

General aspects of QCD at future colliders

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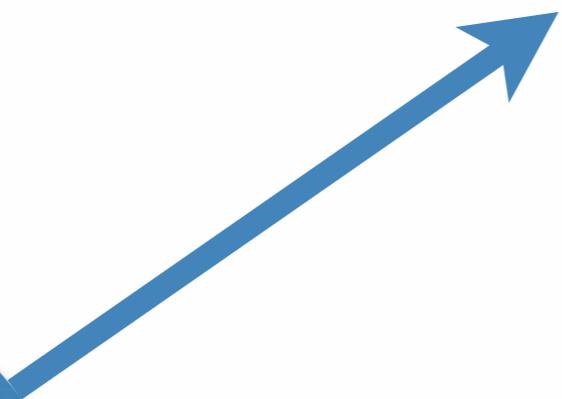
SLAC Workshop on Physics at a 100 TeV Collider
23-25 April 2014

We have seen / will see talks on many of the
key topics of QCD:

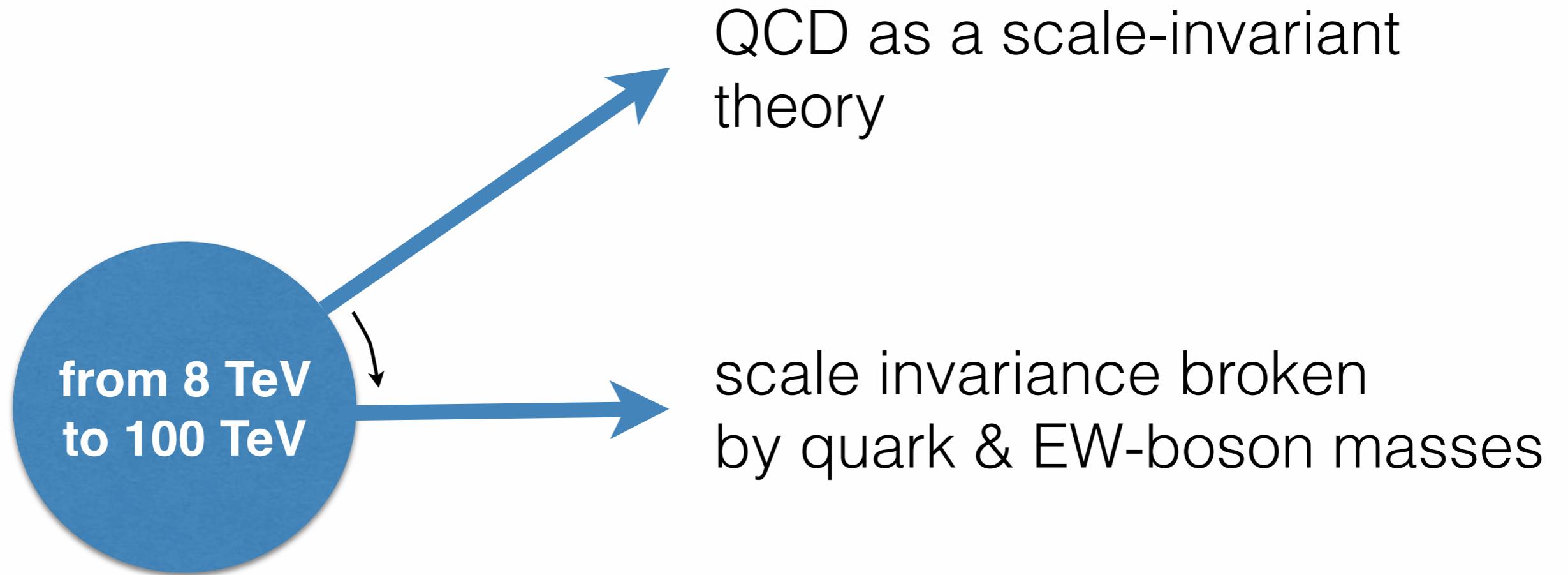
PDFs, MC matching, Jets

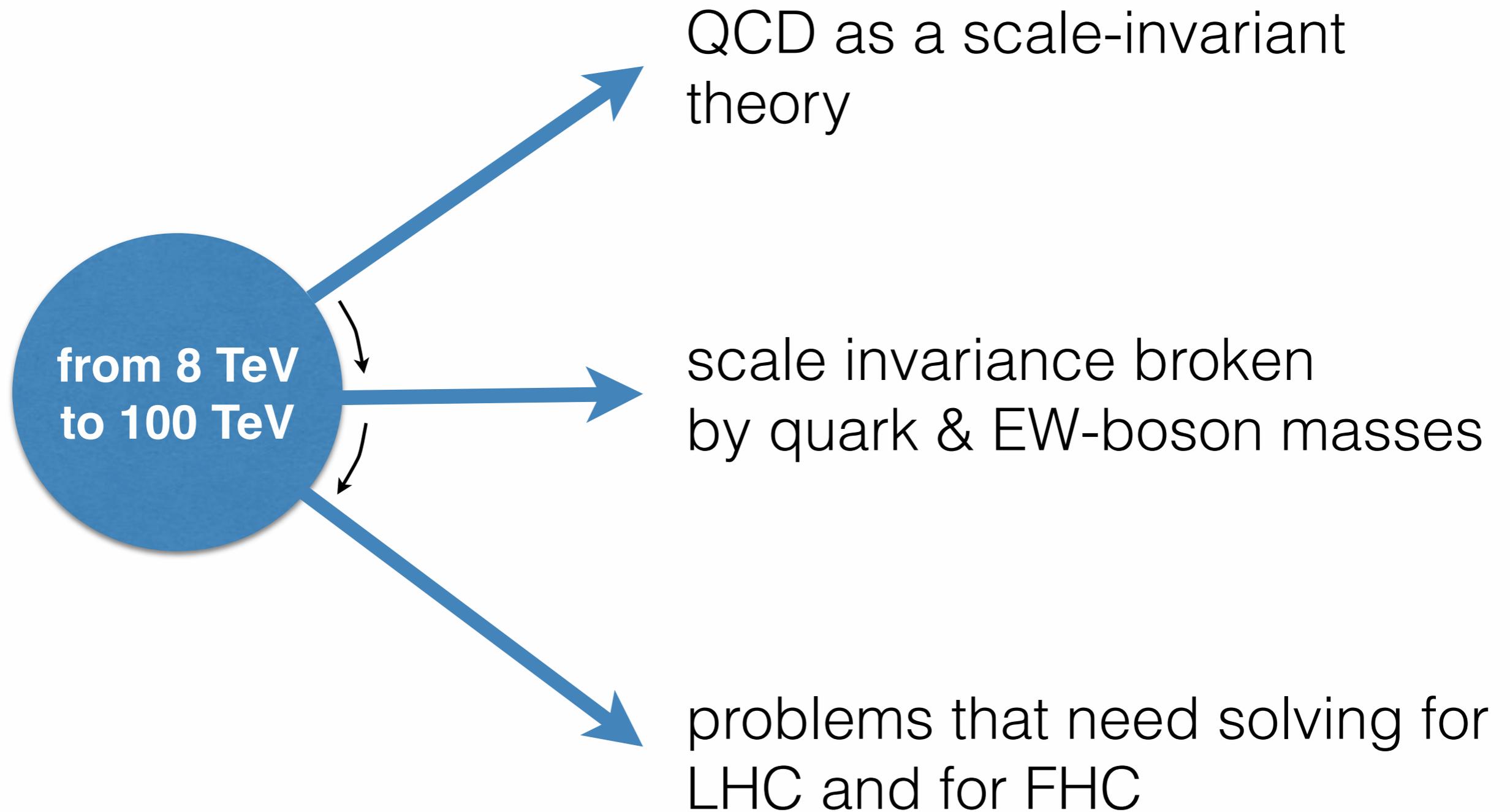
What is there left for me to tell you?

**from 8 TeV
to 100 TeV**

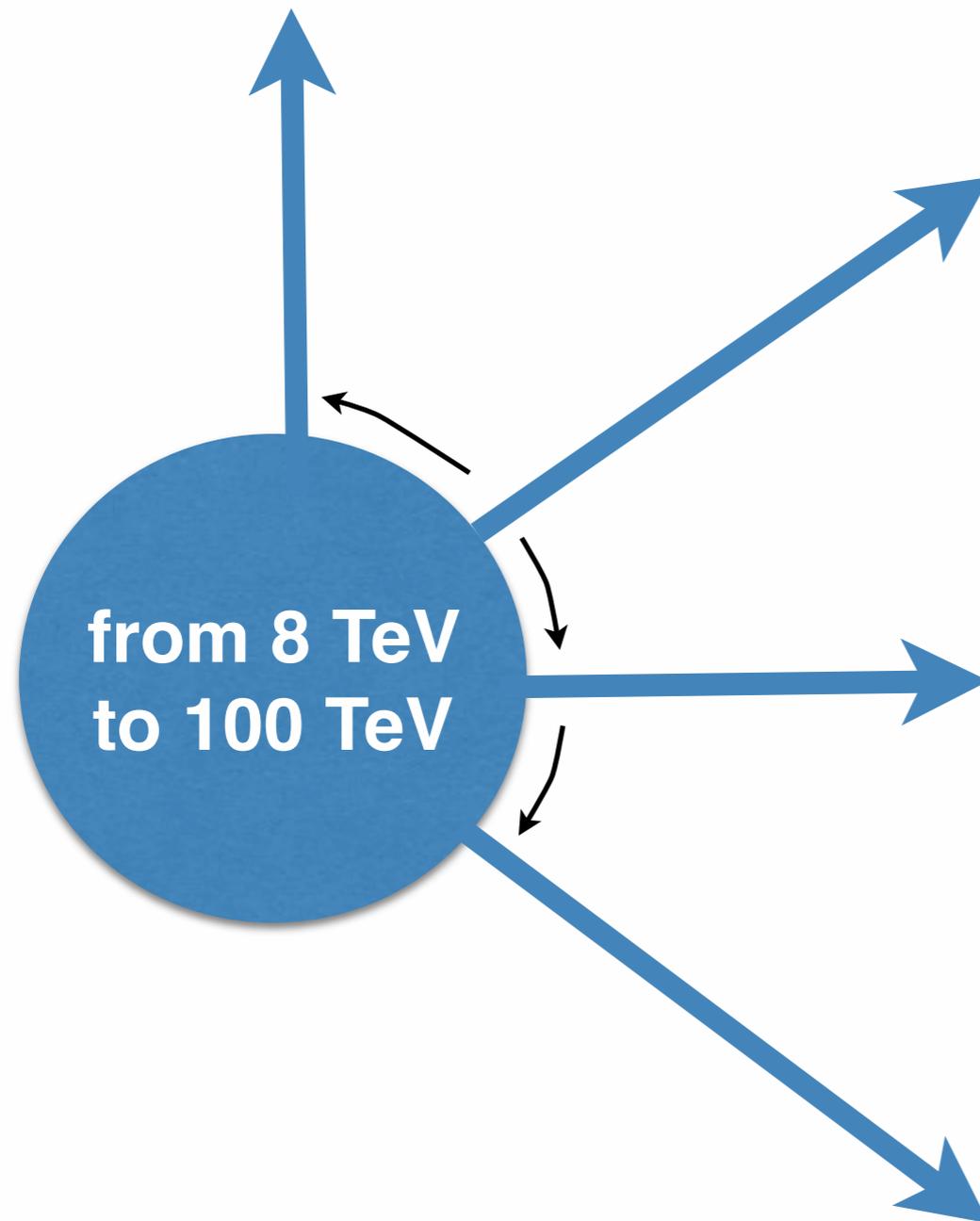


QCD as a scale-invariant
theory





Collider Reach



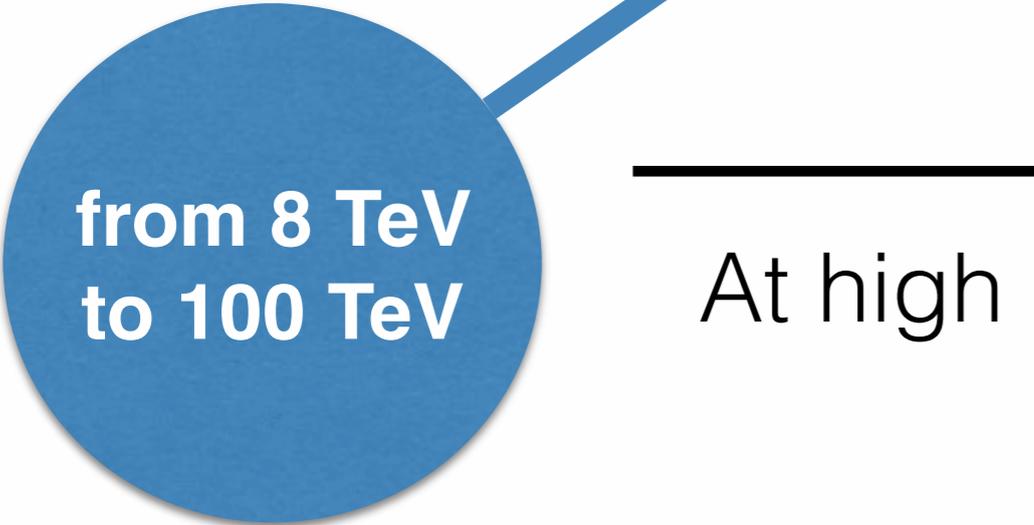
**from 8 TeV
to 100 TeV**

QCD as a scale-invariant theory

scale invariance broken by quark & EW-boson masses

problems that need solving for LHC and for FHC

QCD as a scale-invariant theory



from 8 TeV
to 100 TeV

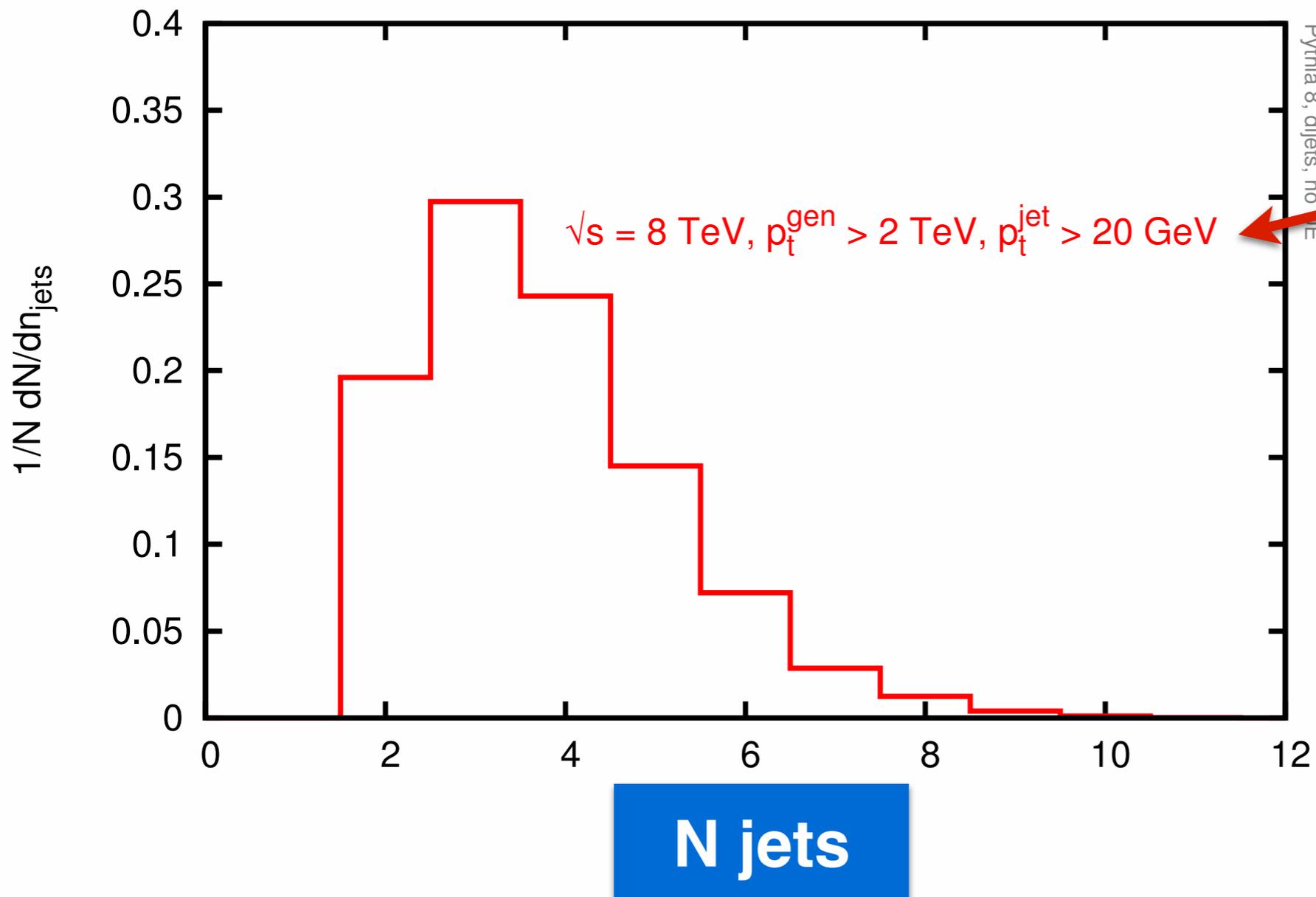
At high scales, α_s runs slowly, as do PDFs

Little difference between
2 TeV physics at an 8 TeV collider
and 25 TeV physics at a 100 TeV collider

$$\alpha_s (2 \text{ TeV}) = 0.083$$

$$\alpha_s (25 \text{ TeV}) = 0.067$$

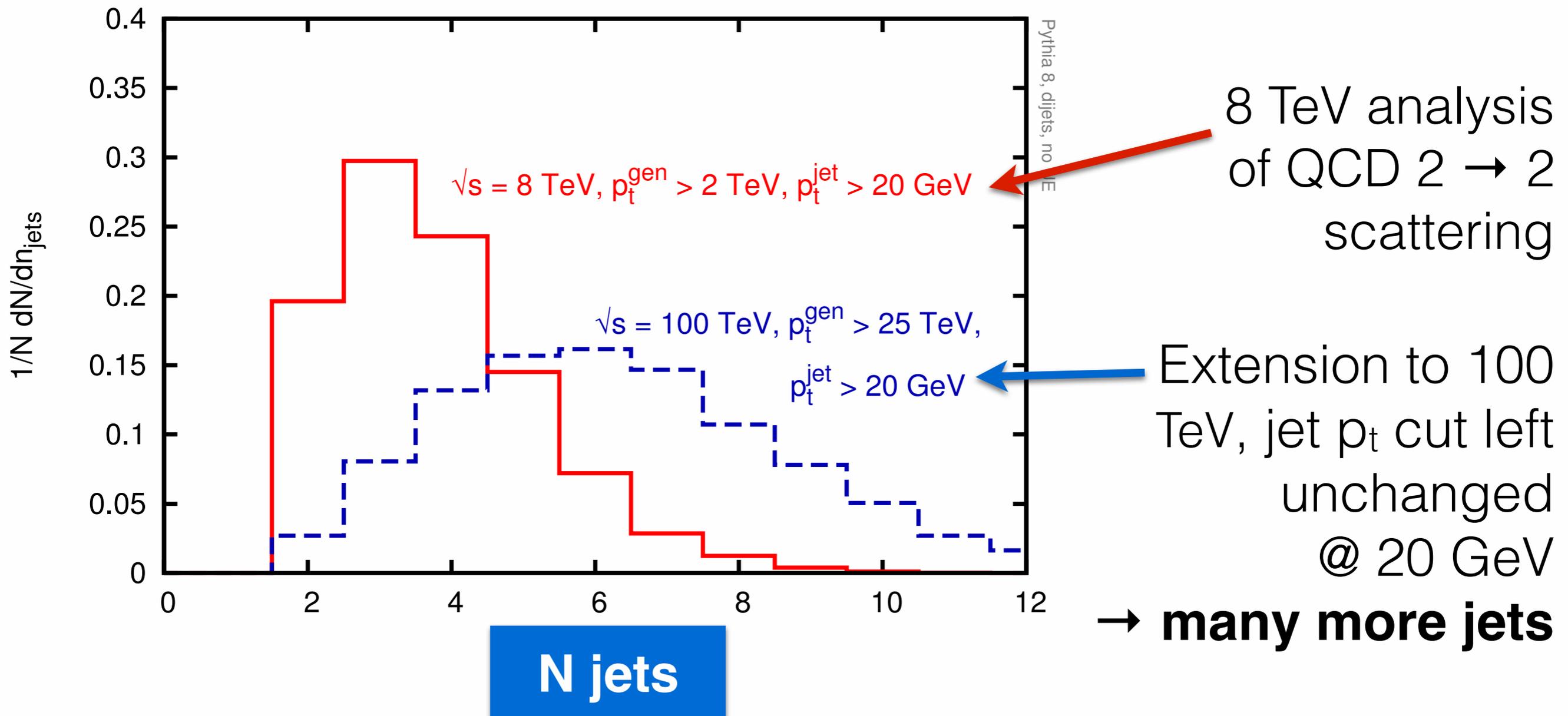
Scale invariance holds if **all ratios of scales kept fixed**



8 TeV analysis
of QCD $2 \rightarrow 2$
scattering

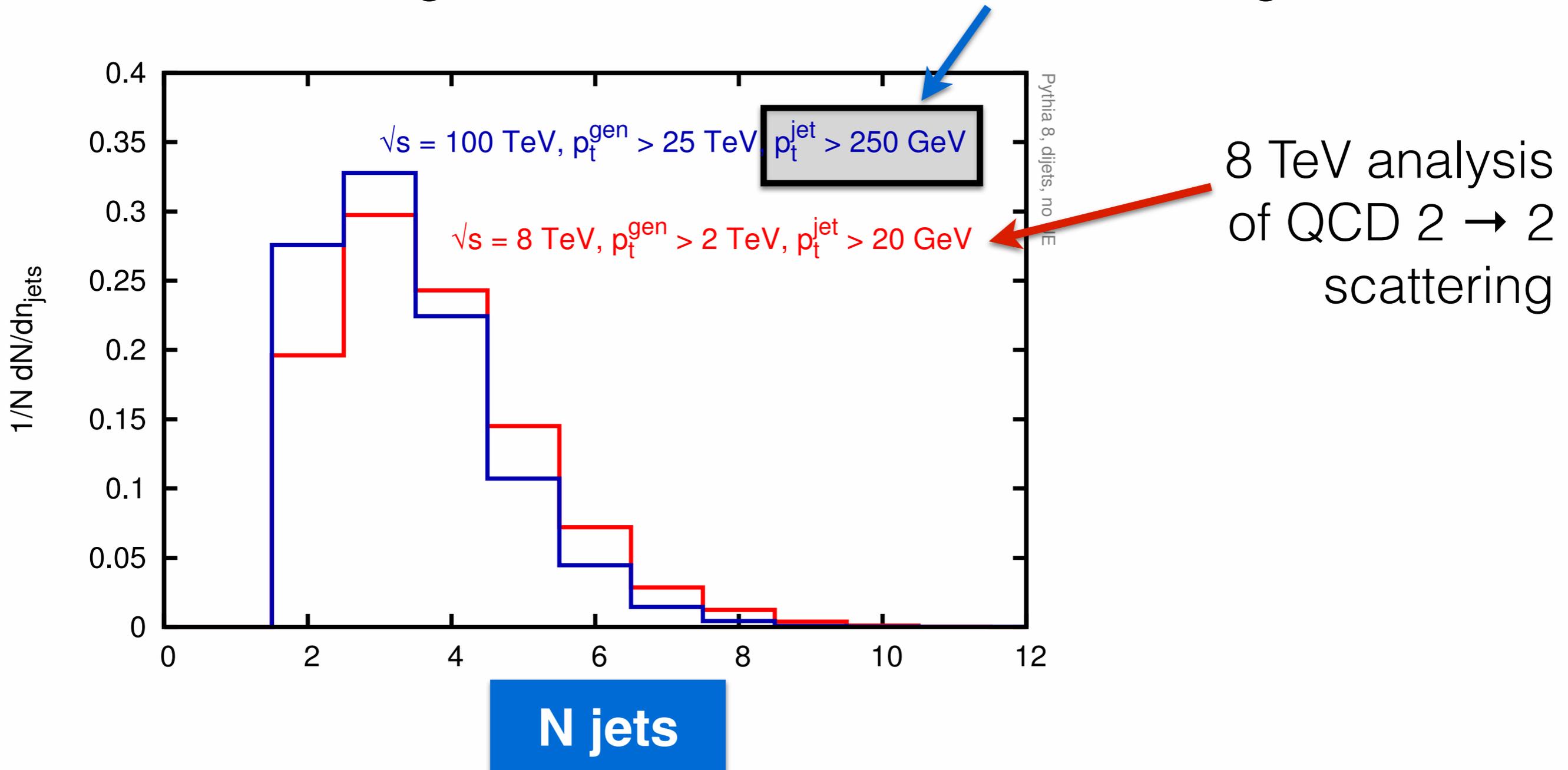
Count the jets

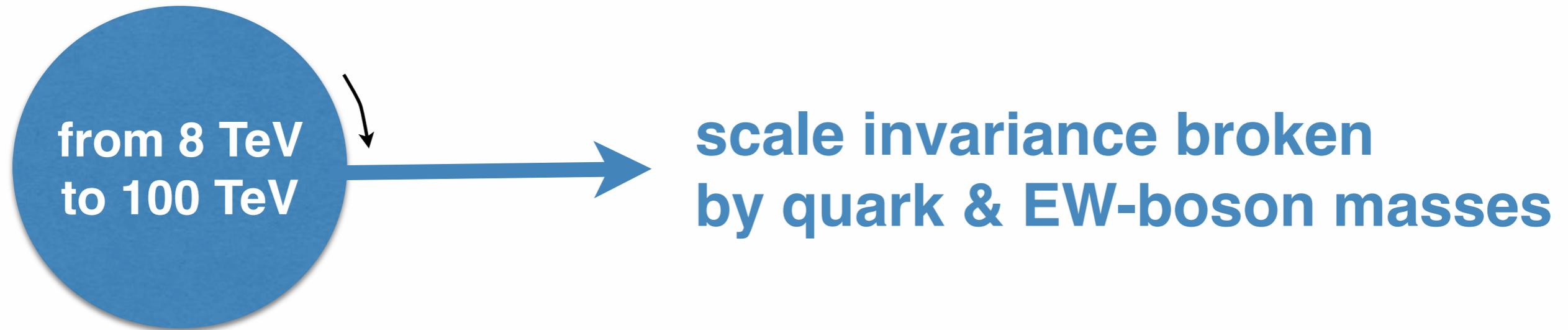
Scale invariance holds if **all ratios of scales kept fixed**



Scale invariance holds if **all ratios of scales kept fixed**

100 TeV, scaling also the **jet cut** \rightarrow **250 GeV**
gives a distribution much like the original





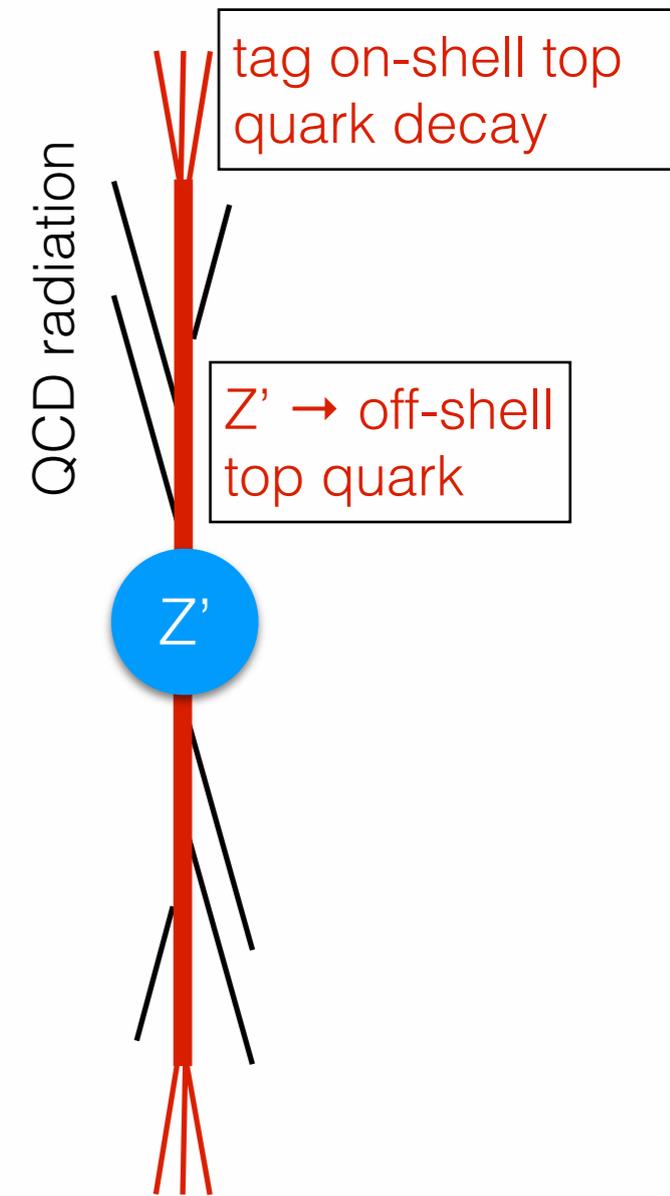
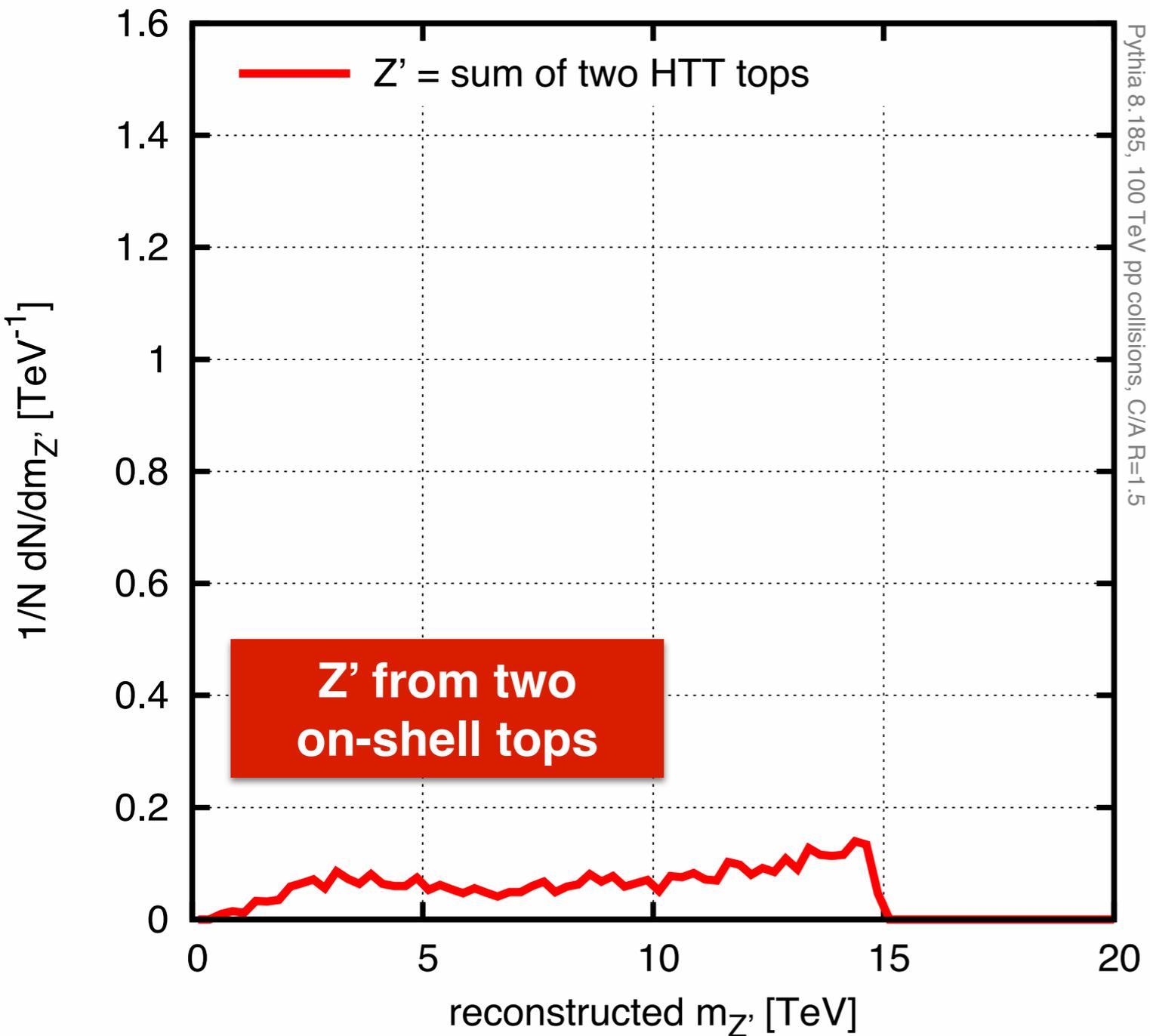
top quarks v. top jets

