

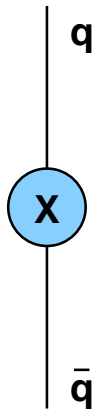
# Towards Jetography

Gavin Salam

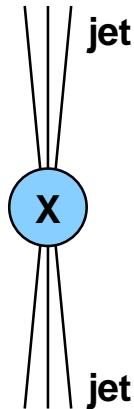
LPTHE, CNRS and UPMC (Univ. Paris 6)

DESY Theory Seminar  
18 November 2008

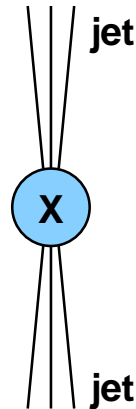
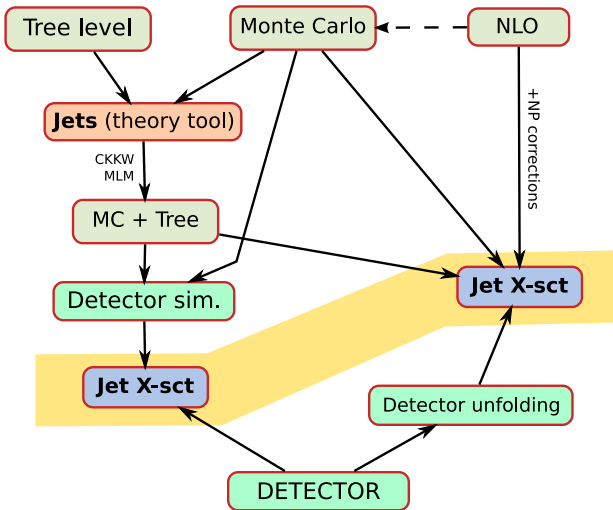
Based on papers with  
Jon Butterworth, Matteo Cacciari, Mrinal Dasgupta, Adam Davison,  
Lorenzo Magnea, Juan Rojo, Mathieu Rubin & Gregory Soyez



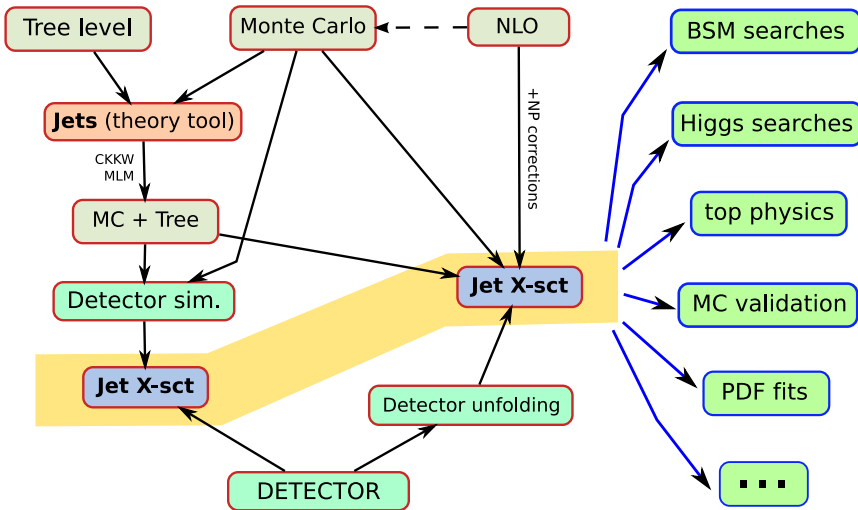
We never see quarks or gluons, only jets



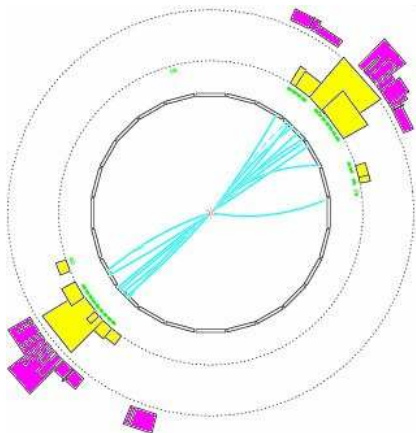
We never see quarks or gluons, only **jets**



Jets are common language of experiment and theory



And the input to nearly all hadronic analyses

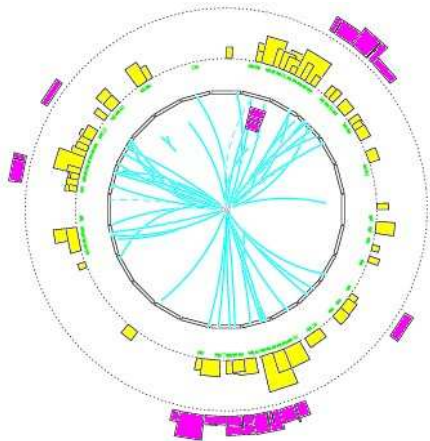
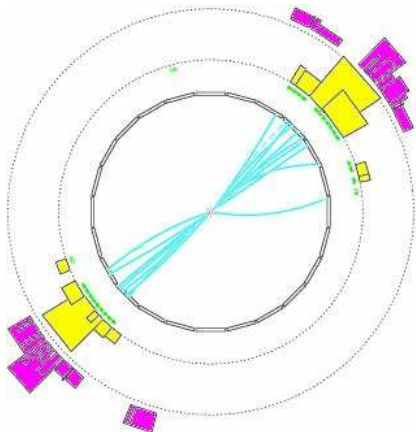


Jets are what we see.  
Clearly(?) 2 of them.

2 partons?

$$E_{parton} = M_z/2?$$

How many jets do you see?  
Do you really want to ask yourself  
this question for  $10^8$  events?



