



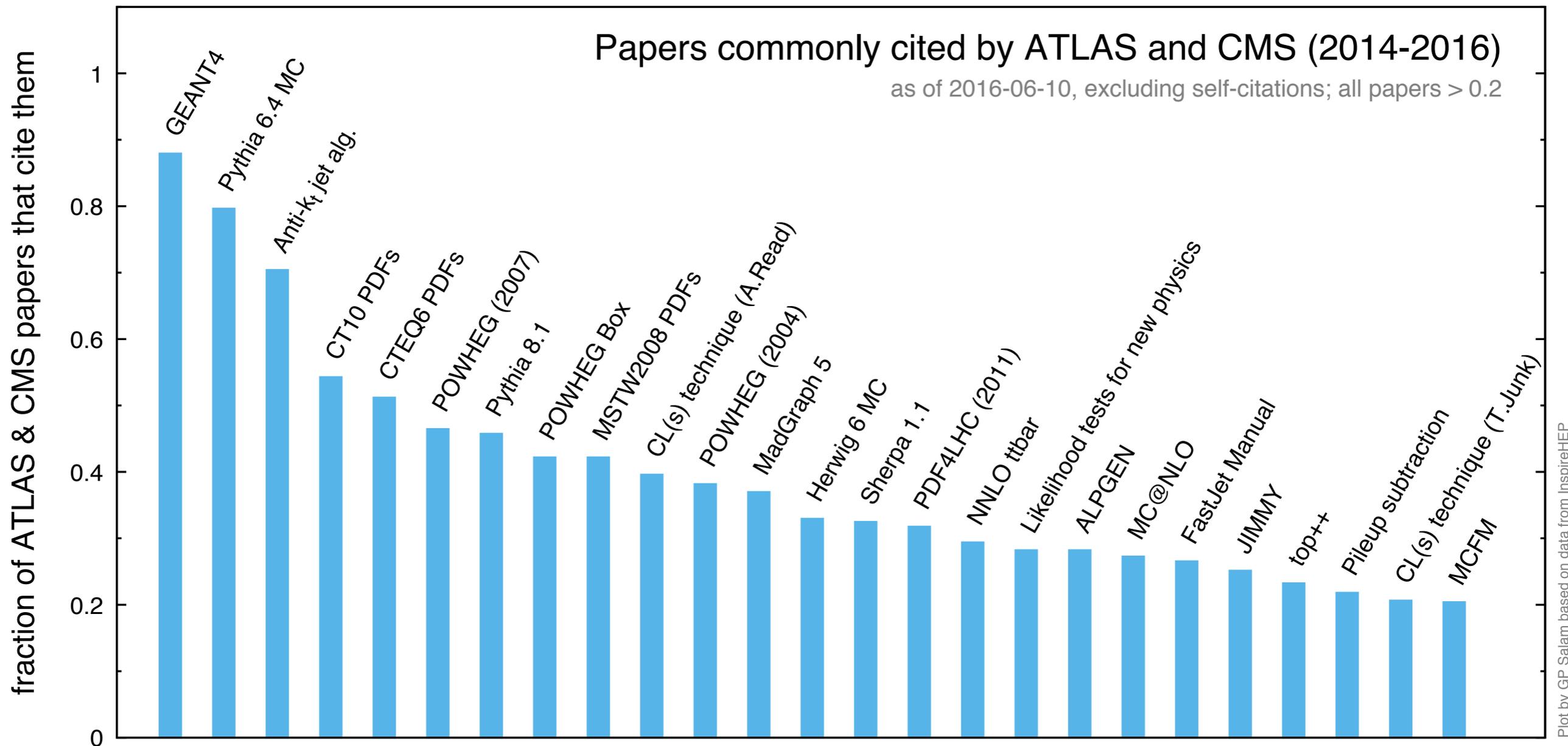
# QCD THEORY OVERVIEW TOWARDS PRECISION AT LHC

Gavin Salam, CERN

Fourth Annual Large Hadron Collider Physics Conference  
14 June 2016, Lund, Sweden

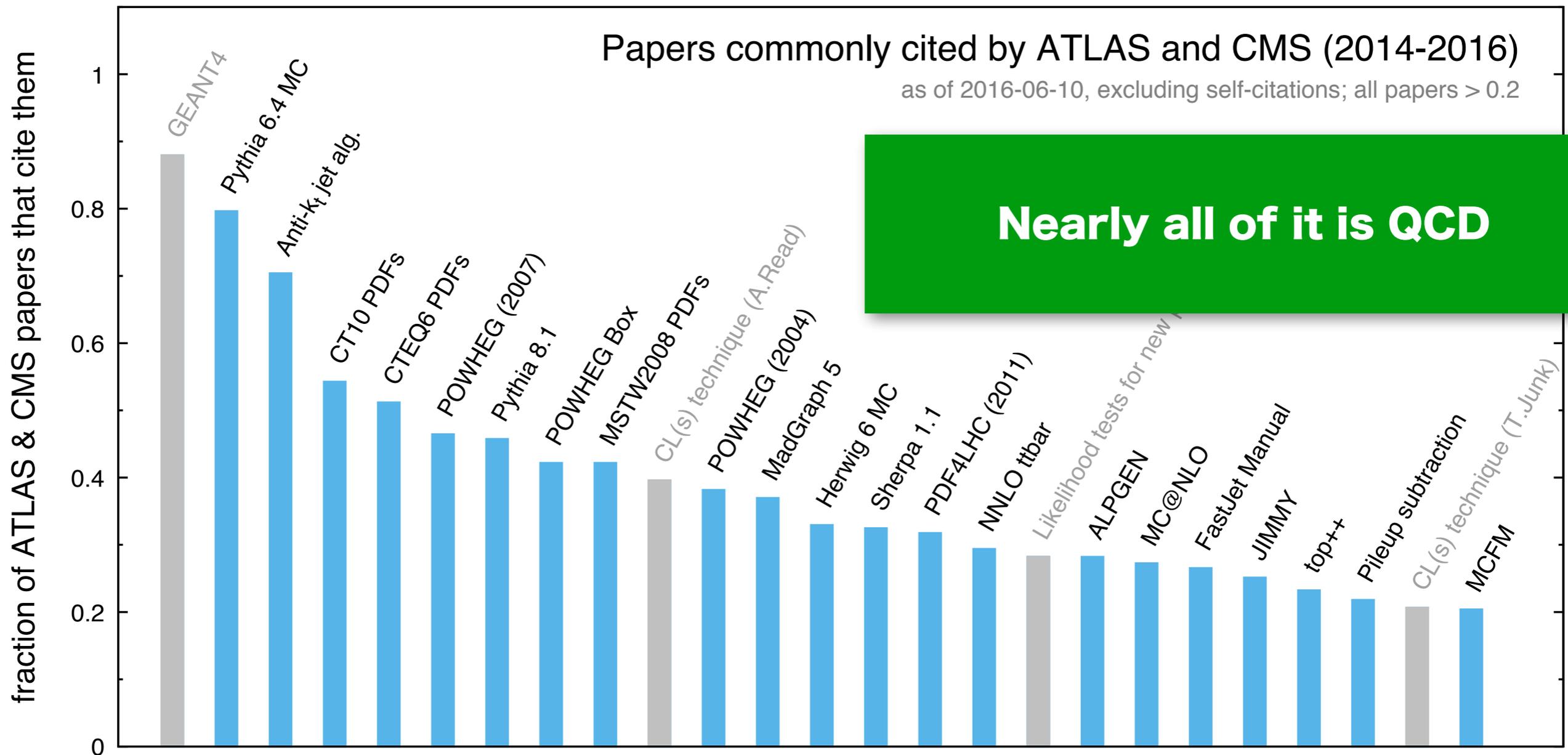


# WHAT DO ATLAS & CMS USE MOST FREQUENTLY?

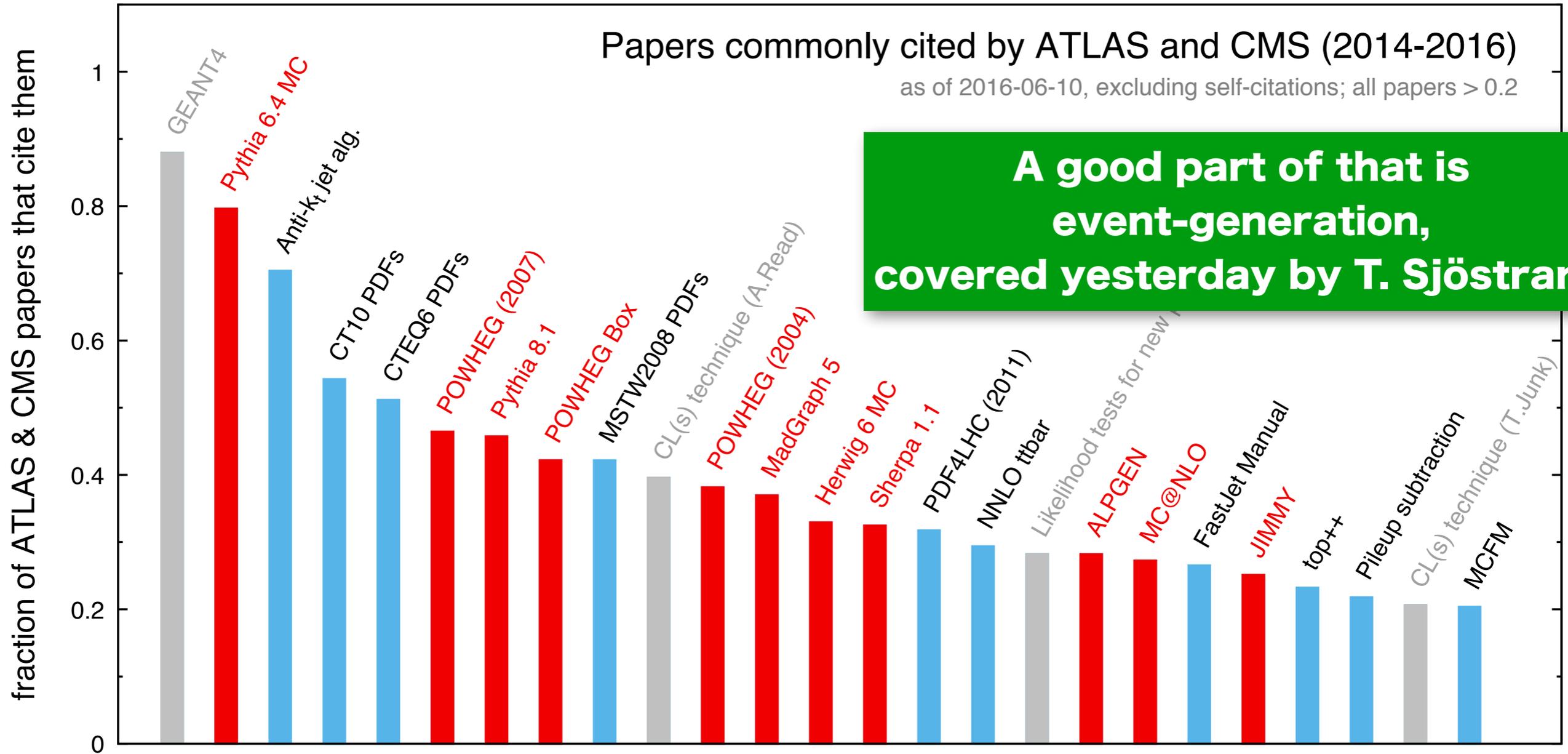


Plot by GP Salam based on data from InspireHEP

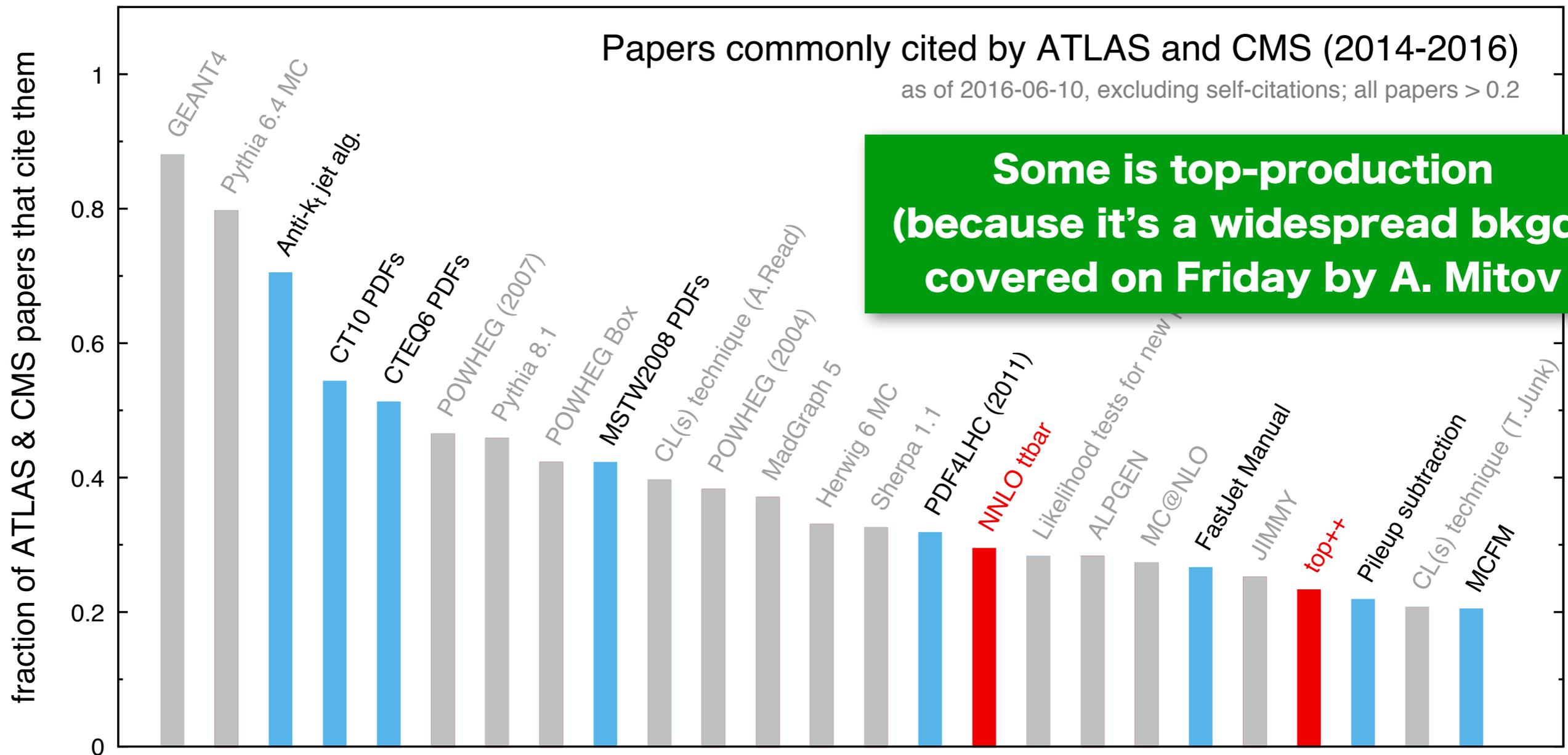
# WHAT DO ATLAS & CMS USE MOST FREQUENTLY?



