

# Jet algorithms

Gavin P. Salam

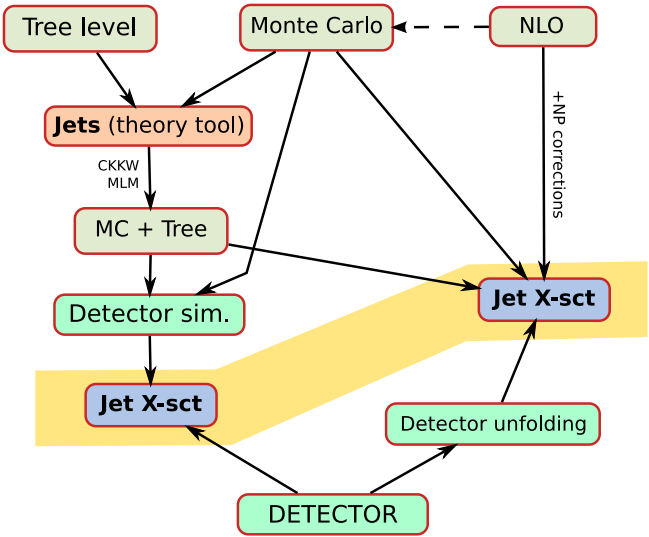
LPTHE, UPMC Paris 6 & CNRS

CMS JetMet meeting

CERN, Geneva

27 March 2008

*Based on work with M. Cacciari (LPTHE) & G. Soyez (BNL)*

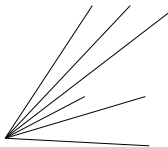


**Jet (definitions) provide central link between expt., "theory" and theory**

- ▶ Jet algorithms and infrared & collinear safety
- ▶ Pileup subtraction

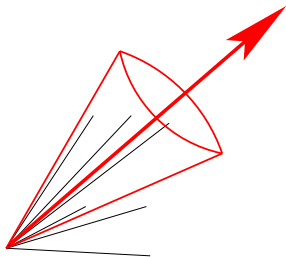
Many cone algs have two main steps:

- ▶ Find some/all stable cones
  - ≡ cone pointing in same direction as the momentum of its contents
- ▶ Resolve cases of overlapping stable cones
  - By running a 'split-merge' procedure [Blazey et al. '00 (Run II jet physics)]



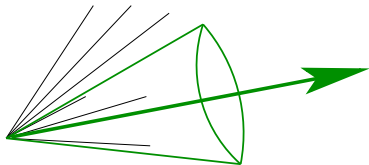
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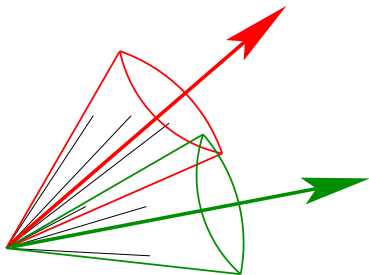
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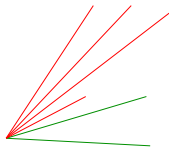
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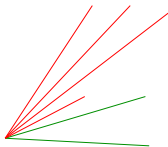
**Qu: How do you find the stable cones?**

Until recently used iterative methods:

- ▶ use each particle as a starting direction for cone; use sum of contents as new starting direction; repeat.

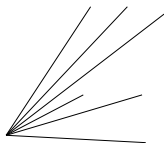
**Iterative Cone with Split Merge (IC-SM)**

e.g. Tevatron cones (JetClu, midpoint)  
ATLAS cone



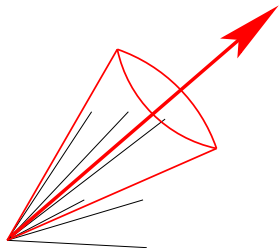
Other cones avoid split-merge:

- ▶ Find one stable cone E.g. by iterating from hardest seed particle
- ▶ Call it a jet; remove its particles from the event; repeat



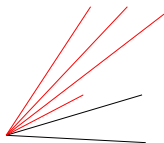
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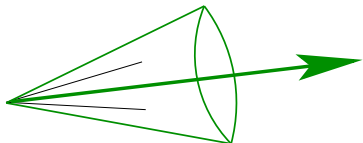
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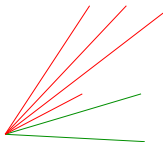
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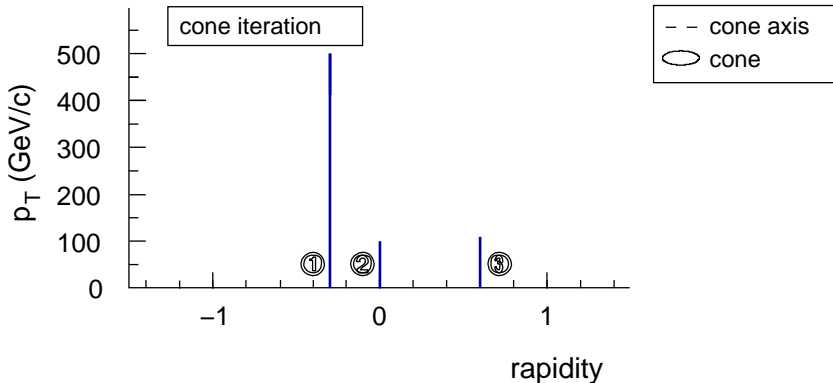
- ▶ This is not the same algorithm
- ▶ Many physics aspects differ

## **Iterative Cone with Progressive Removal (IC-PR)**

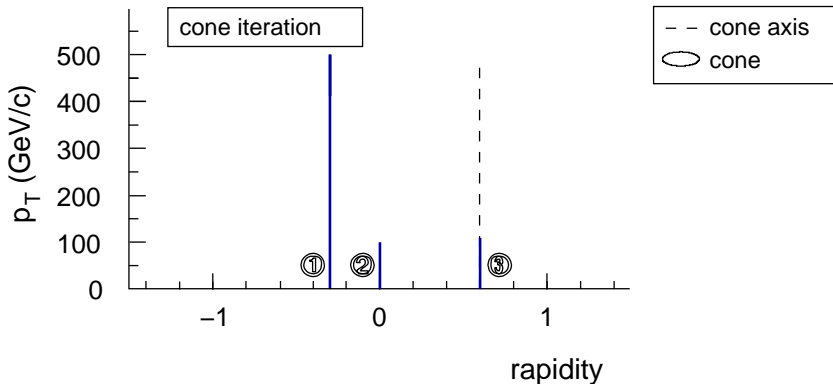
e.g. CMS it. cone, [Pythia Cone, GetJet], ...



