

Recent progress in defining and understanding jets

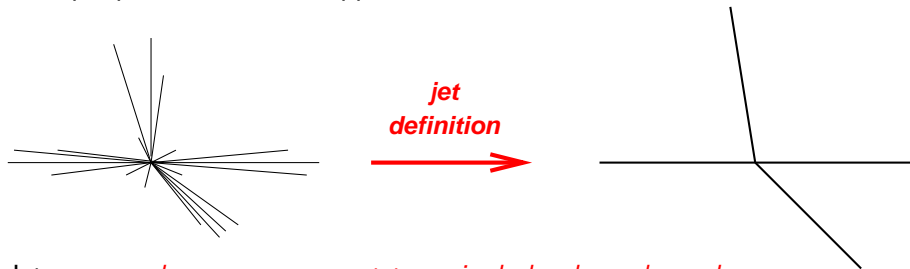
Gavin Salam

LPTHE, Universities of Paris VI and VII and CNRS

A summary of work (in progress) with A. Banfi, M. Cacciari,
M. Dasgupta, L. Magnea, G. Soyez, G. Zanderighi

ISMD 2007
Berkeley, 5–9 August 2007

Jets essentially **project away the multiparticle dynamics**, so as to leave a simple picture of what happened in an event:



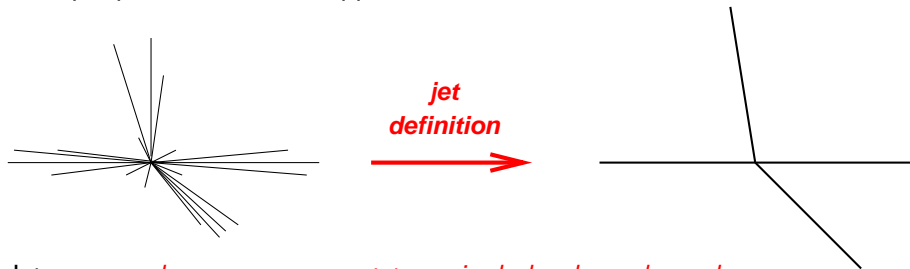
Jets are *as close as we can get to a single hard quark or gluon*:

- ▶ A jet has almost the same momentum as the 'initiating parton'
- ▶ A jet may maintain heavy flavour from the initiating parton

But projection to jets is fundamentally ambiguous, reflecting divergent and quantum-mechanical nature of QCD.

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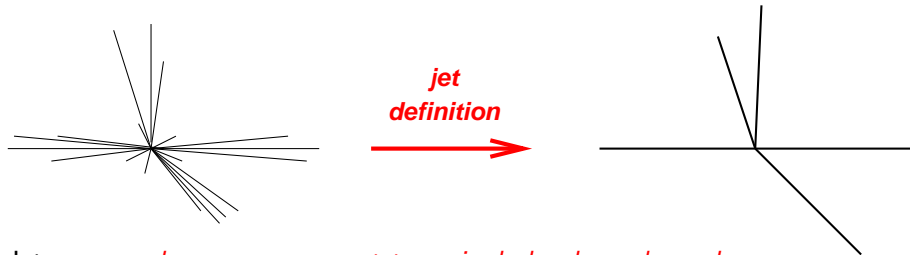
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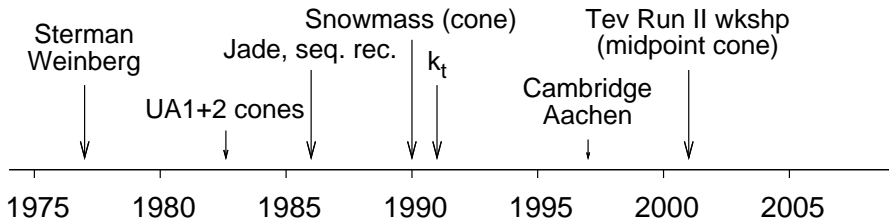
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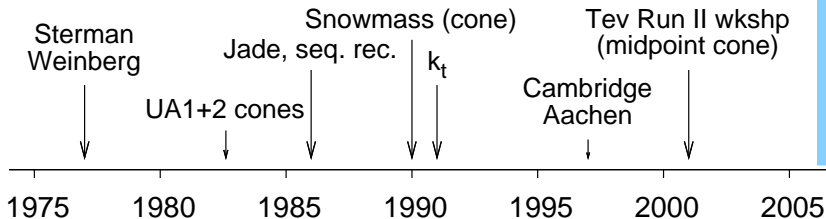
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- ▶ Periodic key developments in jet definitions spurred by ever-increasing experimental sophistication.
- ▶ Approach of LHC provides motivation for taking a new, fresh, systematic look at jets.
- ▶ This talk: **some of the discoveries along the way**



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NB: also ARCLUS, OJF, ...

