

Gavin Salam

CERN Theory Unit

ICTP-SAIFR school on QCD and LHC physics July 2015, São Paulo, Brazil



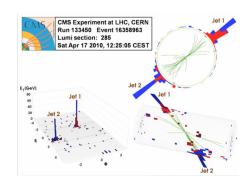
QUANTUM CHROMODYNAMICS

The theory of quarks, gluons and their interactions

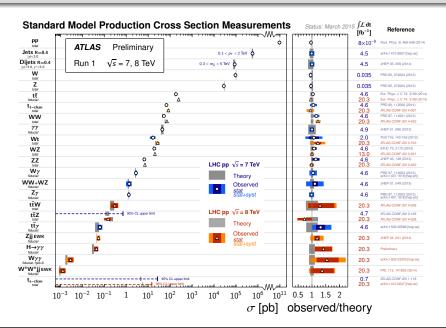
It's central to all modern colliders.

(And QCD is what

we're made of)



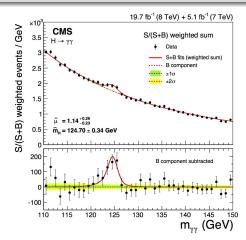
QCD predictions v. data for many processes



QCD for Higgs physics

QCD is especially relevant in order to deduce information about the **Higgs boson**.

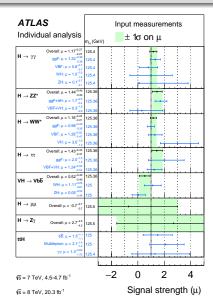
[cf. lectures by Andre Sznajder & Claude Duhr]



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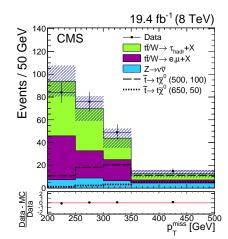
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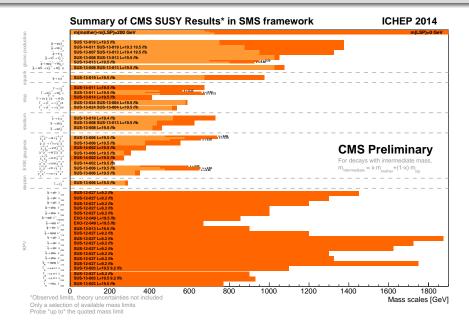
QCD and searches for new physics

Identification and/or exclusion of potential new physics relies in diverse ways on a QCD-based understanding of signals and backgrounds.

Search for stop squarks



QCD and searches for new physics



The school will cover many aspects of QCD, from the advanced calculation techniques to the experimental consequences.

This course:

A reminder of what QCD is

A few core equations & concepts (running coupling, collider cross sections infrared divergences and infrared safety)

More depth on topics not covered in other lectures (parton distribution functions, jets)

- ▶ Quarks (and anti-quarks): they come in 3 colours
- ► Gluons: a bit like photons in QED

 But there are 8 of them, and they're colour charged
- ▶ And a coupling, α_s , that's not so small and runs fast At LHC, in the range 0.08(@5 TeV) to $\mathcal{O}(1)(@0.5 \text{ GeV})$

Quarks — 3 colours:
$$\psi_a = \begin{pmatrix} \psi_1 \\ \psi_2 \\ \psi_3 \end{pmatrix}$$

Quark part of Lagrangian:

Let's write down QCD in full detail

(There's a lot to absorb here — but it should become more palatable as we return to individual elements later)

A representation is:
$$t'' = \frac{1}{2}\lambda''$$
,

$$\lambda^{1} = \begin{pmatrix} 0 & 1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}, \ \lambda^{2} = \begin{pmatrix} 0 & -i & 0 \\ i & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}, \ \lambda^{3} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 0 \end{pmatrix}, \ \lambda^{4} = \begin{pmatrix} 0 & 0 & 1 \\ 0 & 0 & 0 \\ 1 & 0 & 0 \end{pmatrix}$$

$$\lambda^{5} = \begin{pmatrix} 0 & 0 & -i \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}, \ \lambda^{6} = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 0 & 1 \end{pmatrix}, \ \lambda^{7} = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & -i \\ 0 & 0 & 0 \end{pmatrix}, \ \lambda^{8} = \begin{pmatrix} \frac{1}{\sqrt{3}} & 0 & 0 \\ 0 & \frac{1}{\sqrt{3}} & 0 \\ 0 & \frac{1}{\sqrt{3}} & 0 \\ 0 & 0 & 0 \end{pmatrix}$$

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$$\mathcal{L}_{q} = \bar{\psi}_{a} (i\gamma^{\mu}\partial_{\mu}\delta_{ab} - g_{s}\gamma^{\mu}t_{ab}^{C}\mathcal{A}_{\mu}^{C} - m)\psi_{b}$$

SU(3) local gauge symmetry $\leftrightarrow 8 \ (= 3^2 - 1)$ generators $t_{ab}^1 \dots t_{ab}^8$ corresponding to 8 gluons $\mathcal{A}_{\mu}^1 \dots \mathcal{A}_{\mu}^8$.