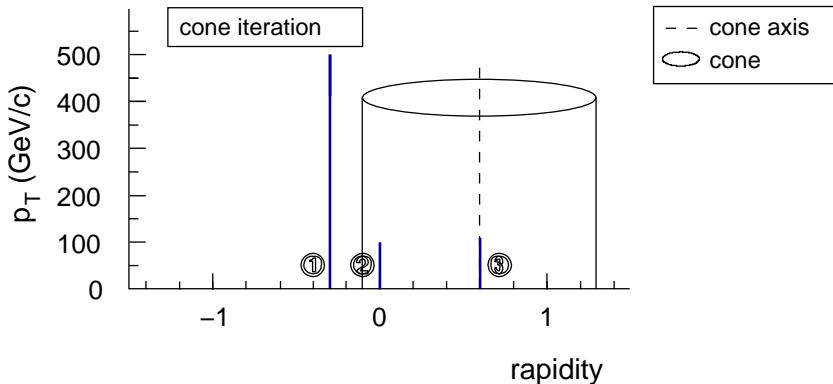




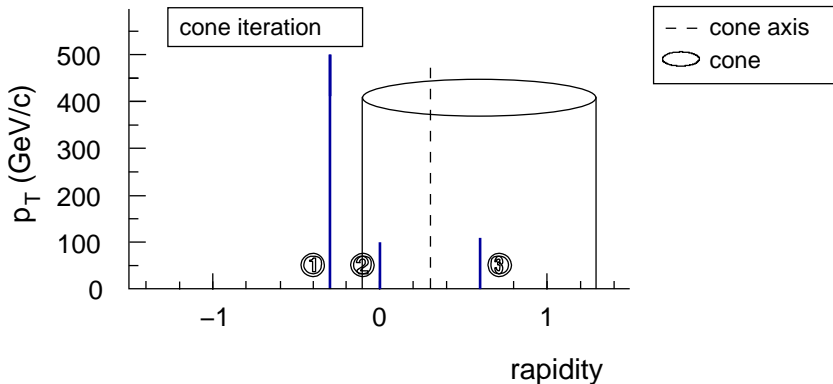
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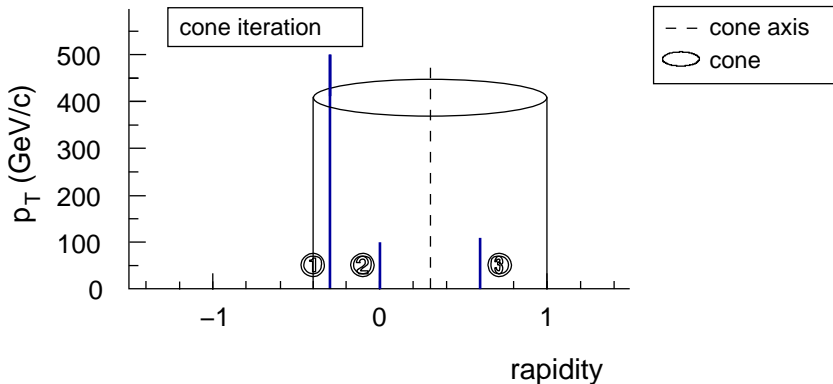
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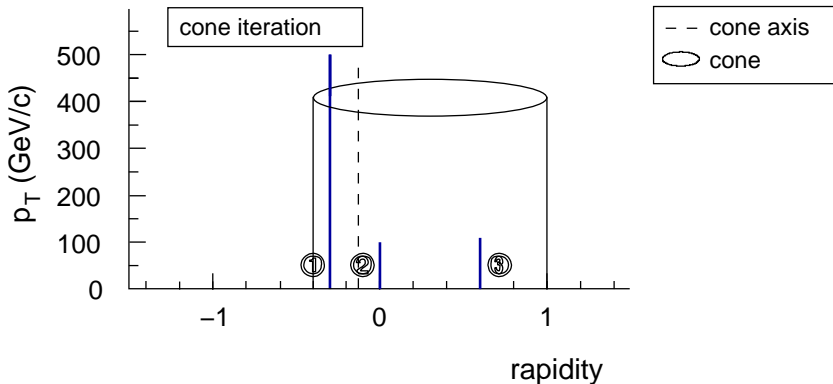
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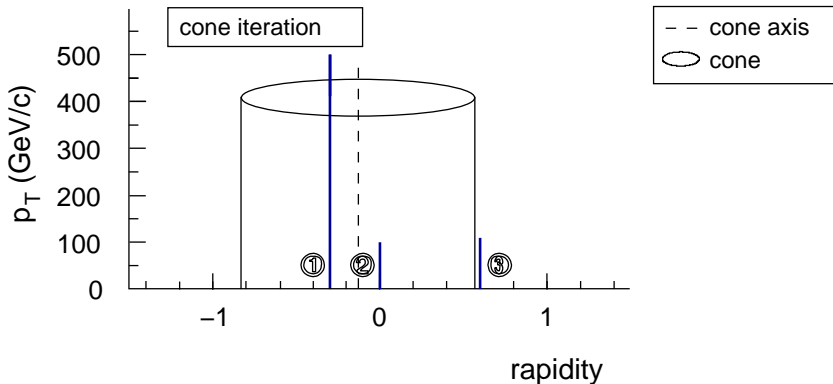
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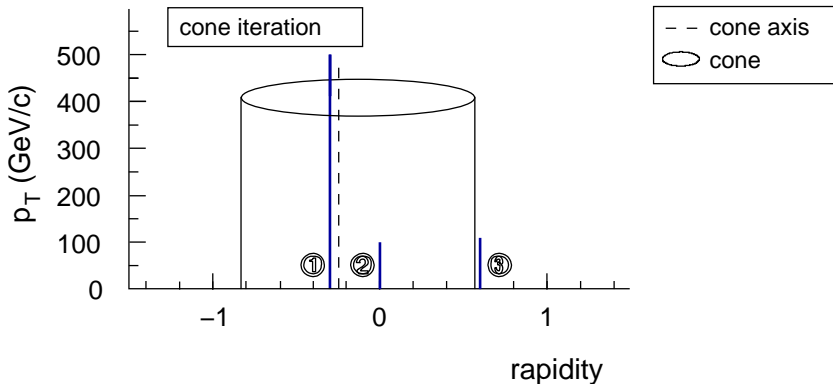
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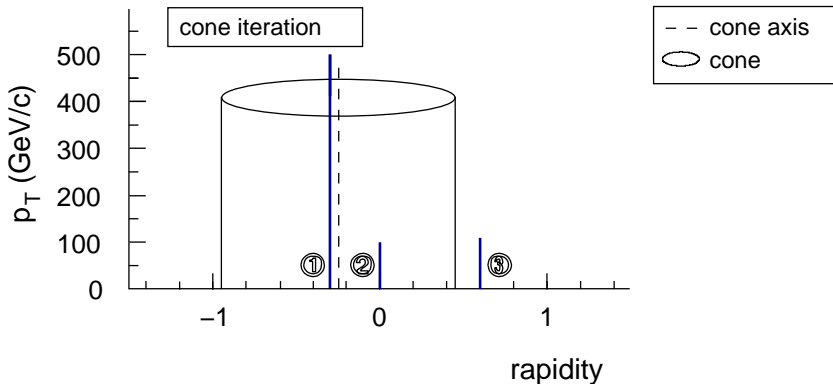


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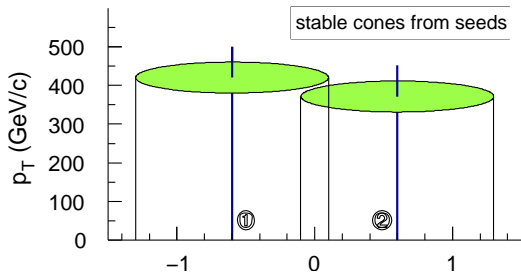
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Extra soft particle adds new seed  $\rightarrow$  changes final jet configuration.

This is **IR unsafe**.

Kilgore & Giele '97

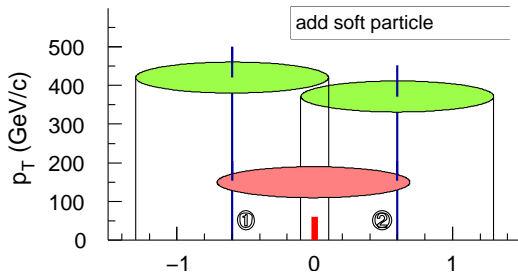
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Adopted for Tevatron Run II

But only **postpones** the problem by one order ...

Analogy: if you rely on Minuit to find minima of a function, in complex cases, results depend crucially on starting points

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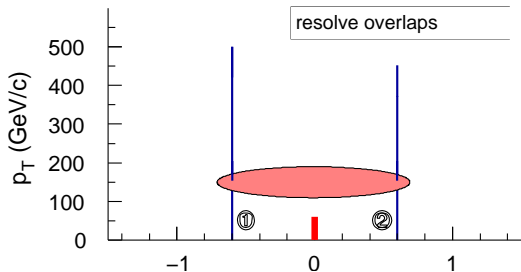
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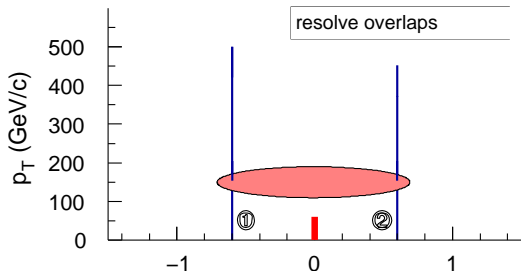
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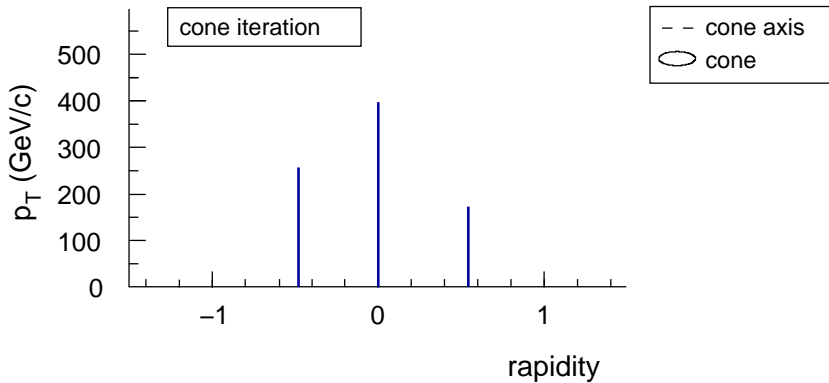
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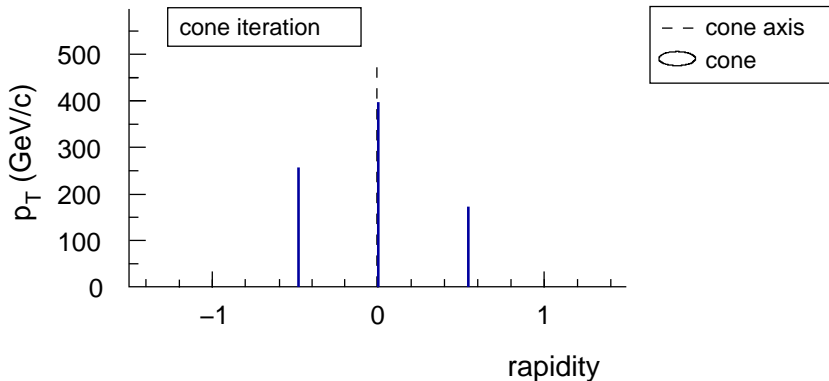
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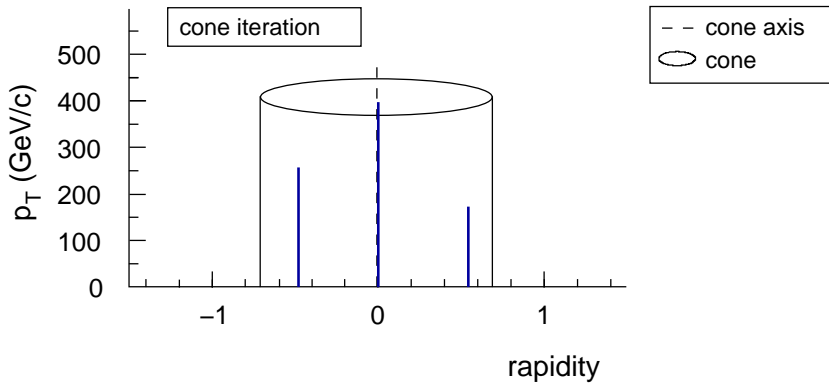
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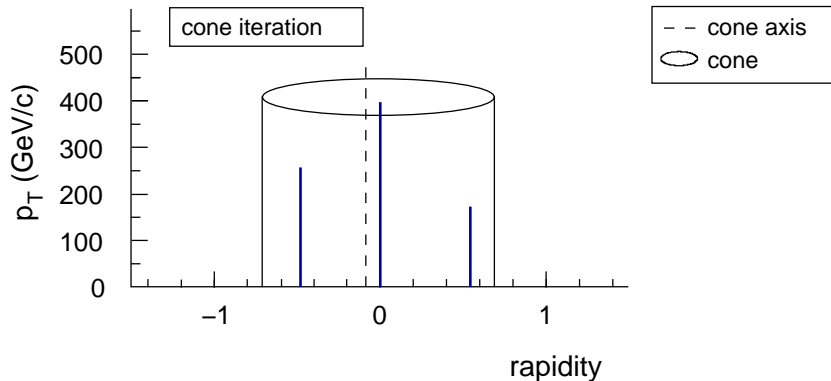