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Speed, IR safety, Jet Areas
Non-pert. effects, Jet Flavour

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Number of particles:

Experiment	N
LEP, HERA	50
Tevatron	100–400
LHC low-lumi	800
LHC high-lumi	4000
LHC PbPb	30000

Range of processes:

- ▶ jets, $t\bar{t}$, tj , Wj , Hj , $t\bar{t}j$, WWj , Wjj , ...
- ▶ Many NLO calculations being done
- ▶ 50 people \times 10 years (\$30 – 50M)
- ▶ Multijet-NLO calculations only make sense for *infrared safe* jet definitions

Physics scales:

Experiment	Physics	Scale
LEP, HERA	Electroweak	100 GeV
	+ Hadronisation	0.5 GeV
Tevatron	+ Underlying event	2.5 – 5 GeV
LHC	+ BSM	1 TeV?
	+ Pileup	5 – 20 GeV

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Three (short) parts

▶ Technical advances

- ▶ k_t and Cam/Aachen speed
- ▶ seedless cone \leftrightarrow IR safety + speed

Cacciari & GPS '05
GPS & Soyez '07

▶ Understanding of jet-alg. behaviour

- ▶ Jet areas
- ▶ Hadronisation

Cacciari, GPS & Soyez, prelim.
Cacciari, Dasgupta, Magnea & GPS, prelim.

▶ Using understanding to make better algorithms

- ▶ Area-based subtraction
- ▶ The flavour- k_t alg, and b -jets

Cacciari & GPS '07
Banfi, GPS & Zanderighi '06–07

Sequential recombination

k_t , Jade, Cam/Aachen, ...

Bottom-up:

Cluster 'closest' particles repeatedly until few left \rightarrow jets.

Works because of mapping:

closeness \Leftrightarrow QCD divergence

Loved by e^+e^- , ep and theorists

Cone

UA1, JetClu, Midpoint, ...

Top-down:

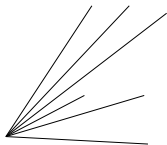
Find coarse regions of energy flow (cones), and call them jets.

Works because *QCD only modifies energy flow on small scales*

Loved by pp and few(er) theorists

k_t algorithm

- ▶ Find smallest of all $d_{ij} = \min(k_{ti}^2, k_{tj}^2) \Delta R_{ij}^2 / R^2$ and $d_{iB} = k_i^2$
- ▶ Recombine i, j (if iB : $i \rightarrow \text{jet}$)
- ▶ Repeat



'Trivial' computational issue:

- ▶ for N particles: N^2 d_{ij} searched through N times = N^3
- ▶ 4000 particles (or calo cells): 1 minute
NB: often study $10^7 - 10^8$ events

Advance #1: factorise momentum and geometry

Borrow methods & tools from Computational Geometry:

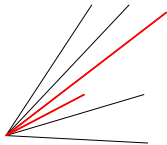
Bucketing, dynamic Voronoi diagrams, CGAL, Chan CP

Time reduced to $N \ln N$ or $N \ln N$: 25ms for $N=4000$.