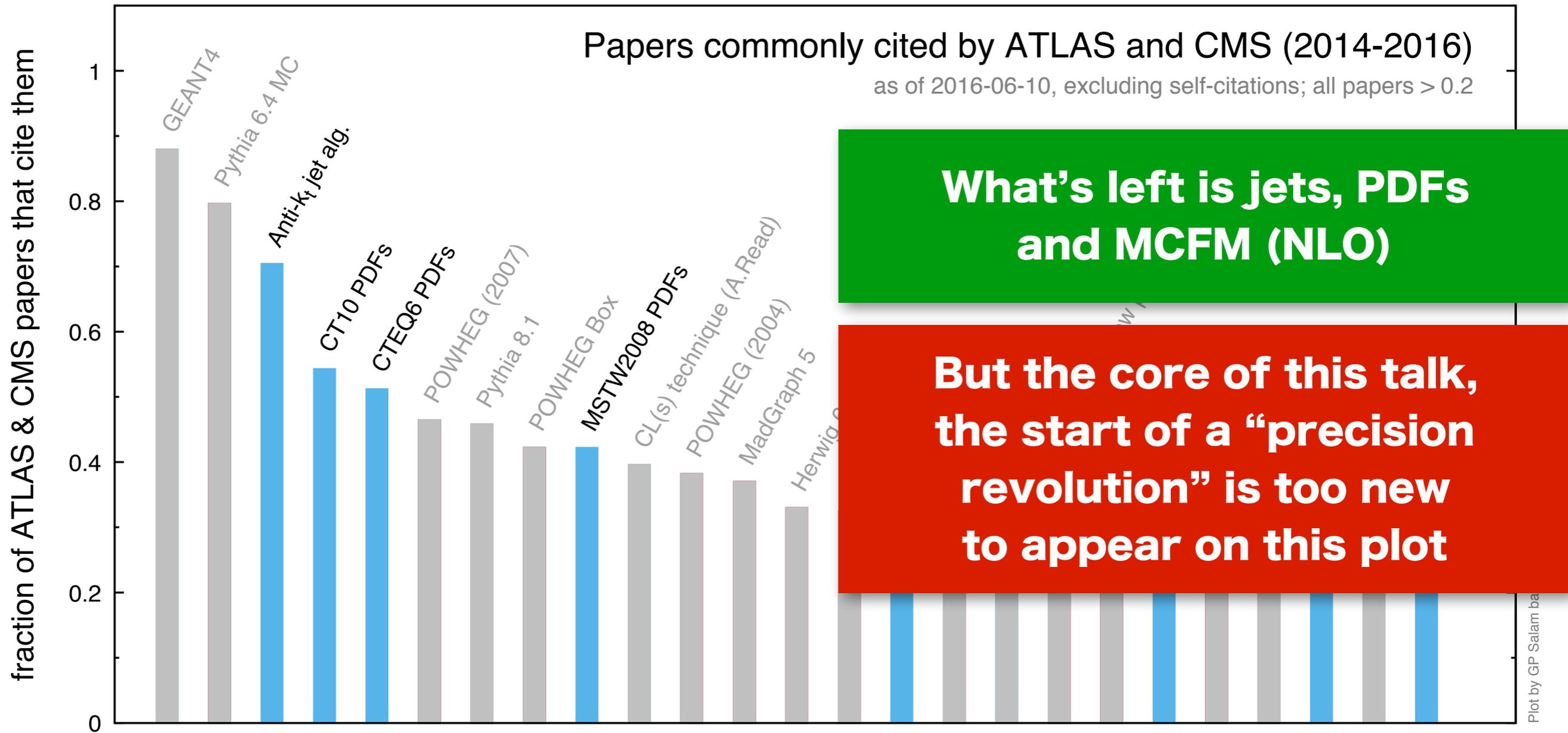
# WHAT DO ATLAS & CMS USE MOST FREQUENTLY?



# WHAT DO ATLAS & CMS USE MOST FREQUENTLY?



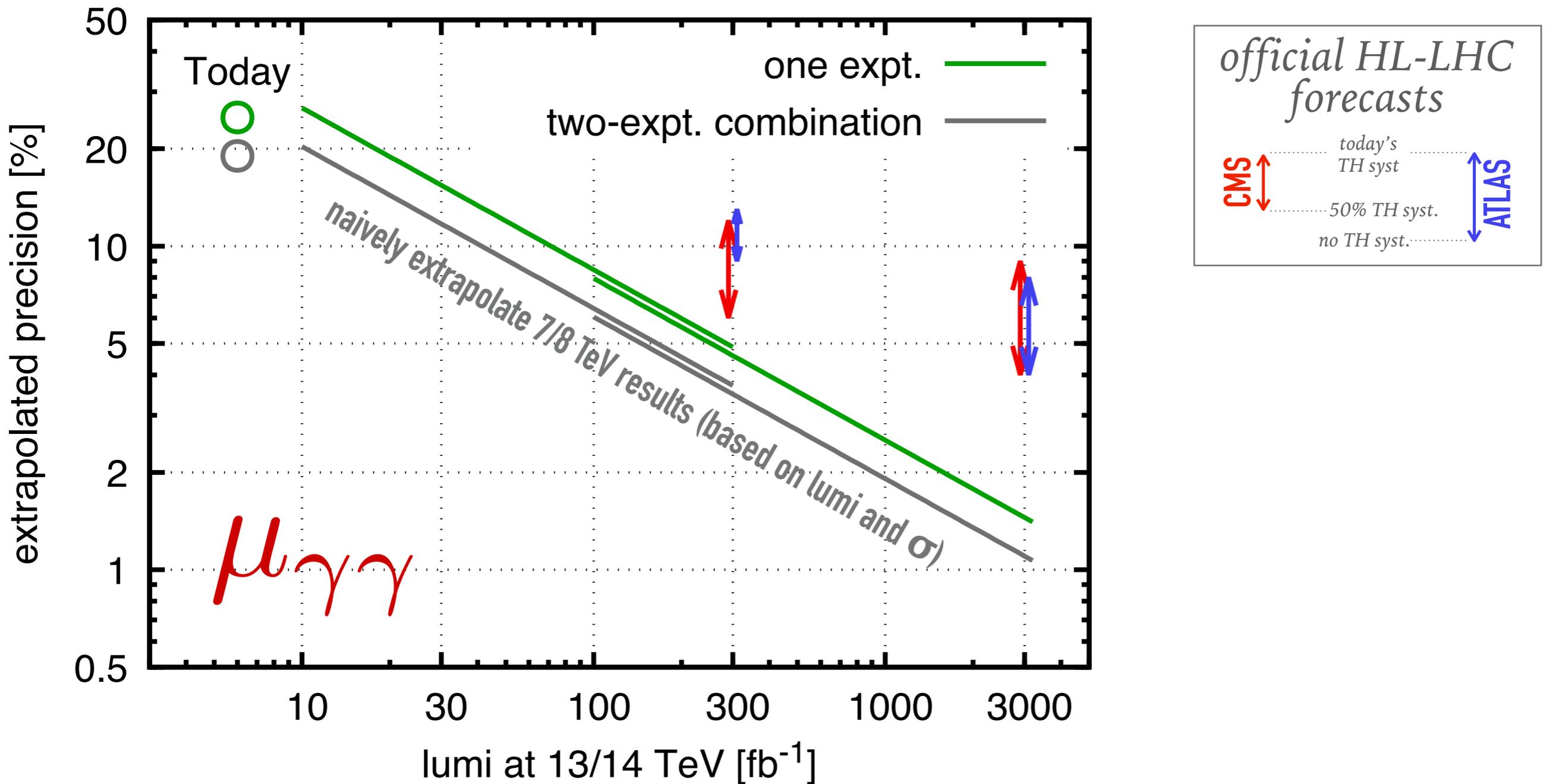
# WHAT DO ATLAS & CMS USE MOST FREQUENTLY?



**what precision will we want?**

**what precision do we have?**

# LONG-TERM HIGGS PRECISION?



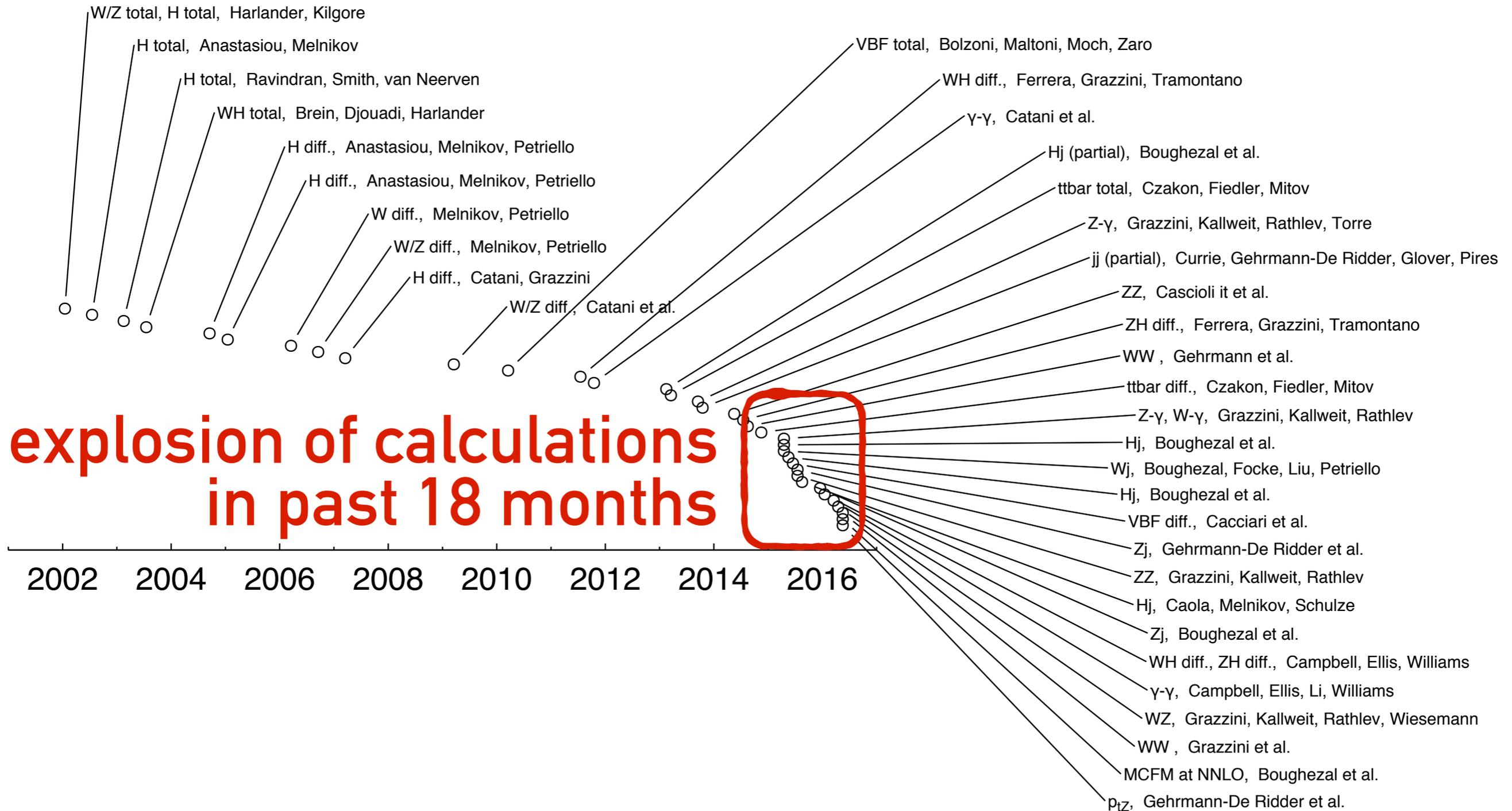
Naive extrapolation suggests LHC has long-term potential to do Higgs physics at **1% accuracy**

**nnlo**

---

# NNLO hadron-collider calculations v. time

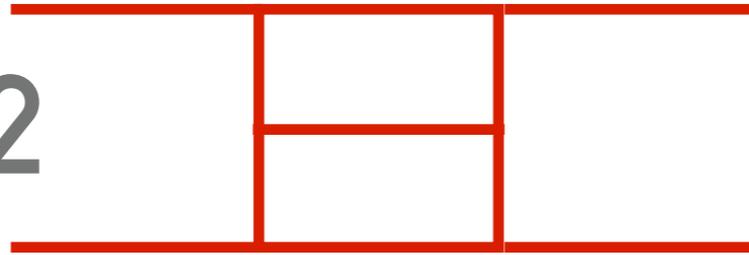
*let me know of any significant omissions*



# NNLO INGREDIENTS (for a $2 \rightarrow 2$ process)

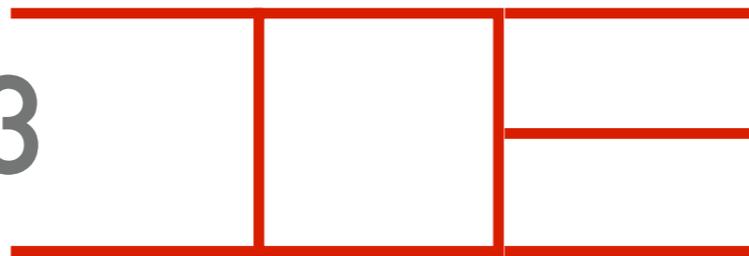
---

2-loop  $2 \rightarrow 2$



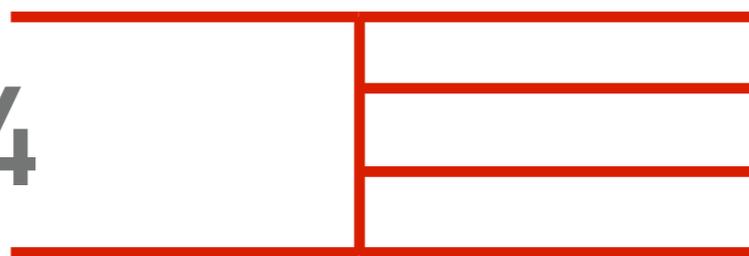
calculations here  
enabled  
 $pp \rightarrow VV$

1-loop  $2 \rightarrow 3$



within scope of  
existing tools

tree  $2 \rightarrow 4$



ideas for handling  
sum of singularities  
enabled  
 $pp \rightarrow X + \text{jet}(s)$

-----  
**sum**

# Combining 2-loops / 1-loop / tree

---

$f(z)$  is some function with finite limit for  $z \rightarrow 0$

## “SLICING”

$$\sigma = \left( c - \ln \frac{1}{\text{cut}} \right) \cdot f(0) + \int_{\text{cut}}^1 dz \frac{f(z)}{z}$$

*virtual & counterterm:  
get from soft-collinear  
resummation*

*real part:  
use MC integration  
(cut has to be small,  
but not too small)*

qT-subtraction: Catani, Grazzini

N-jettiness subtraction: Boughezal, Focke, Liu, Petriello; Gaunt, Stahlhofen, Tackmann, Walsh

# Combining 2-loops / 1-loop / tree

---

$f(z)$  is some function with finite limit for  $z \rightarrow 0$

## LOCAL SUBTRACTION

$$\sigma = c \cdot f(0) + \int_0^1 dz \left[ \frac{f(z)}{z} - \frac{f(0)}{z} \right]$$