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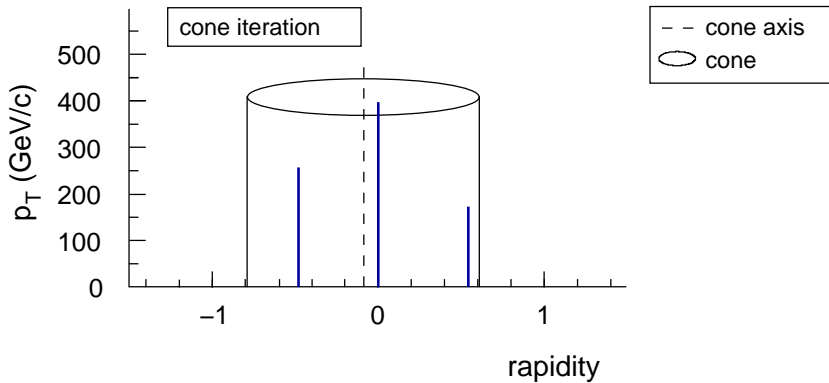


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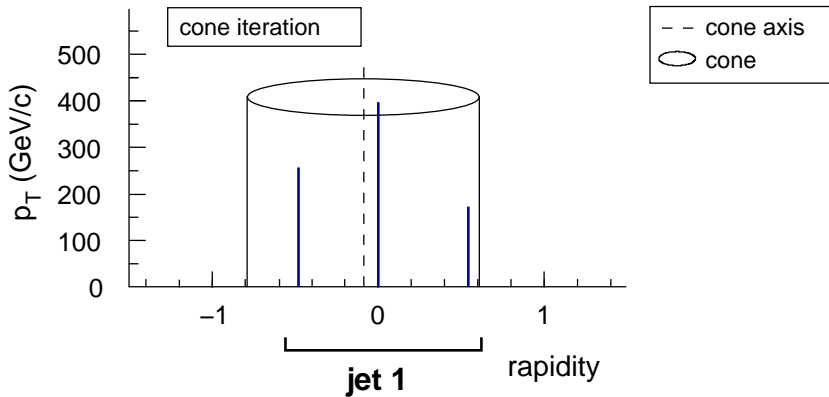




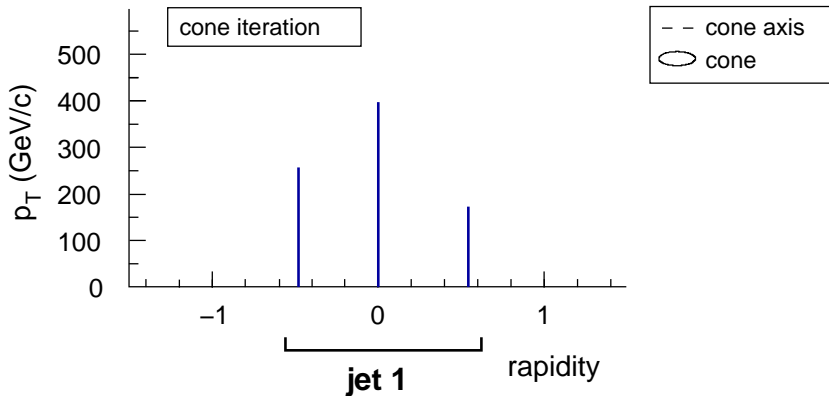
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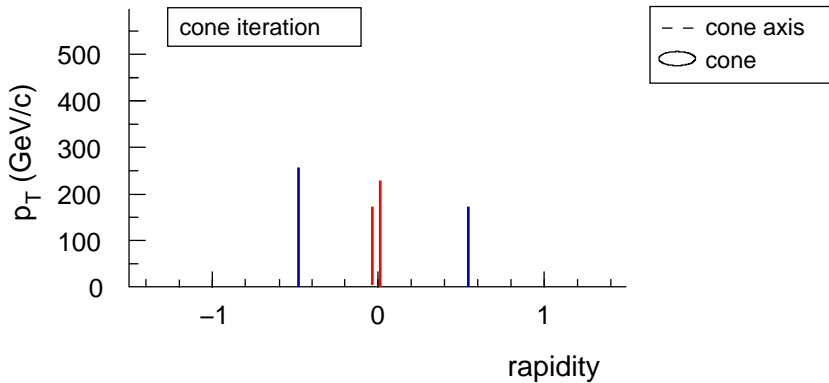
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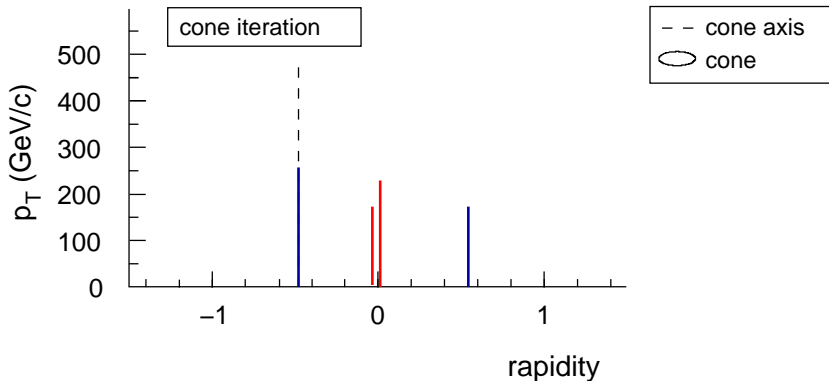
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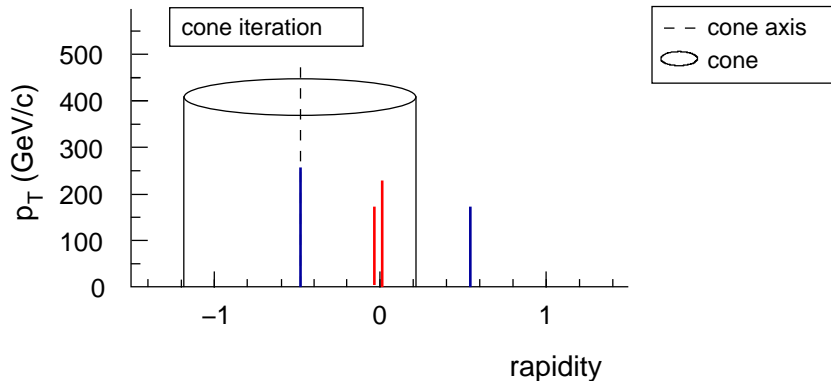
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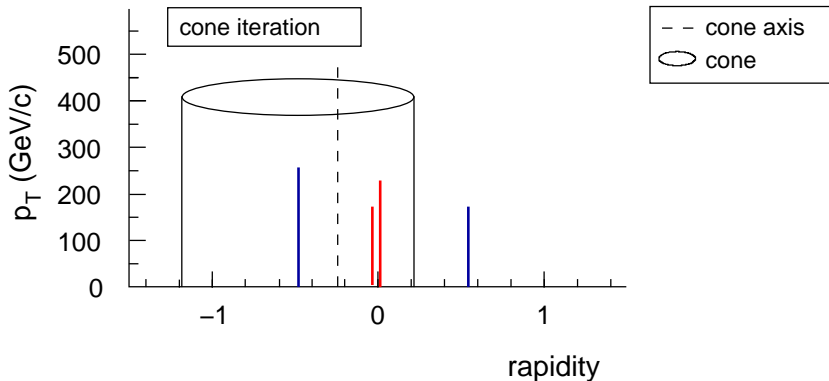
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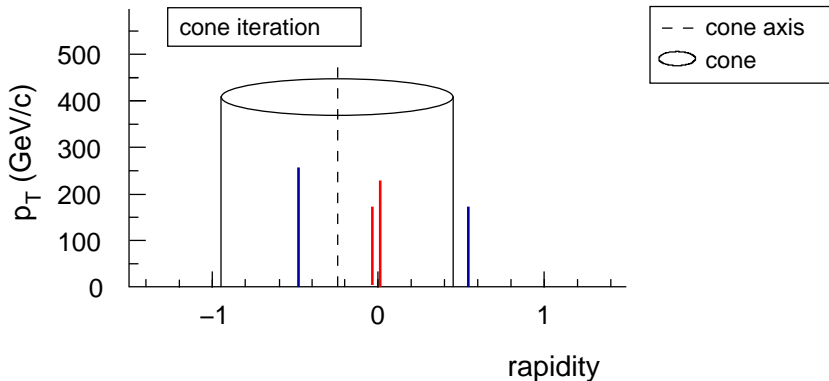


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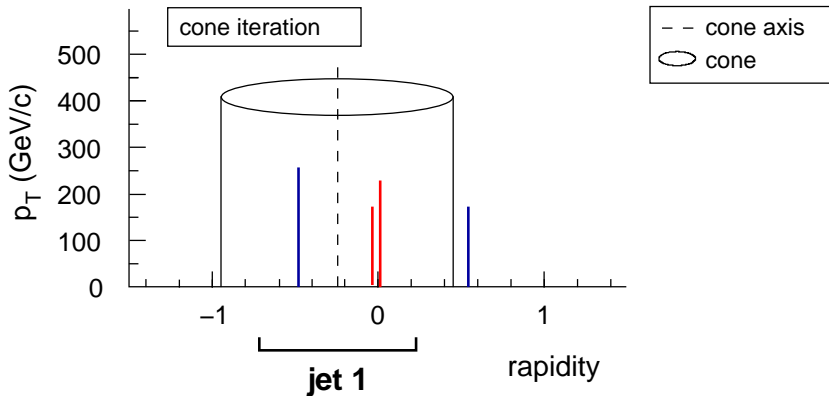


