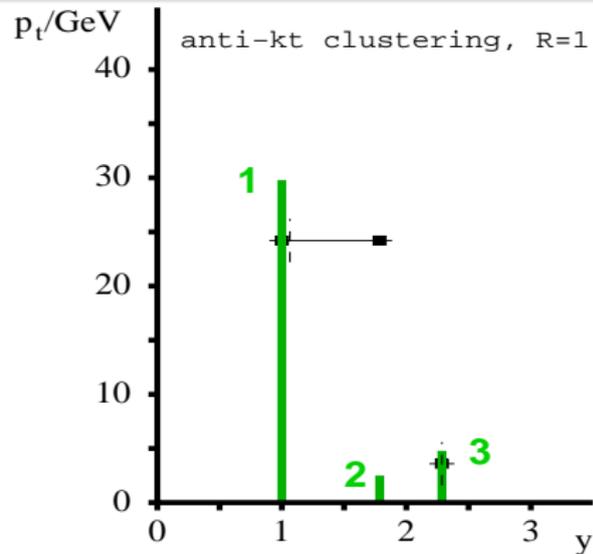
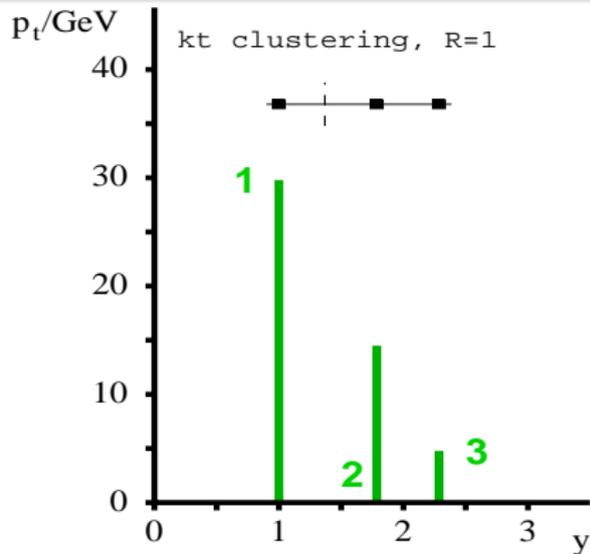


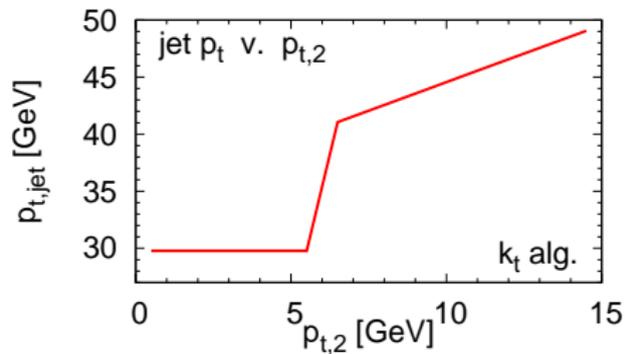
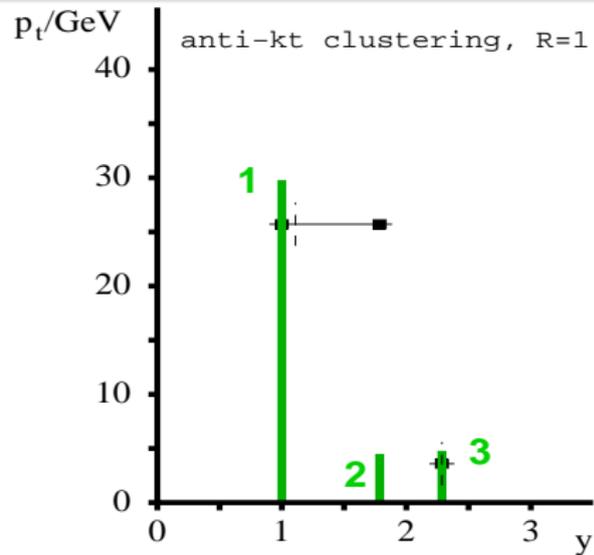
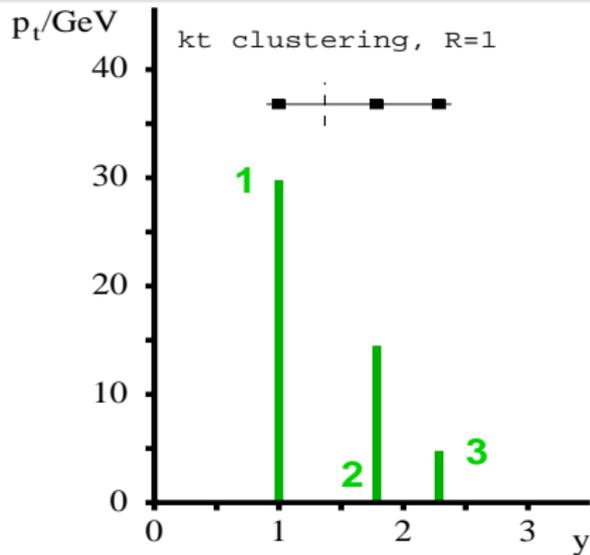


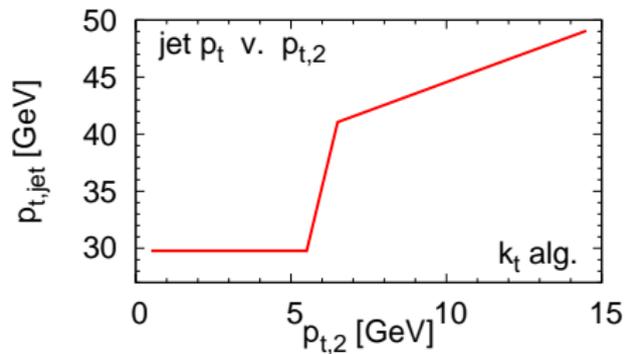
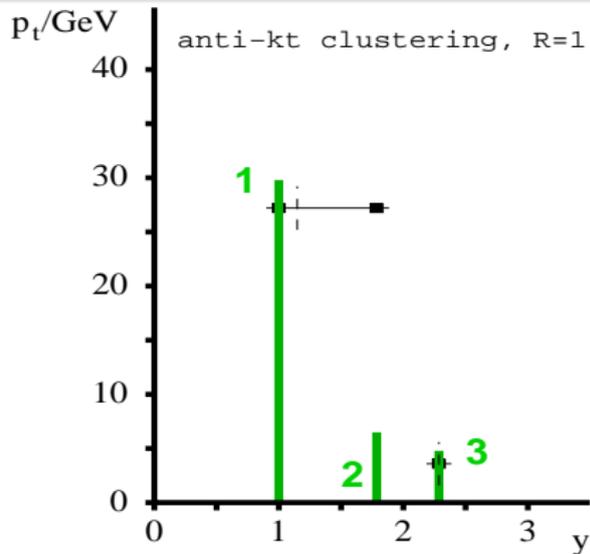
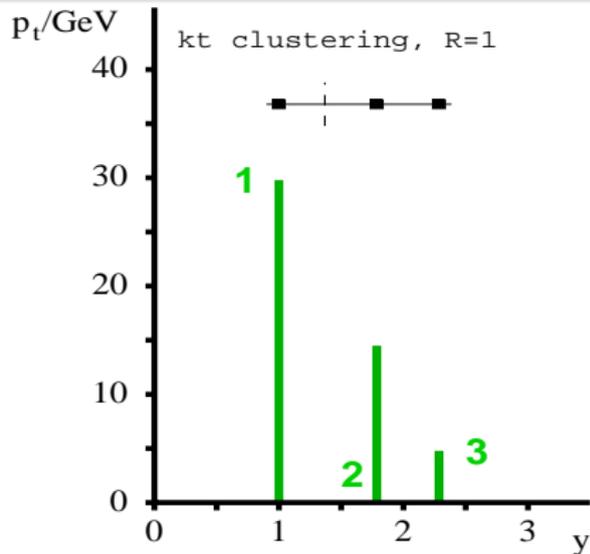


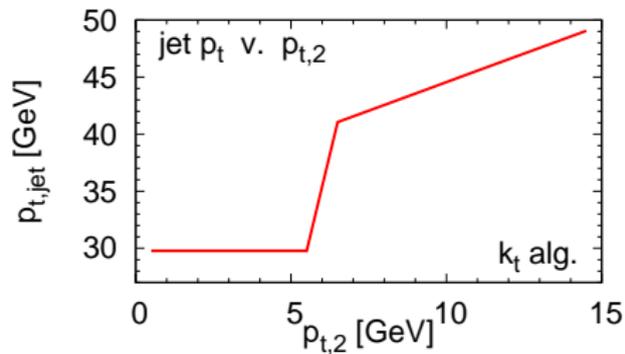
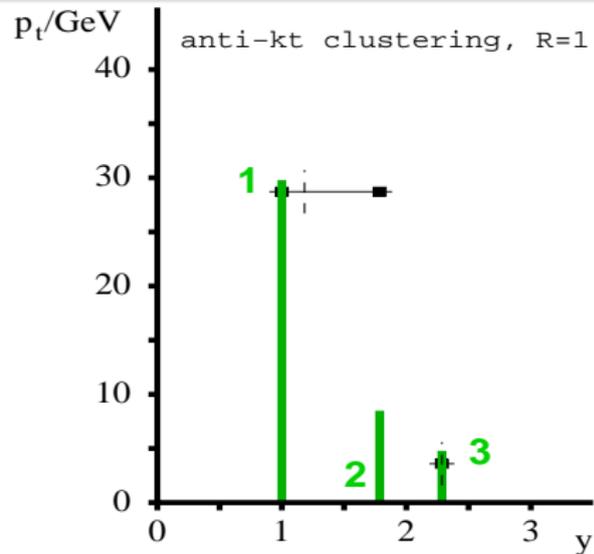
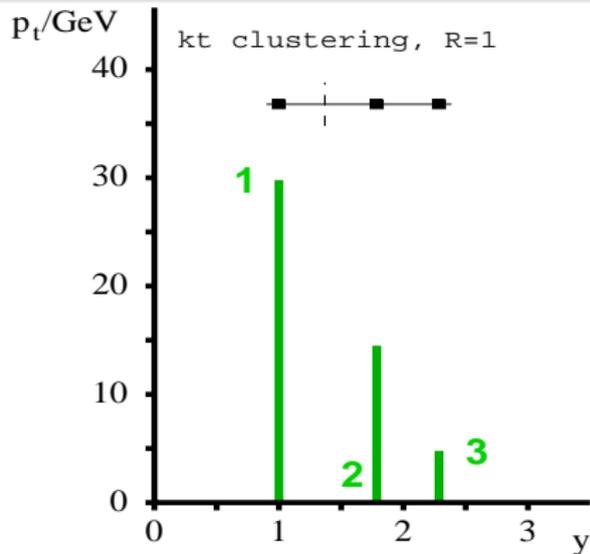


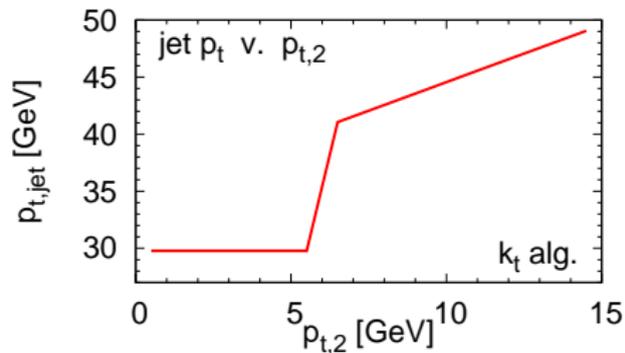
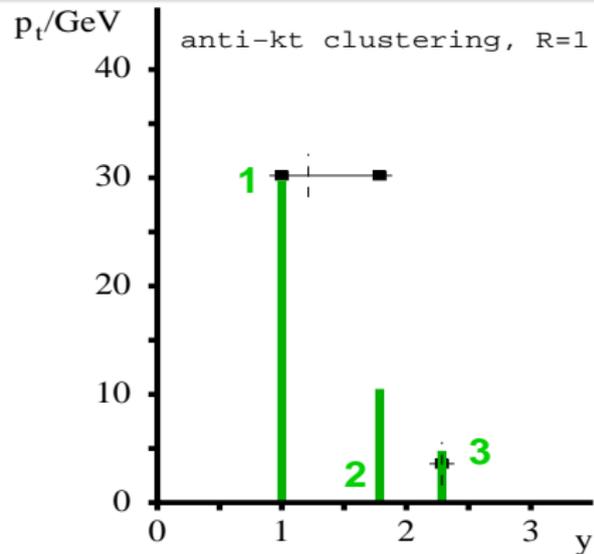
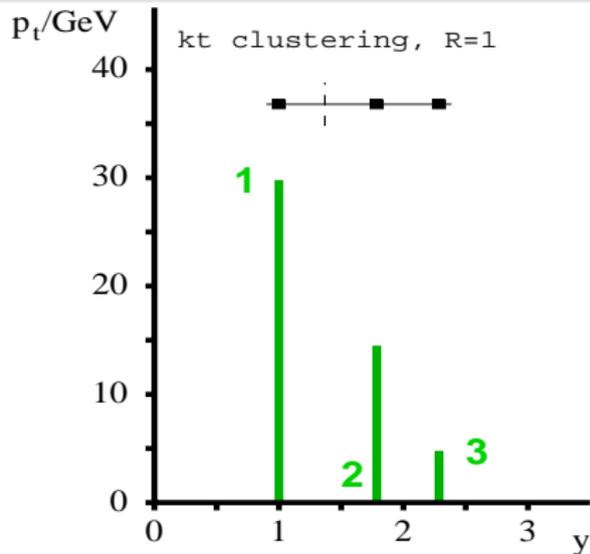


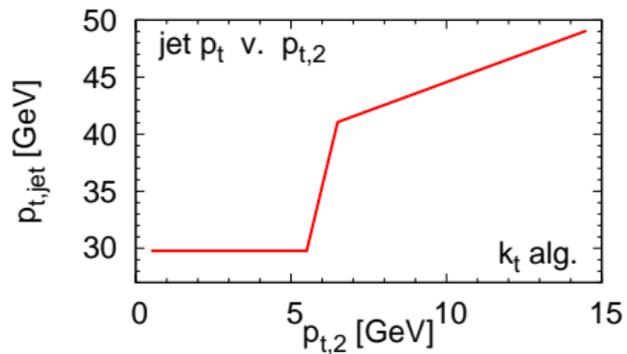
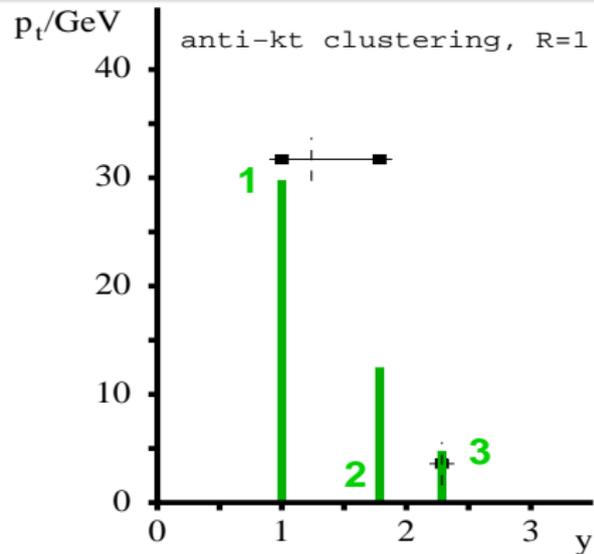
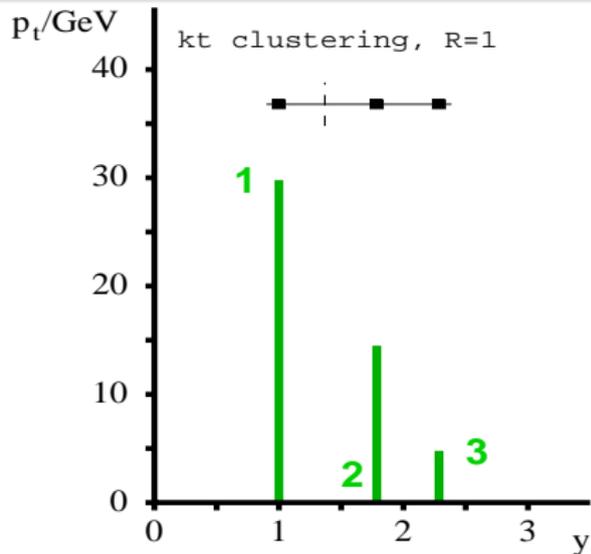


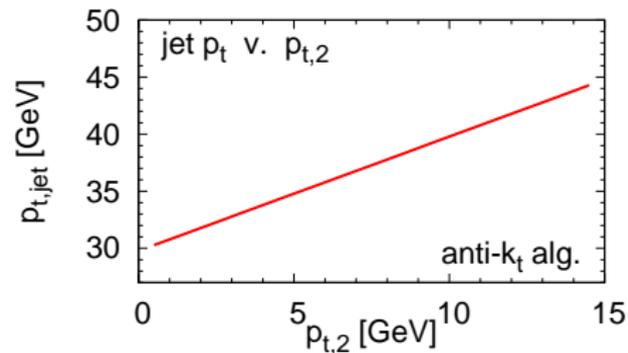
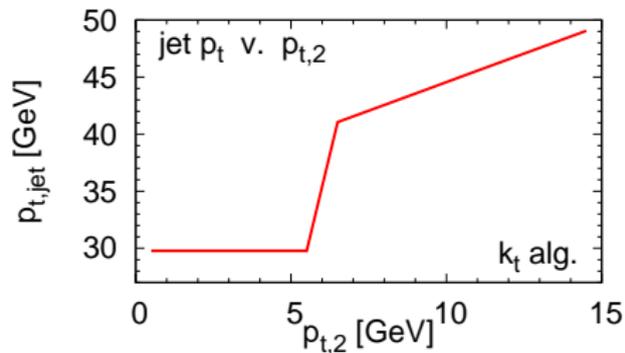
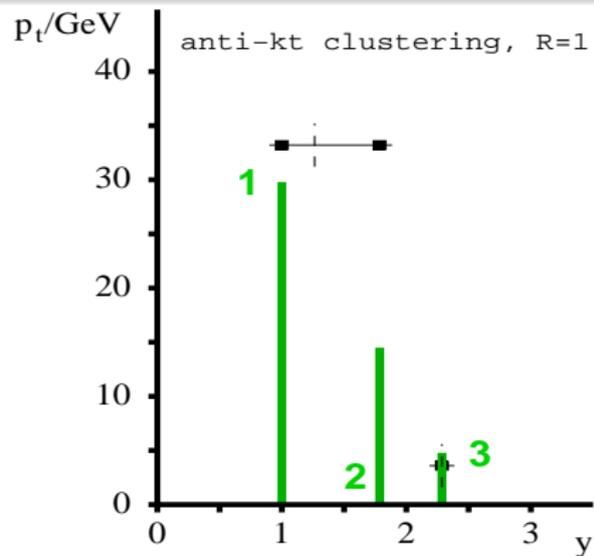
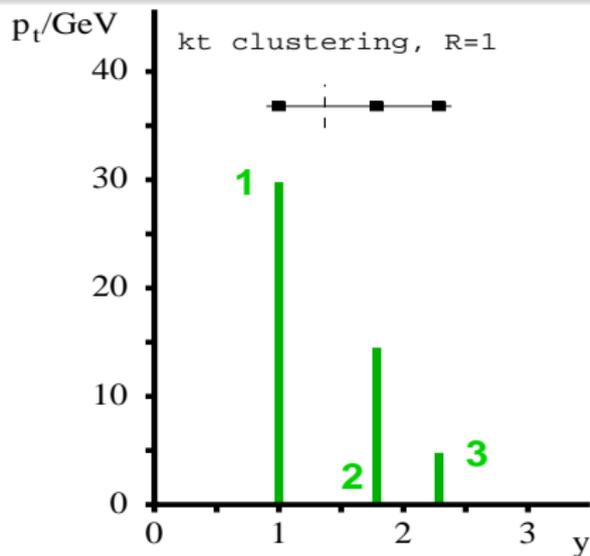


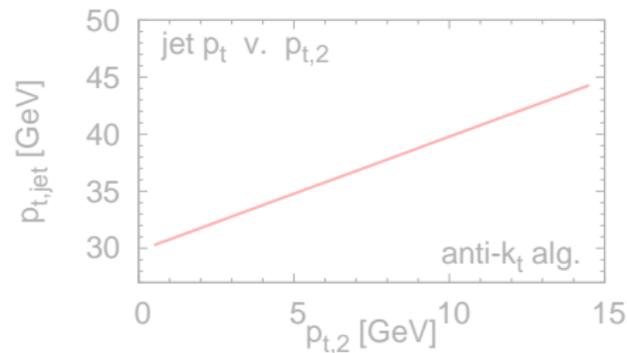
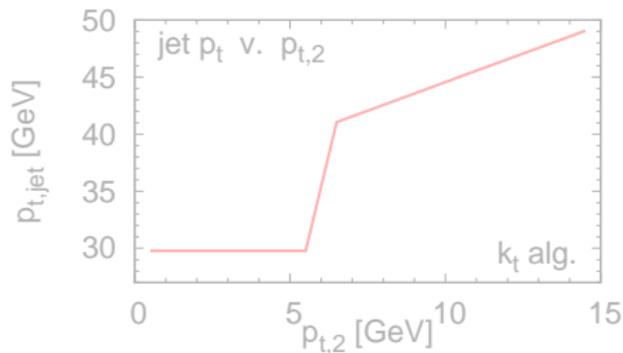
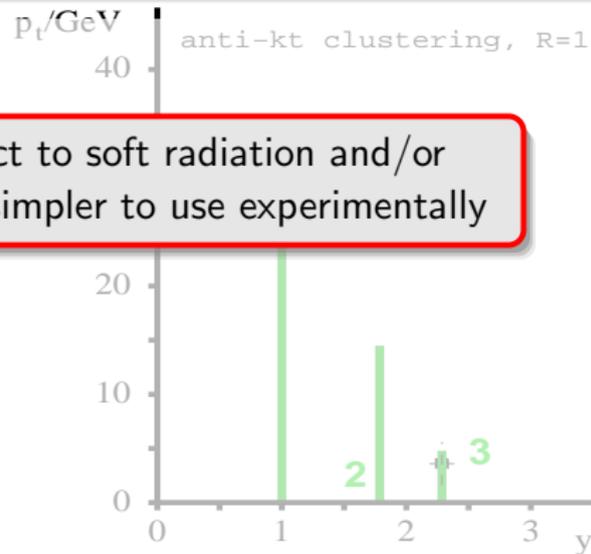
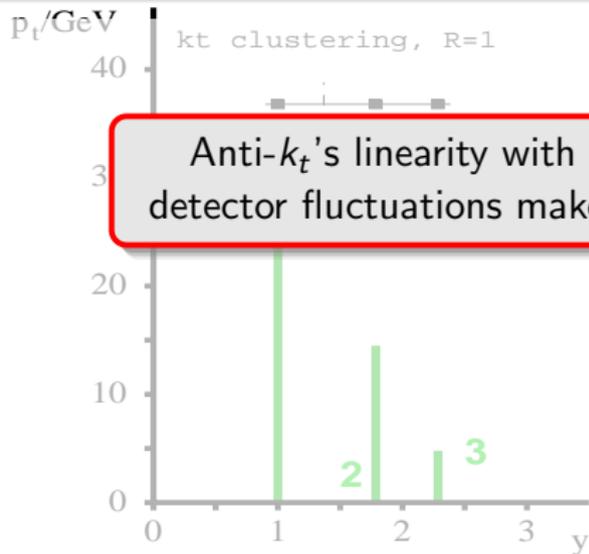












The full cross section that you measure in experiment should correspond to an expression looking roughly as follows:

$$\sigma^{full} = \sigma_{LO} \left( 1 + \alpha_s c_1 + \alpha_s^2 c_2 + \alpha_s^3 c_3 + \dots + \mathcal{O} \left( \frac{\Lambda_{QCD}}{p_t} \right) \right)$$

A perturbative series  
plus a non-perturbative contribution, suppressed by a power of  $\Lambda_{QCD}/p_t$

We don't have the technology to calculate the full series or the non-perturbative part. Typically, one might “just” calculate next-to-leading order

$$\sigma^{NLO} = \sigma_{LO} (1 + \alpha_s c_1)$$

The point to perturbation theory is that the  $c_2 \alpha_s^2$ , etc. terms are small compared to the ones you have calculated — *hence (e.g.) NLO should be a good approximation.*

The full cross section that you measure in experiment should correspond to an expression looking roughly as follows:

$$\sigma^{full} = \sigma_{LO} \left( 1 + \alpha_s c_1 + \alpha_s^2 c_2 + \alpha_s^3 c_3 + \dots + \mathcal{O} \left( \frac{\Lambda_{QCD}}{p_t} \right) \right)$$

A perturbative series  
plus a non-perturbative contribution, suppressed by a power of  $\Lambda_{QCD}/p_t$

We don't have the technology to calculate the full series or the non-perturbative part. Typically, one might “just” calculate next-to-leading order

$$\sigma^{NLO} = \sigma_{LO} (1 + \alpha_s c_1)$$

The point to perturbation theory is that the  $c_2 \alpha_s^2$ , etc. terms are small compared to the ones you have calculated — *hence (e.g.) NLO should be a good approximation.*

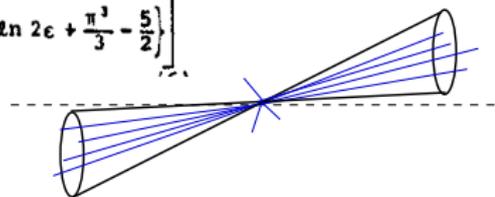
What happens with an infrared or collinear unsafe algorithm?