*virtual & counterterm:*

*may need (tough)*

*analytic calc<sup>n</sup>*

*real part:*

*MC integration is finite*

*even without cut*

Sector decomposition: Anastasiou, Melnikov, Petriello; Binoth, Heinrich

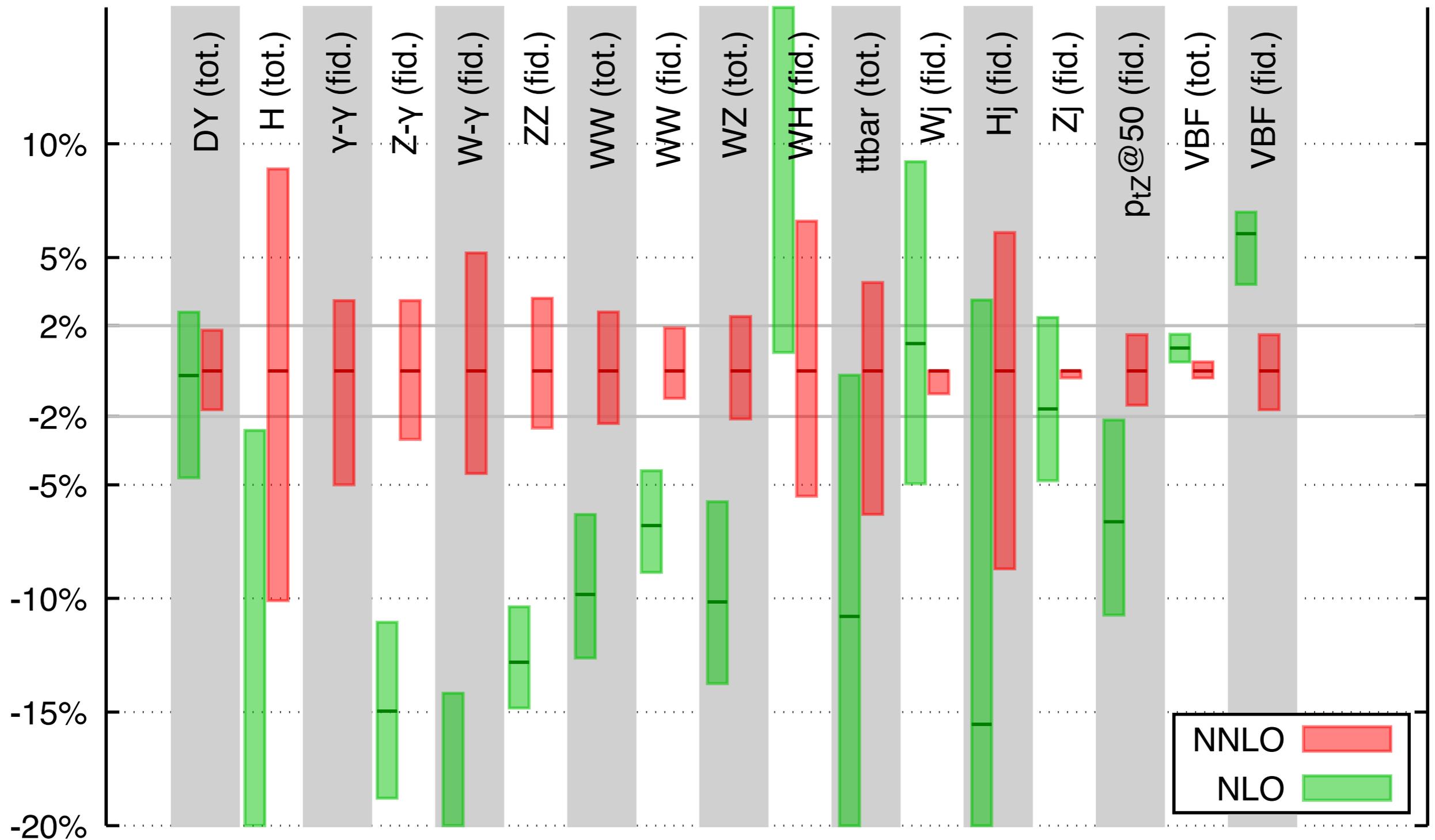
Antennae subtraction: Kosower; Gehrmann, Gehrmann-de Ridder, Glover

Sector-improved residue subtraction: Czakon; Boughezal, Melnikov, Petriello

CoLorFul subtraction: Del Duca, Somogyi, Trocsanyi

Projection-to-Born: Cacciari, Dreyer, Karlberg, GPS, Zanderighi

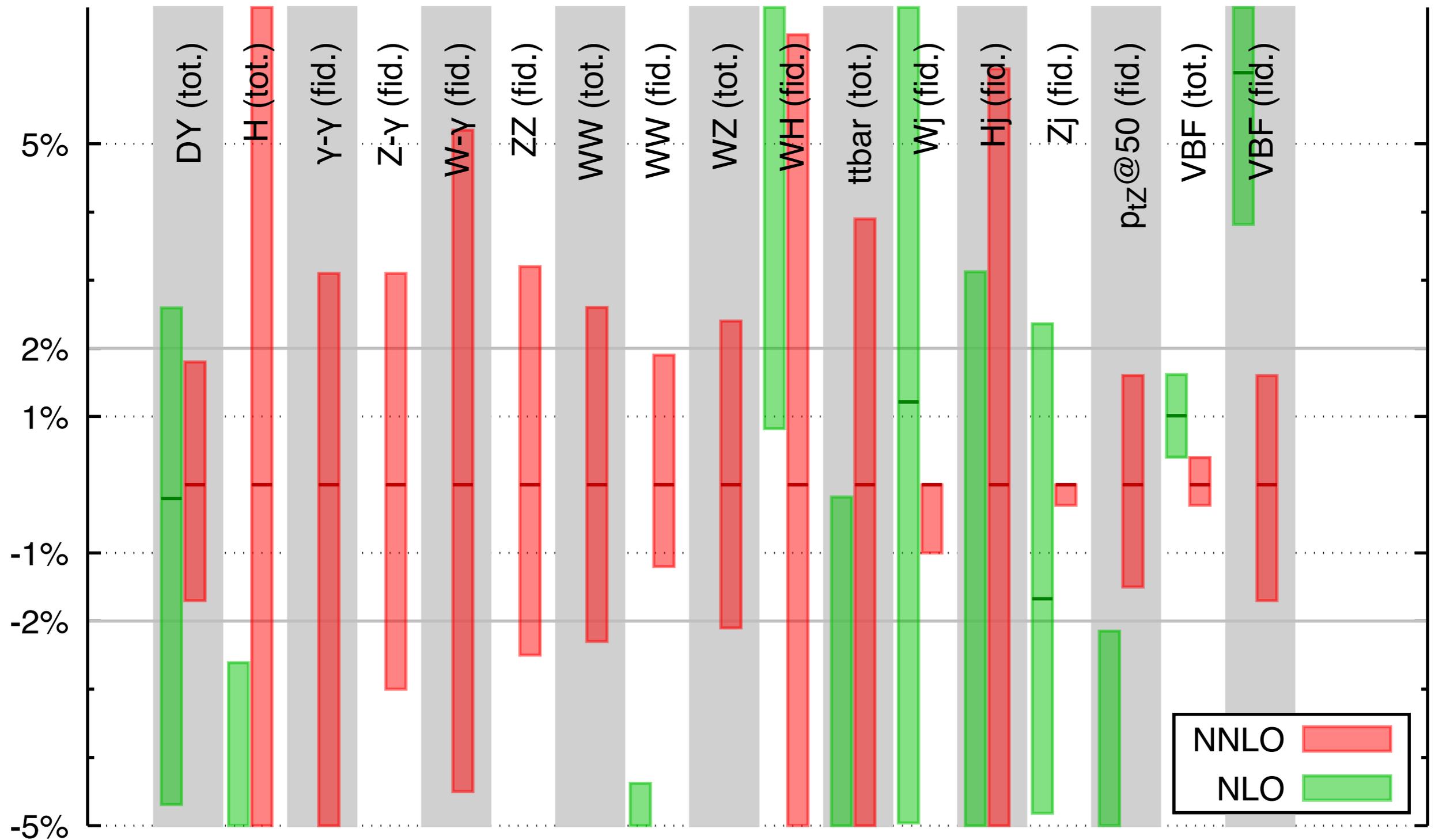
# WHAT PRECISION AT NNLO?



For many processes NNLO scale band is  $\sim \pm 2\%$

But only in 3/17 cases is NNLO (central) within NLO scale band...

# WHAT PRECISION AT NNLO?



For many processes NNLO scale band is  $\sim \pm 2\%$

But only in 3/17 cases is NNLO (central) within NLO scale band...