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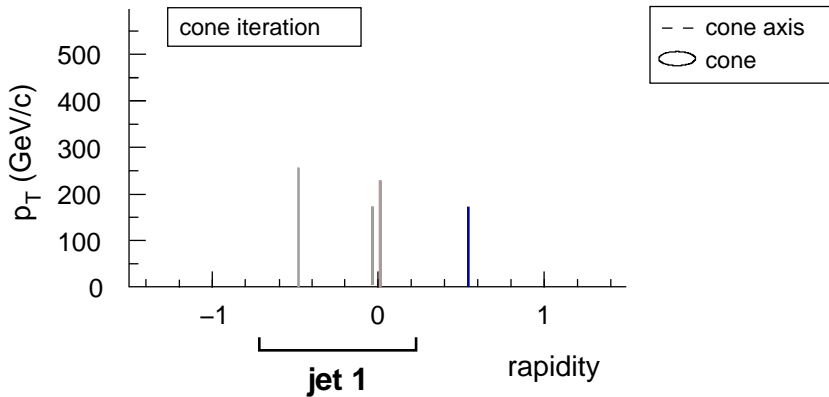




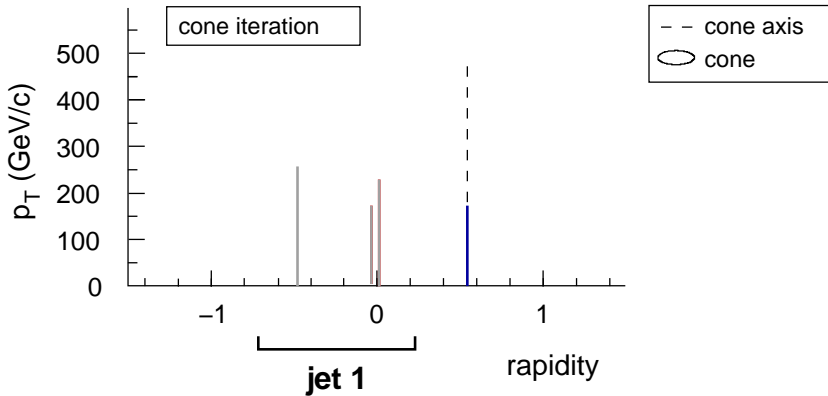
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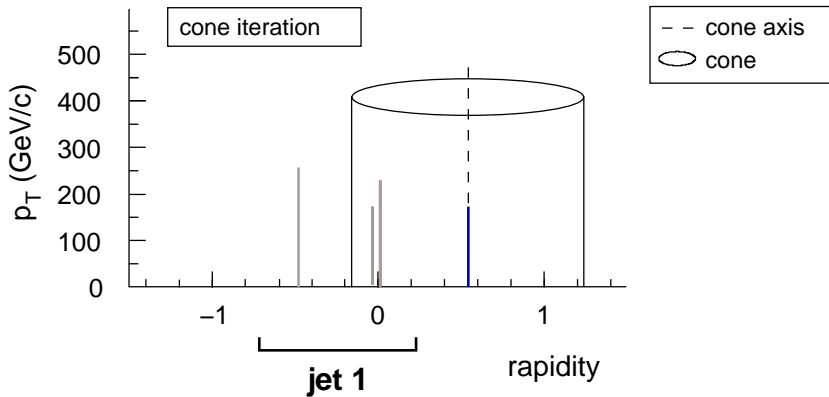
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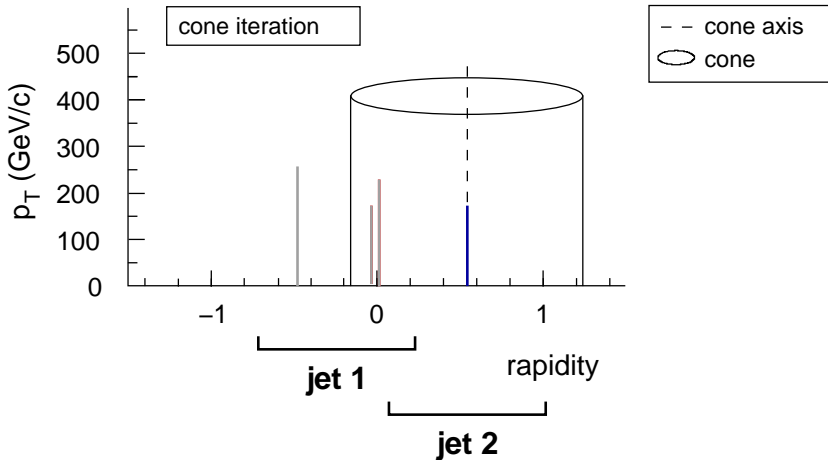
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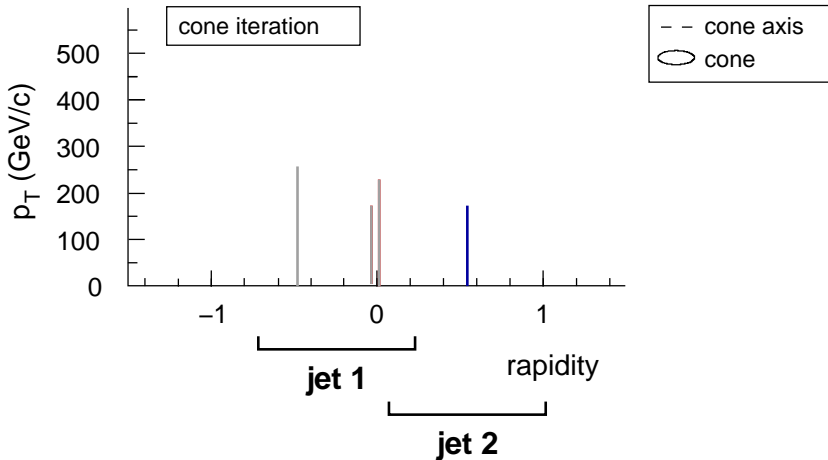
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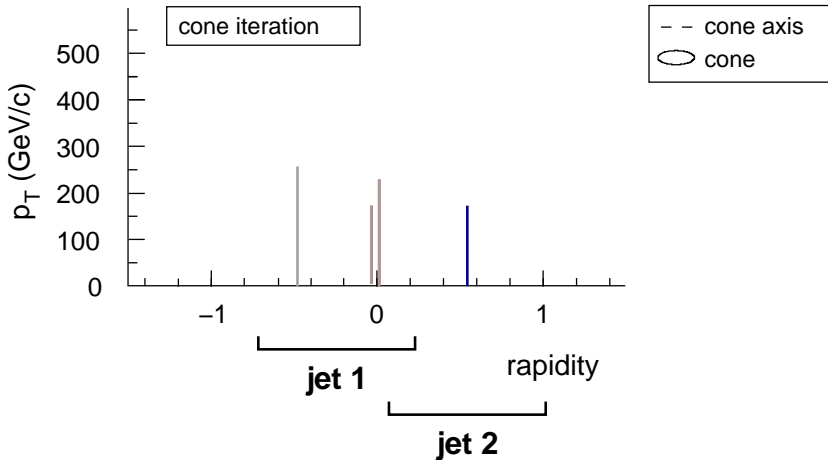
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Snowmass Accord (1990):

FERMILAB-Conf-90/249-E  
[E-741/CDF]

## Toward a Standardization of Jet Definitions ·

Several important properties that should be met by a jet definition are [3]:

1. Simple to implement in an experimental analysis;
2. Simple to implement in the theoretical calculation;
3. Defined at any order of perturbation theory;
4. Yields finite cross section at any order of perturbation theory;
5. Yields a cross section that is relatively insensitive to hadronization.

Property 4  $\equiv$  Infrared and Collinear (IRC) Safety. It helps ensure:

- ▶ Non-perturbative effects are suppressed by powers of  $\Lambda_{QCD}/p_t$
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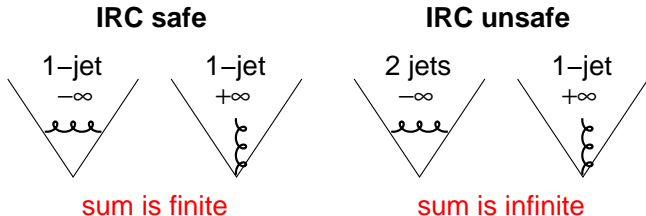
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Soft emission, collinear splitting are both **infinite** in pert. QCD.

Infinites **cancel** with loop diagrams if jet-alg IRC safe



Some calculations simply become **meaningless**

Real life does not have infinities, but pert. infinity **leaves a real-life trace**

Among consequences of IR unsafety:

	<i>Last meaningful order</i>			Known at
	ATLAS cone [IC-SM]	MidPoint [IC <sub>mp</sub> -SM]	CMS it. cone [IC-PR]	
Inclusive jets	LO	NLO	NLO	NLO (→ NNLO)
W/Z + 1 jet	LO	NLO	NLO	NLO
3 jets	<b>none</b>	LO	LO	NLO [nlojet++]
W/Z + 2 jets	<b>none</b>	LO	LO	NLO [MCFM]
$m_{\text{jet}}$ in $2j + X$	<b>none</b>	<b>none</b>	<b>none</b>	LO

NB: \$30 – 50M investment in NLO

Note: simple environments (e.g. dijets) suffer less (“a jet is a jet”).