First 'jet algorithm' dates back to **Sterman and Weinberg (1977)** — the original infrared-safe cross section:

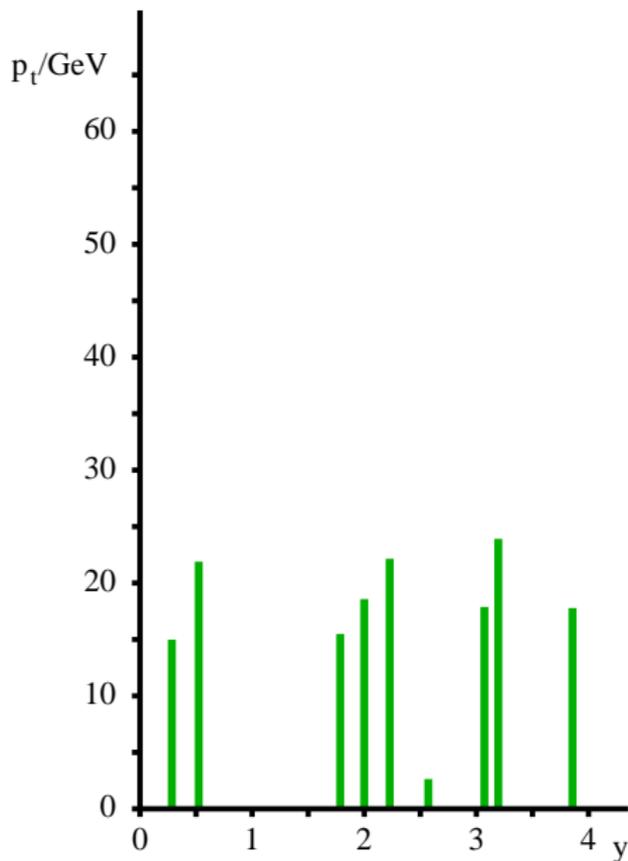
To study jets, we consider the partial cross section

$\sigma(E, \theta, \Omega, \epsilon, \delta)$  for  $e^+e^-$  hadron production events, in which all but a fraction  $\epsilon \ll 1$  of the total  $e^+e^-$  energy  $E$  is emitted within some pair of oppositely directed cones of half-angle  $\delta \ll 1$ , lying within two fixed cones of solid angle  $\Omega$  (with  $\pi\delta^2 \ll \Omega \ll 1$ ) at an angle  $\theta$  to the  $e^+e^-$  beam line. We expect this to be measur-

$$\sigma(E, \theta, \Omega, \epsilon, \delta) = (d\sigma/d\Omega)_0 \Omega \left[ 1 - (g_E^2/3\pi^2) \left\{ 3\ln \delta + 4\ln \delta \ln 2\epsilon + \frac{\pi^2}{3} - \frac{5}{2} \right\} \right]$$



Groundbreaking; good for 2 jets in  $e^+e^-$  but generalisations to hadron colliders often had problems

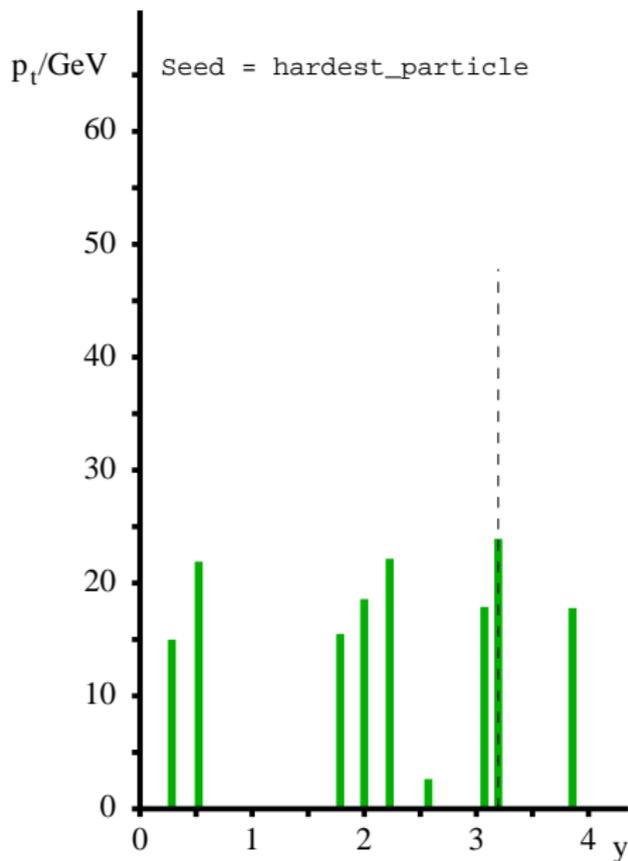


One of the simplest of the cone algs  
e.g. CMS iterative cone

- ▶ Take hardest particle as seed for cone axis
- ▶ Draw cone around seed
- ▶ Sum the momenta use as new seed direction, iterate until stable
- ▶ Convert contents into a “jet” and remove from event

## Notes

- ▶ “Hardest particle” is collinear unsafe more right away...



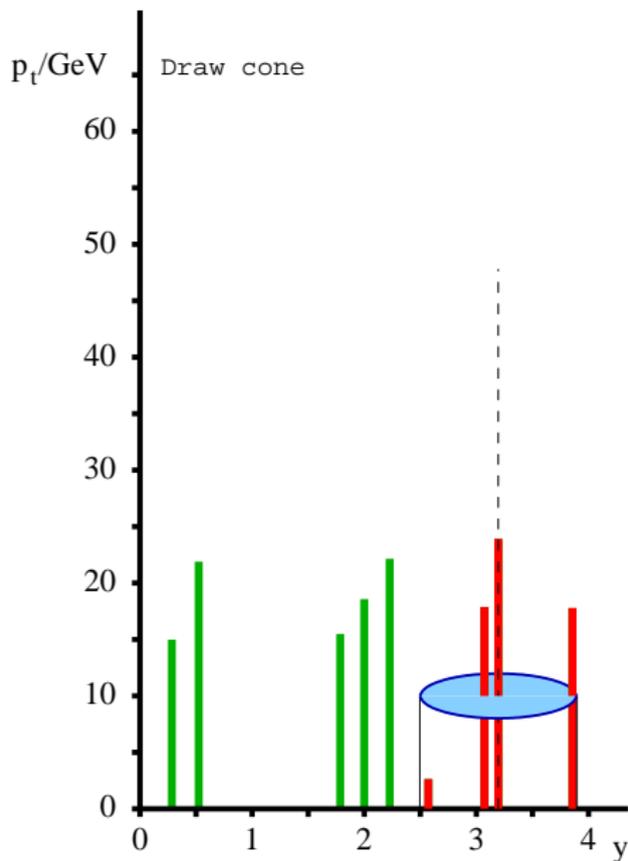
One of the simplest of the cone algs

e.g. CMS iterative cone

- ▶ Take hardest particle as seed for cone axis
- ▶ Draw cone around seed
- ▶ Sum the momenta use as new seed direction, iterate until stable
- ▶ Convert contents into a “jet” and remove from event

Notes

- ▶ “Hardest particle” is collinear unsafe more right away...



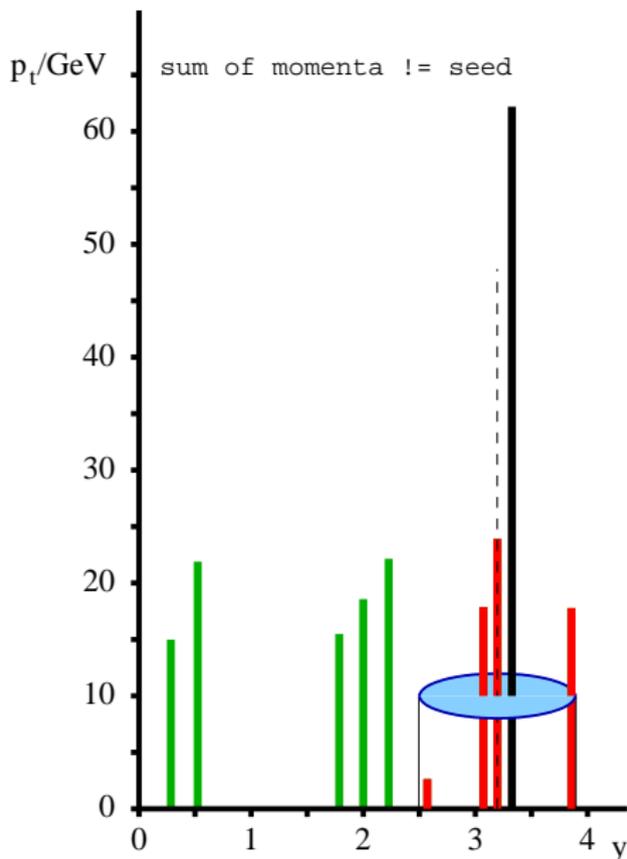
One of the simplest of the cone algs

e.g. CMS iterative cone

- ▶ Take hardest particle as seed for cone axis
- ▶ Draw cone around seed
- ▶ Sum the momenta use as new seed direction, iterate until stable
- ▶ Convert contents into a “jet” and remove from event

Notes

- ▶ “Hardest particle” is collinear unsafe
- ▶ more right away...



One of the simplest of the cone algs

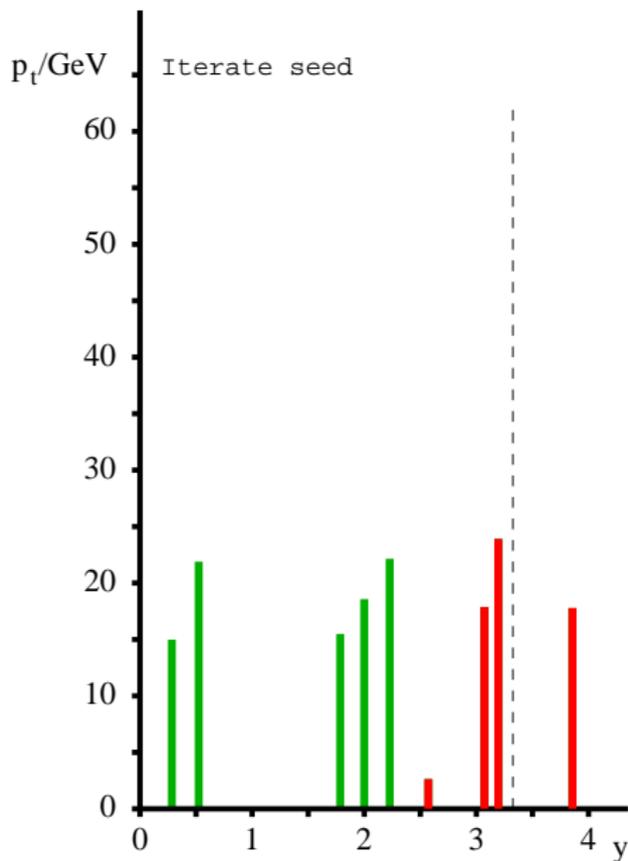
e.g. CMS iterative cone

- ▶ Take hardest particle as seed for cone axis
- ▶ Draw cone around seed
- ▶ **Sum the momenta** use as new seed direction, iterate until stable

▶ Convert contents into a “jet” and remove from event

Notes

▶ “Hardest particle” is collinear unsafe  
more right away...



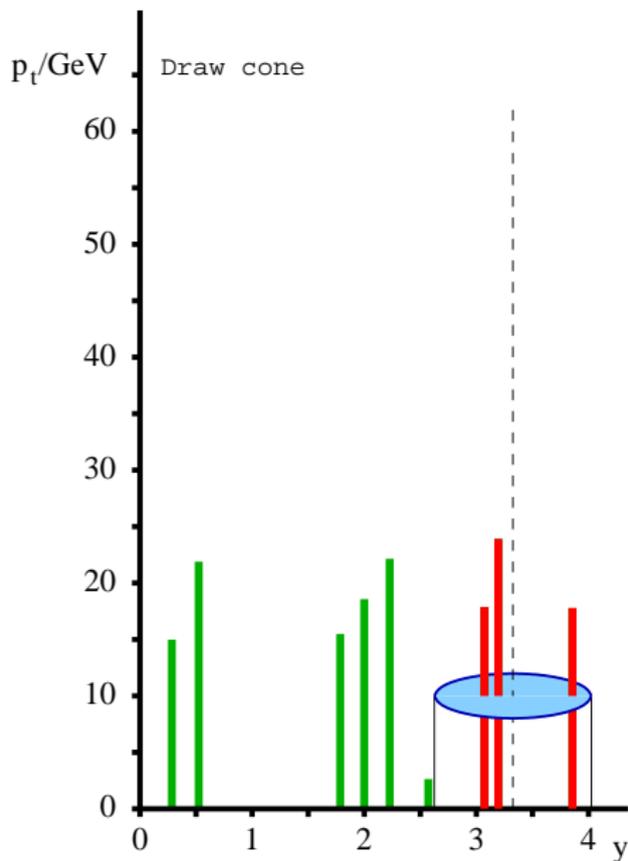
One of the simplest of the cone algs

e.g. CMS iterative cone

- ▶ Take hardest particle as seed for cone axis
- ▶ Draw cone around seed
- ▶ Sum the momenta **use as new seed direction**, iterate until stable
- ▶ Convert contents into a “jet” and remove from event

Notes

- ▶ “Hardest particle” is collinear unsafe more right away...



One of the simplest of the cone algs

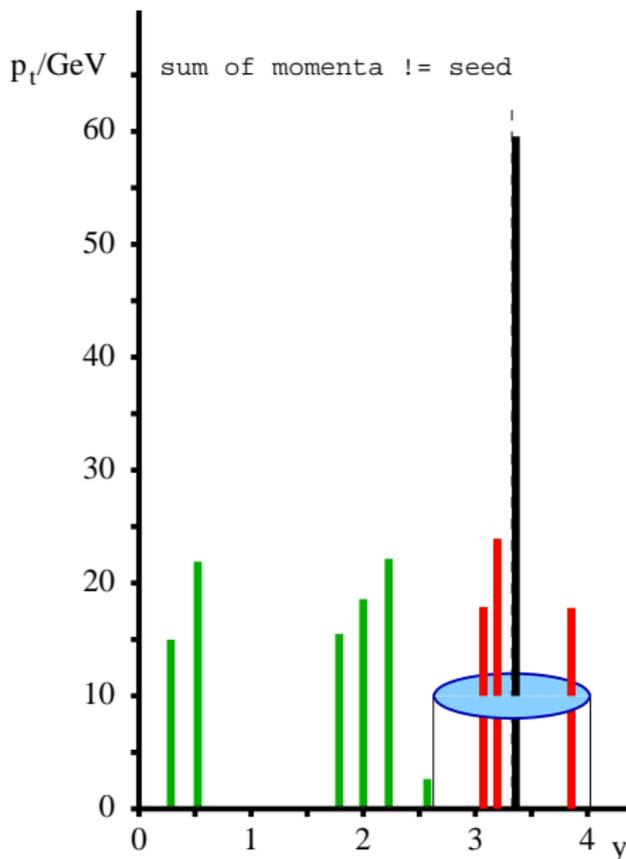
e.g. CMS iterative cone

- ▶ Take hardest particle as seed for cone axis
- ▶ Draw cone around seed
- ▶ Sum the momenta use as new seed direction, iterate until stable

▶ Convert contents into a "jet" and remove from event

Notes

▶ "Hardest particle" is collinear unsafe  
▶ more right away...



One of the simplest of the cone algs

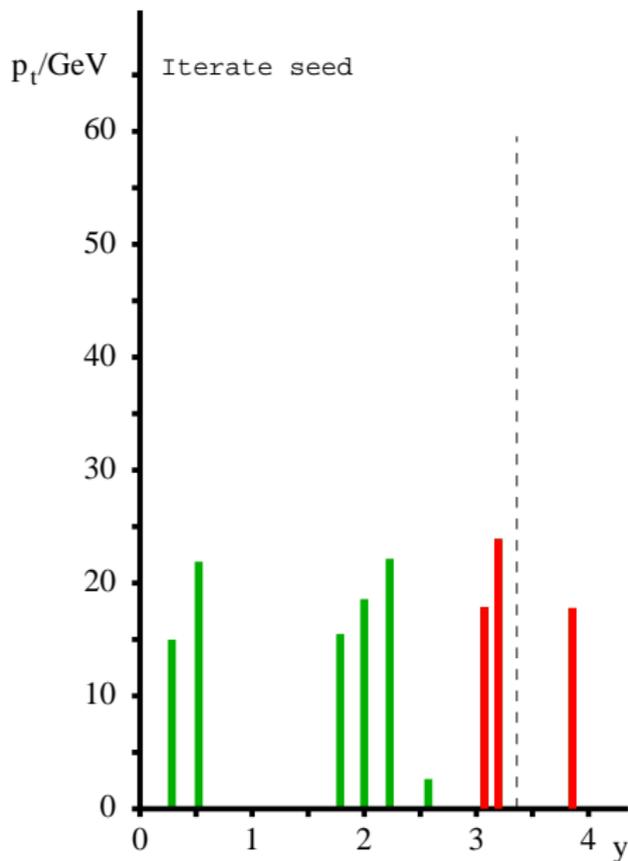
e.g. CMS iterative cone

- ▶ Take hardest particle as seed for cone axis
- ▶ Draw cone around seed
- ▶ **Sum the momenta** use as new seed direction, iterate until stable

▶ Convert contents into a “jet” and remove from event

Notes

▶ “Hardest particle” is collinear unsafe  
more right away...



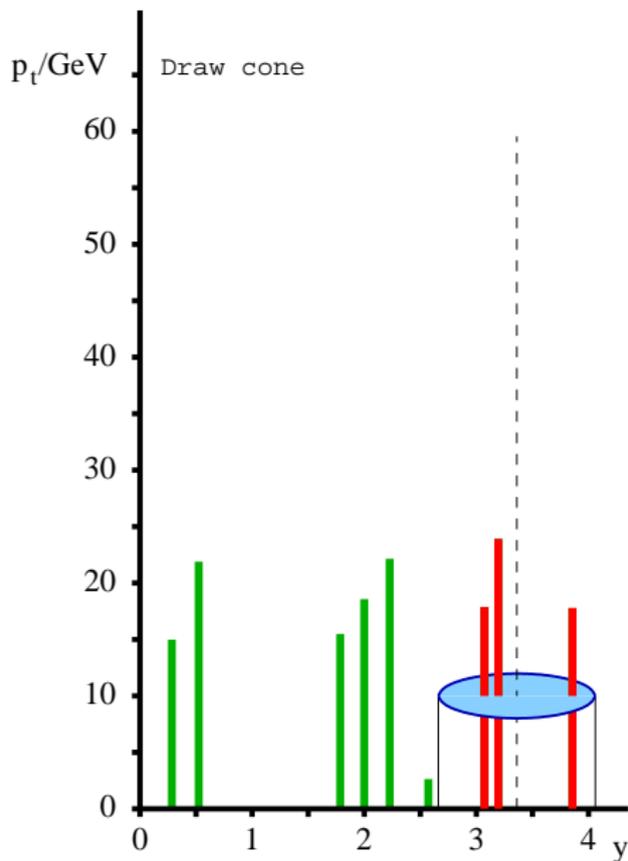
One of the simplest of the cone algs

e.g. CMS iterative cone

- ▶ Take hardest particle as seed for cone axis
- ▶ Draw cone around seed
- ▶ Sum the momenta **use as new seed direction**, iterate until stable
- ▶ Convert contents into a “jet” and remove from event

Notes

- ▶ “Hardest particle” is collinear unsafe more right away...



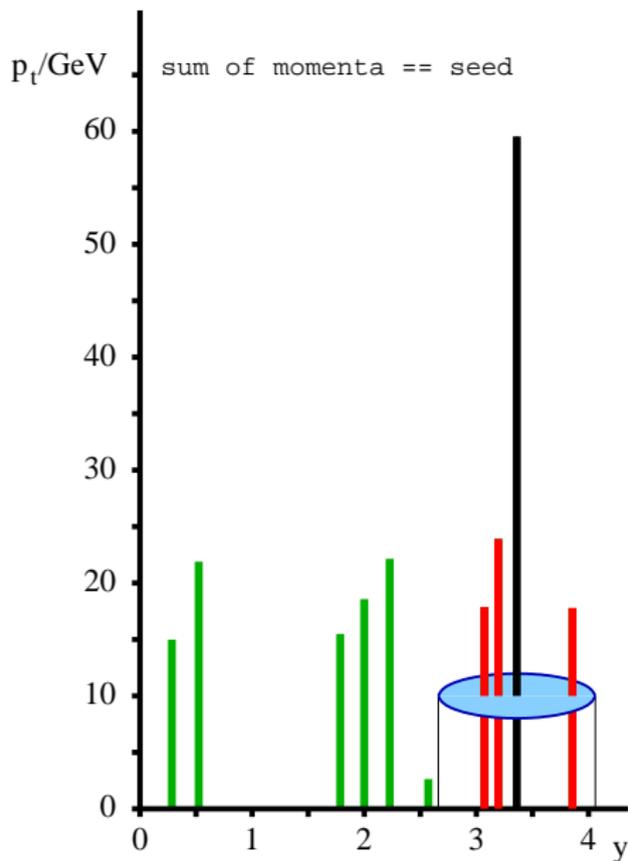
One of the simplest of the cone algs

e.g. CMS iterative cone

- ▶ Take hardest particle as seed for cone axis
- ▶ Draw cone around seed
- ▶ Sum the momenta use as new seed direction, iterate until stable
- ▶ Convert contents into a “jet” and remove from event

Notes

- ▶ “Hardest particle” is collinear unsafe
- ▶ more right away...



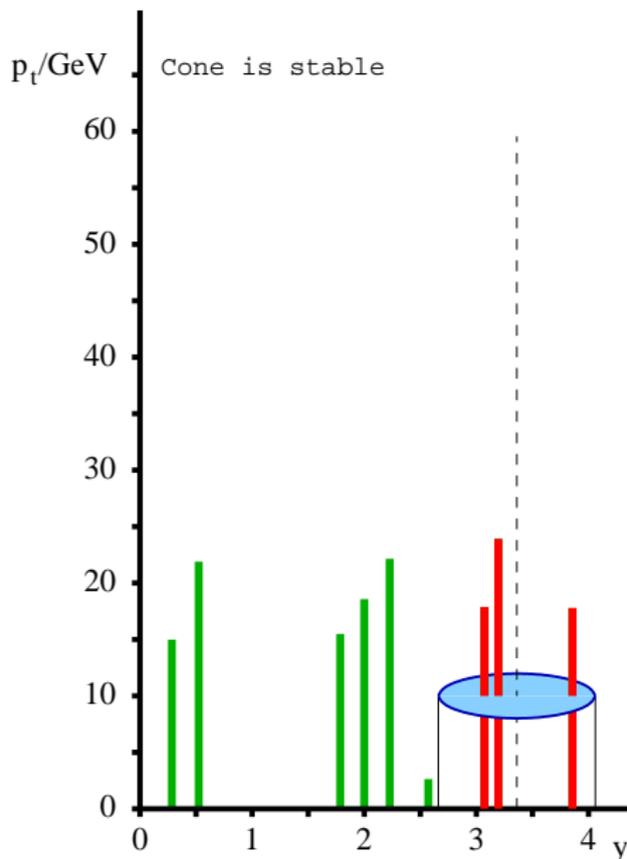
One of the simplest of the cone algs

e.g. CMS iterative cone

- ▶ Take hardest particle as seed for cone axis
- ▶ Draw cone around seed
- ▶ Sum the momenta use as new seed direction, iterate **until stable**
- ▶ Convert contents into a “jet” and remove from event

Notes

- ▶ “Hardest particle” is collinear unsafe more right away...