# n<sup>3</sup>lo

**Higgs via  
gluon fusion**

**Higgs via  
weak-boson  
fusion**

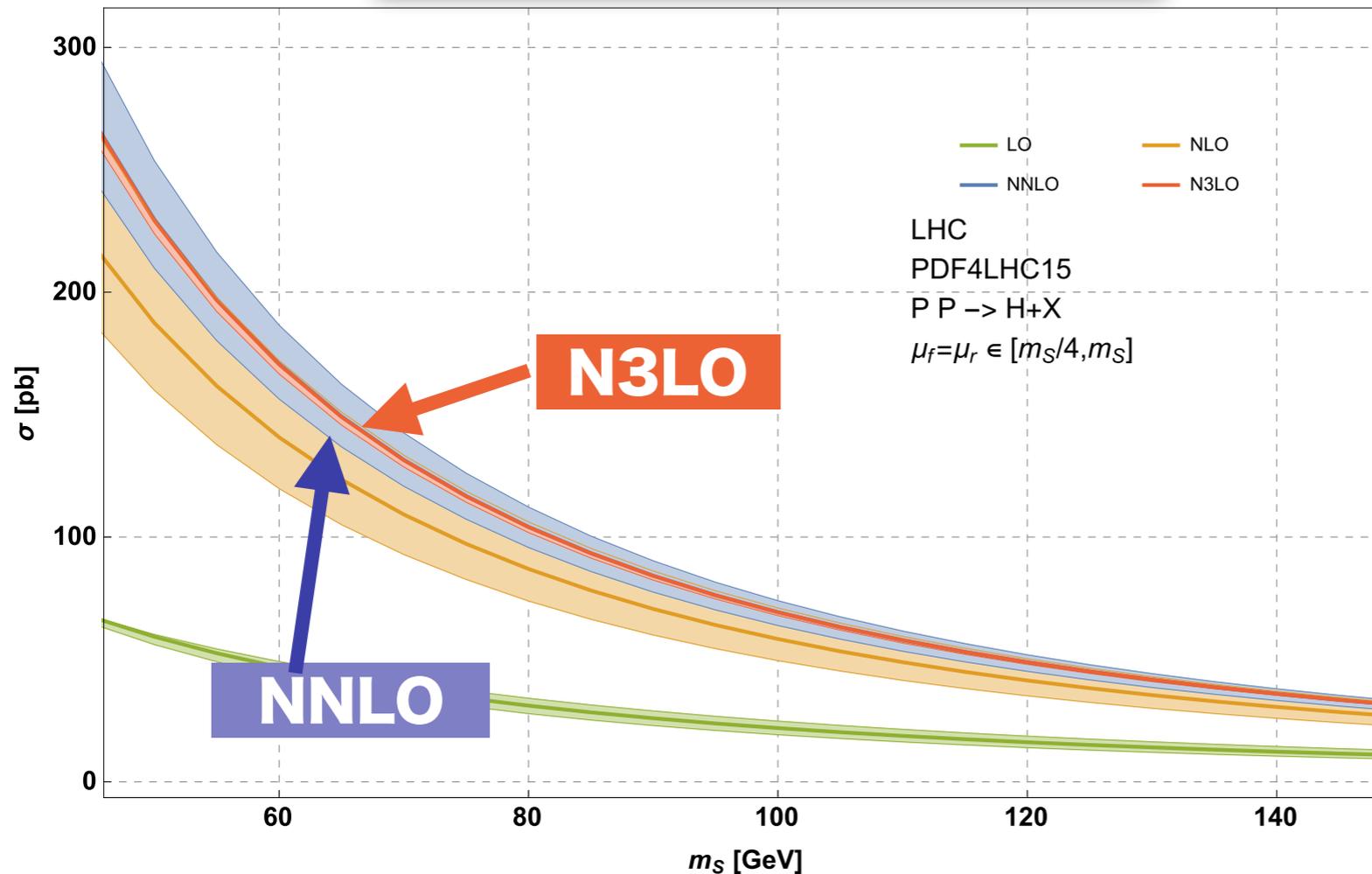
**PDFs?**

# N3LO CONVERGENCE?

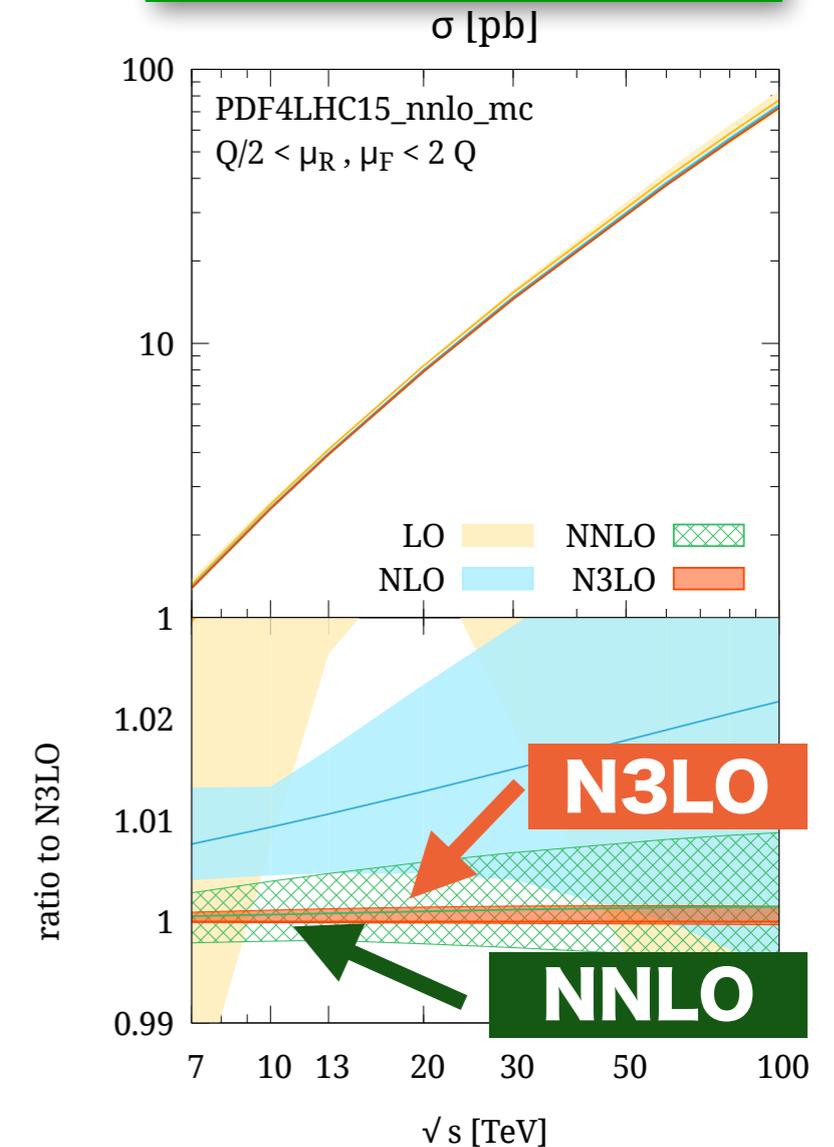
Anastasiou et al, 1602.00695

Dreyer & Karlberg, 1606.00840

## N3LO ggF Higgs



## N3LO VBF Higgs



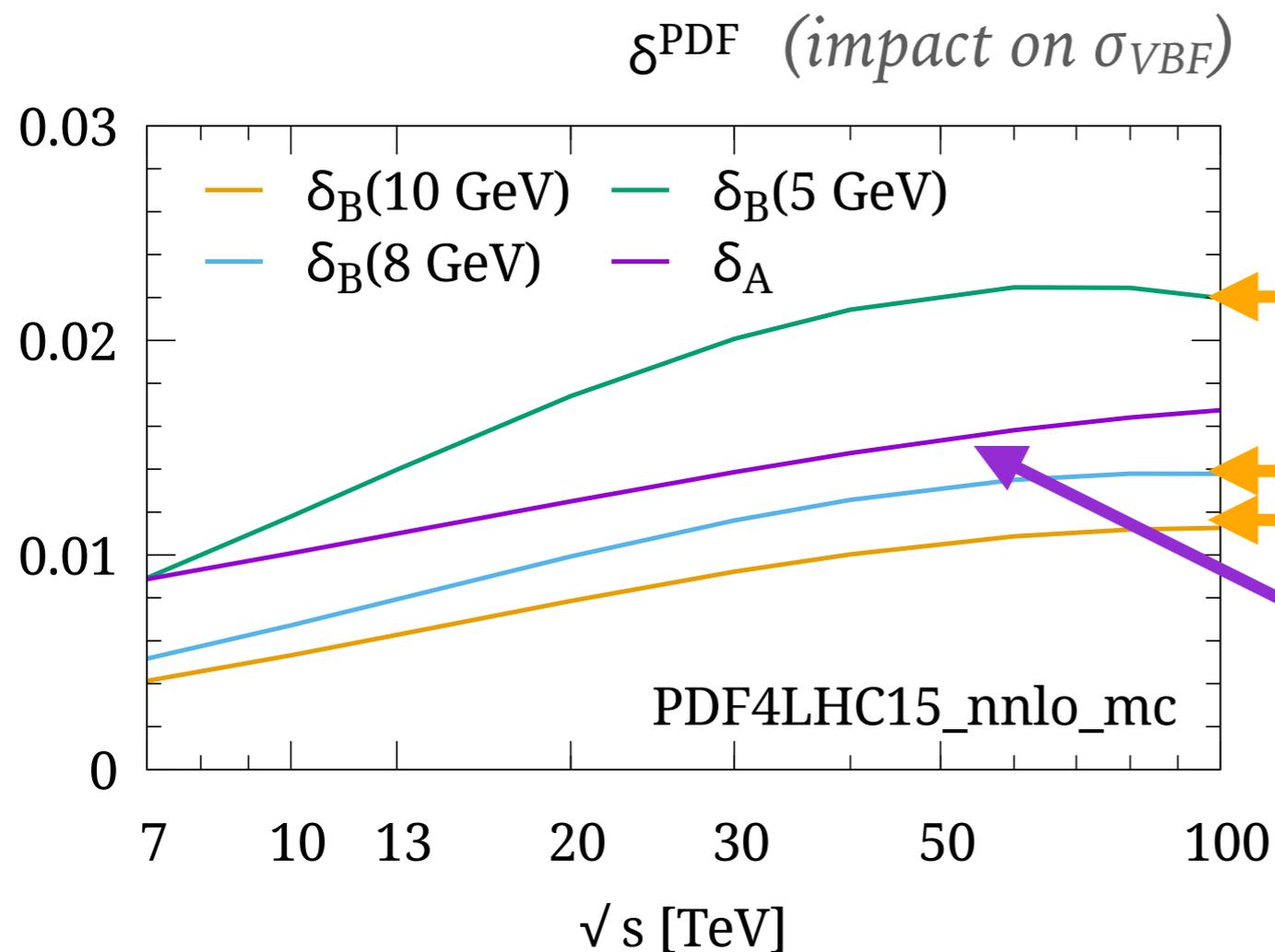
VBF converges much faster than ggF

But both calc<sup>ns</sup> share feature that NNLO fell outside NLO scale band, while N3LO (with good central scale choice) is very close to NNLO

# N3LO PDFS ?

N3LO splitting functions not known. But N3LO DIS coefficient functions are known and their impact for quarks is  $\gg$  NNLO splitting-function scale variation ( $\sim 0.1\%$ )

*Dreyer & Karlberg, 1606.00840*



**impact of N3LO  
coefficient functions  
non-negligible on PDFs**

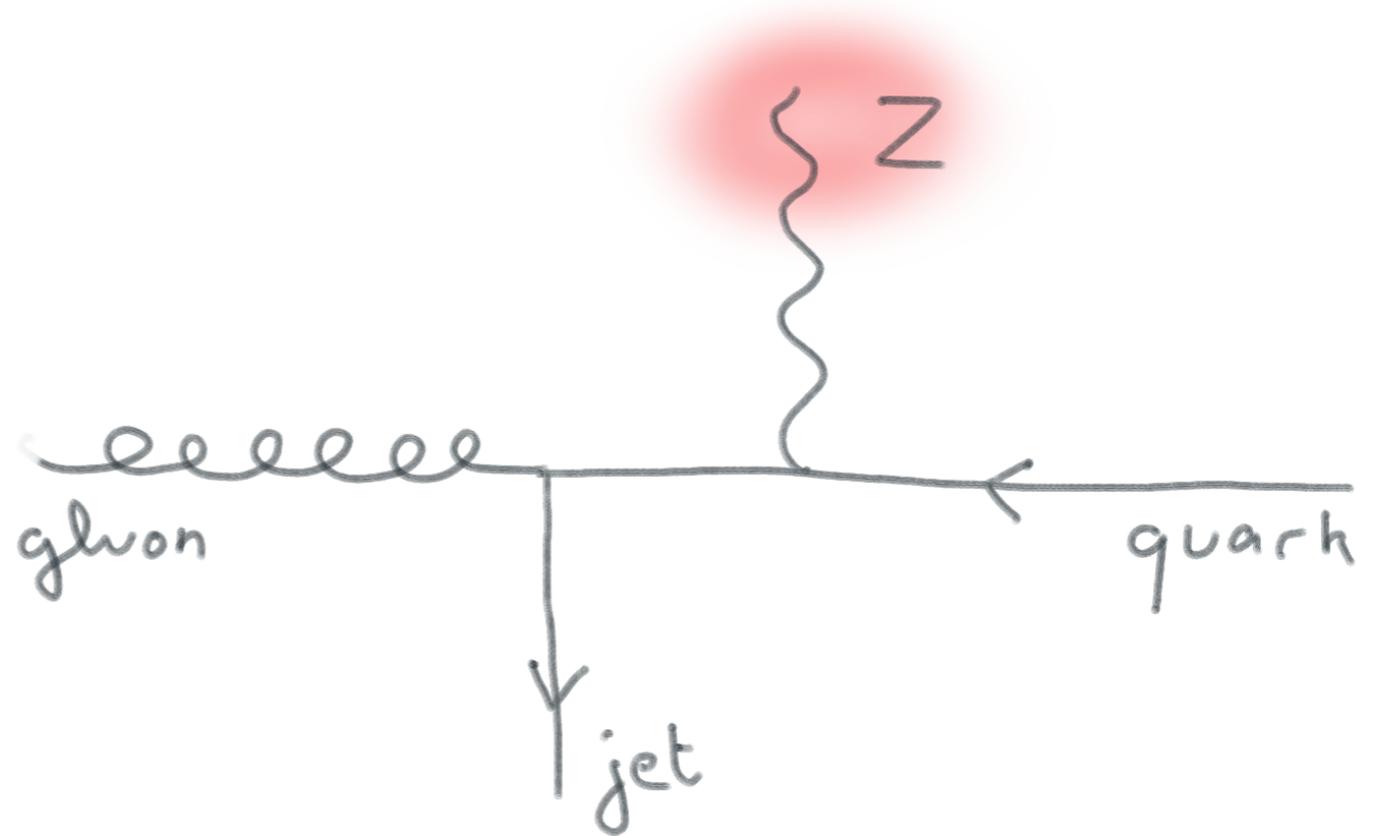
$$\frac{1}{2} \left( \frac{\text{NNLO}}{\text{NLO}} - 1 \right)$$

**First results on N3LO splitting-fn moments** e-Print: [arXiv:1605.08408](https://arxiv.org/abs/1605.08408)

**First Forcer results on deep-inelastic scattering and related quantities**

B. Ruijl, T. Ueda, J.A.M. Vermaseren (NIKHEF, Amsterdam), J. Davies, A. Vogt (Liverpool U., Dept. Math.).

# $Z p_T$ : the “ideal” hard process for testing NNLO precision?



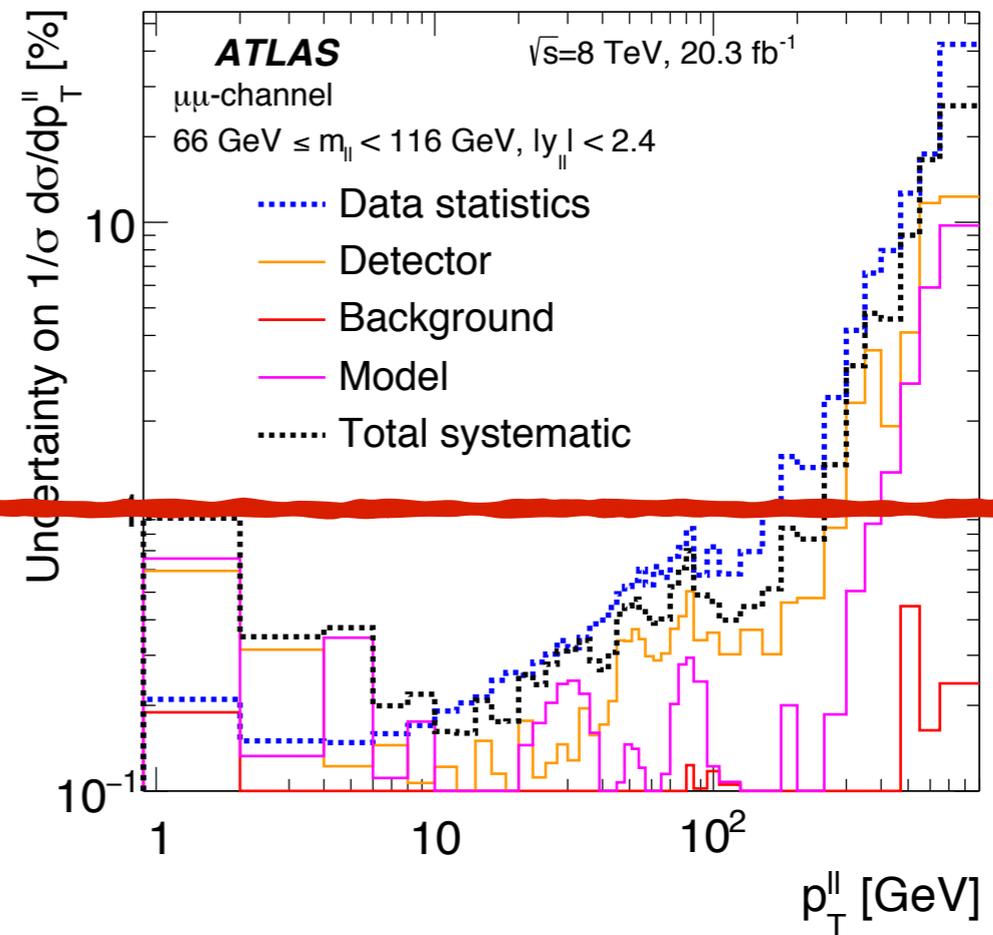
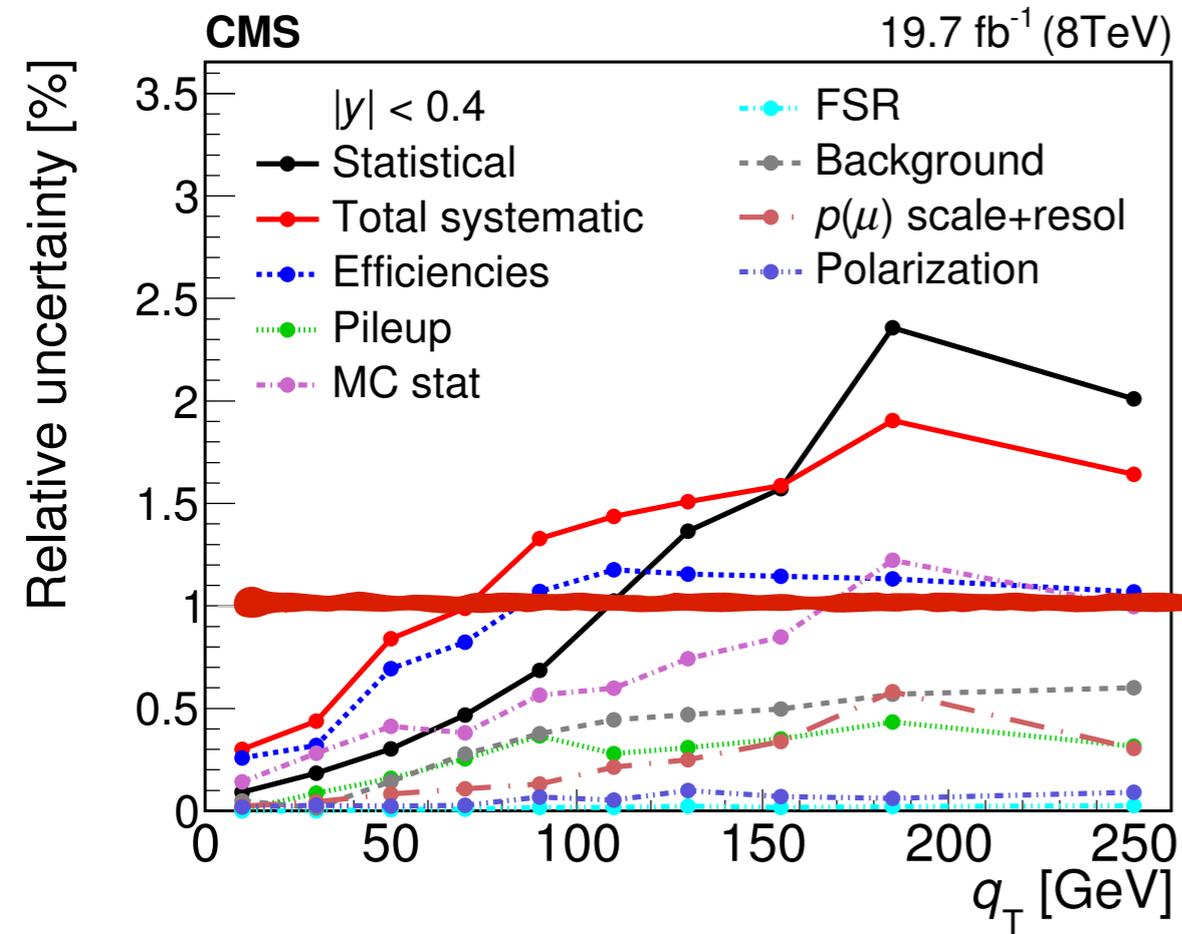
---