Multi-jet contexts much more sensitive: **ubiquitous at LHC**

And you’ll rely on QCD for background double-checks  
 extraction of cross sections, extraction of parameters

1. Detectors play tricks with soft particles
  - calorimeter thresholds
  - magnetic fields acting on charged particles
  - calorimeter noise
2. Detectors split/merge collinear particles
  - Two particles into single calo-tower
  - One particles showers into two calo-towers
3. High lumi adds lots of extra soft seeds

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- ▶ IRC safety is non-negotiable
  - ▶ It's part of why jets were defined originally Sternan-Weinberg '77
  - ▶ It's essential for theory calculations to make sense
  - ▶ This is a consensus view — or at least, has been affirmed by every major “jet-workshop” since 1991. Snowmass '91, Run II '00  
Tev4LHC '06, Les Houches '07
- ▶ **But:** some IRC unsafe algorithms might have other “nice” properties
  - ▶ especially low UE sensitivity
  - ▶ circularity of jets

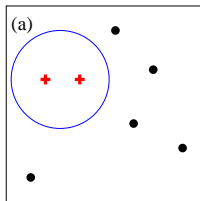
**So let's keep those nice properties, but engineer away the IRC unsafety.**

May require non-obvious approaches

Cones are just *circles* in the  $y - \phi$  plane. To find all stable cones:

1. Find all distinct ways of enclosing a subset of particles in a  $y - \phi$  circle
2. Check, for each enclosure, if it corresponds to a stable cone

Finding all distinct circular enclosures of a set of points is **geometry**:



*Any enclosure can be moved until a pair of points lies on its edge.*

Result: Seedless Infrared Safe Cone algorithm (SIS Cone)

Runs in  $N^2 \ln N$  time ( $\simeq$  midpoint's  $N^3$ )

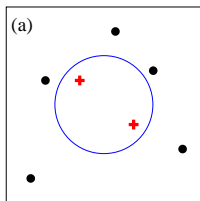
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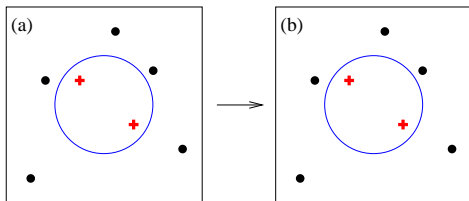
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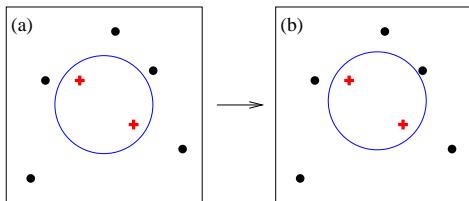
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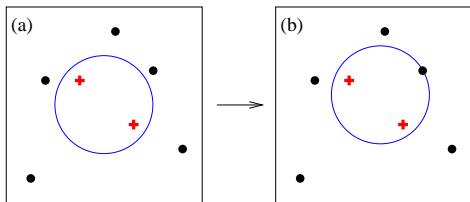
Runs in  $N^2 \ln N$  time ( $\simeq$  midpoint's  $N^3$ )

GPS & Soyez '07

Cones are just **circles** in the  $y - \phi$  plane. To find all stable cones:

1. Find all distinct ways of enclosing a subset of particles in a  $y - \phi$  circle
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Finding all distinct circular enclosures of a set of points is **geometry**:



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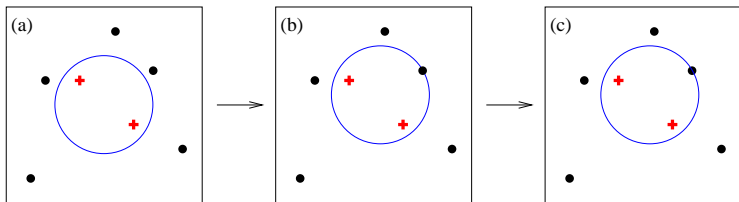
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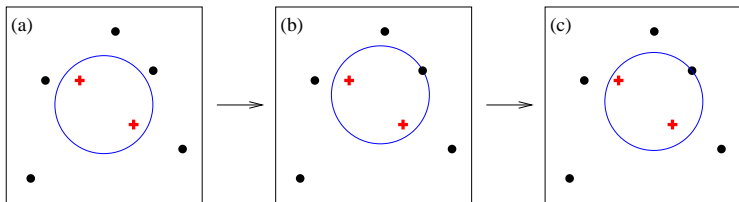
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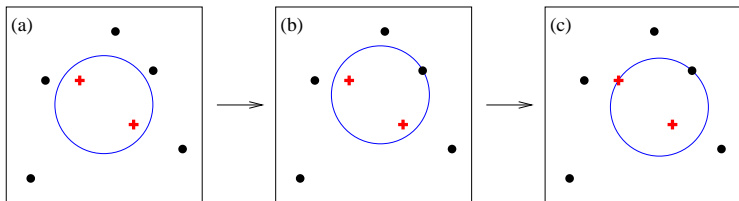
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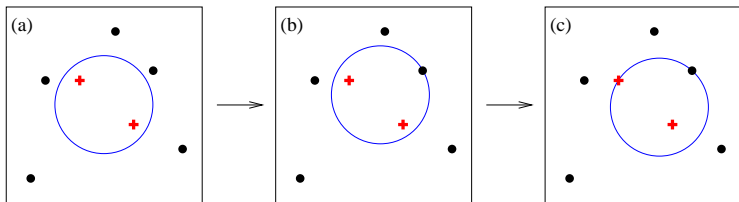
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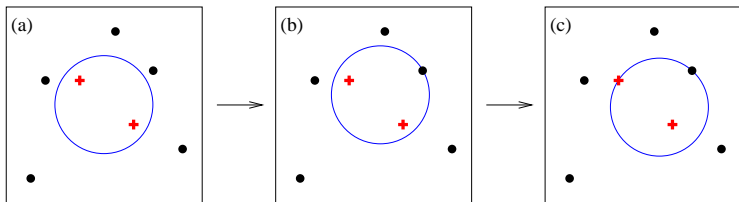
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GPS & Soyez '07

- 1: Put the set of current particles equal to the set of all particles in the event.
- 2: **repeat**
- 3: Find *all* stable cones of radius  $R$  for the current set of particles, e.g. using algorithm 2.
- 4: For each stable cone, create a protojet from the current particles contained in the cone, and add it to the list of protojets.
- 5: Remove all particles that are in stable cones from the list of current particles.
- 6: **until** No new stable cones are found, or one has gone around the loop  $N_{\text{pass}}$  times.
- 7: Run a Tevatron Run-II type split-merge procedure, algorithm 3, on the full list of protojets, with overlap parameter  $f$  and transverse momentum threshold  $p_{t,\text{min}}$ .

- ▶ Generate event with  $2 < N < 10$  hard particles, find jets
- ▶ Add  $1 < N_{soft} < 5$  soft particles, find jets again [repeatedly]
- ▶ If the jets are different, algorithm is IR unsafe.

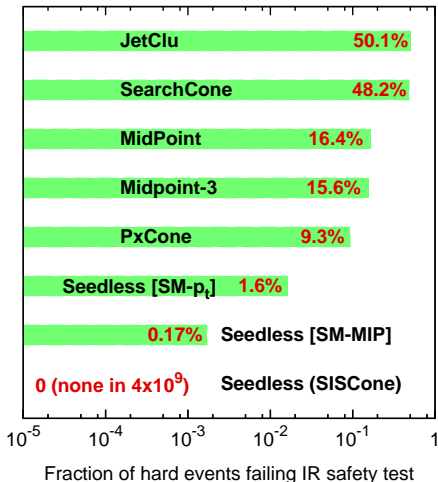
Unsafety level	failure rate
2 hard + 1 soft	~ 50%
3 hard + 1 soft	~ 15%
SISCone	IR safe !

Be careful with split-merge too

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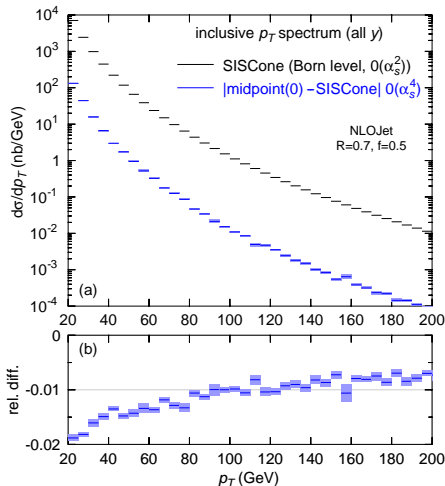
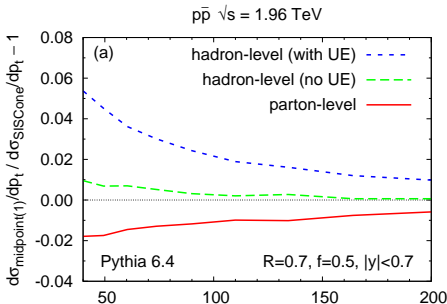


## Compare midpoint and SIScone

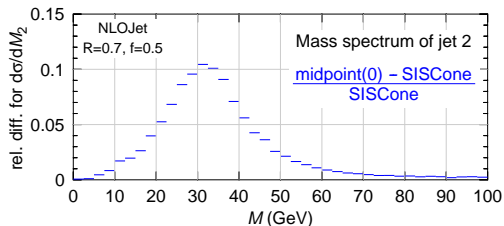
Result depends on observable:

- ▶ inclusive jet spectrum is the least sensitive (affected at NNLO)
- ▶ larger differences (5 – 10%) at hadron level

seedless reduces UE effect



Look at jet masses in multijet events. **NB: Jet masses reconstruct boosted  $W/Z/H/top$  in BSM searches**



Select 3-jet events

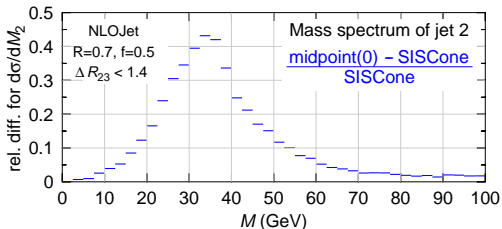
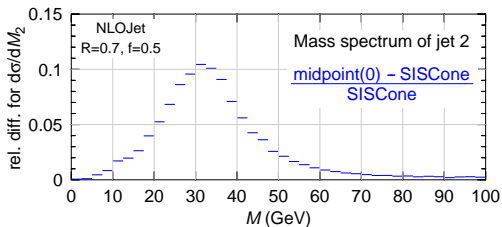
$$p_{t1,2,3} > \{120, 60, 20\} \text{ GeV,}$$

Calculate LO jet-mass spectrum for jet 2, compare midpoint with SISCone.