Cacciari & GPS '05

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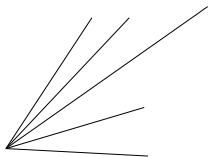
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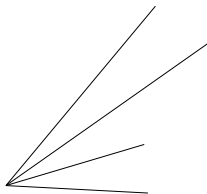
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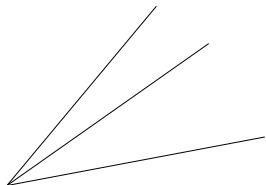
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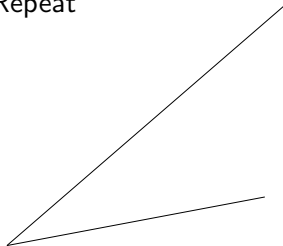
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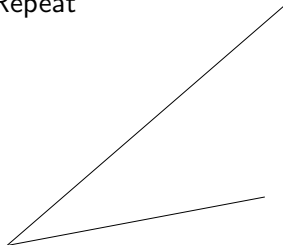
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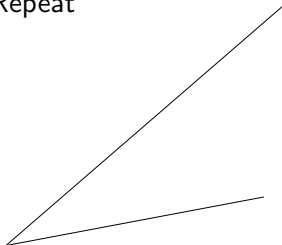
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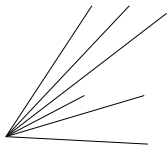
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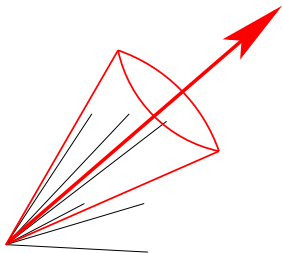
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- ▶ Find some/all stable cones
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- ▶ Resolve cases of overlapping stable cones
By running a 'split-merge' procedure



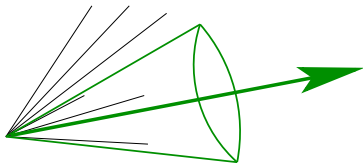
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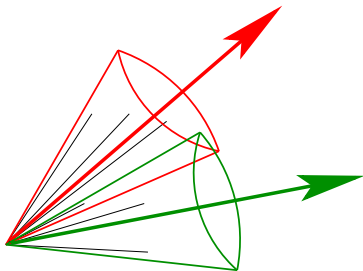
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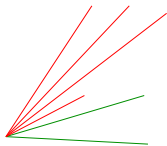
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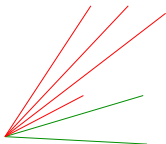
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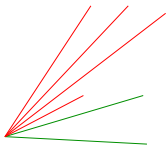


- ▶ Iterate from 'seed' particles
Done originally, very IR unsafe, N^2
- ▶ Iterate from 'midpoints' between cones from seeds
Midpoint cone, less IR unsafe, N^3
- ▶ Seedless: try all subsets of particles IR safe, $N2^N$
100 particles: 10^{17} years

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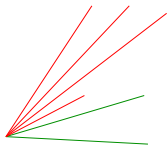


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Among consequences of IR unsafety:

	<i>Last meaningful order</i>	
	lt. cone	MidPoint
Inclusive jets	LO	NLO
$W/Z + 1$ jet	LO	NLO
3 jets	none	LO
$W/Z + 2$ jets	none	LO
m_{jet} in $2j + X$	none	none

Recall \$30 – 50M investment in NLO

Advance #2: IR safe seedless cone separate mom. and geometry (again)