EW radiation in jets

The top quark as a light parton

[informal studies with Tilman Plehn]

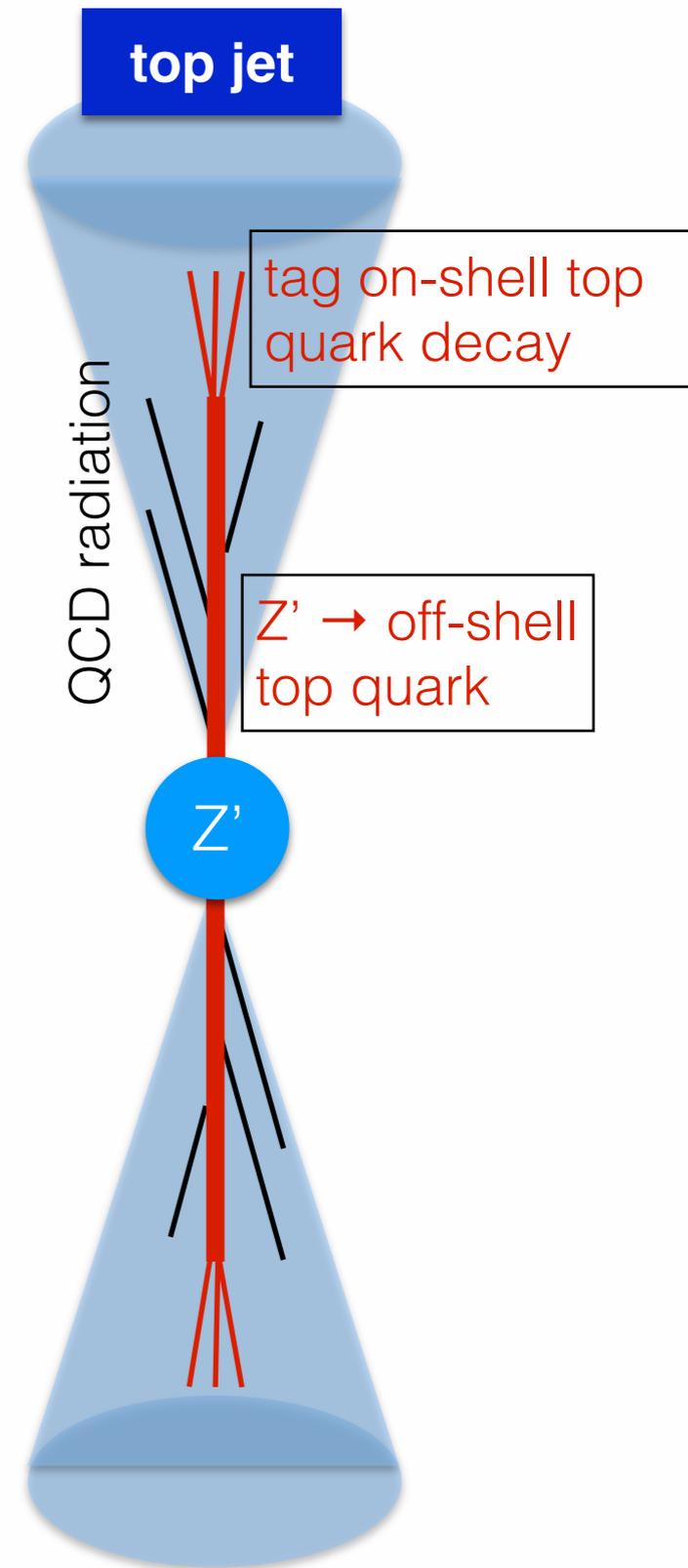
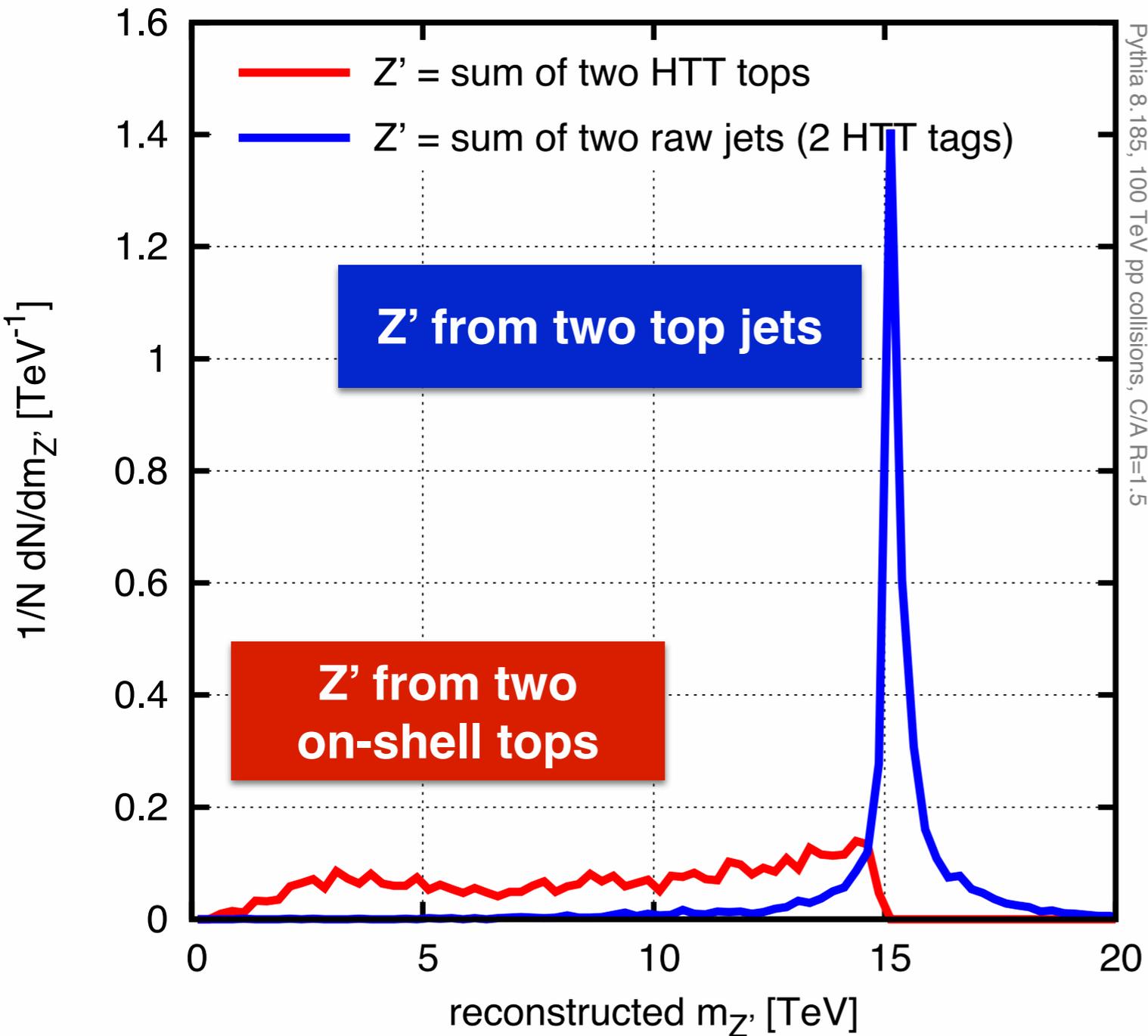
tag two hadr. tops (HEPTopTagger), reconstruct "tt" mass



The top quark as a light parton

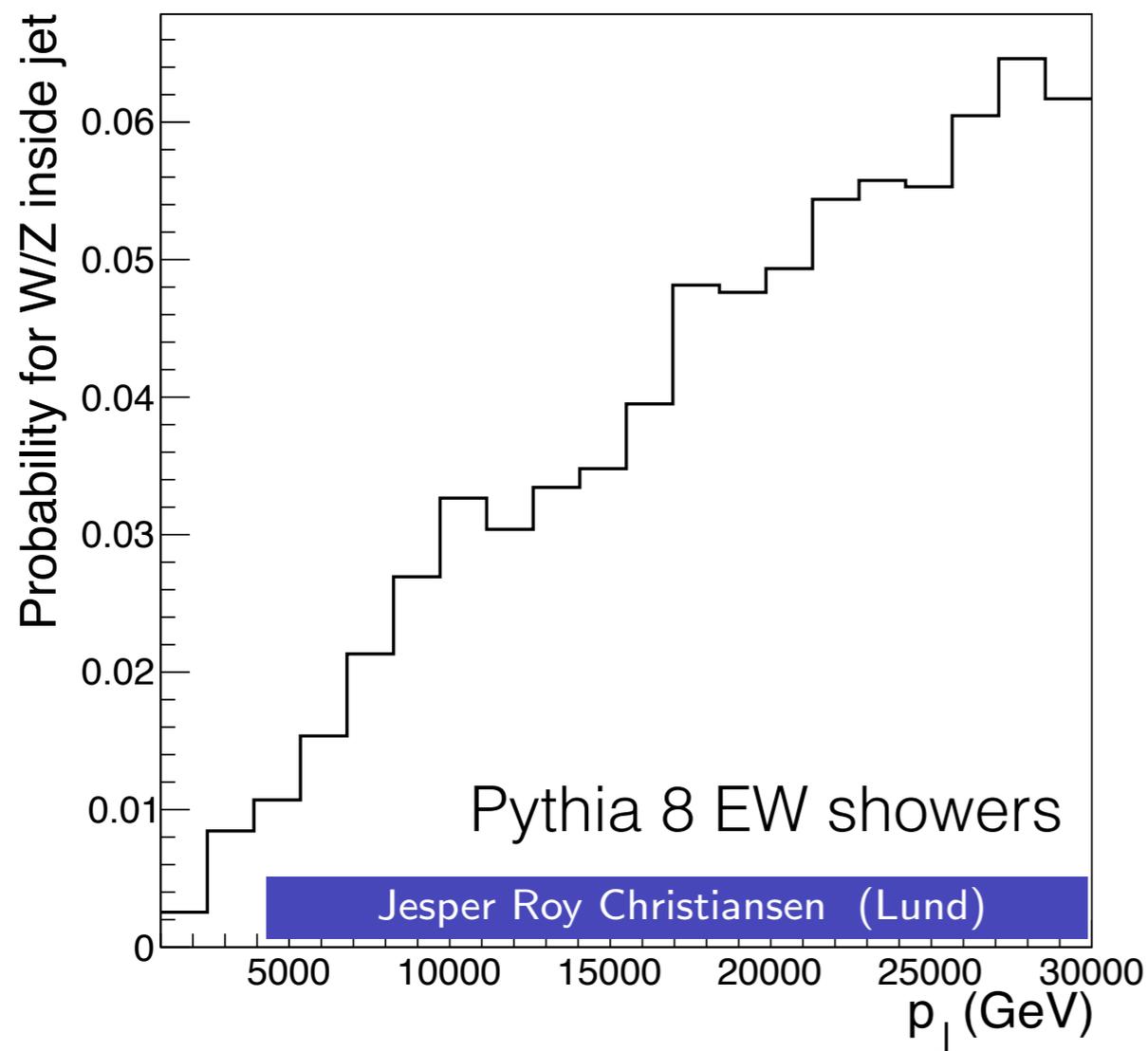
[informal studies with Tilman Plehn]

tag two hadr. tops (HEPTopTagger), reconstruct "tt" mass



EW radiation in jets

Prob. of Z/W in jet v. jet p_t



+ analogous plots at fixed order from MLM

Significant enhancement of W's and Z's in jets:

$$\sim \alpha_{EW} \ln^2 \frac{p_t}{M_W}$$

New, fun theory!

Experimentally, how different is this from bottom and charm in jet?

cf. 20% BR for $b \rightarrow c \nu l^{\pm}$ and $O(10\%)$ of 1 TeV gluon jets having b's inside

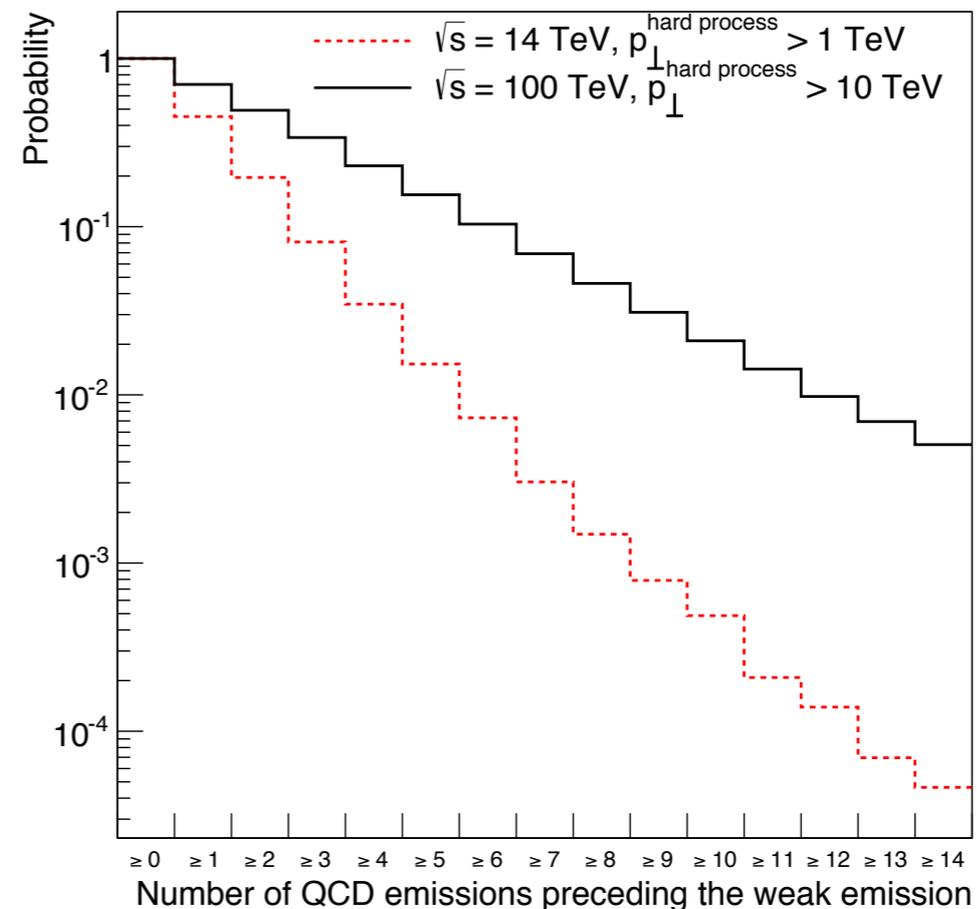
EW radiation in initial state

It polarizes the incoming partons
Can we make use of this?

How to simulate EW radiation correctly?

Competition between QCD and weak emissions

- Need to include up to 11 emissions, to only miss 1 %
⇒ Does this become problematic for merging techniques?

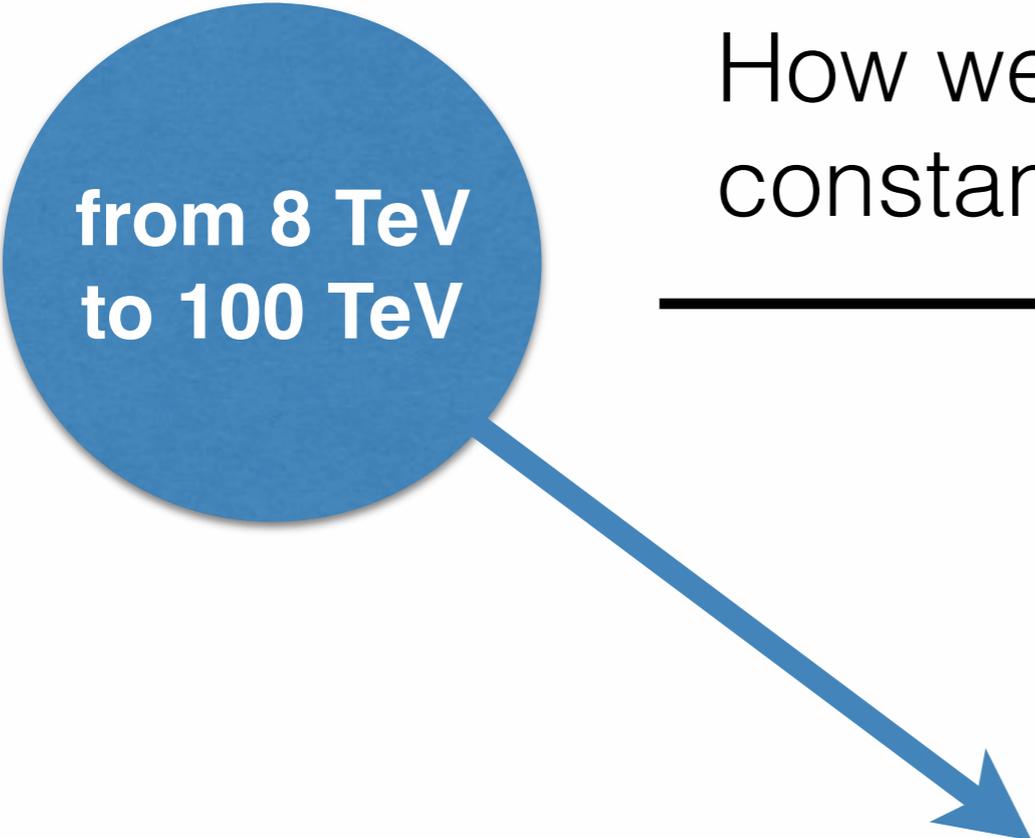


Some long-standing problems:

Why is QCD so poorly convergent at hadron colliders?

How well do we know our fundamental constants?

**from 8 TeV
to 100 TeV**



**problems that need solving for
LHC and for FHC**

Radically worse perturbative series at hadron colliders:

e^+e^- collisions: $R_{\text{hadrons}} \propto 1 + 0.32\alpha_s + 0.14\alpha_s^2 + \dots$

pp collisions: $\sigma_{gg \rightarrow H} \propto 1 + 9.8\alpha_s + 33\alpha_s^2 + ?$

C_A / C_F explains twice worse convergence

But convergence is 10–30 times worse

WHY?

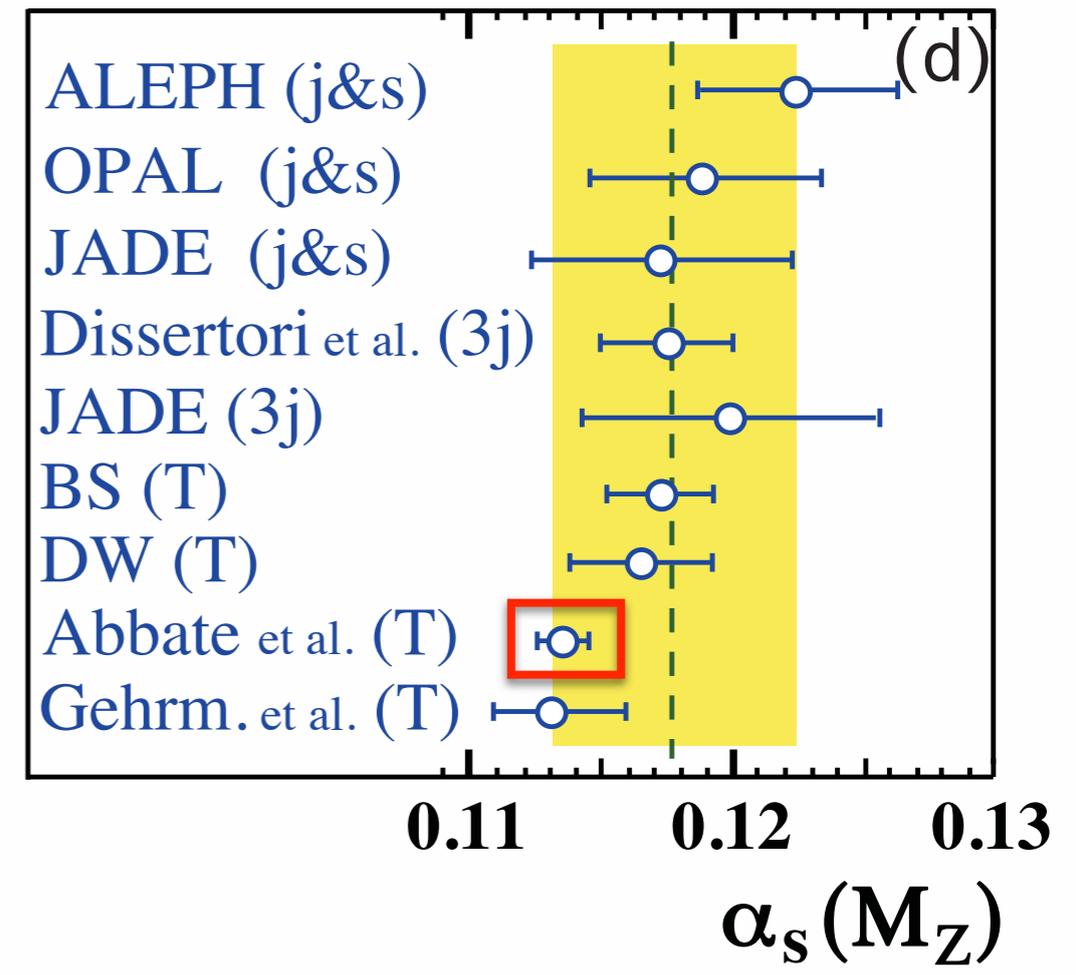
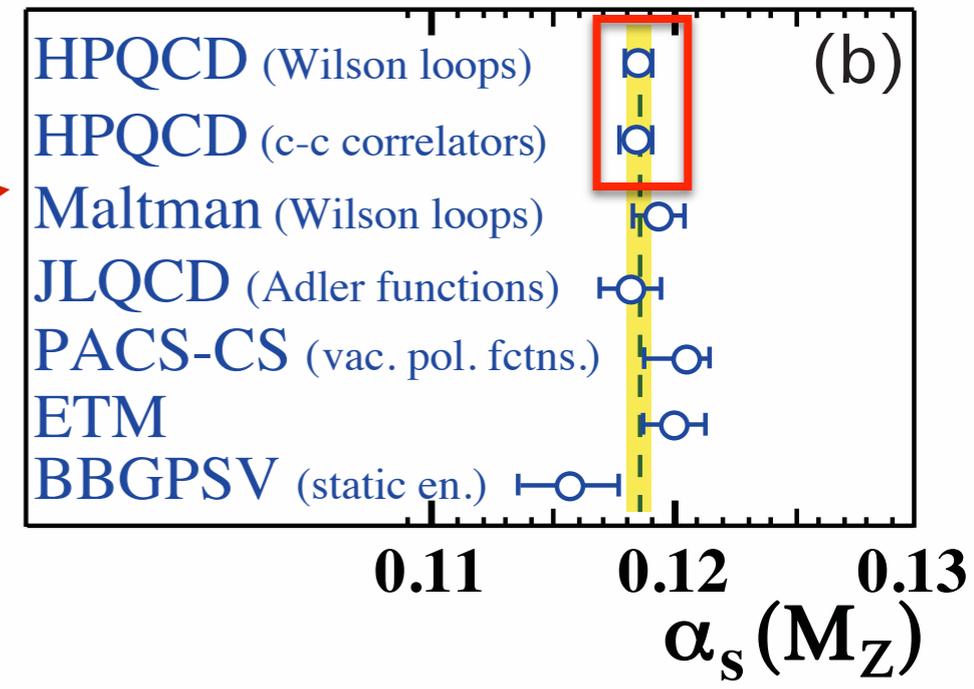
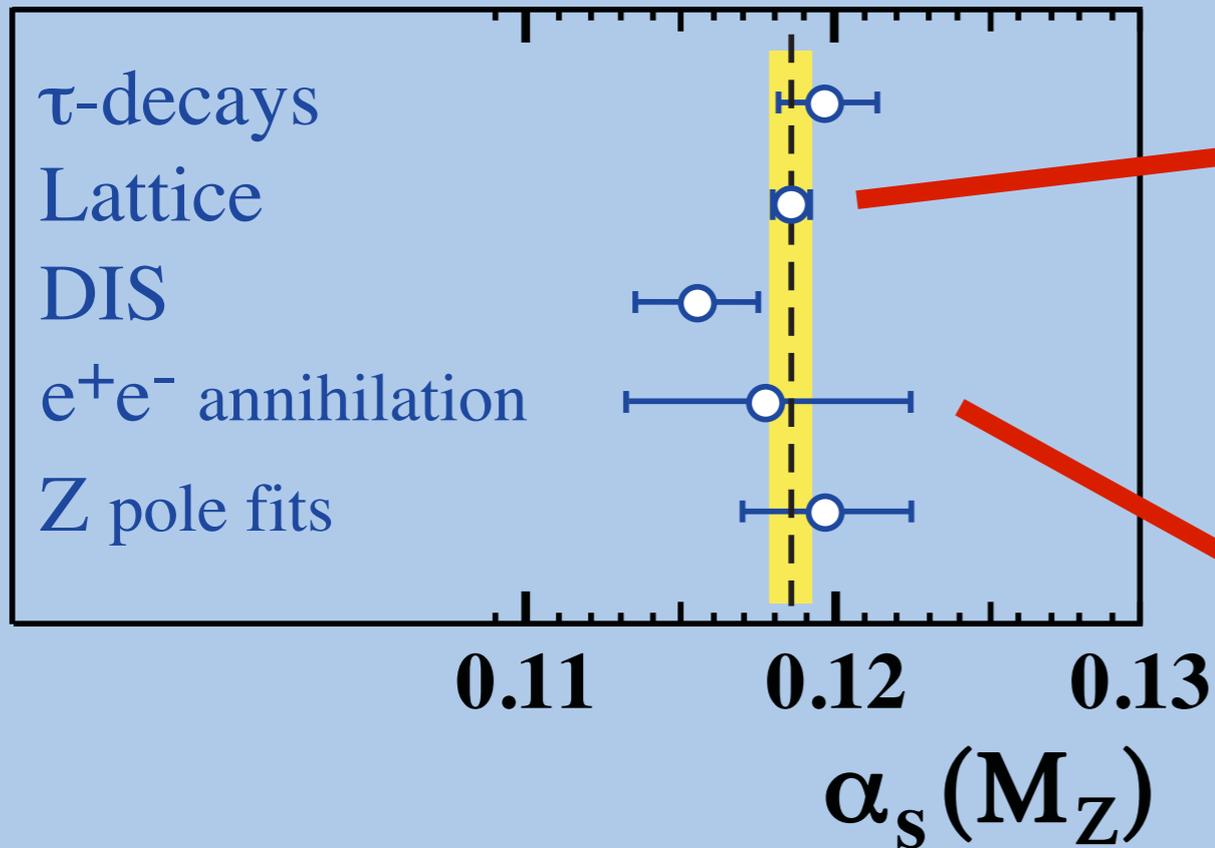
Strong Coupling Constant

PDG world average: $\alpha_s(M_Z) = 0.1184 \pm 0.0006$

w/o lattice inputs:
(~ choice by PDF4LHC) $\alpha_s(M_Z) = 0.1183 \pm 0.0012$

Uncertainty gets amplified in cross sections, e.g. $gg \rightarrow H$

$$\frac{\delta\sigma_{ggH}}{\sigma_{ggH}} \sim 3 \frac{\delta\alpha_s}{\alpha_s}$$



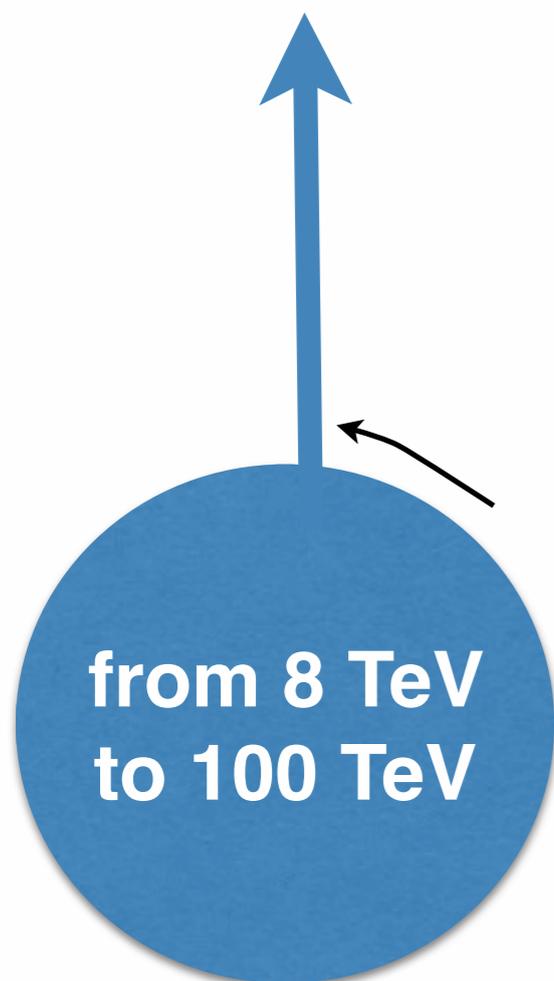
Different extractions quoting small uncertainties are not consistent

Thrust + SCET: 0.1135 ± 0.0010

Wilson loops: 0.1184 ± 0.0006

Differ at 4σ — how do we resolve this?

Collider Reach



Quick and dirty estimates of the reach of future colliders based on existing limits

with Andi Weiler

How soon will LHC@13TeV beat 8TeV searches?

What can high-lumi LHC (3000fb^{-1}) do compared to original LHC plan (300fb^{-1})?

What is the gain from a future 33/50/100/150 TeV collider?