- ▶ 10% differences by default
- ▶ **40% differences** with extra cut  $\Delta R_{2,3} < 1.4$   
e.g. for jets from common decay chain

In complex events, IR safety matters

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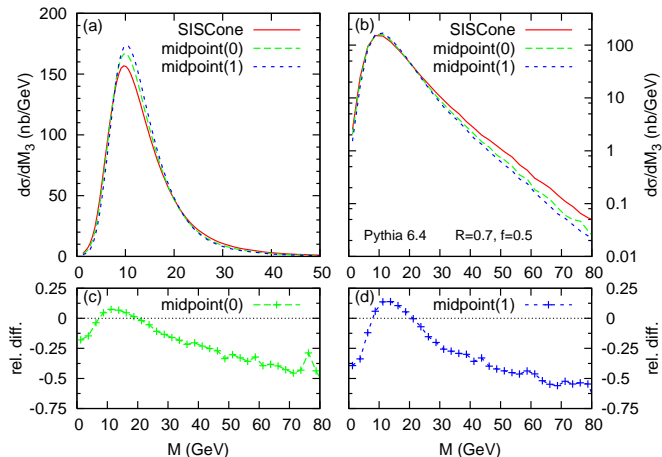
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**In complex events, IR safety matters**

Showering puts in many extra seeds: missing stable cones (in midpoint) should be less important?

Look at 3rd jet mass distribution (no  $\Delta R_{23}$  cut):



**Missing stable cones  $\rightarrow$  50% effects even after showering**



SISCone is good replacement for JetClu, Atlas iterative cone, and MidPoint type cones

**But these (xC-SM) all rather different from CMS It. Cone (IC-PR)**

Differ @ NLO for incl. jets

Do not have area =  $\pi R^2$

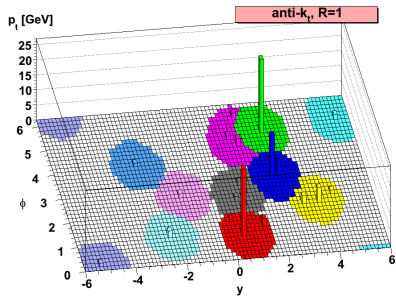
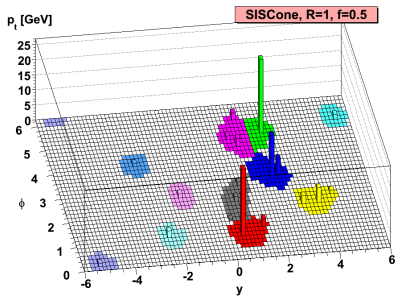
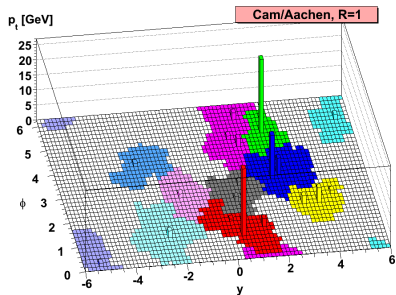
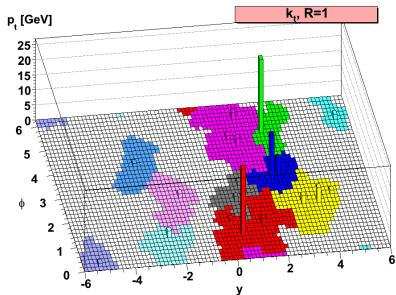
Alternative: drop the “cone” in definition, but get an algorithm that still acts like a cone: **anti- $k_t$**

1. Find smallest of  $d_{ij}$ ,  $d_{iB}$ :  $d_{ij} = \min(p_{ti}^{-2}, p_{tj}^{-2}) \Delta R_{ij}^2 / R^2$ ,  $d_{iB} = p_{ti}^{-2}$
2. if  $ij$ , recombine them; if  $iB$ , call  $i$  a jet, and remove from list of particles
3. repeat from step 1 until no particles left.

Cacciari, GPS & Soyez '08

Looks like  $k_t$  but behaves IC-PR.

# Jet contours – visualised



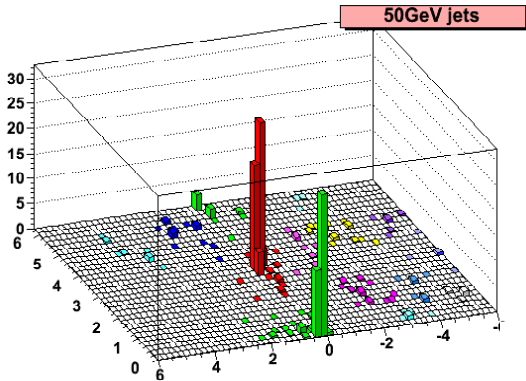
## Tevatron approach:

- ▶ Measure min-bias
- ▶ subtract  $n_{\text{vertex}} - 1 \times \pi R^2 \times \text{min-bias density}$ 
  - Assumes jet area =  $\pi R^2$ ; min-bias doesn't fluctuate
  - Used as “argument” against new jet algs

## Two approaches that I see as worth thinking about:

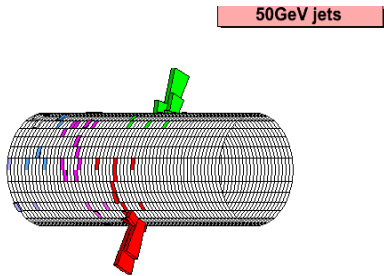
- ▶ Subtract pileup from calorimeter, before passing information to the jet algorithm
  - Issues: is calorimeter right scale to be subtracting on?
  - Some towers end up being negative — how does one address this?
- ▶ Subtract pileup from jets, after having carried out jet finding on calorimeter that includes the pileup.
  - Negative jets easily dealt with (throw them away)
  - But pileup can modify clustering (back-reaction)

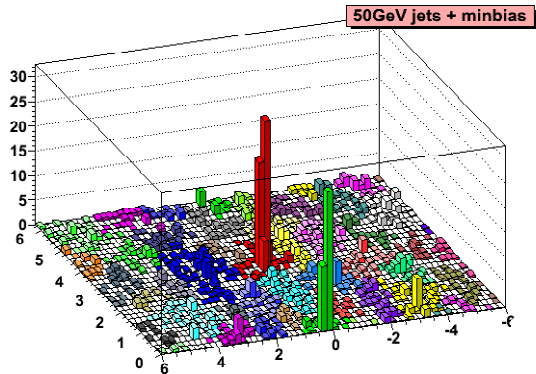
Last one developed with Cacciari ('07), to show that one can subtract pileup effectively with any alg.



'Standard hard' event  
Two well isolated jets

~ 200 particles  
Clustering takes  $\lesssim 1ms$

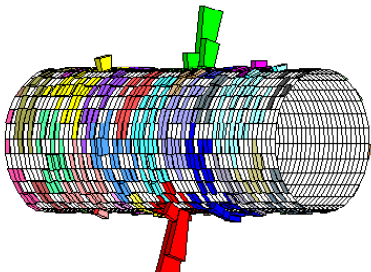


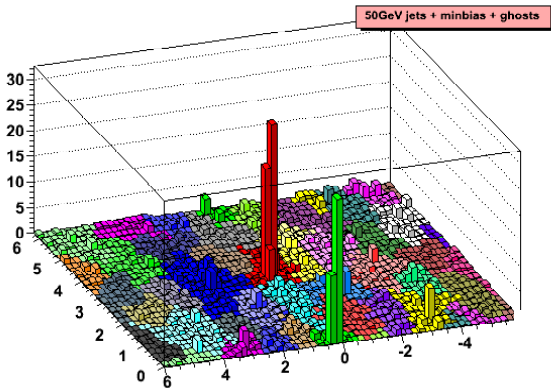


Add 10 min-bias events  
(moderately high lumi)

~ 2000 particles

Clustering takes ~ 10ms



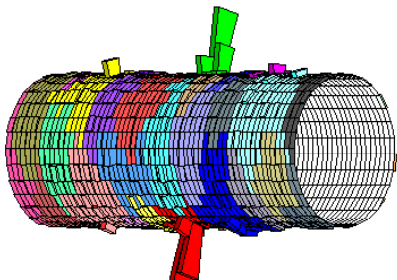


Add dense coverage of infinitely soft *"ghosts"*

See how many end up in jet to measure jet area

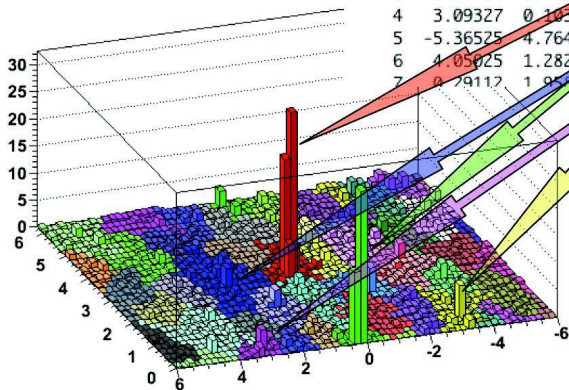
~ 10000 particles

Clustering takes ~ 0.2s



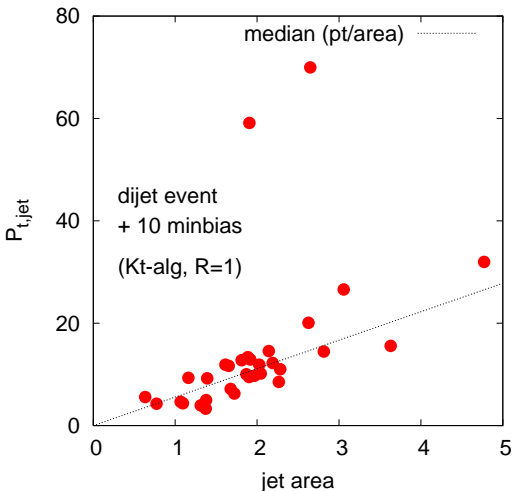
iev 0 (irepeat 24): number of particles = 1428  
 strategy used = NlnN  
 number of particles = 9051  
 Total area: 76.0265  
 Expected area: 76.0265

ijet	eta	phi	Pt	area +-	err
0	0.15050	3.24498	69.970	2.625 +-	0.020
1	0.18579	0.13150	59.133	1.896 +-	0.020
2	2.33840	3.23960	31.976	4.749 +-	0.028
3	-3.41796	0.52394	26.595	3.084 +-	0.021
4	3.09327	0.10350	20.072	2.688 +-	0.023
5	-5.36525	4.76491	19.593	2.780 +-	0.012
6	4.05025	1.28279	15.861	3.592 +-	0.028
7	0.29112	1.95745	12.566	2.114 +-	0.018



Approximate linear relation  
 between Pt and area for  
 minimum bias jets.