New comp. geometry techniques: 2D all distinct circular enclosures

Then for each check whether \rightarrow stable cone

Time reduced from $N^2 N$ to $N^2 \ln N$: 6s for $N=4000$. GPS & Soyez '07

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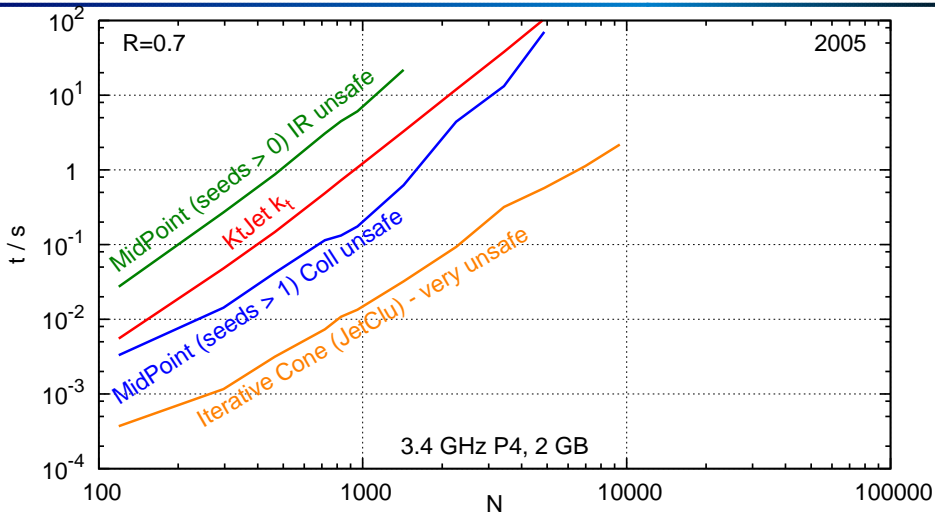
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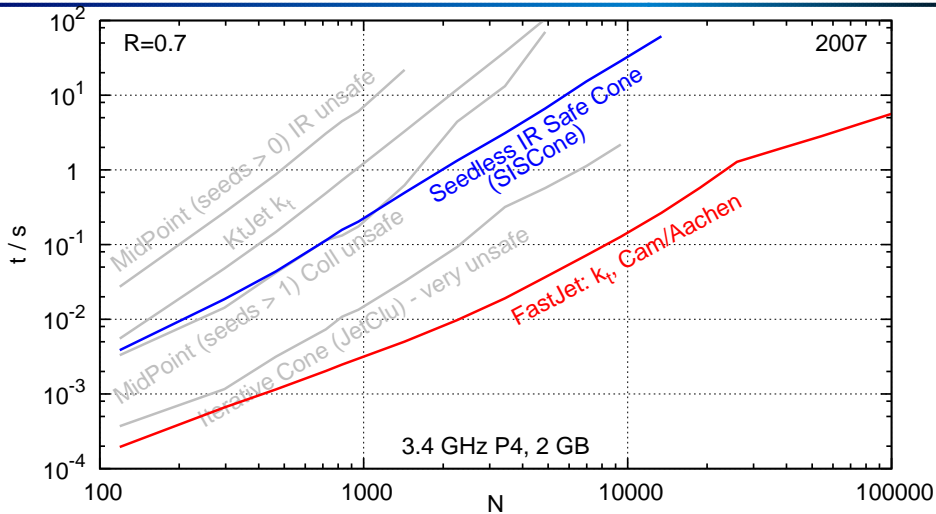
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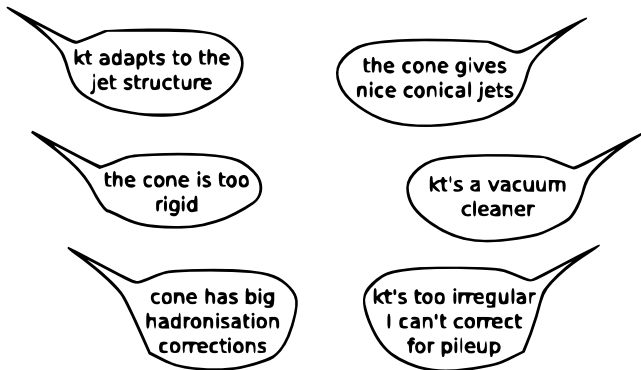
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Jet discussions: polarised, often driven by unquantified statements



Instead let's quantify things:

- ▶ Areas = susceptibility to pileup and underlying event (UE)
- ▶ Hadronisation = change in momentum from parton \rightarrow hadron level (excluding UE)

Can show that jet area goes as:

$$A = A_0 + D \frac{C_{F/A}}{\pi b_0} \ln \frac{\alpha_s(Q_0)}{\alpha_s(Rp_t)} + \mathcal{O}(\alpha_s^2 \ln p_t^2)$$

Cacciari, GPS & Soyez, prelim

Passive area: suscept. to **point-like** radiation:

	$A_0/\pi R^2$	$D/\pi R^2$
k_t	1	0.56
Cam/Aachen	1	0.08
SISCone	1	-0.06

- ▶ Analytical calcs capture main MC features
- ▶ k_t has larger area than cone, neither is πR^2
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Cacciari, GPS & Soyez, prelim

Active area: suscept. to **diffuse** radiation:

	$A_0/\pi R^2$	$D/\pi R^2$
k_t	1 → 0.81	0.56 → 0.52
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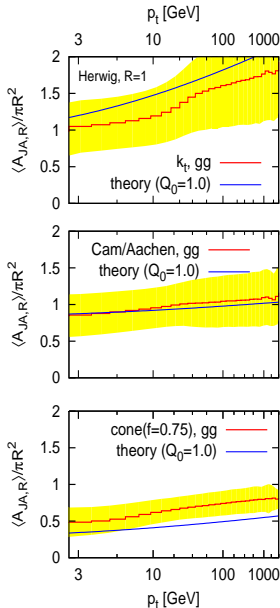
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How does the jet p_t change in parton \rightarrow hadron transition?