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Field tensor:
$$F_{\mu\nu}^A = \partial_{\mu}A_{\nu}^A - \partial_{\nu}A_{\nu}^A - g_s f_{ABC}A_{\mu}^BA_{\nu}^C$$
 $[t^A, t^B] = if_{ABC}t^C$

 f_{ABC} are structure constants of SU(3) (antisymmetric in all indices — SU(2) equivalent was ϵ^{ABC}). Needed for gauge invariance of gluon part of Lagrangian:

$$\mathcal{L}_{G} = -\frac{1}{4} F_{A}^{\mu\nu} F^{A\mu\nu}$$

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Exercise

Consider gauge transformations

$$\psi \to U(x)\psi$$
, $U(x) = e^{iu^A(x)t^A}$

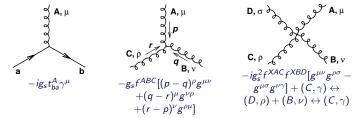
How should the gluon field A_{μ}^{C} transform in order for \mathcal{L}_{q} to be gauge invariant? Show that with the same transformations, \mathcal{L}_{G} is gauge invariant.

Perturbation theory

Relies on idea of order-by-order expansion small coupling, $lpha_{
m s}\ll 1$

$$\alpha_{s} + \underbrace{\alpha_{s}^{2}}_{small} + \underbrace{\alpha_{s}^{3}}_{smaller} + \underbrace{\dots}_{negligible?}$$

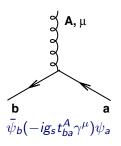
Interaction vertices of Feynman rules:

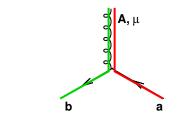


These expressions are fairly complex, so you really don't want to have to deal with too many orders of them! i.e. α_s had better be small. . .

[Zvi Bern will show you how to do things more easily!]

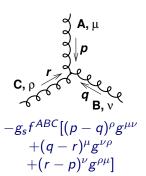
What do Feynman rules mean physically?

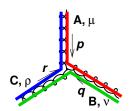




$$\underbrace{\begin{pmatrix} 0 & 1 & 0 \\ & & & \\ & & & \\ & & & \\ \hline{\psi}_b & & & \\ & & & \\ \hline{\psi}_b & & & \\ \end{pmatrix}}_{\bar{\psi}_b} \underbrace{\begin{pmatrix} 0 & 1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}}_{t_b^1} \underbrace{\begin{pmatrix} 1 \\ 0 \\ 0 \\ \end{pmatrix}}_{\psi_a}$$

A gluon emission **repaints** the quark colour. A gluon itself carries colour and anti-colour.





A gluon emission also repaints the gluon colours.

Because a gluon carries colour + anti-colour, it emits \sim twice as strongly as a quark (just has colour)

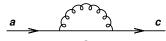
$$\operatorname{Tr}(t^A t^B) = T_R \delta^{AB}, \quad T_R = \frac{1}{2}$$

$$\sum_{A} t_{ab}^{A} t_{bc}^{A} = C_{F} \delta_{ac} \,, \quad C_{F} = \frac{N_{c}^{2} - 1}{2N_{c}} = \frac{4}{3}$$

$$\sum_{C,D} f^{ACD} f^{BCD} = C_A \delta^{AB}$$
, $C_A = N_c = 3$

$$t_{ab}^A t_{cd}^A = \frac{1}{2} \delta_{bc} \delta_{ad} - \frac{1}{2N_c} \delta_{ab} \delta_{cd} \ \ (\text{Fierz})$$







$$\begin{array}{c}
b \\
3 \\
3 \\
1 \\
2
\end{array}$$

$$\begin{array}{c}
-1 \\
2N
\end{array}$$

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$$\begin{array}{c}
b \\
3 \\
3 \\
4
\end{array} = \frac{1}{2} \quad \boxed{\begin{array}{c}
-\frac{1}{2N} \\
2N
\end{array}}$$

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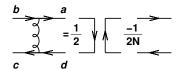
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$$\begin{array}{c}
b \\
3 \\
3 \\
-\frac{1}{2}
\end{array}$$



Use the Fierz identity (fourth line of previous slide) to derive the second line.

All couplings run (QED, QCD, EW), i.e. they depend on the momentum scale (Q^2) of your process.

The evolution equation for the QCD coupling, $\alpha_s(Q^2)$, is:

$$Q^2 \frac{\partial \alpha_s}{\partial Q^2} = \beta(\alpha_s), \qquad \beta(\alpha_s) = -\alpha_s^2 (b_0 + b_1 \alpha_s + b_2 \alpha_s^2 + \ldots),$$

$$b_0 = \frac{11C_A - 2n_f}{12\pi}$$
, $b_1 = \frac{17C_A^2 - 5C_An_f - 3C_Fn_f}{24\pi^2} = \frac{153 - 19n_f}{24\pi^2}$

Note sign: Asymptotic Freedom, due to gluon to self-interaction

- ▶ At high scales *Q*, coupling becomes small
 - ⇒quarks and gluons are almost free, interactions are weak
- ▶ At low scales, coupling becomes strong
 - ⇒quarks and gluons interact strongly confined into hadrons

 Perturbation theory fails.