Can be used on an event-by-  
 event basis to correct the hard  
 jets



Jet areas in  $k_t$  algorithm are quite varied

Because  $k_t$ -alg adapts to the jet structure

- ▶ Hard jets' contamination from min-bias  $\sim$  area  
Area varies even for SISConc
- ▶ Soft jets'  $p_t/area$  tells you about min-bias normalisation and fluctuations

Median  $p_t/area$  across the set of jets in an event is a good estimator of pileup+UE in *that event*



## Basic Procedure:

- ▶ Use  $p_t/A$  from majority of jets (pileup jets) to get level,  $\rho$ , of pileup and UE in event
- ▶ Subtract pileup from hard jets:

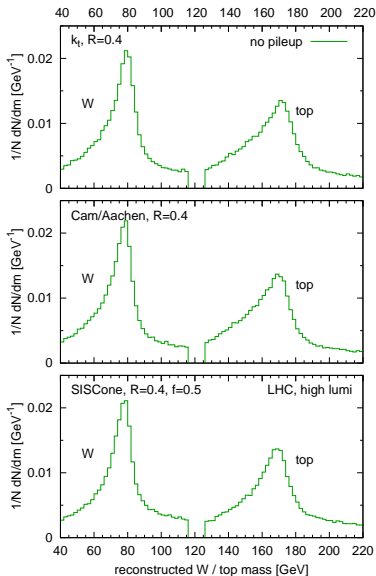
$$p_t \rightarrow p_{t,sub} = p_t - A\rho$$

Cacciari & GPS '07

## Illustration:

- ▶ semi-leptonic  $t\bar{t}$  production at LHC
- ▶ high-lumi pileup ( $\sim 20$  ev/bunch-X)

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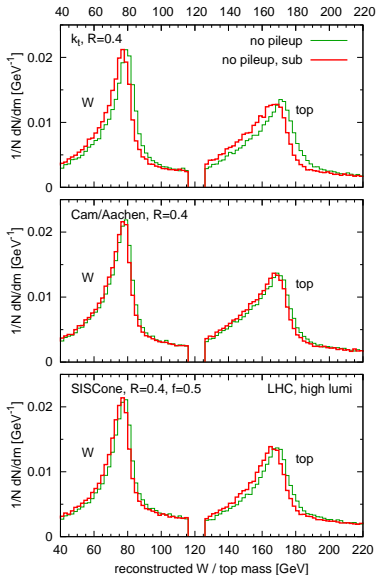
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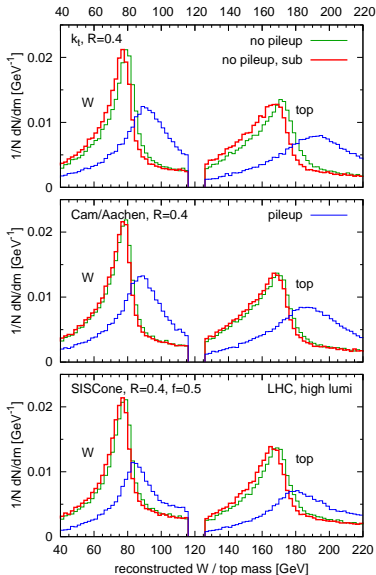
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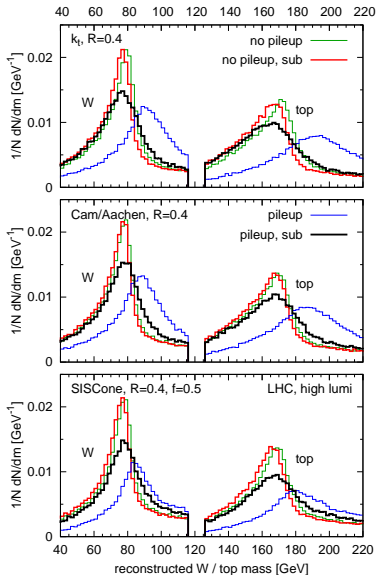
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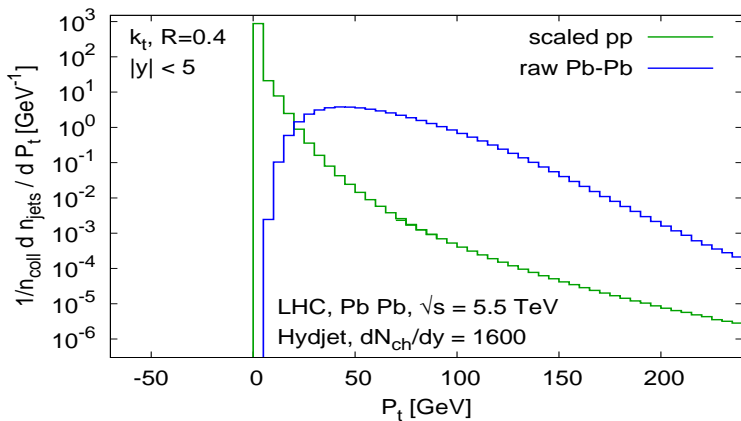
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## Example: inclusive jet spectrum

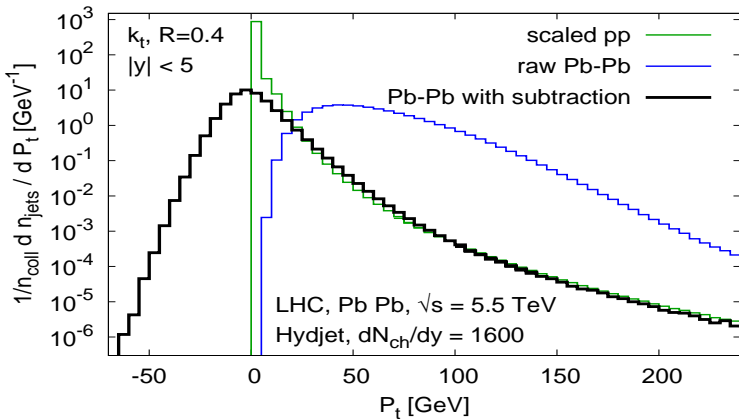
- ▶ Speed makes it easy to run  $k_t$  and Cam/Aachen on all 30k particles in HI event

- ▶ Subtraction provides a way to get sensible results, without biases from cut on low- $p_t$  particles.



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- ▶ Different algorithms are complementary Subject for a whole talk!
- ▶ You want to have access to that variety
- ▶ But you **do not** want to have IR unsafe algorithms  
Less stable, compromise benefit from \$50M theory
  
- ▶ For each type of IRC unsafe cone alg.,  $\exists$  a sensible replacement  
IC-SM  $\rightarrow$  SIScone, IC-PR  $\rightarrow$  anti- $k_t$
- ▶ No major cost in speed All accessible through fastjet
  
- ▶ You want to be able to subtract pileup *independently* from the jet algorithm
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# EXTRA MATERIAL

# SIScone part 2: finding stable cones

- 1: For any group of collinear particles, merge them into a single particle.
- 2: **for** particle  $i = 1 \dots N$  **do**
- 3: Find all particles  $j$  within a distance  $2R$  of  $i$ . If there are no such particles,  $i$  forms a stable cone of its own.
- 4: Otherwise for each  $j$  identify the two circles for which  $i$  and  $j$  lie on the circumference. For each circle, compute the angle of its centre  $C$  relative to  $i$ ,  $\zeta = \arctan \frac{\Delta\phi_{iC}}{\Delta y_{iC}}$ .
- 5: Sort the circles into increasing angle  $\zeta$ .
- 6: Take the first circle in this order, and call it the current circle. Calculate the total momentum and checkxor for the cones that it defines. Consider all 4 permutations of edge points being included or excluded. Call these the "current cones".
- 7: **repeat**
- 8:     **for** each of the 4 current cones **do**
- 9:         If this cone has not yet been found, add it to the list of distinct cones.
- 10:         If this cone has not yet been labelled as unstable, establish if the in/out status of the edge particles (with respect to the cone momentum axis) is the same as when defining the cone; if it is not, label the cone as unstable.
- 11:     **end for**
- 12:     Move to the next circle in order. It differs from the previous one either by a particle entering the circle, or one leaving the circle. Calculate the momentum for the new circle and corresponding new current cones by adding (or removing) the momentum of the particle that has entered (left); the checkxor can be updated by XORing with the label of that particle.
- 13:     **until** all circles considered.
- 14: **end for**
- 15: **for** each of the cones not labelled as unstable **do**
- 16:     Explicitly check its stability, and if it is stable, add it to the list of stable cones (protojets).
- 17: **end for**

**1: repeat**

Remove all protojets with  $p_t < p_{t,\min}$ .

Identify the protojet ( $i$ ) with the highest  $\tilde{p}_t$  ( $\tilde{p}_{t,\text{jet}} = \sum_{i \in \text{jet}} |p_{t,i}|$ ).

Among the remaining protojets identify the one ( $j$ ) with highest  $\tilde{p}_t$  that shares particles (overlaps) with  $i$ .

**5: if there is such an overlapping jet then**

**6:** Determine the total  $\tilde{p}_{t,\text{shared}} = \sum_{k \in i \& j} |p_{t,k}|$  of the particles shared between  $i$  and  $j$ .

