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# Hadronic final states and resummation

Gavin Salam

LPTHE — Univ. Paris VI & VII and CNRS

HERA–LHC workshop

26 March 2004

# Background and Aim [of HERA LHC Workshop]

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<http://www.desy.de/~heralhc/#aim>

The impact of measurements made at HERA, present and future, on the physics of the LHC is potentially large. However, this potential is currently not as well explored as e.g. the more obvious connection between the Tevatron and the LHC.

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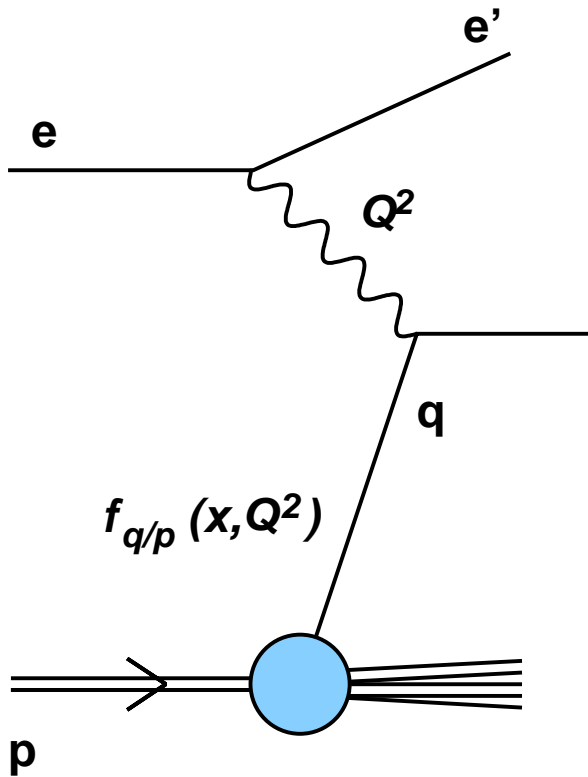
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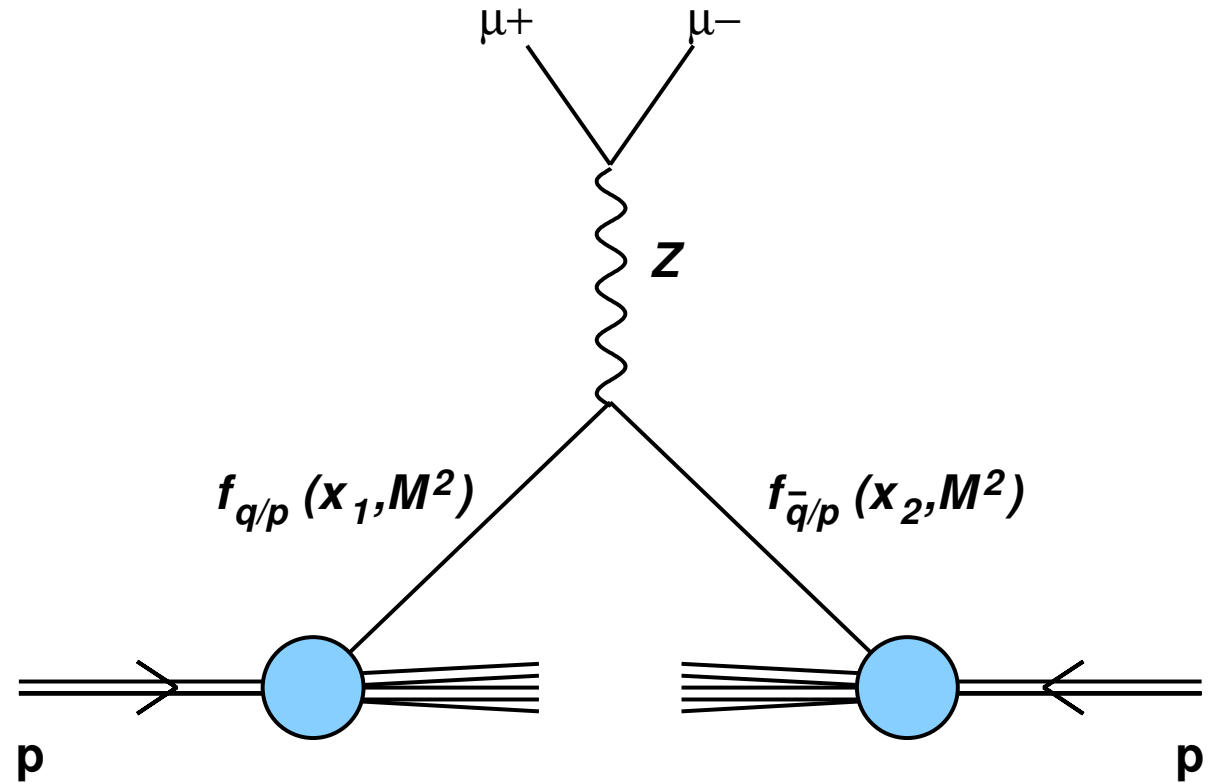
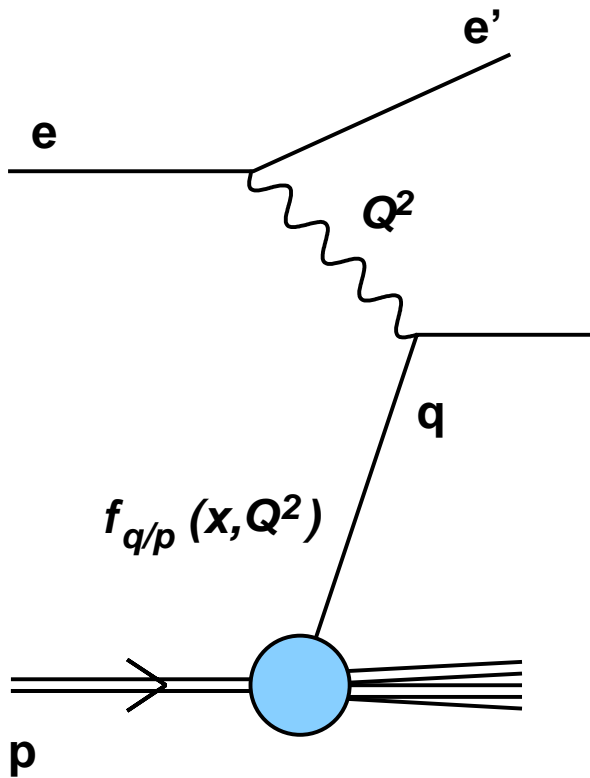
The most obvious area of impact is in the determination of proton structure from very low to very high  $x$ , which is measured precisely at HERA. **Other topics include QCD production of heavy flavors and the study of multi-jet final states, energy flows and structure of underlying events.**

# 'Problem' is (collinear) factorization



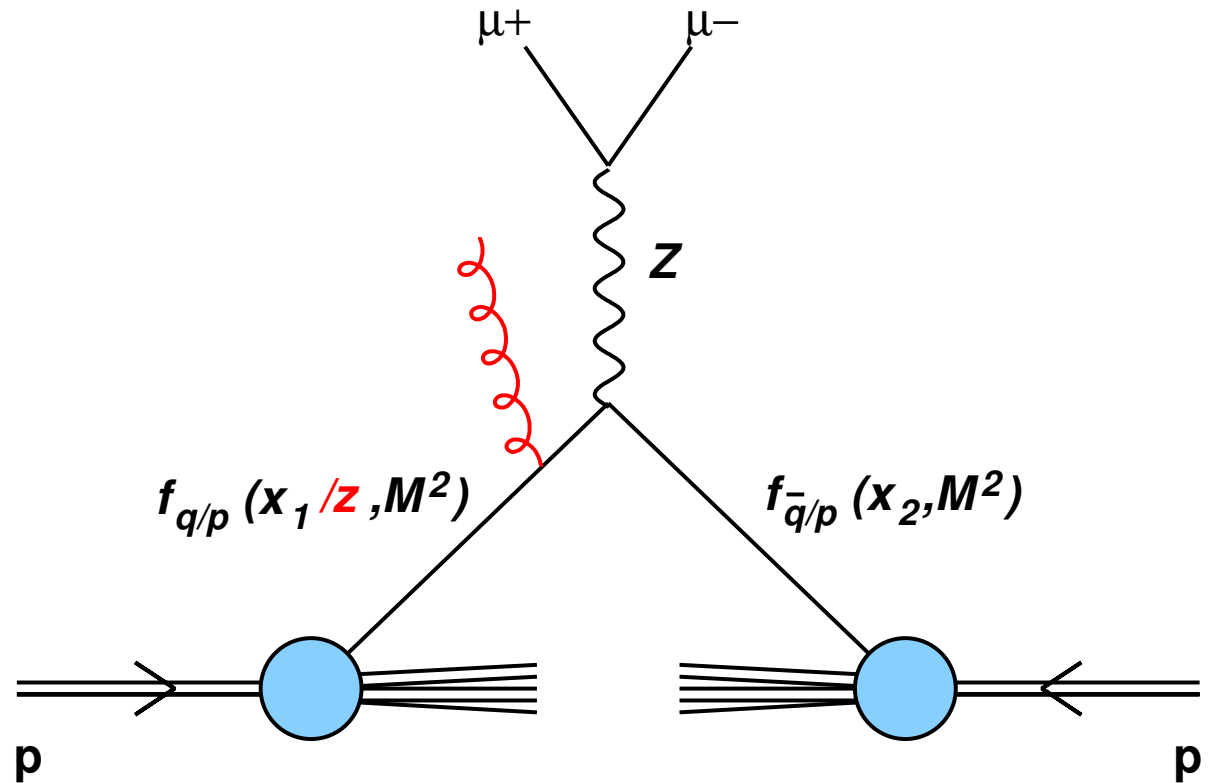
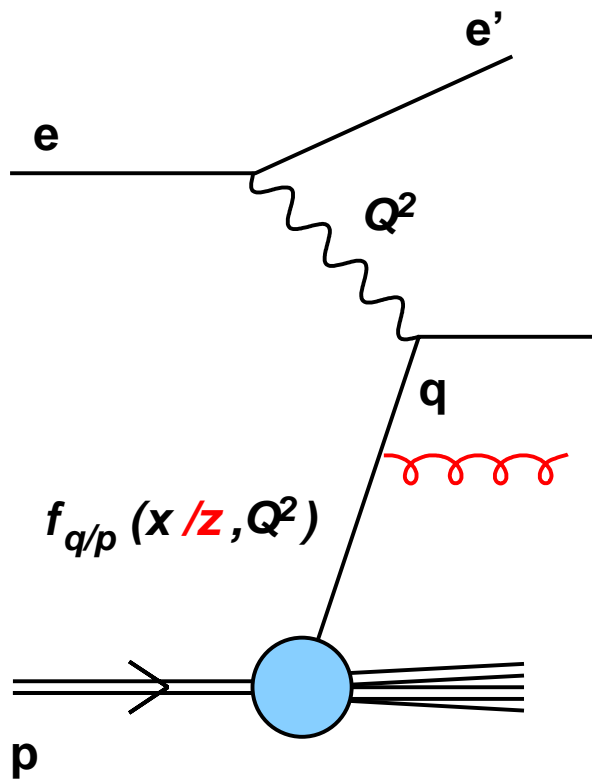
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- Measure PDFs, measure  $\alpha_s(Q^2)$ , evolve with DGLAP
- Predict, perturbatively, cross sections for other hard processes
- Predict, perturbatively, any (infrared-collinear safe) final-state observable  
[Initial-state collinear singularities are absorbed into PDFs]

# Final-state tools based on pert. QCD & coll. fact.

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- LO calculations with many partons / arbitrary final states
  - NJETS, VECBOS, ALPGEN, COMPHEP, GRACE, AMEGIC, ...
- NLO calculations (2 jets, 3 jets)
  - JETRAD, DYRAD, MEPJET, DISENT, DISASTER++, JETVIP, NLOJET, MCFM, PHOX family, ...
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  - coming soon...



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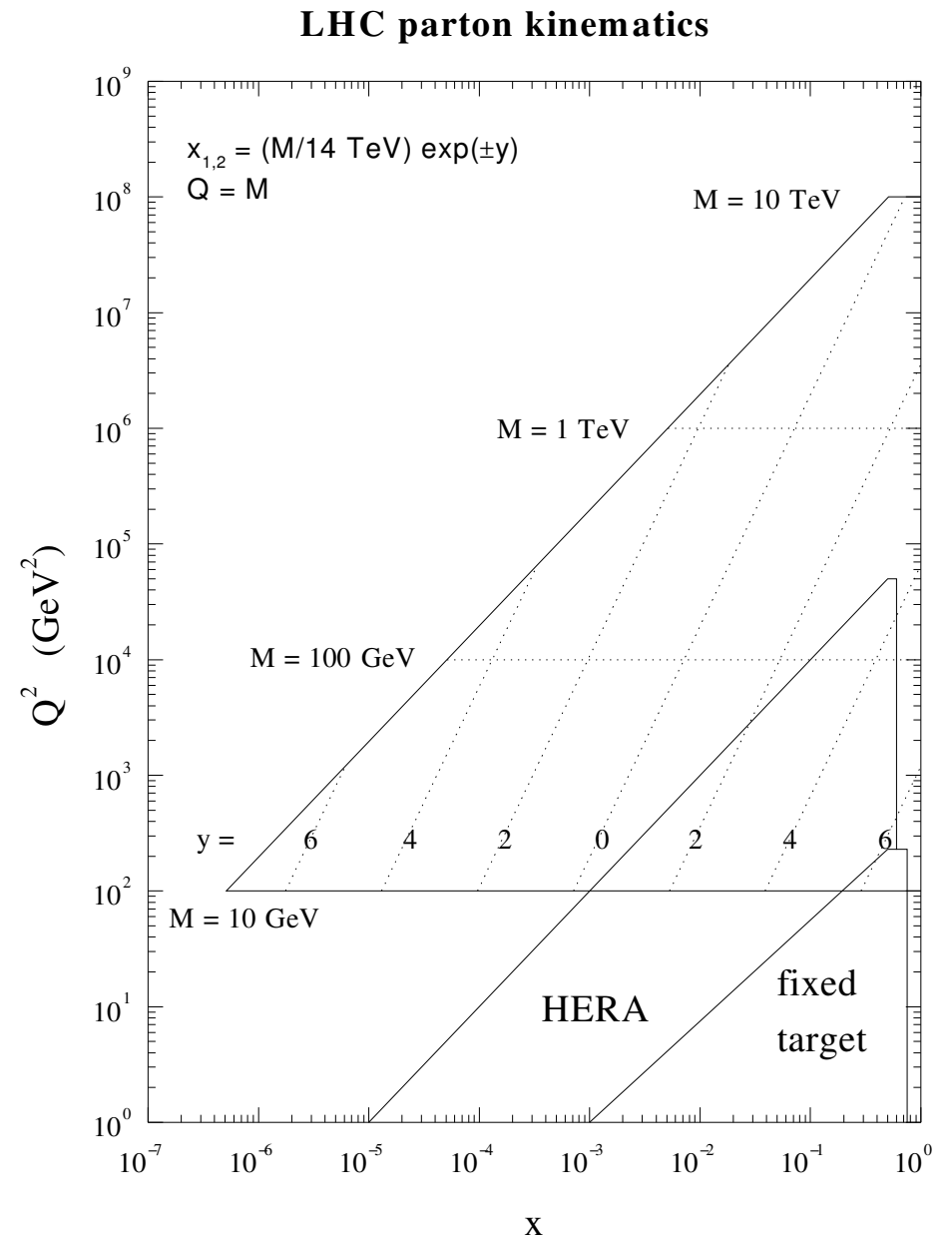
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*So that's all we need from HERA...*