*For both data and theory,  $Z p_T$  is  
an immediate testing ground for 1% effects.*

*(& unlike  $Z$  &  $W$  prod<sup>n</sup> it's sensitive to  $\alpha_s$   
& the gluon distribution)*

# Z $p_T$ : run 1 measurements have already reached 0.5–1% !

(normalised to fiducial Z cross section)



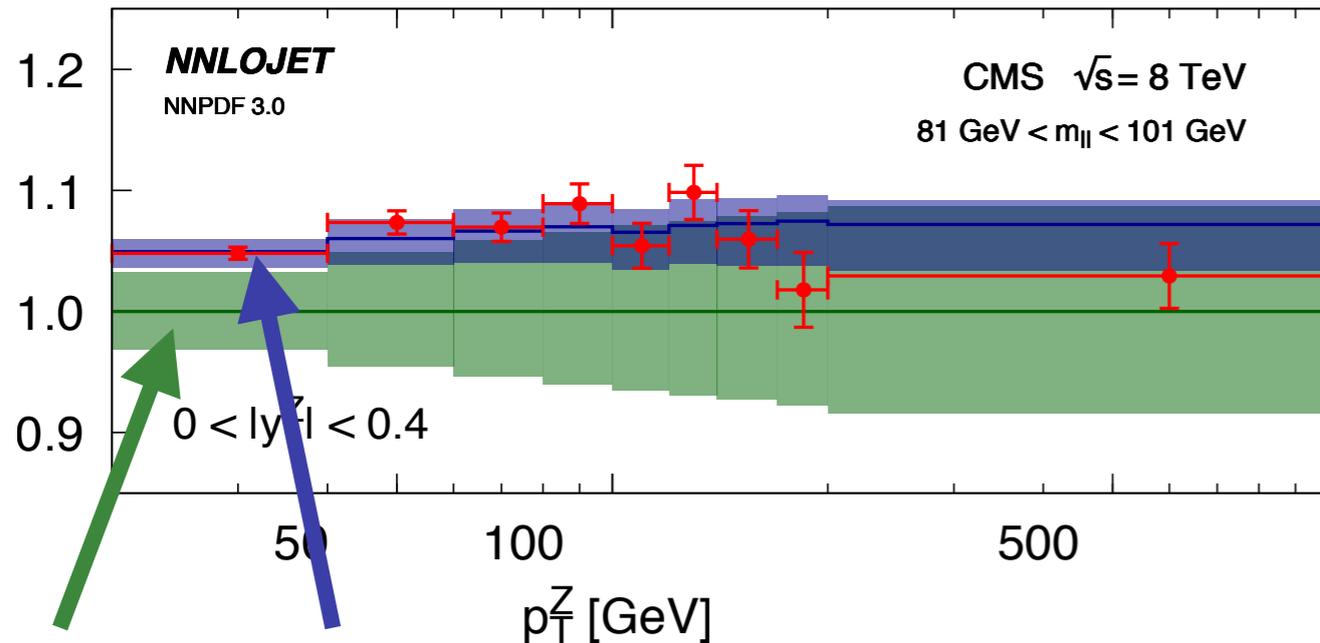
1%

# Z $p_T$ : Data v. two theory calculations

**NNLO  $\sim \pm 1.5\%$**

$p p \rightarrow Z + \geq 0 \text{ jet}$  ( $p_T^Z > 20 \text{ GeV}$ )

NLO — NNLO — Data —●—



**NLO**

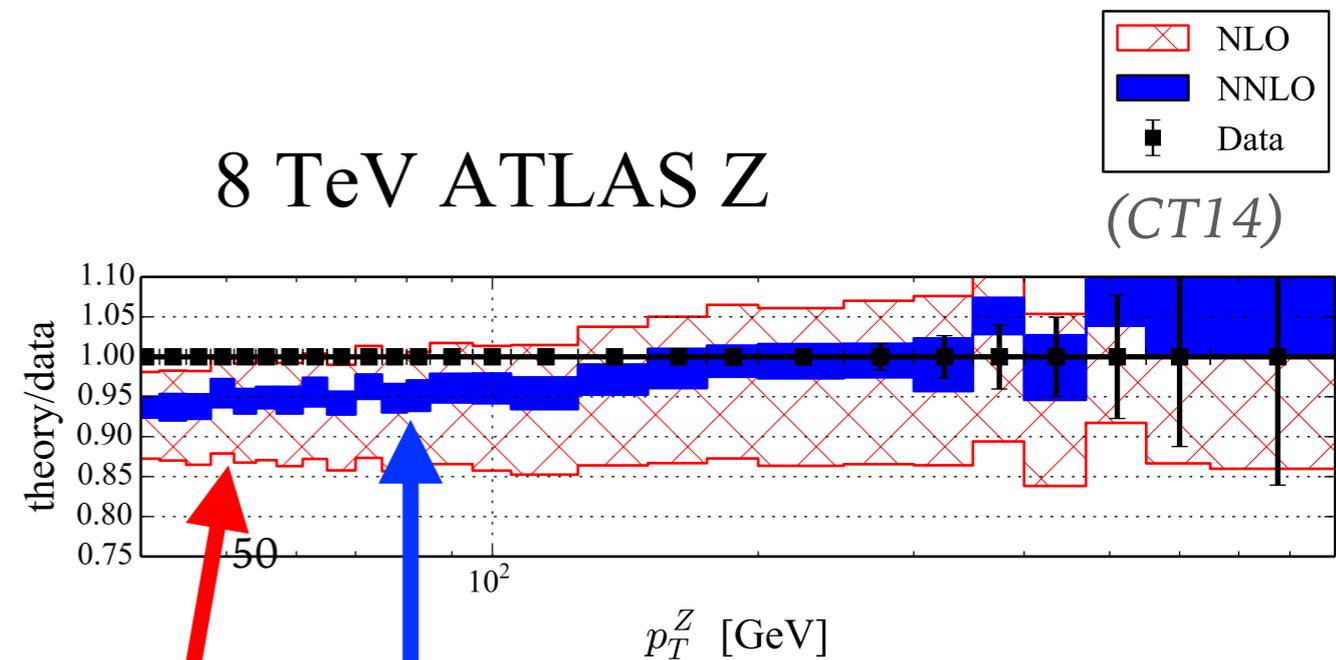
**NNLO**

*Gehrmann-de Ridder, Gehrmann  
Glover, Huss & Morgan*

*arXiv:1605.04295*

8 TeV ATLAS Z

(CT14)



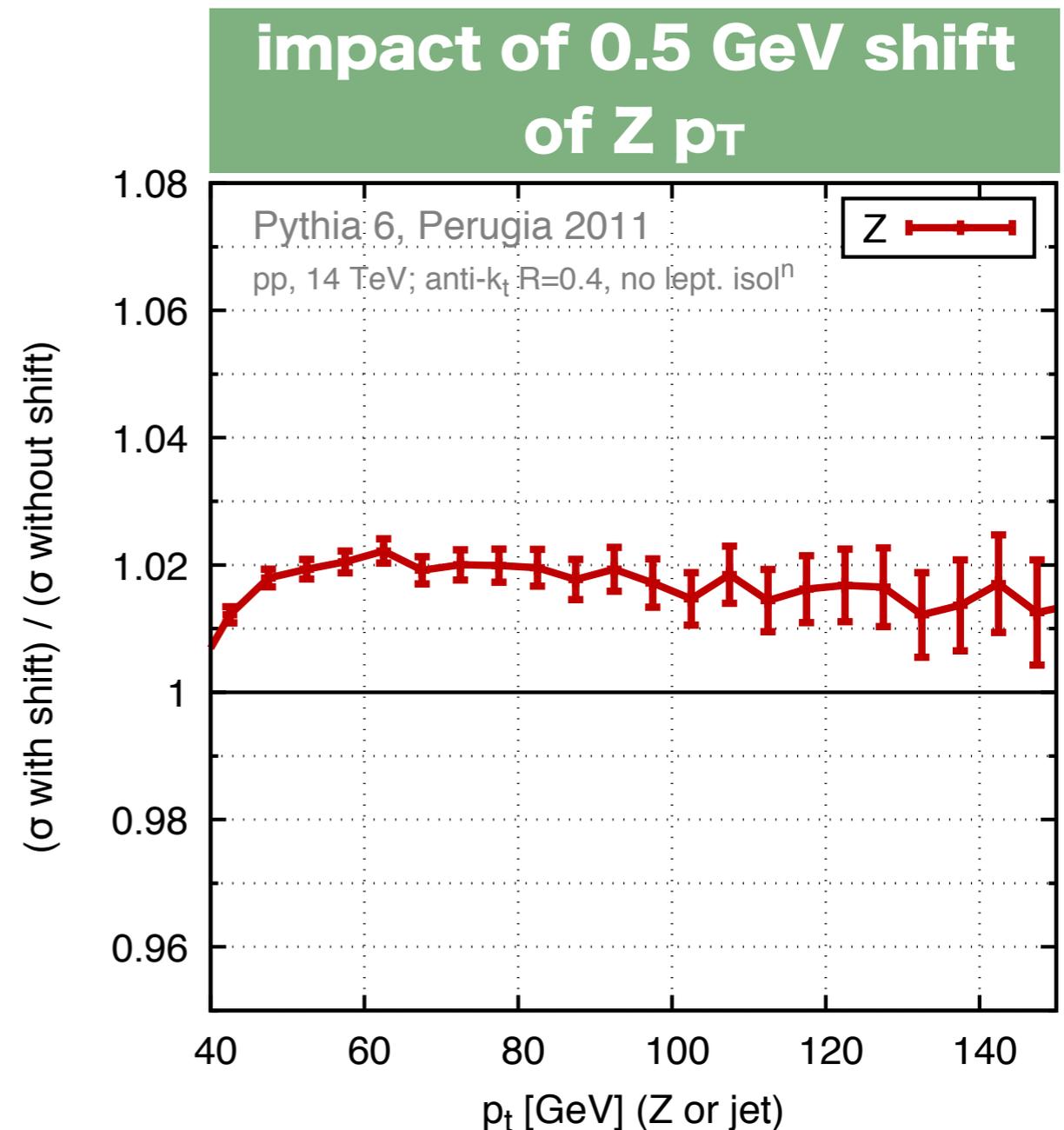
**NLO**

**NNLO**

*Boughezal, Liu & Petriello  
'16 preliminary*

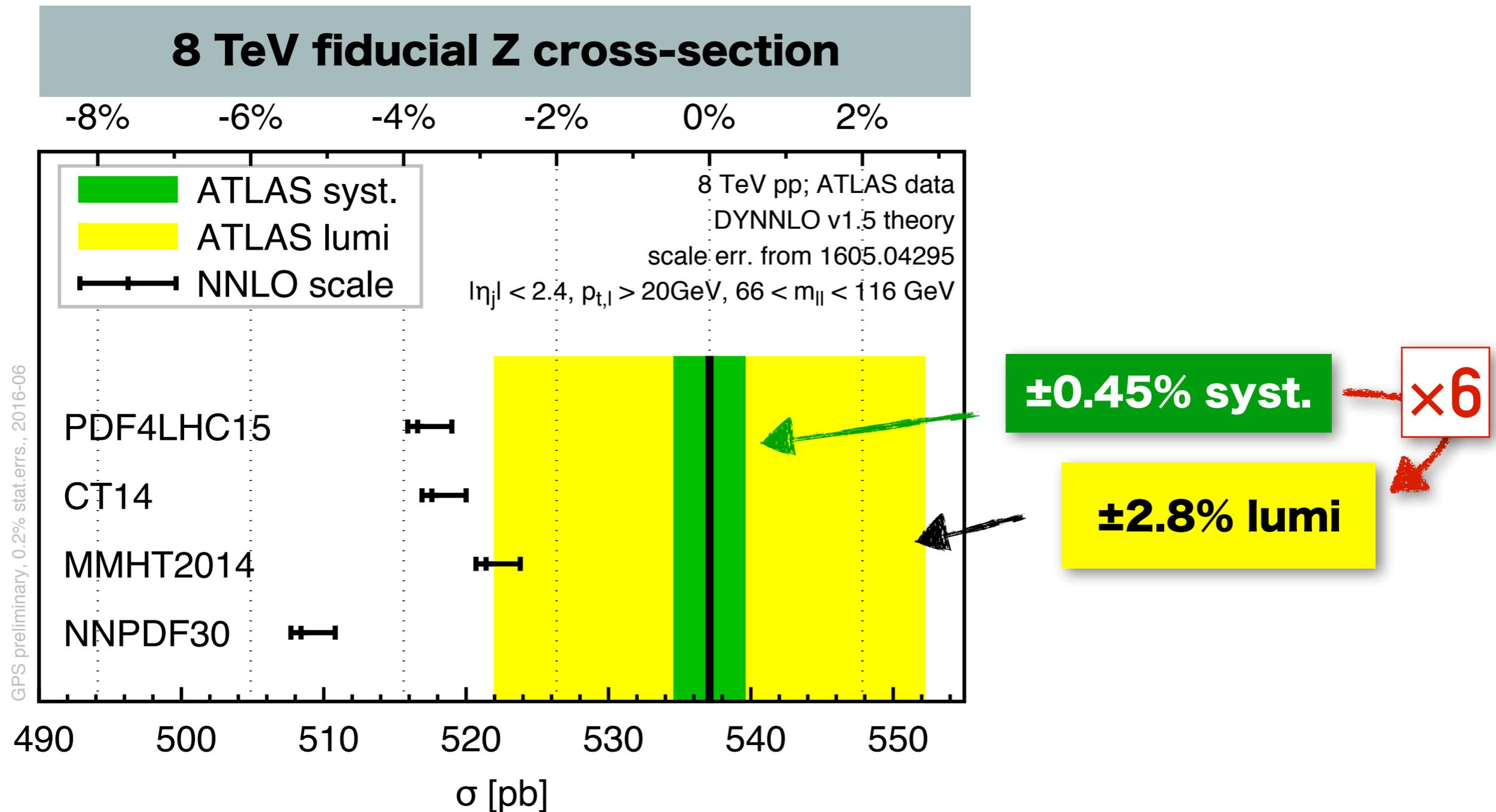
# CAVEAT #1: Non-perturbative effects in Z (& H?) $p_T$

- Inclusive Z & H cross sections should have  $\sim \Lambda^2/M^2$  corrections ( $\sim 10^{-4}$ ?)
- Z (&H)  $p_T$  **not inclusive** so corrections can be  $\sim \Lambda/M$ .
- Size of effect can't be probed by turning MC hadronisation on/off [maybe by modifying underlying MC parameters?]
- Shifting Z  $p_T$  by a finite amount illustrates what could happen



0.5 GeV is perhaps conservative(?)  
But suggests up to 2% effects could be present.

# X-sections normalised to Z are great, **if we understand Z production**



Up to 5% discrepancy?