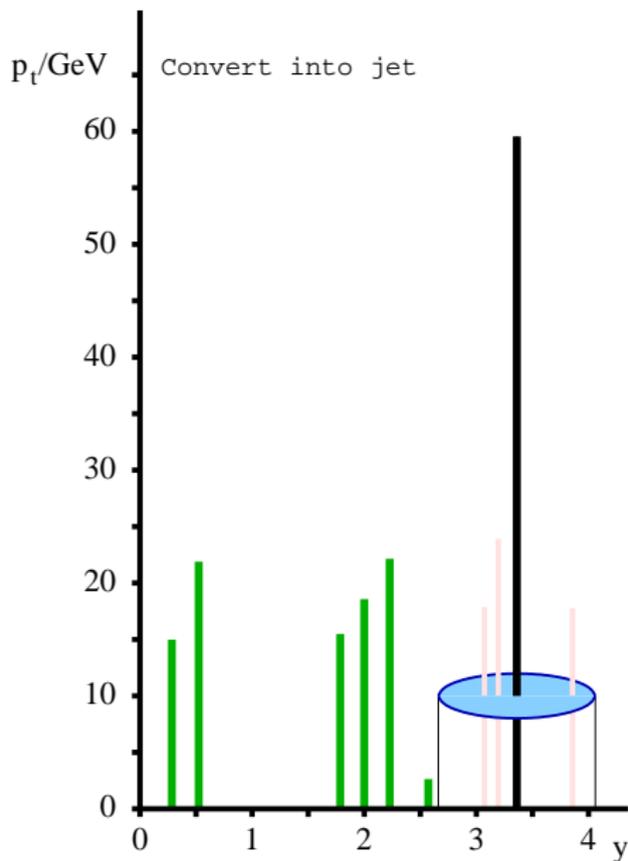
One of the simplest of the cone algs

e.g. CMS iterative cone

- ▶ Take hardest particle as seed for cone axis
- ▶ Draw cone around seed
- ▶ Sum the momenta use as new seed direction, iterate until stable
- ▶ Convert contents into a “jet” and remove from event

Notes

- ▶ “Hardest particle” is collinear unsafe
- ▶ more right away...



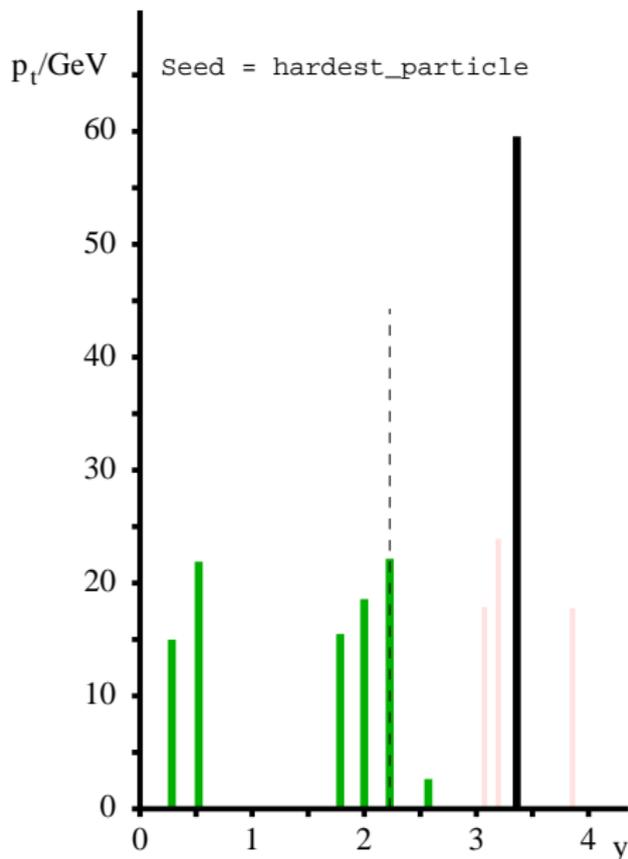
One of the simplest of the cone algs

e.g. CMS iterative cone

- ▶ Take hardest particle as seed for cone axis
- ▶ Draw cone around seed
- ▶ Sum the momenta use as new seed direction, iterate until stable
- ▶ Convert contents into a “jet” and remove from event

Notes

- ▶ “Hardest particle” is collinear unsafe more right away...



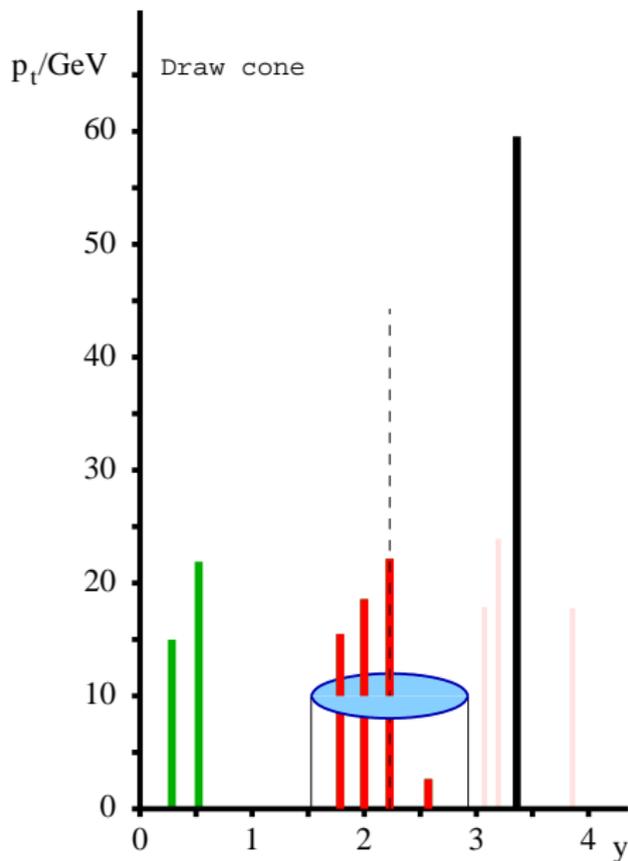
One of the simplest of the cone algs

e.g. CMS iterative cone

- ▶ Take hardest particle as seed for cone axis
- ▶ Draw cone around seed
- ▶ Sum the momenta use as new seed direction, iterate until stable
- ▶ Convert contents into a “jet” and remove from event

Notes

- ▶ “Hardest particle” is collinear unsafe more right away...

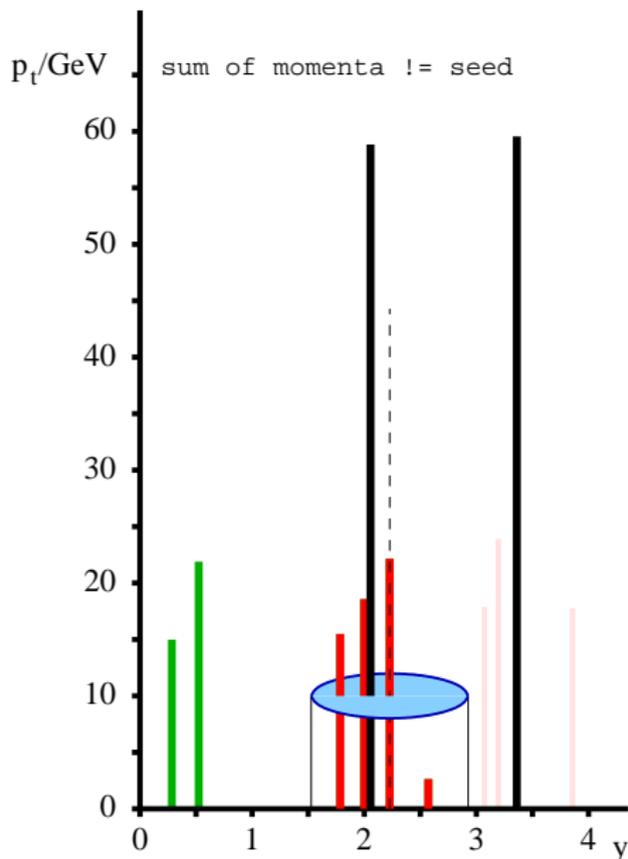


One of the simplest of the cone algs  
e.g. CMS iterative cone

- ▶ Take hardest particle as seed for cone axis
- ▶ Draw cone around seed
- ▶ Sum the momenta use as new seed direction, iterate until stable
- ▶ Convert contents into a “jet” and remove from event

## Notes

- ▶ “Hardest particle” is collinear unsafe more right away...



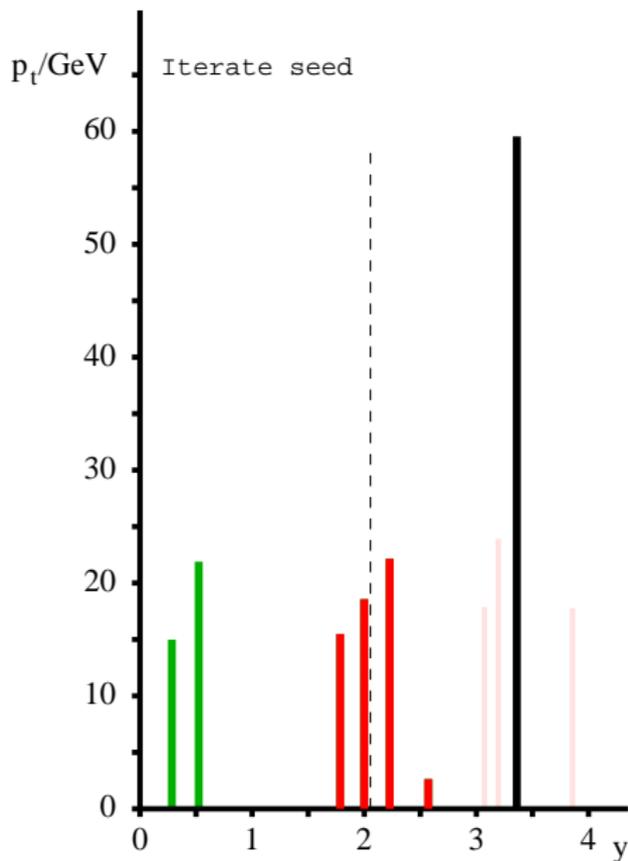
One of the simplest of the cone algs

e.g. CMS iterative cone

- ▶ Take hardest particle as seed for cone axis
- ▶ Draw cone around seed
- ▶ Sum the momenta use as new seed direction, iterate until stable
- ▶ Convert contents into a “jet” and remove from event

Notes

- ▶ “Hardest particle” is collinear unsafe more right away...

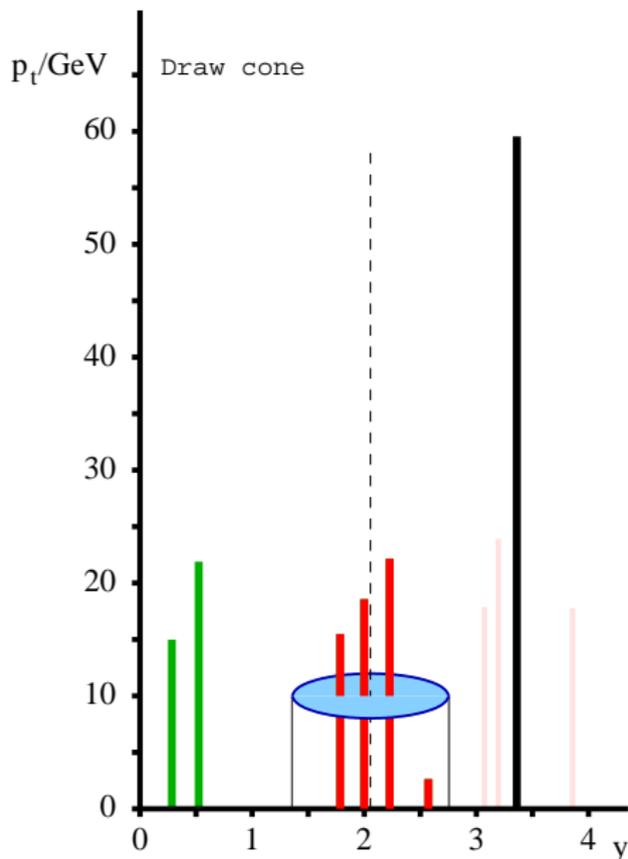


One of the simplest of the cone algs  
e.g. CMS iterative cone

- ▶ Take hardest particle as seed for cone axis
- ▶ Draw cone around seed
- ▶ Sum the momenta use as new seed direction, iterate until stable
- ▶ Convert contents into a “jet” and remove from event

## Notes

- ▶ “Hardest particle” is collinear unsafe more right away...

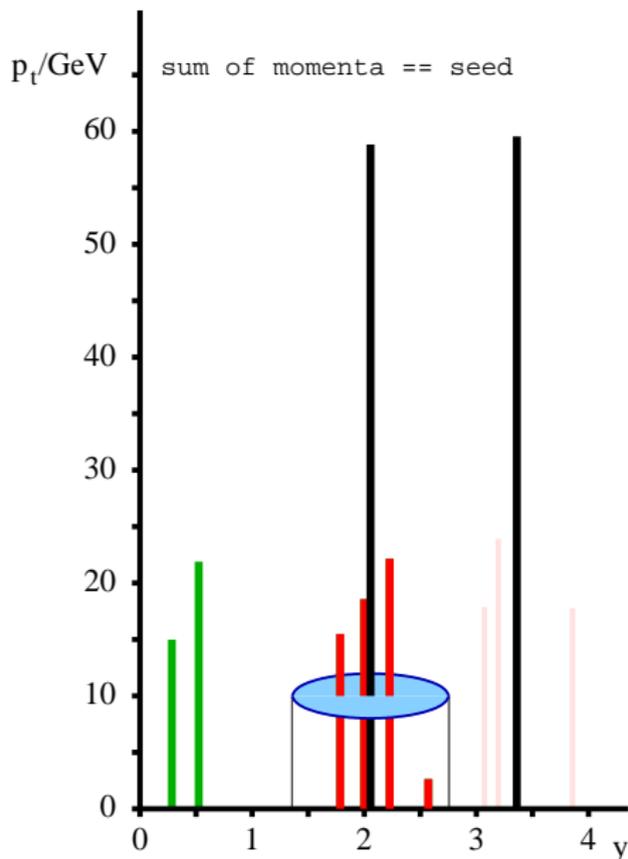


One of the simplest of the cone algs  
e.g. CMS iterative cone

- ▶ Take hardest particle as seed for cone axis
- ▶ Draw cone around seed
- ▶ Sum the momenta use as new seed direction, iterate until stable
- ▶ Convert contents into a “jet” and remove from event

## Notes

- ▶ “Hardest particle” is collinear unsafe  
more right away...



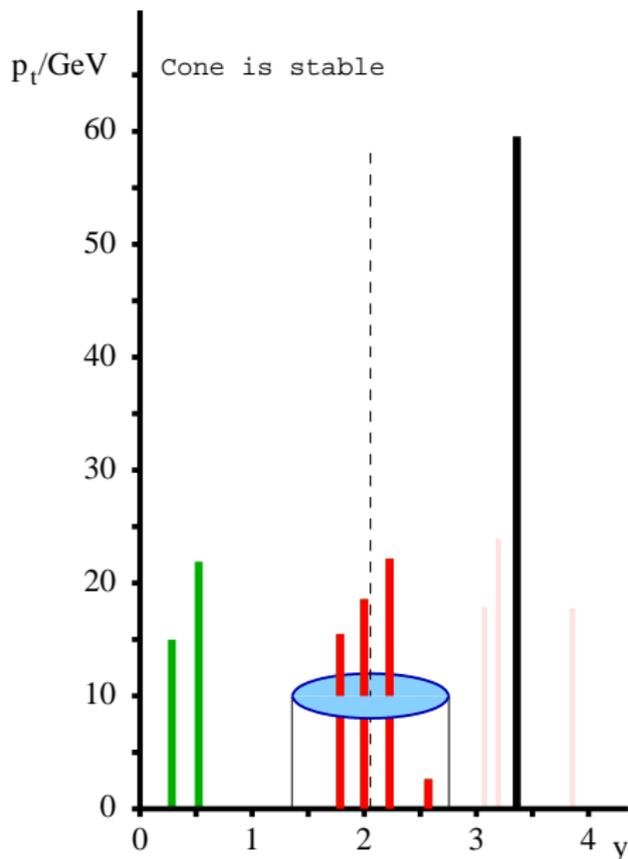
One of the simplest of the cone algs

e.g. CMS iterative cone

- ▶ Take hardest particle as seed for cone axis
- ▶ Draw cone around seed
- ▶ Sum the momenta use as new seed direction, iterate until stable
- ▶ Convert contents into a “jet” and remove from event

Notes

- ▶ “Hardest particle” is collinear unsafe more right away...



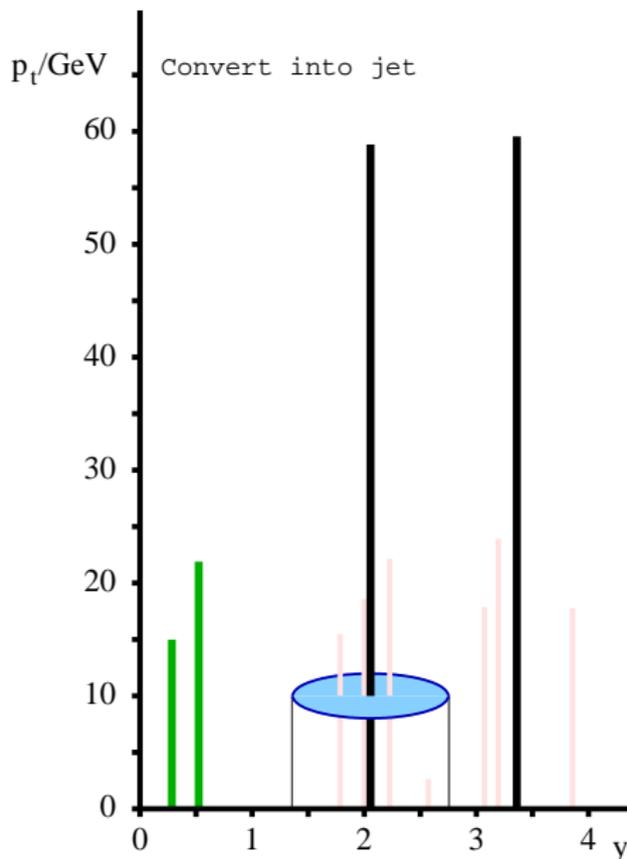
One of the simplest of the cone algs

e.g. CMS iterative cone

- ▶ Take hardest particle as seed for cone axis
- ▶ Draw cone around seed
- ▶ Sum the momenta use as new seed direction, iterate until stable
- ▶ Convert contents into a “jet” and remove from event

Notes

- ▶ “Hardest particle” is collinear unsafe
- ▶ more right away...



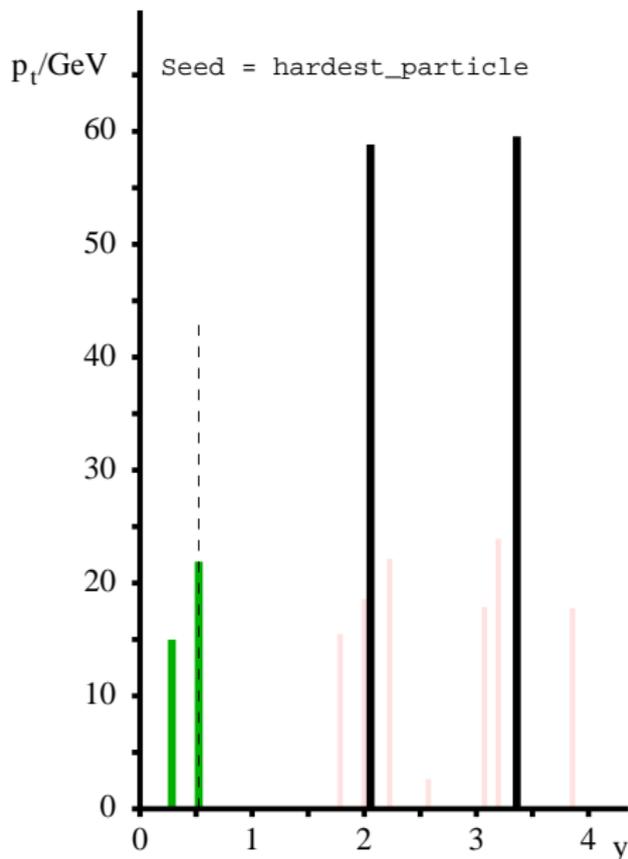
One of the simplest of the cone algs

e.g. CMS iterative cone

- ▶ Take hardest particle as seed for cone axis
- ▶ Draw cone around seed
- ▶ Sum the momenta use as new seed direction, iterate until stable
- ▶ Convert contents into a “jet” and remove from event

Notes

- ▶ “Hardest particle” is collinear unsafe more right away...



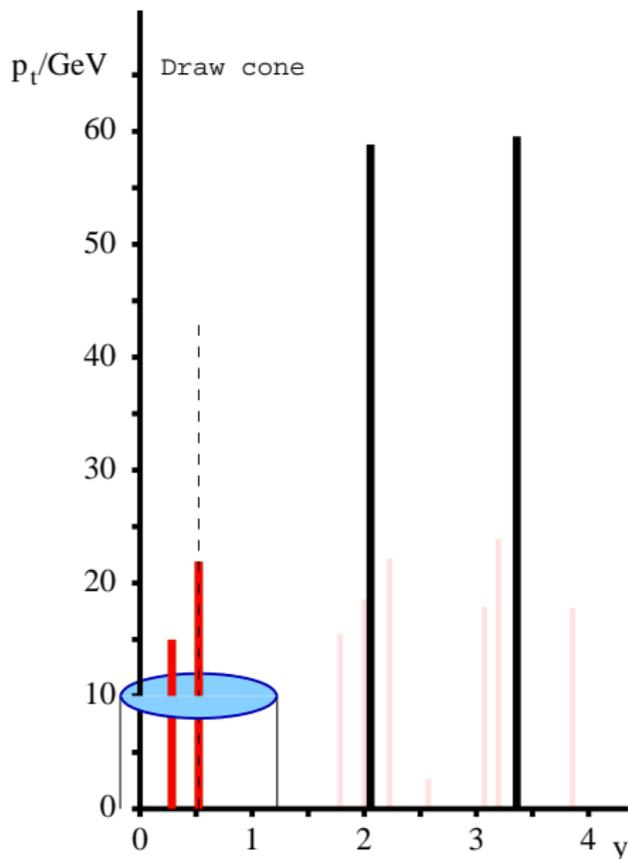
One of the simplest of the cone algs

e.g. CMS iterative cone

- ▶ Take hardest particle as seed for cone axis
- ▶ Draw cone around seed
- ▶ Sum the momenta use as new seed direction, iterate until stable
- ▶ Convert contents into a “jet” and remove from event

Notes

- ▶ “Hardest particle” is collinear unsafe more right away...

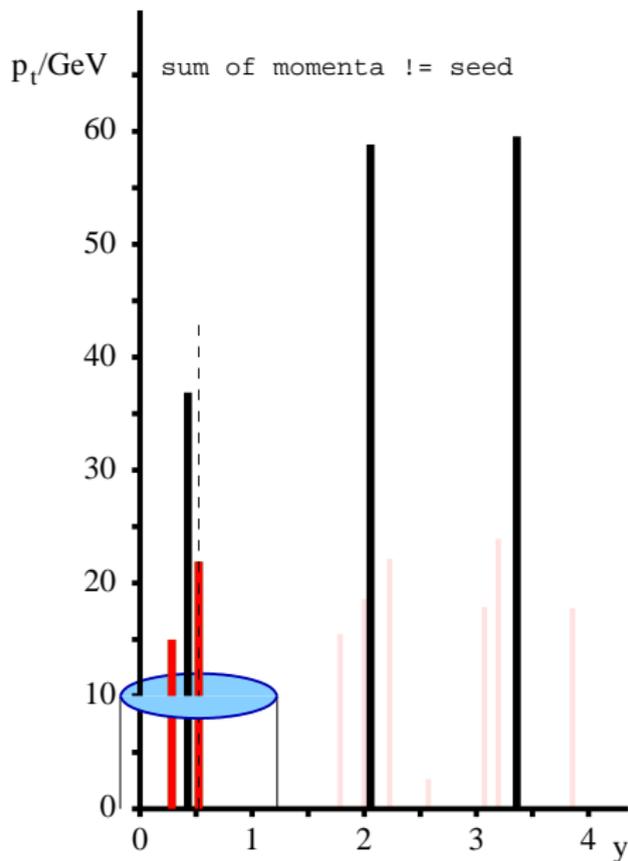


One of the simplest of the cone algs  
e.g. CMS iterative cone

- ▶ Take hardest particle as seed for cone axis
- ▶ Draw cone around seed
- ▶ Sum the momenta use as new seed direction, iterate until stable
- ▶ Convert contents into a “jet” and remove from event

## Notes

- ▶ “Hardest particle” is collinear unsafe
- ▶ more right away...