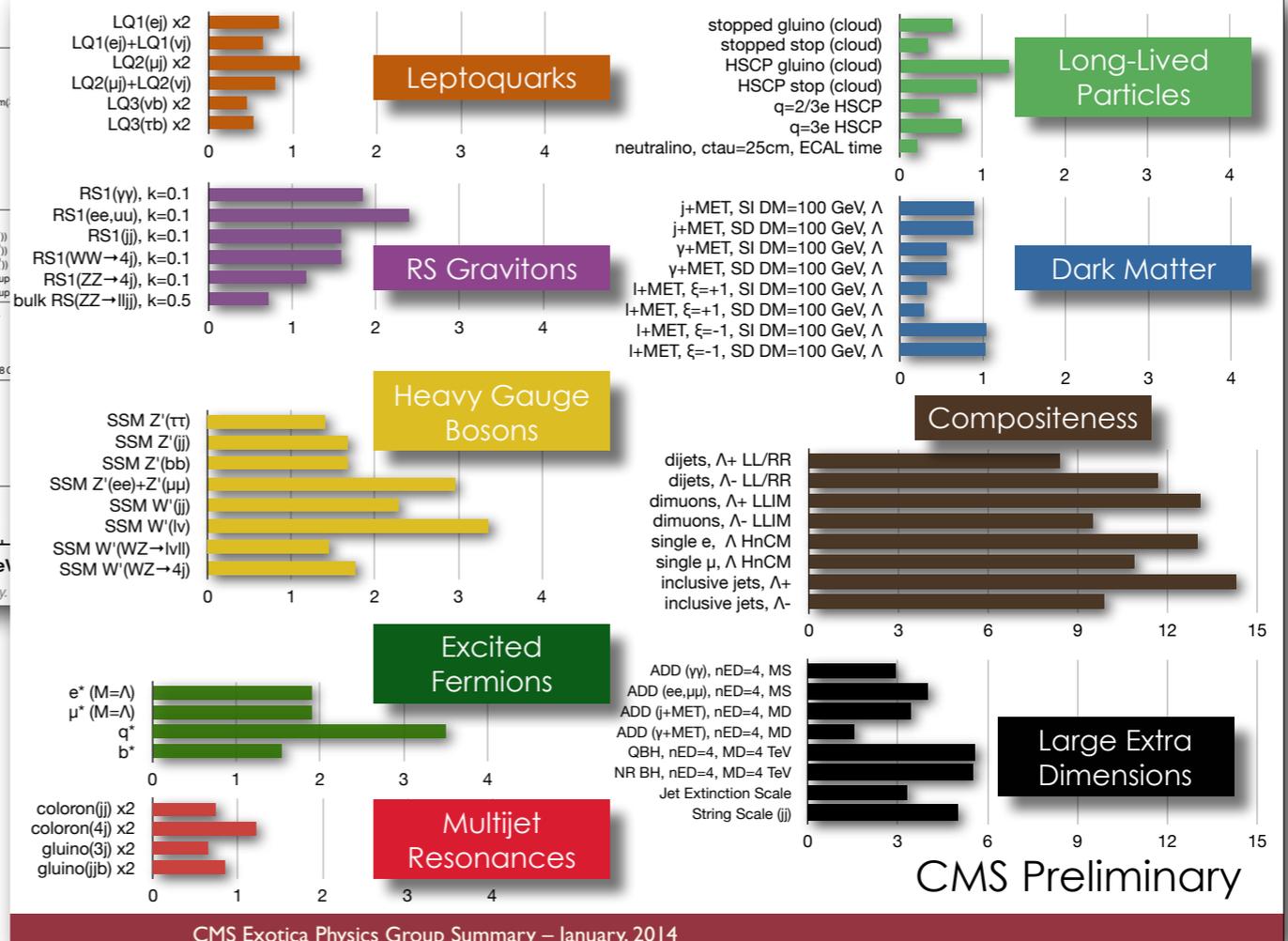
There are already many well-designed searches

ATLAS SUSY Searches* - 95% CL Lower Limits
 Status: SUSY 2013 ATLAS Preliminary
 $\int \mathcal{L} dt = (4.6 - 22.9) \text{ fb}^{-1}$ $\sqrt{s} = 7, 8 \text{ TeV}$

Model	e, μ, τ, γ	Jets	E_T^{miss}	$\int \mathcal{L} dt [\text{fb}^{-1}]$	Mass limit	Reference	
Inclusive Searches	MSUGRA/CMSSM	0	2-6 jets	Yes	20.3	\tilde{g}, \tilde{g} 1.7 TeV	ATLAS-CONF-2013-047
	MSUGRA/CMSSM	1 e, μ	3-6 jets	Yes	20.3	\tilde{g} 1.2 TeV	ATLAS-CONF-2013-062
	MSUGRA/CMSSM	0	7-10 jets	Yes	20.3	\tilde{g} 1.1 TeV	1308.1841
	$\tilde{q}\tilde{q}, \tilde{q} \rightarrow q\tilde{\chi}_1^0$	0	2-6 jets	Yes	20.3	\tilde{q} 740 GeV	ATLAS-CONF-2013-047
	$\tilde{g}\tilde{g}, \tilde{g} \rightarrow q\tilde{q}\tilde{\chi}_1^0$	0	2-6 jets	Yes	20.3	\tilde{g} 1.3 TeV	ATLAS-CONF-2013-047
	$\tilde{g}\tilde{g}, \tilde{g} \rightarrow q\tilde{q}\tilde{\chi}_1^0 + qqW^{\pm}\tilde{\chi}_1^0$	1 e, μ	3-6 jets	Yes	20.3	\tilde{g} 1.18 TeV	ATLAS-CONF-2013-062
	GMSB (\tilde{L} NLSP)	2 e, μ	0-3 jets	-	20.3	\tilde{g} 1.12 TeV	ATLAS-CONF-2013-089
	GMSB (\tilde{L} NLSP)	2 e, μ	2-4 jets	Yes	4.7	\tilde{g} 1.24 TeV	1208.4688
	GGM (bino NLSP)	1-2 τ	0-2 jets	Yes	20.7	\tilde{g} 1.4 TeV	ATLAS-CONF-2013-026
	GGM (wino NLSP)	2 γ	-	Yes	4.8	\tilde{g} 1.07 TeV	1209.0753
3 rd gen. squarks & gluons	$\tilde{g} \rightarrow b\tilde{b}^0$	0	3 b	Yes	20.1	\tilde{g} 1.2 TeV	$m(\tilde{\chi}_1^0) < 600 \text{ GeV}$
	$\tilde{g} \rightarrow t\tilde{t}^0$	0	7-10 jets	Yes	20.3	\tilde{g} 1.1 TeV	$m(\tilde{\chi}_1^0) < 350 \text{ GeV}$
	$\tilde{g} \rightarrow \tau\tilde{\tau}^0$	0-1 e, μ	3 b	Yes	20.1	\tilde{g} 1.34 TeV	$m(\tilde{\chi}_1^0) < 400 \text{ GeV}$
	$\tilde{g} \rightarrow b\tilde{t}_1^0$	0-1 e, μ	3 b	Yes	20.1	\tilde{g} 1.3 TeV	$m(\tilde{\chi}_1^0) < 300 \text{ GeV}$
	$b_1\tilde{b}_1, \tilde{b}_1 \rightarrow b\tilde{\chi}_1^0$	2 e, μ (SS)	0-3 b	Yes	20.7	b_1 100-620 GeV	$m(\tilde{\chi}_1^0) < 90 \text{ GeV}$
	$b_2\tilde{b}_2, \tilde{b}_2 \rightarrow b\tilde{\chi}_1^0$	2 e, μ (SS)	0-3 b	Yes	20.7	b_2 275-430 GeV	$m(\tilde{\chi}_1^0) = 2 m(\tilde{\chi}_1^0)$
	$\tilde{t}_1\tilde{t}_1$ (light), $\tilde{t}_1 \rightarrow b\tilde{\chi}_1^0$	1-2 e, μ	1-2 b	Yes	4.7	\tilde{t}_1 110-167 GeV	$m(\tilde{\chi}_1^0) = 55 \text{ GeV}$
	$\tilde{t}_1\tilde{t}_1$ (medium), $\tilde{t}_1 \rightarrow Wb\tilde{\chi}_1^0$	2 e, μ	0-2 jets	Yes	20.3	\tilde{t}_1 130-220 GeV	$m(\tilde{\chi}_1^0) = m(\tilde{\chi}_1^0) - m(W) - 50 \text{ GeV}, m(\tilde{\chi}_1^0) < m(\tilde{g})$
	$\tilde{t}_1\tilde{t}_1$ (heavy), $\tilde{t}_1 \rightarrow b\tilde{\chi}_1^0$	2 e, μ	2 jets	Yes	20.3	\tilde{t}_1 225-525 GeV	$m(\tilde{\chi}_1^0) < 200 \text{ GeV}, m(\tilde{\chi}_1^0) - m(\tilde{\chi}_1^0) = 5 \text{ GeV}$
	$\tilde{t}_1\tilde{t}_1$ (heavy), $\tilde{t}_1 \rightarrow t\tilde{\chi}_1^0$	1 e, μ	1 b	Yes	20.7	\tilde{t}_1 150-580 GeV	$m(\tilde{\chi}_1^0) = 0 \text{ GeV}$
EW direct	$\tilde{L}_L\tilde{L}_R, \tilde{L} \rightarrow \tilde{\chi}_1^0 \ell$	2 e, μ	0	Yes	20.3	\tilde{L} 85-315 GeV	$m(\tilde{\chi}_1^0) = 0 \text{ GeV}$
	$\tilde{L}_1\tilde{L}_1, \tilde{L}_1 \rightarrow \tilde{\chi}_1^0 \ell$	2 e, μ	0	Yes	20.3	\tilde{L}_1 125-450 GeV	$m(\tilde{\chi}_1^0) = 0 \text{ GeV}, m(\tilde{L}) = 0.5(m(\tilde{L}_1) + m(\tilde{\chi}_1^0))$
	$\tilde{L}_1\tilde{L}_1, \tilde{L}_1 \rightarrow \tilde{\chi}_1^0 \nu$	2 τ	-	Yes	20.7	\tilde{L}_1 180-330 GeV	$m(\tilde{\chi}_1^0) = 0 \text{ GeV}, m(\tilde{L}) = 0.5(m(\tilde{L}_1) + m(\tilde{\chi}_1^0))$
	$\tilde{L}_1\tilde{L}_1, \tilde{L}_1 \rightarrow \tilde{\chi}_1^0 \nu$	3 e, μ	0	Yes	20.7	\tilde{L}_1 315 GeV	$m(\tilde{\chi}_1^0) = m(\tilde{\chi}_1^0), m(\tilde{L}_1) = 0, \text{ sleptons decouple}$
	$\tilde{L}_1\tilde{L}_1, \tilde{L}_1 \rightarrow W\tilde{\chi}_1^0 Z$	3 e, μ	0	Yes	20.7	\tilde{L}_1 315 GeV	$m(\tilde{\chi}_1^0) = m(\tilde{\chi}_1^0), m(\tilde{L}_1) = 0, \text{ sleptons decouple}$
	$\tilde{L}_1\tilde{L}_1, \tilde{L}_1 \rightarrow W\tilde{\chi}_1^0 h$	1 e, μ	2 b	Yes	20.3	\tilde{L}_1 285 GeV	$m(\tilde{\chi}_1^0) = m(\tilde{\chi}_1^0), m(\tilde{L}_1) = 0, \text{ sleptons decouple}$
	Direct $\tilde{\chi}_1^0\tilde{\chi}_1^0$ prod., long-lived $\tilde{\chi}_1^0$	Disapp. trk	1 jet	Yes	20.3	$\tilde{\chi}_1^0$ 270 GeV	$m(\tilde{\chi}_1^0) - m(\tilde{\chi}_1^0) = 160 \text{ MeV}, \tau(\tilde{\chi}_1^0) = 0.2 \text{ ns}$
	Stable, stopped \tilde{g} -hadron	0	1-5 jets	Yes	22.9	\tilde{g} 832 GeV	$m(\tilde{\chi}_1^0) = 100 \text{ GeV}, 10 \mu\text{s} < \tau(\tilde{g}) < 1000 \text{ s}$
	GMSB, stable $\tilde{\tau}, \tilde{\chi}_1^0 \rightarrow \tau(e, \mu) + \tau$	1-2 μ	-	-	15.9	$\tilde{\tau}$ 475 GeV	$10^{-4} < \text{BR}(\tilde{\tau}) < 50$
	GMSB, $\tilde{\chi}_1^0 \rightarrow \gamma G$, long-lived $\tilde{\chi}_1^0$	2 γ	-	-	4.7	$\tilde{\chi}_1^0$ 230 GeV	$0.4 < \tau(\tilde{\chi}_1^0) < 2 \text{ ns}$
RPV	$\tilde{q}\tilde{q}, \tilde{\chi}_1^0 \rightarrow q\tilde{q}\mu$ (RPV)	1 μ , displ. vtx	-	-	20.3	\tilde{q} 1.0 TeV	$1.5 < c\tau < 156 \text{ mm}, \text{BR}(\mu) = 1, m(\tilde{\chi}_1^0) = 108 \text{ GeV}$
	LFV $pp \rightarrow \tilde{\nu}_e + X, \tilde{\nu}_e \rightarrow e + \mu$	2 e, μ	-	-	4.6	$\tilde{\nu}_e$ 1.61 TeV	$A_{131} = 0.10, A_{132} = 0.05$
	LFV $pp \rightarrow \tilde{\nu}_e + X, \tilde{\nu}_e \rightarrow e(\mu) + \tau$	1 $e, \mu + \tau$	-	-	4.6	$\tilde{\nu}_e$ 1.1 TeV	$A_{131} = 0.10, A_{132(133)} = 0.05$
	Bilinear RPV CMSSM	1 e, μ	7 jets	Yes	4.7	\tilde{g}, \tilde{g} 1.2 TeV	$m(\tilde{g}) = m(\tilde{g}), c\tau_{\text{LSP}} < 1 \text{ mm}$
	$\tilde{\chi}_1^0\tilde{\chi}_1^0, \tilde{\chi}_1^0 \rightarrow W\tilde{\chi}_1^0, \tilde{\chi}_1^0 \rightarrow ee\nu_e, e\mu\nu_e$	4 e, μ	-	-	20.7	$\tilde{\chi}_1^0$ 760 GeV	$m(\tilde{\chi}_1^0) > 300 \text{ GeV}, A_{131} > 0$
	$\tilde{\chi}_1^0\tilde{\chi}_1^0, \tilde{\chi}_1^0 \rightarrow W\tilde{\chi}_1^0, \tilde{\chi}_1^0 \rightarrow \tau\nu_e, e\tau\nu_e$	3 $e, \mu + \tau$	-	-	20.7	$\tilde{\chi}_1^0$ 350 GeV	$m(\tilde{\chi}_1^0) > 80 \text{ GeV}, A_{131} > 0$
	$\tilde{g} \rightarrow q\tilde{q}$	0	6-7 jets	-	20.3	\tilde{g} 916 GeV	$\text{BR}(\tau) = \text{BR}(\mu) = \text{BR}(c) = 0\%$
	$\tilde{g} \rightarrow \tilde{t}_1 t, \tilde{t}_1 \rightarrow b\tilde{s}$	2 e, μ (SS)	0-3 b	Yes	20.7	\tilde{g} 880 GeV	
	Scalar gluon pair, $sgluon \rightarrow q\tilde{q}$	0	4 jets	-	4.6	sgluon 100-287 GeV	incl. limit from 1110.2693
	Scalar gluon pair, $sgluon \rightarrow t\tilde{t}$	2 e, μ (SS)	1 b	Yes	14.3	sgluon 800 GeV	
WIMP interaction (D5, Dirac χ)	0	mono-jet	Yes	10.5	\tilde{L}^* scale 704 GeV	$m(\chi) < 80 \text{ GeV}$, limit of $\sim 687 \text{ GeV}$ for D8	

Legend: $\sqrt{s} = 7 \text{ TeV}$ full data (blue), $\sqrt{s} = 8 \text{ TeV}$ partial data (green), $\sqrt{s} = 8 \text{ TeV}$ full data (red)

*Only a selection of the available mass limits on new states or phenomena is shown. All limits quoted are observed minus 1σ theoretical signal cross section uncertainty.



How do we leverage that experience to guesstimate future reaches?

A rough way of doing it

Suppose ATLAS/CMS are currently sensitive to gluinos of 1250 GeV (95% CL_s , 8 TeV, 20 fb⁻¹)



Work out how many signal events that corresponds to



Find out for what gluino mass you would get the same number of signal events at 14 TeV with 300 fb⁻¹ (assume # of background events scales same way)

What we're discussing is solution of the following equation for M_{high}

$$\frac{N_{\text{signal-events}}(M_{\text{high}}^2, 14 \text{ TeV}, \text{Lumi})}{N_{\text{signal-events}}(M_{\text{low}}^2, 8 \text{ TeV}, 19 \text{ fb}^{-1})} = 1$$

Many complications (e.g. coupling constants & other prefactors) mostly cancel in the ratio.

Dependence on M and on \sqrt{s} mostly comes about through parton distribution functions (PDFs) & simple dimensions.

Instead of cross section ratio, use **parton luminosity ratio**

Assume dominance of a single partonic scattering channel, ij (you have to know enough physics to figure out which is most appropriate).

Equation we solve to find M_{high} is then

$$\frac{\mathcal{L}_{ij}(M_{\text{high}}^2, s_{\text{high}})}{\mathcal{L}_{ij}(M_{\text{low}}^2, s_{\text{low}})} \times \frac{\text{lumi}_{\text{high}}}{\text{lumi}_{\text{low}}} = \frac{M_{\text{high}}^2}{M_{\text{low}}^2}$$

The tools we use for this are
LHAPDF and HOPPET
most plots with MSTW2008 NNLO PDFs

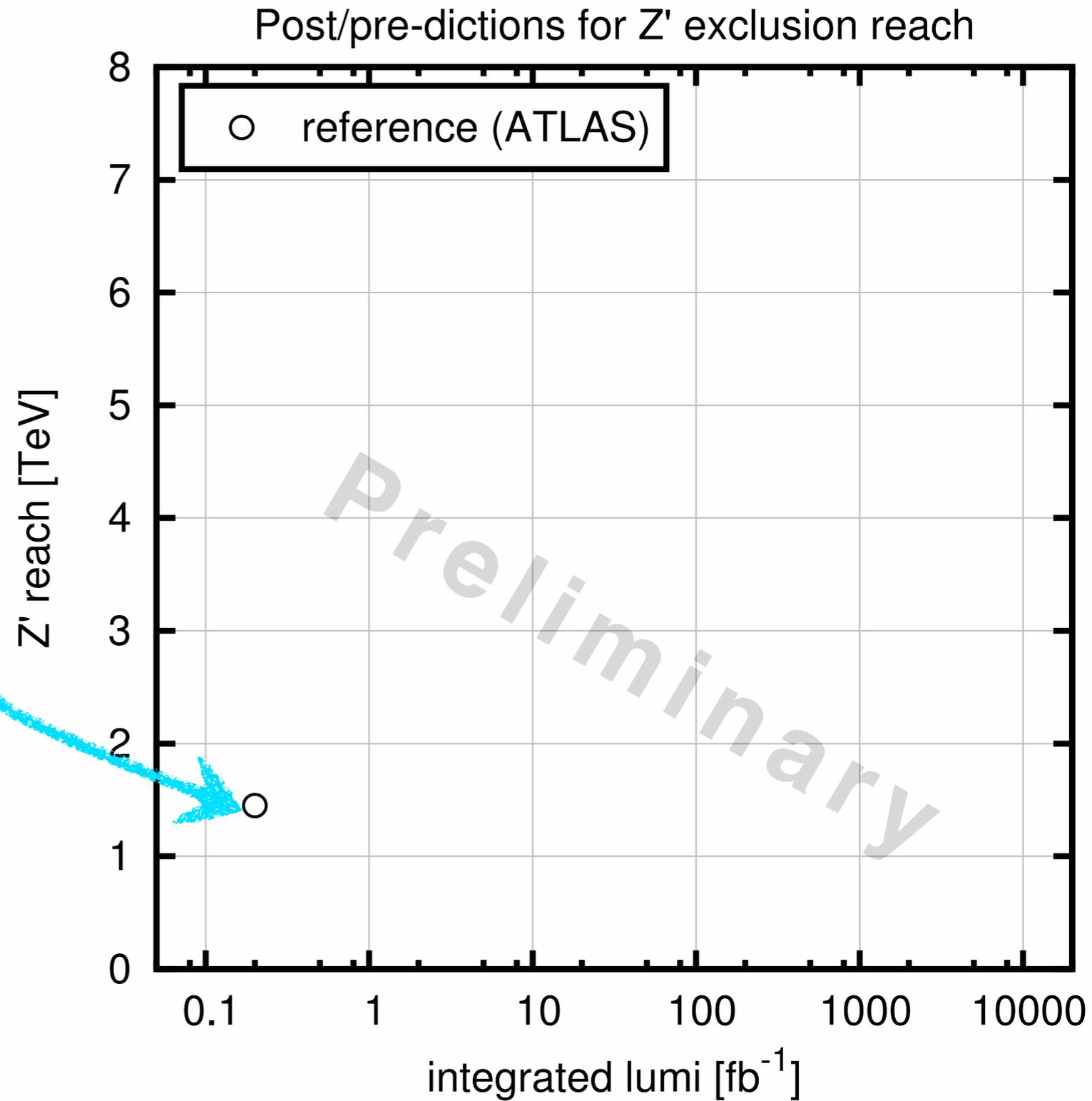
$$\mathcal{L}_{ij}(M^2, s) = \int_{\tau}^1 \frac{dx}{x} x f_i(x, M^2) \frac{\tau}{x} f_j\left(\frac{\tau}{x}, M^2\right) \quad \tau \equiv \frac{M^2}{s}$$

i & j parton

Does it work?

Try a Z' search. Take a baseline analysis:

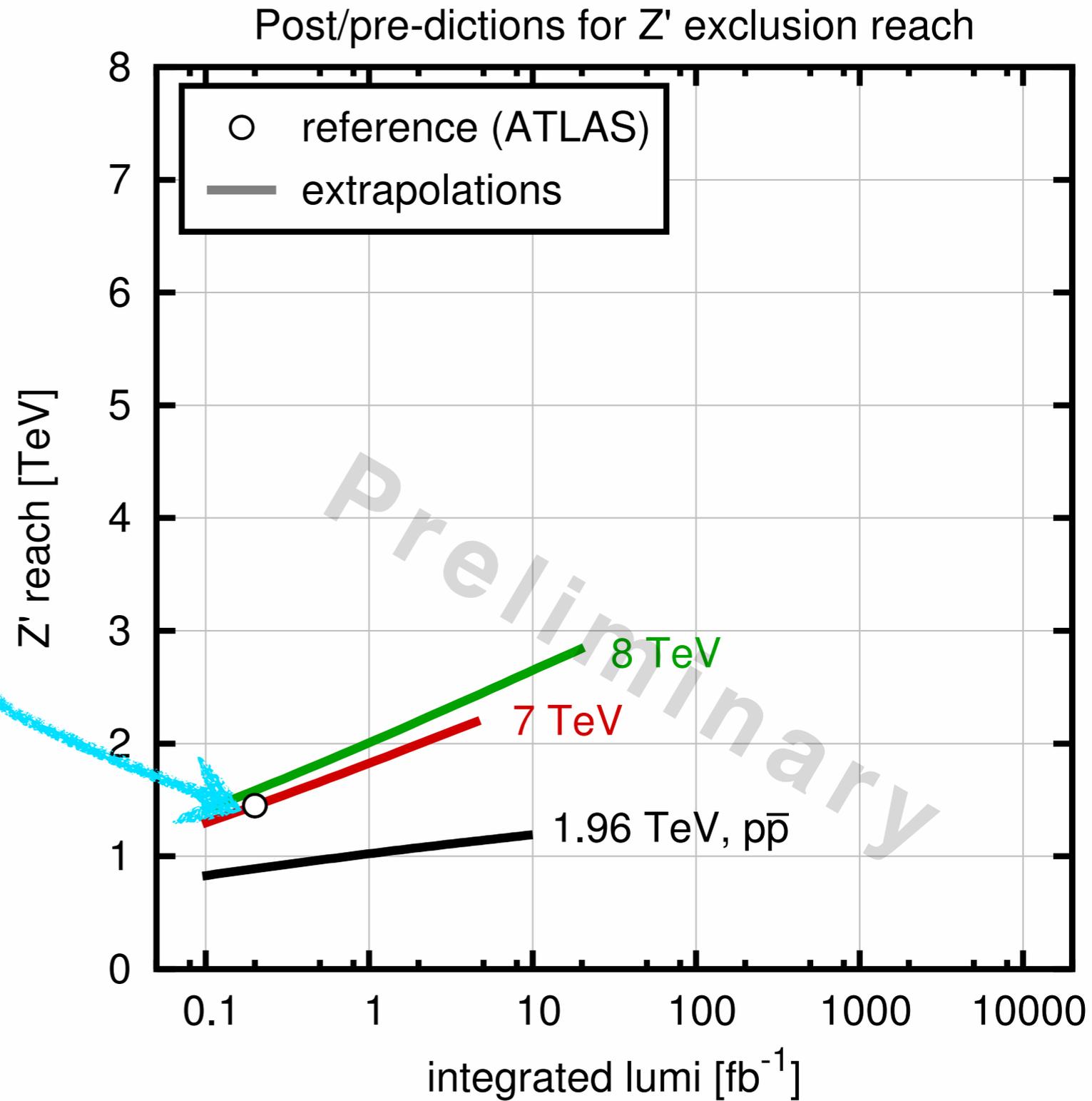
ATLAS,
0.2 fb⁻¹ @ 7 TeV
excludes M < 1450 GeV



Try a Z' search. Take a baseline analysis:

ATLAS,
 0.2 fb^{-1} @ 7 TeV
excludes $M < 1450 \text{ GeV}$

“Predict” exclusions
at other lumis &
energies (assume $q\bar{q}$)

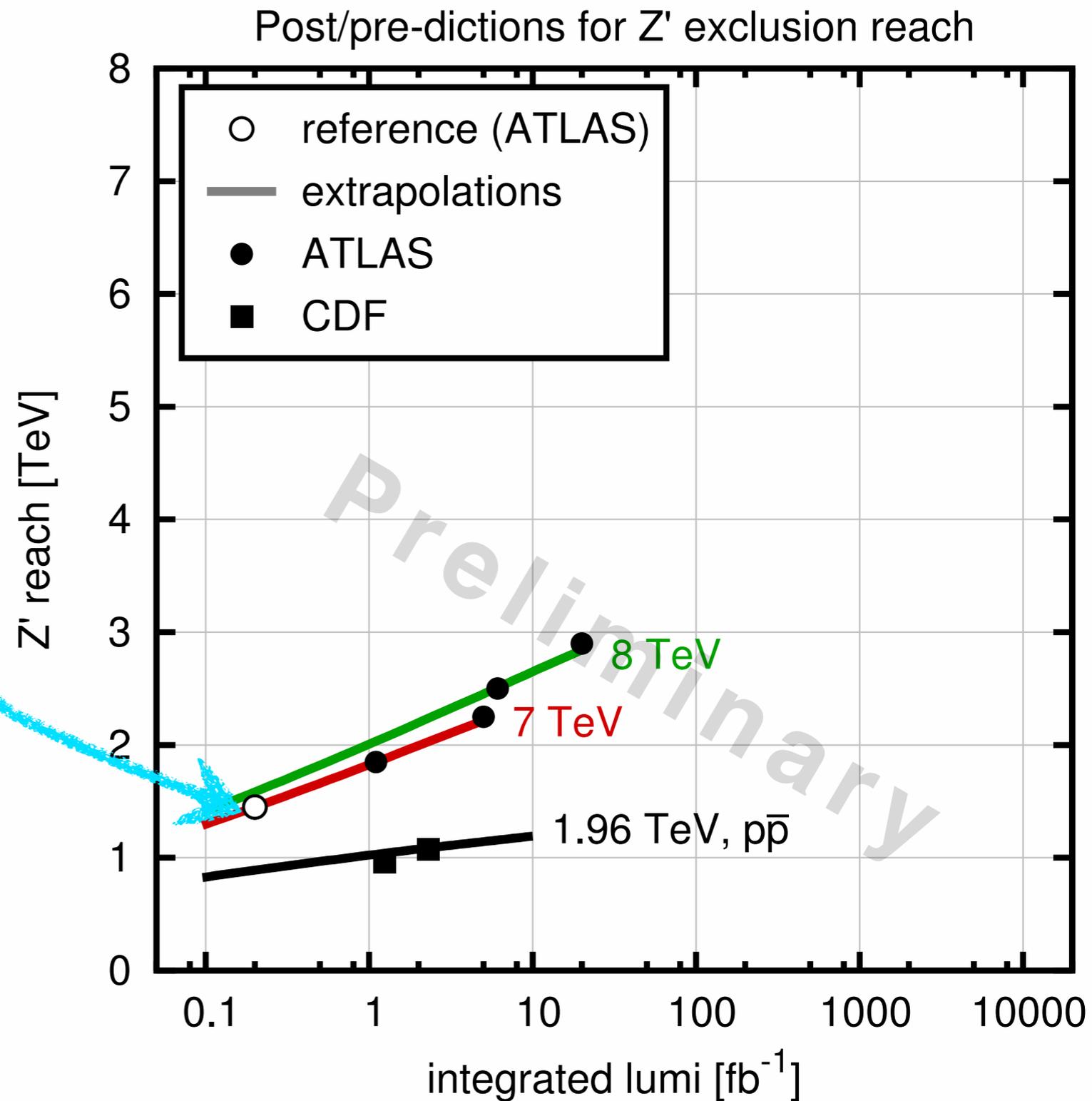


Try a Z' search. Take a baseline analysis:

ATLAS,
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“Predict” exclusions
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Compare to actual
exclusions