Are NNLO scale errors (~0.5%) a reliable indicator of uncertainties?

Does it matter, given the large luminosity uncertainty?

# HOW DO EXPERIMENTS COMPARE FOR LUMINOSITY DETERMINATIONS?

Experiment <i>pp</i> running period $\sqrt{s}$ (TeV)	ALICE 2010 7.0	ATLAS 2012 8.0	CMS 2012 8.0	LHCb 2012 8.0		
Absolute-calibration method	<i>vdM</i>	<i>vdM</i>	<i>vdM</i>	<i>vdM</i>	Combined	BGI
Calibration uncertainty $\Delta \sigma_{vis} / \sigma_{vis}$ (%)	3.5	1.2	2.3	1.47	1.12	1.43
$\mu$ or total-rate dependence (%)	-	1.4	< 0.1		0.17	
Long-term stability (%)	1.5	0.6	1.0		0.22	
Subtraction of luminosity backgrounds (%)	3.0	0.2	0.5		0.13	
Other luminosity-dependent effects (%)	1.5		0.5		-	
Total luminosity uncertainty (%)	5.0	1.9	2.6	1.5	1.2	1.5

*From yesterday's talk by W. Kozanecki*

LHCb can do  $\pm 1.1\%$ . Can that be transferred to the other experiments?  
(e.g. with fiducial  $J/\Psi$  measurements? Or some other way?)

ATLAS's final lumi. error has improved relative to that used for fiducial Z x-sct.  
Can key legacy 8 TeV results be updated with new lumi?

**luminosity is potential keystone measurement for LHC precision programme**

**closing remarks**

# THE THINGS I DIDN'T COVER

---

- **strong coupling:** hasn't seen real progress in several years.
  - Need to exclude/validate 0.113.
  - My view: highest prec. will come from progress in lattice
- **PDFs:** maybe we need a roadmap of how we're going to increase precision here? (E.g. which processes are robust & sensitive)
- **Jets:** there are many “systematics” in jet physics
  - perturbative radiation (esp. at small R, log R effects)
  - hadronisation ( $\sim 1/R$ )
  - underlying event ( $\sim R^2$ )

If we're to use them for precision physics we'll probably need measurements over a range of R (0.2 – 0.7?) that goes beyond the R values intended for normal analyses

# KEY MESSAGES

---

- major progress in NNLO calculations
- we're on the eve of a **new precision era: 1–2%**
- many things will need to come together for precision to become ubiquitous
  - QCD inputs: couplings & PDFs
  - QCD “modelling”: hadronisation & UE?
  - Insight into how we make cuts
  - Choice of a few good processes to measure (e.g. just how good are leptons?)
  - LHC machine knowledge, esp. luminosity error?

an exciting time ahead as we learn to do precision  
across the spectrum of LHC physics!

# EXTRA SLIDES

# Processes currently known through NNLO

dijets	$O(3\%)$	gluon-gluon, gluon-quark	PDFs, strong couplings, BSM
H+0 jet	$O(3-5 \%)$	fully inclusive (N3LO)	Higgs couplings
H+1 jet	$O(7\%)$	fully exclusive; Higgs decays, infinite mass tops	Higgs couplings, Higgs $p_t$ , structure for the ggH vertex.
tT pair	$O(4\%)$	fully exclusive, stable tops	top cross section, mass, $p_t$ , FB asymmetry, PDFs, BSM
single top	$O(1\%)$	fully exclusive, stable tops, t-channel	$V_{tb}$ , width, PDFs
WBF	$O(1\%)$	exclusive, VBF cuts	Higgs couplings
W+j	$O(1\%)$	fully exclusive, decays	PDFs
Z+j	$O(1-3\%)$	decays, off-shell effects	PDFs
ZH	$O(3-5 \%)$	decays to bb at NLO	Higgs couplings (H-> bb)
ZZ	$O(4\%)$	fully exclusive	Trilinear gauge couplings, BSM
WW	$O(3\%)$	fully inclusive	Trilinear gauge couplings, BSM
top decay	$O(1-2 \%)$	exclusive	Top couplings
H -> bb	$O(1-2 \%)$	exclusive, massless	Higgs couplings, boosted

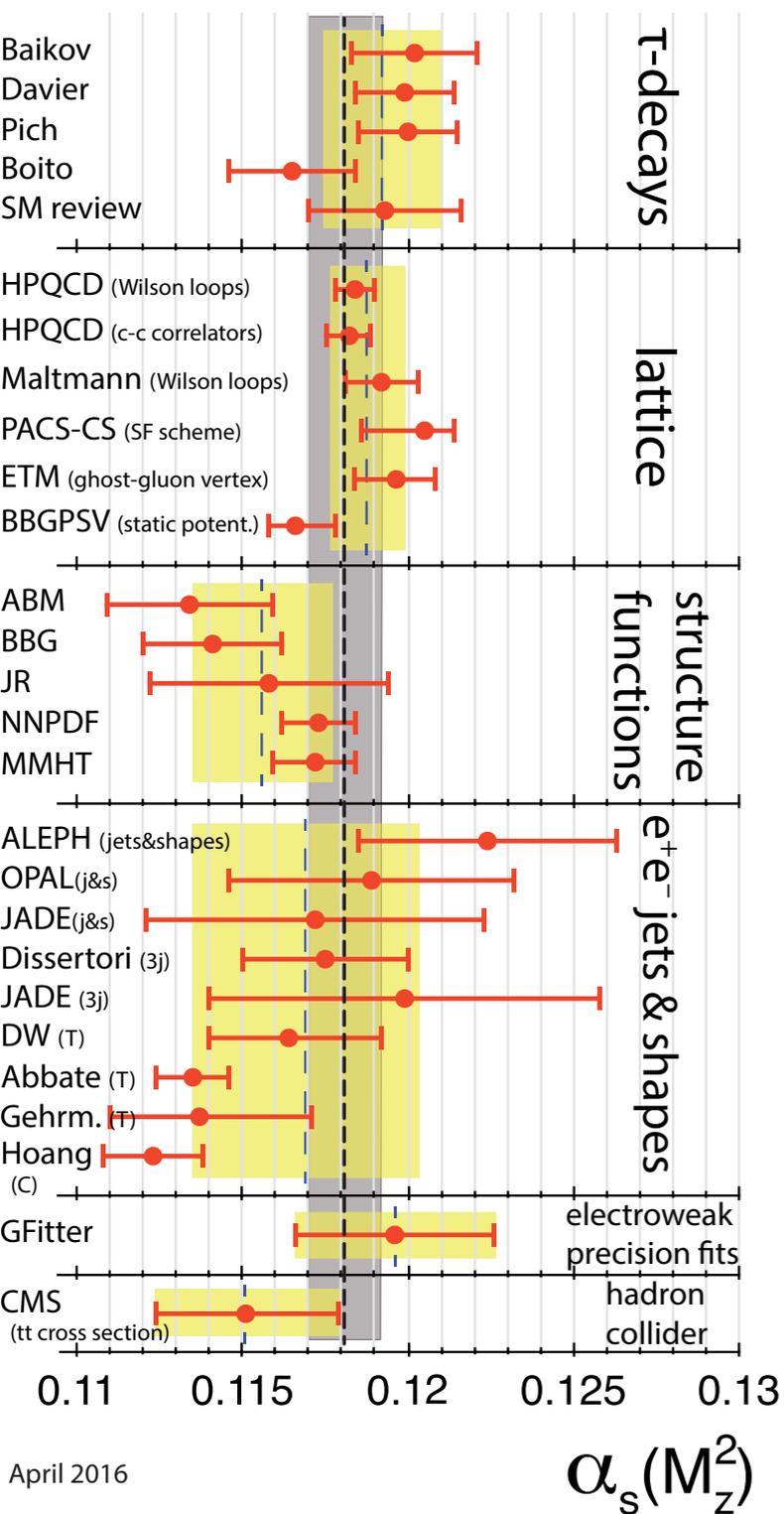
done ~ in past year

*K. Melnikov @ KITP*

# the inputs

---

*strong coupling (e.g.  $\pm 2.6\%$  on  $ggF$ )*  
*PDFs (e.g.  $\pm 1.9\%$  on  $ggF$ )*



PDG World Average:  $\alpha_s(M_Z) = 0.1181 \pm 0.0011$  (0.9%)

- Most consistent set of independent determinations is from lattice
- Two best determinations are from same group (HPQCD, 1004.4285, 1408.4169)

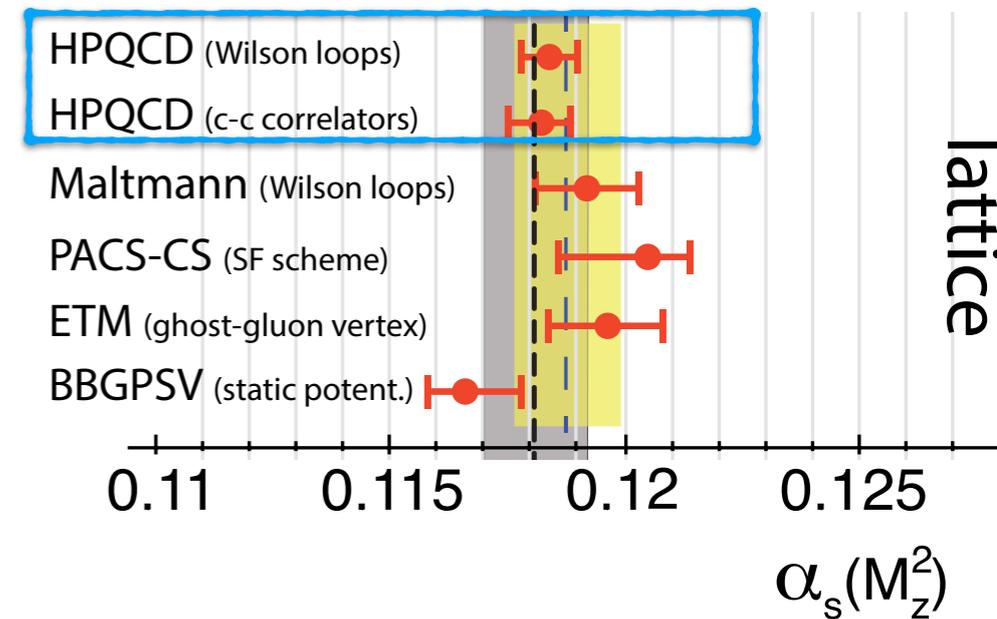
$\alpha_s(M_Z) = 0.1183 \pm 0.0007$  (0.6%) [heavy-quark correlators]

$\alpha_s(M_Z) = 0.1183 \pm 0.0007$  (0.6%) [Wilson loops]

- Error criticised by FLAG, who suggest

$\alpha_s(M_Z) = 0.1184 \pm 0.0012$  (1%)

- Worries include missing perturbative contributions, non-perturbative effects in 3–4 flavour transition at charm mass [addressed in some work], etc.



April 2016

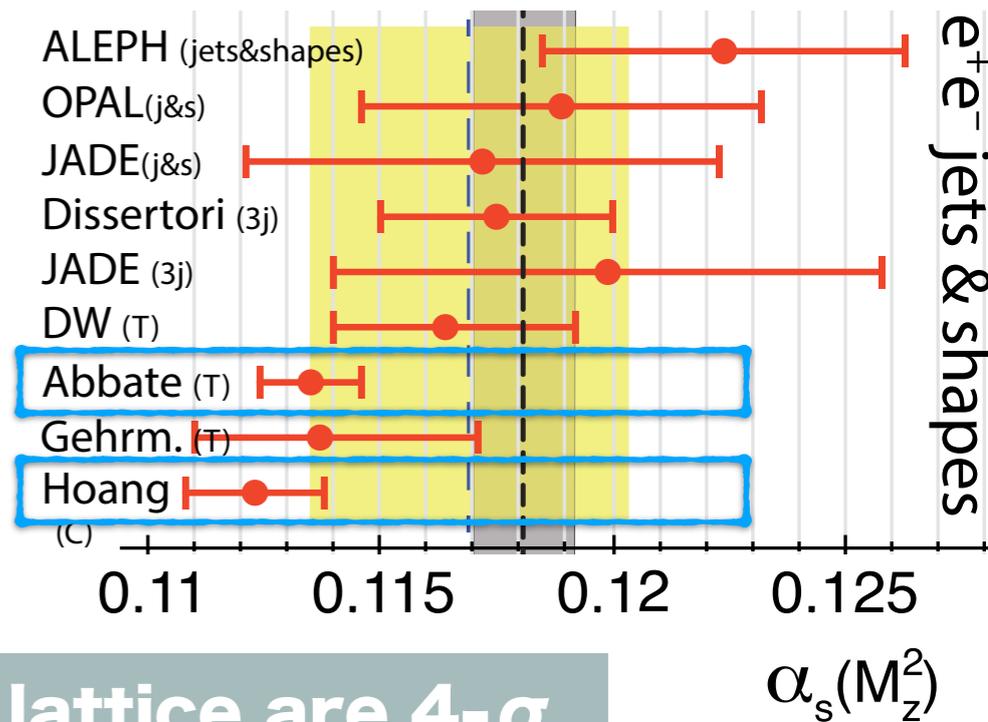
# E+E- EVENT SHAPES AND JET RATES

- Two “best” determinations are from same group

(Hoang et al, 1006.3080,1501.04111)