# How might HERA final-states be useful to LHC?

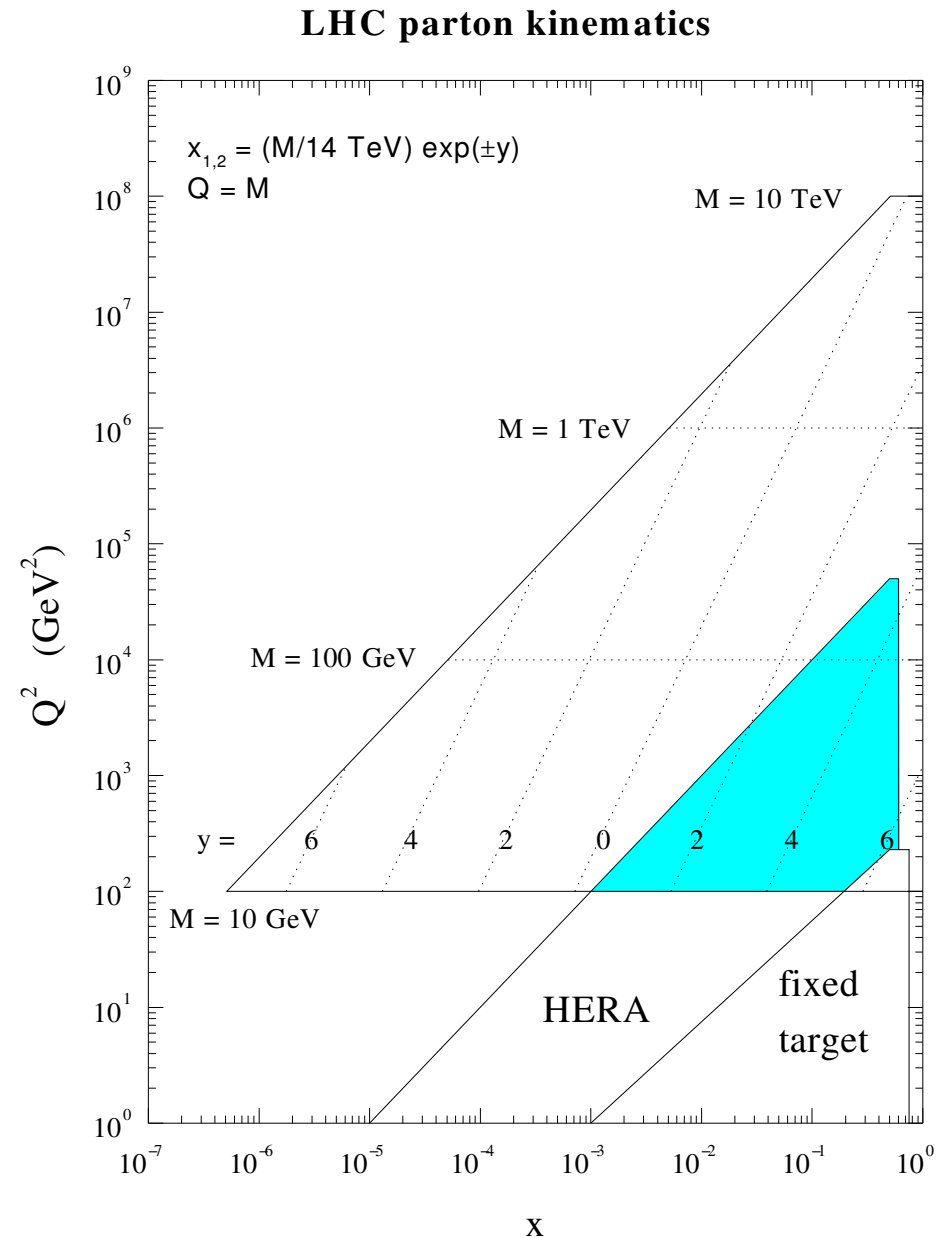
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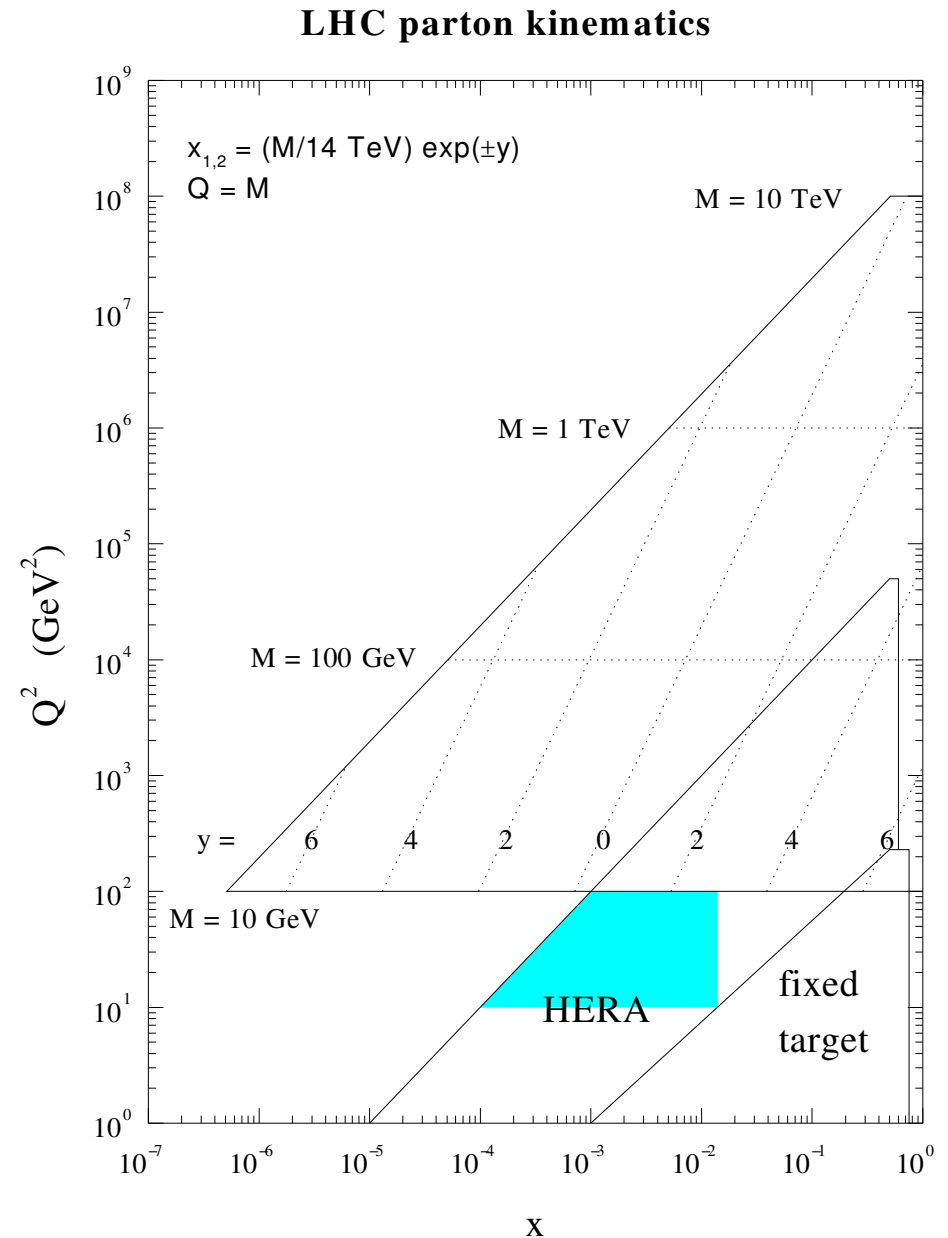
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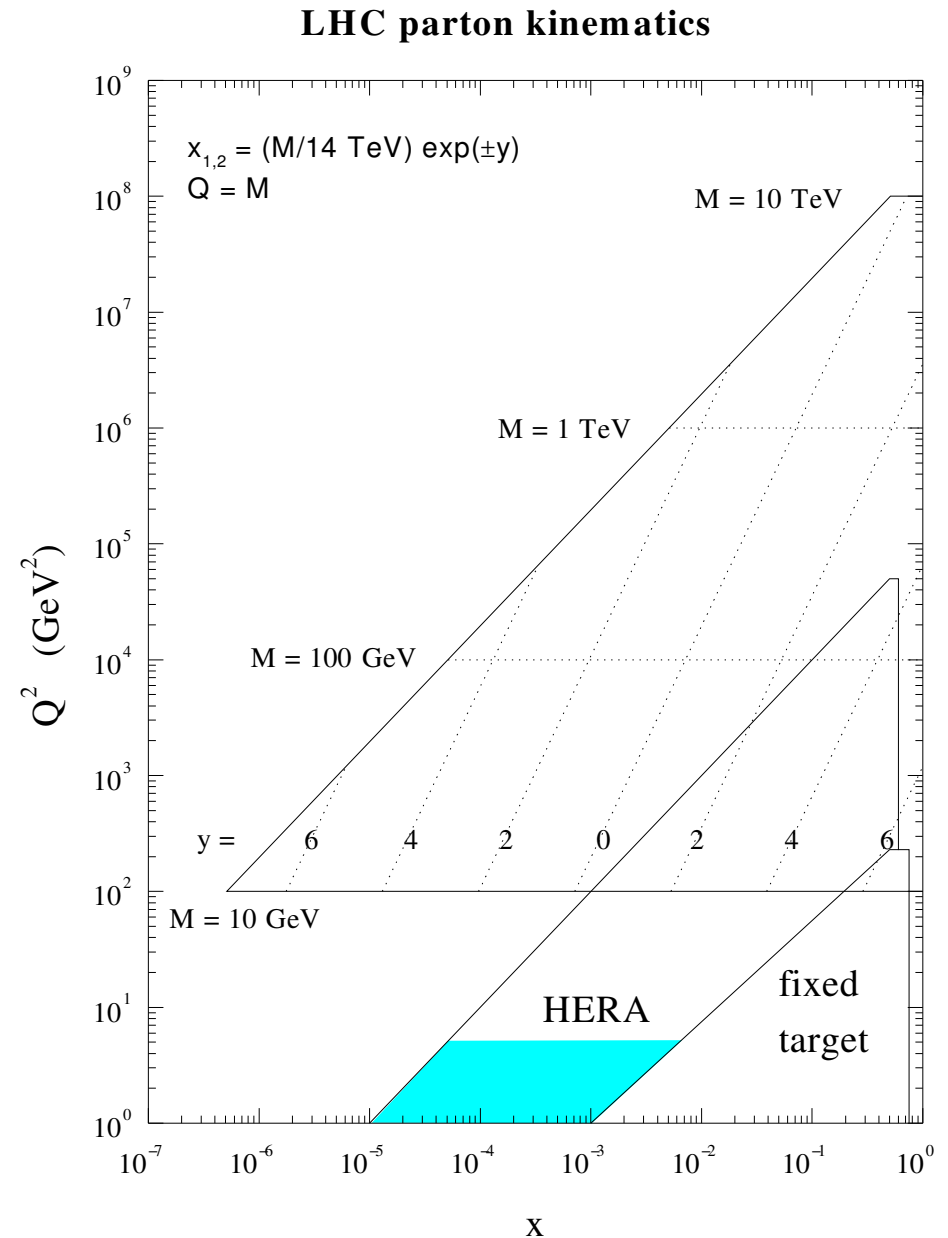
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- low  $Q$ , small  $x$ 
  - BFKL, saturation & high parton densities?
  - Relevant for minimum bias & underlying event at LHC?

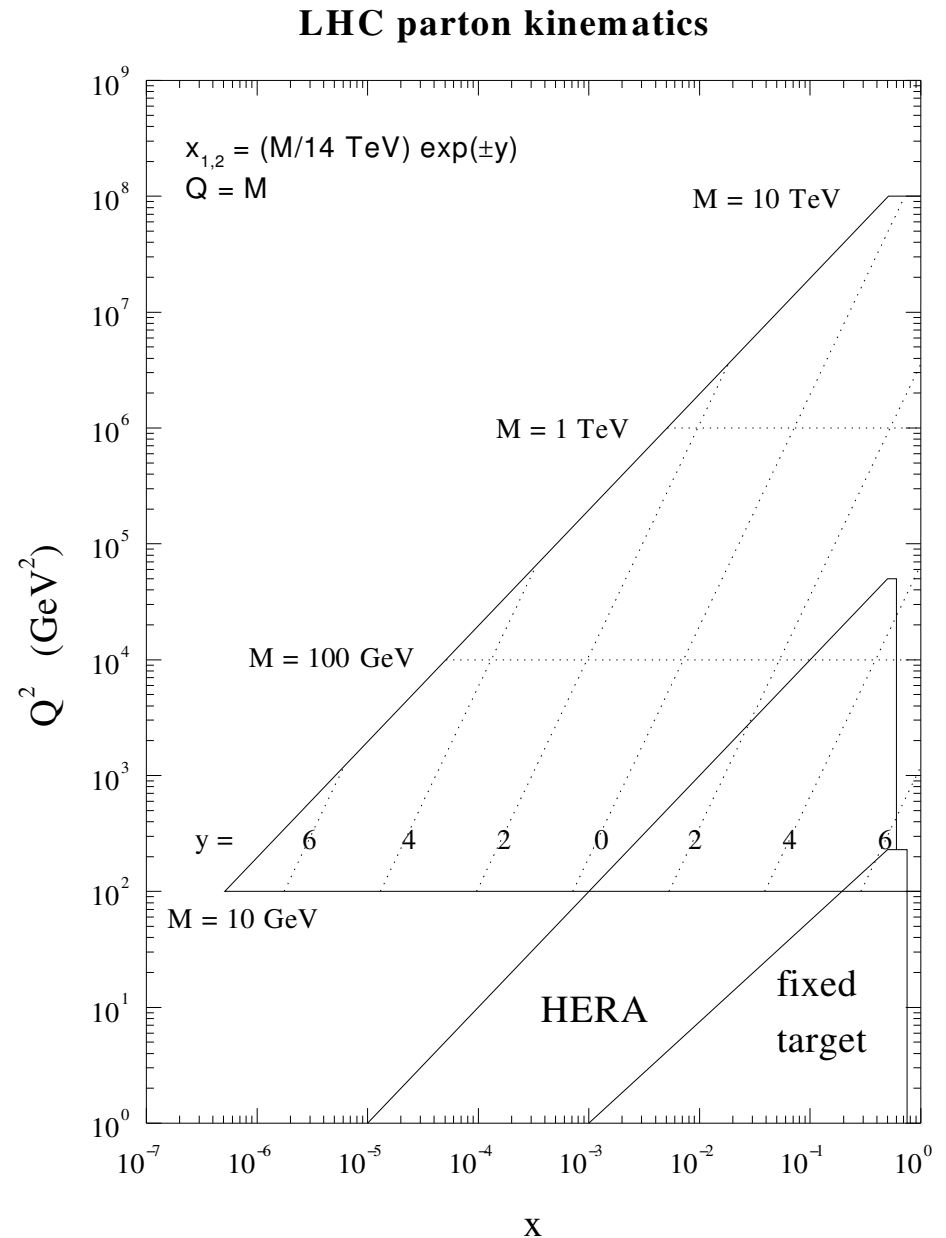




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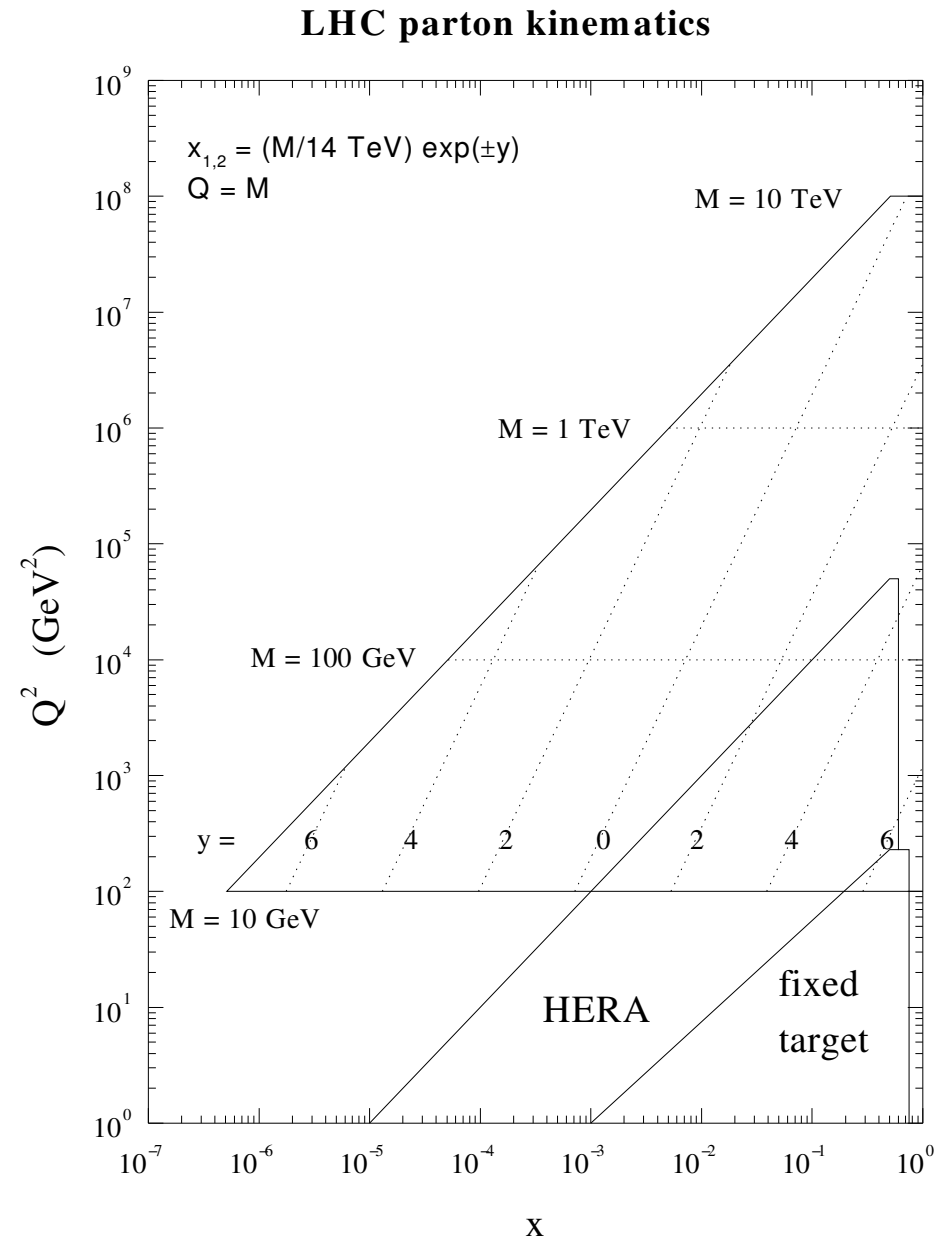