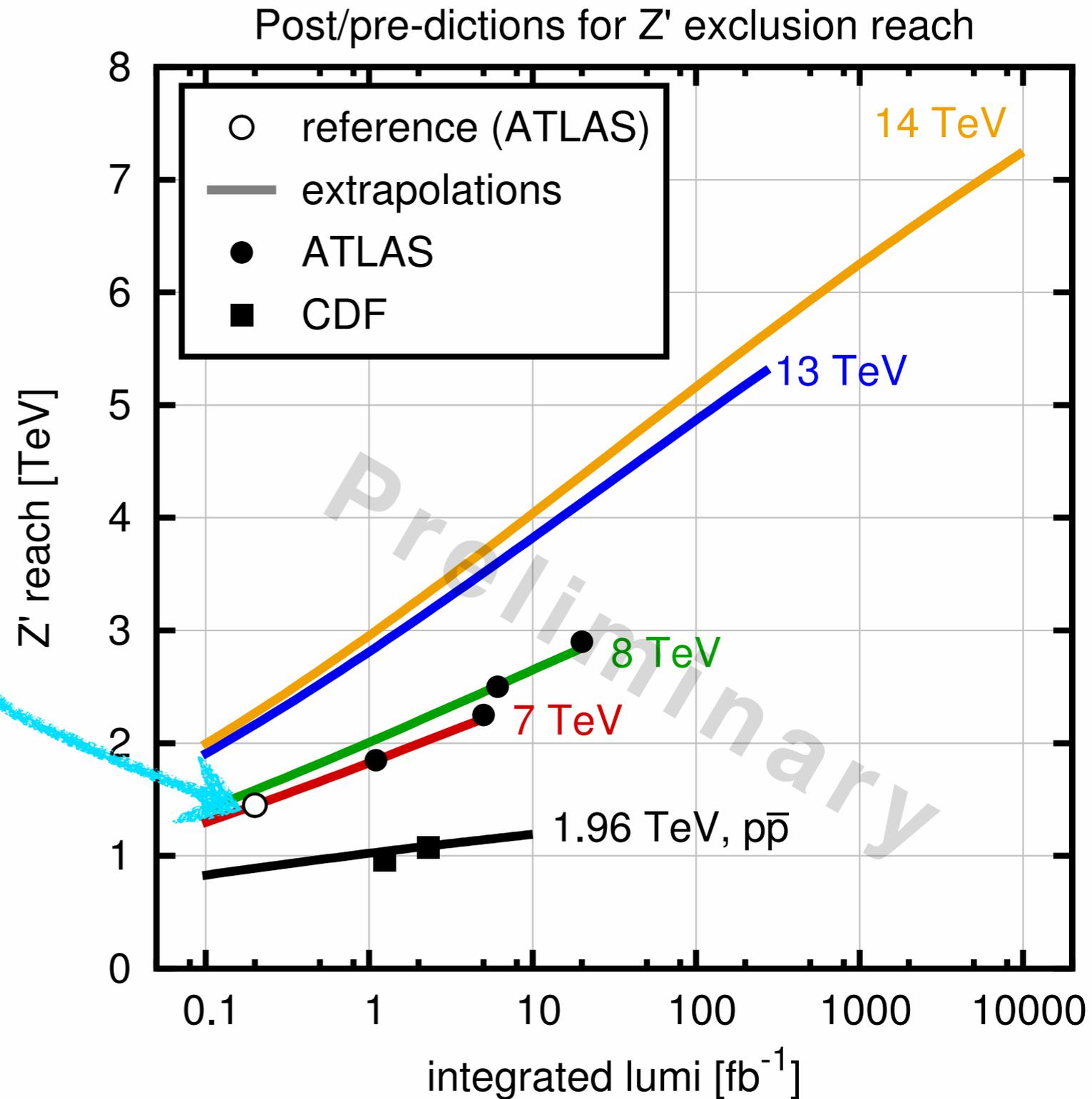


Try a Z' search. Take a baseline analysis:

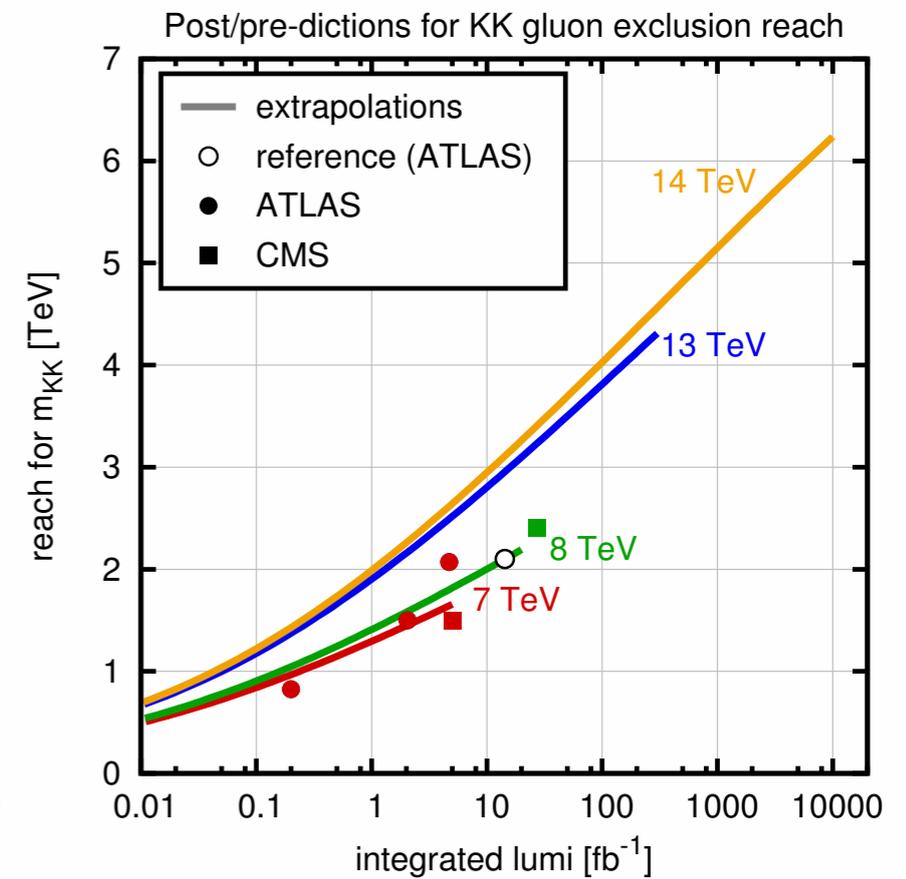
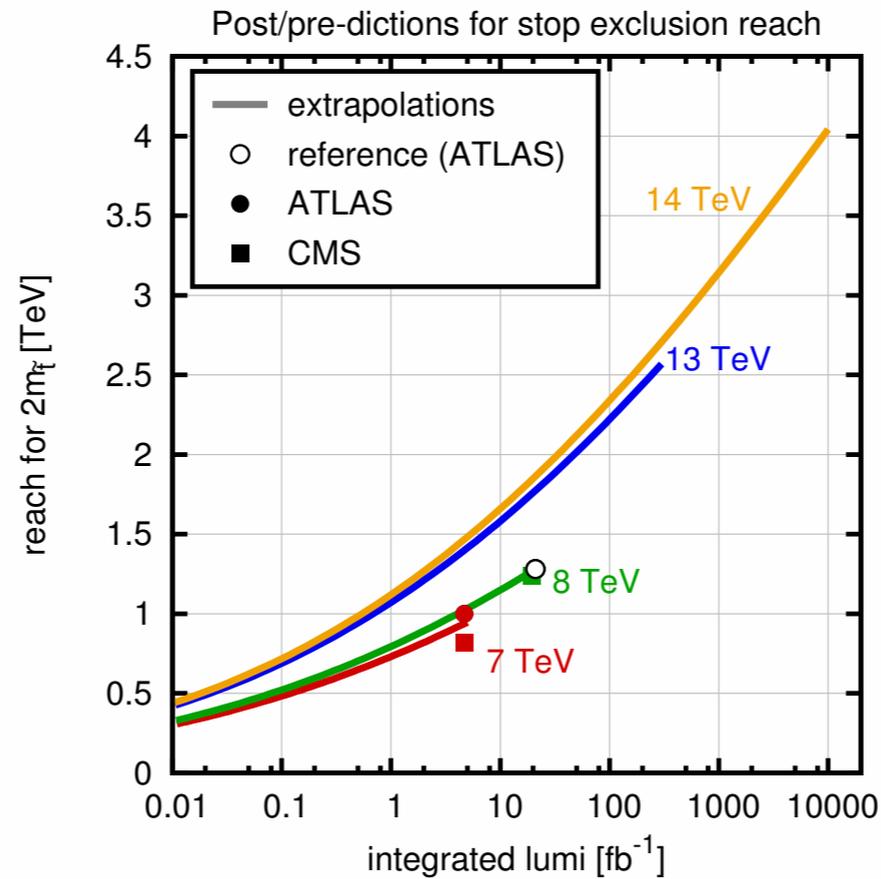
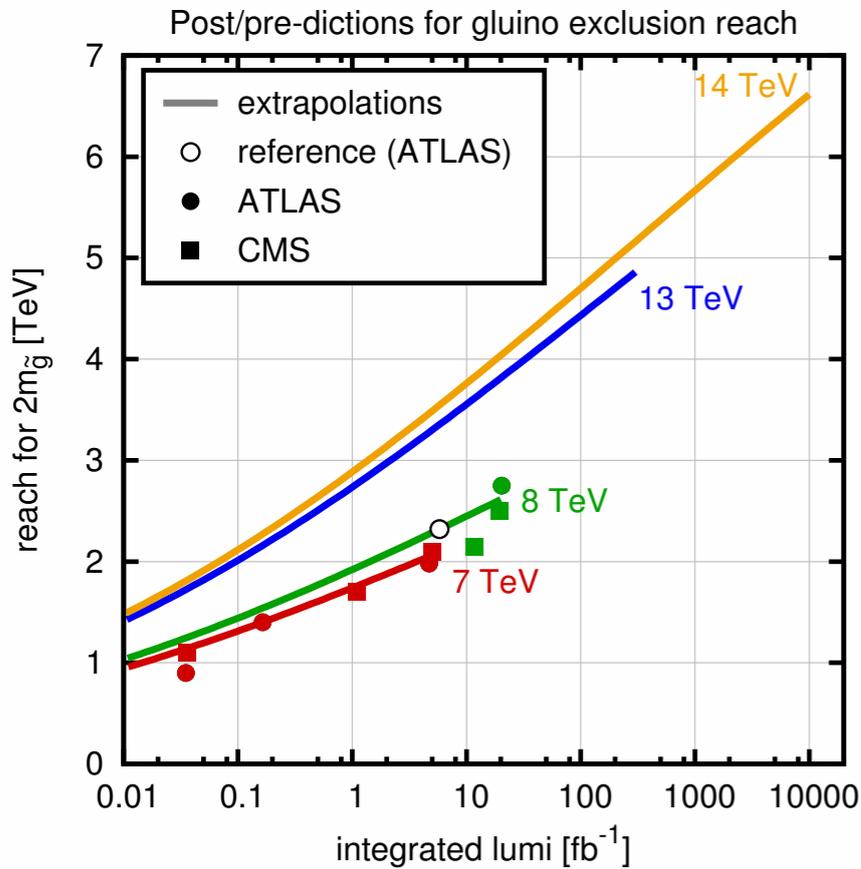
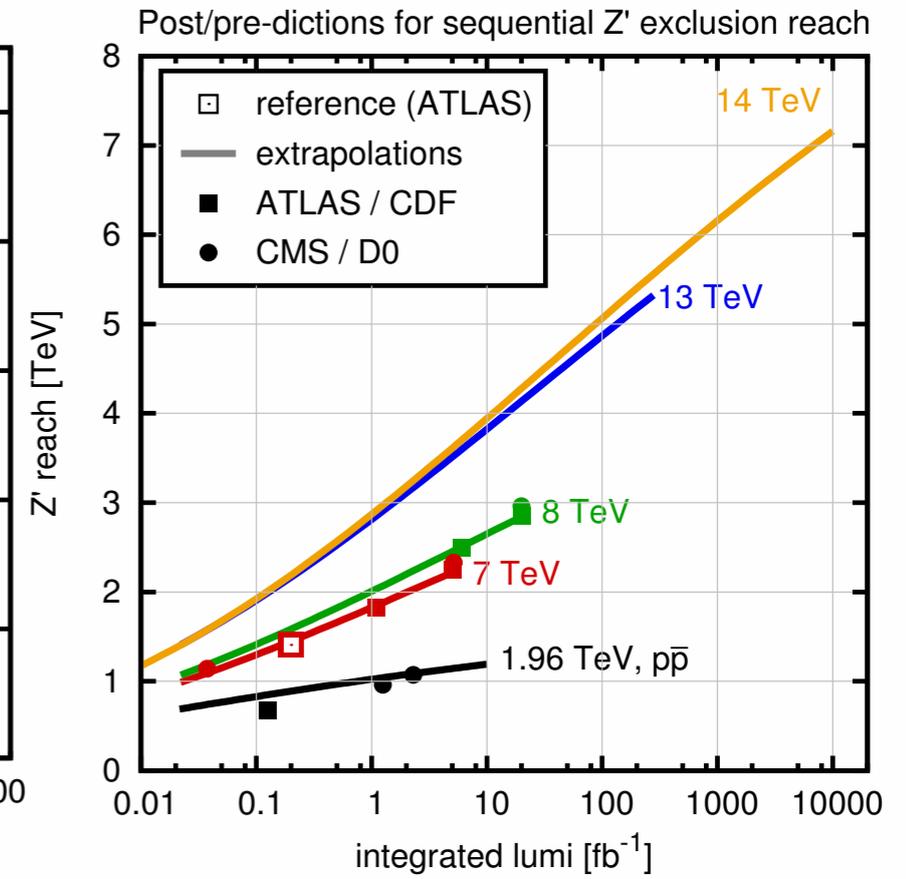
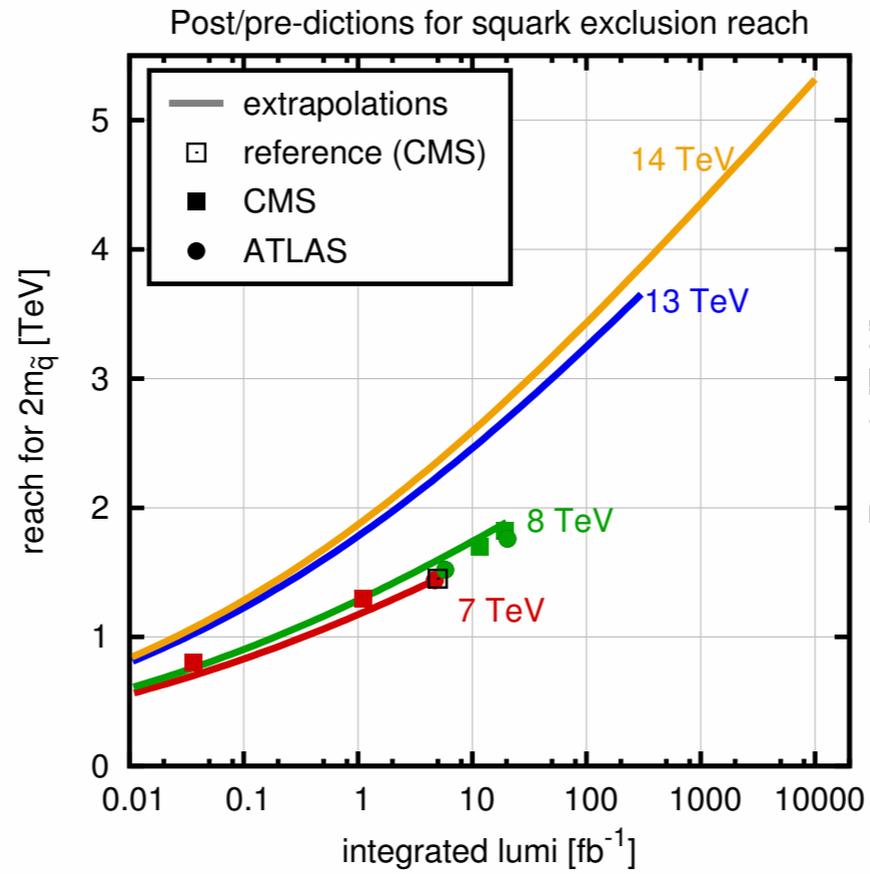
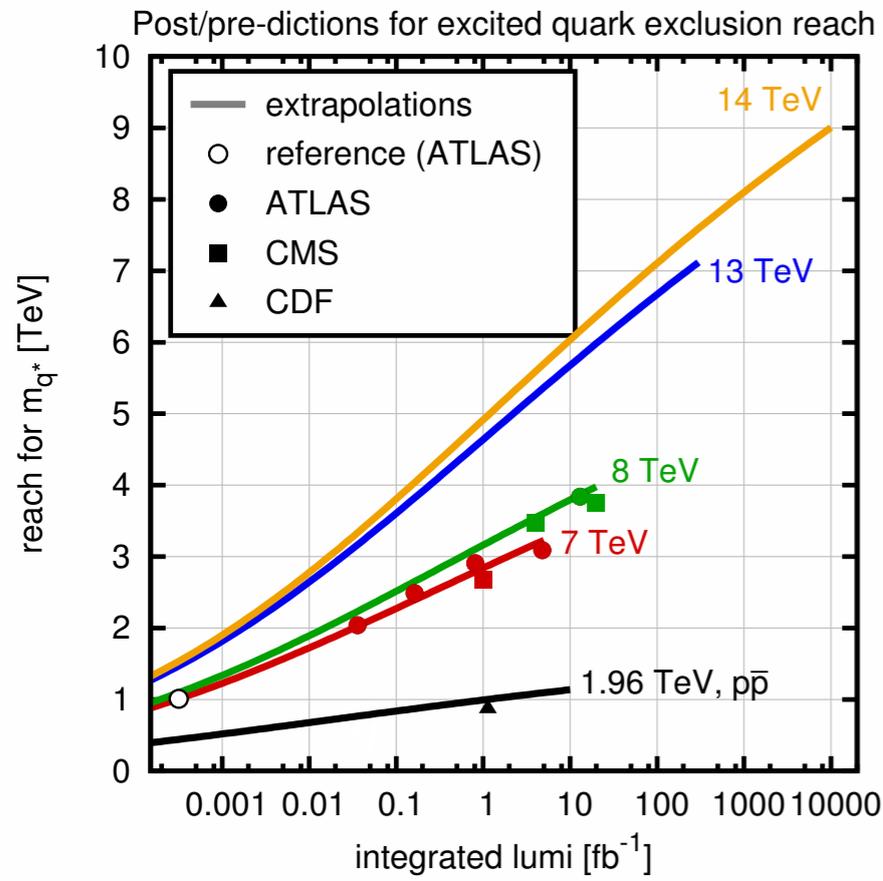
ATLAS,
 0.2 fb^{-1} @ 7 TeV
excludes $M < 1450 \text{ GeV}$

“Predict” exclusions
at other lumis &
energies (assume $q\bar{q}$)

Compare to actual
exclusions



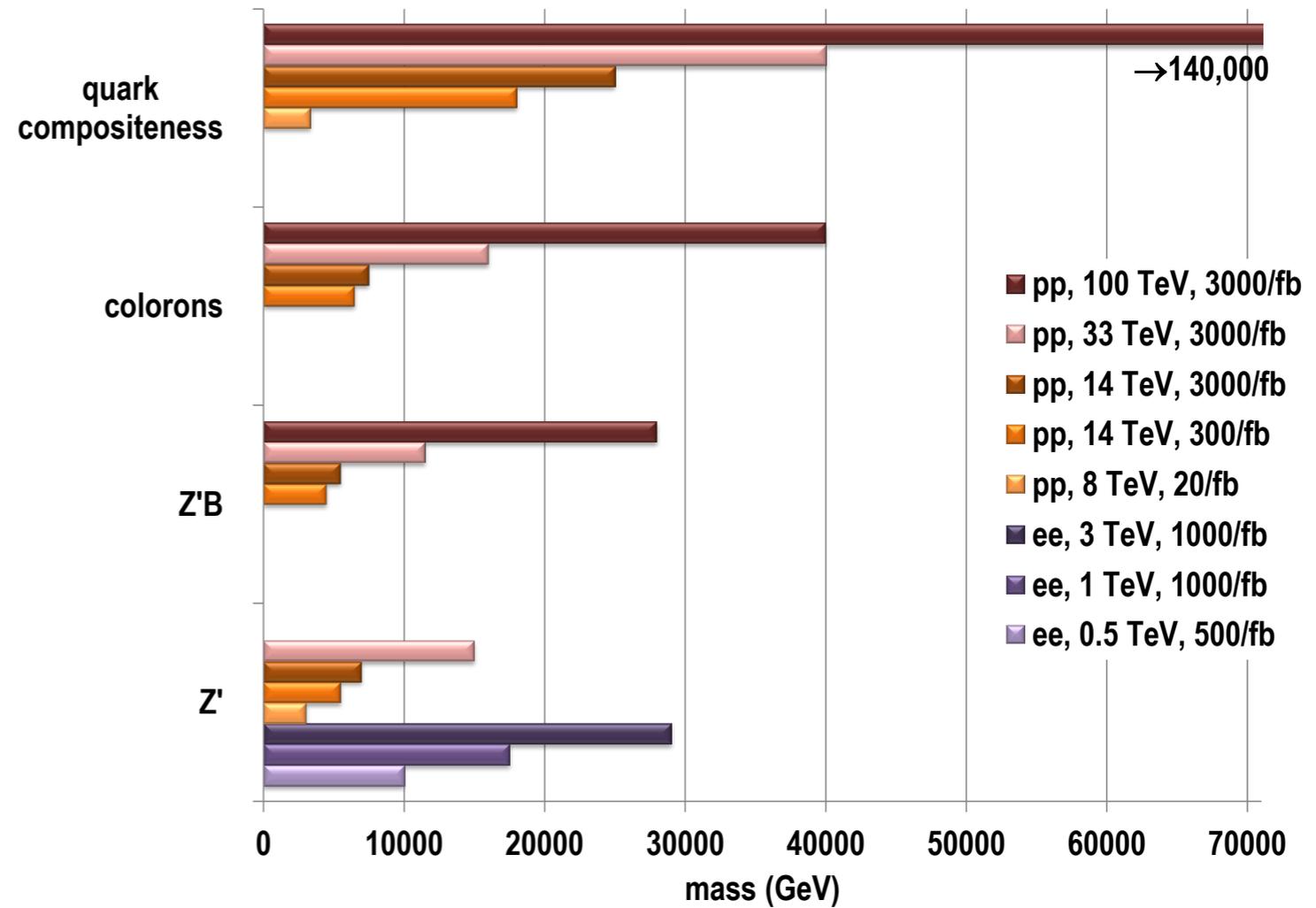
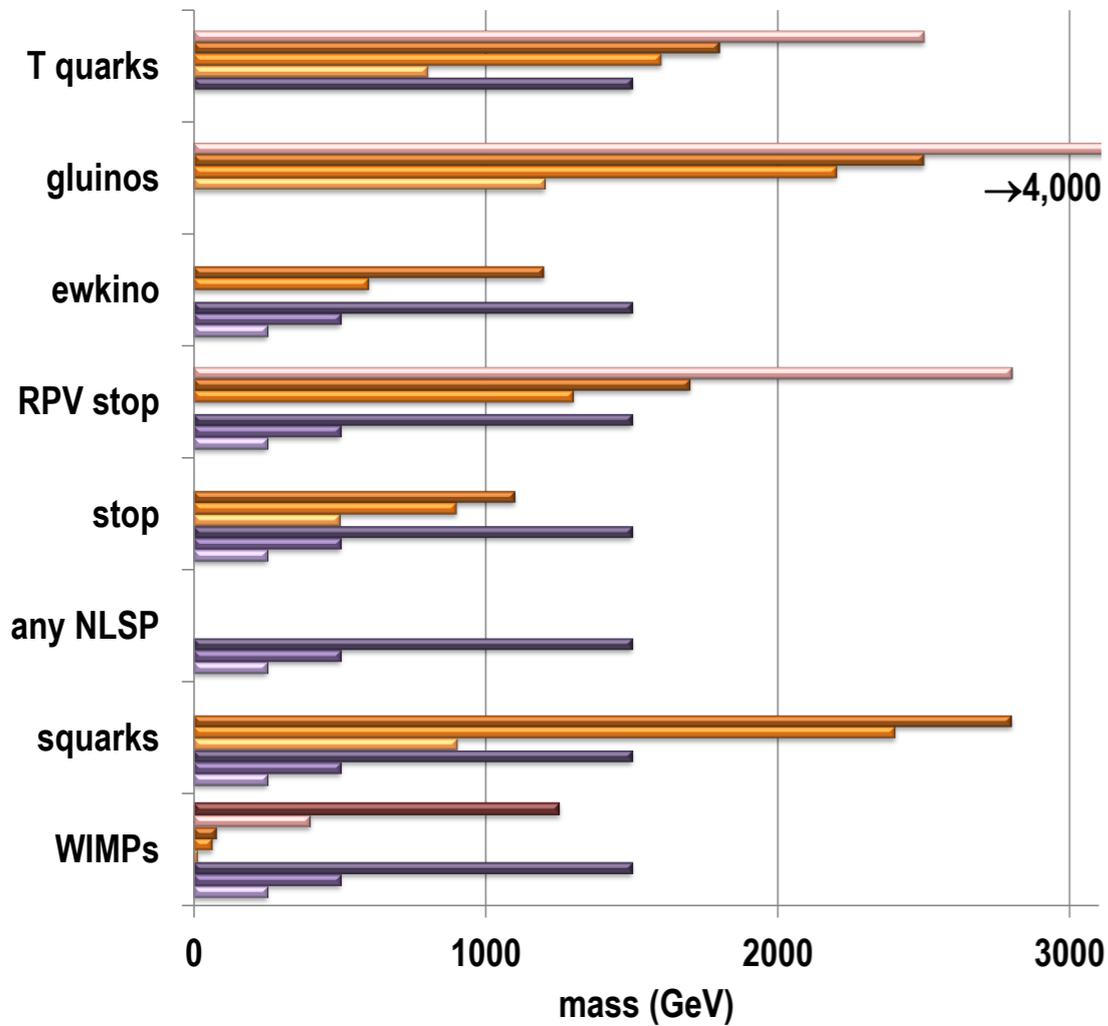
Maybe it only works so well because it's a simple search?
(Signal & Bkgd are both $q\bar{q}$ driven)



Future colliders

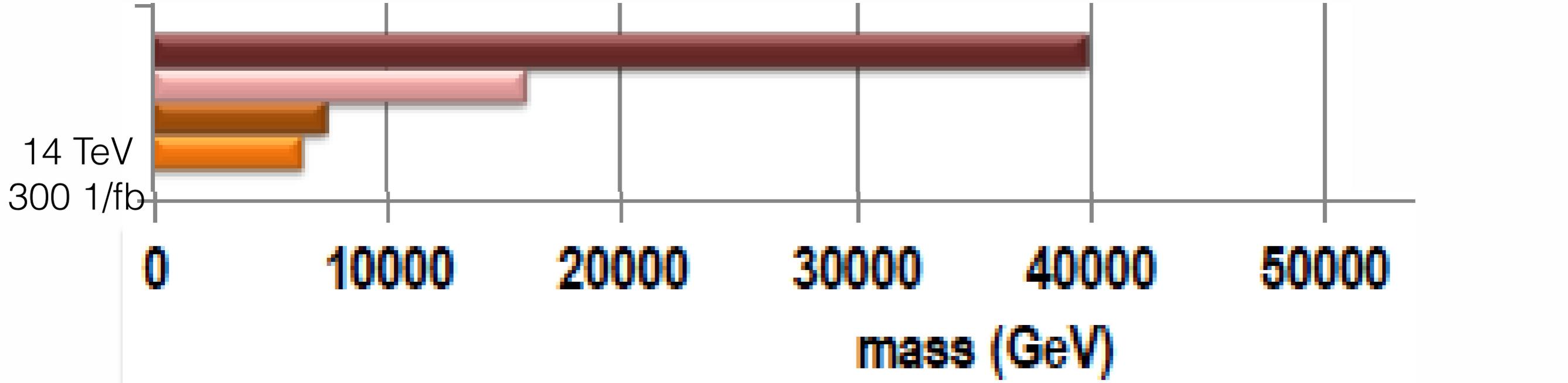
- We're ignoring all subtleties, just going for a baseline check
- If our estimate differs a lot from sophisticated simulations, something interesting has happened:
 - brick-wall (new irreducible backgrounds, granularity of assumed detectors, ...)
 - overly conservative or non-optimal estimates

Future colliders comparison



Energy Frontier Snowmass study ([1311.0299](#))

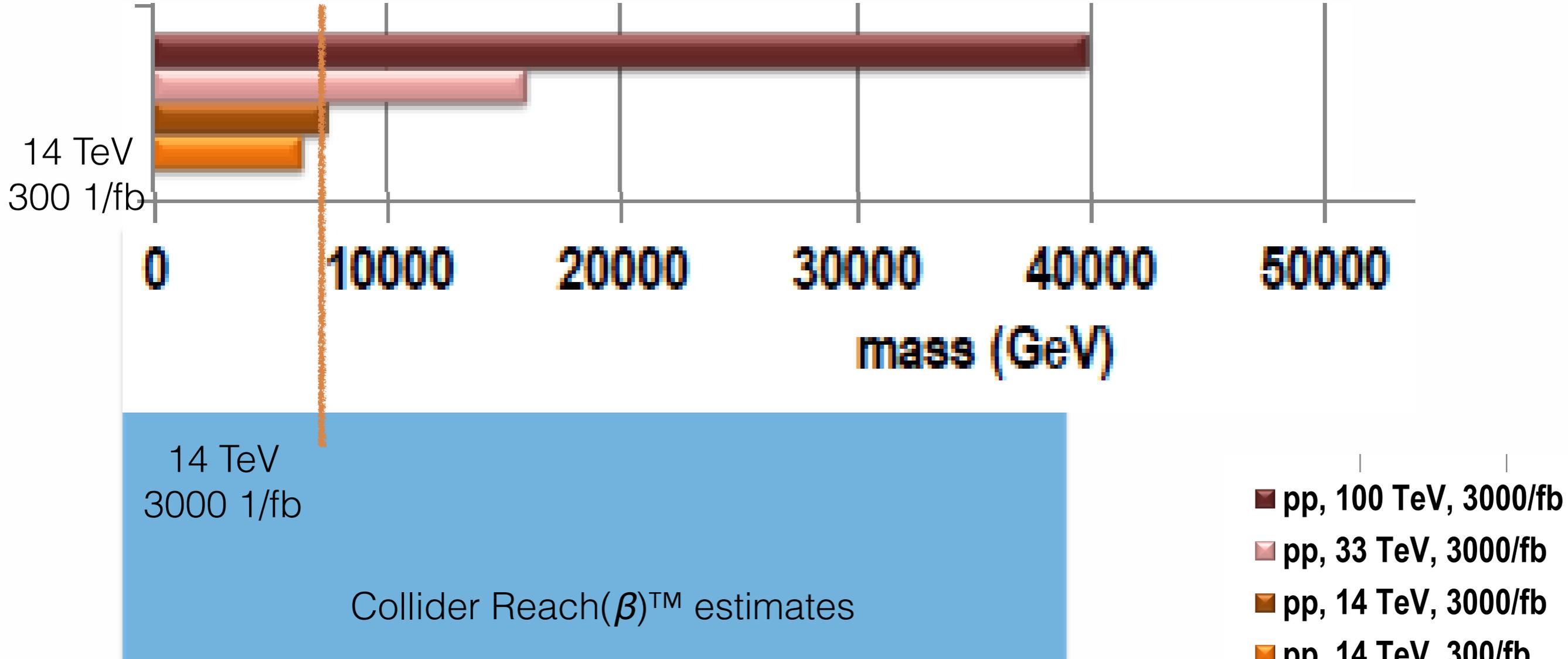
Colorons



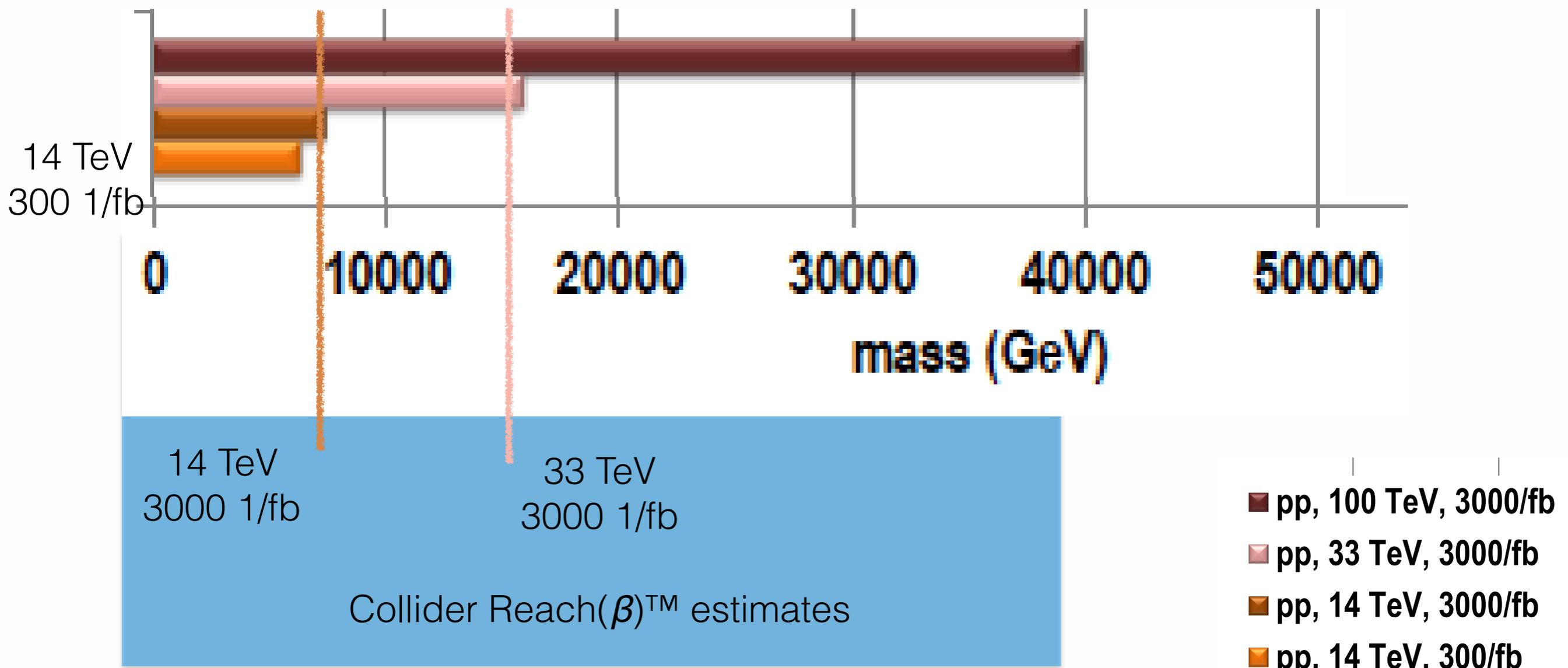
Collider Reach(β)™ estimates

- pp, 100 TeV, 3000/fb
- pp, 33 TeV, 3000/fb
- pp, 14 TeV, 3000/fb
- pp, 14 TeV, 300/fb
- pp, 8 TeV, 20/fb
- ee, 3 TeV, 1000/fb
- ee, 1 TeV, 1000/fb
- ee, 0.5 TeV, 500/fb