$$\alpha_s(M_Z) = 0.1135 \pm 0.0010 \text{ (0.9\%)} \text{ [thrust]}$$

$$\alpha_s(M_Z) = 0.1123 \pm 0.0015 \text{ (1.3\%)} \text{ [C-parameter]}$$



**thrust & “best” lattice are 4-σ**

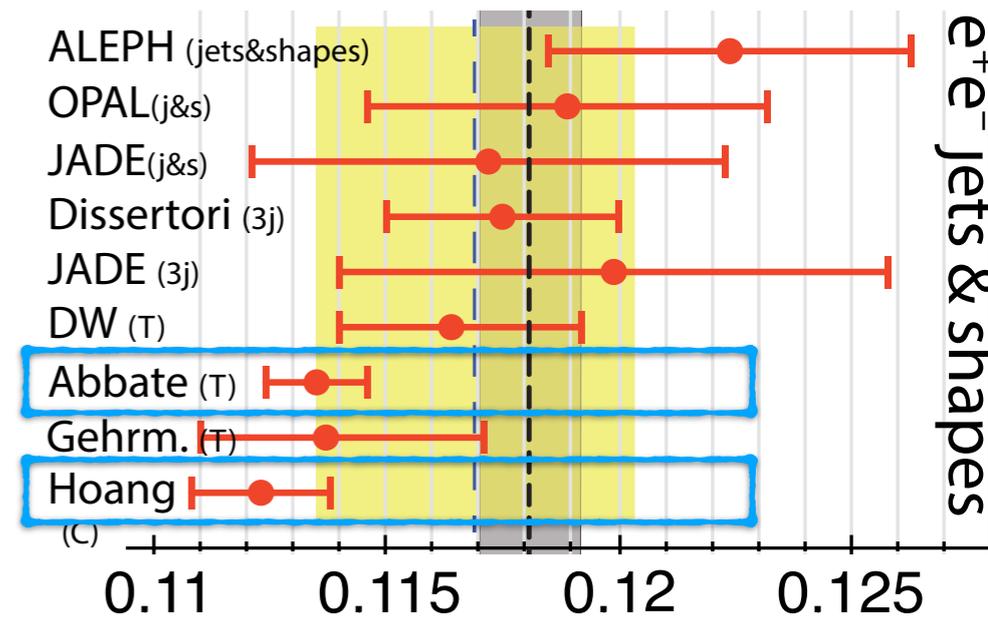
# E+E- EVENT SHAPES AND JET RATES

- Two “best” determinations are from same group

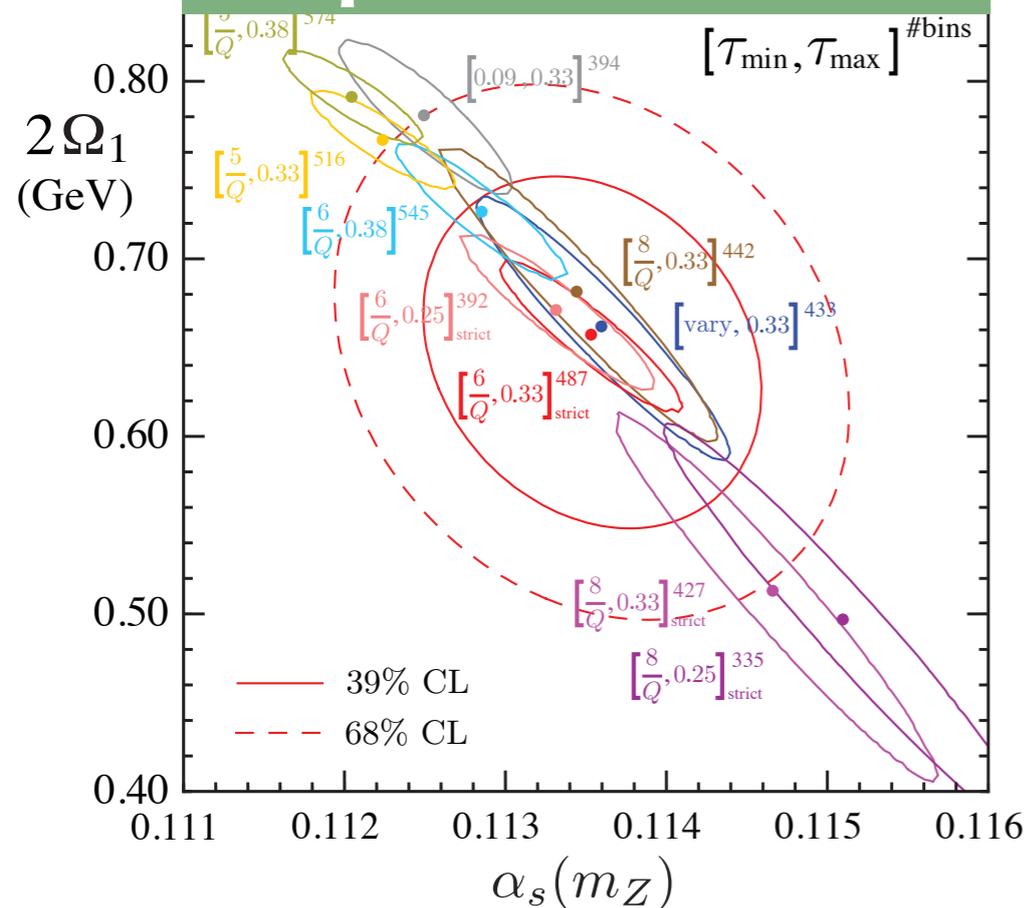
(Hoang et al, 1006.3080,1501.04111)

$$\alpha_s(M_Z) = 0.1135 \pm 0.0010 \text{ (0.9\%)} \text{ [thrust]}$$

$$\alpha_s(M_Z) = 0.1123 \pm 0.0015 \text{ (1.3\%)} \text{ [C-parameter]}$$



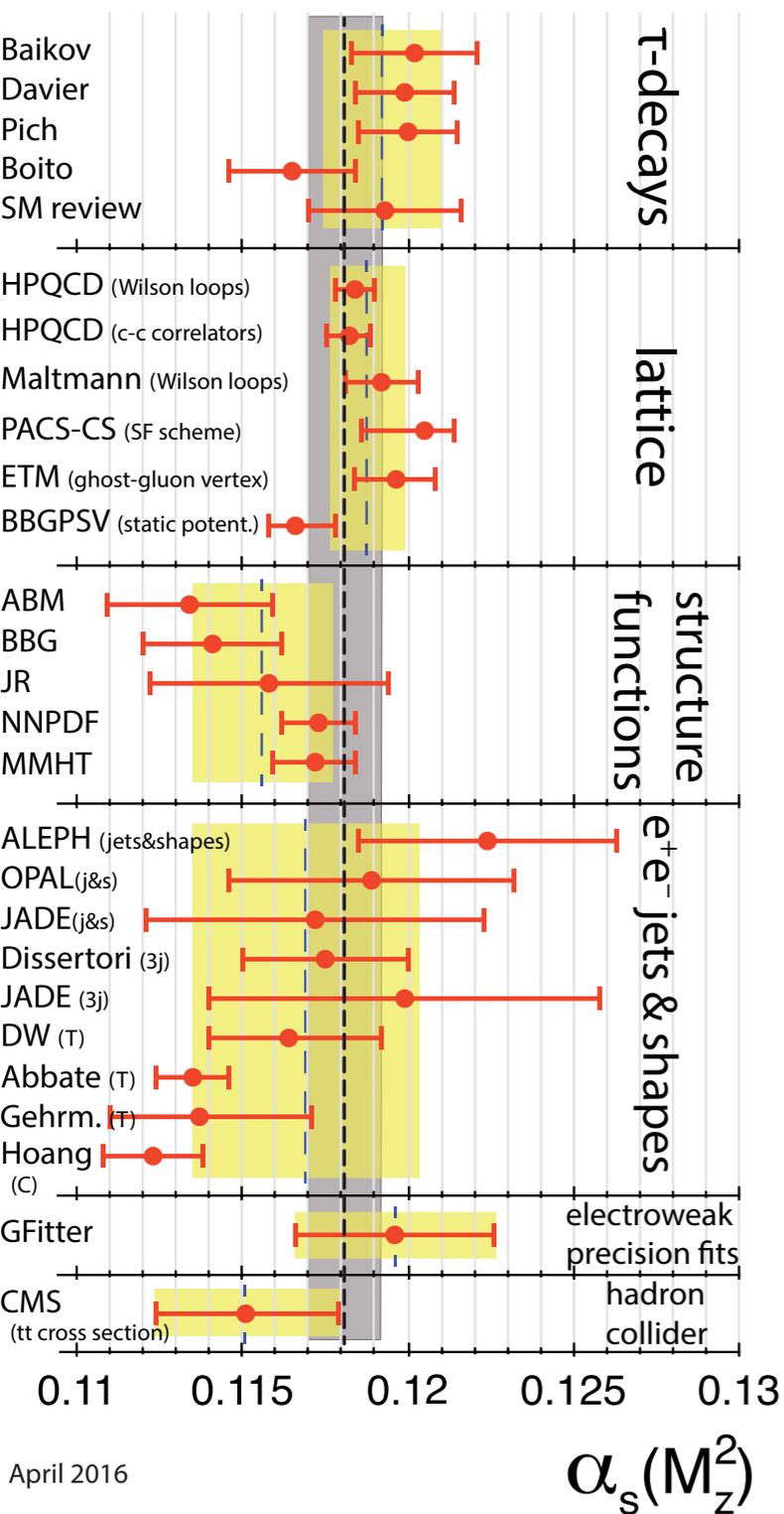
## dependence on fit



**thrust & “best” lattice are 4- $\sigma$**

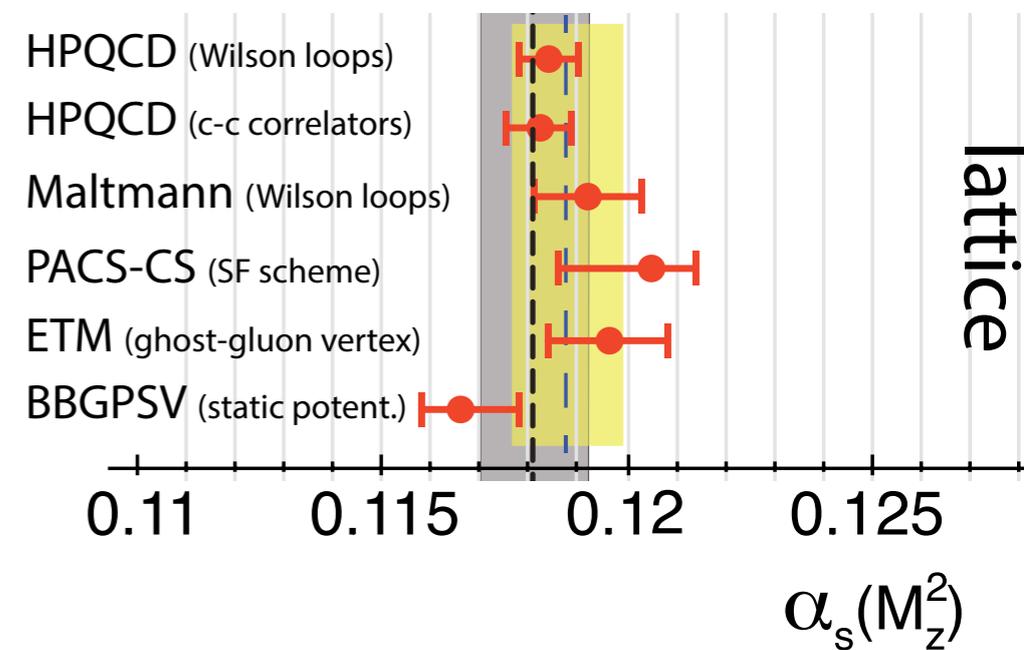
### Comments:

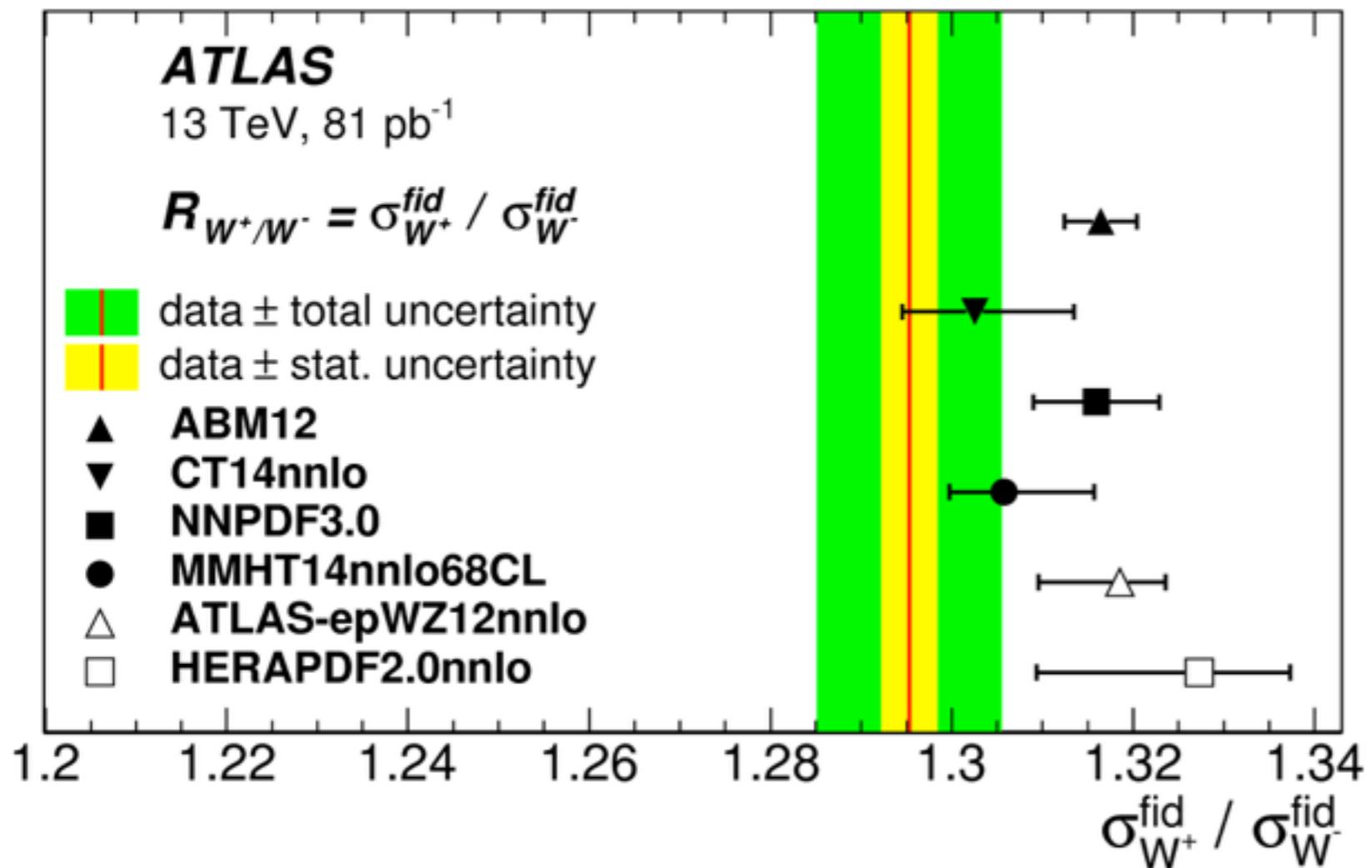
- thrust & C-parameter are highly correlated observables
- Analysis valid far from 3-jet region, but not too deep into 2-jet region — at LEP, not clear how much of distribution satisfies this requirement
- thrust fit shows noticeable sensitivity to fit region (C-parameter doesn't)



PDG World Average:  $\alpha_s(M_Z) = 0.1181 \pm 0.0011$  (0.9%). WHAT WAY FORWARD?