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→ Bartels



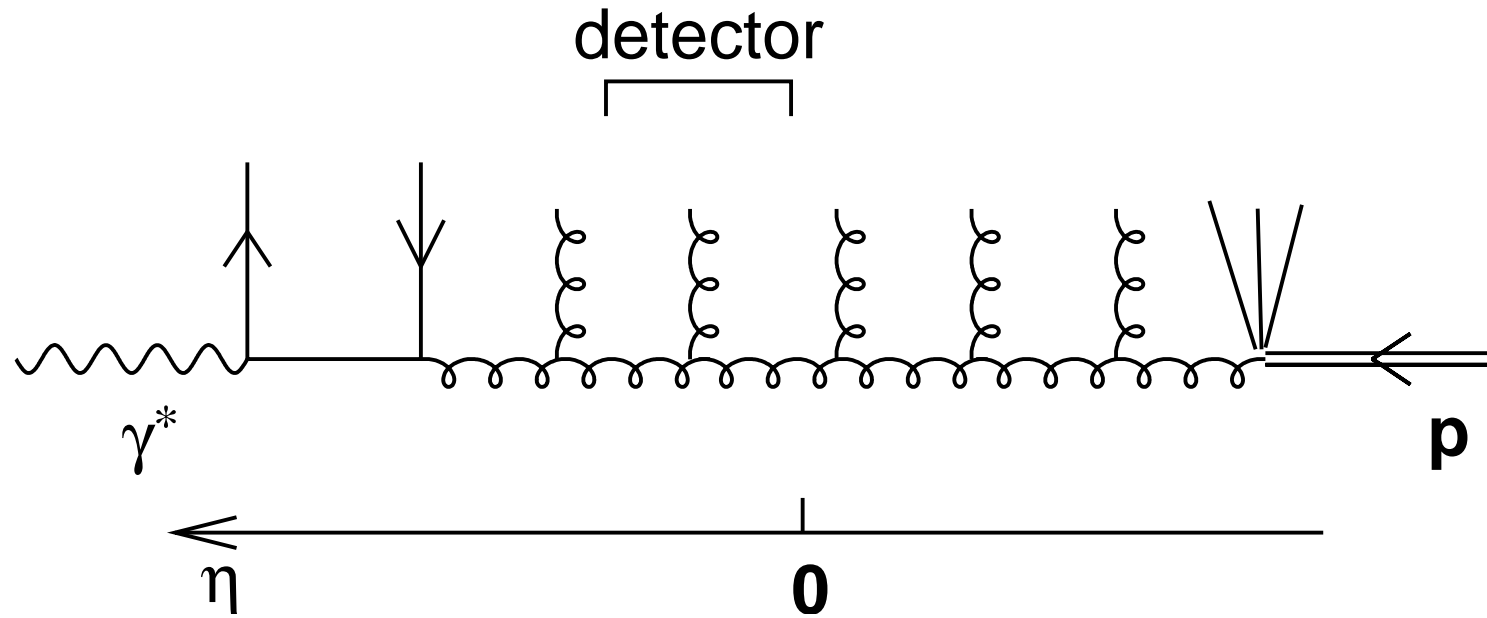
# What works, what does not

SMALLX 'collaboration' hep-ph/0312333	collinear factorization				$k_t$ - factorization
	direct		resolved		
	LO+PS	higher order NLO (dijet)	LO+PS	higher order NLO (dijet)	LO+PS
<b>HERA observables</b>					
DIS $D^*$ production photoprod. of $D^*$	ok	ok	?	?	ok
DIS B production (visible)	ok	ok	—	—	ok
DIS B production (total)	no	ok	—	—	no
photoprod. of B (visible)	ok	?			ok
photoprod. of B (total)	no	no	?	?	ok
high $Q^2$ di-jets	?	ok	?	?	?
low $Q^2$ di-jets (cross sec.)	?	ok	?	no	?
low $Q^2$ di-jets (azim.corr.)	no	no	ok	?	ok
photoprod. of di-jets	?	NLO 3-jet no ok	?	no ok	?
particle spectra	no	—	ok	—	ok
energy flow	no	—	ok	—	?
<b>HERA small-<math>x</math> observables</b>					
DIS forward jet production	no	no	ok	ok	ok
DIS forward $\pi$ production	no	?	ok	?	1/2
DIS $J/\psi$ prod.	?		?	?	ok
photoprod. of $J/\psi$	no	ok		ok	ok
$J/\psi$ polarization				low.stat.	low.stat.

# What works, what does not

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particle spectra energy flow	no no	— —

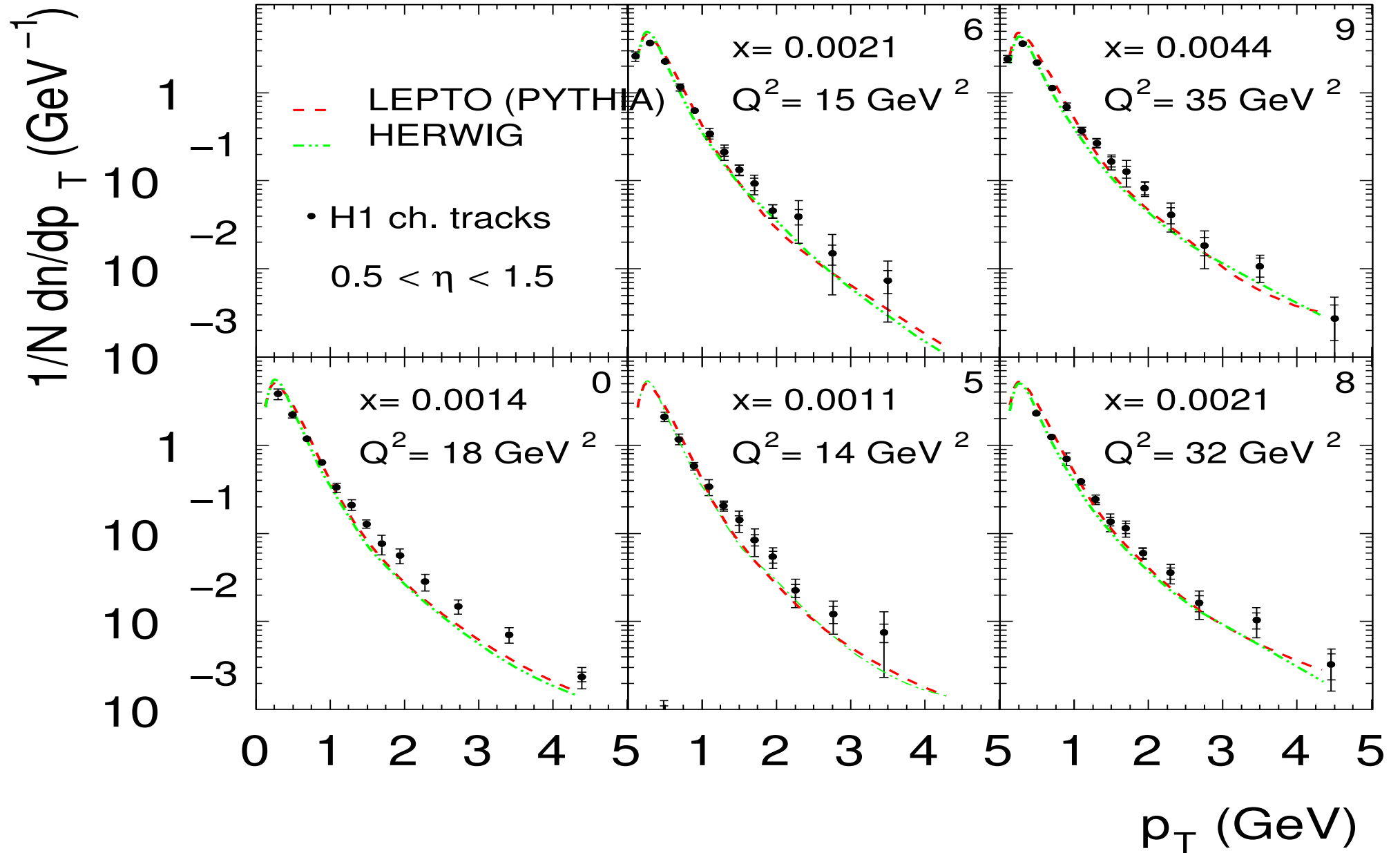
# E.g.: charged-particle $p_t$ spectra



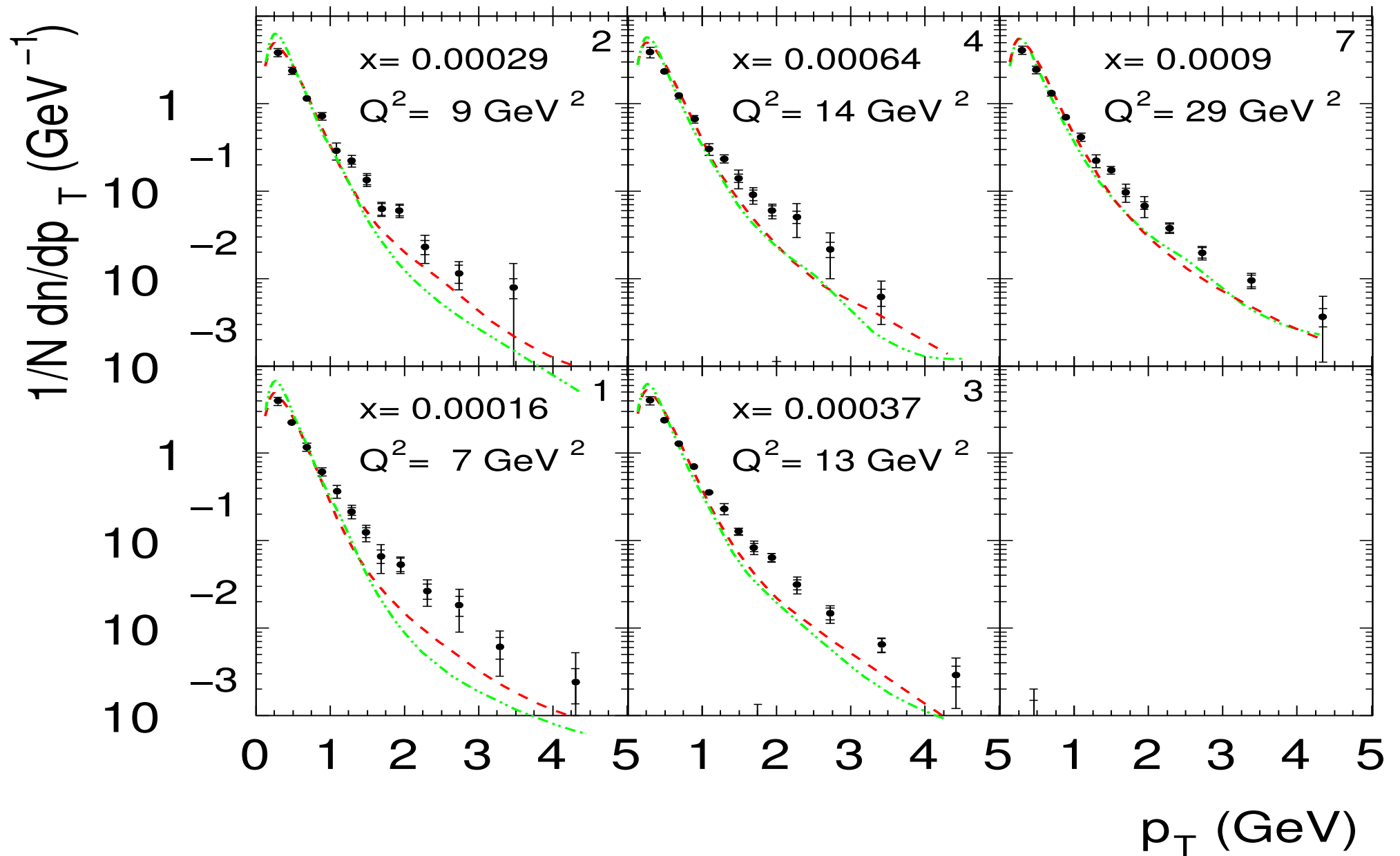
Study charged particle spectra as a function of

- photon virtuality  $Q^2$
- Bjorken- $x$
- particle rapidity

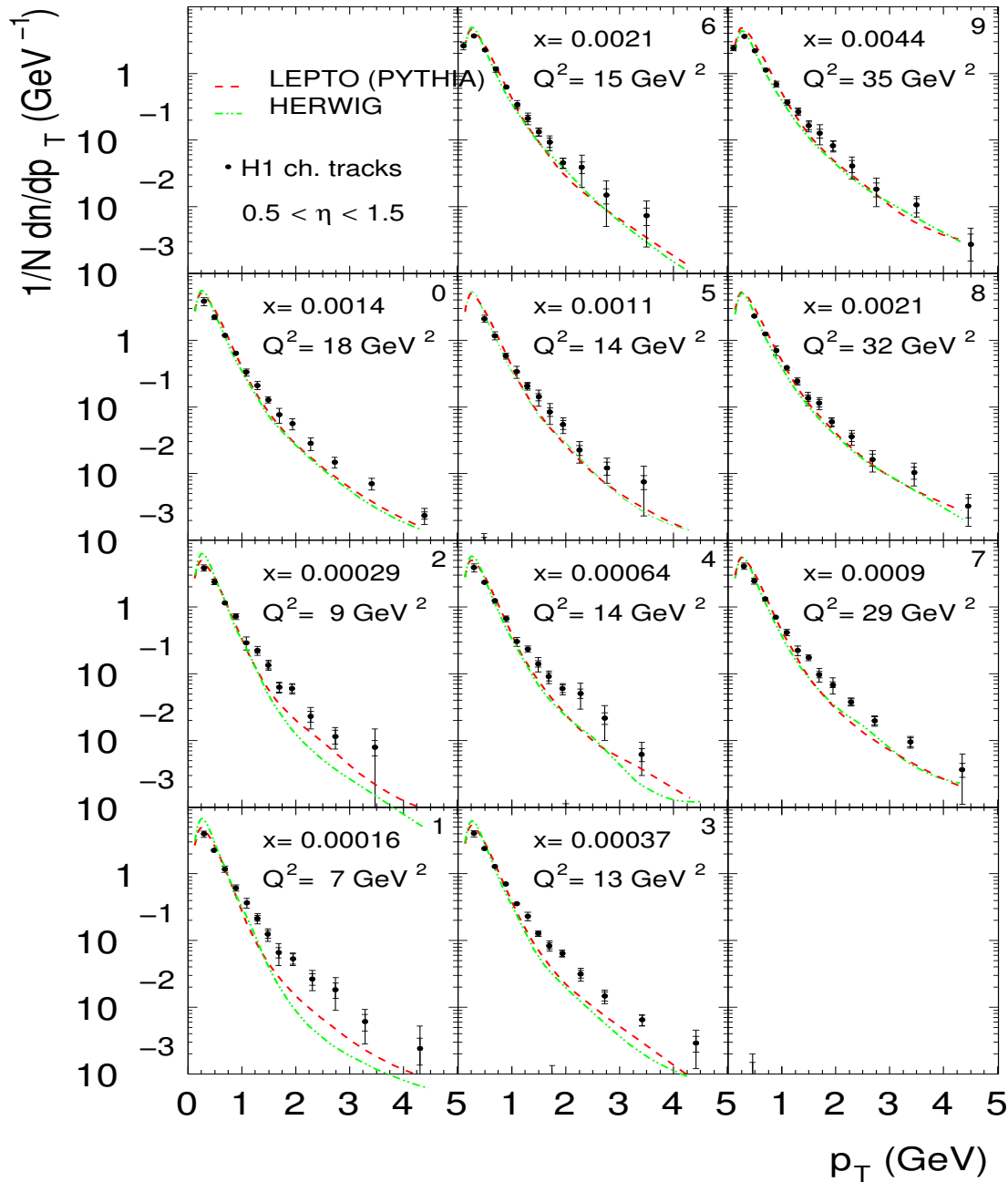
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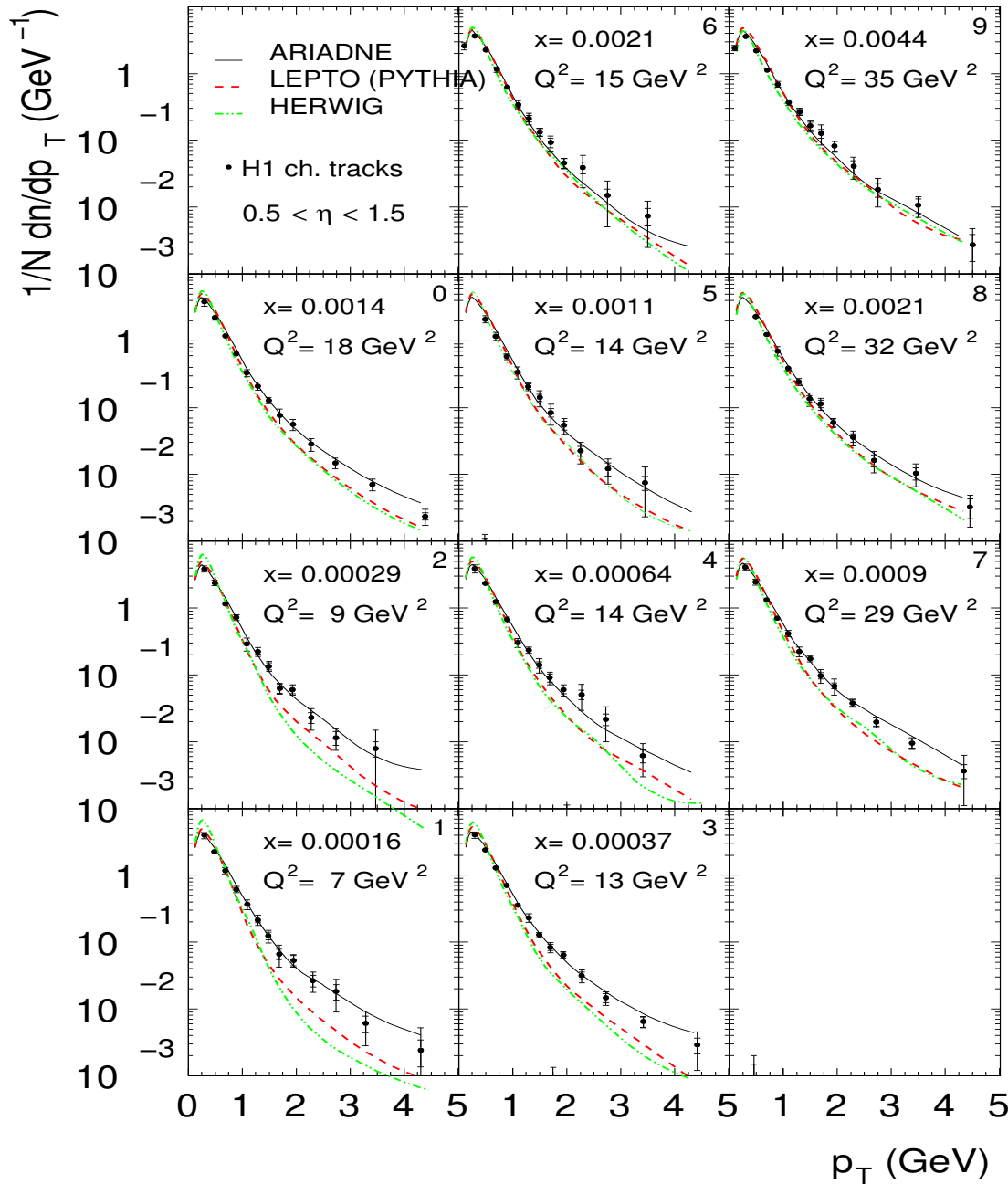
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- Independently of  $Q^2$ , clear problem for PYTHIA & HERWIG at  $x \lesssim 10^{-3}$ .