Methods from e^+e^- event shapes predict same at LO for all algs:

$$\text{quark jets: } \delta p_t \simeq -\frac{0.5 \text{ GeV}}{R} + \mathcal{O}(R)$$

$$\text{gluon jets: } \delta p_t \simeq -\frac{1.1 \text{ GeV}}{R} + \mathcal{O}(R)$$

Cacciari, Dasgupta, Magnea & GPS, prelim

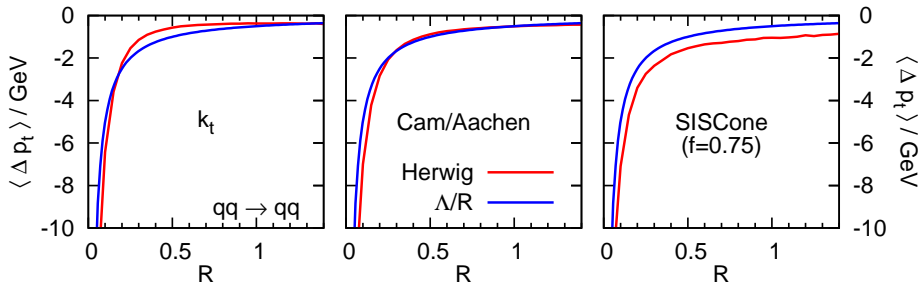
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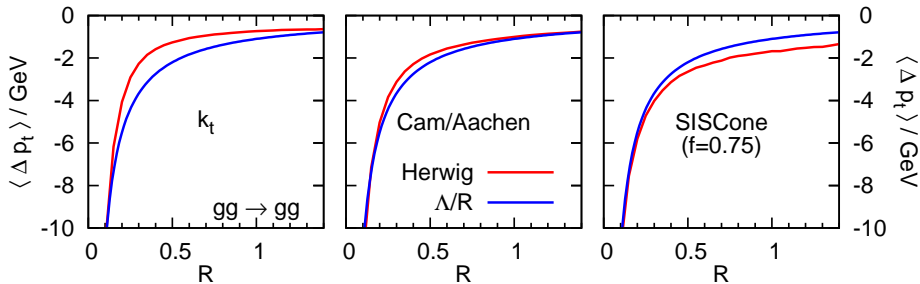
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$$\text{gluon jets: } \delta p_t \simeq -\frac{1.1 \text{ GeV}}{R} + \mathcal{O}(R)$$

Cacciari, Dasgupta, Magnea & GPS, prelim



These and other results help produce a **quantitative** picture of jet behaviour:

- ▶ Similarities between algorithms are greater than differences
- ▶ Once you have tools to quantify behaviours of algorithms you can start to think about designing new, better procedures and algorithms

Illustrations that follow:

- ▶ subtraction of pileup based on jet areas
- ▶ properly incorporating the *'flavour dimension'* into the k_t algorithm.

Basic Procedure:

- ▶ Use p_t/A from majority of jets (pileup jets) to get level, ρ , of pileup and UE in event
- ▶ Subtract pileup from hard jets:

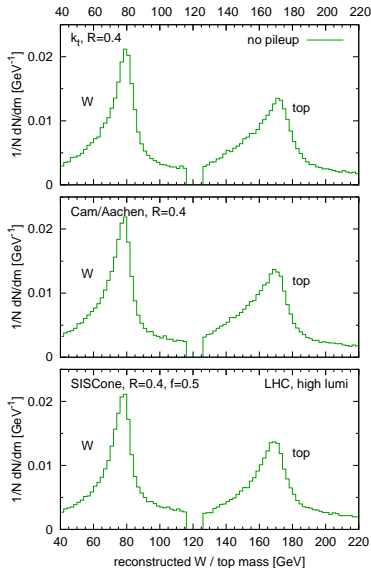
$$p_t \rightarrow p_{t,sub} = p_t - A\rho$$