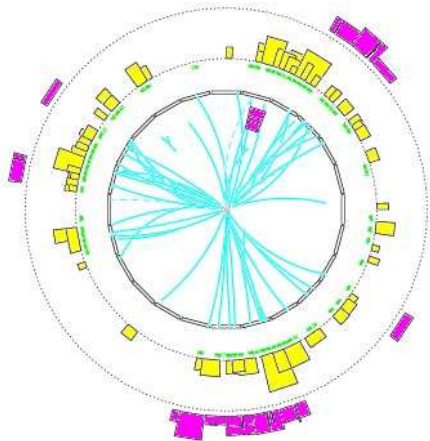
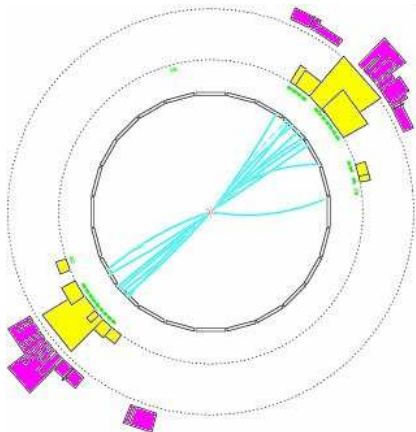
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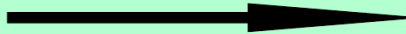


## jet definition

 $\{P_i\}$ 

particles,  
4-momenta,  
calorimeter towers, ...

jet algorithm

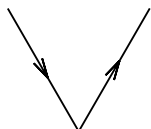
 $\{j_k\}$ 

jets

+ parameters (usually at least the radius  $R$ )

+ recombination scheme

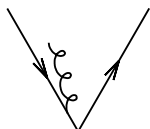
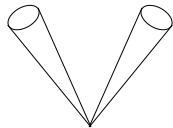
Reminder: running a jet definition gives a well defined physical observable,  
which we can measure and, hopefully, calculate



LO partons

Jet ↓ Def<sup>n</sup>

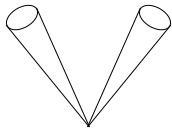
jet 1      jet 2



NLO partons

Jet ↓ Def<sup>n</sup>

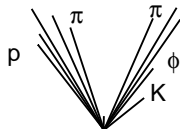
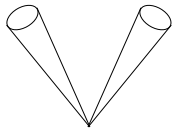
jet 1      jet 2



parton shower

Jet ↓ Def<sup>n</sup>

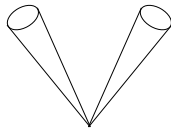
jet 1      jet 2



hadron level

Jet ↓ Def<sup>n</sup>

jet 1      jet 2



**Projection to jets should be resilient to QCD effects**

Which jet definition(s) for LHC?

Can we address this question  
scientifically?

Jetography

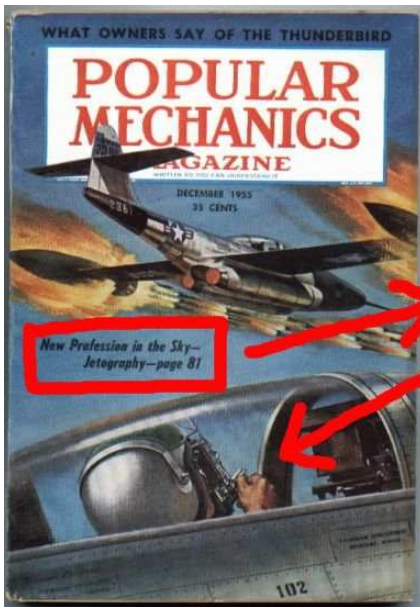
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**Jetography**

# Jetography dates back to 1955





*New Profession in the Sky—  
Jetography—page 81*

Question #1:  
What's wrong with what we have?

## HERA:

- ▶ jets from 5 – 100 GeV
- ▶ very quiet environment

use single jet-def:  
 $k_t$  with  $R = 1$

## Tevatron:

- ▶ jets from 50 – 500 GeV
  - ▶ some noise: 2 – 10 GeV/unit rapidity
  - ▶ multi-jet important (e.g.  $t\bar{t} \rightarrow 6$  jets)
- use two jet-defs: cone with  $R = 0.4, R = 0.7$

## LHC:

- ▶ jets from 50 – 5000 GeV [that's why it's being built]
- ▶ lots of noise: 10 – 100 GeV/unit rapidity [high-lumi pileup]
- ▶ multi-jet still important (e.g.  $t\bar{t} \rightarrow 6$  jets)

2 orders of magnitude in jet energy + 1 order of magnitude in noise  
"Fixed-focus" jet finding just won't be good enough at LHC

Just as fixed-focus cameras aren't adequate for professional photography



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Question #2:

what jet algorithms are out there?

sequential recombination ( $k_t$ )  
& cone type

# Sequential recombination ( $k_t$ alg)

Sequential recombination algorithms:

- ▶ introduce distance  $d_{ij}$  between pairs of particles
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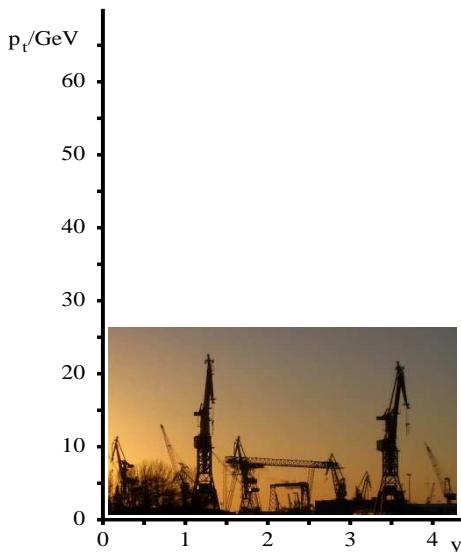
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One parameter,  $R$ , sets the angular reach for the jets