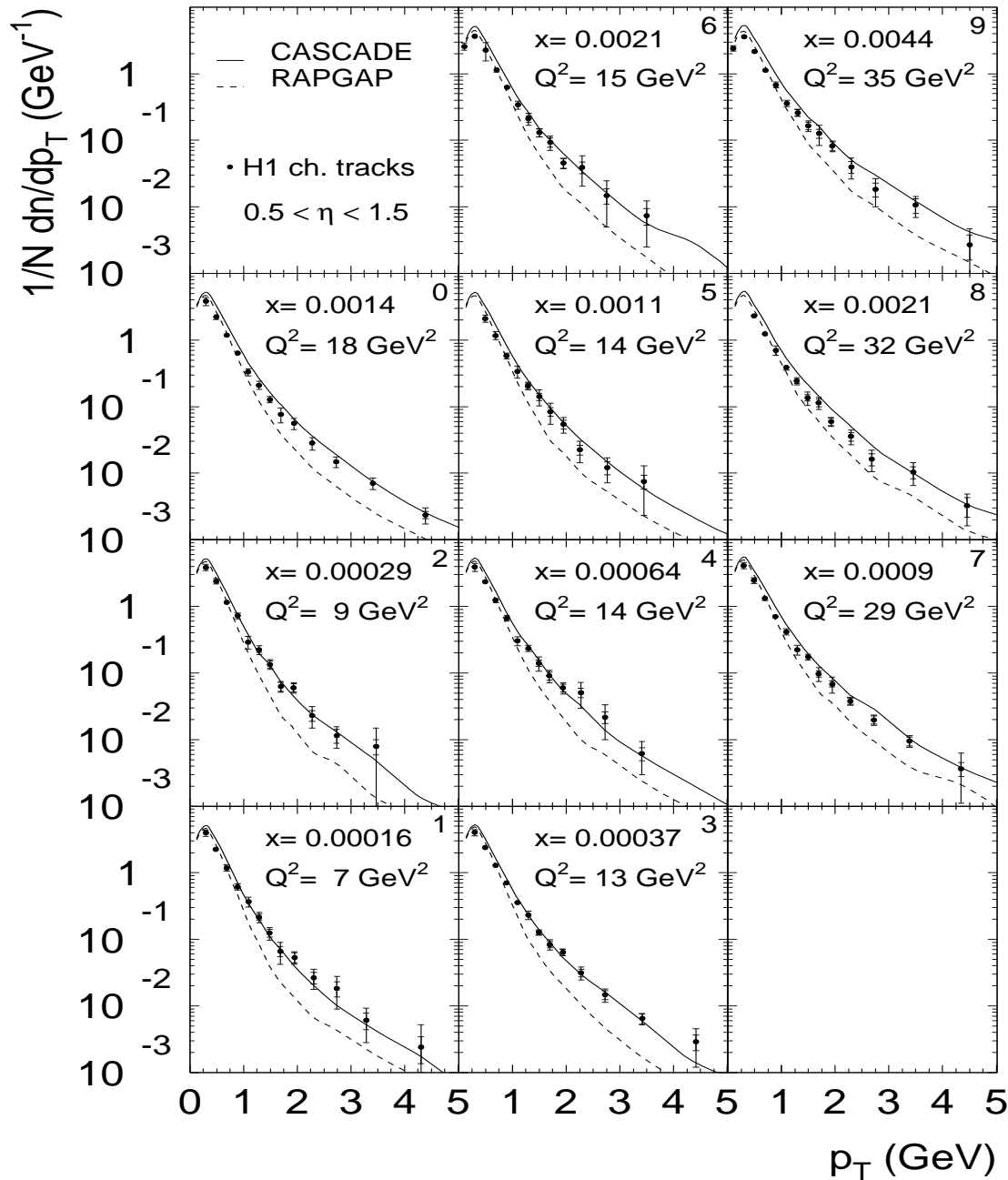


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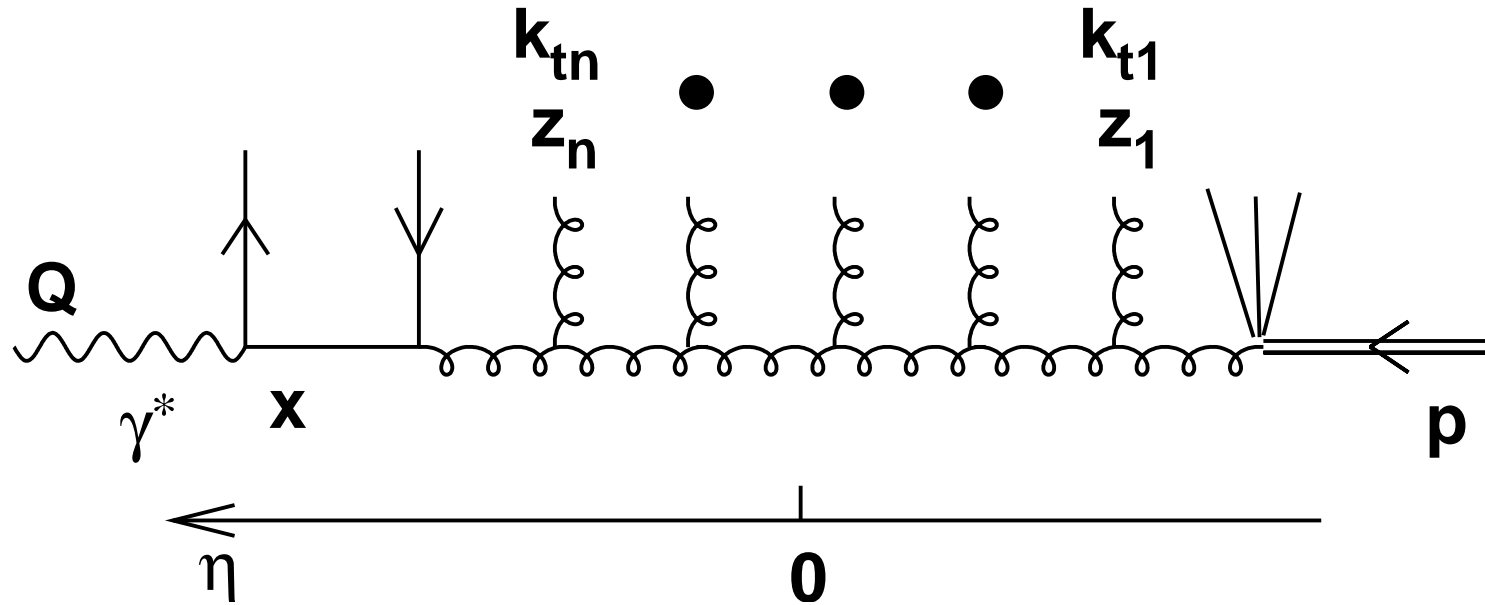
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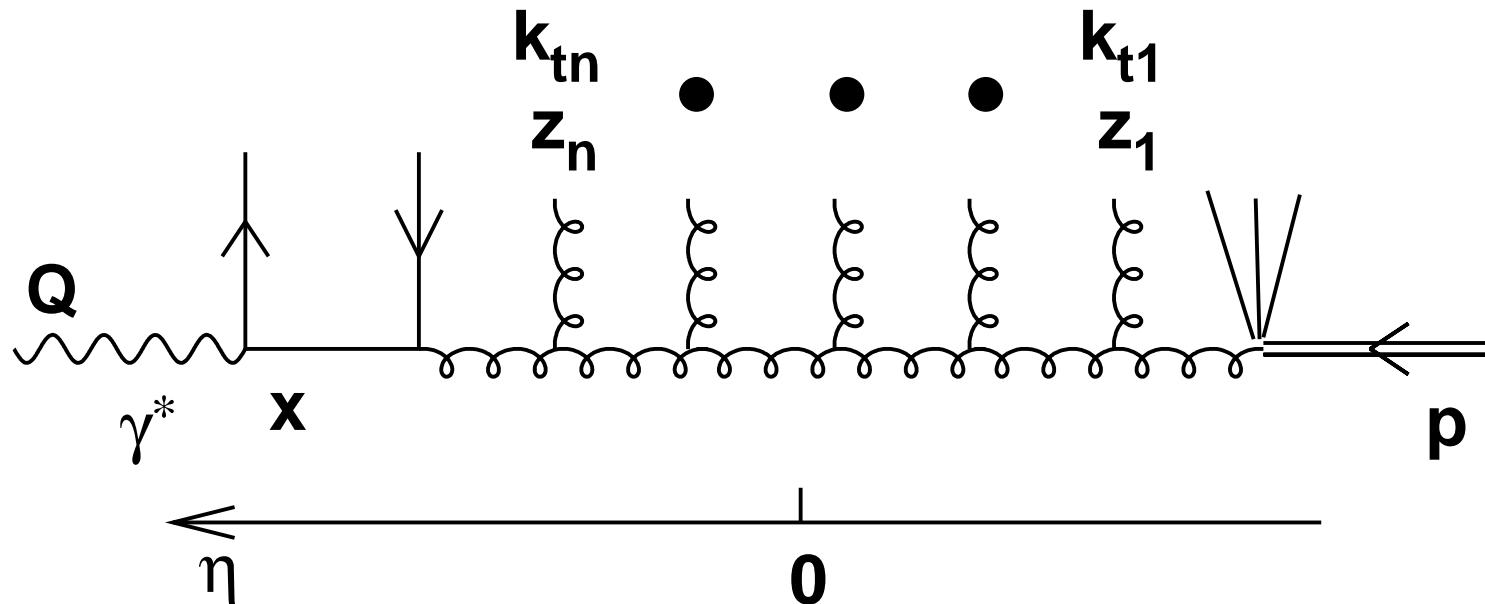


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- Theoretical interpretation unclear
- CASCADE (& LDC) does too
- CASCADE & LDC are CCFM/BFKL based — they resum  $(\alpha_s \ln x)^n$
- Is this a sign of onset of small- $x$  effects?

# Brief recap on small- $x$ effects (BFKL/CCFM)



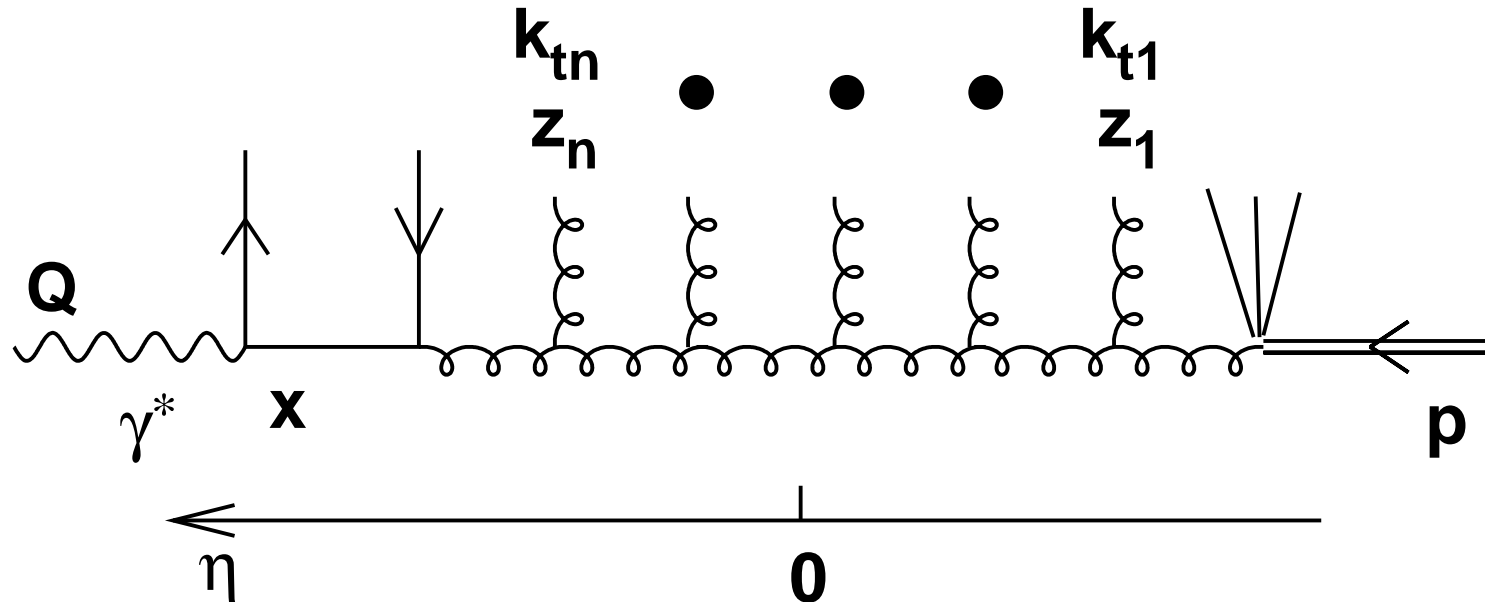
# Brief recap on small- $x$ effects (BFKL/CCFM)



## Collinear factorization

- transverse momentum ordering  
 $Q \gg k_n \gg \dots \gg k_1$
- resummation of  $(\alpha_s \ln Q)^n$
- $k_t$  unordered configs are suppressed by powers of  $\alpha_s$
- theoretically very well understood

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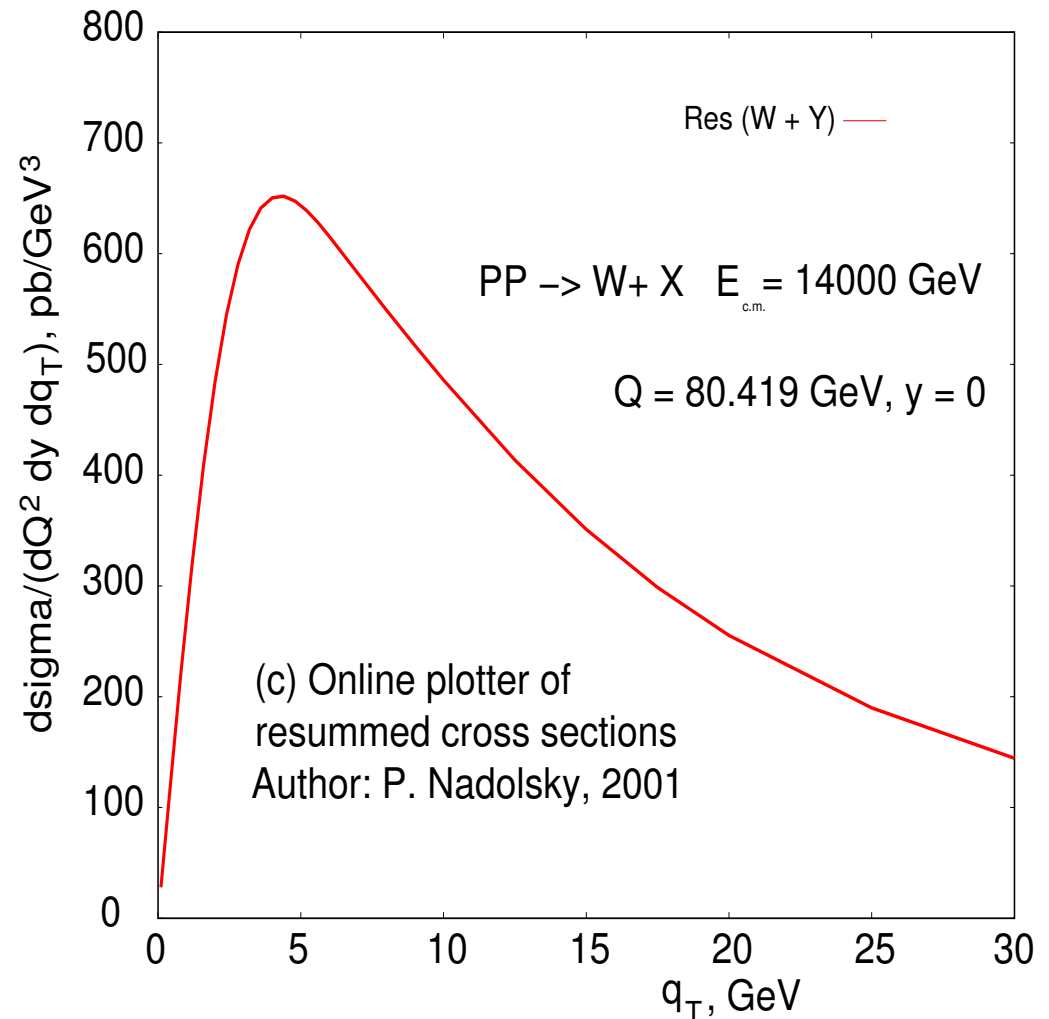
## Small- $x$ resummation

- longitudinal momentum ordering  
 $x_{Bj} \ll z_n \ll \dots \ll z_1$
- resummation of  $(\alpha_s \ln x)^n$
- $k_t$  unordered configs **dominate**
- theory treatment is 'work in progress'

- Light Higgs and W/Z bosons are produced at moderately small  $x \lesssim 10^{-2}$ .
- Effective scale for PDFs in total X-section is  $\sim M_{W/Z/H}$

# W/Z and Higgs $q_T$ spectra

- Light Higgs and W/Z bosons are produced at moderately small  $x \lesssim 10^{-2}$ .
- Effective scale for PDFs in total X-section is  $\sim M_{W/Z/H}$
- But  $q_T$  distribution of boson is concentrated in small(ish)  $q_T$  region  
↳ dangerous region at HERA?