Cacciari & GPS '07

Illustration:

- ▶ semi-leptonic $t\bar{t}$ production at LHC
- ▶ high-lumi pileup (~ 20 ev/bunch-X)

Same simple procedure works for a range of algorithms



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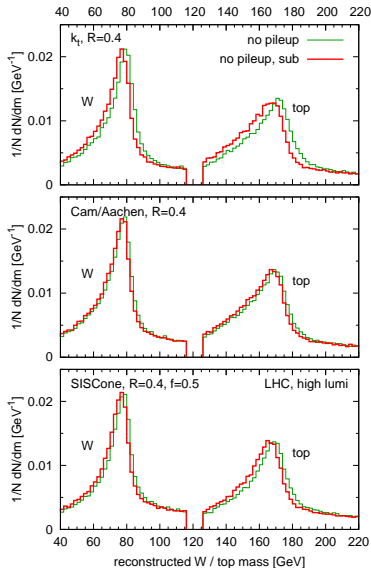
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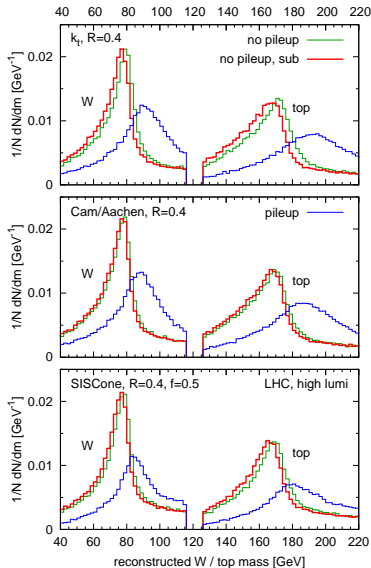
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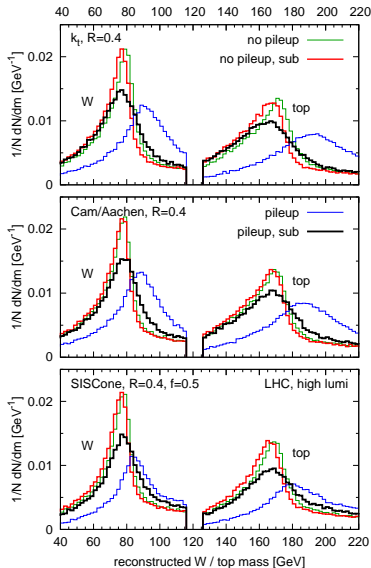
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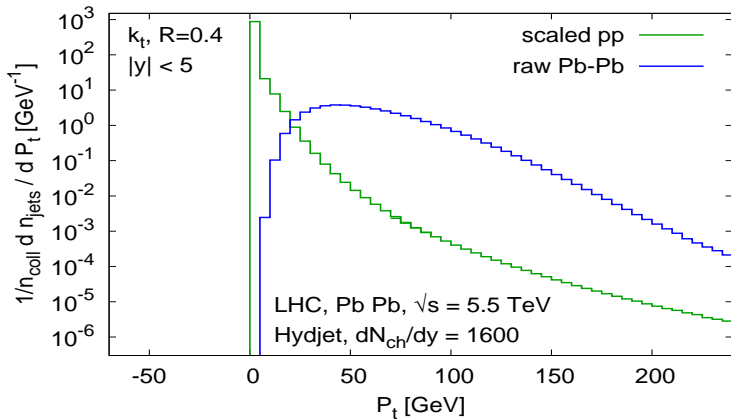
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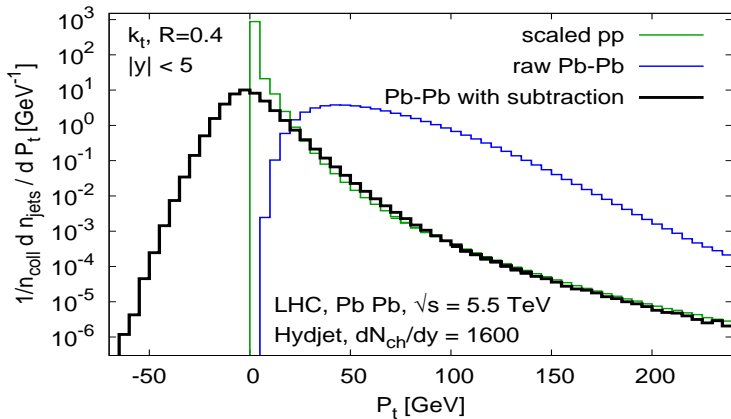
Example: inclusive jet spectrum