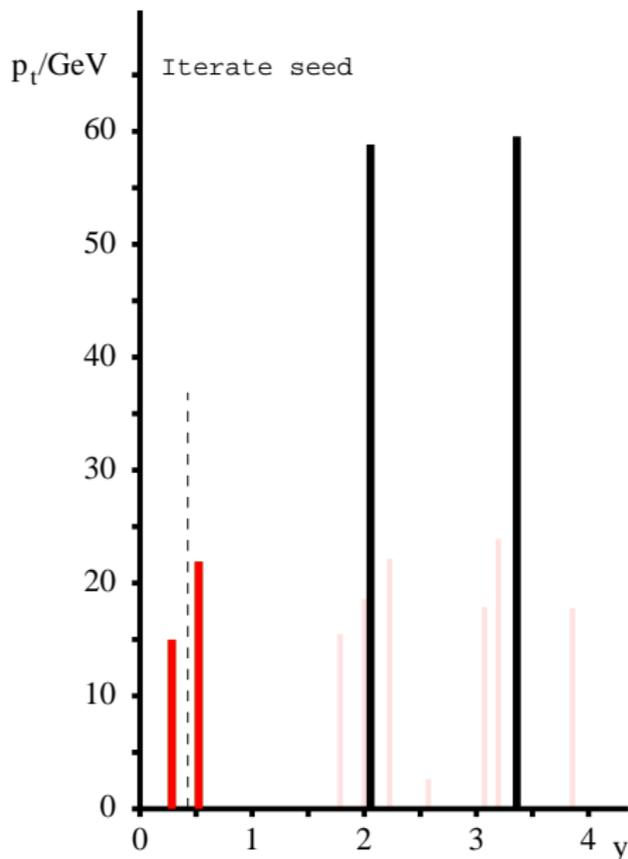
One of the simplest of the cone algs

e.g. CMS iterative cone

- ▶ Take hardest particle as seed for cone axis
- ▶ Draw cone around seed
- ▶ Sum the momenta use as new seed direction, iterate until stable
- ▶ Convert contents into a “jet” and remove from event

Notes

- ▶ “Hardest particle” is collinear unsafe more right away...

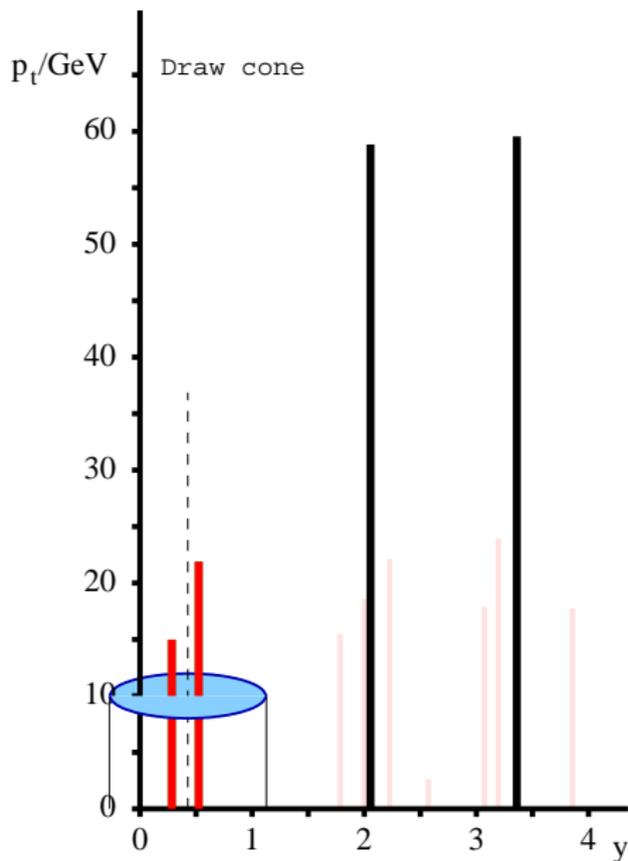


One of the simplest of the cone algs  
e.g. CMS iterative cone

- ▶ Take hardest particle as seed for cone axis
- ▶ Draw cone around seed
- ▶ Sum the momenta use as new seed direction, iterate until stable
- ▶ Convert contents into a “jet” and remove from event

## Notes

- ▶ “Hardest particle” is collinear unsafe more right away...



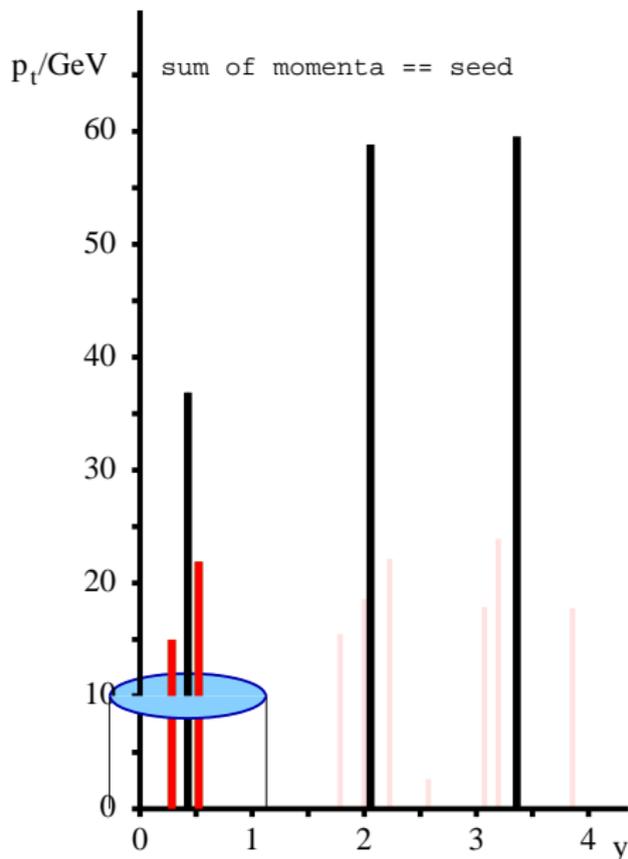
One of the simplest of the cone algs

e.g. CMS iterative cone

- ▶ Take hardest particle as seed for cone axis
- ▶ Draw cone around seed
- ▶ Sum the momenta use as new seed direction, iterate until stable
- ▶ Convert contents into a “jet” and remove from event

Notes

- ▶ “Hardest particle” is collinear unsafe more right away...



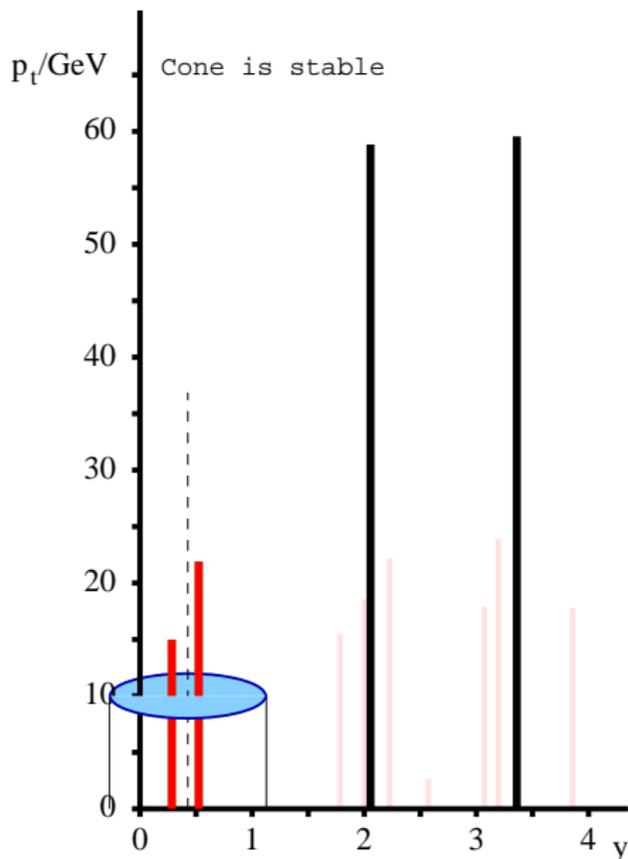
One of the simplest of the cone algs

e.g. CMS iterative cone

- ▶ Take hardest particle as seed for cone axis
- ▶ Draw cone around seed
- ▶ Sum the momenta use as new seed direction, iterate until stable
- ▶ Convert contents into a “jet” and remove from event

Notes

- ▶ “Hardest particle” is collinear unsafe more right away...



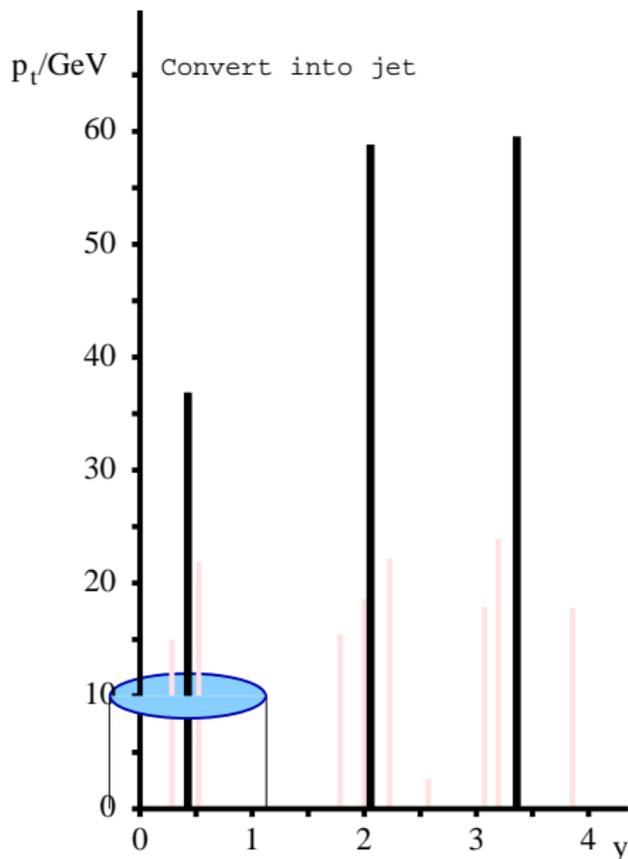
One of the simplest of the cone algs

e.g. CMS iterative cone

- ▶ Take hardest particle as seed for cone axis
- ▶ Draw cone around seed
- ▶ Sum the momenta use as new seed direction, iterate until stable
- ▶ Convert contents into a “jet” and remove from event

Notes

- ▶ “Hardest particle” is collinear unsafe more right away...

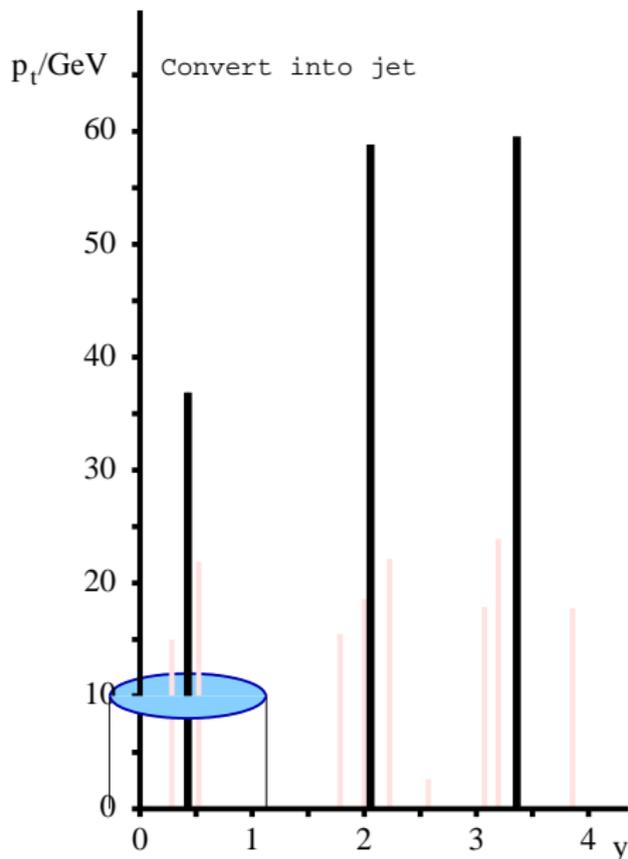


One of the simplest of the cone algs  
e.g. CMS iterative cone

- ▶ Take hardest particle as seed for cone axis
- ▶ Draw cone around seed
- ▶ Sum the momenta use as new seed direction, iterate until stable
- ▶ Convert contents into a “jet” and remove from event

## Notes

- ▶ “Hardest particle” is collinear unsafe more right away...



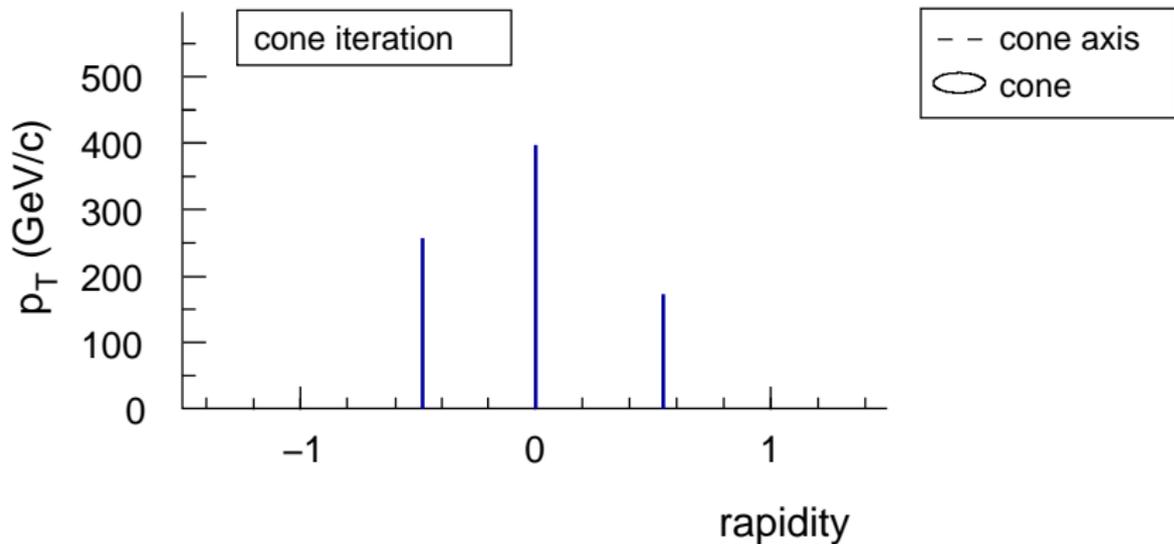
One of the simplest of the cone algs

e.g. CMS iterative cone

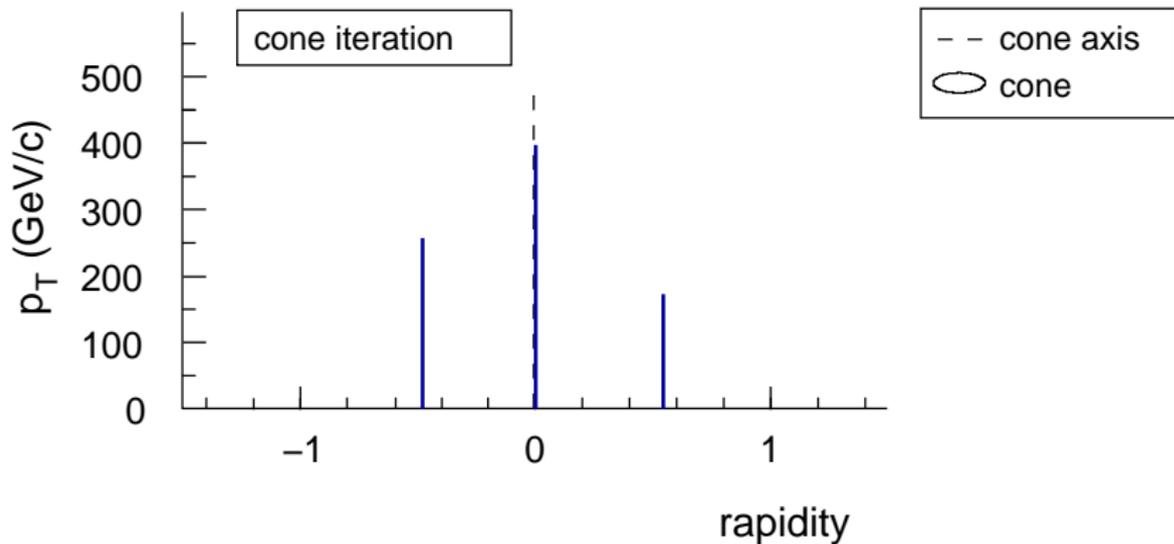
- ▶ Take hardest particle as seed for cone axis
- ▶ Draw cone around seed
- ▶ Sum the momenta use as new seed direction, iterate until stable
- ▶ Convert contents into a “jet” and remove from event

Notes

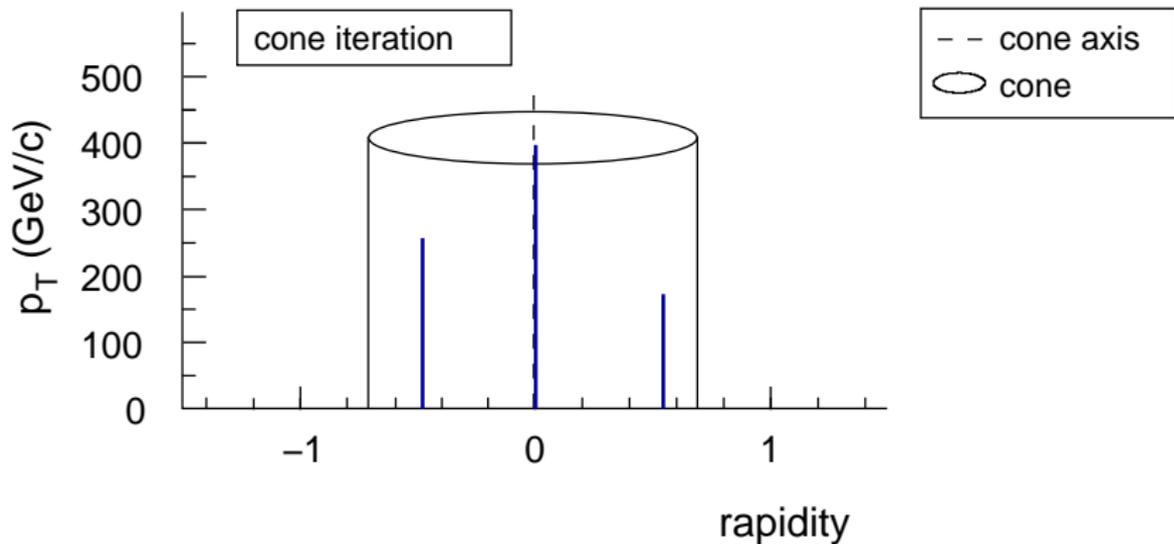
- ▶ “Hardest particle” is collinear unsafe more right away...



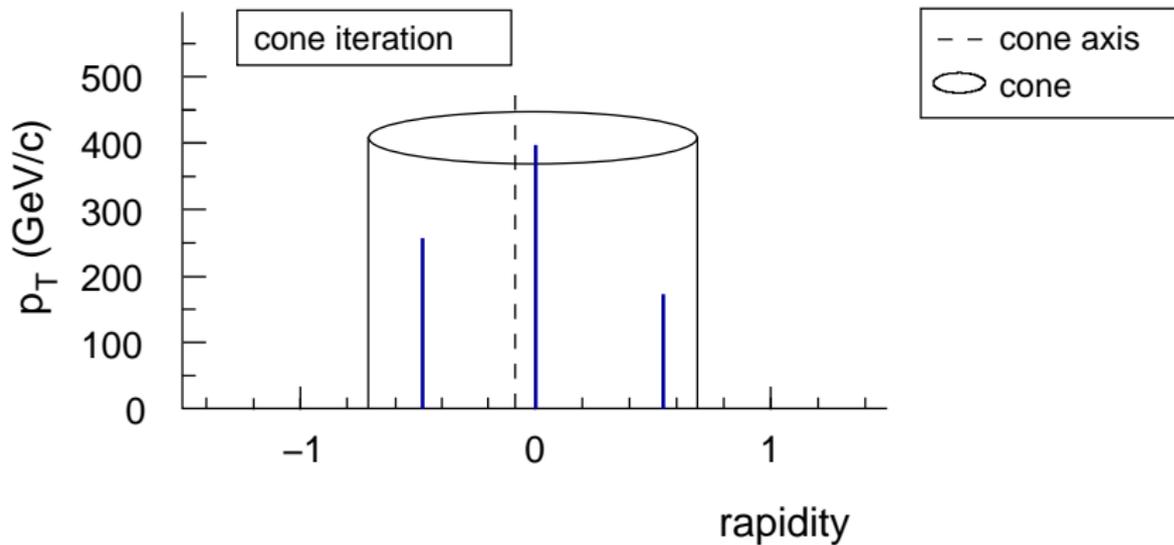
Collinear splitting can modify the hard jets: ICPR algorithms are collinear unsafe  $\implies$  perturbative calculations give  $\infty$



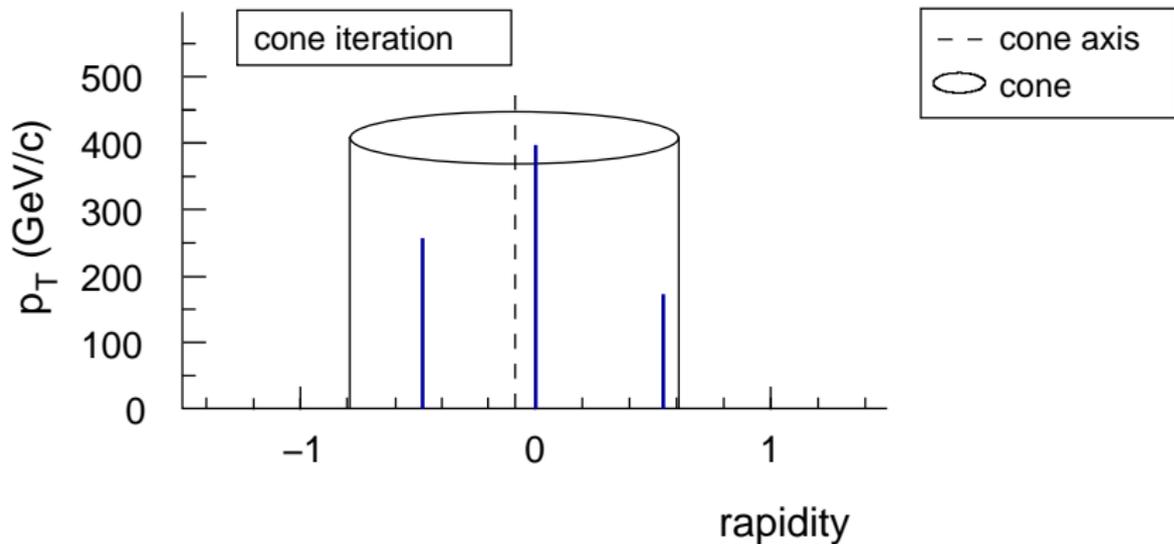
Collinear splitting can modify the hard jets: ICPR algorithms are collinear unsafe  $\implies$  perturbative calculations give  $\infty$



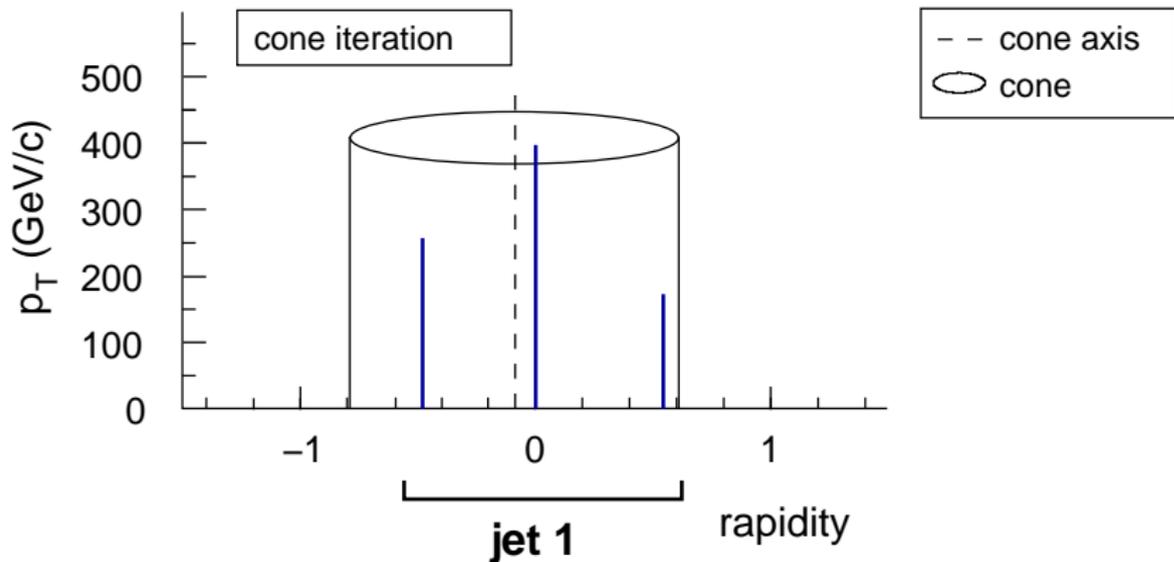
Collinear splitting can modify the hard jets: ICPR algorithms are collinear unsafe  $\implies$  perturbative calculations give  $\infty$