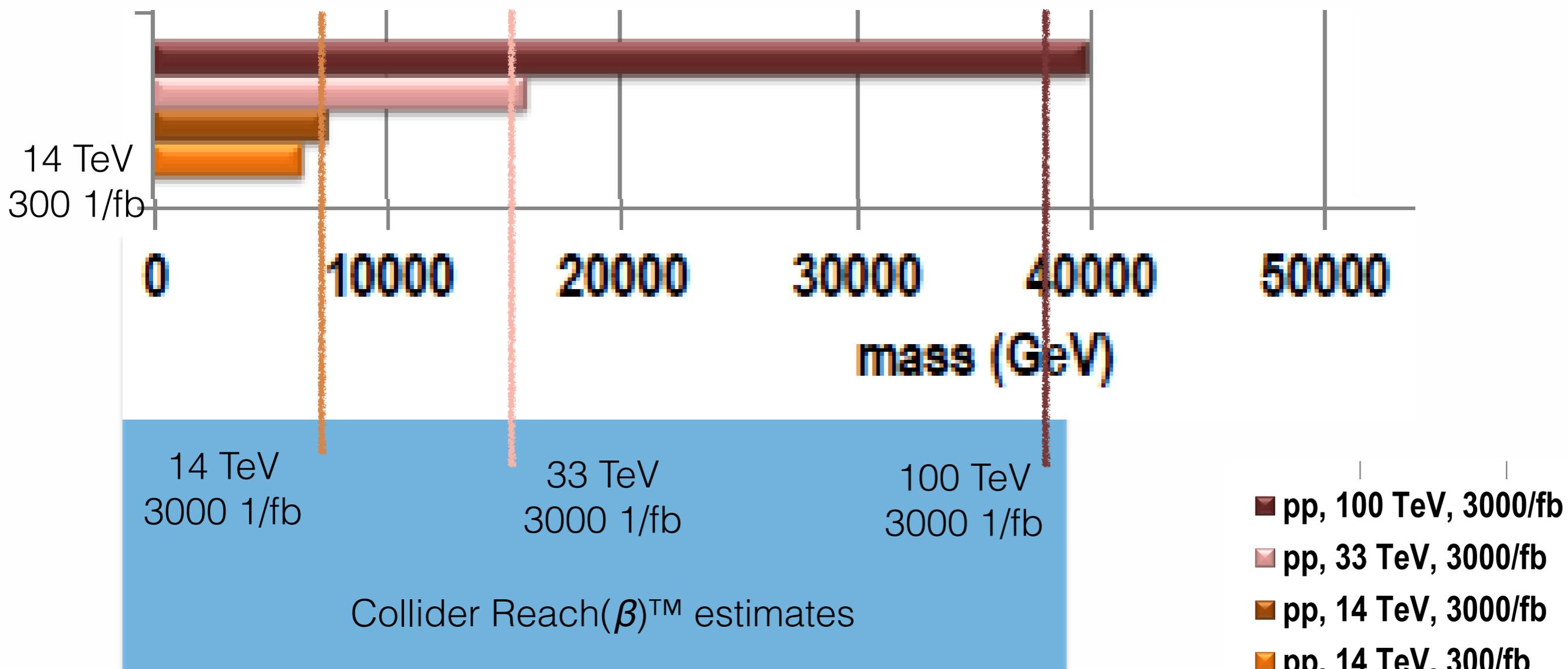
Colorons



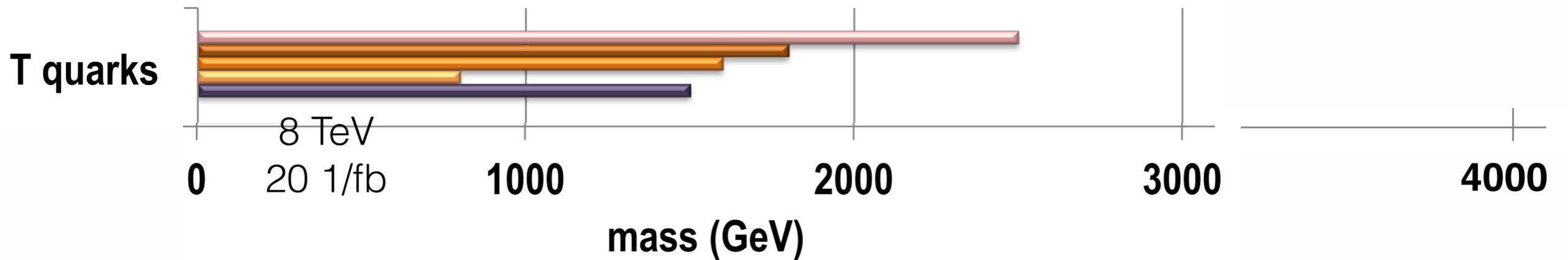
Colorons



Colorons



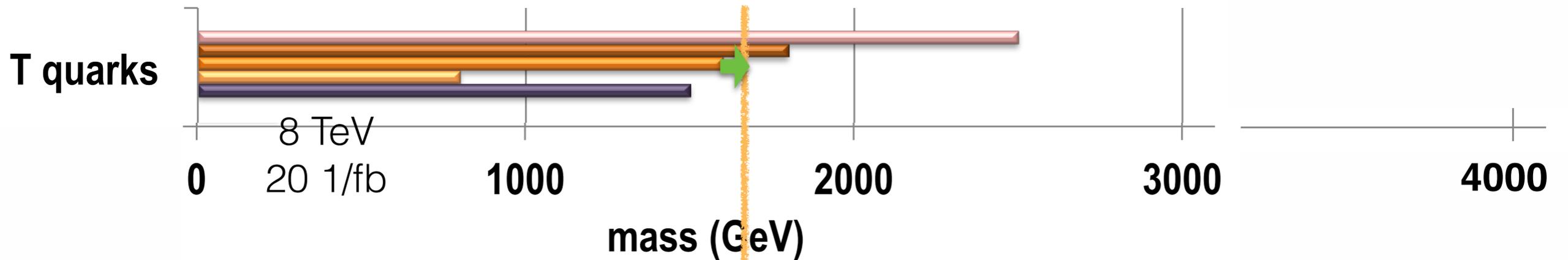
T Quarks



- pp, 100 TeV, 3000/fb
- pp, 33 TeV, 3000/fb
- pp, 14 TeV, 3000/fb
- pp, 14 TeV, 300/fb
- pp, 8 TeV, 20/fb
- ee, 3 TeV, 1000/fb
- ee, 1 TeV, 1000/fb
- ee, 0.5 TeV, 500/fb

Collider Reach(β)TM estimates

T Quarks

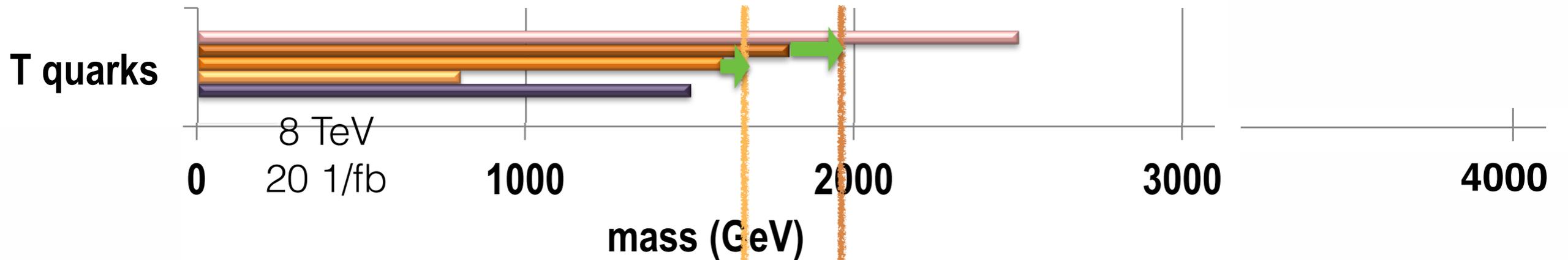


- pp, 100 TeV, 3000/fb
- pp, 33 TeV, 3000/fb
- pp, 14 TeV, 3000/fb
- pp, 14 TeV, 300/fb
- pp, 8 TeV, 20/fb
- ee, 3 TeV, 1000/fb
- ee, 1 TeV, 1000/fb
- ee, 0.5 TeV, 500/fb

14 TeV
300 1/fb

Collider Reach(β)TM estimates

T Quarks



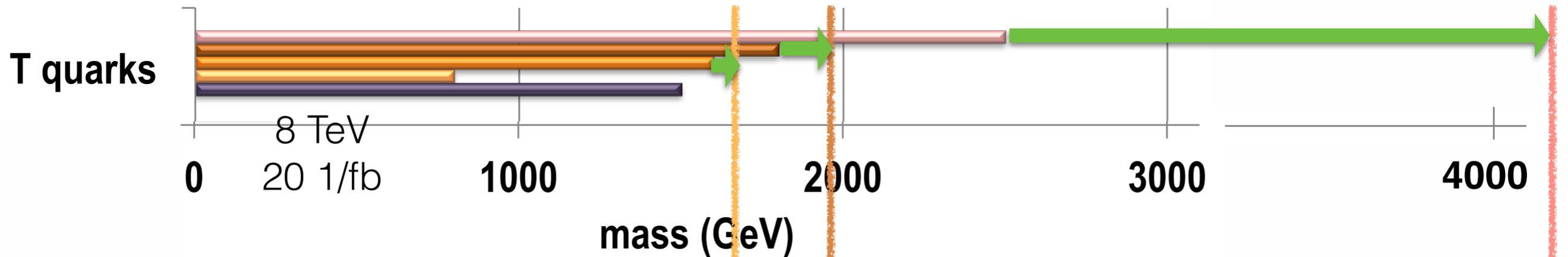
- pp, 100 TeV, 3000/fb
- pp, 33 TeV, 3000/fb
- pp, 14 TeV, 3000/fb
- pp, 14 TeV, 300/fb
- pp, 8 TeV, 20/fb
- ee, 3 TeV, 1000/fb
- ee, 1 TeV, 1000/fb
- ee, 0.5 TeV, 500/fb

14 TeV
300 1/fb

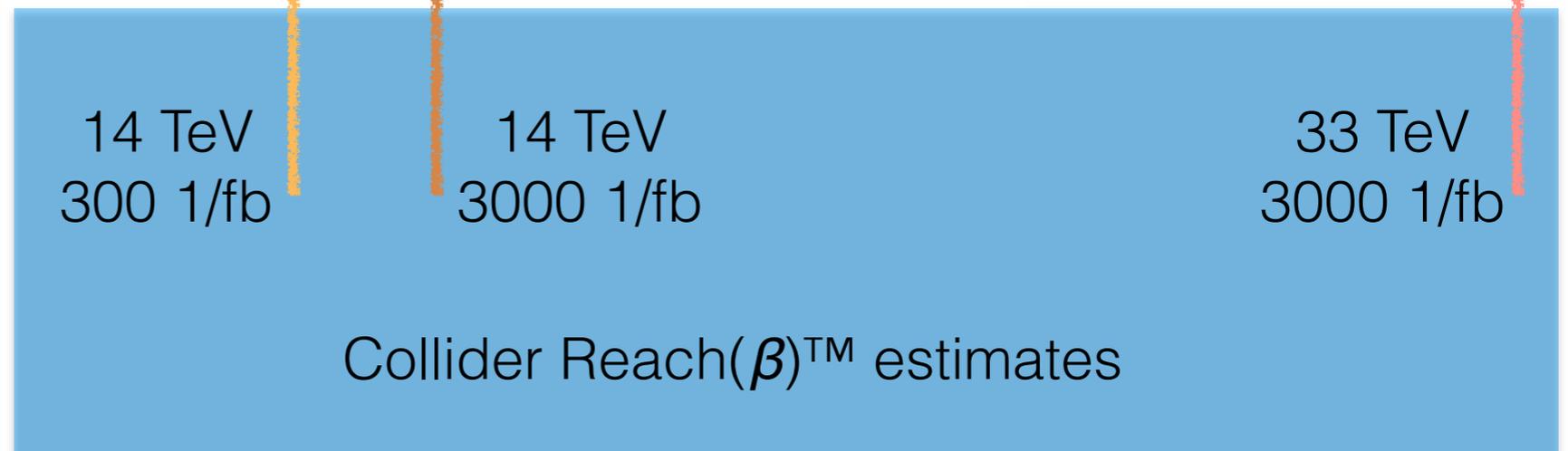
14 TeV
3000 1/fb

Collider Reach(β)TM estimates

T Quarks



- pp, 100 TeV, 3000/fb
- pp, 33 TeV, 3000/fb
- pp, 14 TeV, 3000/fb
- pp, 14 TeV, 300/fb
- pp, 8 TeV, 20/fb
- ee, 3 TeV, 1000/fb
- ee, 1 TeV, 1000/fb
- ee, 0.5 TeV, 500/fb



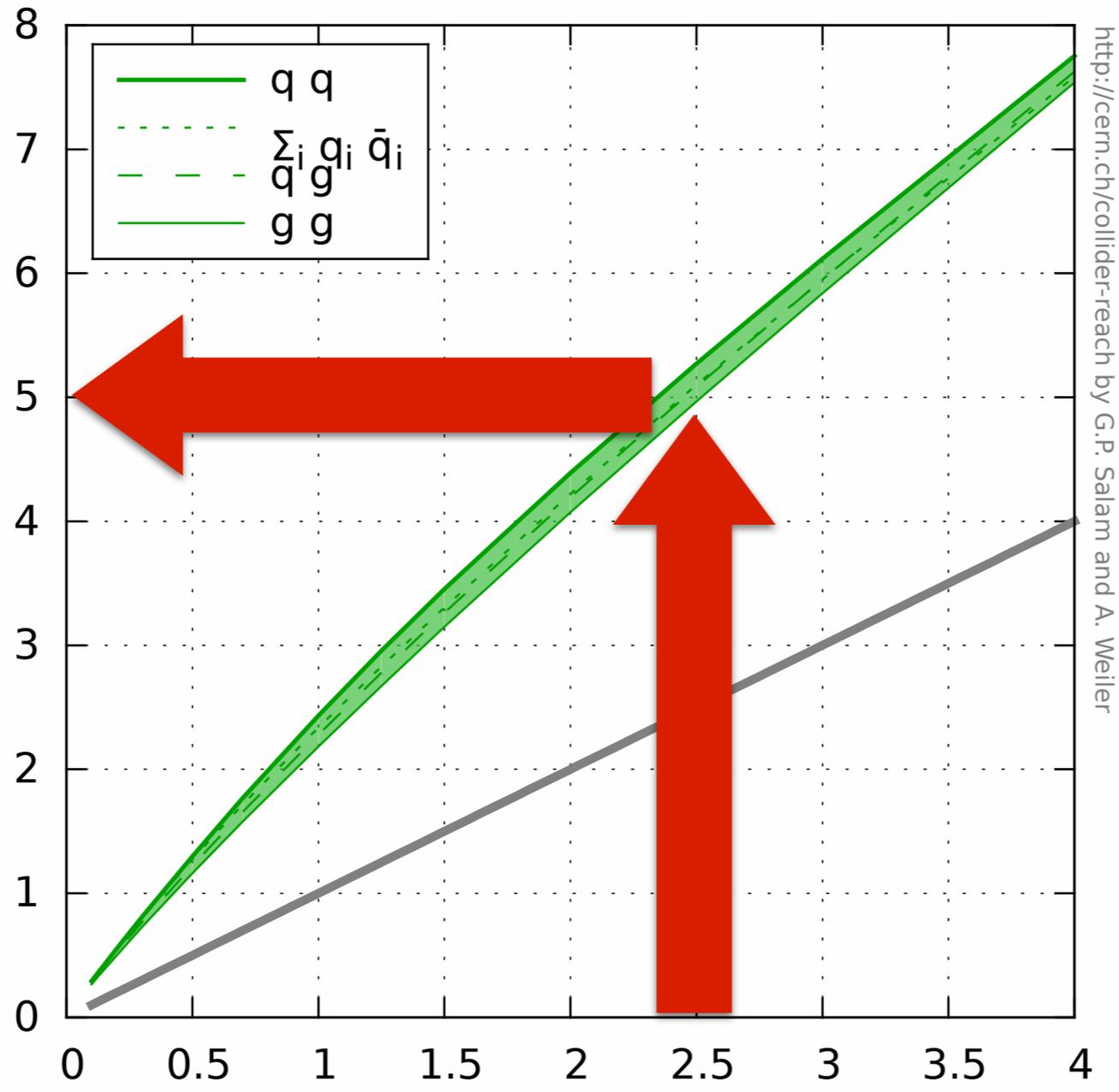
Issue seems to be detector granularity

From your iPhone
(or a generic browser)
cern.ch/collider-reach

From your Android Phone
(or a generic browser)
cern.ch/collider-reach

Collider 1: CoM energy TeV, integrated luminosity fb⁻¹
 Collider 2: CoM energy TeV, integrated luminosity fb⁻¹
 PDF:

**Mass [TeV] at
collider #2**



Mass [TeV] at collider #1

Collider 1: CoM energy

8

TeV, integrated luminosity

20

fb^{-1}

Collider 2: CoM energy

14

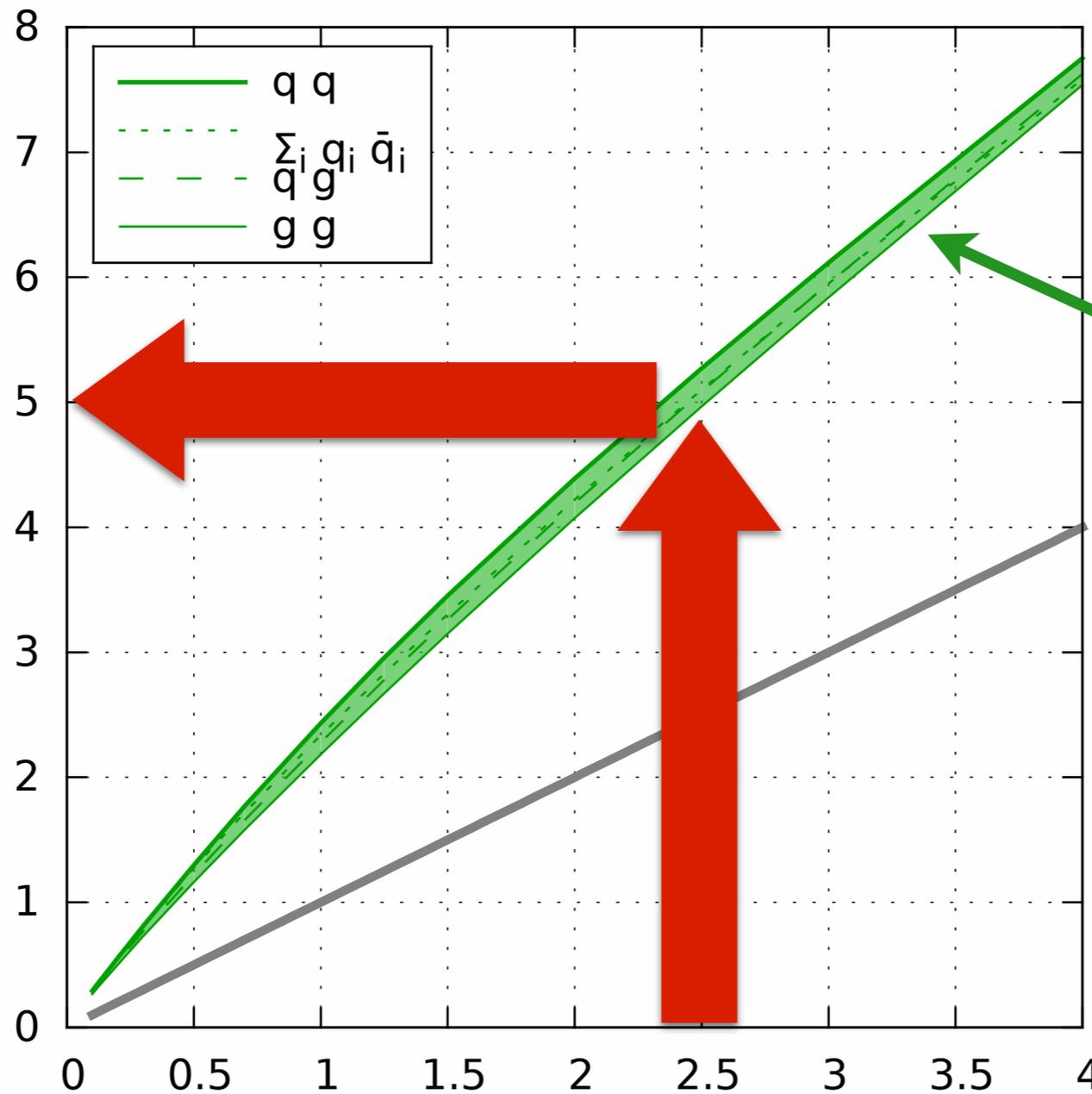
TeV, integrated luminosity

300

fb^{-1}

PDF:

MSTW2008nnlo68cl



Mass [TeV] at
collider #2

Spread of
partonic
channels
(assume same
channel for
S & B)

Mass [TeV] at collider #1

The Collider Reach tool gives you a quick (and dirty) estimate of the relation between the mass reaches of different proton-proton collider setups.

Collider 1: CoM energy TeV, integrated luminosity fb⁻¹

Collider 2: CoM energy TeV, integrated luminosity fb⁻¹

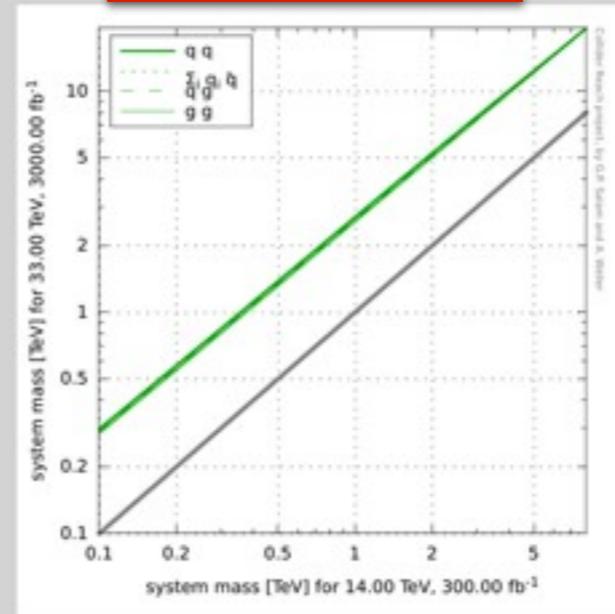
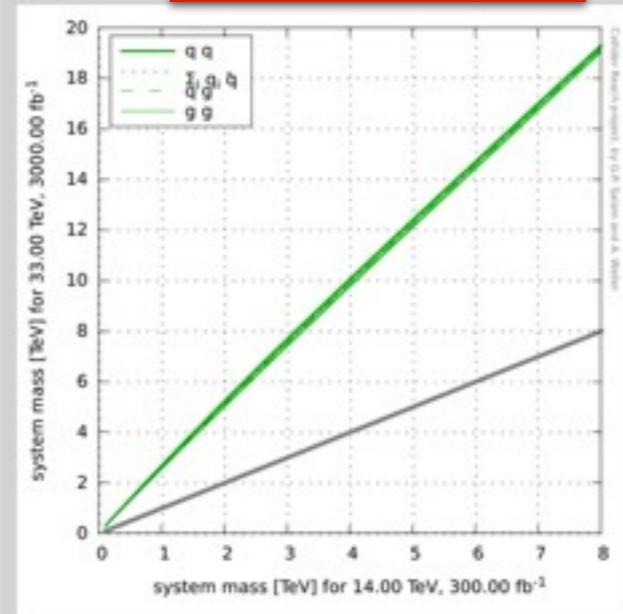
PDF:

Submit

linear plot

log-log plot

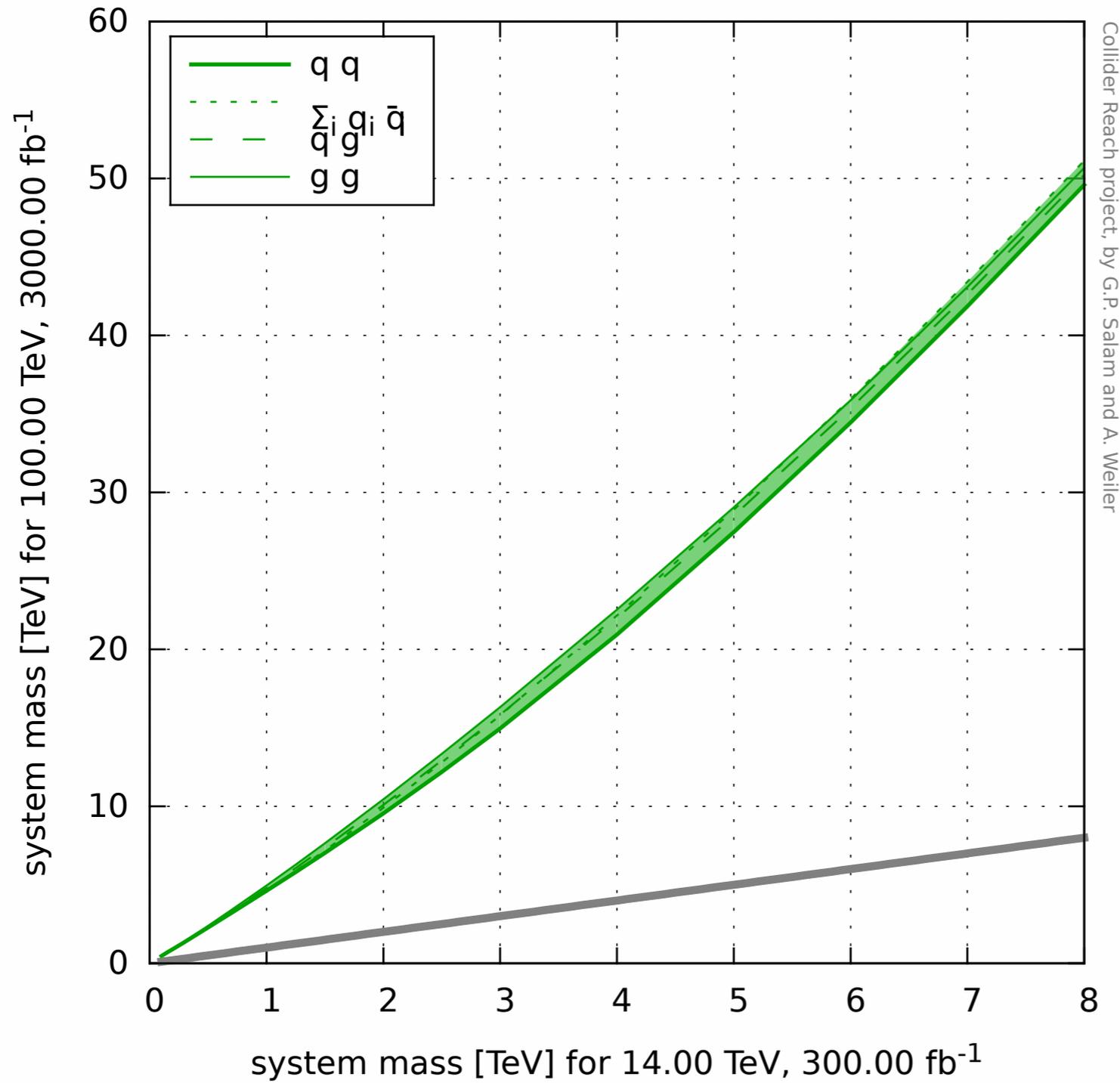
Plots



Download: [collider.pdf](#), [colliderloglog.pdf](#), plot generation [log file](#)
 The PDF choice was CT10nlo.LHgrid

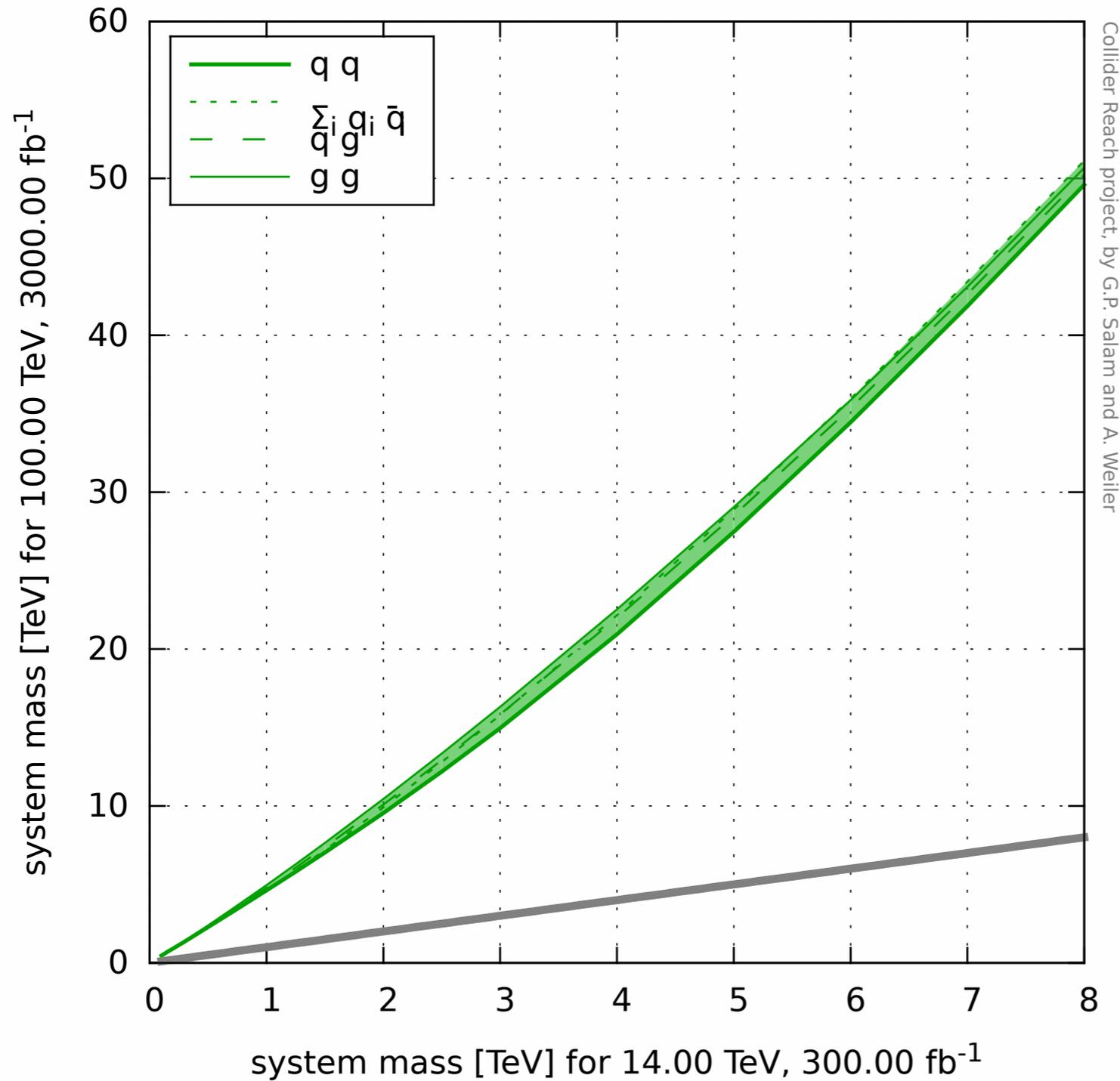
Original mass	gg	qg	allqq	qqbar
100.	283.	291.	298.	297.
125.	350.	359.	368.	367.
150.	416.	427.	438.	437.
200.	547.	562.	576.	575.
300.	806.	827.	848.	847.
500.	1317.	1350.	1386.	1382.
700.	1822.	1866.	1916.	1907.
1000.	2570.	2628.	2702.	2680.
1250.	3188.	3256.	3349.	3314.
1500.	3802.	3879.	3990.	3939.
2000.	5018.	5110.	5251.	5169.
2500.	6223.	6327.	6488.	6380.
3000.	7417.	7530.	7703.	7578.
4000.	9782.	9904.	10082.	9945.
5000.	12120.	12246.	12417.	12284.
6000.	14439.	14565.	14726.	14601.
7000.	16748.	16871.	17021.	16905.
8000.	19053.	19169.	19310.	19206.