# Relevance of HERA ‘problems’ to LHC W/Z/H $q_T$ dists.?

---

## Not a simple issue

- Small- $x$  discrepancy is in *tail* of particle  $p_t$ -spectrum at HERA: at  $Q \sim 5 \text{ GeV}$ , particles with  $p_t \simeq 5 \text{ GeV}$  are quite rare.
- $q_T$  of W/Z/H has origin in Sudakov logarithms,  $\alpha_s \ln^2(M^2/q_T^2)$  — the 5 GeV peak is the *typical* transverse momentum.
- Rare small- $x$  effects may well be swamped by Sudakov effects.



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## Two existing approaches

- Apply usual Sudakov  $q_T$  resummation approach at HERA
  - extract ‘extra’  $x$ -dependence
  - put it into calculations for LHC
- Apply CCFM/Cascade approach directly to LHC (only H)

# Sudakov resummation at HERA?

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Use crossing symmetry

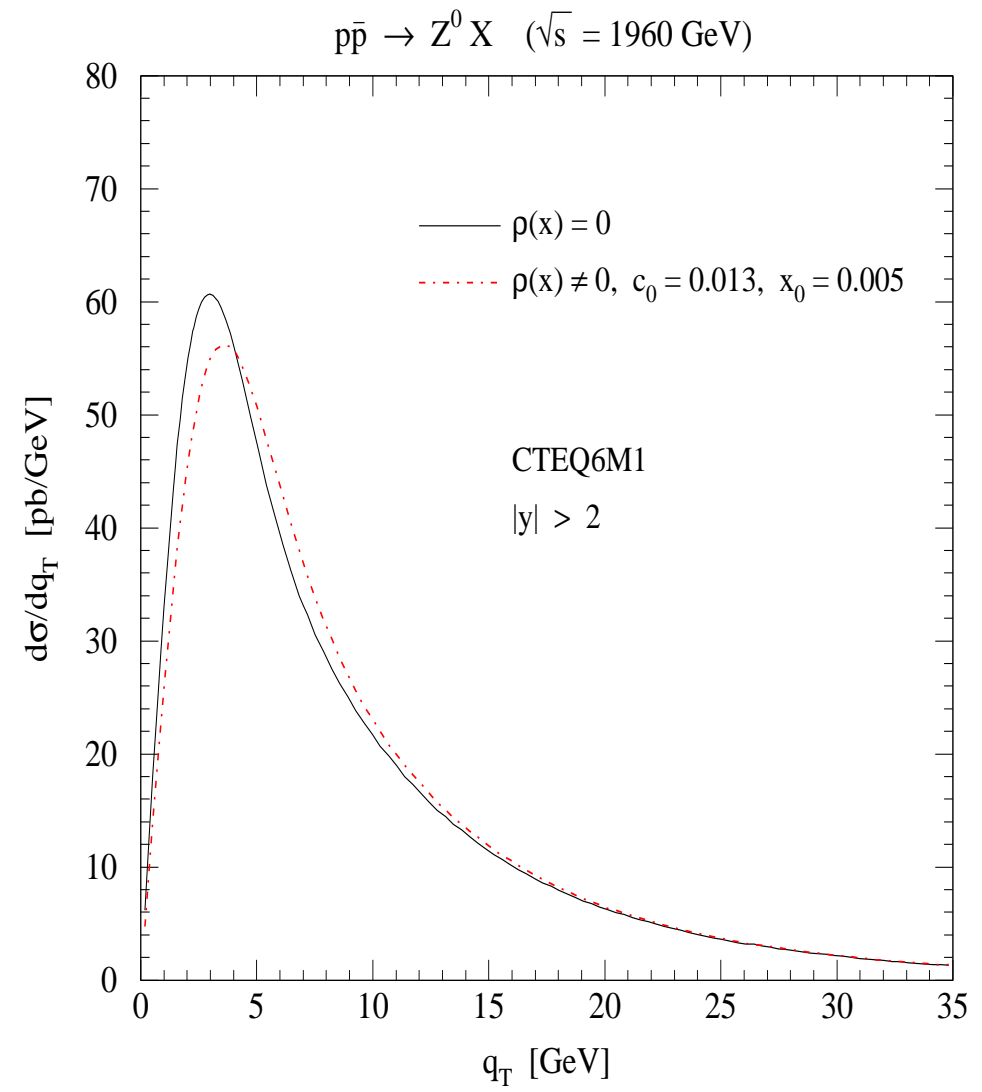
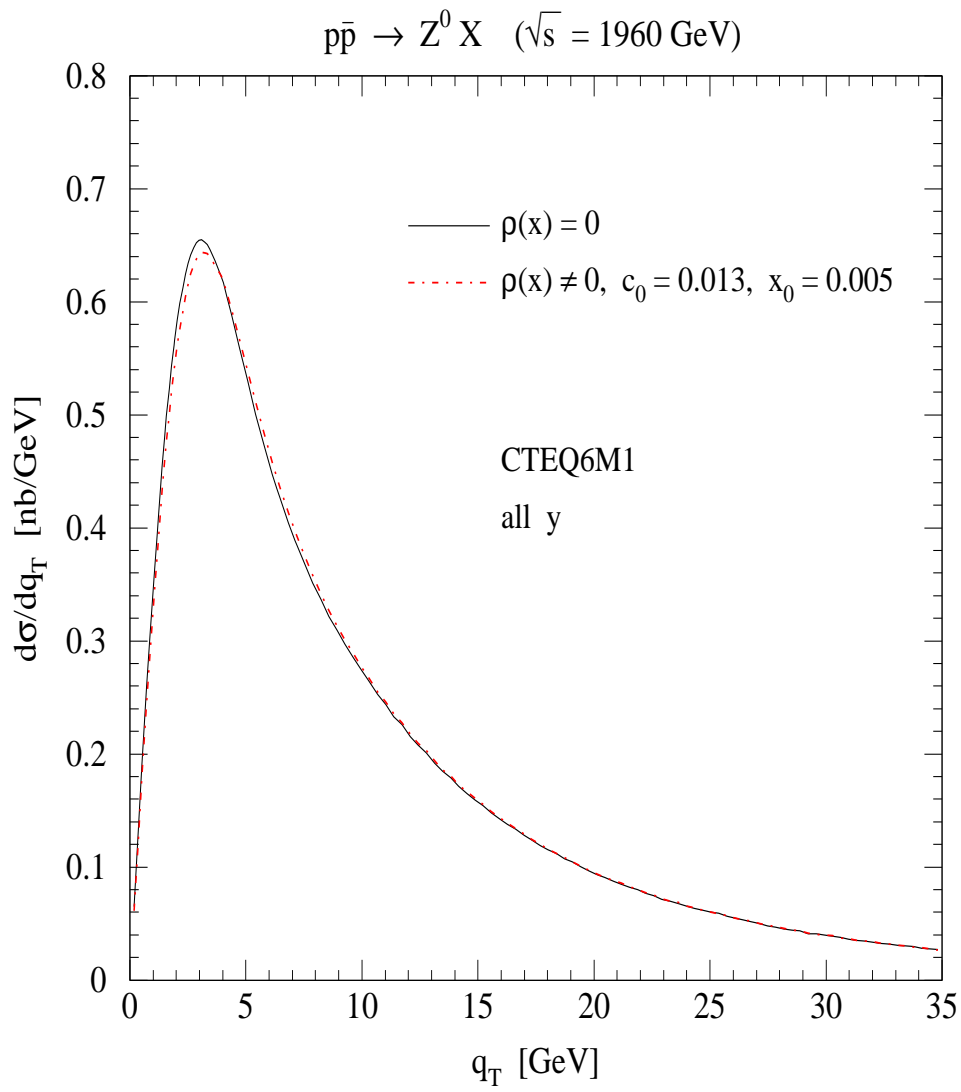
Meng, Olness & Soper, '95

$$h_1 h_2 \rightarrow \ell^+ \ell^- + X \iff h_1 \ell^- \rightarrow \bar{h}_2 \ell^- + X$$

- trade incoming proton for (energy-weighted sum over all) outgoing hadrons
- resum the photon relativistically invariant transverse momentum ( $q_T$ ) with respect to  $h_1, \bar{h}_2$ .
  - $q_T$  is closely related to  $h_2$ 's rapidity, not its  $p_t$ !
- Allow for small- $x$  effects in a 'non-perturbative' correction to Sudakov form factor
  - found, phenomenologically, to grow rapidly with decreasing  $x \lesssim 10^{-2}$

Nadolsky, Stump, Yuan, '00

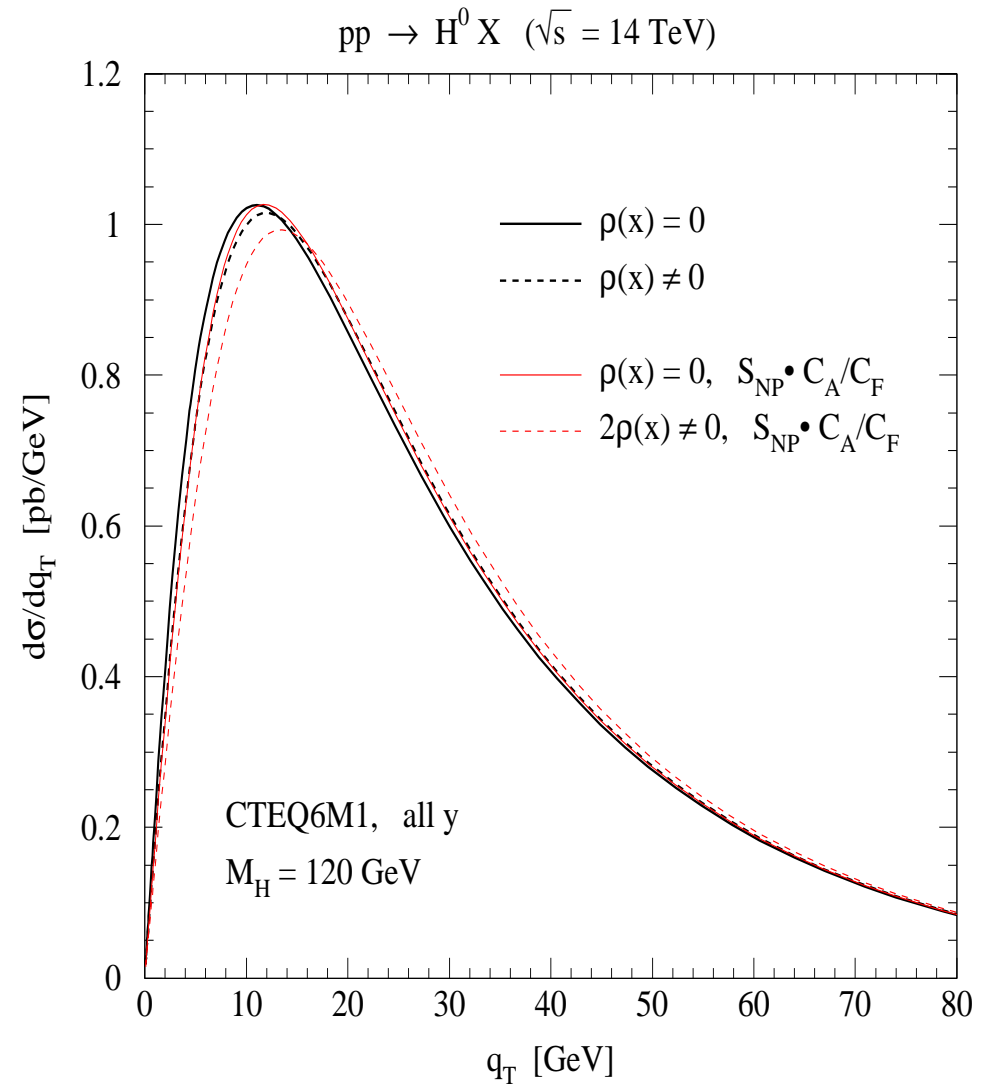
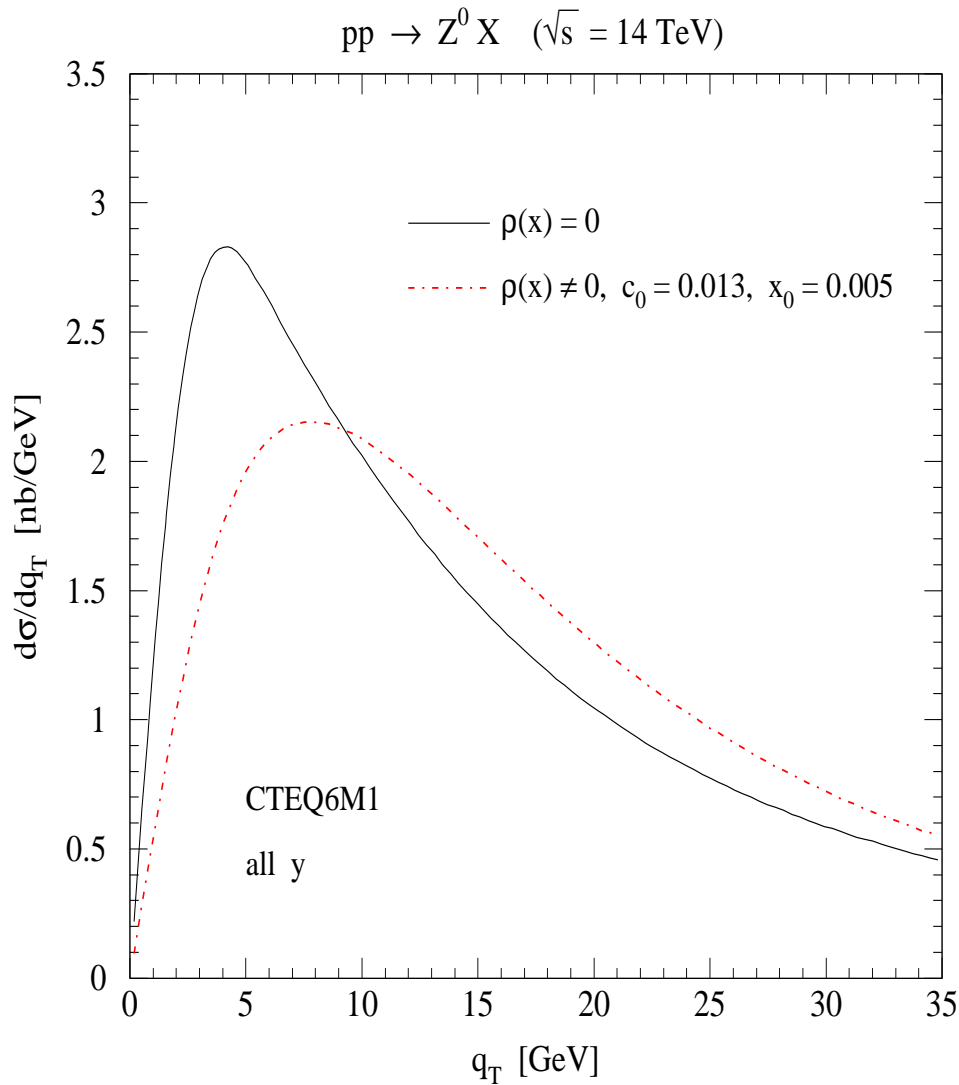
# Apply fitted small- $x$ effects to Tevatron