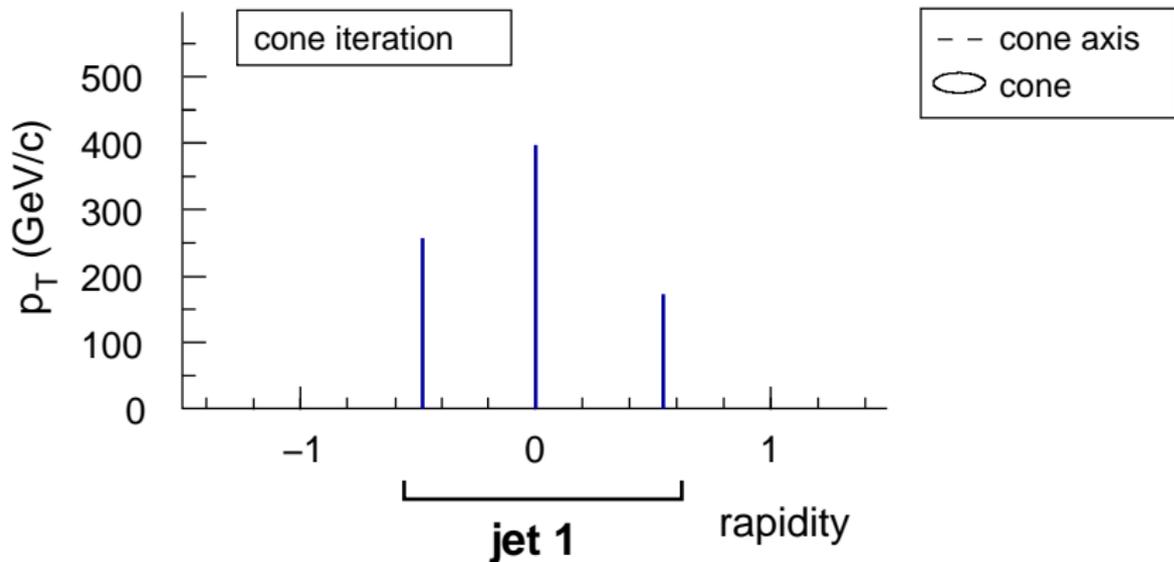
Collinear splitting can modify the hard jets: ICPR algorithms are collinear unsafe  $\Rightarrow$  perturbative calculations give  $\infty$



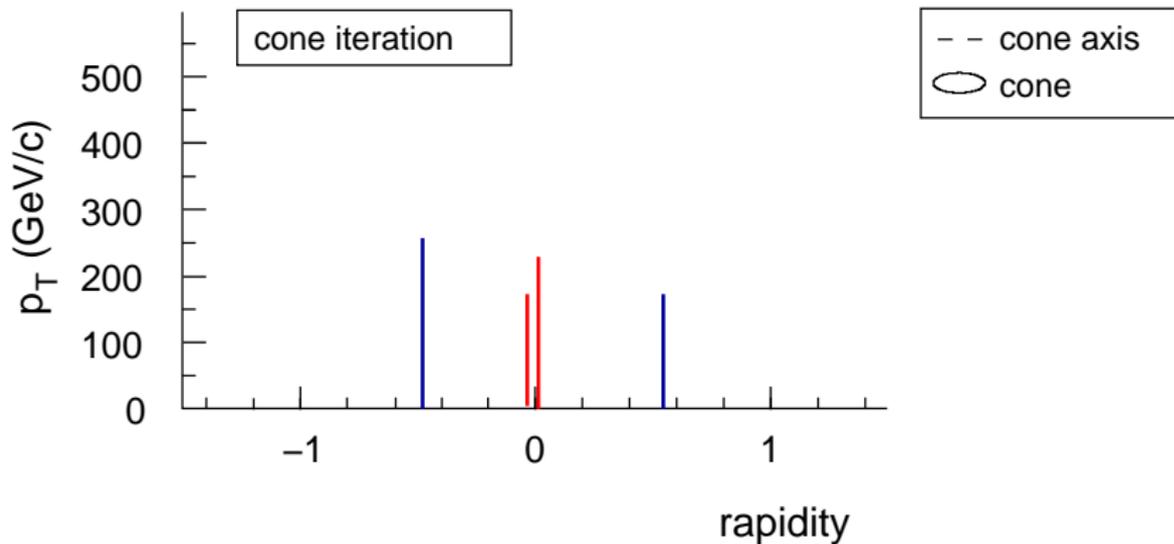
Collinear splitting can modify the hard jets: ICPR algorithms are collinear unsafe  $\Rightarrow$  perturbative calculations give  $\infty$



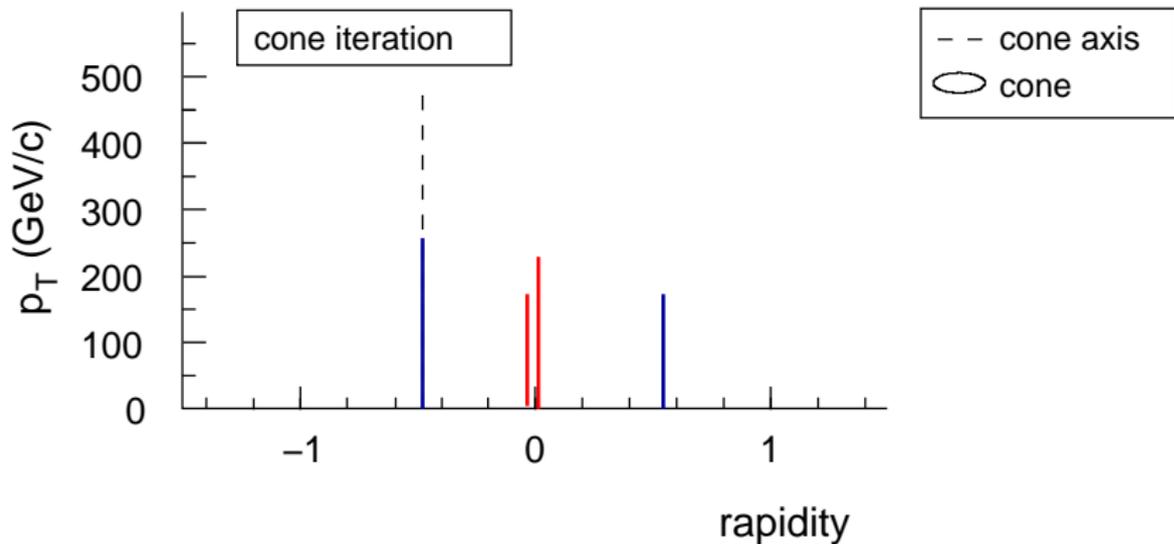
Collinear splitting can modify the hard jets: ICPR algorithms are collinear unsafe  $\implies$  perturbative calculations give  $\infty$



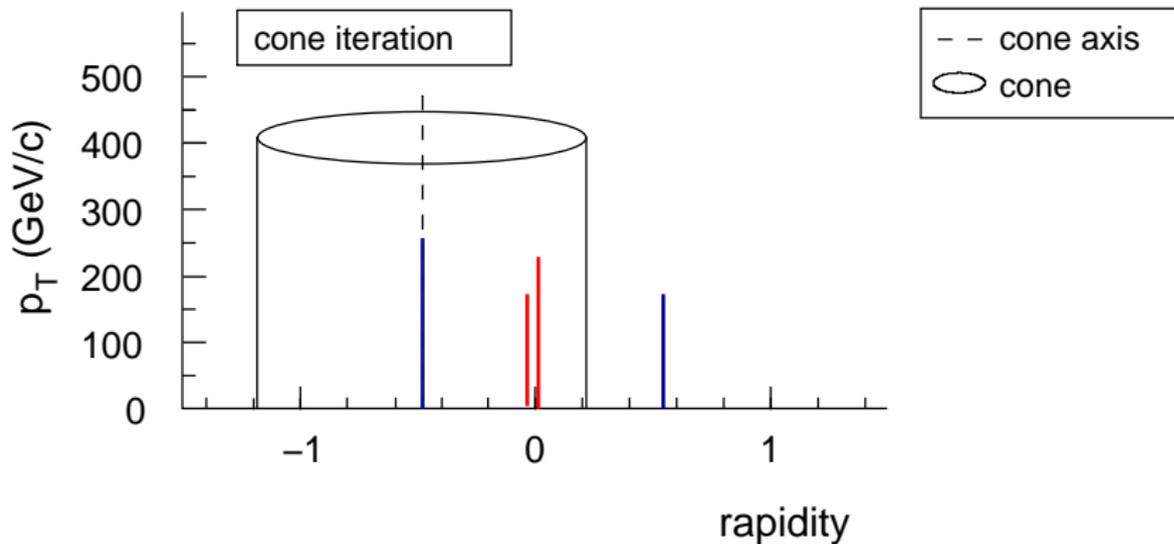
Collinear splitting can modify the hard jets: ICPR algorithms are collinear unsafe  $\Rightarrow$  perturbative calculations give  $\infty$



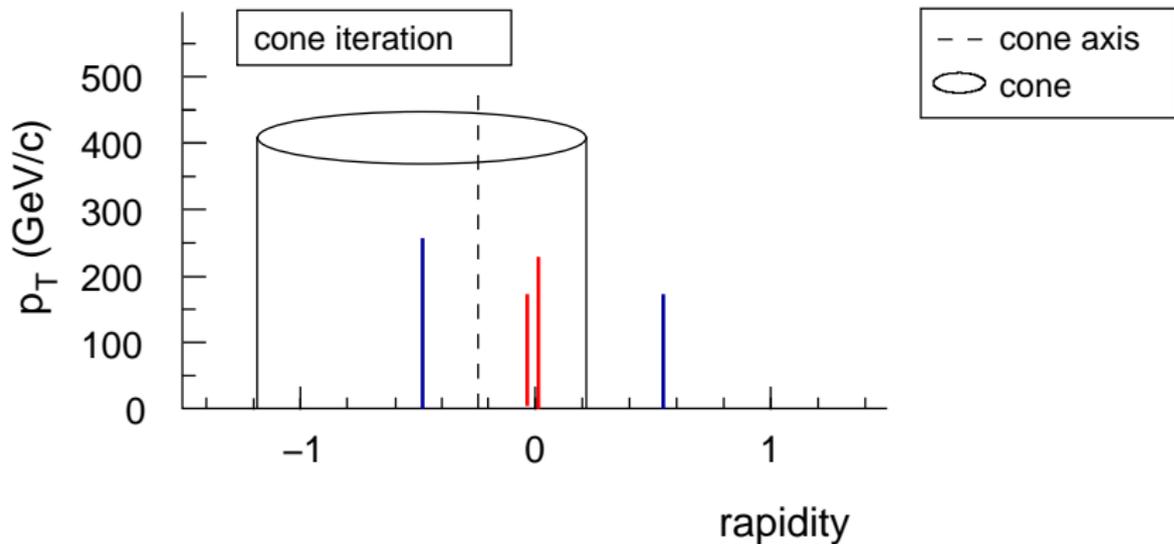
Collinear splitting can modify the hard jets: ICPR algorithms are collinear unsafe  $\implies$  perturbative calculations give  $\infty$



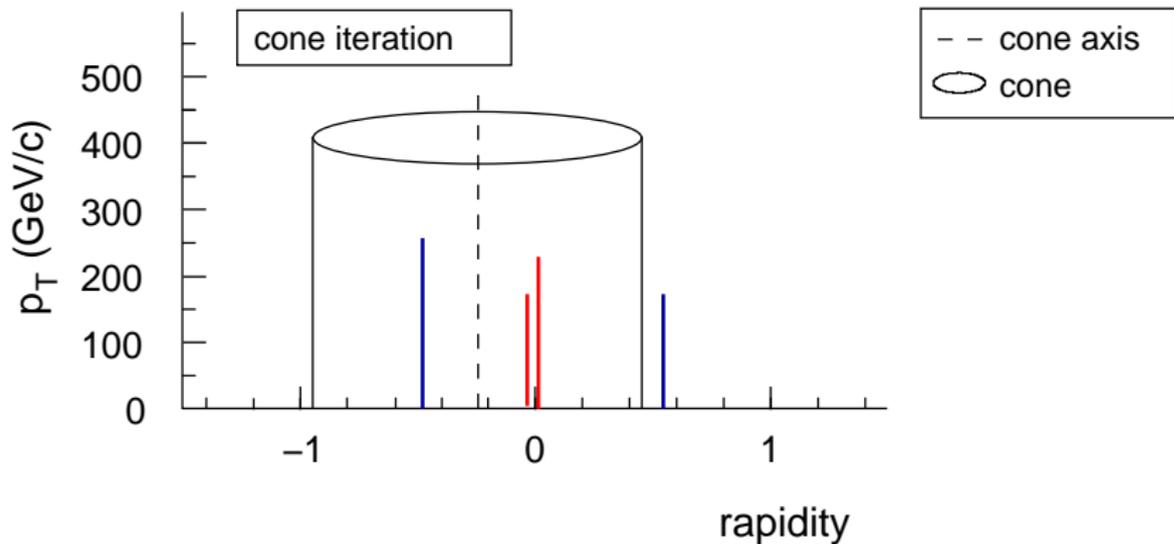
Collinear splitting can modify the hard jets: ICPR algorithms are collinear unsafe  $\implies$  perturbative calculations give  $\infty$



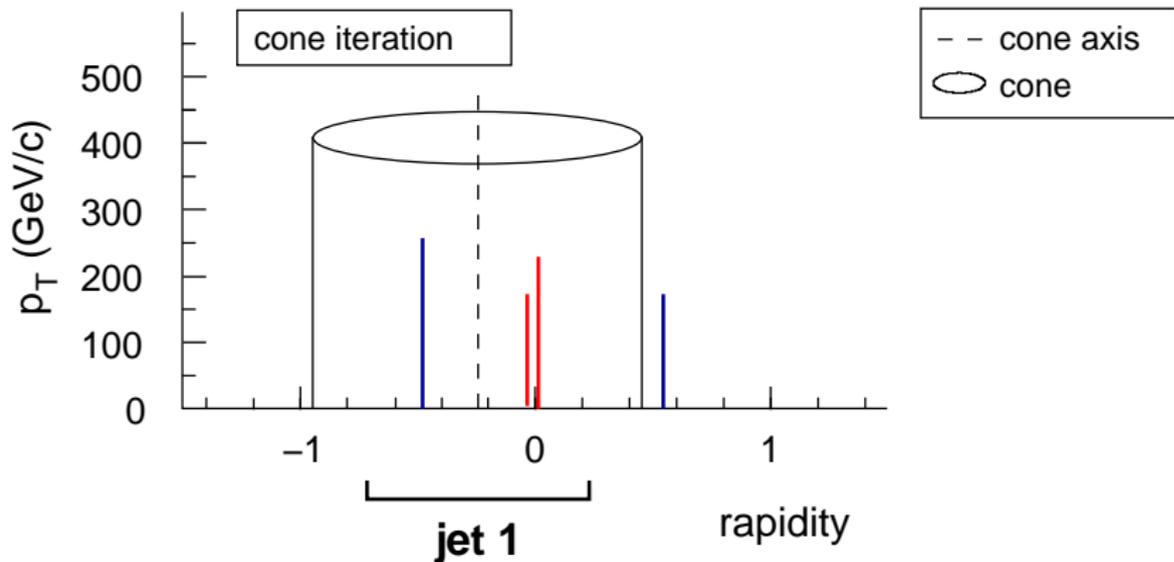
Collinear splitting can modify the hard jets: ICPR algorithms are collinear unsafe  $\implies$  perturbative calculations give  $\infty$



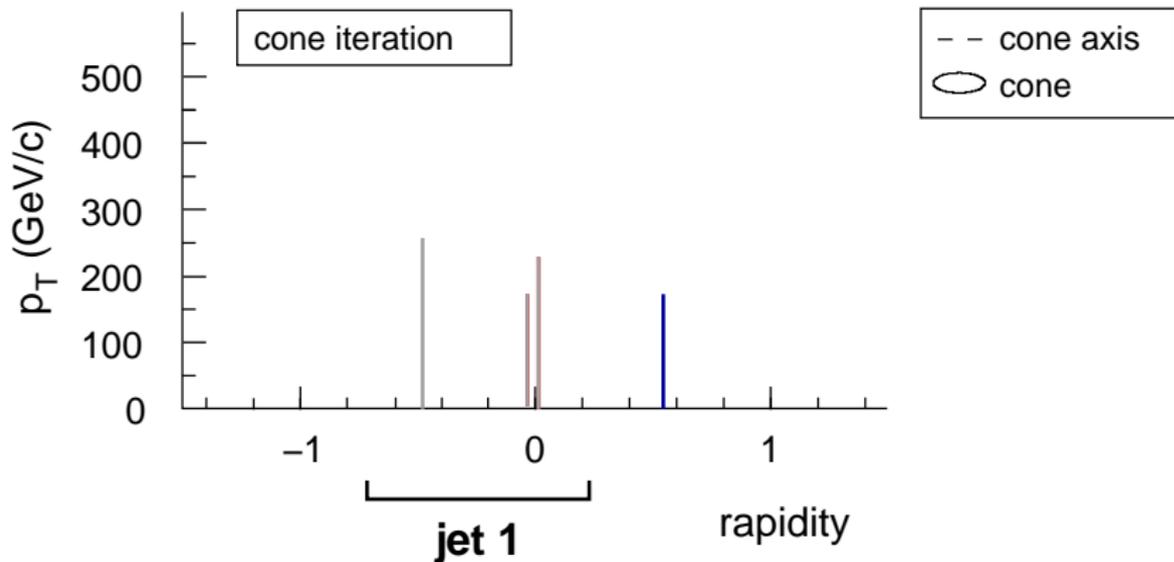
Collinear splitting can modify the hard jets: ICPR algorithms are collinear unsafe  $\implies$  perturbative calculations give  $\infty$



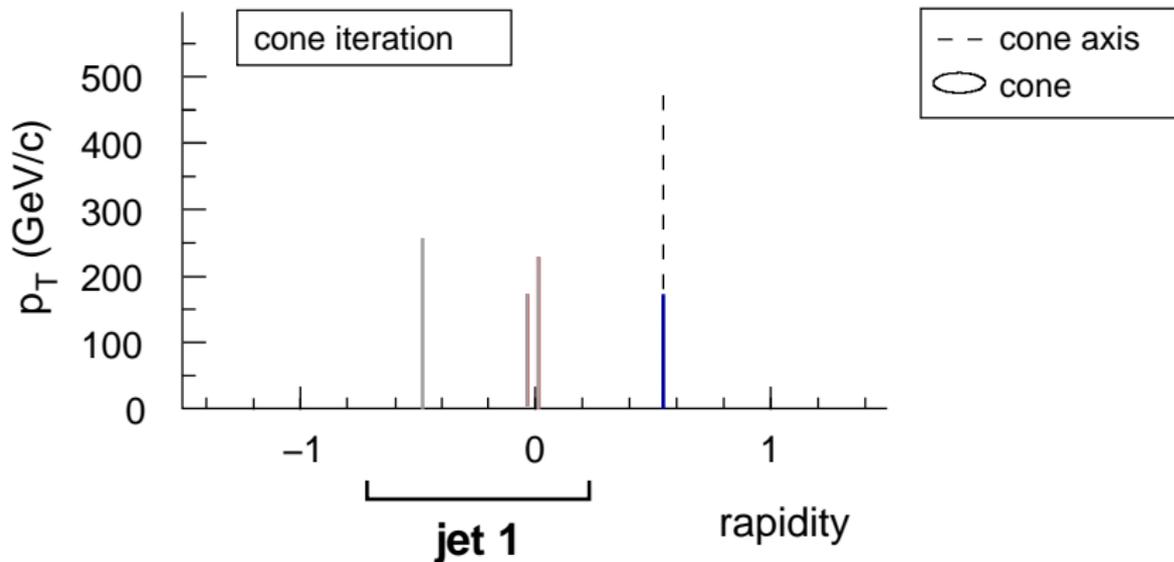
Collinear splitting can modify the hard jets: ICPR algorithms are collinear unsafe  $\implies$  perturbative calculations give  $\infty$



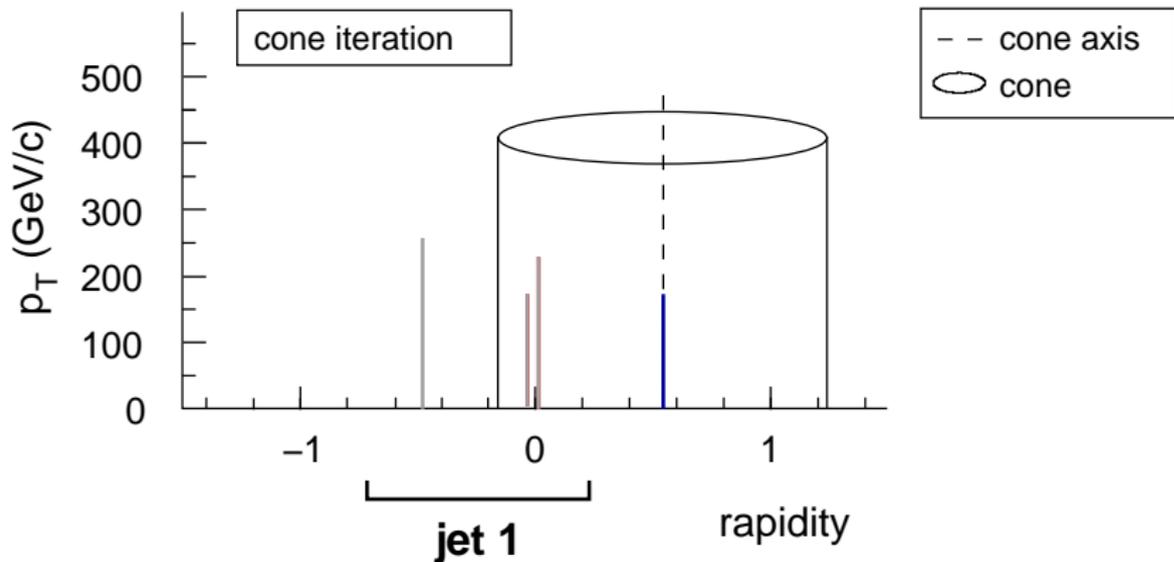
Collinear splitting can modify the hard jets: ICPR algorithms are collinear unsafe  $\Rightarrow$  perturbative calculations give  $\infty$



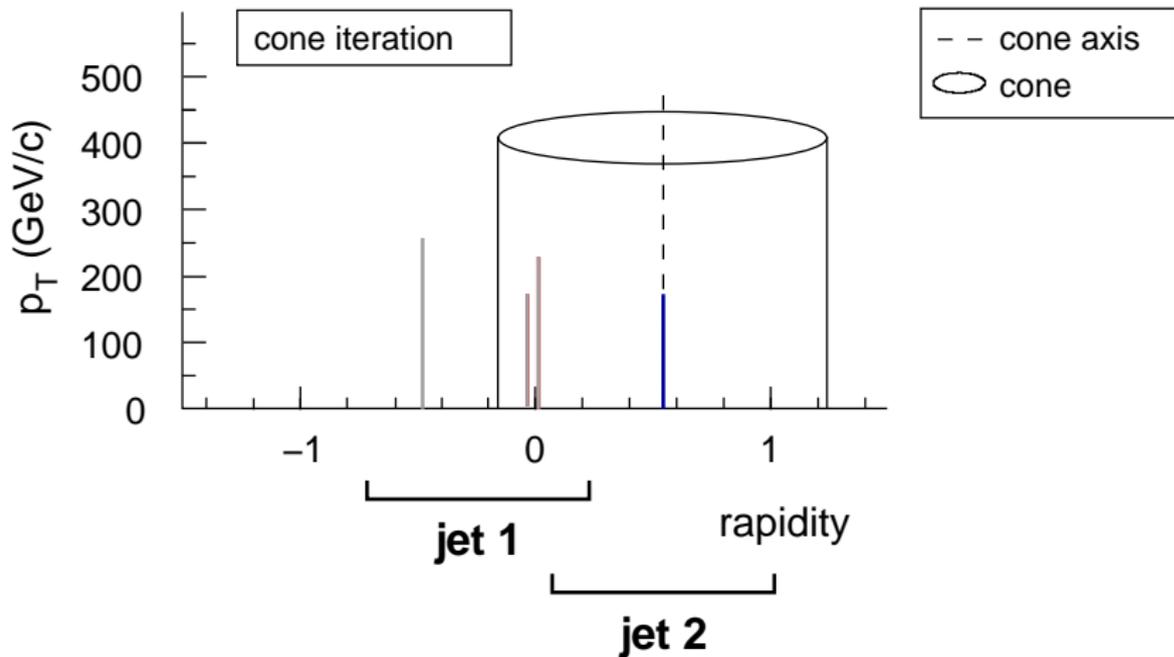
Collinear splitting can modify the hard jets: ICPR algorithms are collinear unsafe  $\Rightarrow$  perturbative calculations give  $\infty$