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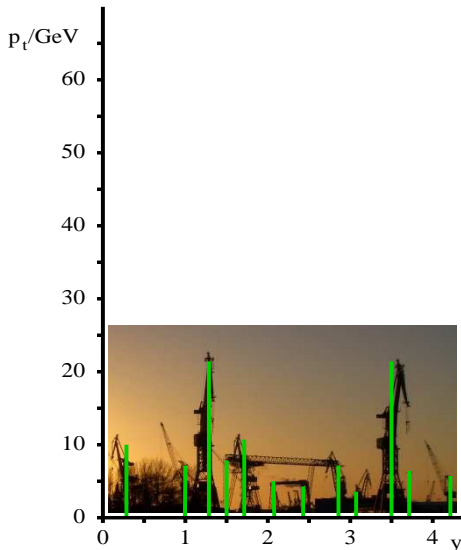
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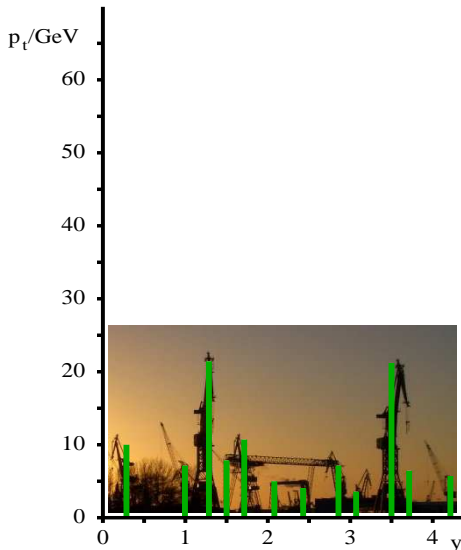
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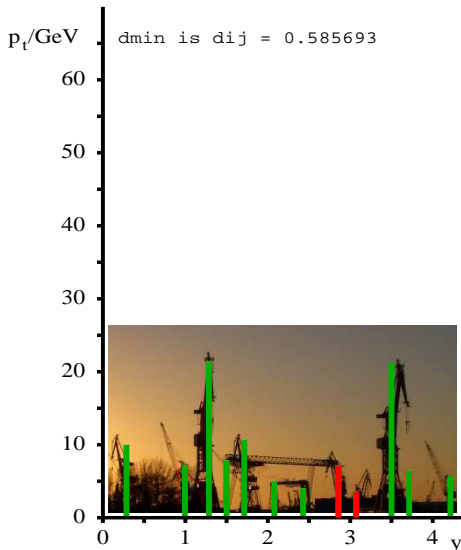
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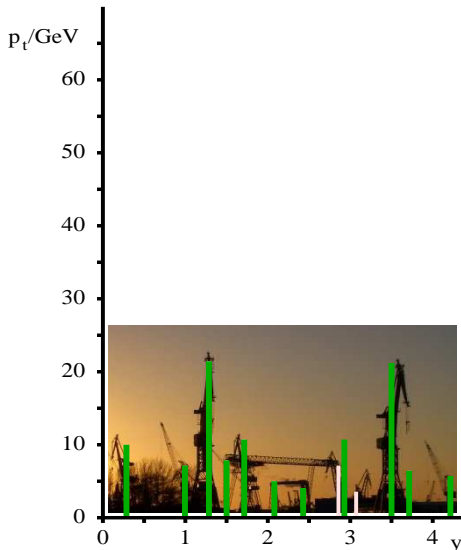
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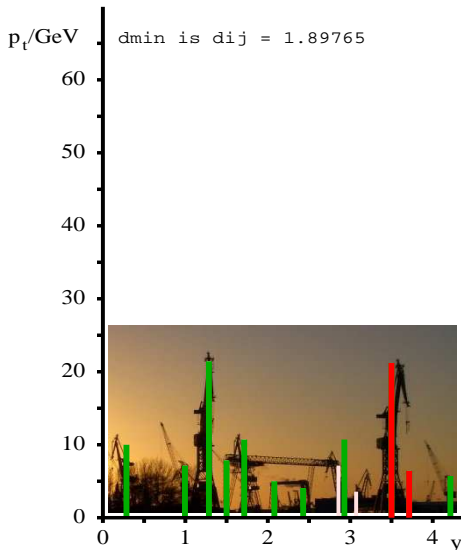
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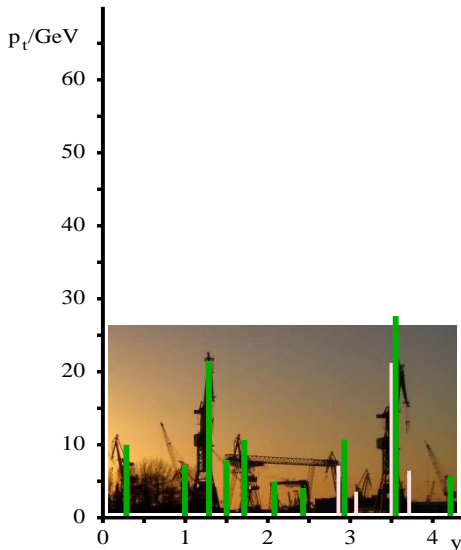
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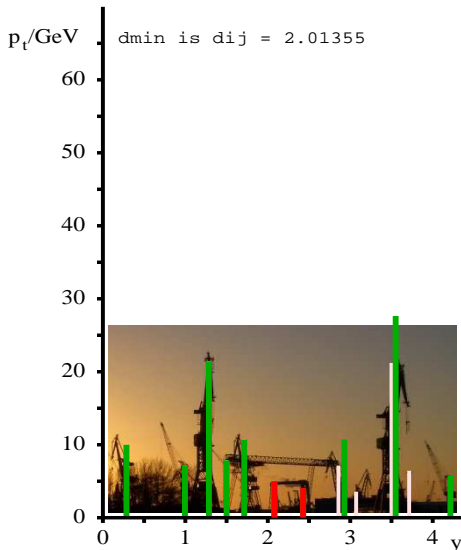