*Small but measurable effect for forward  $Z^0$  production*

Berge et al '04

# Works at Tevatron? Apply to LHC...



*Big effect for  $Z^0$ ; almost negligible for Higgs*

Berge et al '04

# What about small- $x$ predictions?

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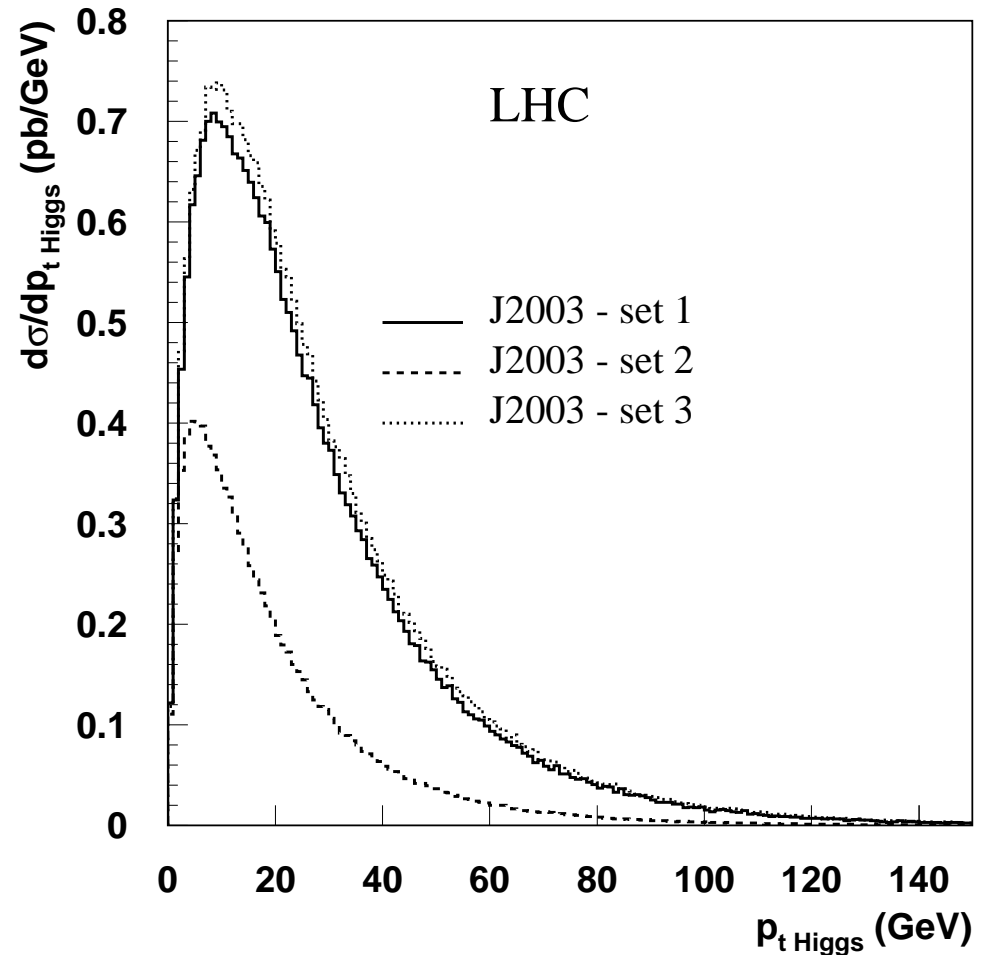
- Recent study using CCFM-based CASCADE

NB: CCFM is like BFKL

- resums leading logs of  $1/x$
  - but with correct Sudakov double logs
  - consistent merging of  $z \rightarrow 0$  and  $z \rightarrow 1$  effects
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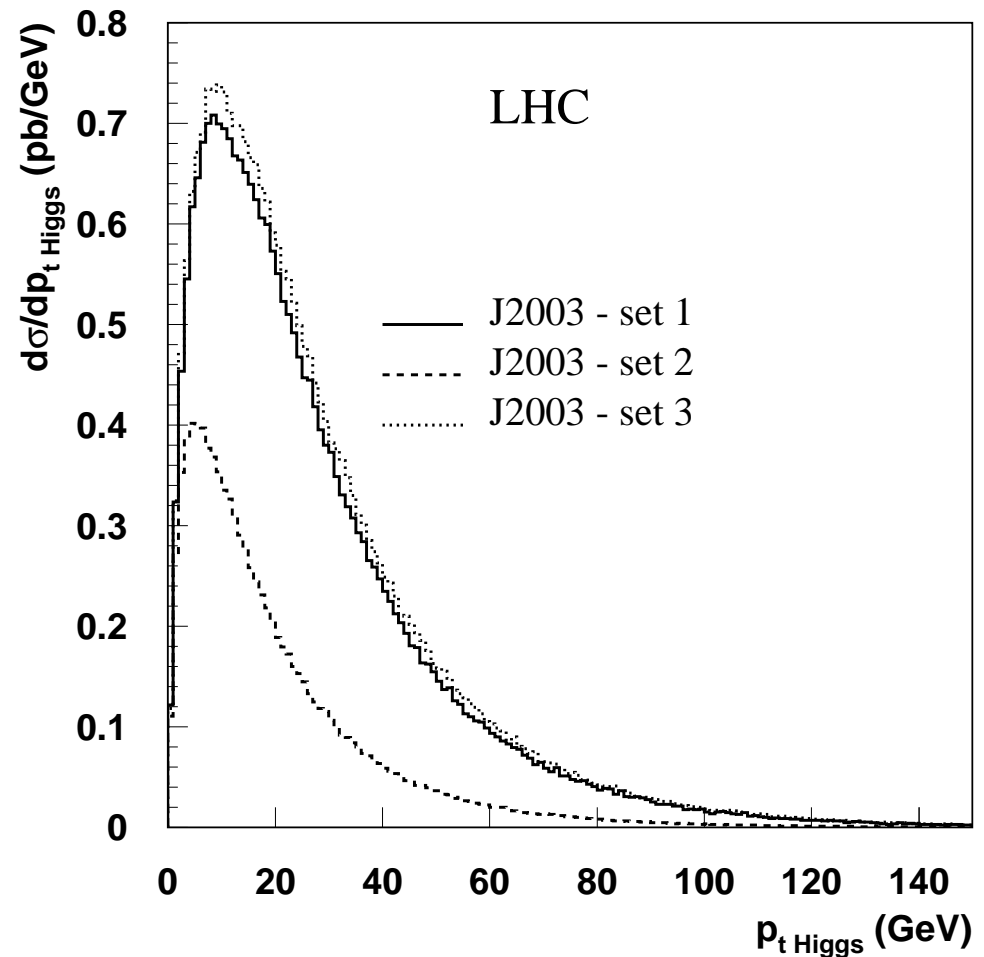
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Jung '03

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  - quark induced processes are trickier, so  $W/Z$  difficult for now...



Jung '03

# Degree of reliability of these predictions?

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*Both have 'issues'...*

## Sudakov resummation

- The corresponding HERA measurement can be contaminated by hadronisation (crossing is not quite exact)
- Parametrization of 'non-perturbative' small- $x$  effects rises very steeply  $\sim 1/x$  — unnatural theoretically?

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- This could matter: Higgs production involves scales up to  $m_t$ .
- tested in limited kinematical domain



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*Ways forward?*

## New HERA measurements?

- distribution of  $\sum_{i \in \text{current}} \vec{p}_{ti}$
- less sensitive to hadronisation
- more complicated perturbatively

## Better theory?

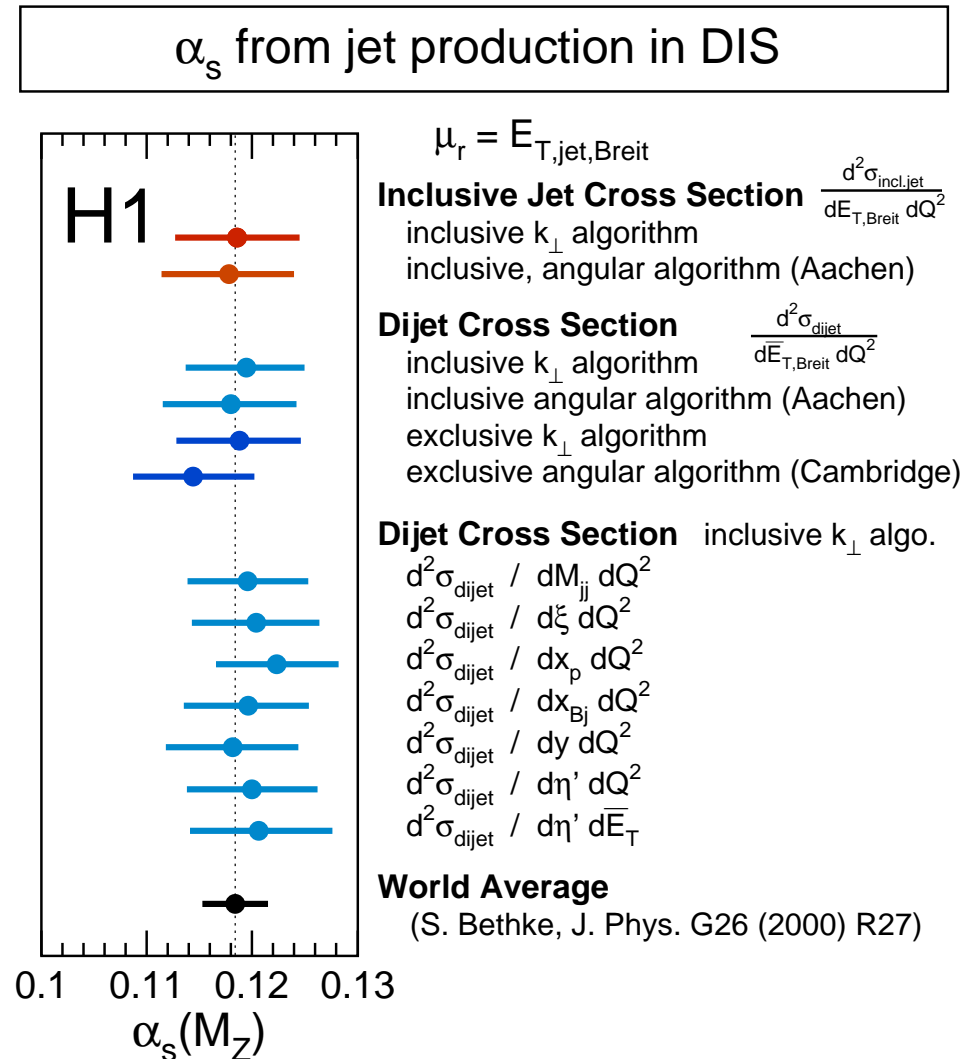
- Put quarks into CCFM (hard!?)
- Learn how to how incorporate small- $x$  resummation analytically in the Sudakov resummation

# Jets at moderate & high(ish) $Q$ , $E_T$

Jets are (next) most basic element of QCD final-state studies

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- Measurements of the coupling
- Measurements of the gluon density
- Tests of multi-jet structure in QCD

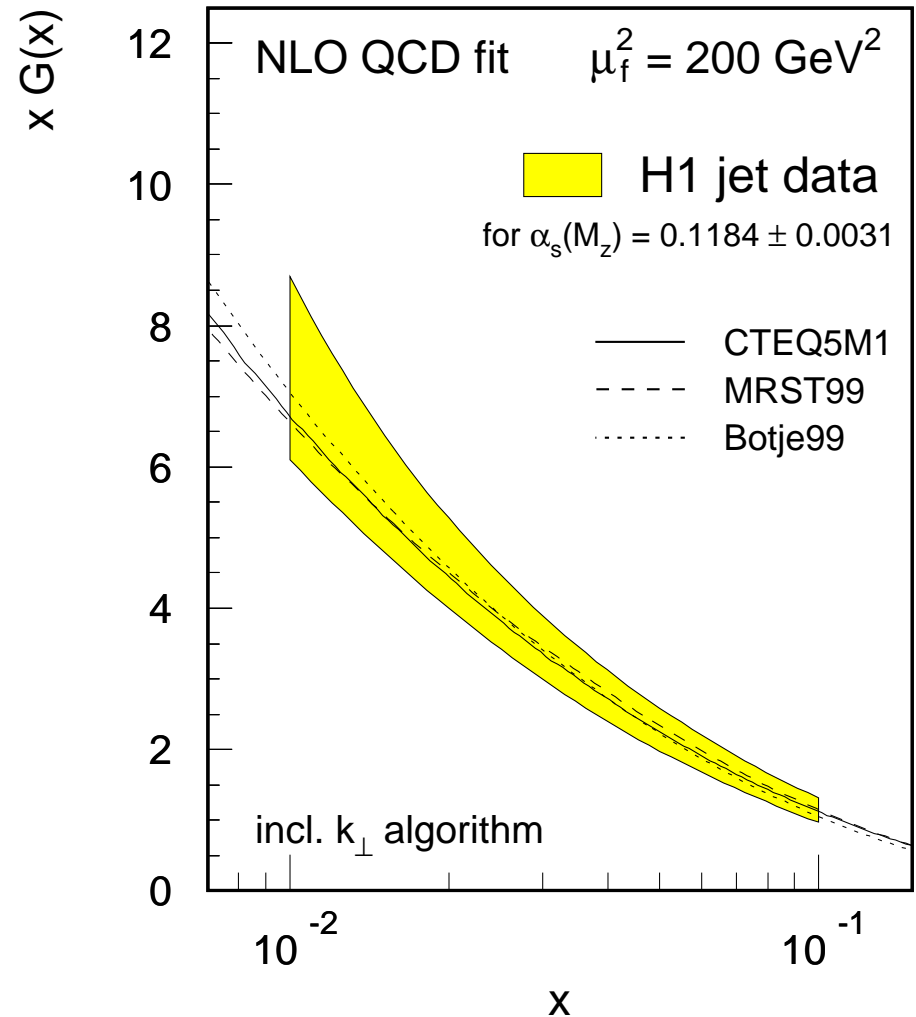


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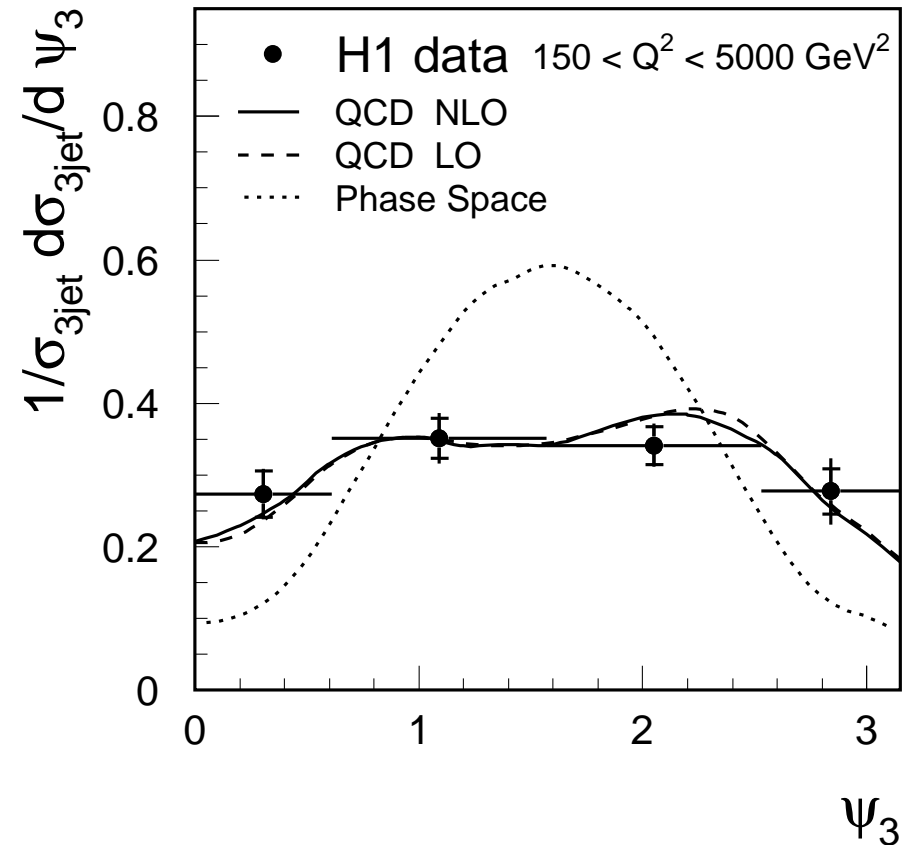


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# Jets at moderate & high(ish) $Q$ , $E_T$