14 TeV_{300 fb⁻¹} → 100 TeV_{3 ab⁻¹}



Collider Reach project, by G.P. Salam and A. Weiler

14 TeV_{300 fb⁻¹} → 100 TeV_{3 ab⁻¹}



The PDF choice was CT10nlo.LHgrid

Original mass	gg	qg	allqq	qqbar
100.	469.	465.	462.	457.
125.	585.	579.	575.	568.
150.	702.	693.	687.	679.
200.	937.	923.	912.	902.
300.	1414.	1386.	1365.	1350.
500.	2394.	2332.	2279.	2261.
700.	3401.	3300.	3206.	3194.
1000.	4956.	4793.	4619.	4640.
1250.	6287.	6072.	5818.	5892.
1500.	7647.	7382.	7038.	7187.
2000.	10444.	10090.	9552.	9905.
2500.	13337.	12908.	12185.	12781.
3000.	16319.	15833.	14954.	15795.
4000.	22531.	21986.	20933.	22162.
5000.	29050.	28508.	27467.	28894.
6000.	35863.	35366.	34451.	35960.
7000.	43079.	42620.	41854.	43411.
8000.	50671.	50230.	49590.	51132.

When you've lost your XPhone

Rule of Thumb #1

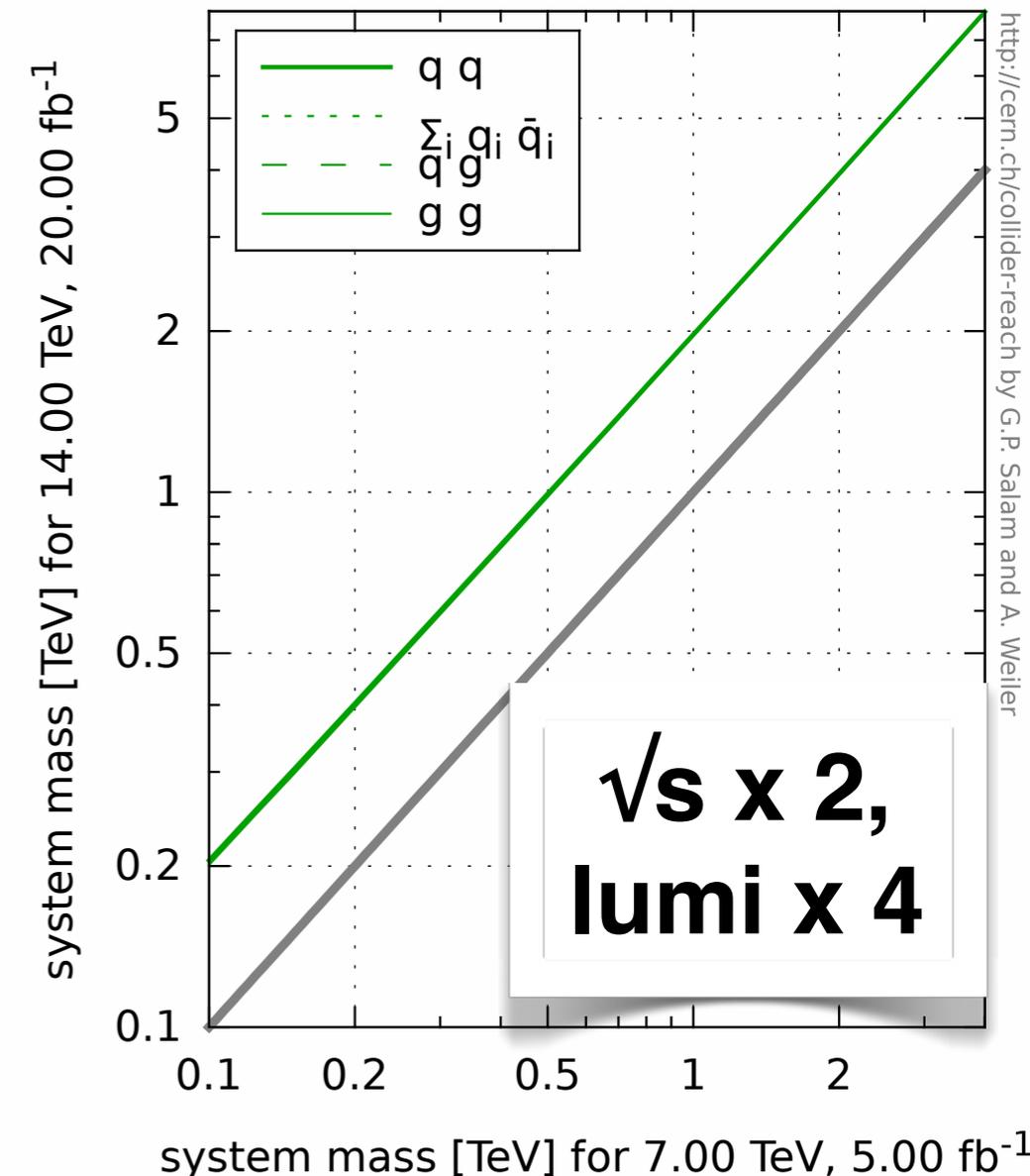
(well known among practitioners)

Increase collider energy by factor X
& increase luminosity by a factor X^2

→ **reach goes up by a factor X**

[Because you keep same Bjorken- x &
luminosity increase compensates for
 $1/\text{mass}^2$ scaling of cross sections]

PDF scaling variations are small effect



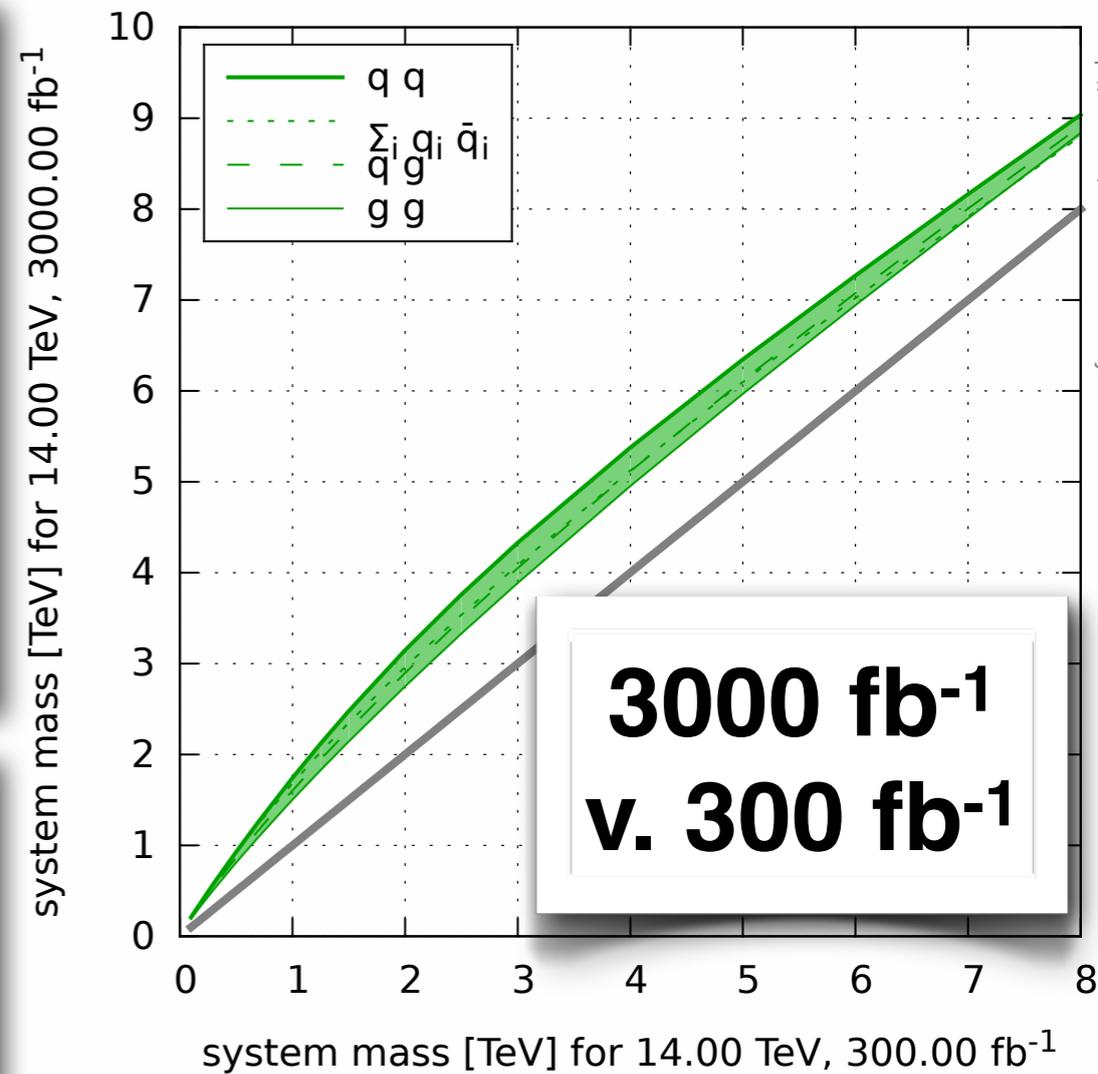
Rule of Thumb #2

(apparently not widely known previously)

Increase luminosity by factor 10
→ **reach increases by constant**
 $\Delta m \approx 0.07\sqrt{s}$

i.e. for $\sqrt{s}=14$ TeV, reach goes by up
1 TeV

No deep reason — a somewhat
random characteristic of large-x PDFs.
Only holds for $0.15 \lesssim M/\sqrt{s} \lesssim 0.6$



Consequence of rule #2

(may be a bit fragile & only for $S \approx B$)

Exclusion is $2\text{-}\sigma$

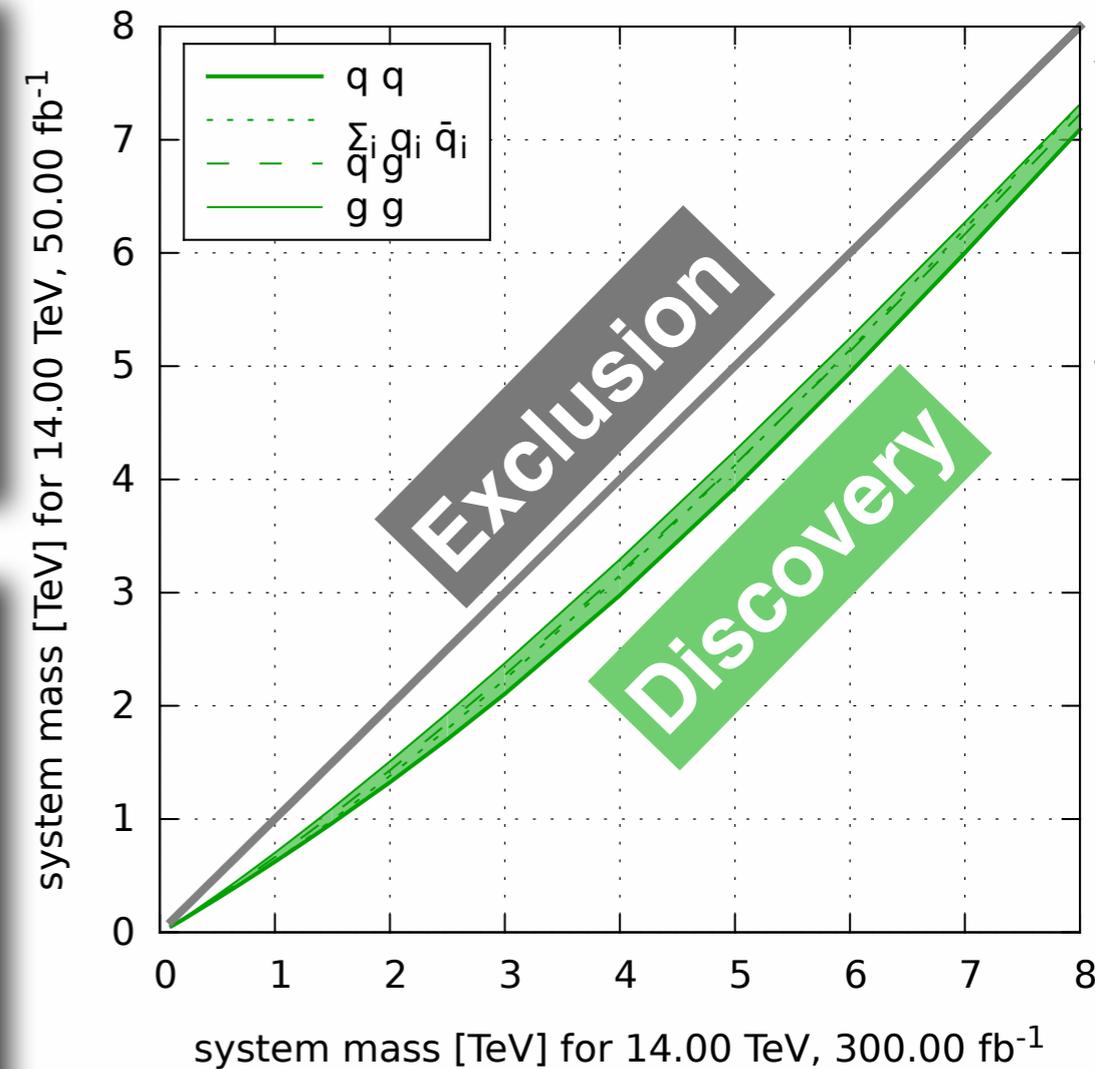
Discovery is $5\text{-}\sigma$

Need $(5/2)^2 = 6.25$ increase in lumi to go from one to the other.

Using rule #2:

discovery reach is about $0.05\sqrt{s}$
below exclusion reach

~ 0.8 TeV at 14 TeV



Conclusions

Amazing recent progress on MC merging/matching, NLO automation, high precision (N)NNLO calculations — hard to imagine how much further we will get by 100 TeV era

FHC as scaled-up LHC is probably not too bad an approx if cuts & analyses are adapted appropriately

→ part of assumption of <http://cern.ch/collider-reach>

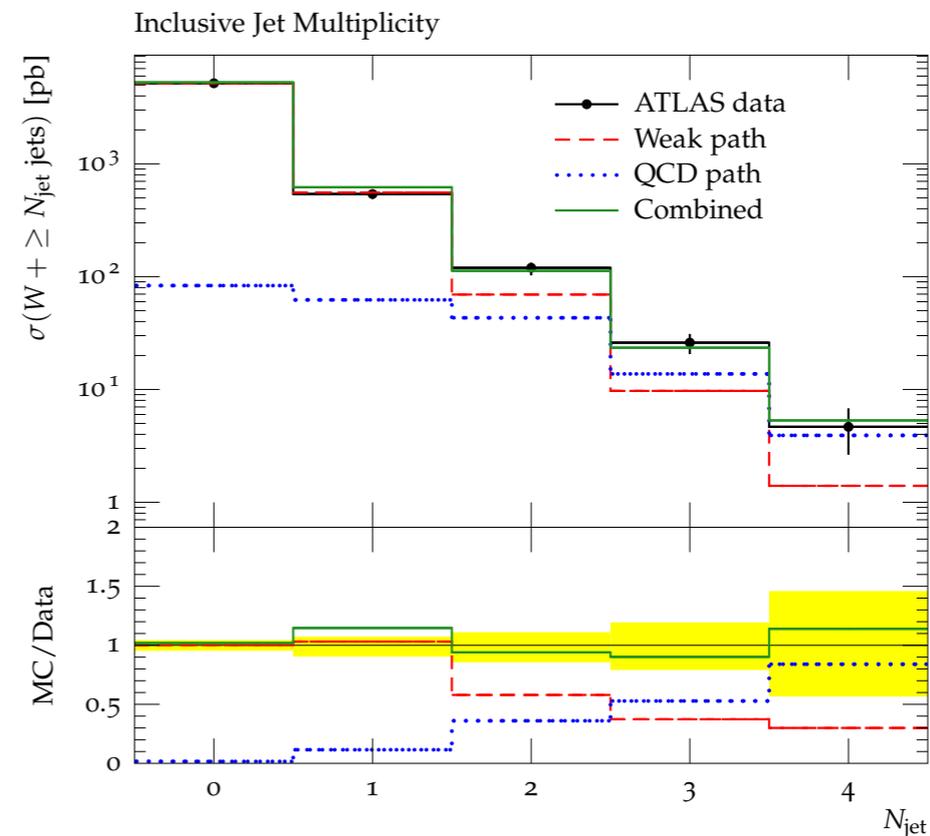
We've maybe only touched the surface on potential from $\sqrt{s} \gg m_{EW}$ — e.g. incoming parton polarization

Hard (= interesting!) problems remain in collider QCD...

BACKUP SLIDES

W + jets

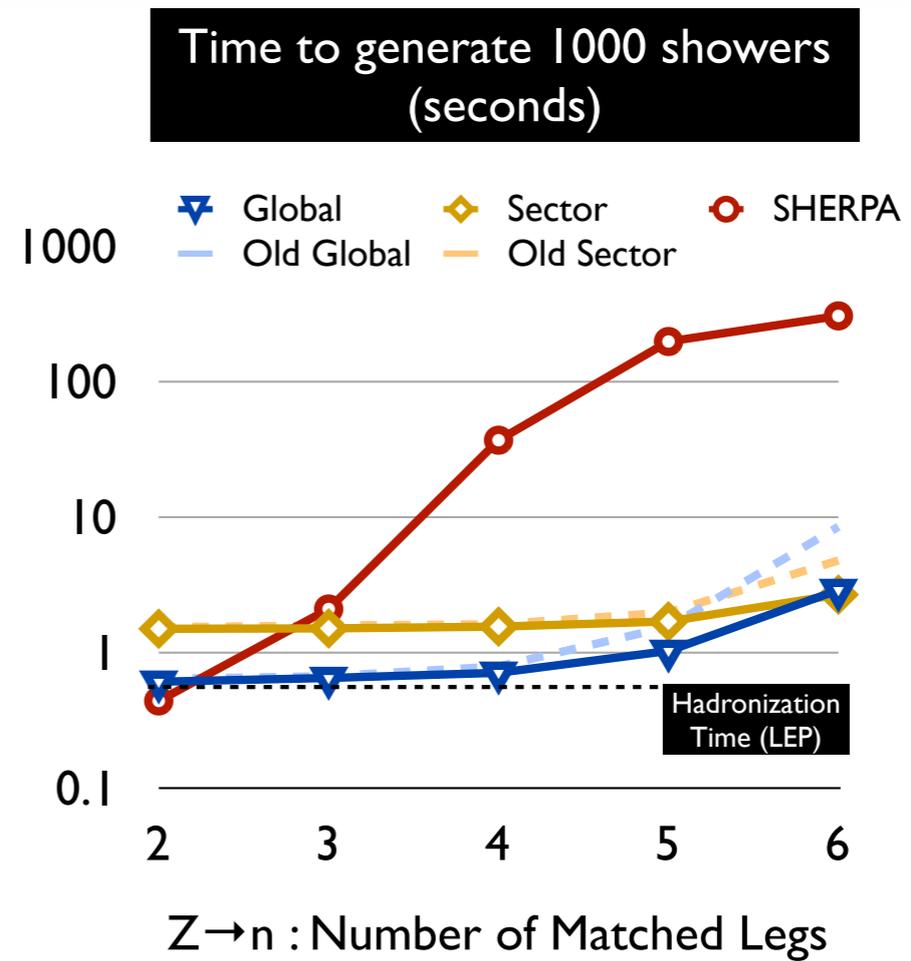
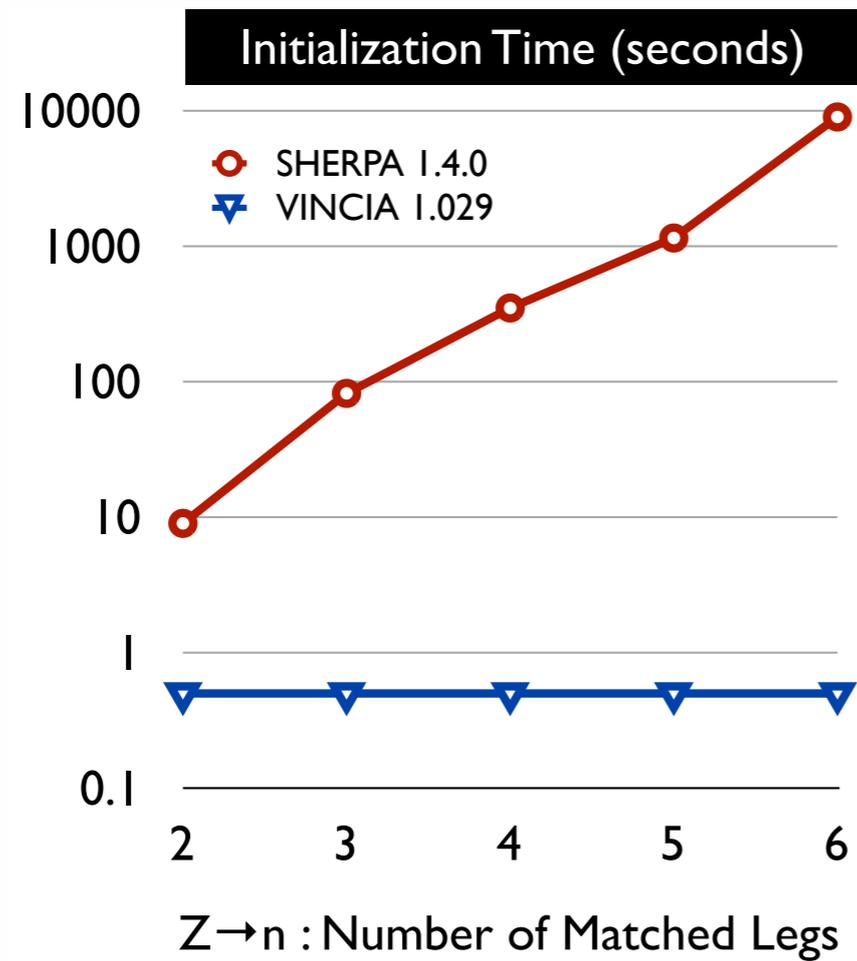
- W + jets is notoriously known for PS not describing data well
- Combine Drell-Yan W production with QCD radiation and $2 \rightarrow 2$ hard QCD processes with weak shower
- Double counting avoided by applying cuts in the spirit of the k_{\perp} jet algorithm
- k-factor applied (normalized to fit first bin)



Some Higgs reference numbers

\sqrt{s} [TeV]	σ [pb]
8	18.4
14	47.6
100	718

large m_{top} , NNLO, MSTW2008 ($\alpha_s = 0.117$)



1301.0933

Can this gain be replicated for pp collisions?

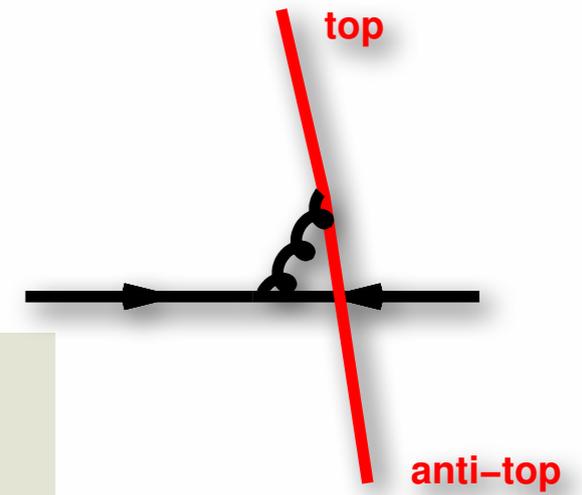
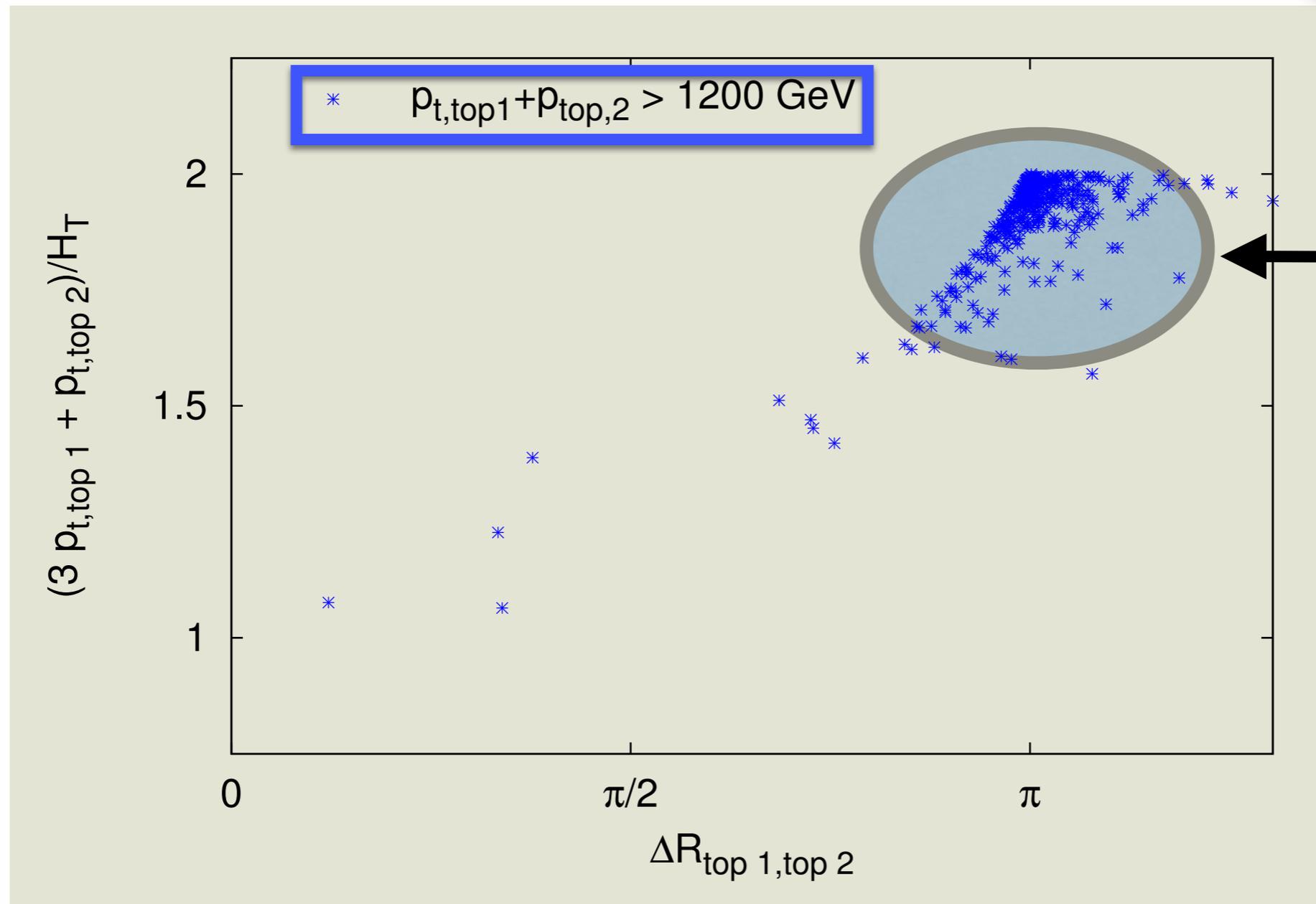
Are top pairs in high- p_t events always back-to-back?