- ▶ Speed makes it easy to run k_t and Cam/Aachen on all 30k particles in HI event
- ▶ Subtraction provides a way to get sensible results, without biases from cut on low- p_t particles.

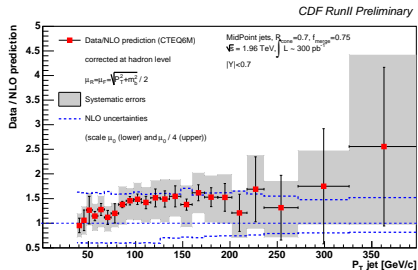


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One of the least accurate NLO predictions is for b -jets: $\pm \sim 50\%$



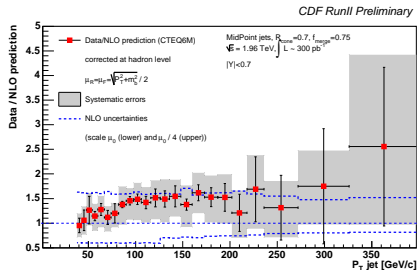
Experimental definition

- ▶ Run normal jet-algorithm
- ▶ a jet containing $\geq 1 b, \bar{b}$ is a b -jet.

Even though $m_b \ll p_t$, this b -jet definition requires a fully massive calculation, and *higher order terms are enhanced by powers of $\ln p_t / m_b$.*

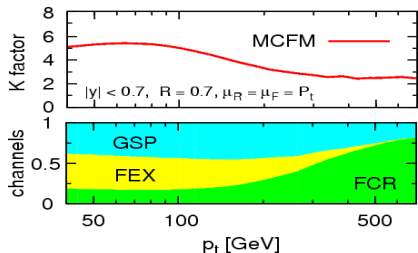
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Jet with b and \bar{b} is *not a b -jet*

Non-trivial experimentally

But removes many logs

'Flavour- k_t ' distance measure:

$$d_{ij} = \frac{\Delta R_{ij}^2}{R^2} \times \begin{cases} \min(k_{ti}^2, k_{tj}^2) & \text{harder is } \not{b} \\ \max(k_{ti}^2, k_{tj}^2) & \text{harder is } b \end{cases}$$

Reflects different divergences for q, g

This allows one to

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Collinear factorisation
- ▶ No logs left → take massless limit
- ▶ **Bring uncertainty down from 50% to 15%.**

Banfi, GPS & Zanderighi '06, '07

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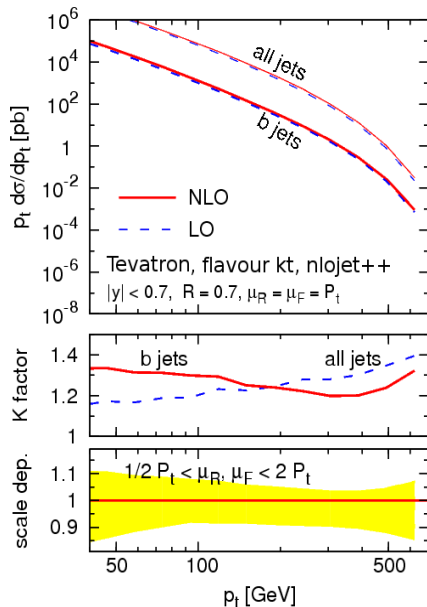
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- ▶ proper (seedless) cone algorithm is now a reality, eliminating need for hacks & approximations

Different jet algorithms starting to be compared quantitatively

- ▶ Measures of jet areas (\rightarrow surprises: cone area not πR^2)
- ▶ Hadronisation has simple fairly universal $1/R$ behaviour
- ▶ Many comparisons in progress for *Les Houches Workshop*

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