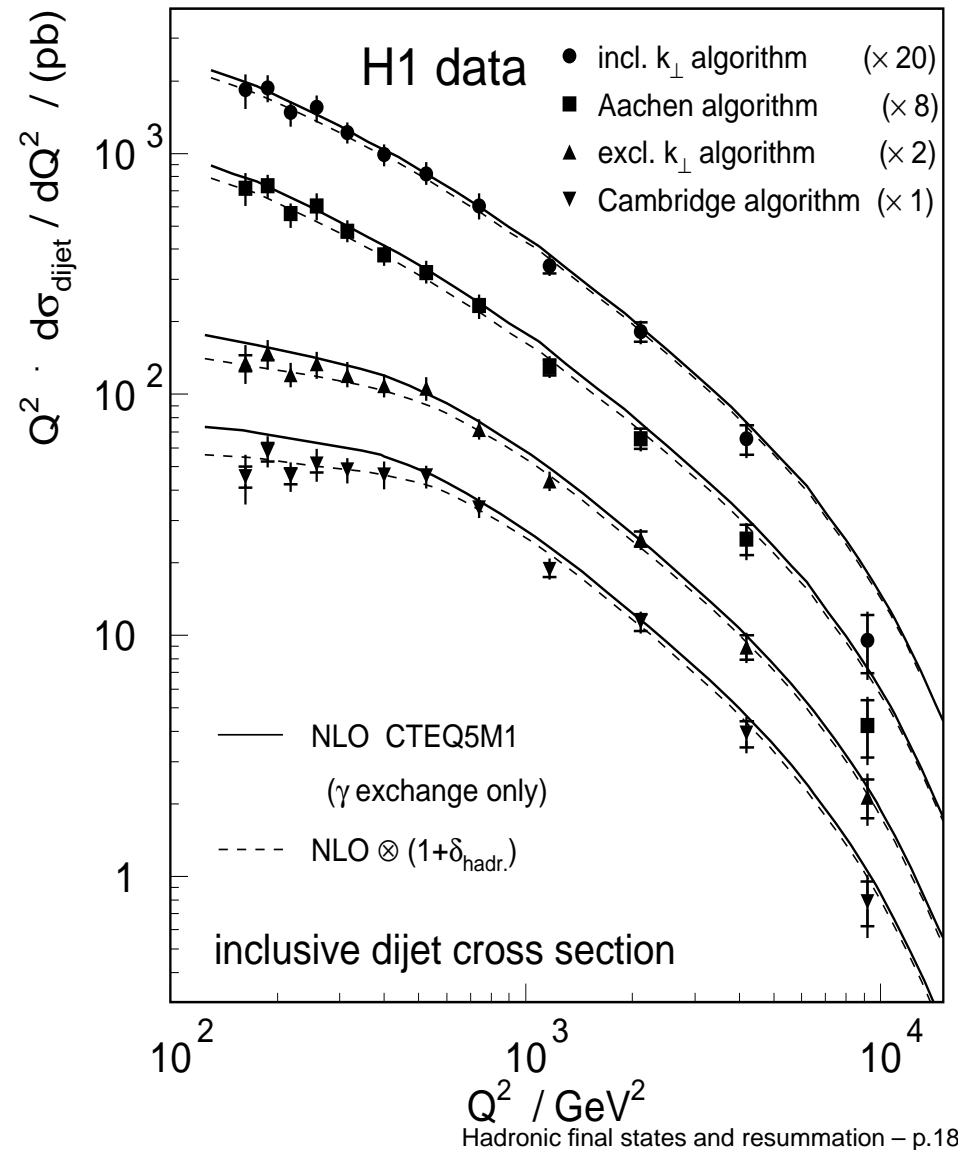
Jets are (next) most basic element of QCD final-state studies

## Amazing array of results from HERA

- Measurements of the coupling
- Measurements of the gluon density
- Tests of multi-jet structure in QCD

## A theorist's litany: the $k_t$ algorithm

- HERA is a convert!
- LHC seems not to be (yet...)
- Algorithm of choice is cone with  $R=0.4(?)$
- Advantage: simple; intuitive. A 'standard' for searches



# Can $k_t$ provide concrete advantages? HERA experience?

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A role of the workshop should be to investigate such questions

Jet algorithms are not just about finding jets of particles

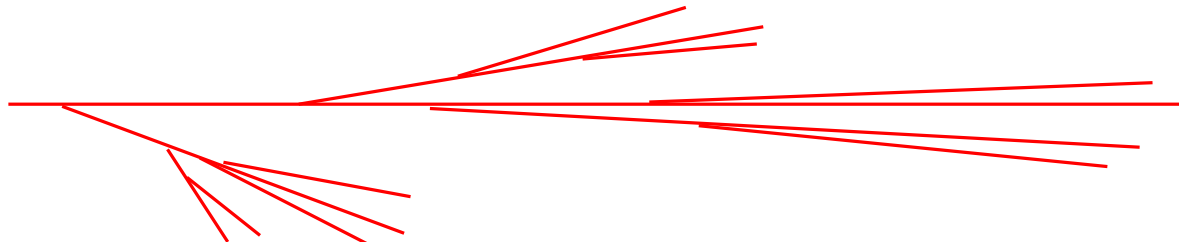
- Connect experimental observations (hadrons) with QCD calculations (partons)
- Connect a shower of particles with intuitive picture of a single hard parton
- Should provide a handle on the ambiguity in making such connections – a meaningful *resolution parameter*
  - This is a strength of the  $k_t$  clustering algorithms
  - Construction of a jet  $\sim$  inverse of QCD showering
  - At finer resolutions, jet is broken into subjects, each of which maintains intuitive connection with a QCD parton

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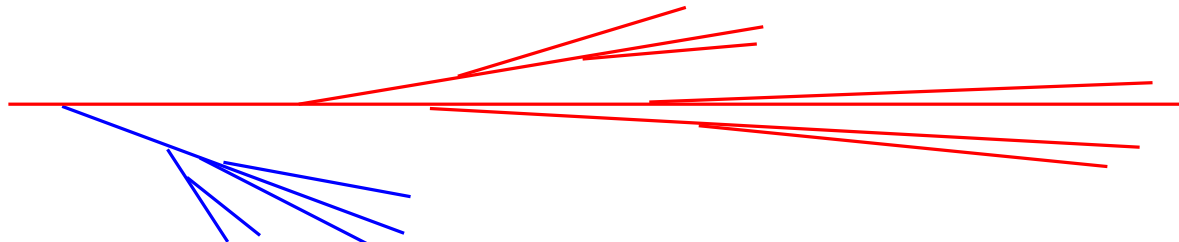


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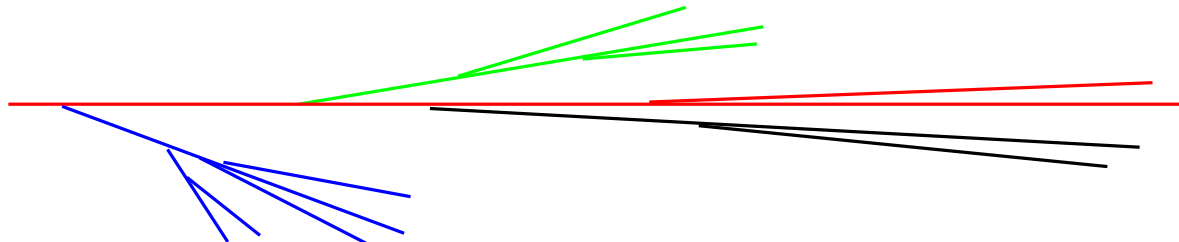


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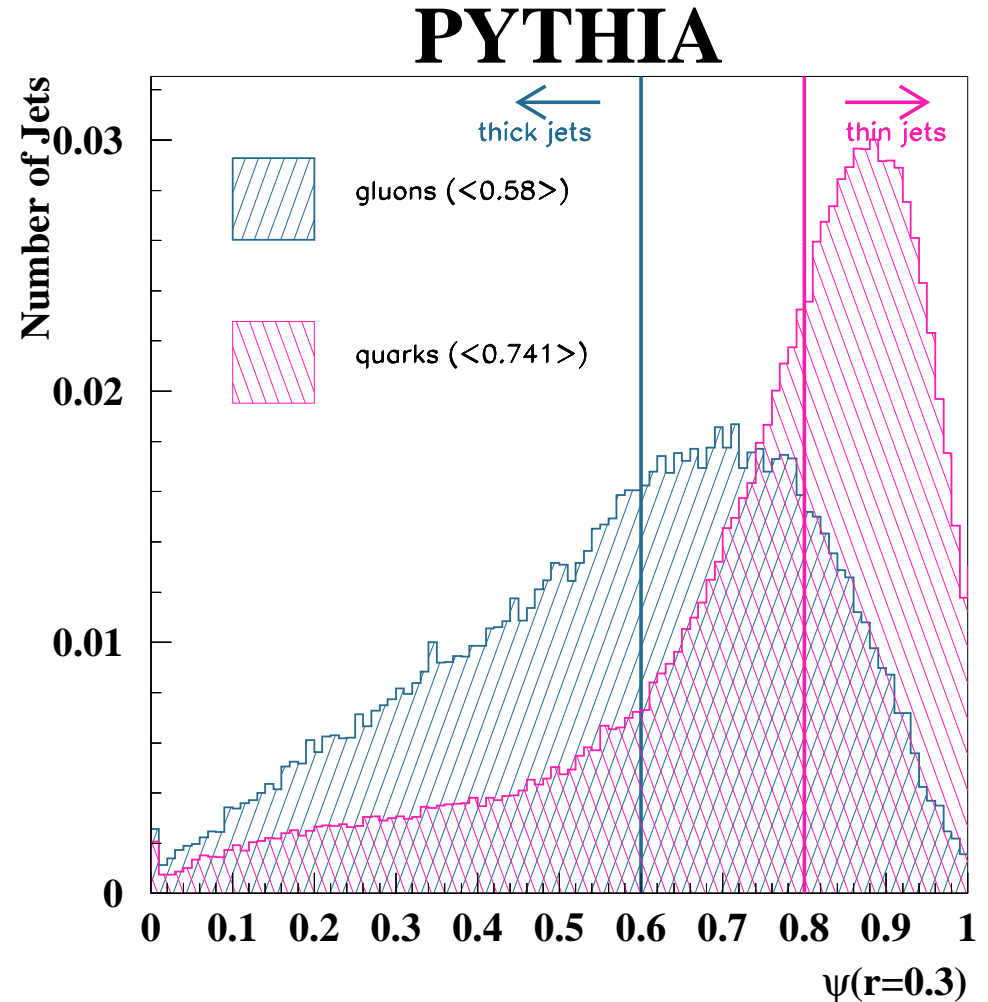
# Distinguishing quark and gluon jets

## ZEUS study of theory predictions

Dokshitzer et al '92, Seymour '94, '96

Forshaw & Seymour '98

● Gluons give wider jets



Distribution of  $\Psi(r) \equiv$  fraction of jet energy inside radius  $r$ .

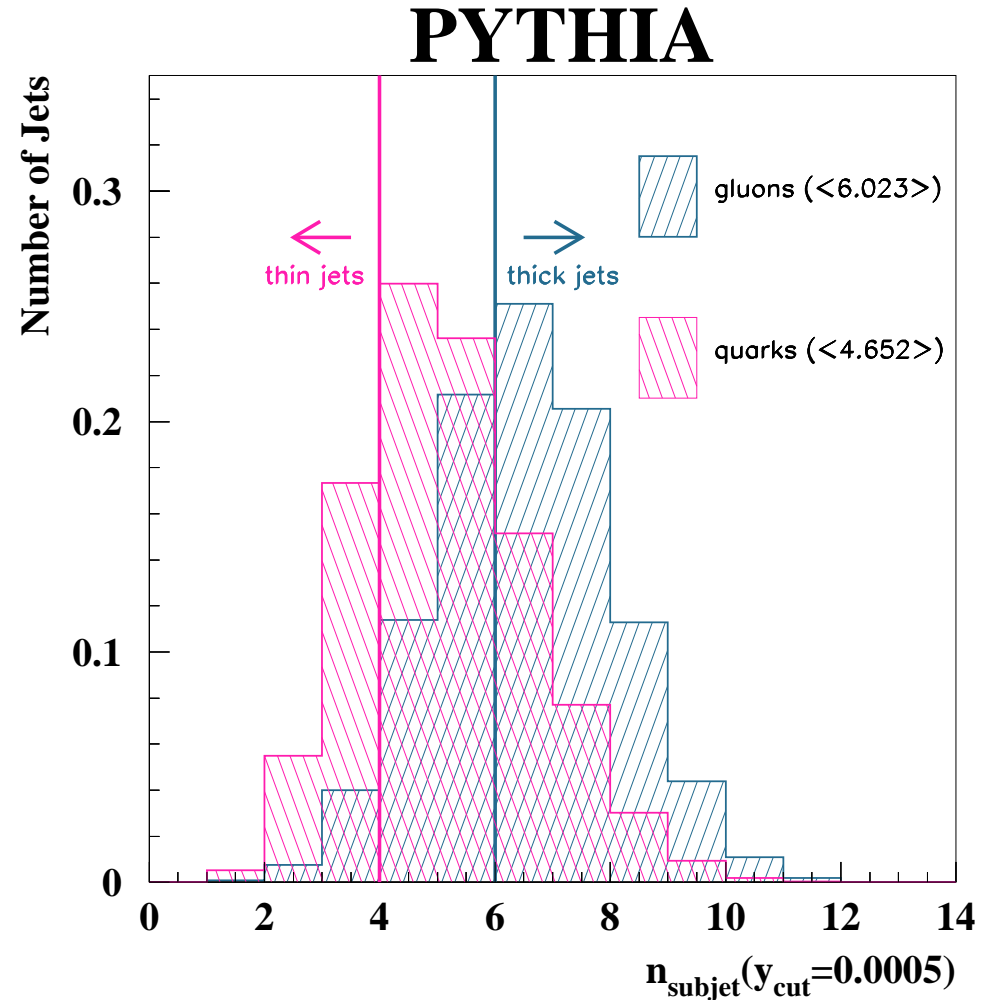
# Distinguishing quark and gluon jets

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- Gluons give wider jets
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Distribution of # of subjects for a small resolution parameter  $y_{\text{cut}}$ .

# Distinguishing quark and gluon jets

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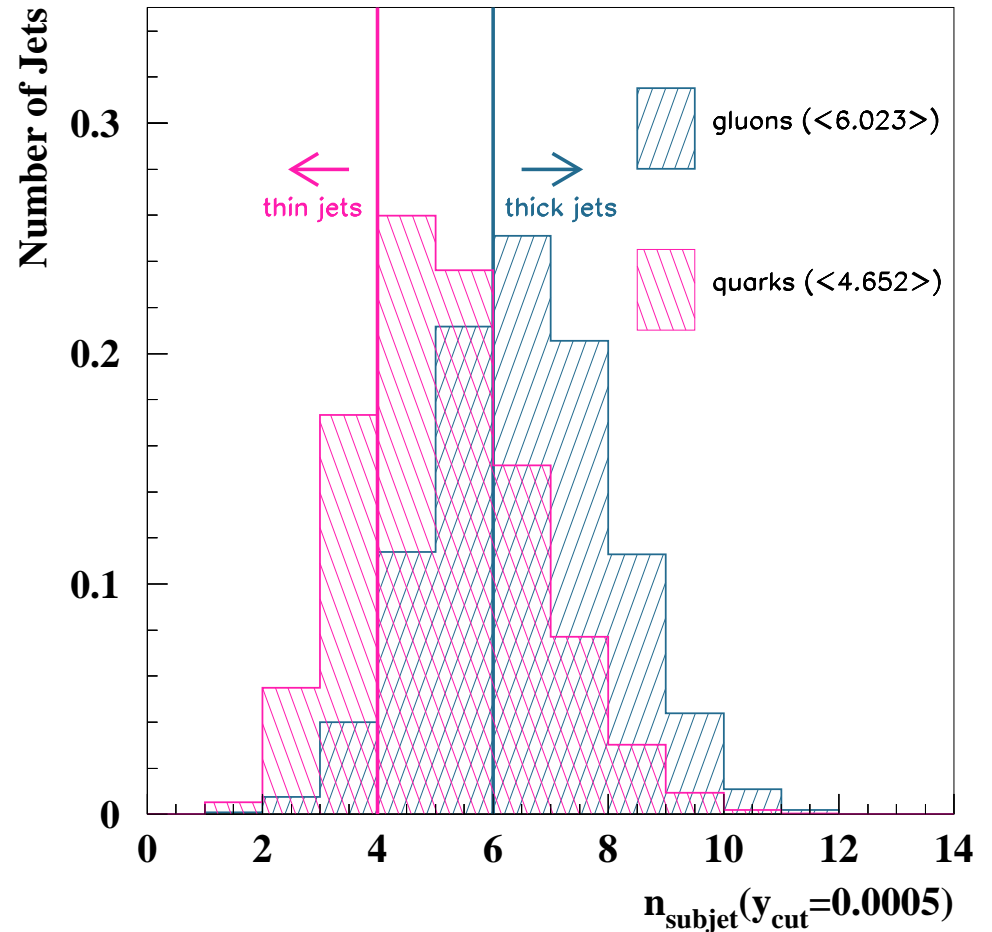
Forshaw & Seymour '98

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## Select gluon and quark jets

- Combine criteria to identify thin (quark) jets and thick (gluon) jets
- 98% (61%) purity for quarks (gluons)
- 15% (?) efficiency