A reminder that top-quarks at LHC are almost “light”

An 8 TeV study with POWHEG, top-pair production, no decay and no parton showering (to keep things simple)

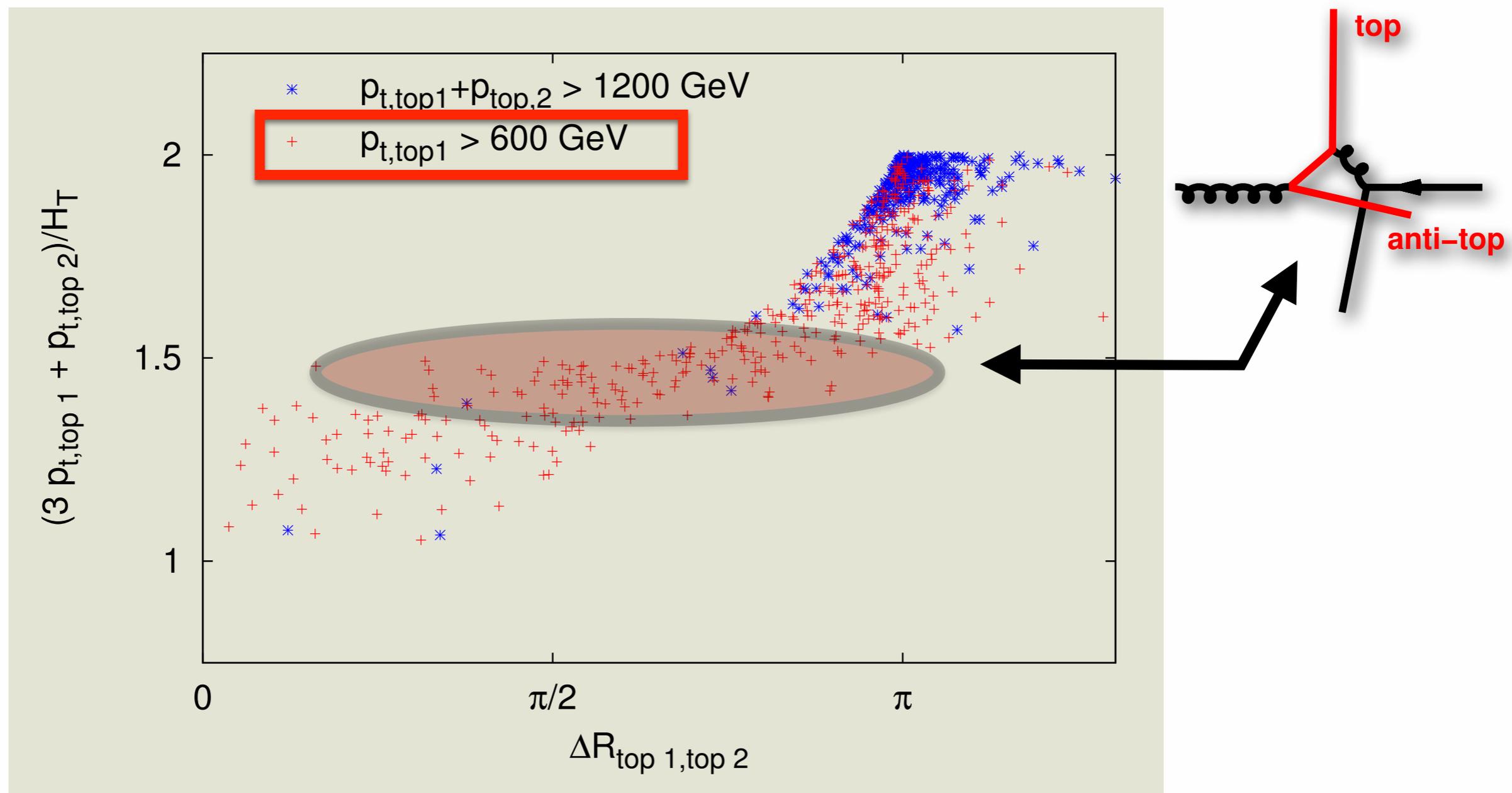
top topology v. cuts

Flavour Creation



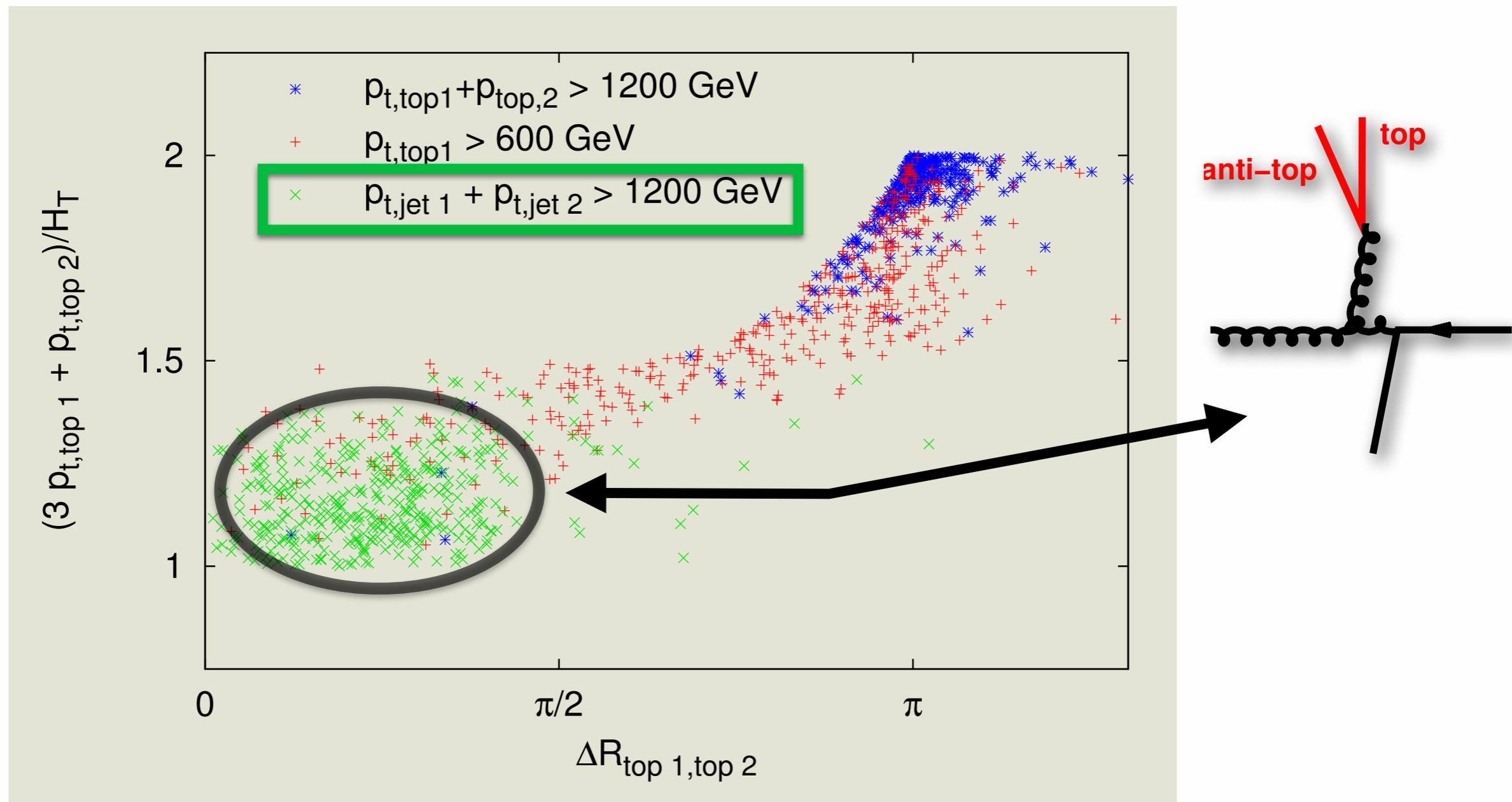
top topology v. cuts

Flavour Excitation – tops inside your PDFs



top topology v. cuts

Gluon Splitting



Assumptions

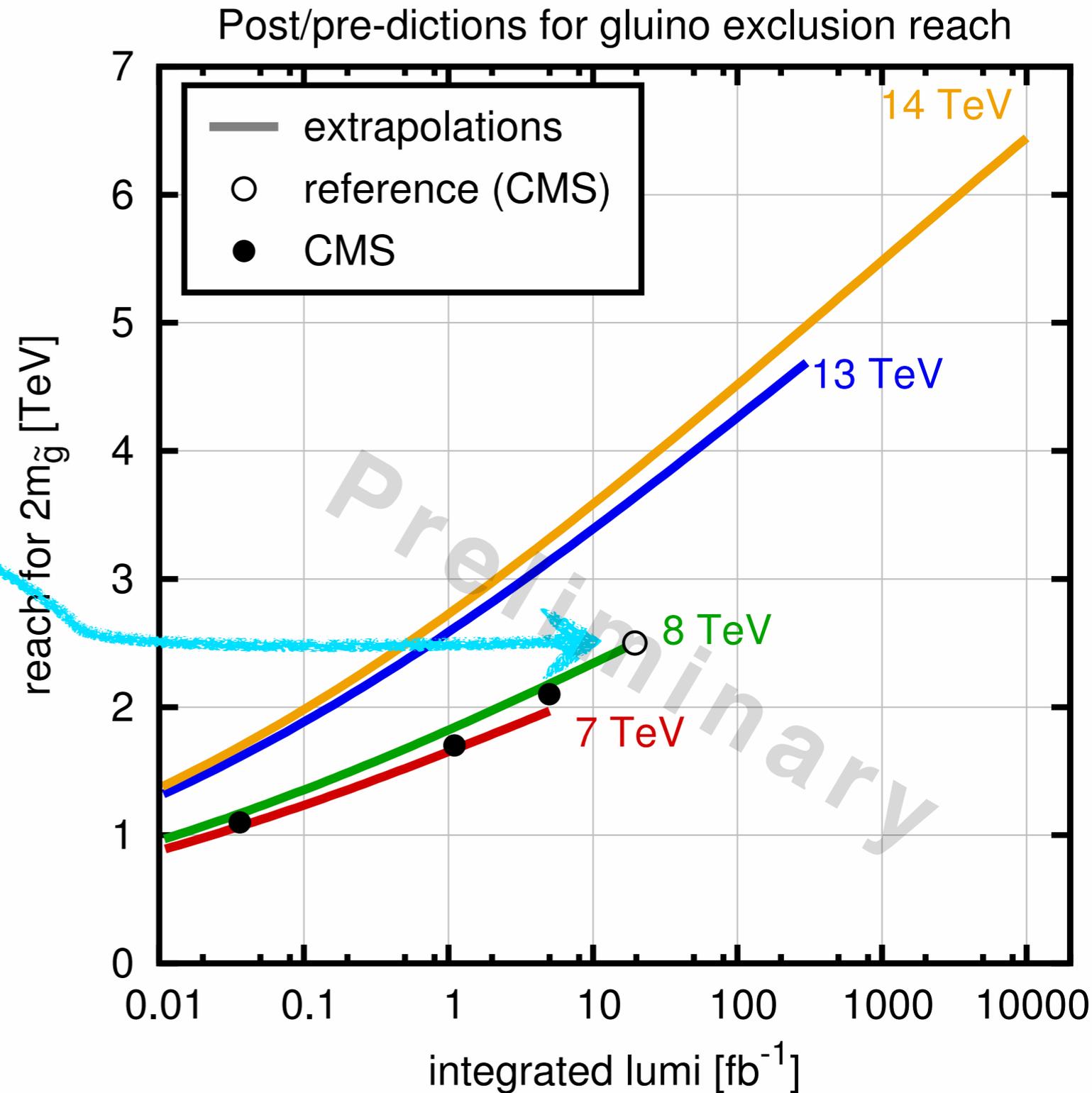
- We don't need to worry about scaling of background vs. signal
- Reconstruction efficiencies, background rejection, etc all stay reasonably constant

Try a SUSY example,
gluinos. Baseline:

CMS, 20 fb⁻¹ @ 8 TeV
excludes $M_{\tilde{g}} < 1250$ GeV
i.e. $2M_{\tilde{g}} < 2.5$ TeV

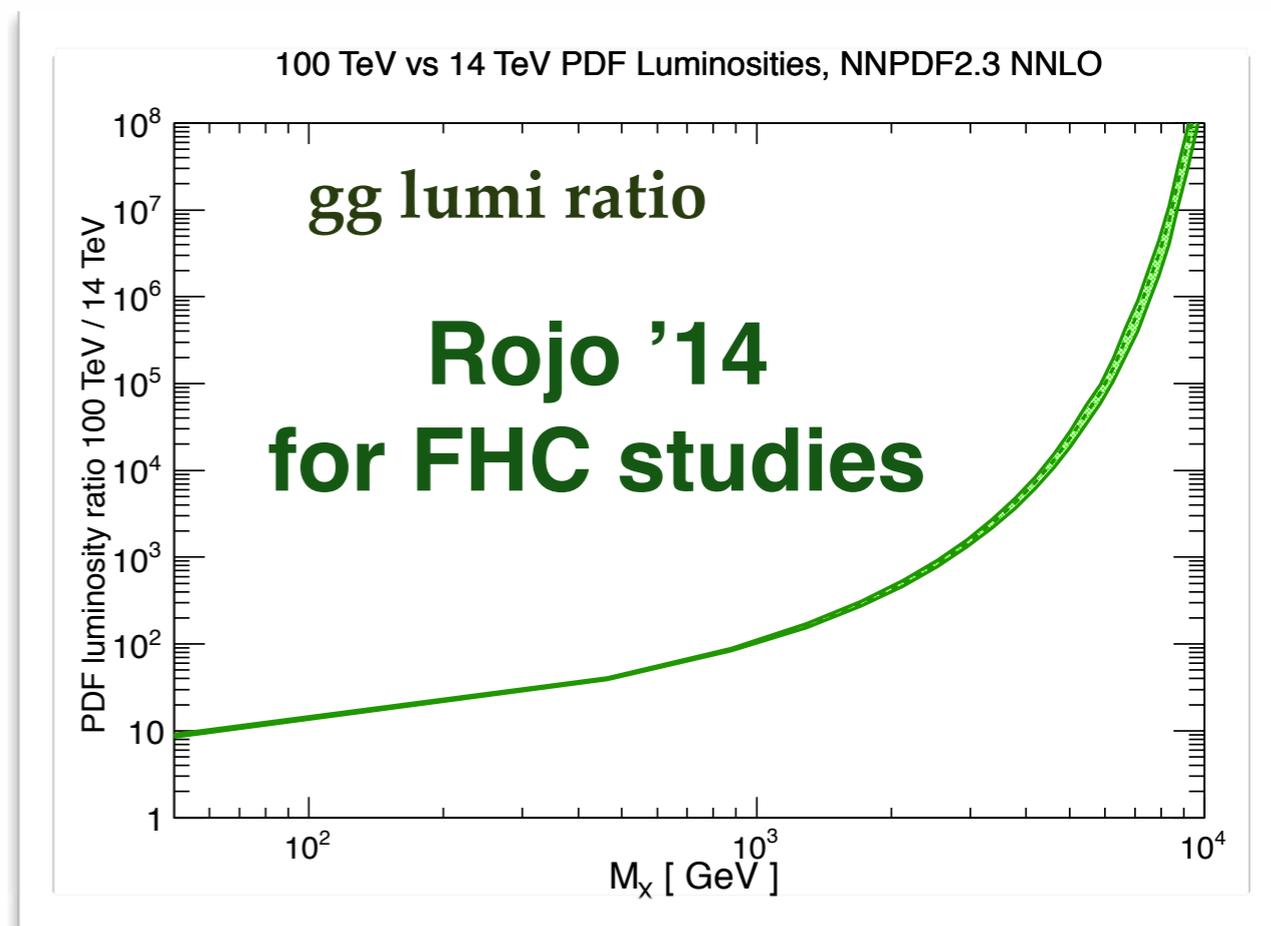
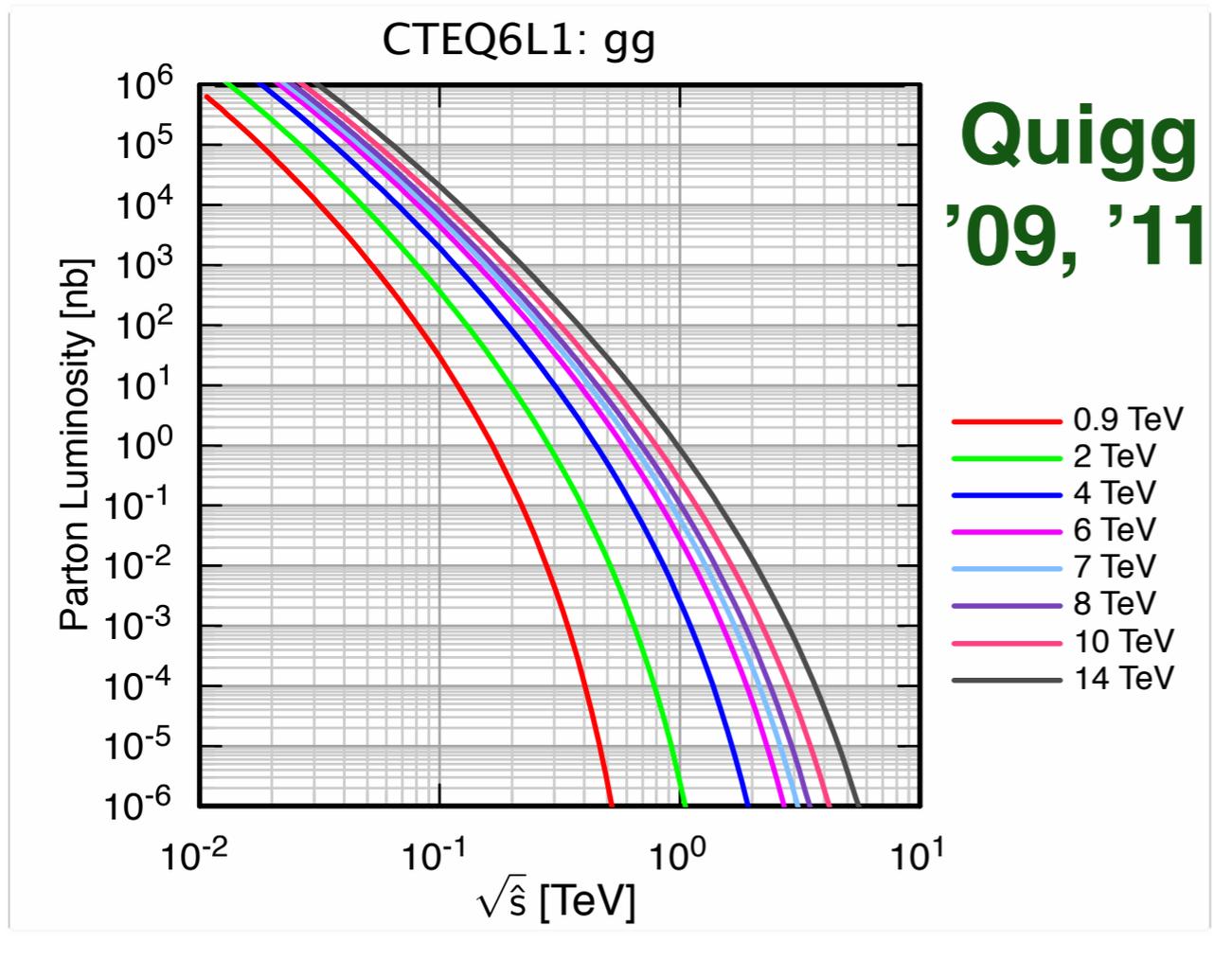
“Predict” exclusions
at other lumis &
energies (assume gg)

Compare to actual
exclusions



**Still works OK, despite (poor) assumption of same
signal and background channels [see also later]**

A side remark: Studying partonic luminosities is a standard technique

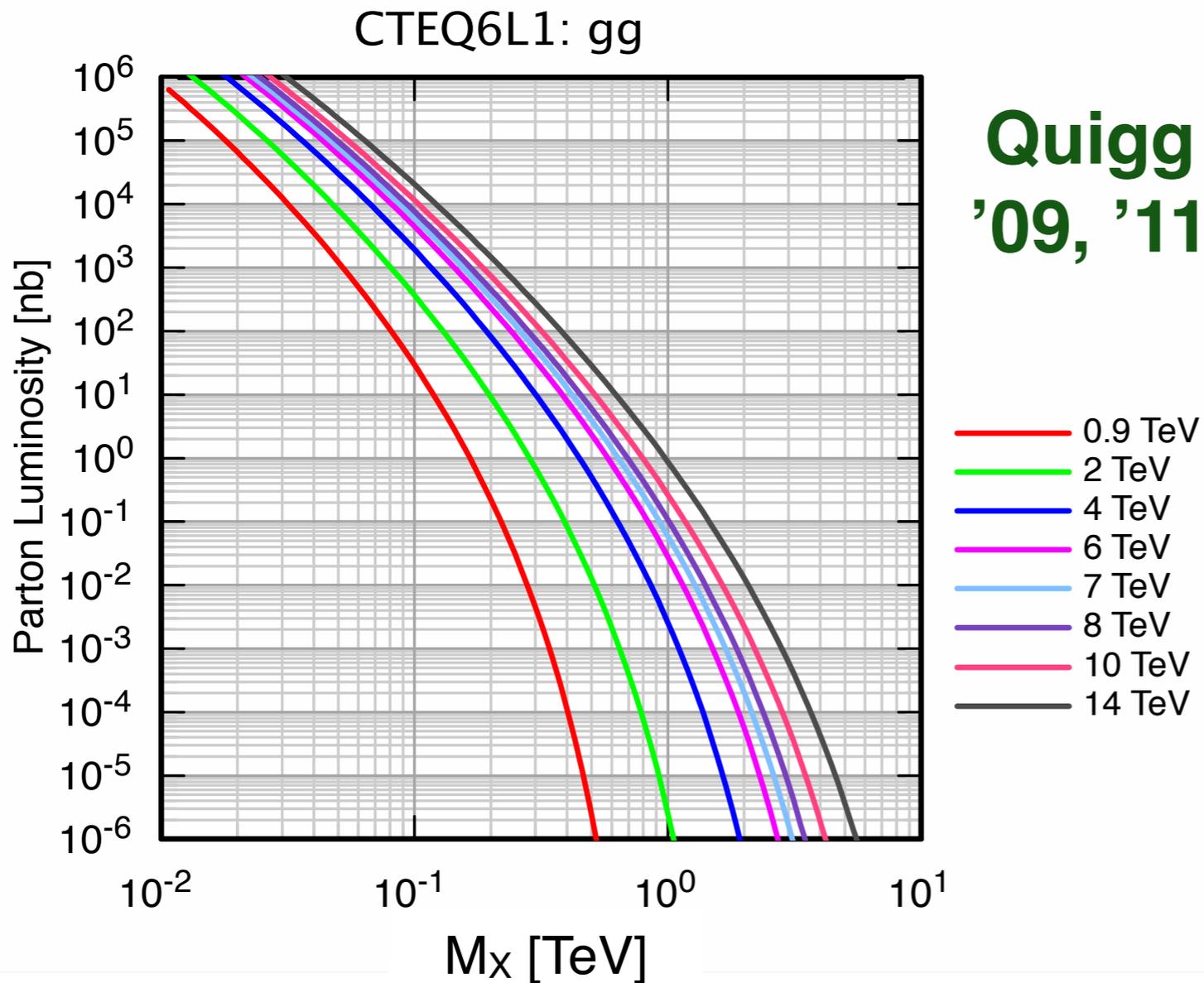


How do we differ?

Study one key question:
relate reaches [TeV] of
different colliders

Validate the approach
by postdicting LHC and
Tevatron results

Why does it work?



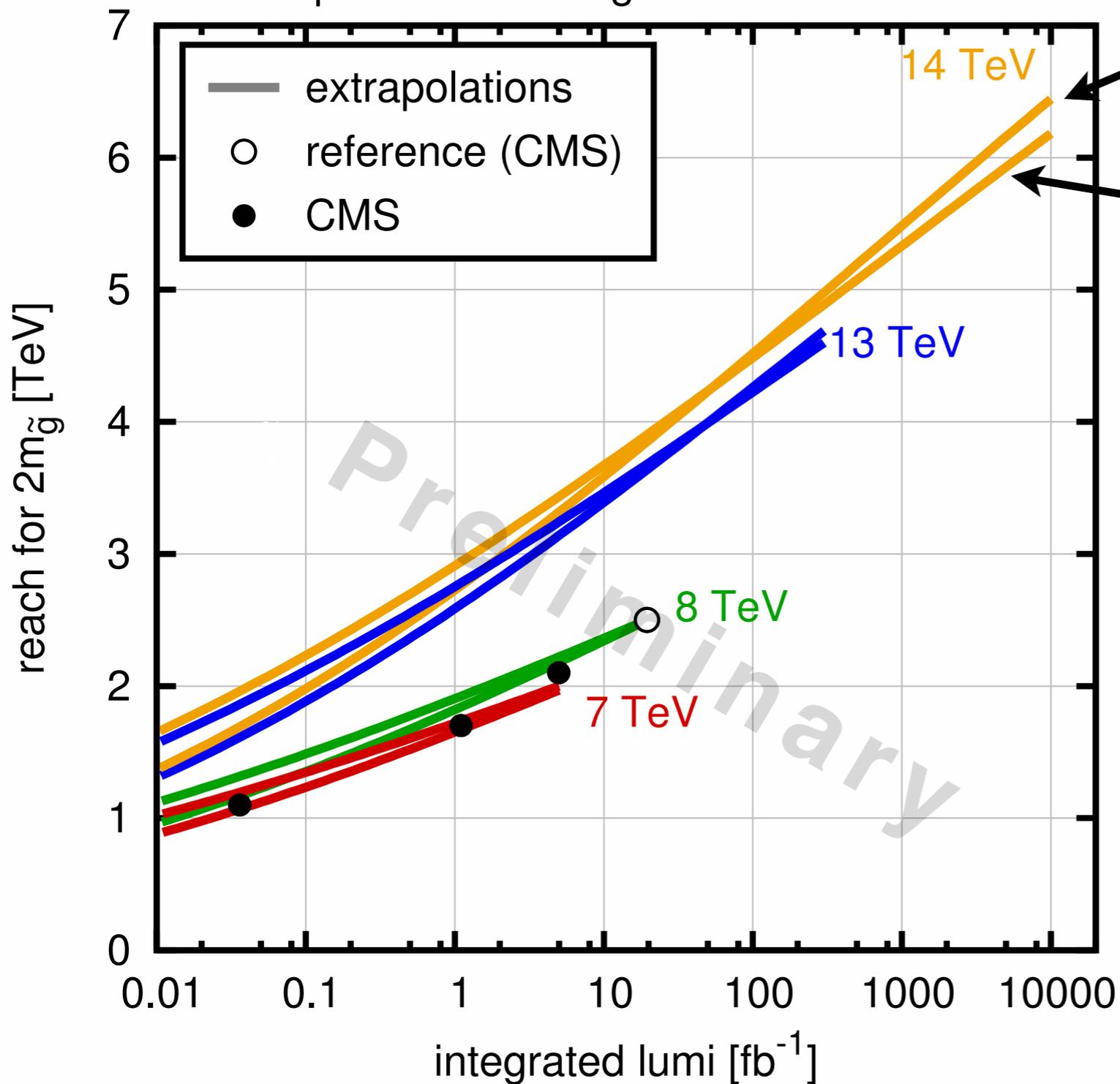
Parton luminosities fall off very fast with increasing M_X

Even when you make a mistake (e.g. wrong partonic channel) the impact on estimated M_X reach is modest

x2 in lumi \sim 10% in M_X

ATLAS						
Search	Signal	Bgd	$E_{\text{CM}}[\text{TeV}]$	$\mathcal{L}_{\text{int}}[\text{fb}^{-1}]$	Expected [GeV]	collider-reach [GeV]
Sequential Z'	$\sum \bar{q}_i q_i$	$\sum \bar{q}_i q_i$	7	0.2	1450 [?]	(base-line)
			7	1.1	1850 [?]	1849
			7	5	2200 [?]	2219
			8	6.1	2550 [?]	2510
			8	20	2900 [?]	2844
Stop ($m_{\text{LSP}} = 0 \text{ GeV}$)	gg	gg	7	4.7	500 [?]	(base-line)
			8	20.5	650 [?]	675
Excited quark	gq	gg	7	$315 \cdot 10^{-6}$	1010 [?]	(base-line)
			7	$36 \cdot 10^{-3}$	2040 [?]	2026 (gq)
			7	$163 \cdot 10^{-3}$	2490 [?]	2395 (gq)
			7	0.81	2910 [?]	2790 (gq)
			7	4.8	3090 [?]	3220 (gq)
			8	13	3840 [?]	3865 (gq)
CMS						
Search	Signal	Bgd	$E_{\text{CM}}[\text{TeV}]$	$\mathcal{L}_{\text{int}}[\text{fb}^{-1}]$	Expected [GeV]	collider-reach [GeV]
gluinos ($m_{\text{LSP}} = 100 \text{ GeV}$)	gg	$gg/gq/qq$	7	0.036	550 [?]	(base-line)
			7	1.1	850 [?]	855
			7	4.98	1050 [?]	1005
			8	19.5	1250 [?]	1275
squarks ($m_{\text{LSP}} = 100 \text{ GeV}$)	gg	$gg/gq/qq$	7	0.036	400 [?]	(base-line)
			7	1.1	650 [?]	663
			7	4.98	725 [?]	801
			8	19.5	910 [?]	1033
T-quarks ($\text{Br}(T \rightarrow tZ) = 1$)	gg	$gg/gq/qq$	7	1.14	510 [?]	(base-line)
			7	5	550 [?]	629
			8	19.6	813 [?]	827