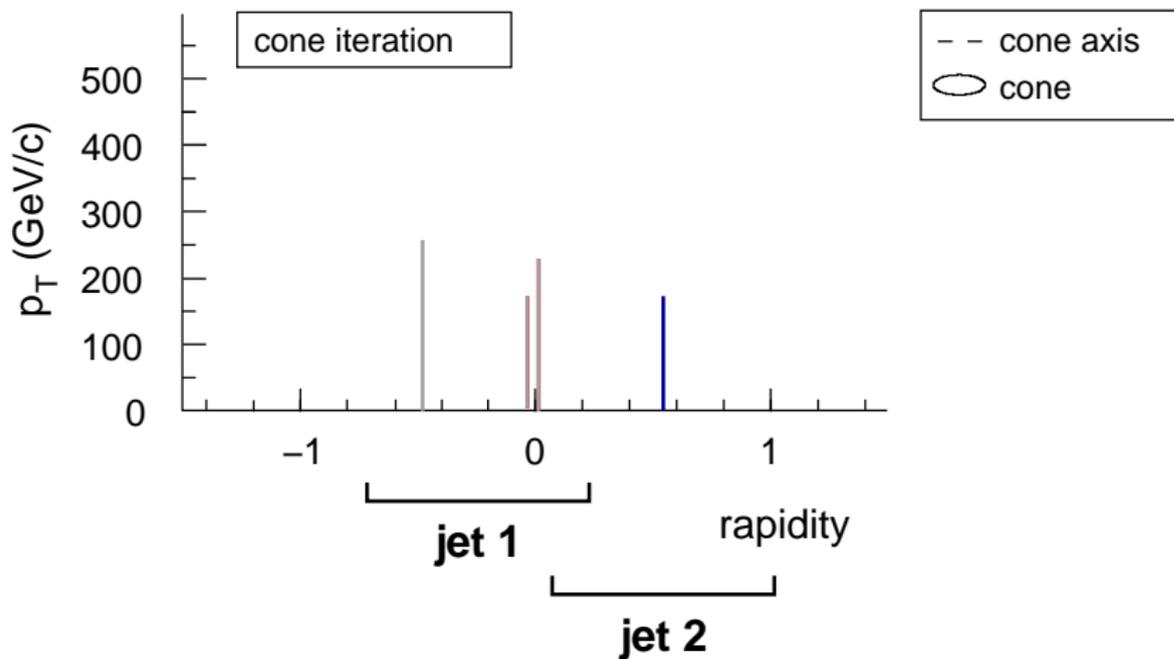
Collinear splitting can modify the hard jets: ICPR algorithms are collinear unsafe  $\implies$  perturbative calculations give  $\infty$



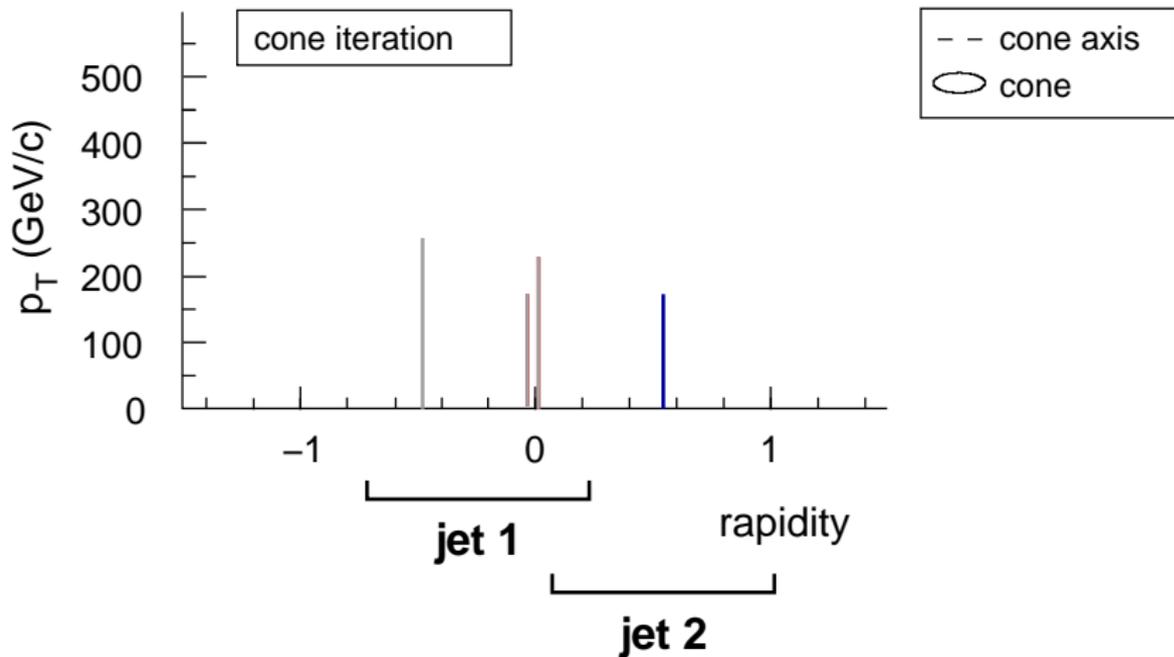
Collinear splitting can modify the hard jets: ICPR algorithms are collinear unsafe  $\implies$  perturbative calculations give  $\infty$



Collinear splitting can modify the hard jets: ICPR algorithms are collinear unsafe  $\implies$  perturbative calculations give  $\infty$

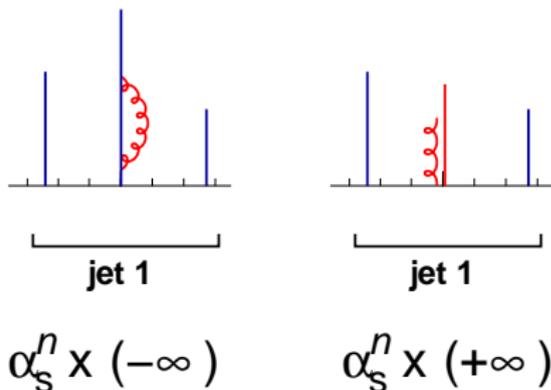


Collinear splitting can modify the hard jets: ICPR algorithms are collinear unsafe  $\implies$  perturbative calculations give  $\infty$



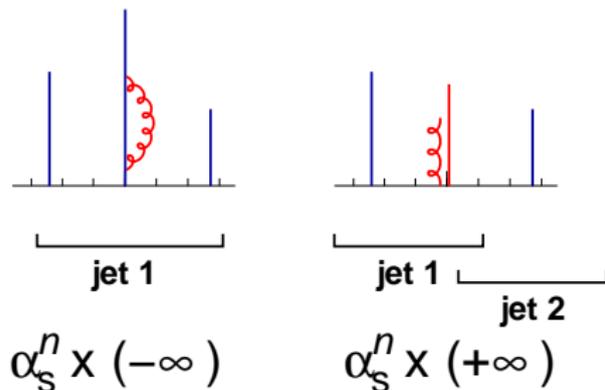
**Collinear splitting can modify the hard jets: ICPR algorithms are collinear unsafe**  $\implies$  perturbative calculations give  $\infty$

## Collinear Safe



**Infinites cancel**

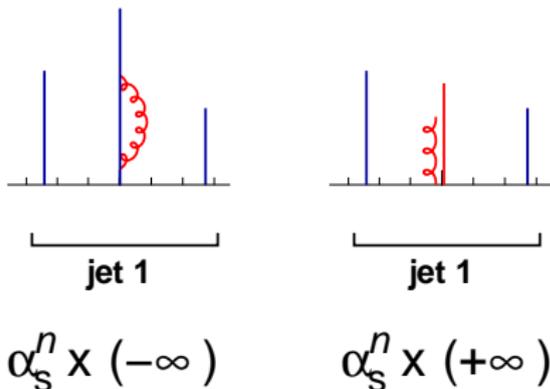
## Collinear Unsafe



**Infinites do not cancel**

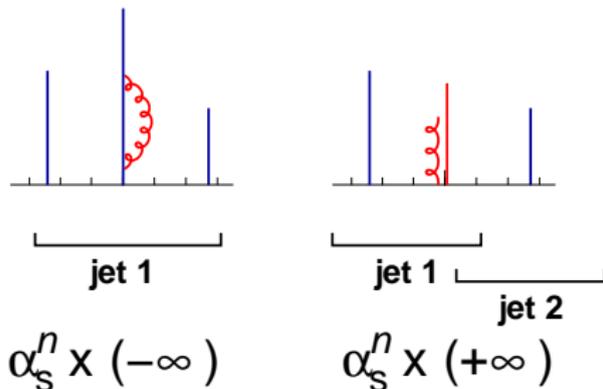
Invalidates perturbation theory

## Collinear Safe



**Infinites cancel**

## Collinear Unsafe



**Infinites do not cancel**

**Invalidates perturbation theory**

Real life does not have infinities, but pert. infinity leaves a real-life trace

$$\alpha_s^2 + \alpha_s^3 + \alpha_s^4 \times \infty \rightarrow \alpha_s^2 + \alpha_s^3 + \alpha_s^4 \times \ln p_t/\Lambda \rightarrow \alpha_s^2 + \underbrace{\alpha_s^3 + \alpha_s^3}_{\text{BOTH WASTED}}$$

Among consequences of IR unsafety:

	<i>Last meaningful order</i>			Known at
	JetClu, ATLAS cone [IC-SM]	MidPoint [IC <sub>mp</sub> -SM]	CMS it. cone [IC-PR]	
Inclusive jets	LO	NLO	NLO	NLO (→ NNLO)
W/Z + 1 jet	LO	NLO	NLO	NLO
3 jets	<b>none</b>	LO	LO	NLO [nlojet++]
W/Z + 2 jets	<b>none</b>	LO	LO	NLO [MCFM]
$m_{\text{jet}}$ in $2j + X$	<b>none</b>	<b>none</b>	<b>none</b>	NLO [Blackhat/Rocket/...]

NB: 50,000,000\$/£/CHF/€ investment in NLO

Multi-jet contexts much more sensitive: **ubiquitous at LHC**

And LHC will rely on QCD for background double-checks  
 extraction of cross sections, extraction of parameters

Real life does not have infinities, but pert. infinity leaves a real-life trace

$$\alpha_s^2 + \alpha_s^3 + \alpha_s^4 \times \infty \rightarrow \alpha_s^2 + \alpha_s^3 + \alpha_s^4 \times \ln p_t/\Lambda \rightarrow \alpha_s^2 + \underbrace{\alpha_s^3 + \alpha_s^3}_{\text{BOTH WASTED}}$$

Among consequences of IR unsafety:

	<i>Last meaningful order</i>			Known at
	JetClu, ATLAS cone [IC-SM]	MidPoint [IC <sub>mp</sub> -SM]	CMS it. cone [IC-PR]	
Inclusive jets	LO	NLO	NLO	NLO (→ NNLO)
W/Z + 1 jet	LO	NLO	NLO	NLO
3 jets	<b>none</b>	LO	LO	NLO [nlojet++]
W/Z + 2 jets	<b>none</b>	LO	LO	NLO [MCFM]
m <sub>jet</sub> in 2j + X	<b>none</b>	<b>none</b>	<b>none</b>	NLO [Blackhat/Rocket/...]

NB: 50,000,000\$/£/CHF/€ investment in NLO

Multi-jet contexts much more sensitive: **ubiquitous at LHC**

And LHC will rely on QCD for background double-checks  
 extraction of cross sections, extraction of parameters

Real life does not have infinities, but pert. infinity leaves a real-life trace

$$\alpha_s^2 + \alpha_s^3 + \alpha_s^4 \times \infty \rightarrow \alpha_s^2 + \alpha_s^3 + \alpha_s^4 \times \ln p_t/\Lambda \rightarrow \alpha_s^2 + \underbrace{\alpha_s^3 + \alpha_s^3}_{\text{BOTH WASTED}}$$

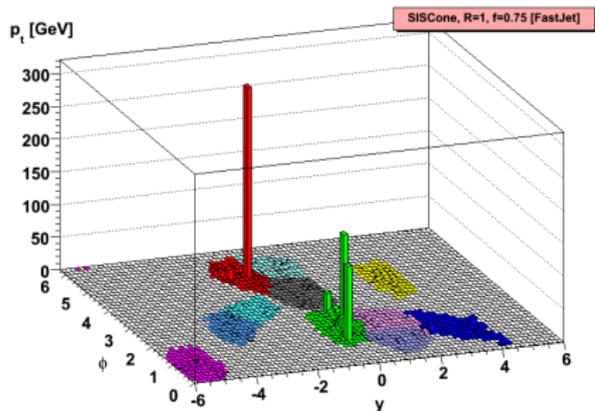
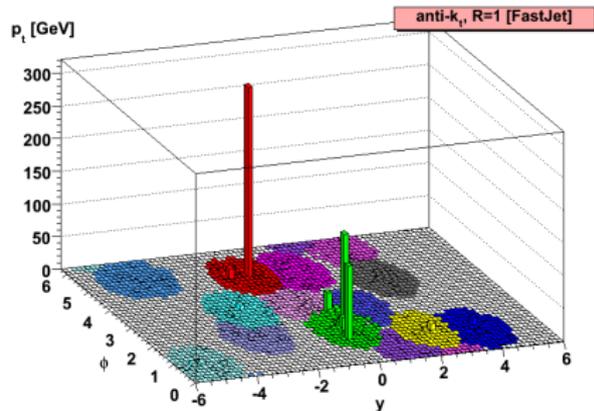
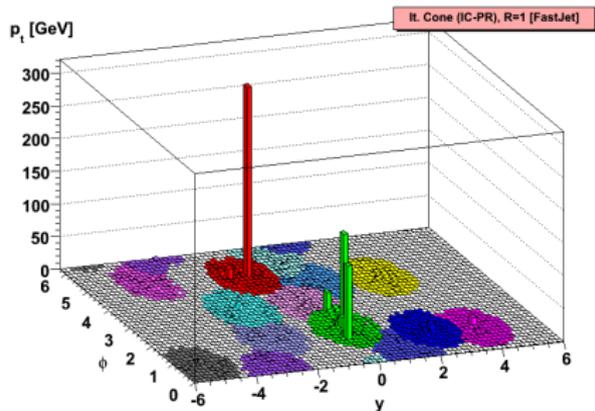
Among consequences of IR unsafety:

	<i>Last meaningful order</i>			Known at
	JetClu, ATLAS cone [IC-SM]	MidPoint [IC <sub>mp</sub> -SM]	CMS it. cone [IC-PR]	
Inclusive jets	LO	NLO	NLO	NLO (→ NNLO)
W/Z + 1 jet	LO	NLO	NLO	NLO
3 jets	<b>none</b>	LO	LO	NLO [nlojet++]
W/Z + 2 jets	<b>none</b>	LO	LO	NLO [MCFM]
m <sub>jet</sub> in 2j + X	<b>none</b>	<b>none</b>	<b>none</b>	NLO [Blackhat/Rocket/...]

NB: 50,000,000\$/£/CHF/€ investment in NLO

Multi-jet contexts much more sensitive: **ubiquitous at LHC**

And LHC will rely on QCD for background double-checks  
 extraction of cross sections, extraction of parameters



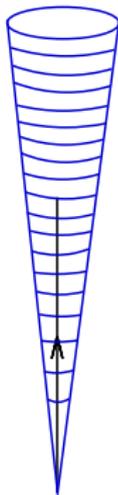
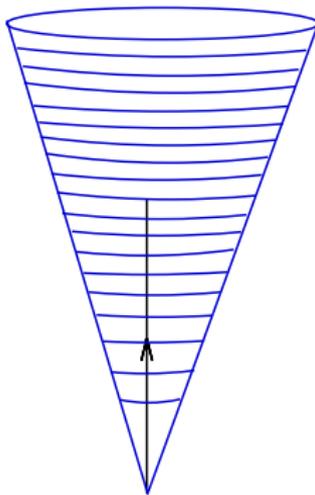
ICPR type cone can straightforwardly be replaced by anti- $k_t$ .

Another class of cones — those with split-merge steps (Tevatron, old ATLAS cone), can be replaced with the *Seedless Infrared Safe Cone (SISCone)*.

# Towards an understanding of jets

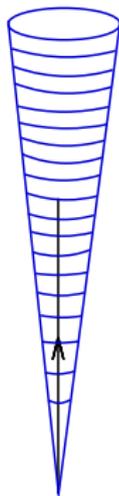
How a jet is and isn't like a parton —  
quantitatively

And how this relationship is affected by the jet  
radius

**Small jet radius****Large jet radius**

single parton @ LO: **jet radius irrelevant**

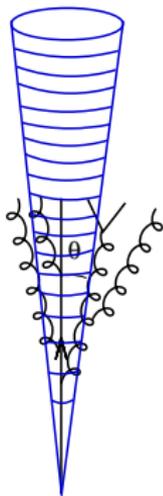
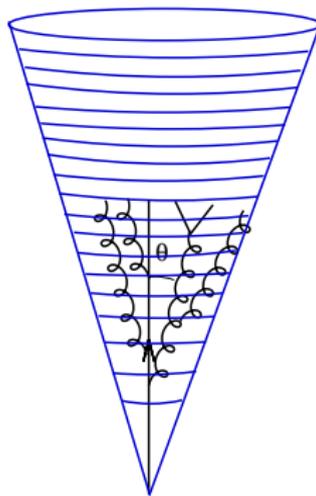
## Small jet radius



single part

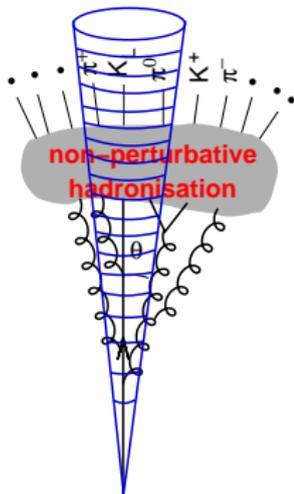
## Large jet radius



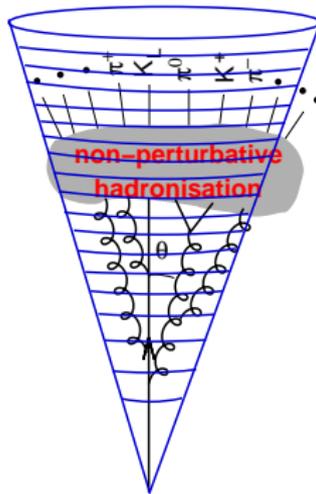
**Small jet radius****Large jet radius**

perturbative fragmentation: **large jet radius better**  
(it captures more)

## Small jet radius

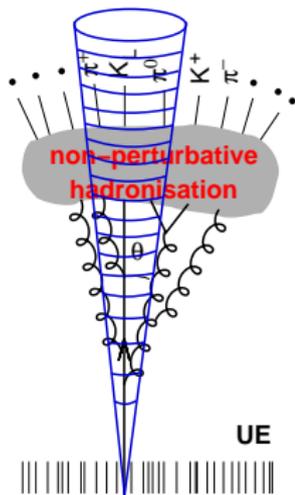


## Large jet radius

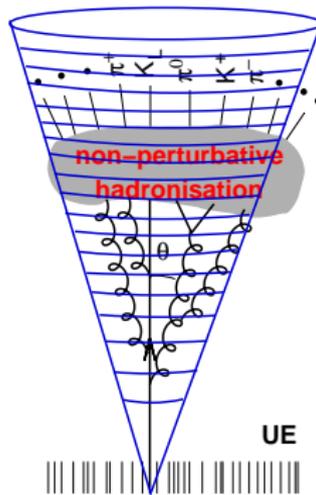


non-perturbative fragmentation: **large jet radius better**  
(it captures more)

## Small jet radius

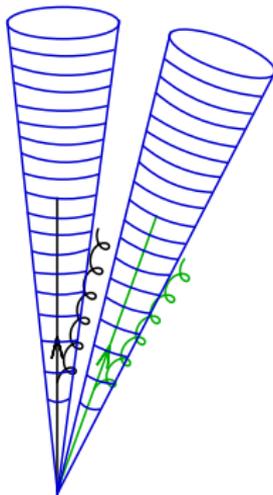


## Large jet radius

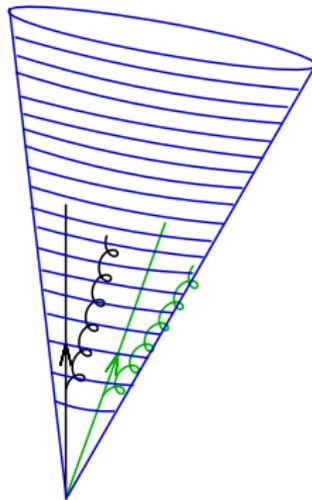


underlying ev. & pileup "noise": **small jet radius better**  
(it captures less)

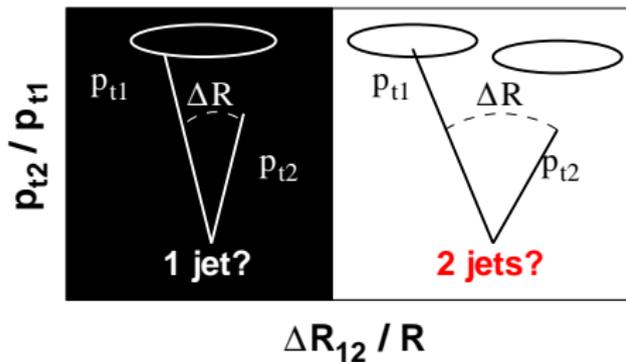
## Small jet radius



## Large jet radius



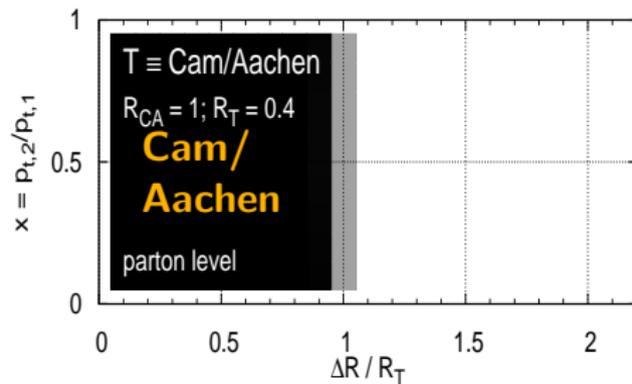
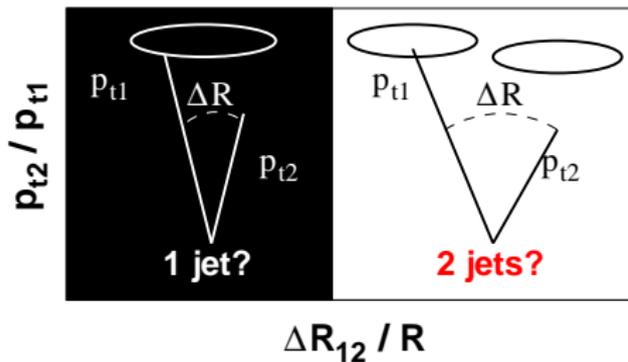
multi-hard-parton events: **small jet radius better**  
(it resolves partons more effectively)