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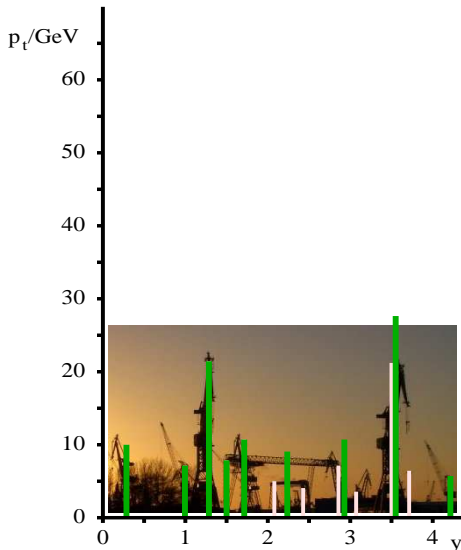
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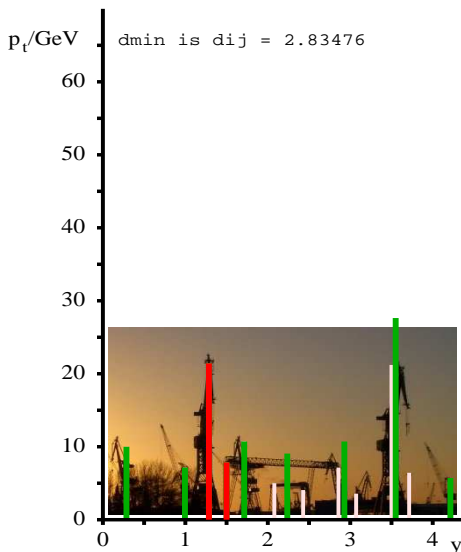
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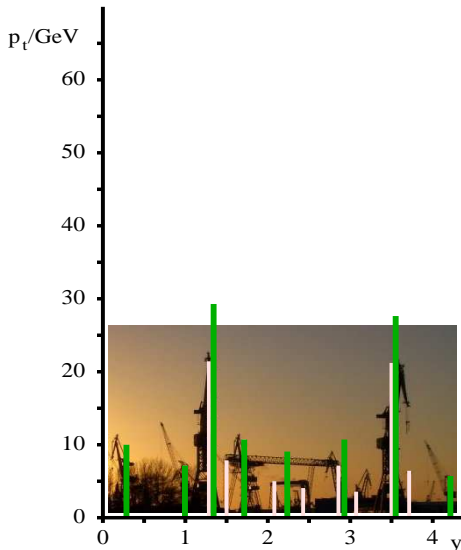
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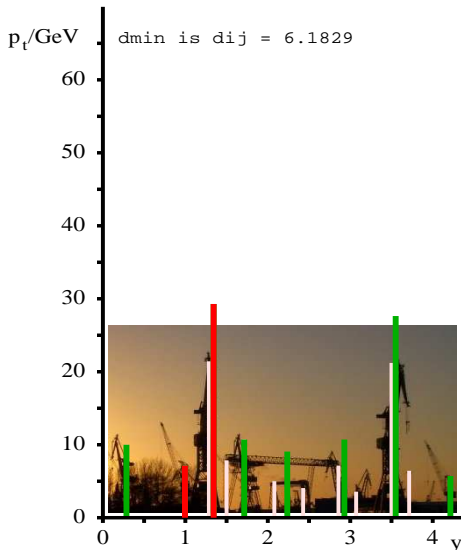
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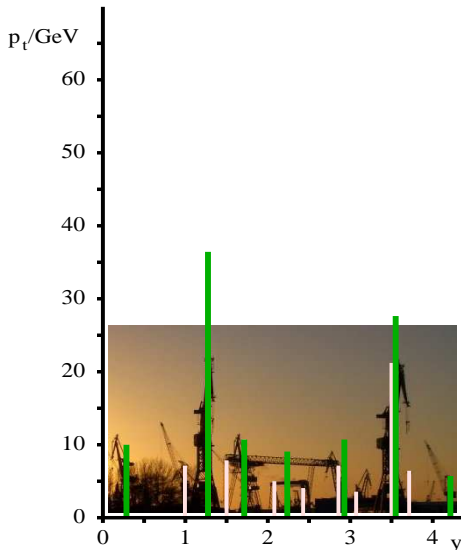
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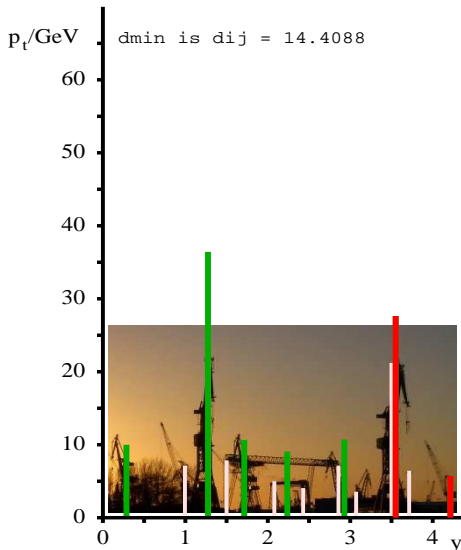
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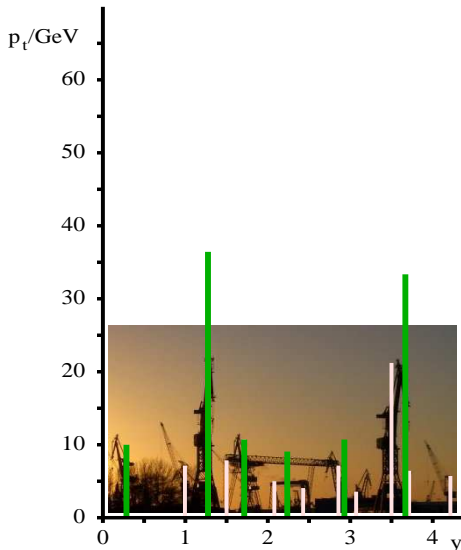