Post/pre-dictions for gluino exclusion reach

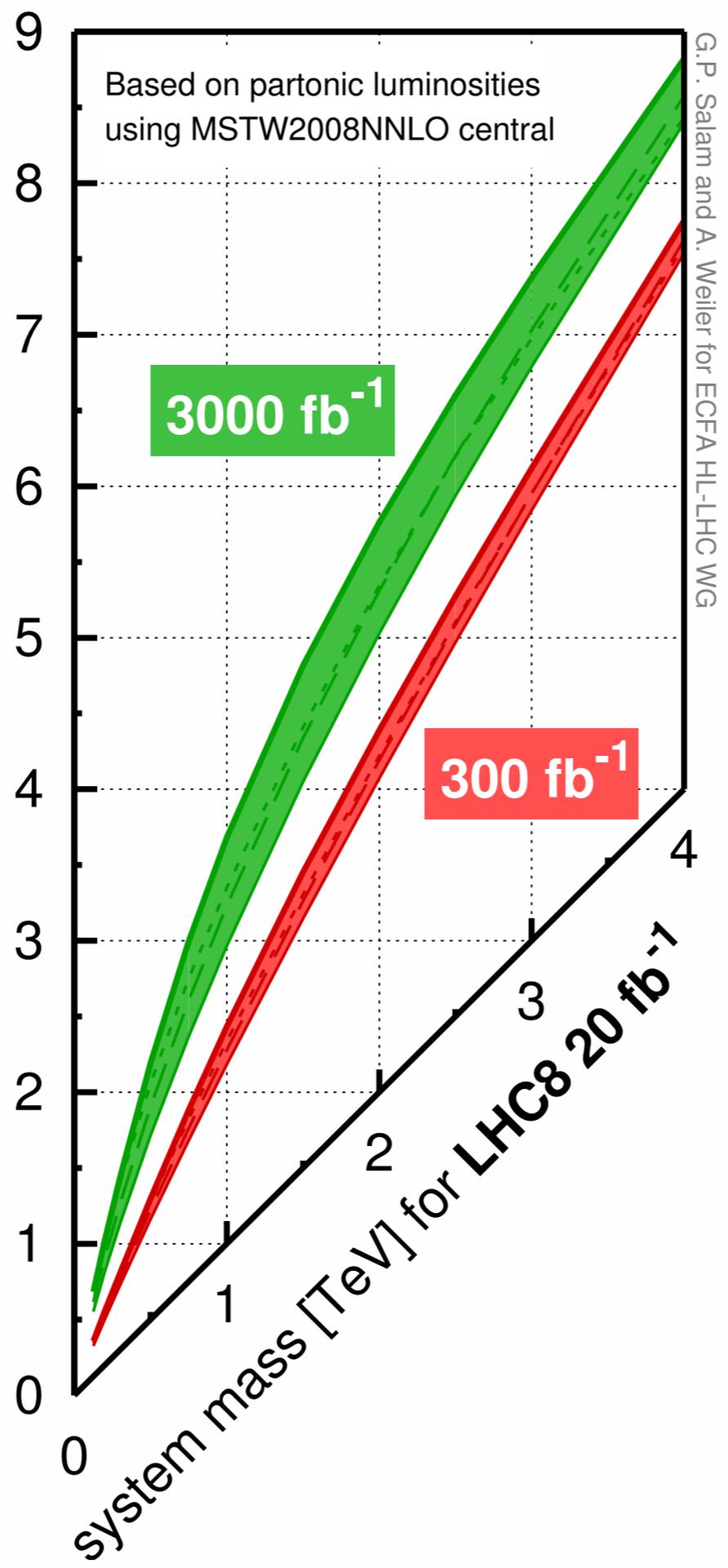


Signal gg ; bkgd: gg

Signal gg ; bkgd: qg

Scattering channel matters, but not too much

system mass [TeV] for LHC14



- $\Sigma\Sigma$
- - Σg
- ... $\Sigma_i q_i \bar{q}_i$
- gg

LHC comparison

1208.1447
ATLAS-CONF-2013-024

gg

stop limits	[expected]	(lsp = 0gev)
7TeV, 4.7 ifb	500 gev	
8TeV, 20.5 ifb	650 gev	----> 675 GeV

qqbar

ATLAS EXOT-2011-06
ATLAS-CONF-2012-129
ATLAS-CONF-2013-017

sequential z-prime	[expected]	
7TeV, 1.1 ifb	1800 gev	
8TeV, 6 ifb,	2550 gev	----> 2450 GeV
8TeV, 20 ifb	2800 gee	----> 2790 GeV

qg

EXOT-2011-07
ATLAS-CONF-2012-088
ATLAS-CONF-2012-148

excited quark q*	[expected]	(NB, sig \neq bgd scaling)
7 TeV, 1 ifb	2900 gev	
8 TeV, 5.8 ifb	3500 gev	----> 3700 GeV
8 TeV, 13 ifb	3700 gev	----> 3900 GeV

LHC comparison

1208.1447
ATLAS-CONF-2013-024

gg
stop limits [expected] (lsp = 0gev) Baseline

7TeV, 4.7 ifb	500 gev	←	
8TeV, 20.5 ifb	650 gev	----	→ 675 GeV

qqbar Baseline

ATLAS EXOT-2011-06
ATLAS-CONF-2012-129
ATLAS-CONF-2013-017

sequential z-prime [expected]

7TeV, 1.1 ifb	1800 gev	←	
8TeV, 6 ifb,	2550 gev	----	→ 2450 GeV
8TeV, 20 ifb	2800 gee	----	→ 2790 GeV

EXOT-2011-07
ATLAS-CONF-2012-088
ATLAS-CONF-2012-148

qq

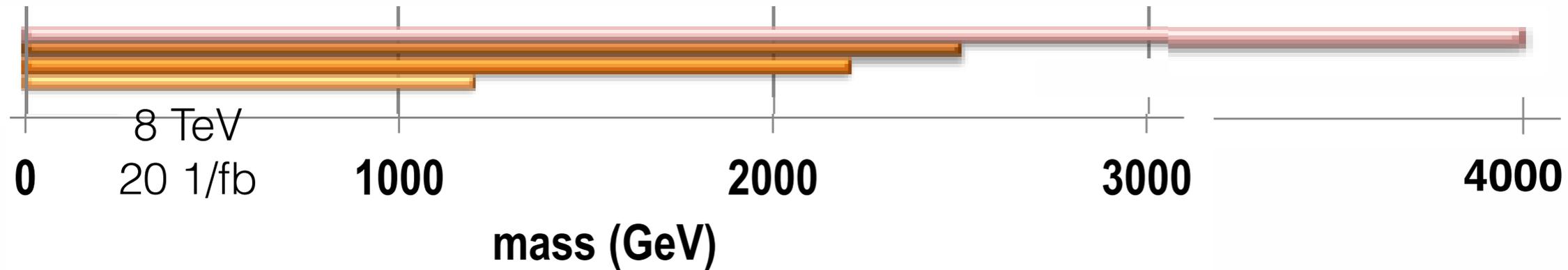
excited quark q* [expected] (NB, sig ≠ bgd scaling)

7 TeV, 1 ifb	2900 gev	←	
8 TeV, 5.8 ifb	3500 gev	----	→ 3700 GeV
8 TeV, 13 ifb	3700 gev	----	→ 3900 GeV

LHC comparison

gg	1208.1447 ATLAS-CONF-2013-024	stop limits	[expected]	(lsp = 0gev)	Baseline
		7TeV, 4.7 ifb	500 gev	←	
		8TeV, 20.5 ifb	650 gev	----> 675 GeV	
qqbar	ATLAS EXOT-2011-06 ATLAS-CONF-2012-129 ATLAS-CONF-2013-017	sequential z-prime	[expected]		Lumi method
		7TeV, 1.1 ifb	1800 gev	←	
		8TeV, 6 ifb,	2550 gev	----> 2450 GeV	
		8TeV, 20 ifb	2800 gee	----> 2790 GeV	
qq	EXOT-2011-07 ATLAS-CONF-2012-088 ATLAS-CONF-2012-148	excited quark q*	[expected]	(NB, sig ≠ bgd scaling)	
		7 TeV, 1 ifb	2900 gev	←	
		8 TeV, 5.8 ifb	3500 gev	----> 3700 GeV	
		8 TeV, 13 ifb	3700 gev	----> 3900 GeV	

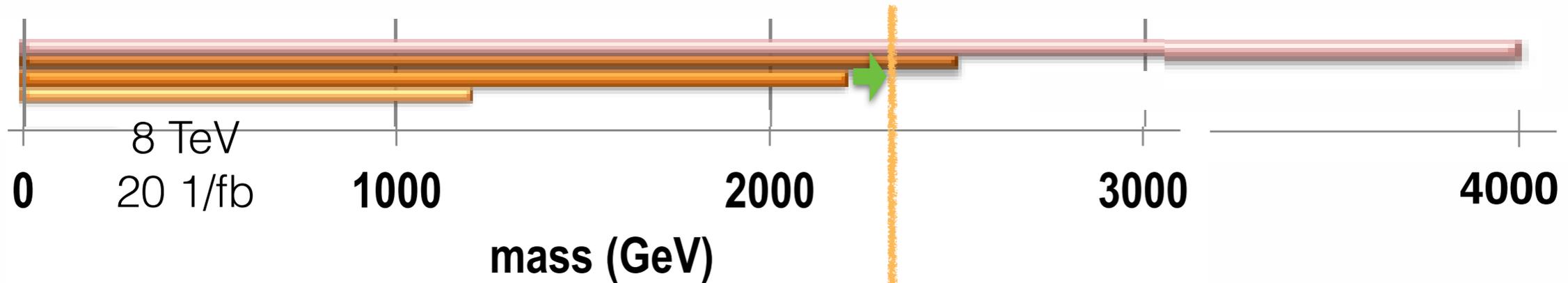
Gluinos



- pp, 100 TeV, 3000/fb
- pp, 33 TeV, 3000/fb
- pp, 14 TeV, 3000/fb
- pp, 14 TeV, 300/fb
- pp, 8 TeV, 20/fb
- ee, 3 TeV, 1000/fb
- ee, 1 TeV, 1000/fb
- ee, 0.5 TeV, 500/fb

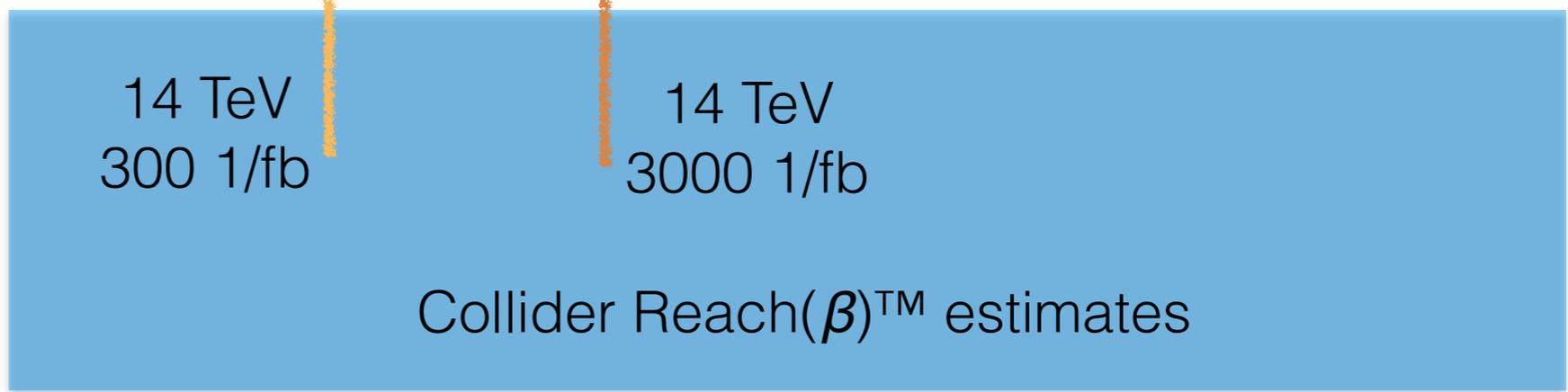
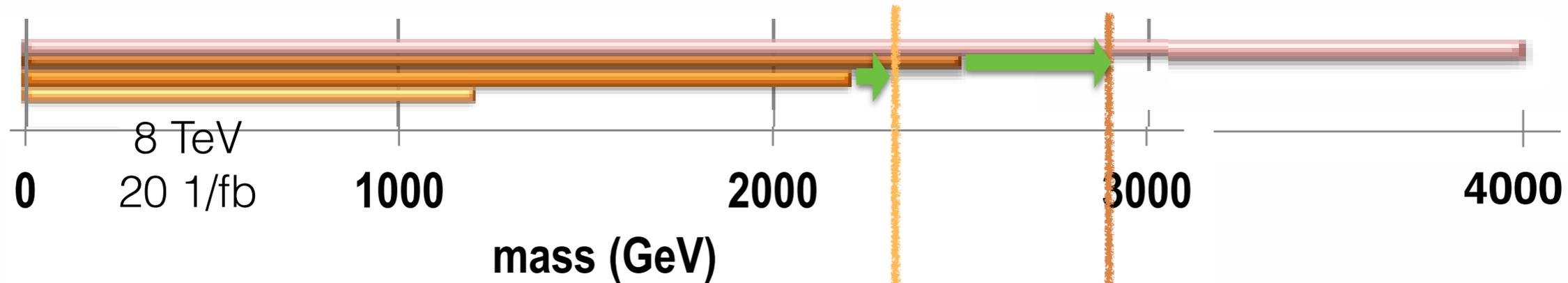
Collider Reach(β)TM estimates

Gluinos



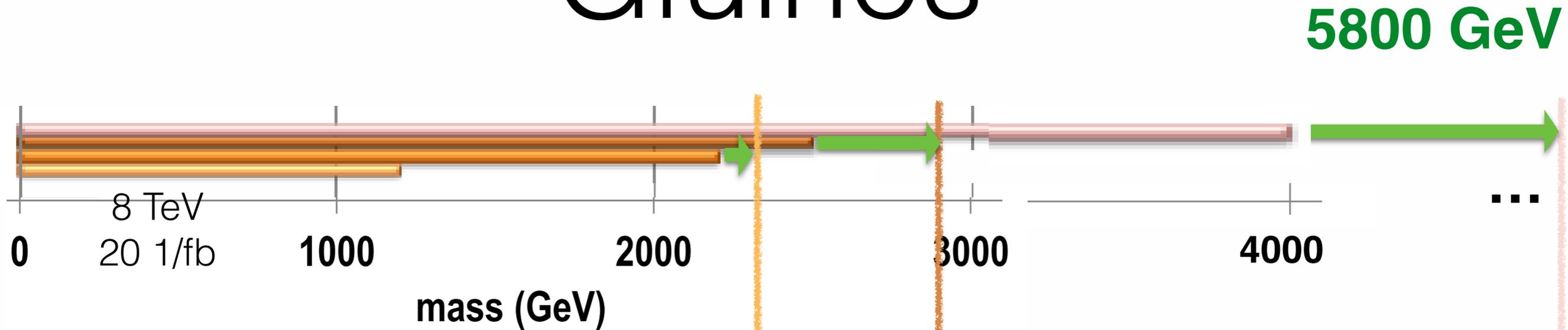
- pp, 100 TeV, 3000/fb
- pp, 33 TeV, 3000/fb
- pp, 14 TeV, 3000/fb
- pp, 14 TeV, 300/fb
- pp, 8 TeV, 20/fb
- ee, 3 TeV, 1000/fb
- ee, 1 TeV, 1000/fb
- ee, 0.5 TeV, 500/fb

Gluinos



- pp, 100 TeV, 3000/fb
- pp, 33 TeV, 3000/fb
- pp, 14 TeV, 3000/fb
- pp, 14 TeV, 300/fb
- pp, 8 TeV, 20/fb
- ee, 3 TeV, 1000/fb
- ee, 1 TeV, 1000/fb
- ee, 0.5 TeV, 500/fb

Gluinos



14 TeV
300 1/fb

14 TeV
3000 1/fb

33 TeV
3000 1/fb

■ pp, 100 TeV, 3000/fb

■ pp, 33 TeV, 3000/fb

■ pp, 14 TeV, 3000/fb

■ pp, 14 TeV, 300/fb

■ pp, 8 TeV, 20/fb

■ ee, 3 TeV, 1000/fb

■ ee, 1 TeV, 1000/fb

■ ee, 0.5 TeV, 500/fb

Collider Reach(β)TM estimates

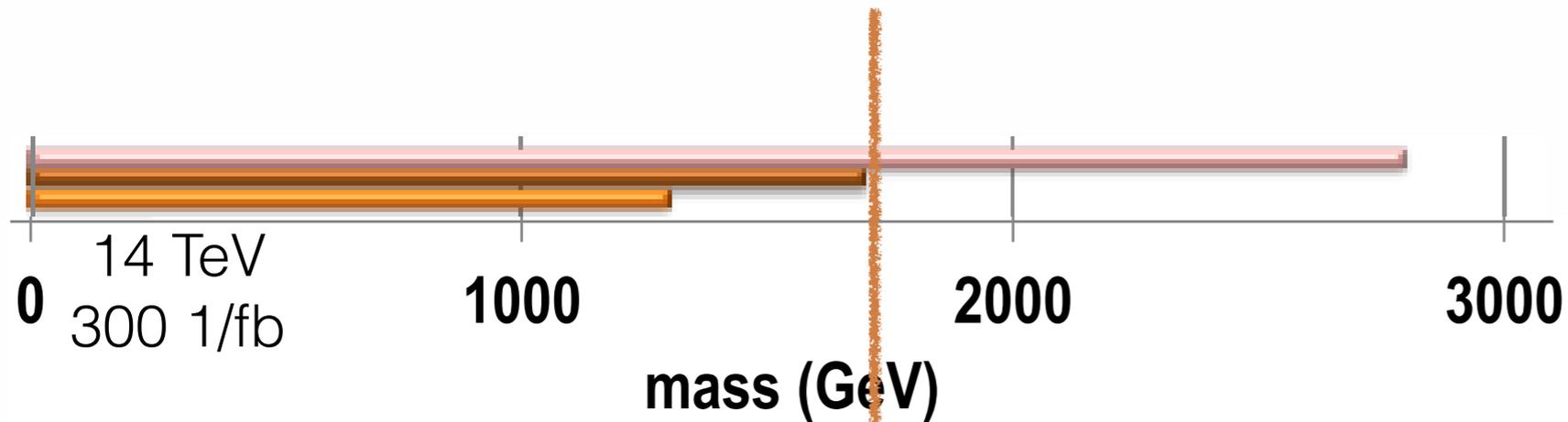
RPV stops



- pp, 100 TeV, 3000/fb
- pp, 33 TeV, 3000/fb
- pp, 14 TeV, 3000/fb
- pp, 14 TeV, 300/fb
- pp, 8 TeV, 20/fb
- ee, 3 TeV, 1000/fb
- ee, 1 TeV, 1000/fb
- ee, 0.5 TeV, 500/fb

Collider Reach(β)TM estimates

RPV stops

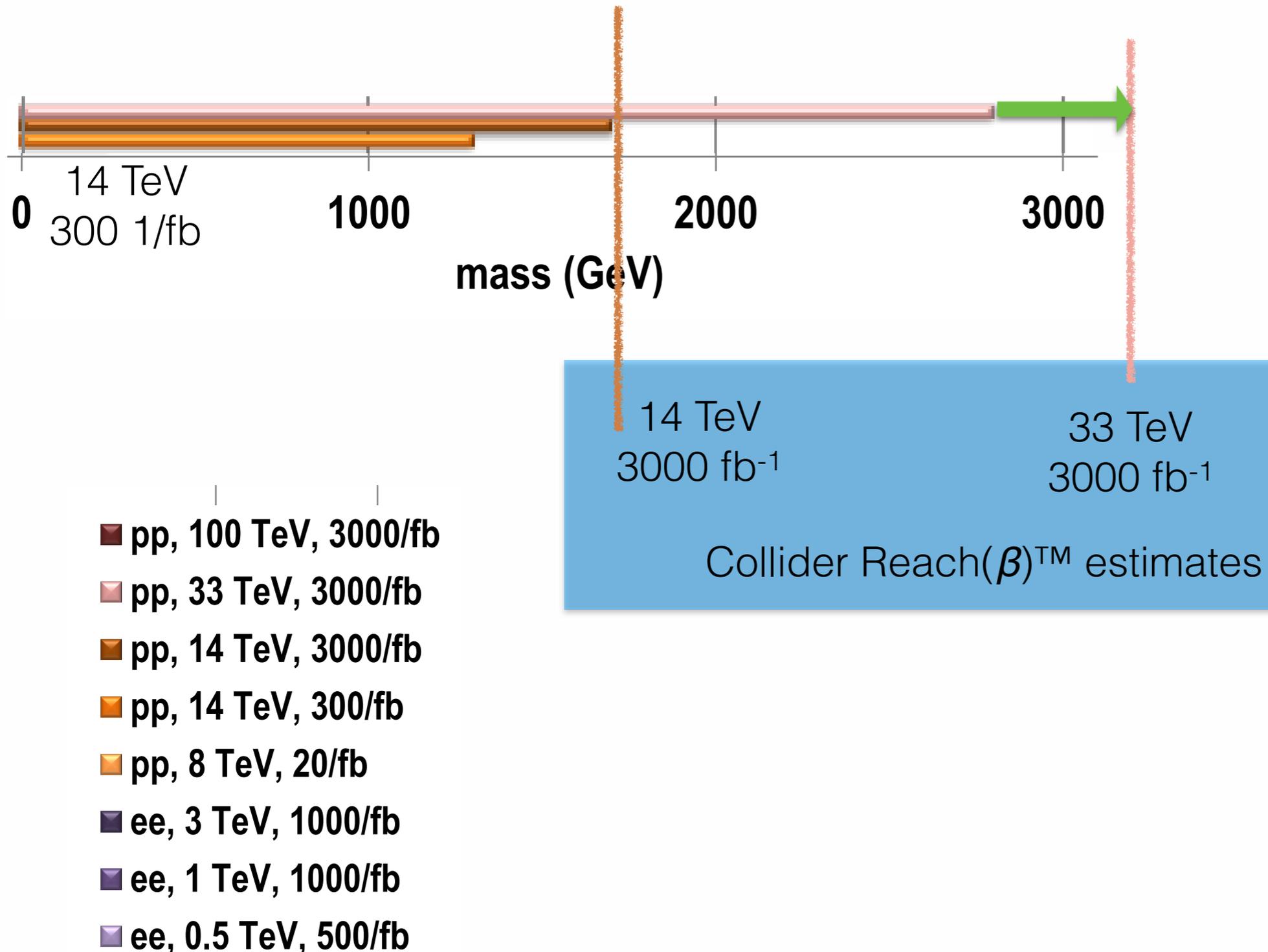


14 TeV
3000 fb⁻¹

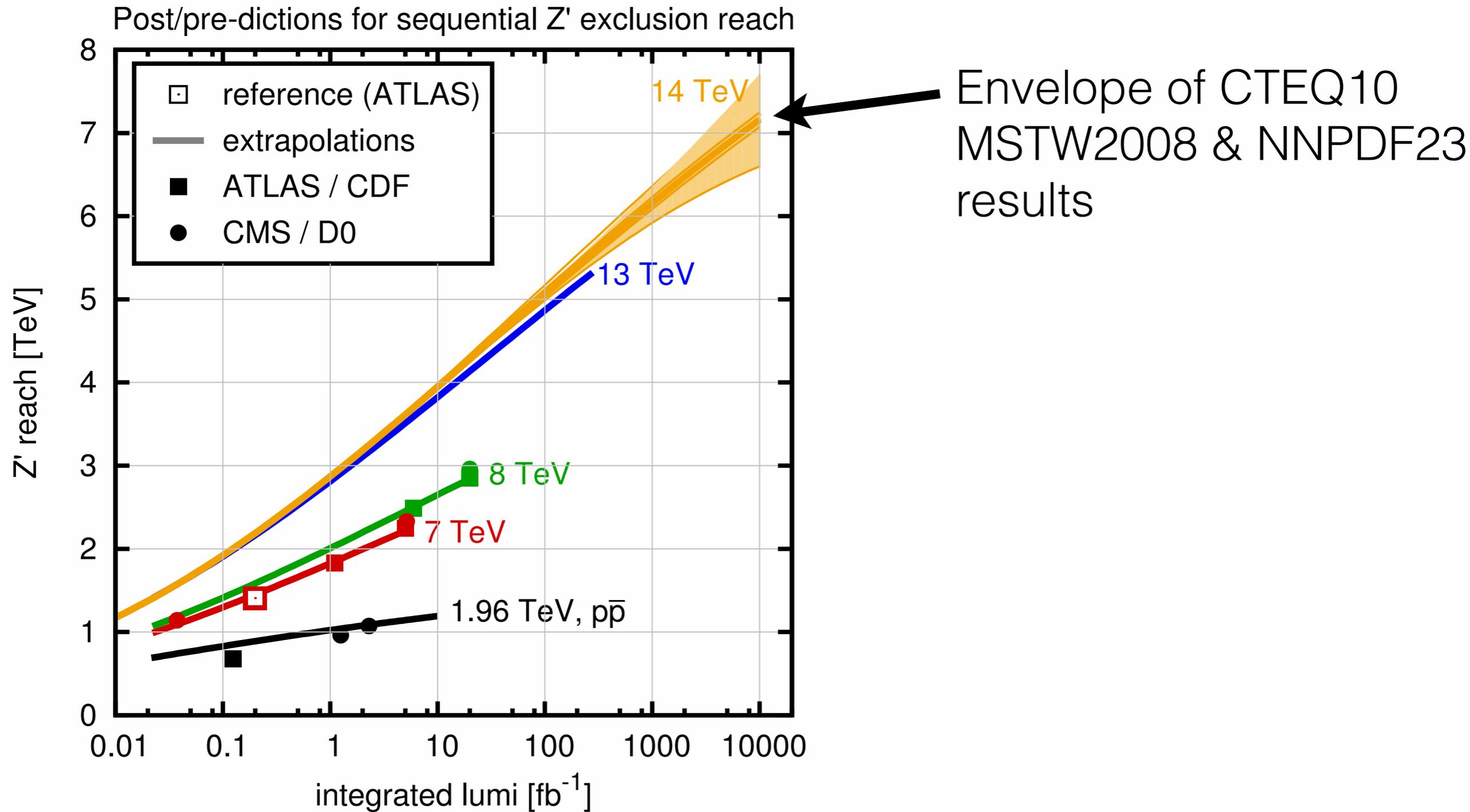
Collider Reach(β)TM estimates

- pp, 100 TeV, 3000/fb
- pp, 33 TeV, 3000/fb
- pp, 14 TeV, 3000/fb
- pp, 14 TeV, 300/fb
- pp, 8 TeV, 20/fb
- ee, 3 TeV, 1000/fb
- ee, 1 TeV, 1000/fb
- ee, 0.5 TeV, 500/fb

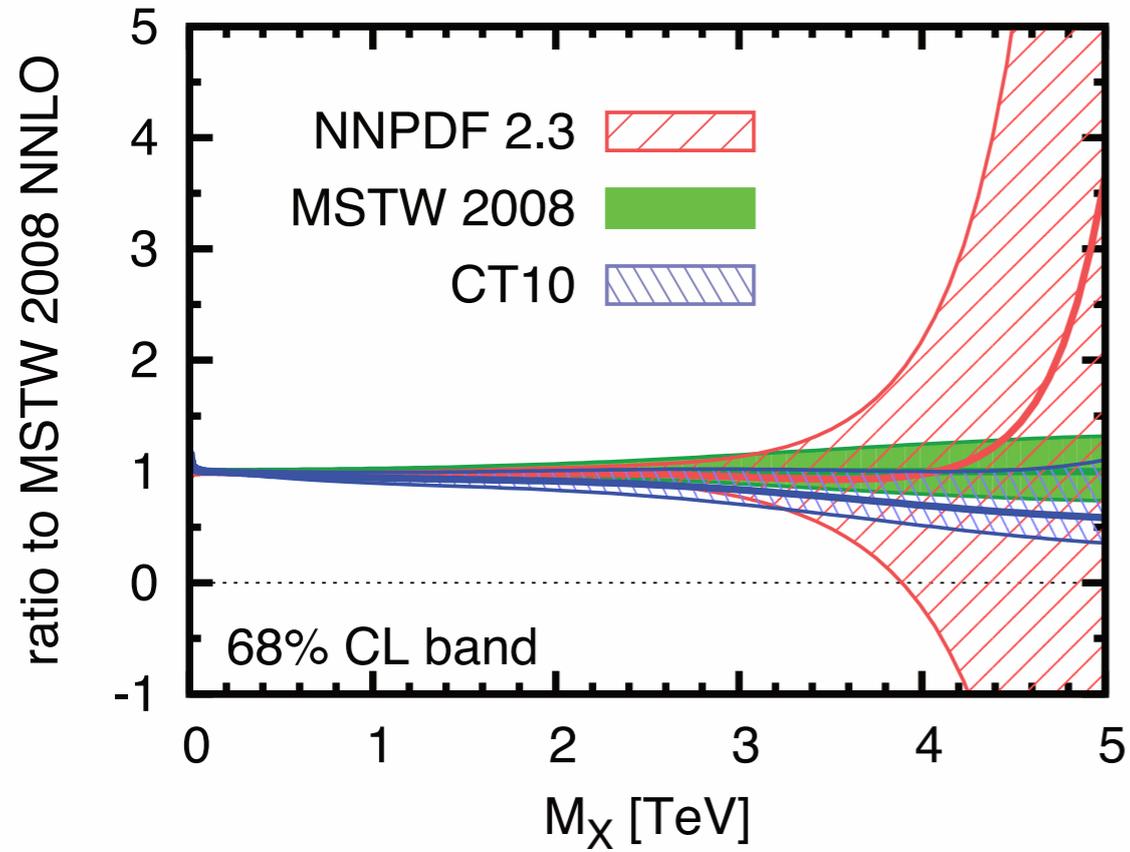
RPV stops



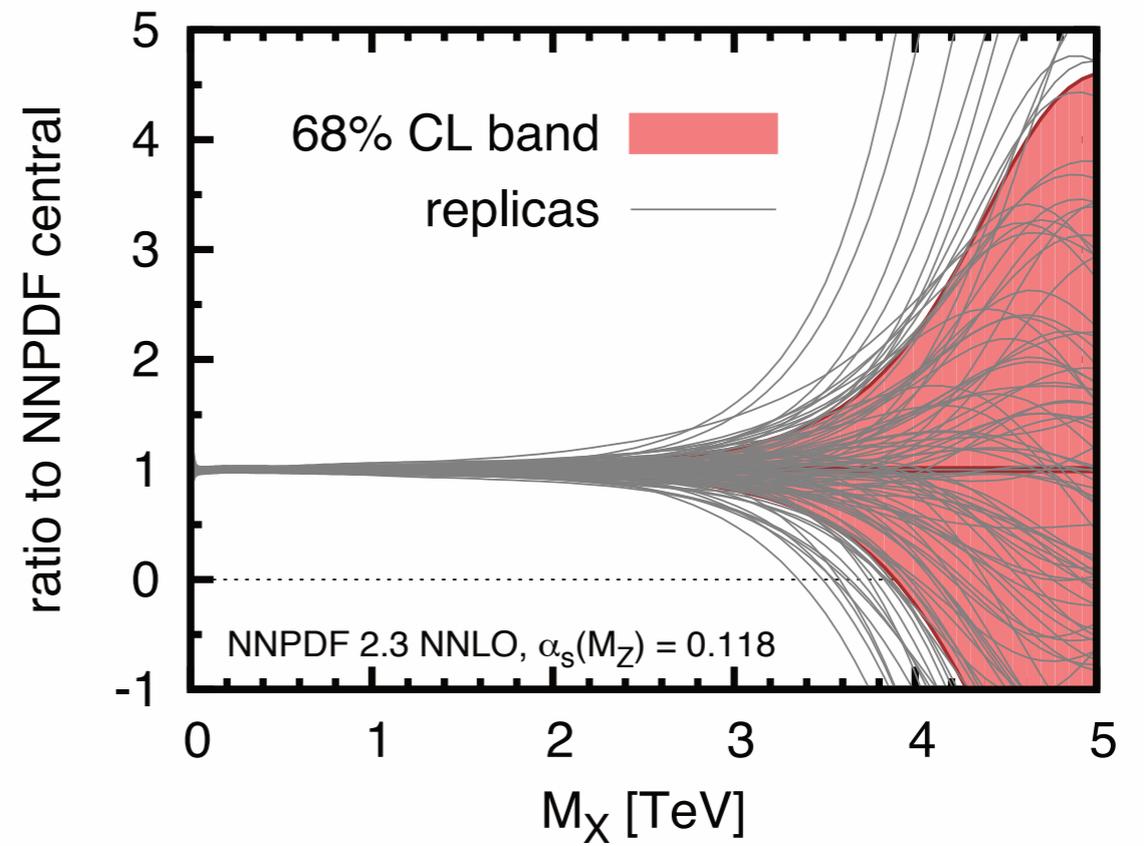
Impact of PDF uncertainties



NNLO $q\bar{q}$ luminosities (LHC 8 TeV)



NNPDF $q\bar{q}$ luminosity replicas (LHC 8 TeV)



$q\bar{q}/qq$ luminosity ratios (LHC 8 TeV)