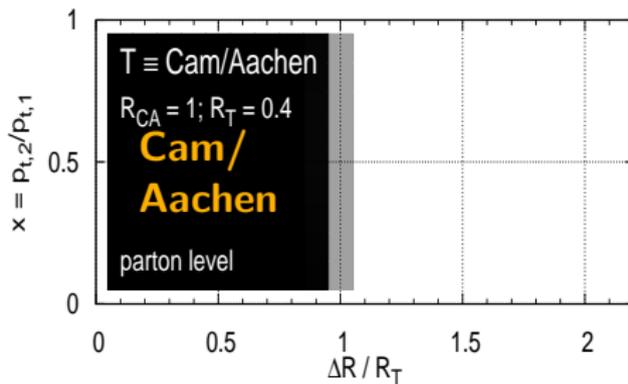
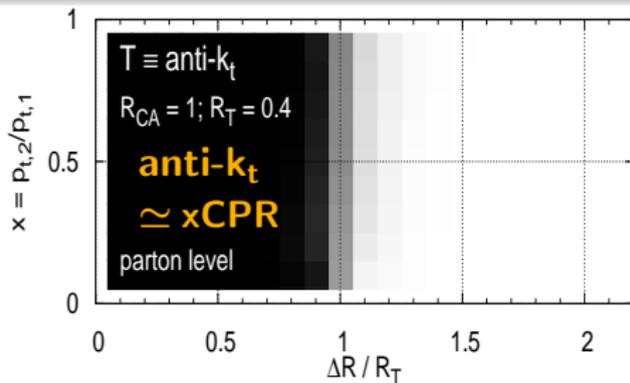
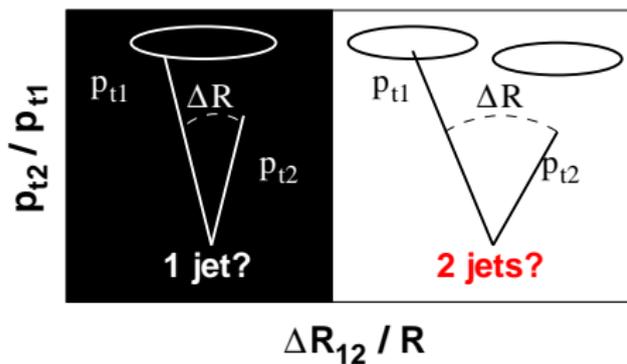
$$\Delta R_{12} / R$$

Most algs reach as far as  $R$  for radiation

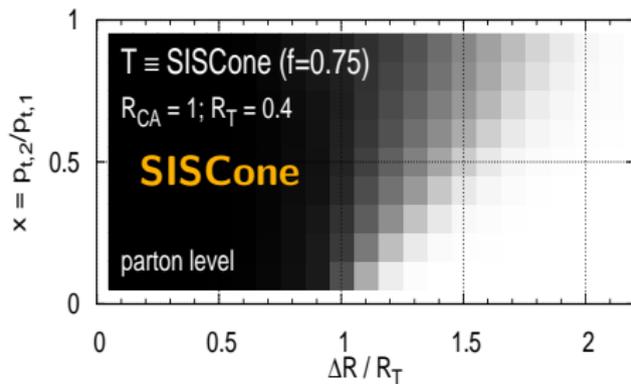
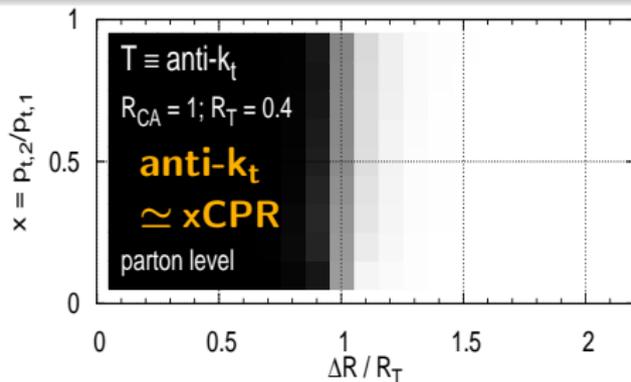
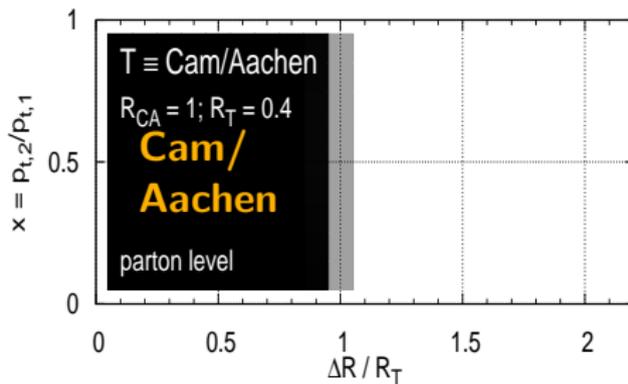
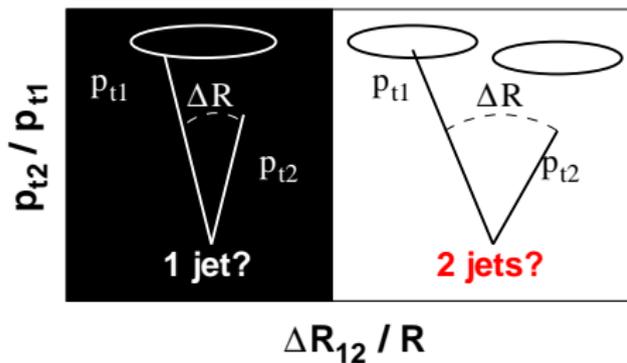
SISCone (xC-5M) reaches further for hard radiation



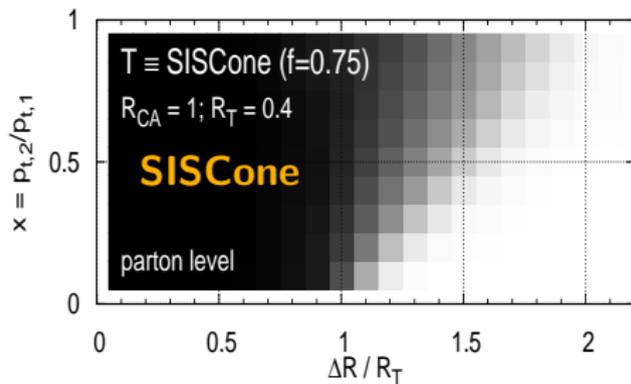
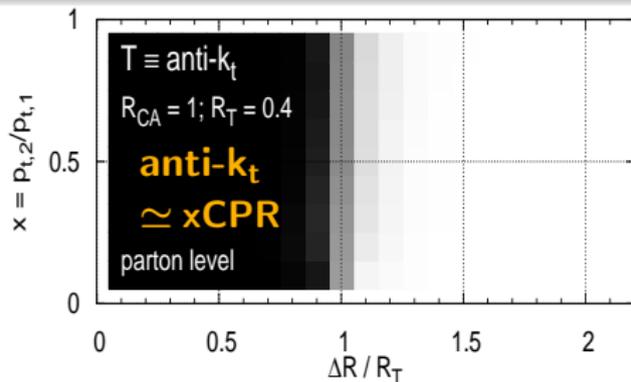
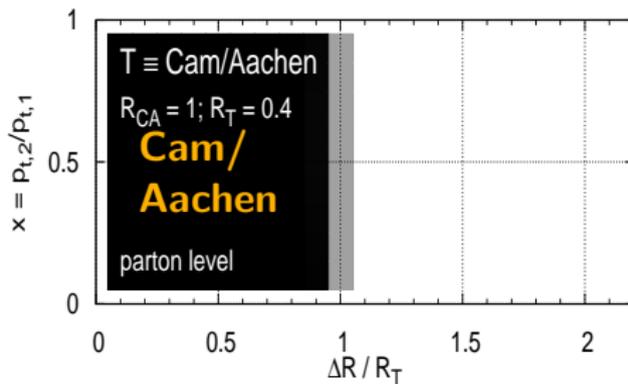
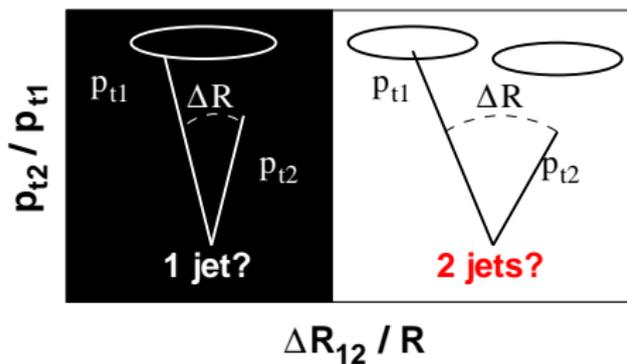
Most algs reach as far as  $R$  for radiation  
 SISCone (xC-SM) reaches further for hard radiation



Most algs reach as far as  $R$  for radiation  
 SIScone (xC-SM) reaches further for hard radiation



Most algs reach as far as  $R$  for radiation  
 SIScone (xC-SM) reaches further for hard radiation



**Most algs reach as far as  $R$  for radiation**  
 SIScone (xC-SM) reaches further for hard radiation

## Parton $p_t$ v. jet $p_t$

### 3 physical effects:

1. Gluon radiation from the parton
2. Hadronisation
3. Underlying Event

### One important consideration:

Whether the parton is a quark or a gluon  
[quarks radiate with colour factor  $C_F = 4/3$   
gluons radiate with colour factor  $C_A = 3$ ]

## The question's dangerous: a "parton" is an ambiguous concept

Three limits can help you:

- ▶ Threshold limit e.g. de Florian & Vogelsang '07
- ▶ Parton from color-neutral object decay ( $Z'$ )
- ▶ Small- $R$  (radius) limit for jet

One simple result (small- $R$  limit)

$$\frac{\langle p_{t,jet} - p_{t,parton} \rangle}{p_t} = \frac{\alpha_s}{\pi} \ln R \times \begin{cases} 1.01 C_F & \text{quarks} \\ 0.94 C_A + 0.07 n_f & \text{gluons} \end{cases} + \mathcal{O}(\alpha_s)$$

only  $\mathcal{O}(\alpha_s)$  depends on algorithm & process  
cf. Dasgupta, Magnea & GPS '07

## Hadronisation: the “parton-shower” → hadrons transition

### Method:

- ▶ “infrared finite  $\alpha_s$ ” à la Dokshitzer & Webber '95
- ▶ **prediction** based on  $e^+e^-$  event shape data
- ▶ could have been deduced from old work Korchemsky & Sterman '95  
Seymour '97

### Main result

$$\langle p_{t,jet} - p_{t,parton-shower} \rangle \simeq -\frac{0.4 \text{ GeV}}{R} \times \begin{cases} C_F & \text{quarks} \\ C_A & \text{gluons} \end{cases}$$

cf. Dasgupta, Magnea & GPS '07  
coefficient holds for anti- $k_t$ ; see Dasgupta & Delenda '09 for  $k_t$  alg.

“Naive” prediction (UE  $\simeq$  colour dipole between  $pp$ ):

$$\Delta p_t \simeq 0.4 \text{ GeV} \times \frac{R^2}{2} \times \begin{cases} C_F & q\bar{q} \text{ dipole} \\ C_A & \text{gluon dipole} \end{cases}$$

Modern Monte Carlo tunes tell you ( $\sqrt{s} = 7 \text{ TeV}$ ):

$$\Delta p_t \simeq \mathbf{8 \text{ GeV}} \times \frac{R^2}{2} \simeq 1.2 \text{ GeV} \times (\pi R^2)$$

This big coefficient motivates special effort to understand interplay between jet algorithm and UE: “jet areas”

How does coefficient depend on algorithm?

How does it depend on jet  $p_t$ ? How does it fluctuate?

cf. Cacciari, GPS & Soyez '08

“Naive” prediction (UE  $\simeq$  colour dipole between  $pp$ ):

$$\Delta p_t \simeq 0.4 \text{ GeV} \times \frac{R^2}{2} \times \begin{cases} C_F & q\bar{q} \text{ dipole} \\ C_A & \text{gluon dipole} \end{cases}$$

Modern Monte Carlo tunes tell you ( $\sqrt{s} = 7 \text{ TeV}$ ):

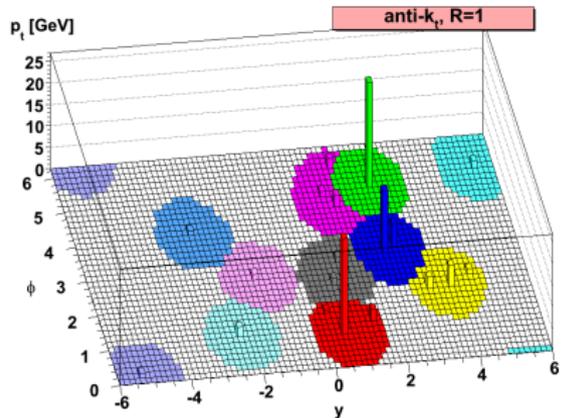
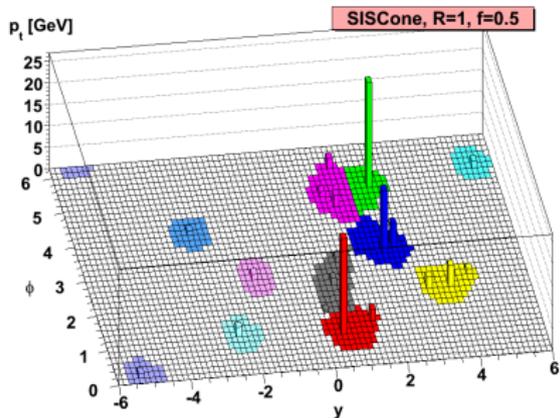
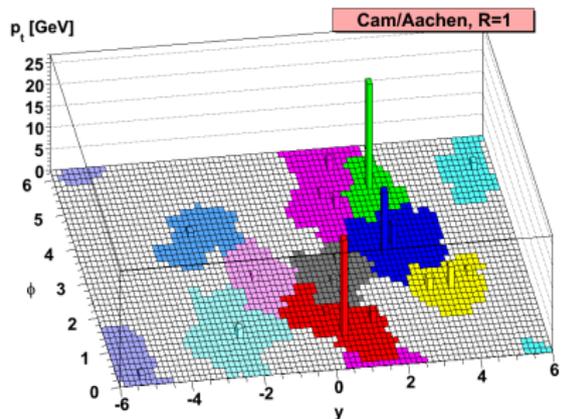
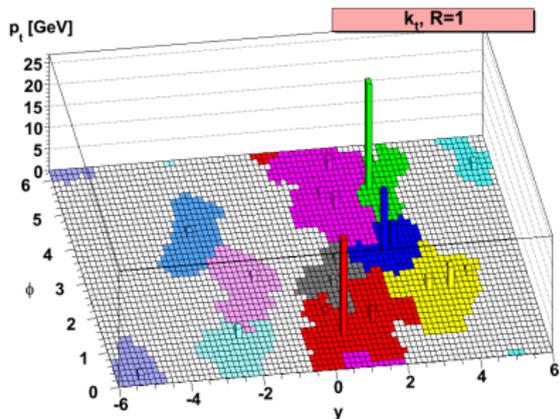
$$\Delta p_t \simeq \mathbf{8 \text{ GeV}} \times \frac{R^2}{2} \simeq 1.2 \text{ GeV} \times (\pi R^2)$$

This big coefficient motivates special effort to understand interplay between jet algorithm and UE: “jet areas”

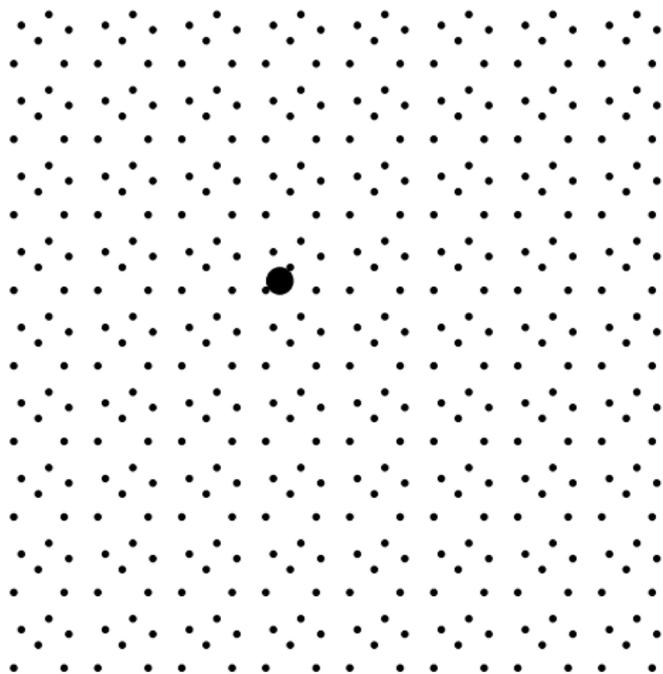
How does coefficient depend on algorithm?

How does it depend on jet  $p_t$ ? How does it fluctuate?

cf. Cacciari, GPS & Soyez '08



## 1. One hard particle, many soft



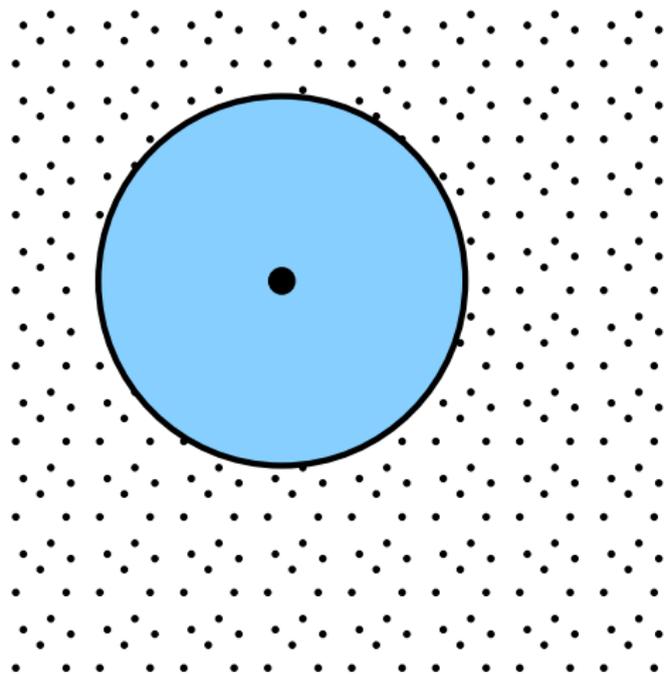
SIScone, any  $R$ ,  $f \gtrsim 0.391$

**Jet area =**

Measure of jet's susceptibility to  
uniform soft radiation

Depends on details of an  
algorithm's clustering dynamics.

2. One hard stable cone, area =  $\pi R^2$



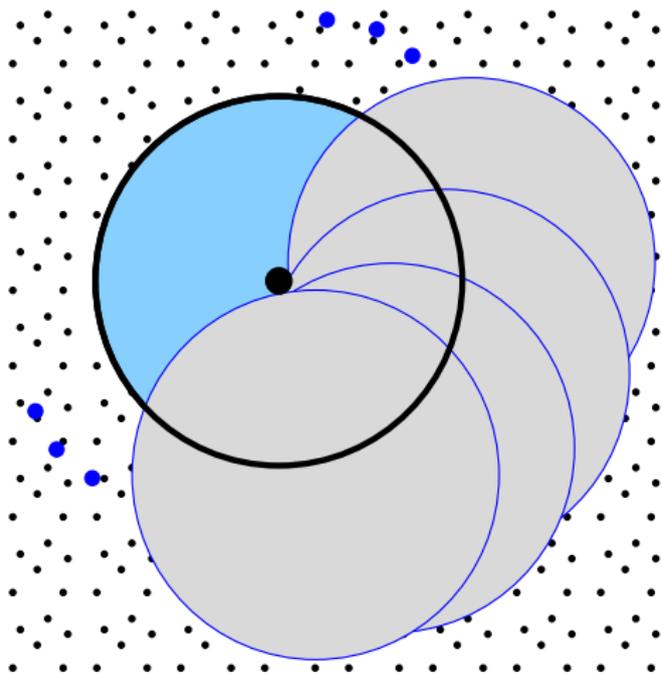
SIScone, any  $R$ ,  $f \gtrsim 0.391$

**Jet area =**

Measure of jet's susceptibility to  
uniform soft radiation

Depends on details of an  
algorithm's clustering dynamics.

### 3. Overlapping “soft” stable cones



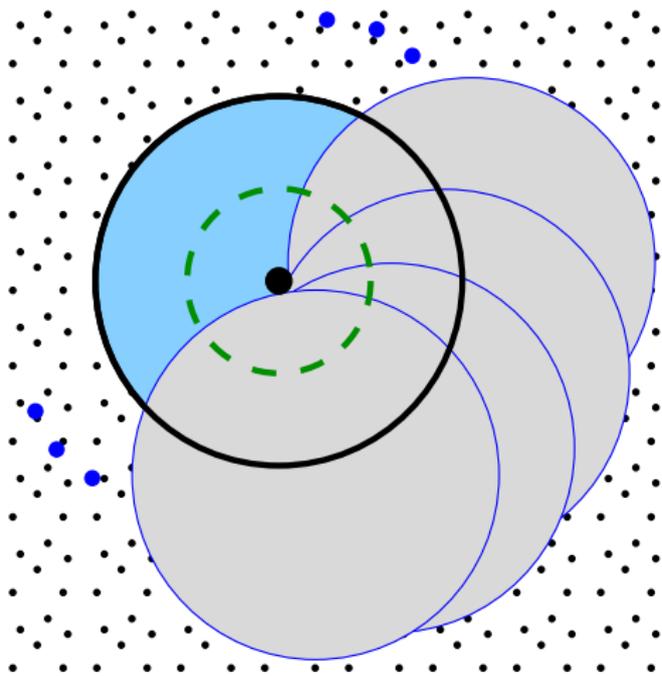
SIScone, any  $R$ ,  $f \gtrsim 0.391$

**Jet area =**

Measure of jet's susceptibility to  
uniform soft radiation

Depends on details of an  
algorithm's clustering dynamics.

#### 4. "Split" the overlapping parts



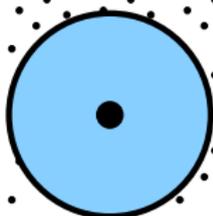
SIScone, any  $R$ ,  $f \gtrsim 0.391$

**Jet area =**

Measure of jet's susceptibility to  
uniform soft radiation

Depends on details of an  
algorithm's clustering dynamics.

## 5. Final hard jet (reduced area)



SIScone, any  $R$ ,  $f \gtrsim 0.391$

**Jet area =**

Measure of jet's susceptibility to uniform soft radiation

Depends on details of an algorithm's clustering dynamics.