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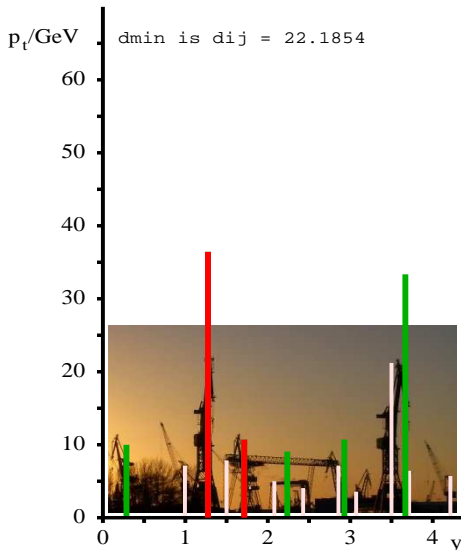
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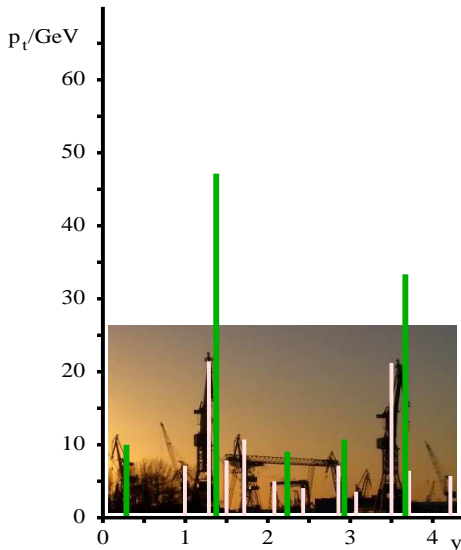
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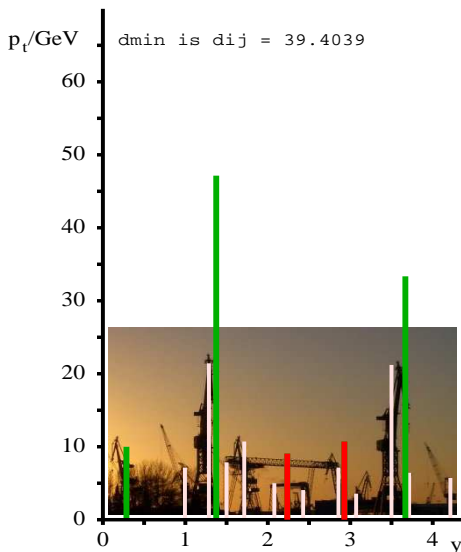
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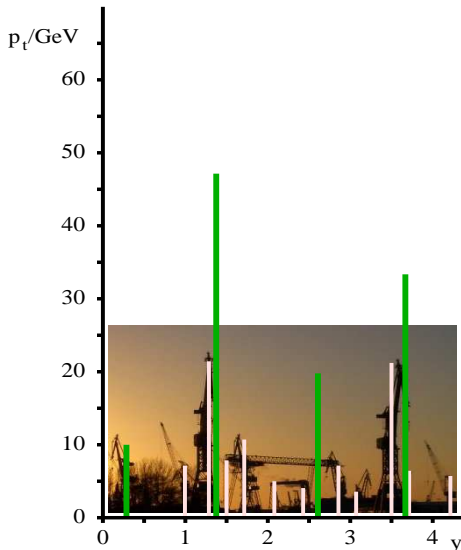
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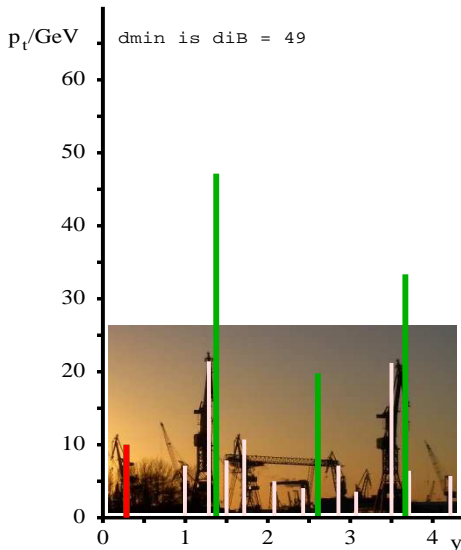
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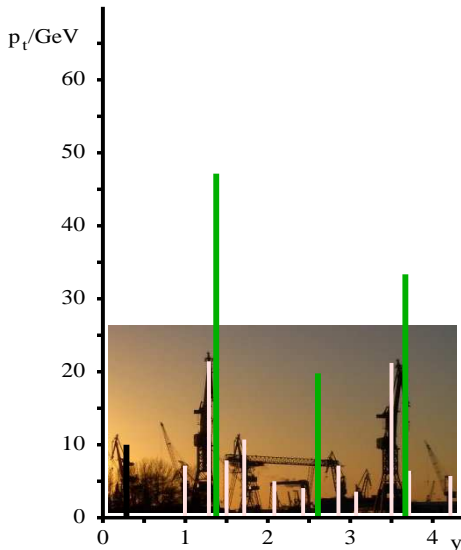
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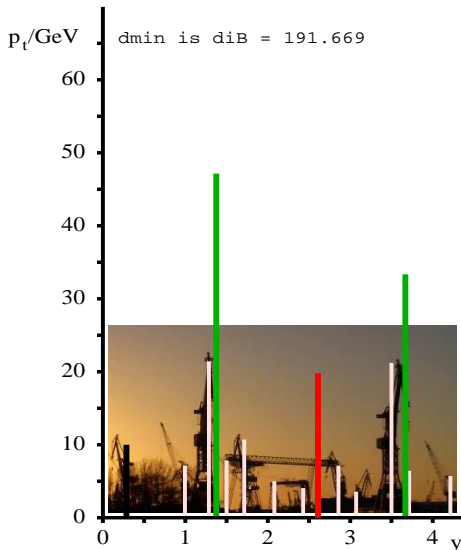