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Solve
$$Q^2 \frac{\partial \alpha_s}{\partial Q^2} = -b_0 \alpha_s^2 \quad \Rightarrow \quad \alpha_s(Q^2) = \frac{\alpha_s(Q_0^2)}{1 + b_0 \alpha_s(Q_0^2) \ln \frac{Q^2}{Q_0^2}} = \frac{1}{b_0 \ln \frac{Q^2}{\Lambda^2}}$$

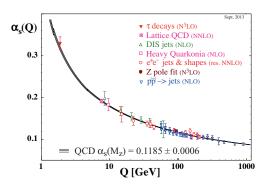
 $\Lambda \simeq 0.2$ GeV (aka Λ_{QCD}) is the fundamental scale of QCD, at which coupling blows up.

- Λ sets the scale for hadron masses
 (NB: Λ not unambiguously defined wrt higher orders)
- ▶ Perturbative calculations valid for scales $Q \gg \Lambda$.

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Nobel prize citation (annotated by Skands)

"What this year's Laureates discovered was something that, at first sight, seemed completely contradictory. The interpretation of their mathematical result was that the closer the quarks are to each other, the weaker is the 'colour charge'. When the quarks are really close to each other, the force is so weak that they behave almost as free particles. This phenomenon is called 'asymptotic freedom'. The converse is true when the quarks move apart:

the force becomes stronger when the

Nobelprize.org

The Nobel Prize in Physics 2004
David J. Gross, H. David Politzer, Frank Wilczek







David J. Gross H. David Politzer Frank Wilczek
The Nobel Prize in Physics 2004 was awarded jointly to David J. Gross, H. David Politzer and Frank
Wilczek Tor the discovery of asymptotic freedom in the theory of the strong interaction".

Photos: Copyright @ The Nobel Foundation



distance increases."

- *I The force still goes to ∞ as $r \to 0$ (Coulomb potential), just less slowly
- *2 The potential grows linearly as r→∞, so the force actually becomes constant (even this is only true in "quenched" QCD. In real QCD, the force eventually vanishes for r>>1fm)

Exercise

There is a freedom in defining the "scheme" for α_s . E.g.

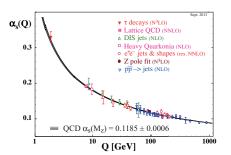
$$lpha_{
m s}^{
m scheme-B} = lpha_{
m s}^{
m scheme-A} + c_B (lpha_{
m s}^{
m scheme-A})^2$$

where c_B is some scheme-conversion coefficient.

The β -function coefficients, usually given in the so-called $\overline{\text{MS}}$ renormalisation scheme, are known up to b_3 .

Which of the b_0 , b_1 , b_2 , etc. coefficients is modified if the scheme is changed?

[Basic methods] A dilemna



- We want to investigate collisions at high energies (~ 100 GeV to few TeV), where the coupling is small → perturbative methods are the natural choice
- ▶ But the LHC collides protons, m ≈ 0.94 GeV, which definitely involve strong coupling physics

There is no escape from non-perturbative physics

- ► Put all the quark and gluon fields of QCD on a 4D-lattice NB: with imaginary time
- Figure out which field configurations are most likely (by Monte Carlo sampling).
- ► You've solved QCD

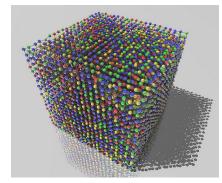
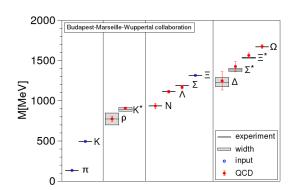


image credits: fdecomite [Flickr]

Lattice QCD is great at calculation static properties of a single hadron.

E.g. the hadron mass spectrum



Durr et al '08

How big a lattice do you need for an LHC collision @ 14 TeV?

Lattice spacing:
$$\frac{1}{14 \text{ TeV}} \sim 10^{-5} \, \mathrm{fm}$$

Lattice extent:

- ▶ non-perturbative dynamics for quark/hadron near rest takes place on timescale $t \sim \frac{1}{0.5~\text{GeV}} \sim 0.4~\text{fm/}c$
- ightharpoonup But guarks at LHC have effective boost factor $\sim 10^4$
- \blacktriangleright So lattice extent should be \sim 4000 fm

 $\label{eq:total:need} \frac{\text{Total:}}{\text{Plus clever tricks to deal with high particle multiplicity,}} \text{ nodes total.}$

Neither lattice QCD nor perturbative QCD can offer a full solution to using QCD at colliders

What the community has settled on is

- 1) **factorisation** of initial state non-perturbative problem from
 - the "hard process," calculated perturbatively supplemented with
- 3) non-perturbative modelling of final-state hadronic-scale processes ("hadronisation").