SIScone's area (1 hard particle)

$$= \frac{1}{4} \pi R^2$$

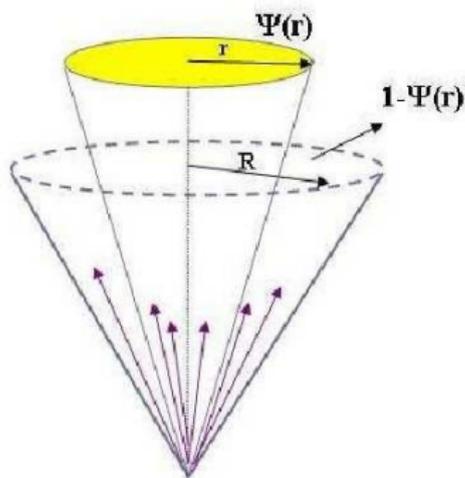
Small area  $\equiv$   
low sensitivity to UE & pileup

	$k_t$	Cam/Aachen	anti- $k_t$	SISCone
reach	$R$	$R$	$R$	$(1 + \frac{p_{t2}}{p_{t1}})R$
$\Delta p_{t,PT} \simeq \frac{\alpha_s C_i}{\pi} \times$	$\ln R$	$\ln R$	$\ln R$	$\ln 1.35R$
$\Delta p_{t,hadr} \simeq -\frac{0.4 \text{ GeV} C_i}{R} \times$	0.7	?	1	?
area = $\pi R^2 \times$	$0.81 \pm 0.28$	$0.81 \pm 0.26$	1	0.25
$+ \pi R^2 \frac{C_i}{\pi b_0} \ln \frac{\alpha_s(Q_0)}{\alpha_s(Rp_t)} \times$	$0.52 \pm 0.41$	$0.08 \pm 0.19$	0	$0.12 \pm 0.07$

## In words:

- ▶  $k_t$ : area fluctuates a lot, depends on  $p_t$  (bad for UE)
- ▶ Cam/Aachen: area fluctuates somewhat, depends less on  $p_t$
- ▶ anti- $k_t$ : area is constant (circular jets)
- ▶ SISCone: reaches far for hard radiation (good for resolution, bad for multijets), area is smaller (good for UE)

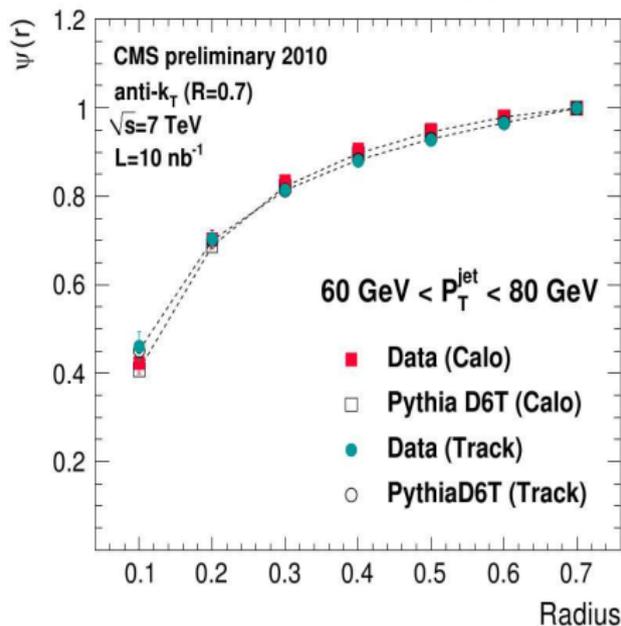
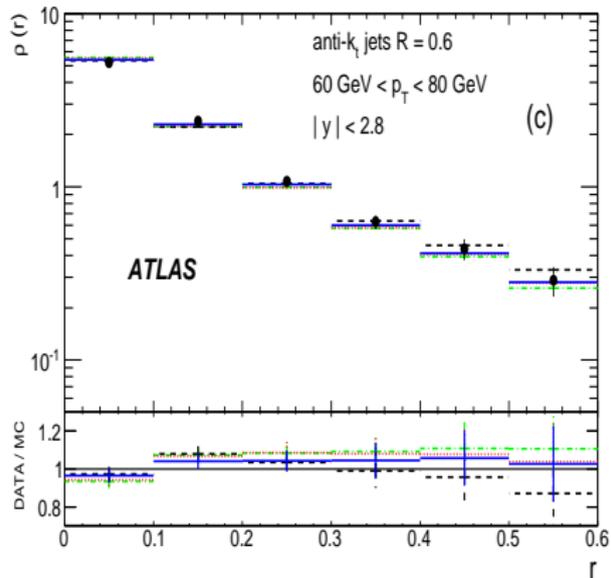
# Where does radiation go? Look at jet “shapes”



Jet Shape:

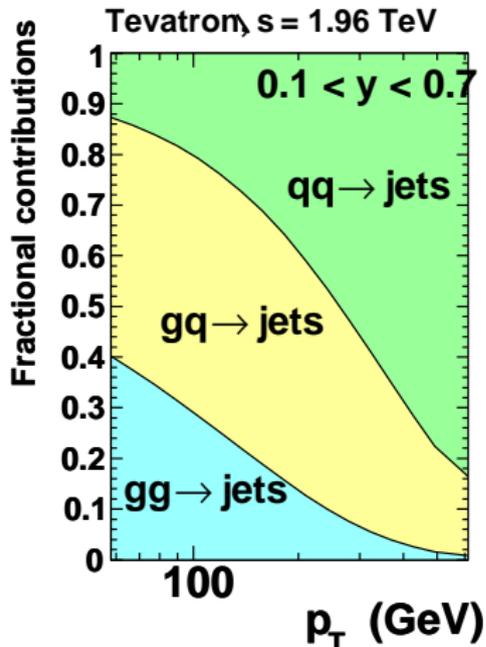
$$\Psi(r) = \int_0^r \frac{p_t(r')}{p_t(\text{jet})} dr'$$

Fraction of energy inside a sub-cone of size  $r$

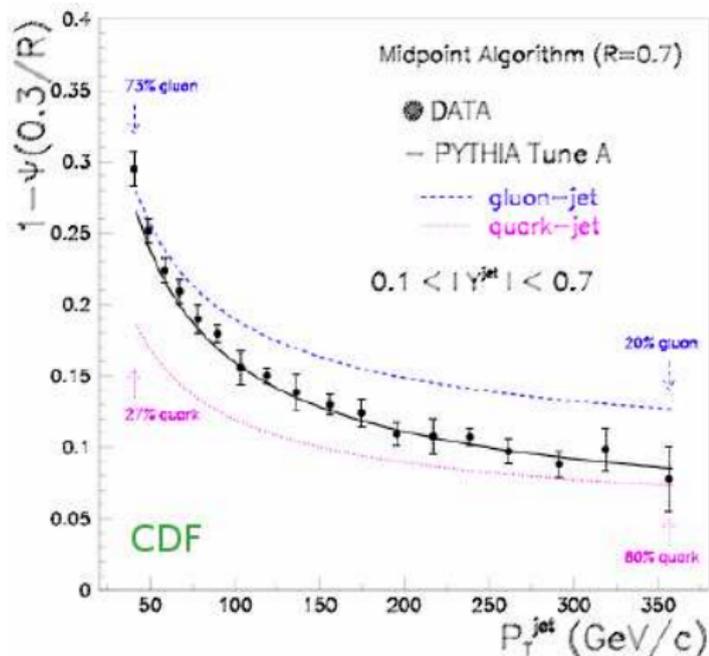
Integrated Jet Shape  $\Psi(r)$  v.  $r$ Differential Jet Shape  $\rho(r) = d/dr\Psi(r)$ 

**50% of energy concentrated in cone of  $\sim 0.1$**

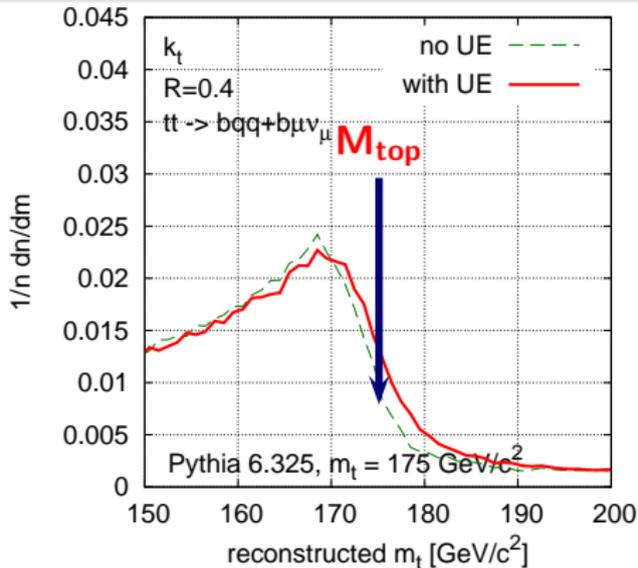
## Inclusive jet cross sections with MSTW 2008 NLO PDFs



see clear sign of quark to gluon ratio evolving



# A qualitative example: top reconstruction



Game: measure top mass to 1 GeV

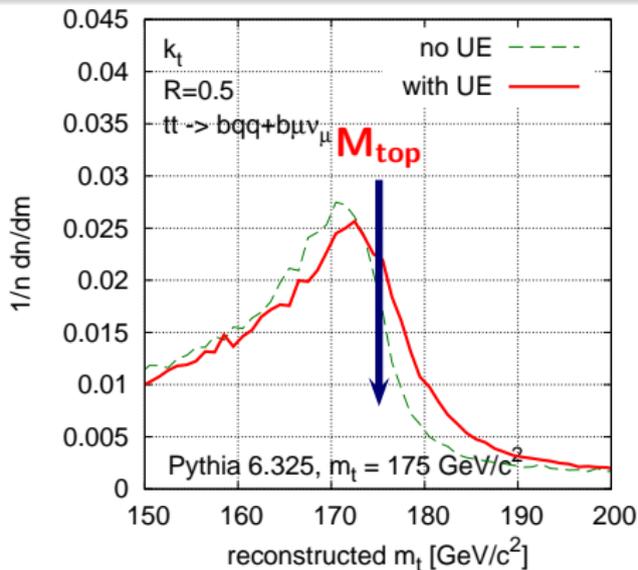
example for Tevatron  
 $m_t = 175 \text{ GeV}$

- ▶ Small  $R$ : lose 6 GeV to PT radiation and hadronisation, UE and pileup irrelevant

- ▶ Large  $R$ : hadronisation and PT radiation leave mass at  $\sim 175 \text{ GeV}$ , UE adds 2 – 4 GeV

*Is the final top mass (after  $W$  jet-energy-scale and Monte Carlo unfolding) independent of  $R$  used to measure jets?*

Flexibility in jet finding gives powerful cross-check of systematic effects  
 cf. Seymour & Tevin '06



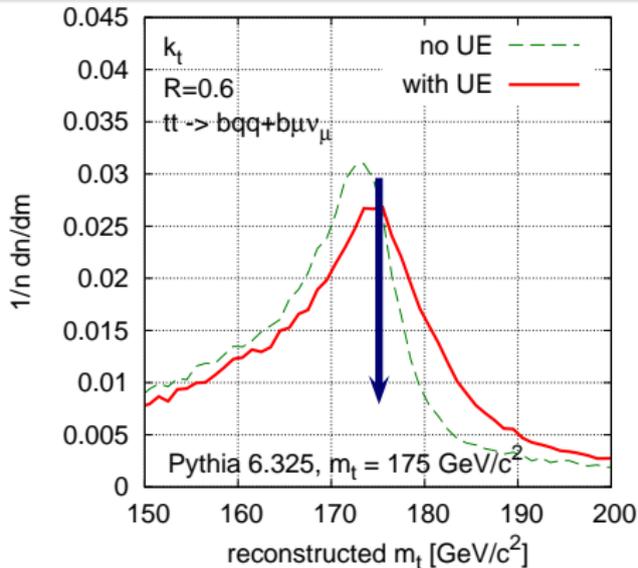
Game: measure top mass to 1 GeV

example for Tevatron  
 $m_t = 175 \text{ GeV}$

- ▶ Small  $R$ : lose 6 GeV to PT radiation and hadronisation, UE and pileup irrelevant
- ▶ Large  $R$ : hadronisation and PT radiation leave mass at  $\sim 175 \text{ GeV}$ , UE adds 2 – 4 GeV.

*Is the final top mass (after  $W$  jet-energy-scale and Monte Carlo unfolding) independent of  $R$  used to measure jets?*

Flexibility in jet finding gives powerful cross-check of systematic effects  
 cf. Seymour & Tevlin '06



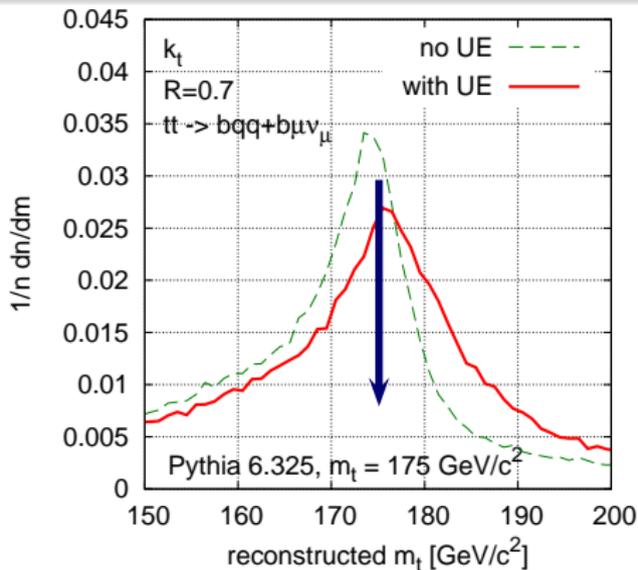
Game: measure top mass to 1 GeV

example for Tevatron  
 $m_t = 175 \text{ GeV}$

- ▶ Small  $R$ : lose 6 GeV to PT radiation and hadronisation, UE and pileup irrelevant
- ▶ Large  $R$ : hadronisation and PT radiation leave mass at  $\sim 175 \text{ GeV}$ , UE adds 2 – 4 GeV.

*Is the final top mass (after  $W$  jet-energy-scale and Monte Carlo unfolding) independent of  $R$  used to measure jets?*

Flexibility in jet finding gives powerful cross-check of systematic effects  
 cf. Seymour & Tevlin '06



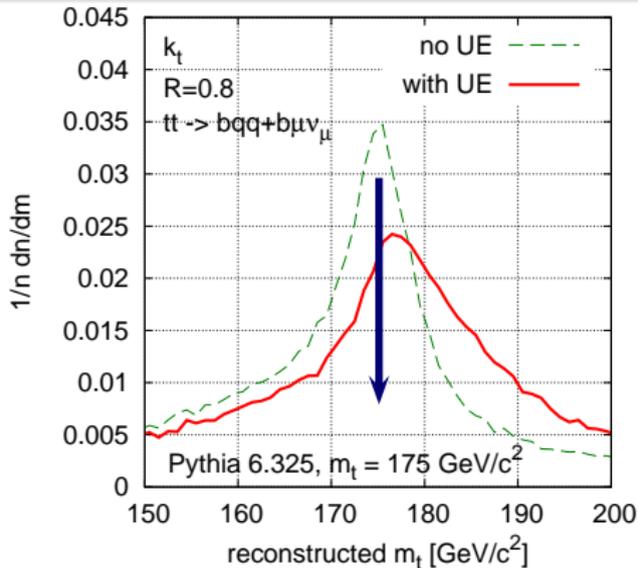
### Game: measure top mass to 1 GeV

example for Tevatron  
 $m_t = 175 \text{ GeV}$

- ▶ Small  $R$ : lose 6 GeV to PT radiation and hadronisation, UE and pileup irrelevant
- ▶ Large  $R$ : hadronisation and PT radiation leave mass at  $\sim 175 \text{ GeV}$ , UE adds 2 – 4 GeV.

*Is the final top mass (after  $W$  jet-energy-scale and Monte Carlo unfolding) independent of  $R$  used to measure jets?*

Flexibility in jet finding gives powerful cross-check of systematic effects  
 cf. Seymour & Tevlin '06



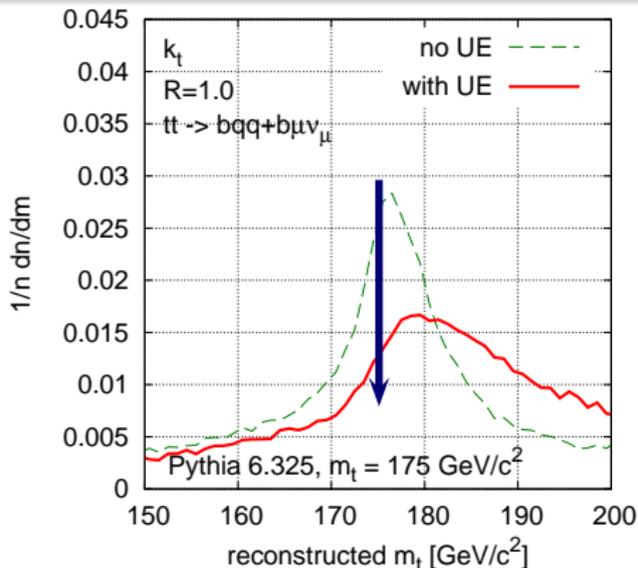
Game: measure top mass to 1 GeV

example for Tevatron  
 $m_t = 175$  GeV

- ▶ Small  $R$ : lose 6 GeV to PT radiation and hadronisation, UE and pileup irrelevant
- ▶ Large  $R$ : hadronisation and PT radiation leave mass at  $\sim 175$  GeV, UE adds 2 – 4 GeV.

*Is the final top mass (after  $W$  jet-energy-scale and Monte Carlo unfolding) independent of  $R$  used to measure jets?*

Flexibility in jet finding gives powerful cross-check of systematic effects  
 cf. Seymour & Tevlin '06



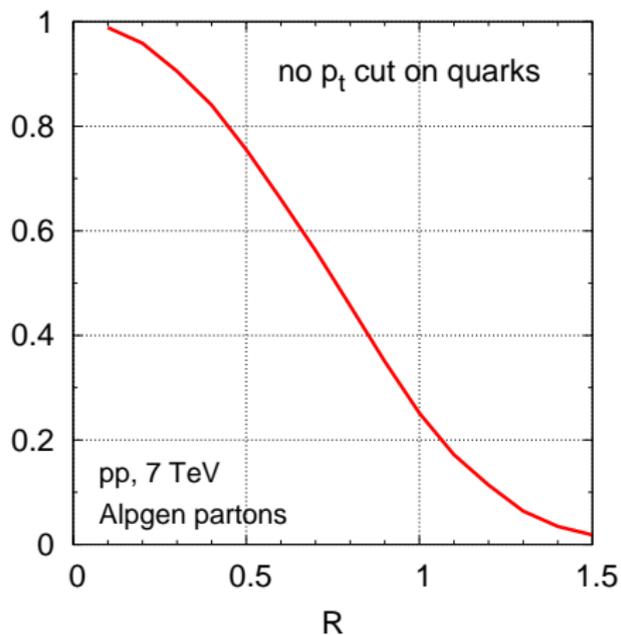
Game: measure top mass to 1 GeV

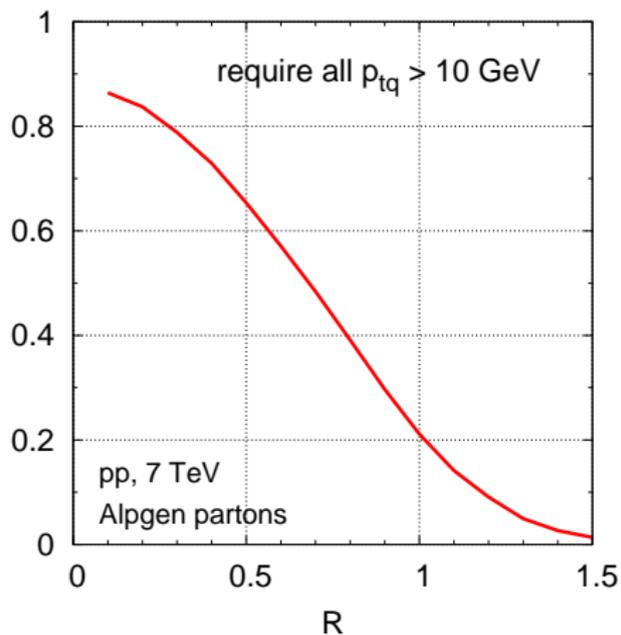
example for Tevatron  
 $m_t = 175$  GeV

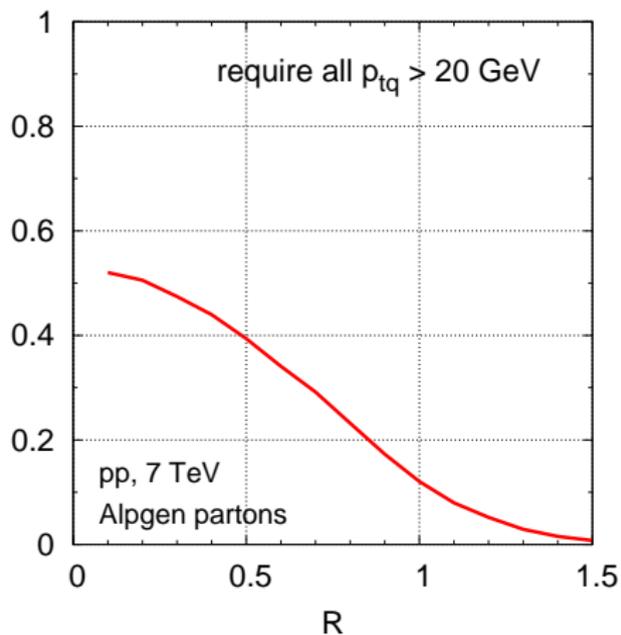
- ▶ Small  $R$ : lose 6 GeV to PT radiation and hadronisation, UE and pileup irrelevant
- ▶ Large  $R$ : hadronisation and PT radiation leave mass at  $\sim 175$  GeV, UE adds 2 – 4 GeV.

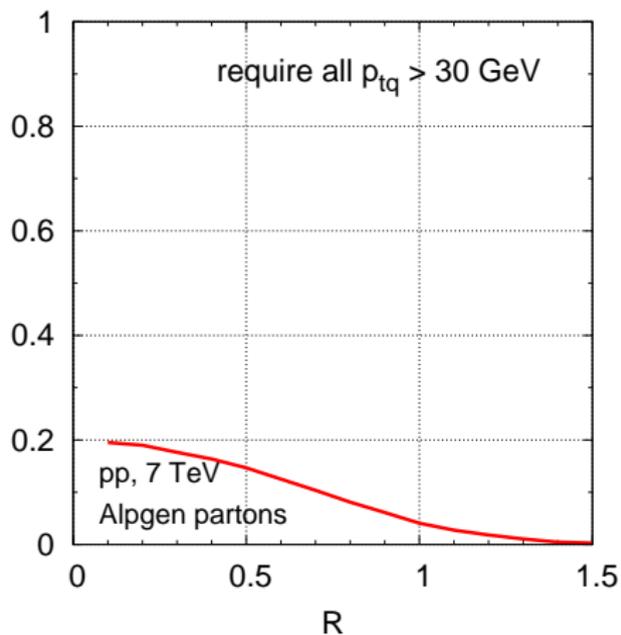
*Is the final top mass (after  $W$  jet-energy-scale and Monte Carlo unfolding) independent of  $R$  used to measure jets?*

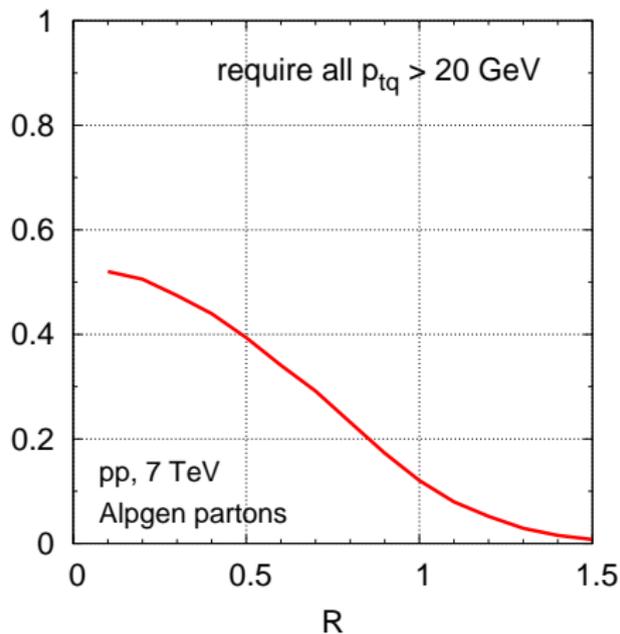
Flexibility in jet finding gives powerful cross-check of systematic effects  
 cf. Seymour & Tevlin '06

**Alpgen  $pp \rightarrow t\bar{t} \rightarrow 6q$** fraction of  $pp \rightarrow t\bar{t} \rightarrow 6q$  events with all  $R_{qq} > R$ 

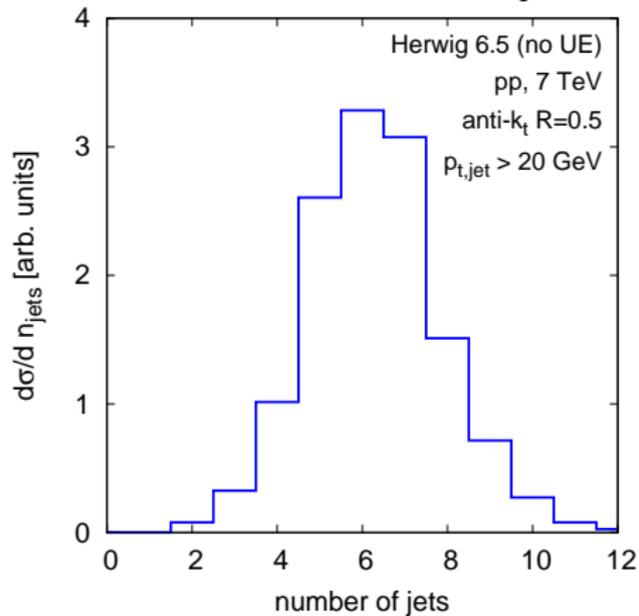
**Alpgen  $pp \rightarrow t\bar{t} \rightarrow 6q$** fraction of  $pp \rightarrow t\bar{t} \rightarrow 6q$  events with all  $R_{qq} > R$ 

**Alpgen  $pp \rightarrow t\bar{t} \rightarrow 6q$** fraction of  $pp \rightarrow t\bar{t} \rightarrow 6q$  events with all  $R_{qq} > R$ 

**Alpgen  $pp \rightarrow t\bar{t} \rightarrow 6q$** fraction of  $pp \rightarrow t\bar{t} \rightarrow 6q$  events with all  $R_{qq} > R$ 

**Alpgen  $pp \rightarrow t\bar{t} \rightarrow 6q$** fraction of  $pp \rightarrow t\bar{t} \rightarrow 6q$  events with all  $R_{qq} > R$ **Herwig  $pp \rightarrow t\bar{t} \rightarrow \text{hadrons}$** 

Distribution of number of jets



Experiment-theory correspondence relies on infrared and collinear safety

Relation between a parton and a jet is ambiguous  
(because “partons” are ambiguous)

But many rule-of-thumb relations can be derived,  
e.g. for  $R$ -dependence from different physics contributions  
[perturbative radiation, hadronisation, underlying event]