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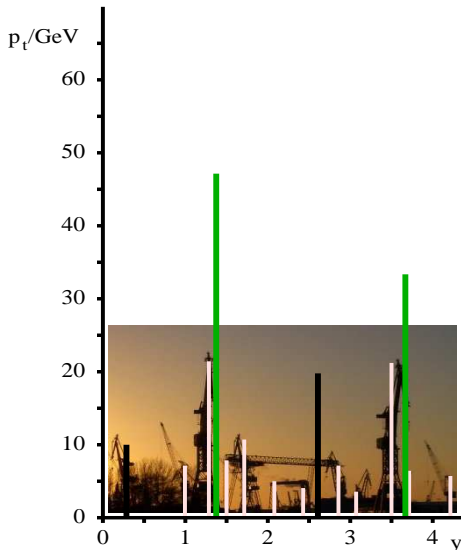
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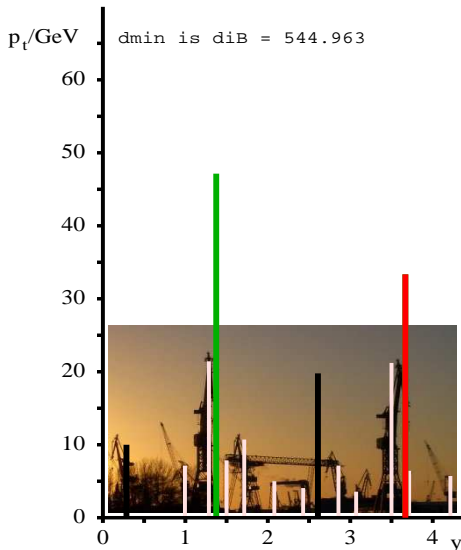
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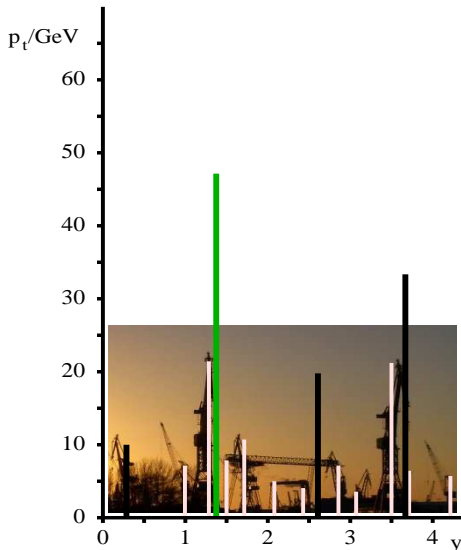
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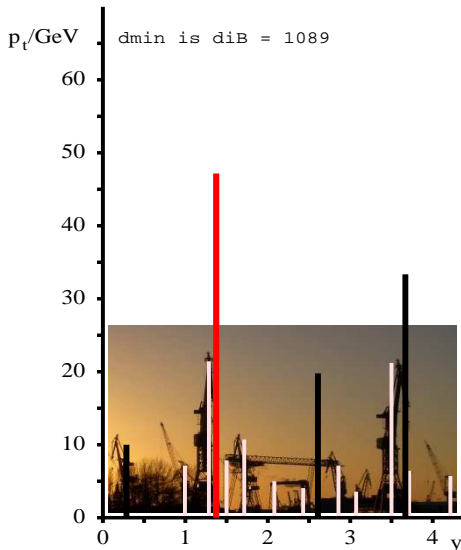
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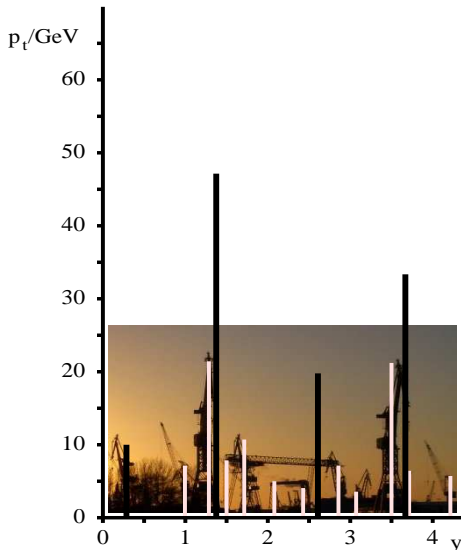
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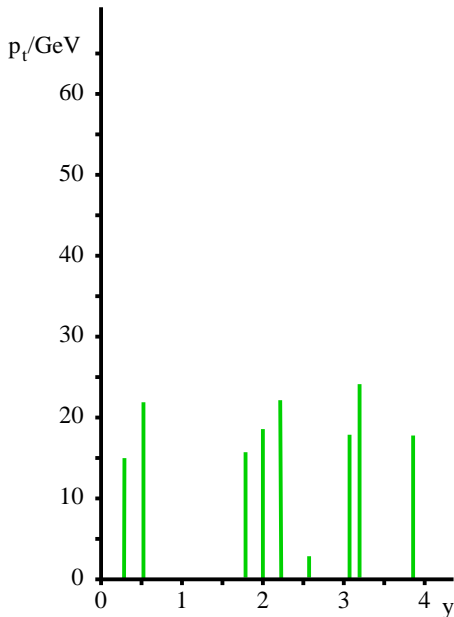
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Aim to identify *all* stable cones, independently of any seeds