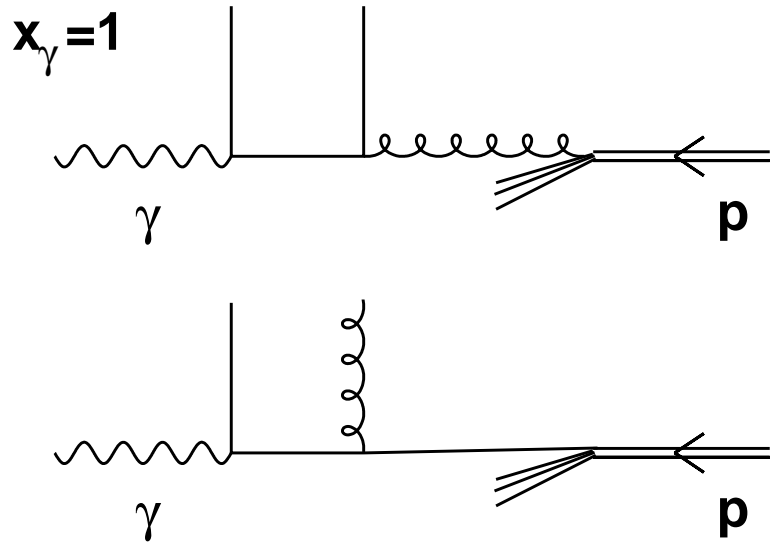
## PYTHIA



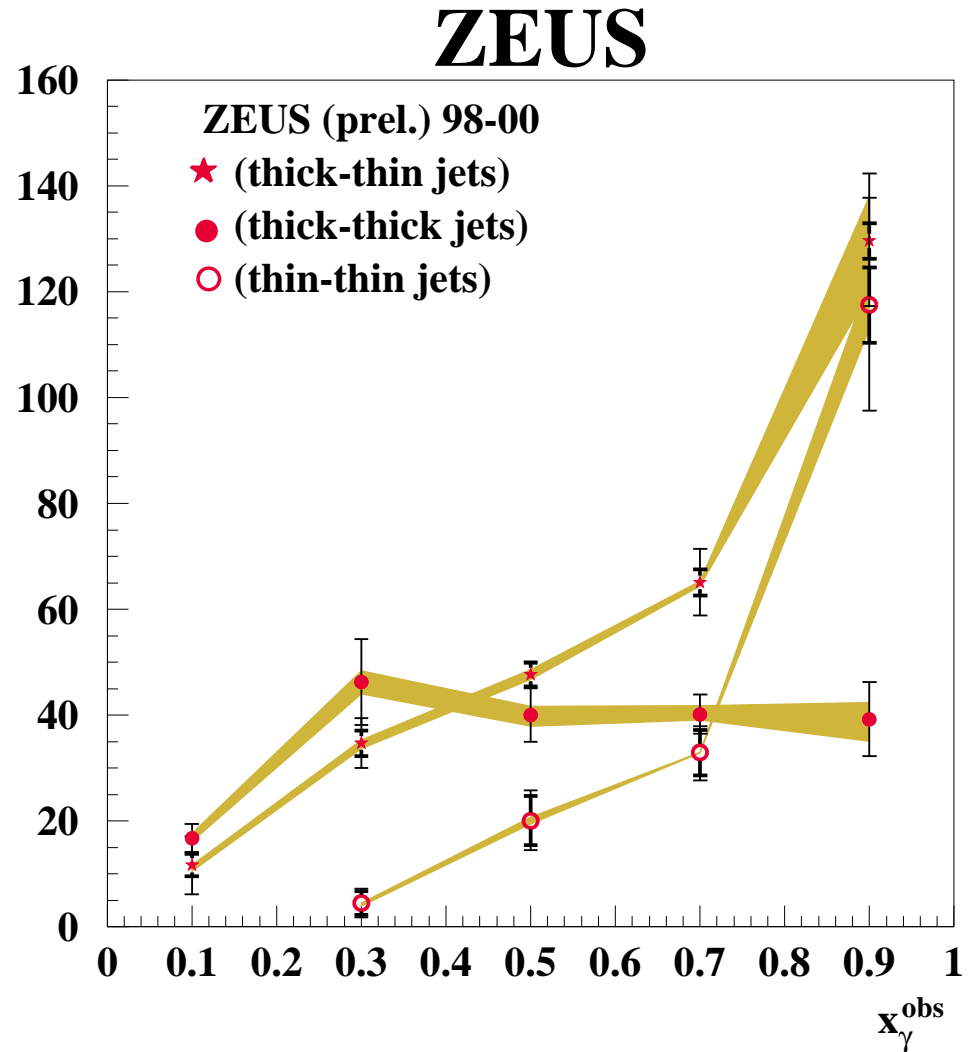
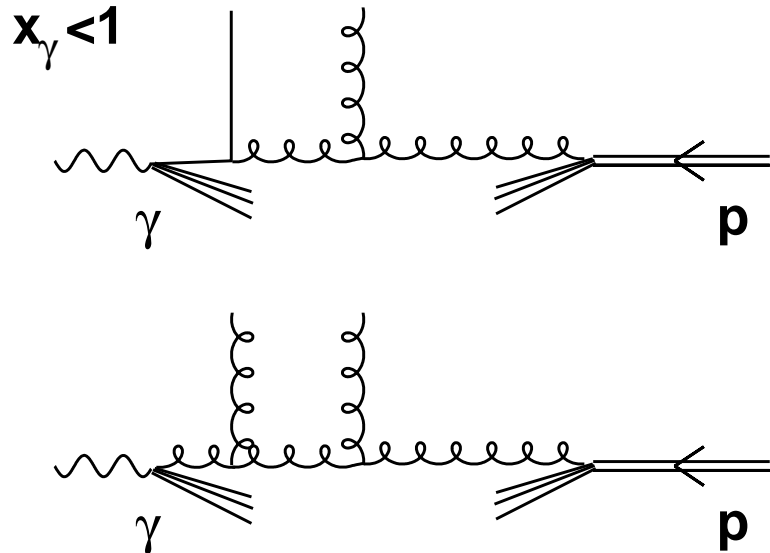
Distribution of # of subjects for a small resolution parameter  $y_{\text{cut}}$ .

# Distinguishing quark and gluon jets: application

D I R E C T

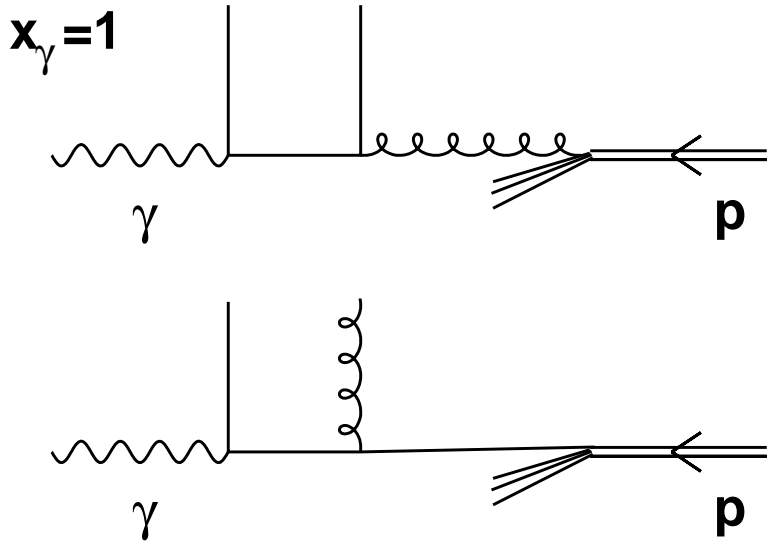


R E S O L V E D

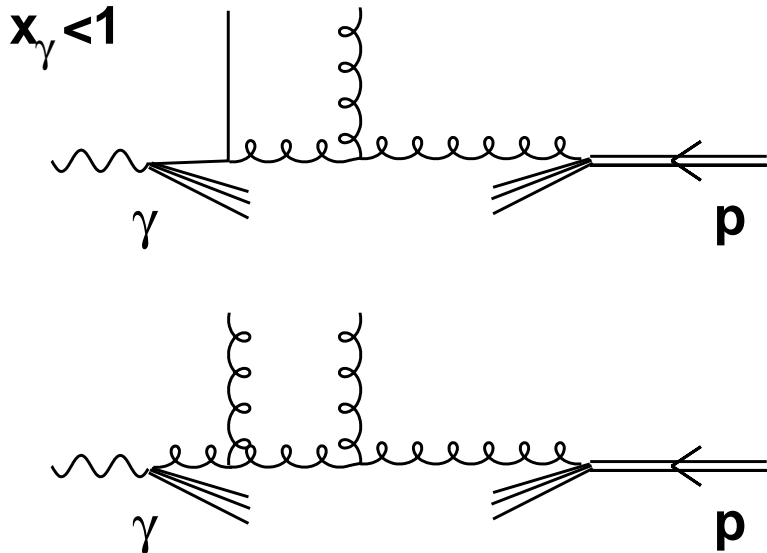


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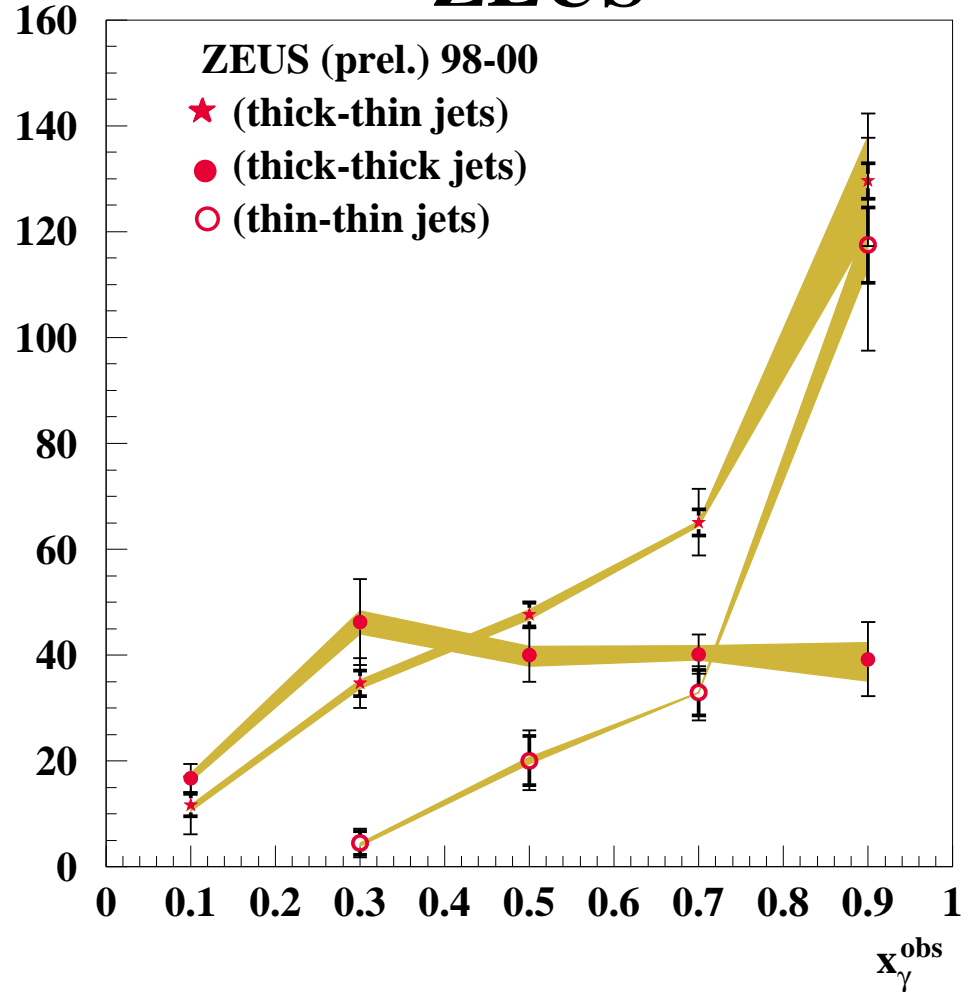
D I R E C T



R E S O L V E D



## ZEUS



Can selection/efficiency be improved?  
How might this be applied at LHC?

## Hard QCD

- Further (mis)uses of jet algorithms;
- Event shapes — in  $e^+e^-$  & DIS, a laboratory for QCD across a range of scales — how about at LHC?
- Diffraction!
- Rapidity gaps: ‘Sudakov’ QCD rapidity gaps v. true rapidity gaps. Perturbative gap survival. Non-perturbative gap survival.

## Moderately hard QCD

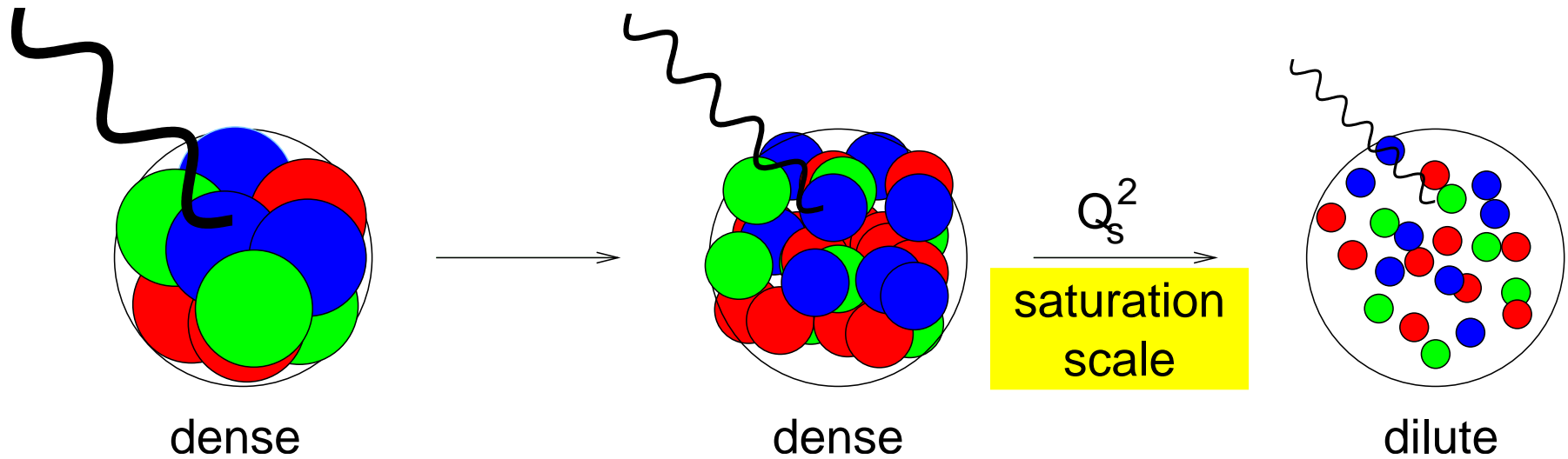
- BFKL for its own sake!

## Softer QCD

- Underlying events, similarities between  $\gamma p$  and  $pp$ ?
- Minimum bias; ways of measuring it; models; connection with saturation;



# Extra time: Saturation scales



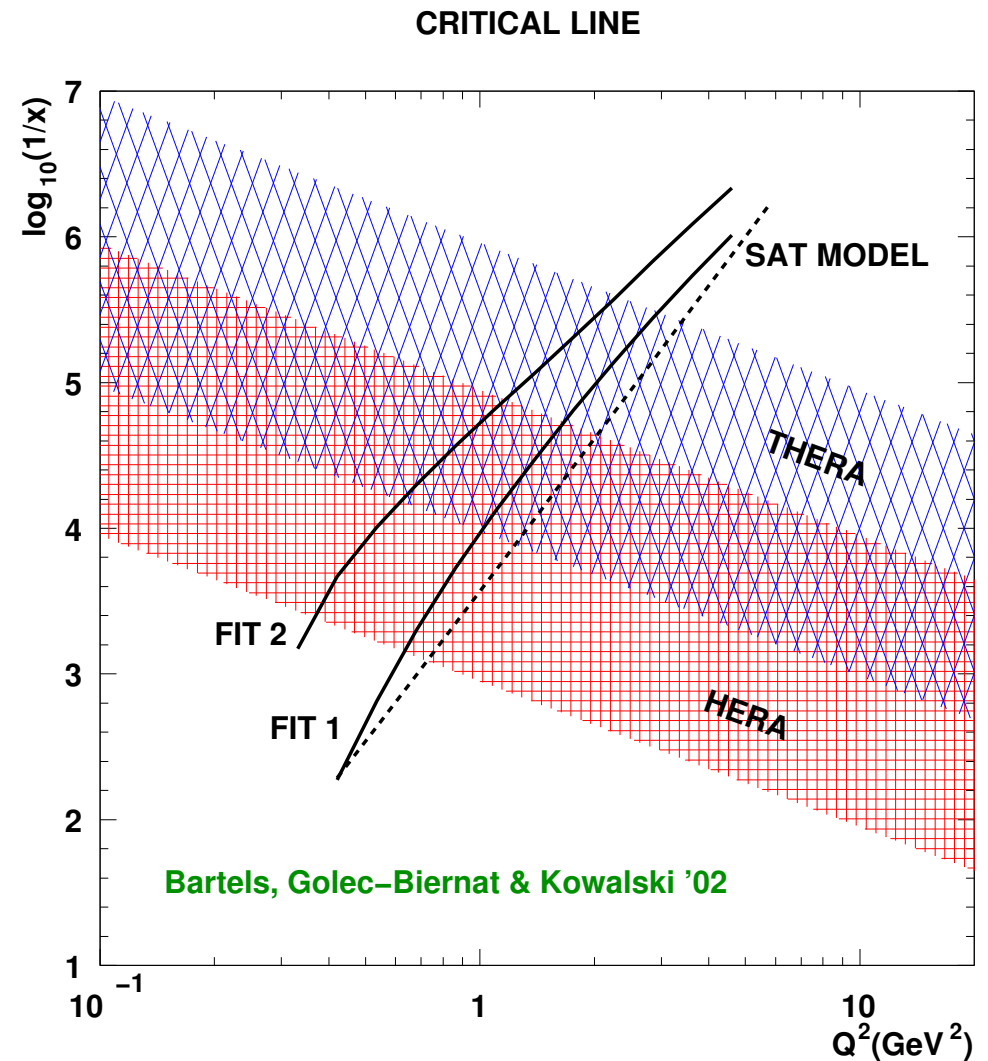
Below saturation scale: *dense system of gluons* ( $\rho \sim 1/\alpha_s$ )

Above saturation scale: *dilute system of gluons* ( $\rho \ll 1/\alpha_s$ )

## Big business at HERA

- Models including saturation are fitted to HERA data
- Saturation sets in (perhaps?) just at limit of perturbative region
- Rises with decreasing  $x$

*What's the connection with final states?*



# Saturation scales (cont.)

## Back of the envelope: Tevatron? LHC?

- Typical transverse momentum in minimum bias is  $Q_s^2$
- Convert from DIS using  $x \sim \frac{Q_s^2(x)}{s}$
- LHC minimum bias  $k_T \simeq 2 \times$  Tevatron minimum bias?
- Very rough? *But beware: transverse momentum/collision could rise much faster than the cross section*