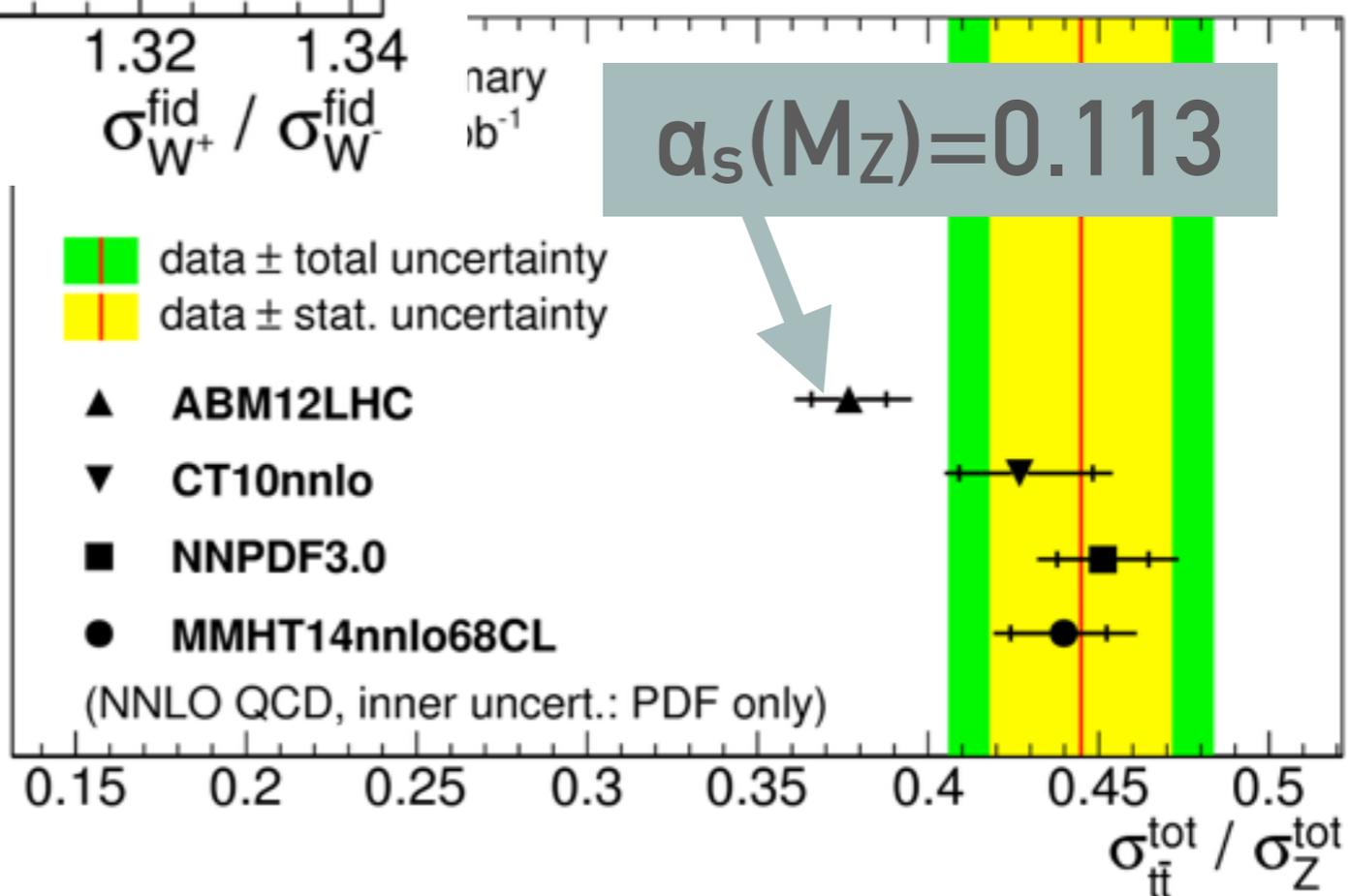
- For gluon-fusion & ttH, this comes in squared. It also correlates with the PDFs and affects backgrounds.
- To go beyond 1%, best hope is probably lattice QCD — on a 10-year timescale, there will likely be enough progress that multiple groups will have high-precision determinations





cross-section ratios  
(W<sup>+</sup>/W<sup>-</sup>, ttbar/Z)  
show tensions with  
some PDFs

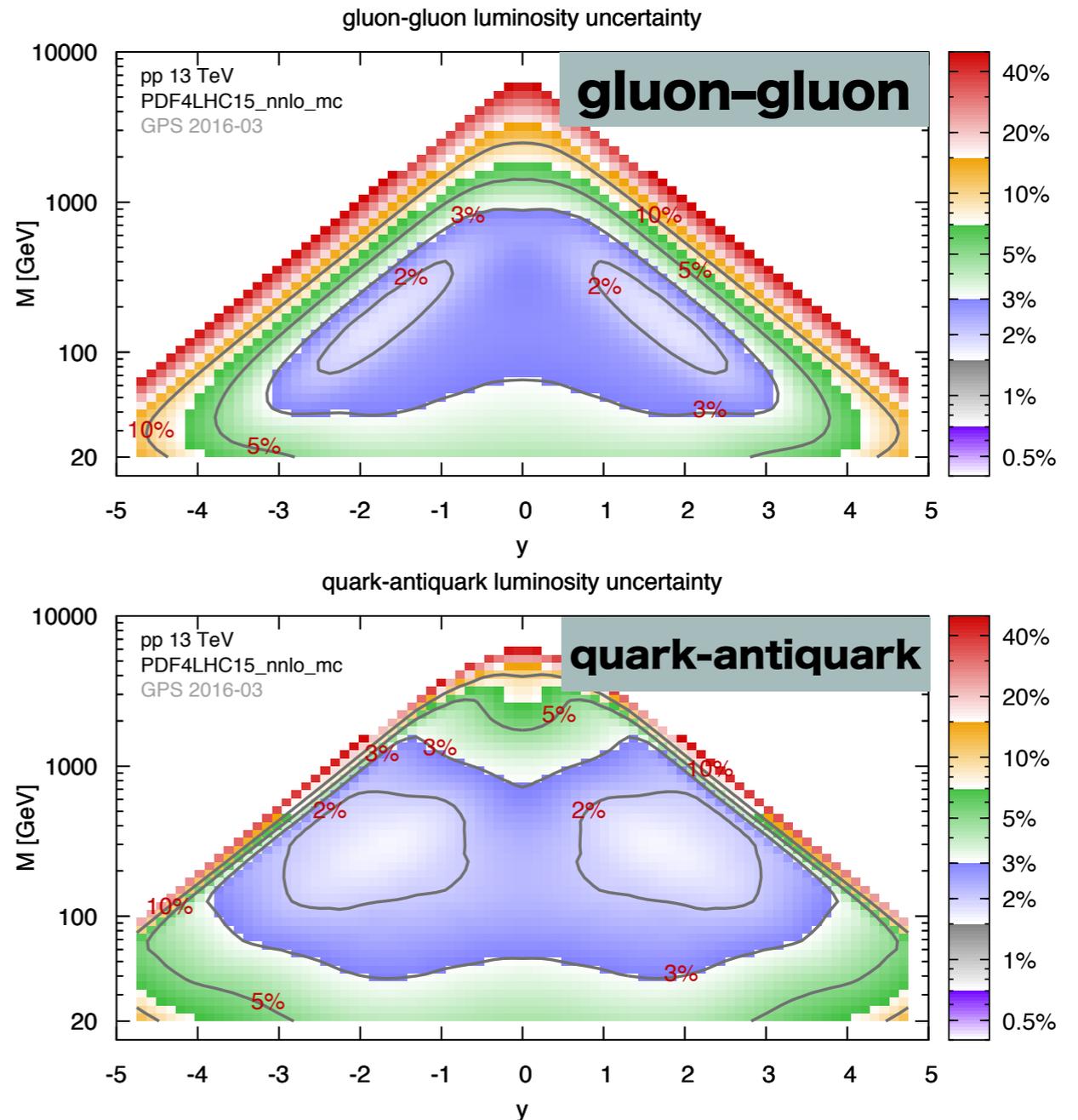
ATLAS-CONF-2015-049



*NB: top-quark mass  
choice affects this plot*

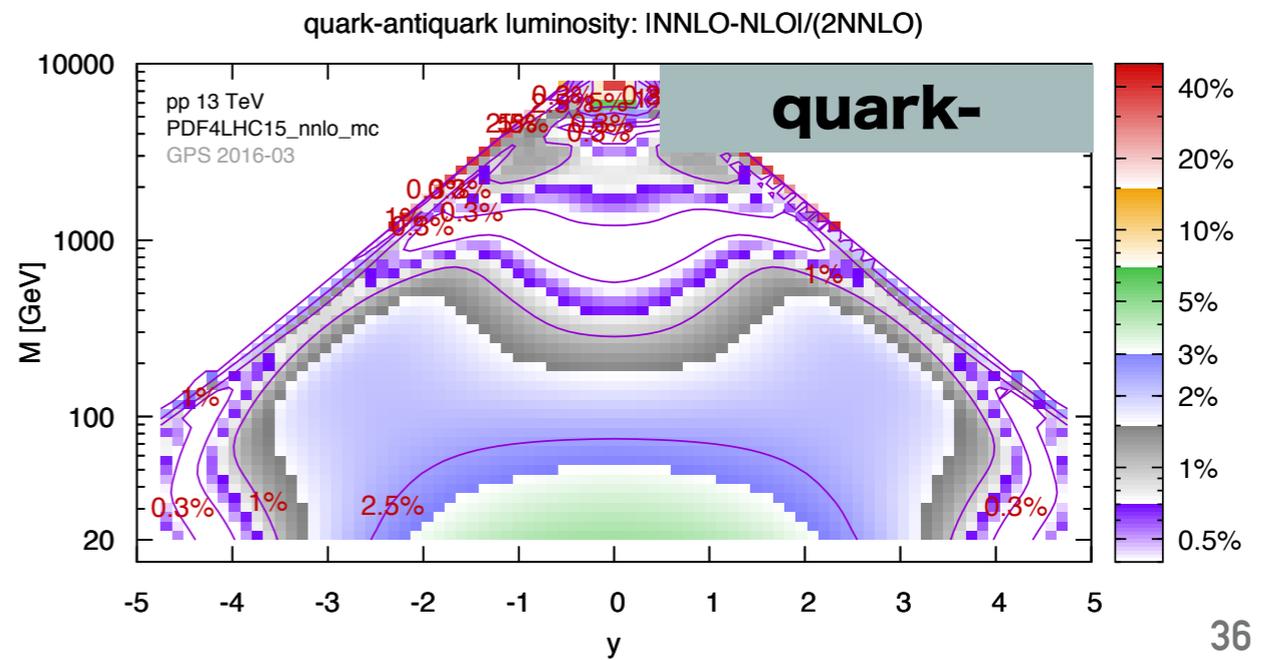
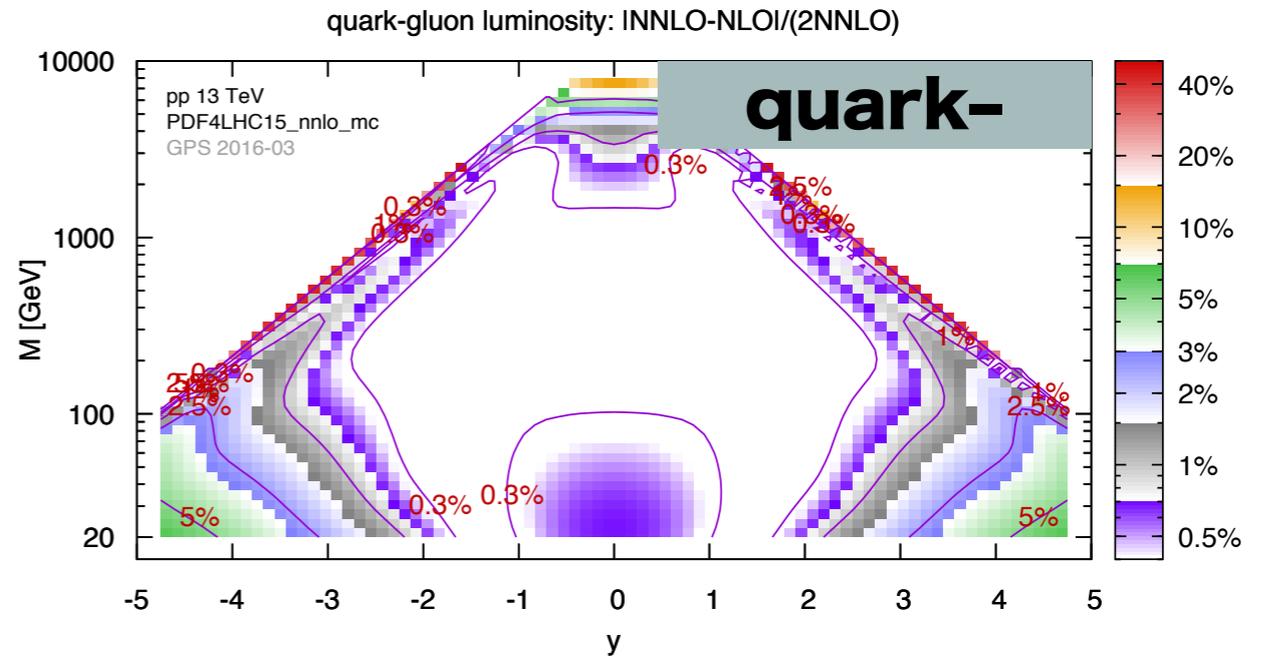
# PDFs: WHAT ROUTE FOR PROGRESS?

- Current status is 2–3% for core “precision” region
- Path to 1% is not clear — e.g.  $Z p_T$ 's strongest constraint is on  $qg$  lumi, which is already best known (why?)
- It'll be interesting to revisit the question once  $t\bar{t}bar$ , incl. jets,  $Z p_T$ , etc. have all been incorporated at NNLO
- **Can expts. get better lumi determination? 0.5%?**



# PDF THEORY UNCERTAINTIES

## Theory Uncertainties



## PDF4LHC recommendations for LHC Run II

Jon Butterworth, Stefano Carrazza, Amanda Cooper-Sarkar, Albert De Roeck, Joel Feltesse, Stefano Forte, Jun Gao, Sasha Glazov, Joey Huston, Zahari Kassabov, Ronan McNulty, Andreas Morsch, Pavel Nadolsky, Voica Radescu, Juan Rojo, Robert Thorne

*(Submitted on 13 Oct 2015 (v1), last revised 12 Nov 2015 (this version, v2))*

We provide an updated recommendation for the usage of sets of parton distribution functions (PDFs) and the assessment of PDF and PDF+ $\alpha_s$  uncertainties suitable for applications at the LHC Run II. We review developments since the previous PDF4LHC recommendation, and discuss and compare the new generation of PDFs, which include substantial information from experimental data from the Run I of the LHC. We then propose a new prescription for the combination of a suitable subset of the available PDF sets, which is presented in terms of a single combined PDF set. We finally discuss tools which allow for the delivery of this combined set in terms of optimized sets of Hessian eigenvectors or Monte Carlo replicas, and their usage, and provide some examples of their application to LHC phenomenology.

## Recommendations for PDF usage in LHC predictions

A. Accardi, S. Alekhin, J. Blümlein, M.V. Garzelli, K. Lipka, W. Melnitchouk, S. Moch, R. Placakyte, J.F. Owens, E. Reya, N. Sato, A. Vogt, O. Zenaiev

*(Submitted on 29 Mar 2016)*

We review the present status of the determination of parton distribution functions (PDFs) in the light of the precision requirements for the LHC in Run 2 and other future hadron colliders. We provide brief reviews of all currently available PDF sets and use them to compute cross sections for a number of benchmark processes, including Higgs boson production in gluon-gluon fusion at the LHC. We show that the differences in the predictions obtained with the various PDFs are due to particular theory assumptions made in the fits of those PDFs. We discuss PDF uncertainties in the kinematic region covered by the LHC and on averaging procedures for PDFs, such as advocated by the PDF4LHC15 sets, and provide recommendations for the usage of PDF sets for theory predictions at the LHC.