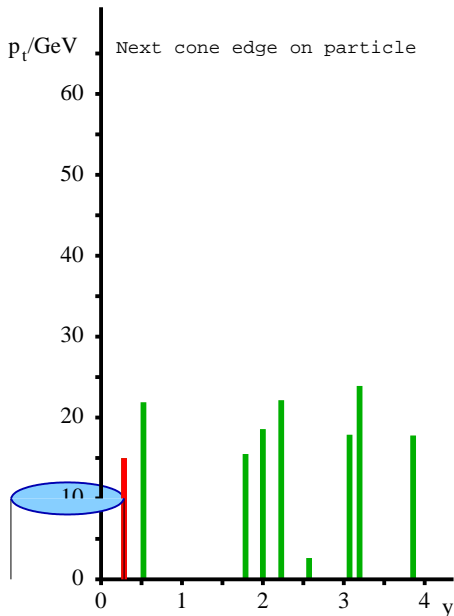
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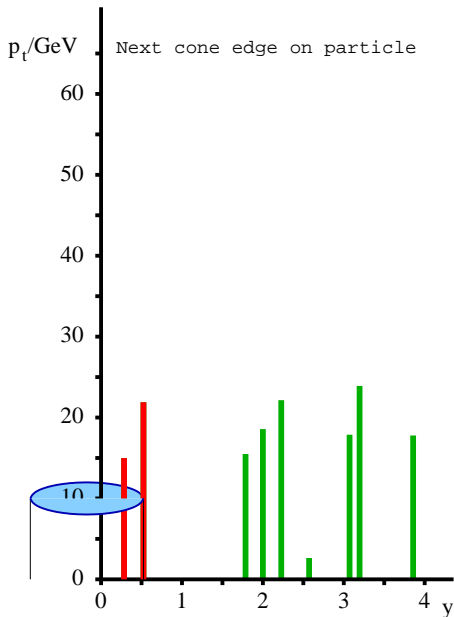
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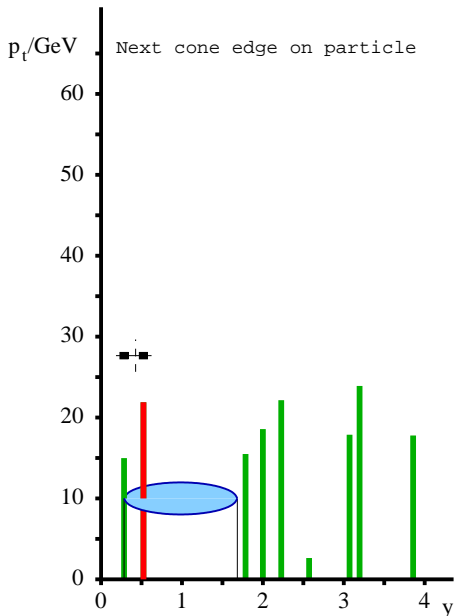
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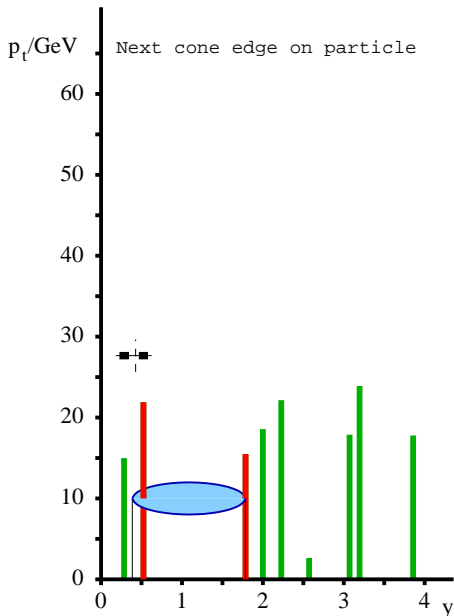
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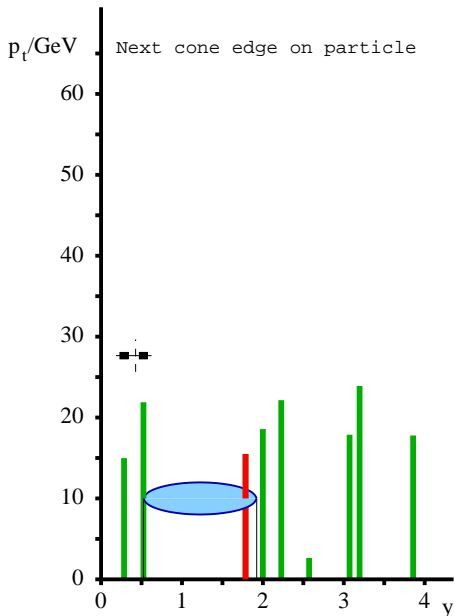
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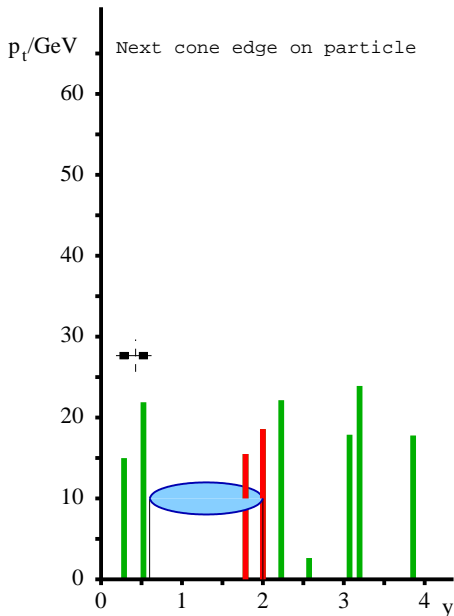
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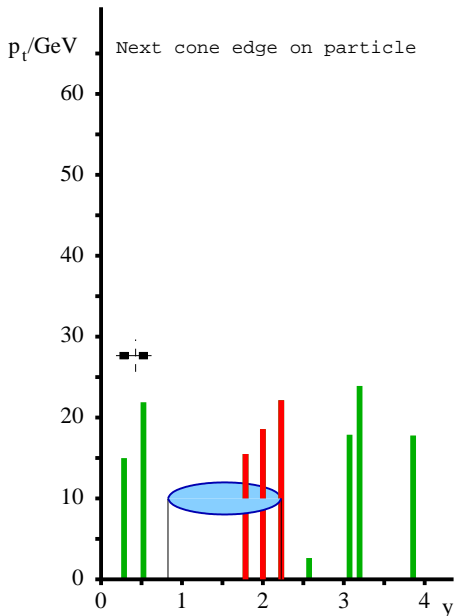
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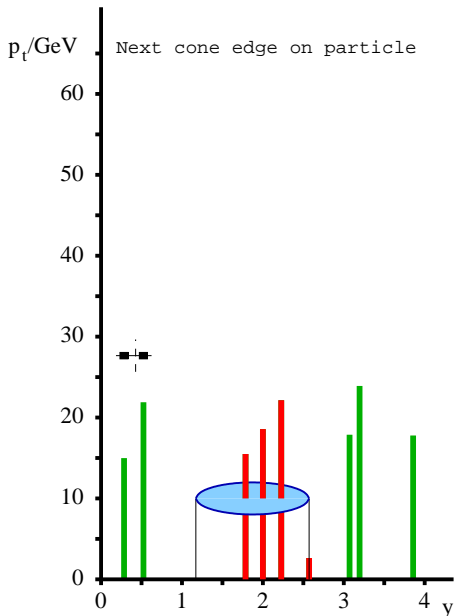
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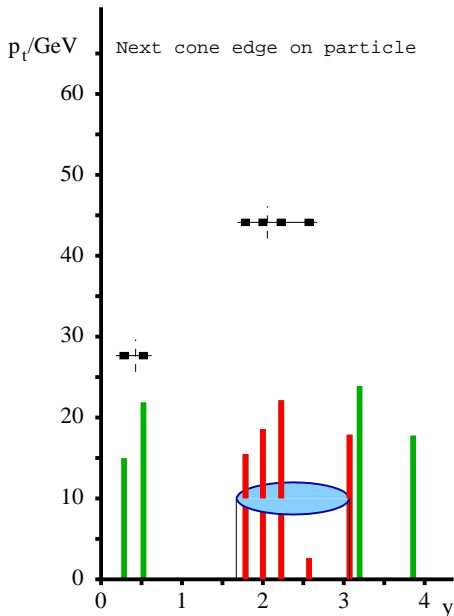