**7: if  $\tilde{p}_{t,\text{shared}} < f \tilde{p}_{t,j}$  then**

Each particle that is shared between the two protojets is assigned to the one to whose axis it is closest. The protojet momenta are then recalculated.

**9: else**

Merge the two protojets into a single new protojet (added to the list of protojets, while the two original ones are removed).

**11: end if**

**12:** If steps 7–11 produced a protojet that coincides with an existing one, maintain the new protojet as distinct from the existing copy(ies).

**13: else**

Add  $i$  to the list of final jets, and remove it from the list of protojets.

**15: end if**

**16: until** no protojets are left.

# How much does IR safety *really* matter?

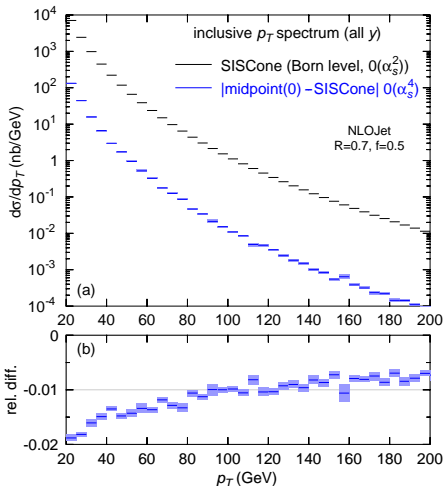
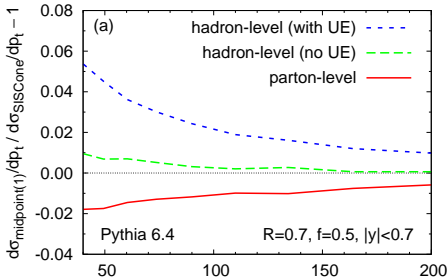
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Result depends on observable:

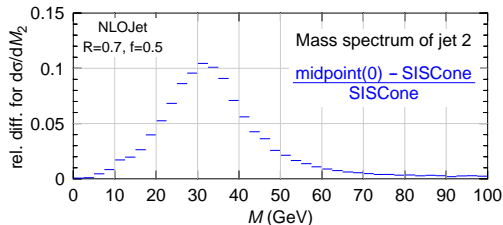
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seedless reduces UE effect

$p\bar{p}$   $\sqrt{s} = 1.96$  TeV



Look at jet masses in multijet events. **NB:** Jet masses reconstruct boosted  $W/Z/H/top$  in BSM searches



Select 3-jet events

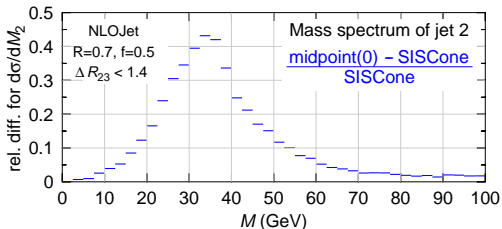
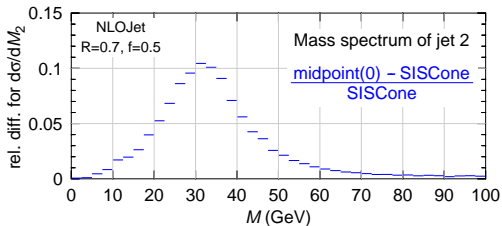
$$p_{t1,2,3} > \{120, 60, 20\} \text{ GeV,}$$

Calculate LO jet-mass spectrum for jet 2, compare midpoint with SISCone.

- ▶ 10% differences by default
- ▶ **40% differences** with extra cut  $\Delta R_{2,3} < 1.4$   
e.g. for jets from common decay chain

In complex events, IR safety matters

Look at jet masses in multijet events. **NB:** Jet masses reconstruct boosted  $W/Z/H/top$  in BSM searches



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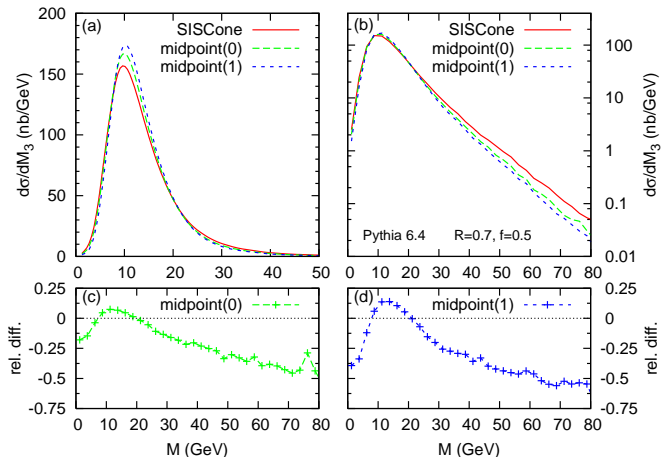
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- ▶ 10% differences by default
- ▶ **40% differences** with extra cut  $\Delta R_{2,3} < 1.4$   
 e.g. for jets from common decay chain

**In complex events, IR safety matters**

Showering puts in many extra seeds: missing stable cones (in midpoint)  
 should be less important?

Look at 3rd jet mass distribution (no  $\Delta R_{23}$  cut):



**Missing stable cones  $\rightarrow$  50% effects even after showering**



# A full set of IRC-safe jet algorithms

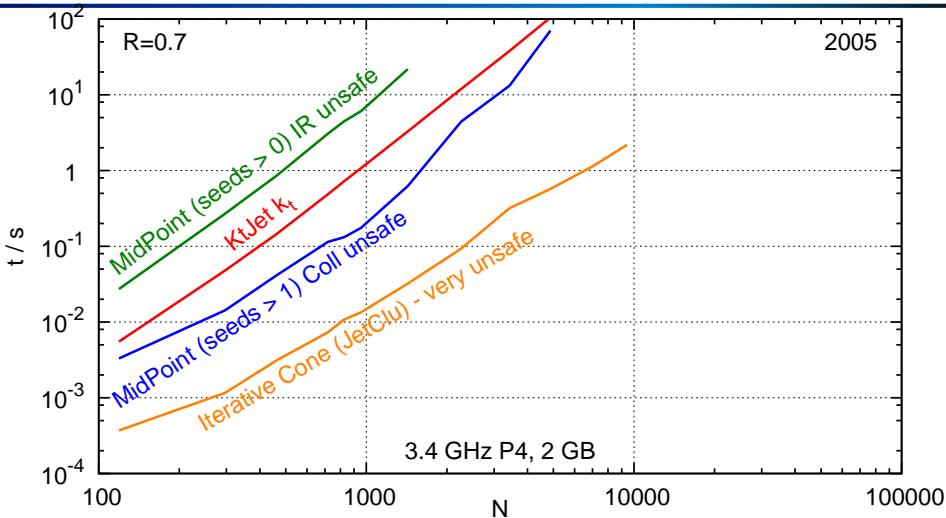
Generalise inclusive-type sequential recombination with

$$d_{ij} = \min(k_{ti}^{2p}, k_{tj}^{2p}) \Delta R_{ij}^2 / R^2 \quad d_{iB} = k_{ti}^{2p}$$

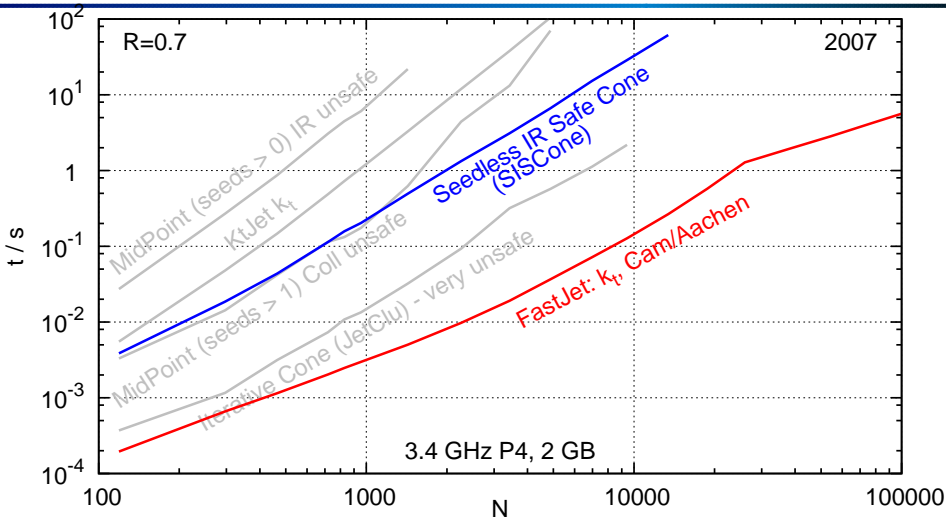
	Alg. name	Comment	time
$p = 1$	$k_t$ CDOSTW '91-93; ES '93	Hierarchical in rel. $k_t$	$N \ln N$ exp.
$p = 0$	Cambridge/Aachen Dok, Leder, Moretti, Webber '97 Wengler, Wobisch '98	Hierarchical in angle Scan multiple $R$ at once $\leftrightarrow$ QCD angular orderin	$N \ln N$
$p = -1$	anti- $k_t$ Cacciari, GPS, Soyez '08 $\sim$ reverse- $k_t$ Delsart, Loch et al.	Hierarchy meaningless. Behaves like IC-PR	$N^{3/2}$
SC-SM	SISCone GPS Soyez '07 + Tevatron run II '00	Replacement for IC-SM notably "MidPoint" cones	$N^2 \ln N$ exp.

One could invent/try others (e.g. OJF, etc.). Our [Paris+BNL] philosophy: 4 algs is enough of a basis to develop first physics understanding.

We already have far more than can be shown here



Single package, **FastJet**, to access all developments, natively ( $k_t$ , Cam/Aachen) or as plugins (SISCone): Cacciari, GPS & Soyez '05-07  
<http://www.lpthe.jussieu.fr/~salam/fastjet/>



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## Reach of jet algorithms