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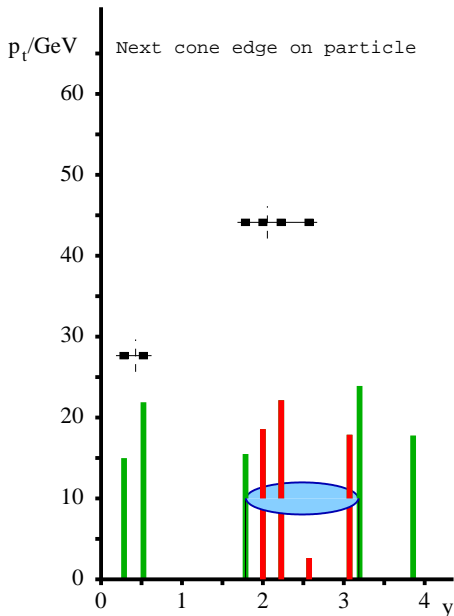
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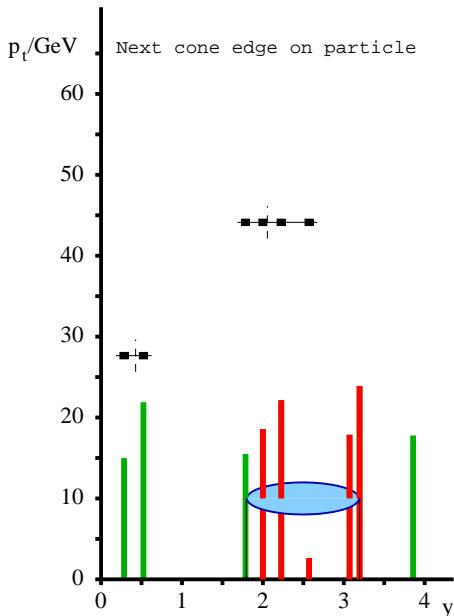
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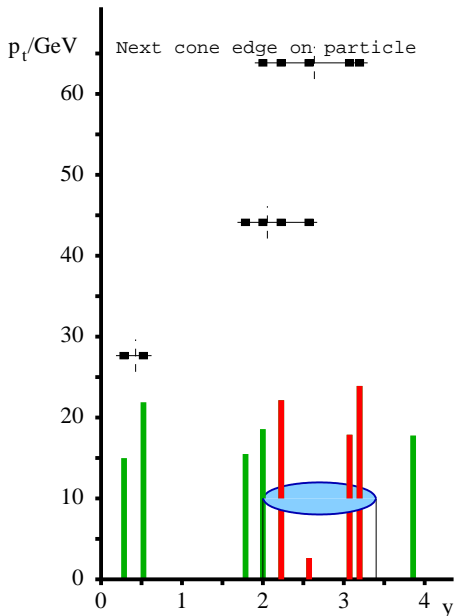
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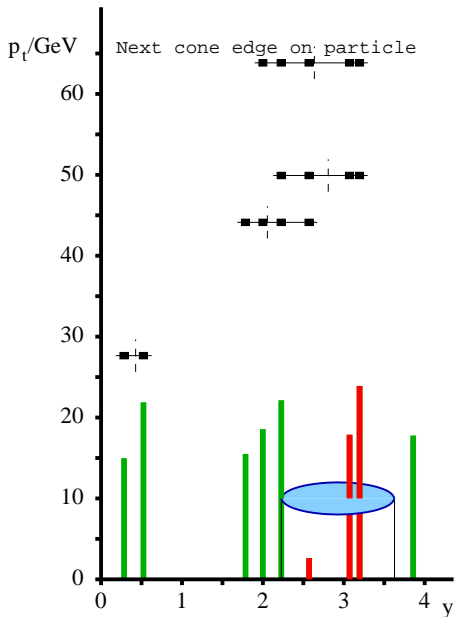
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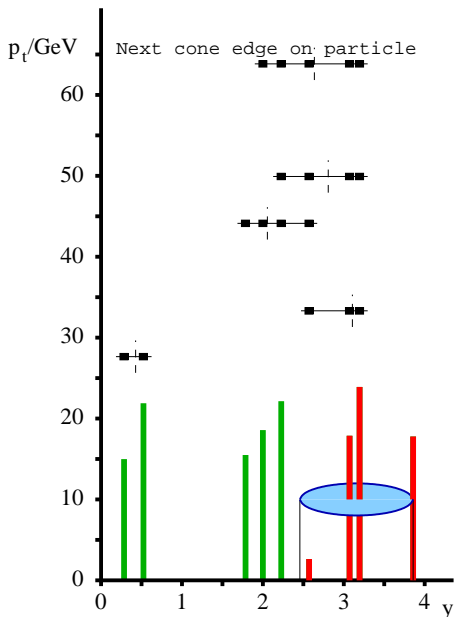
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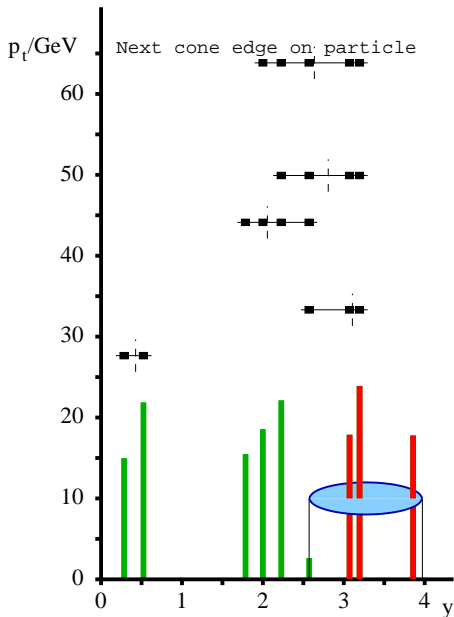
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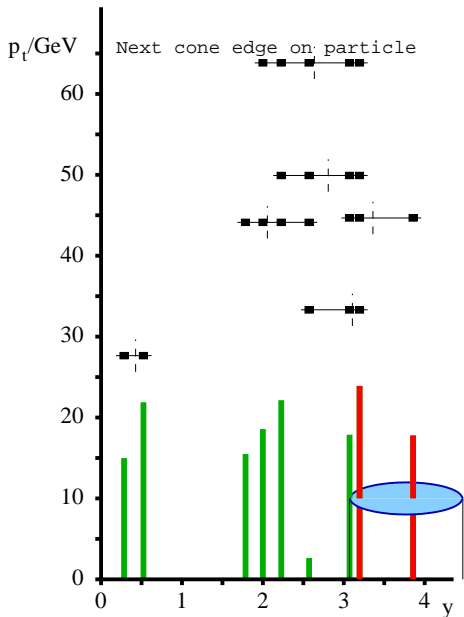
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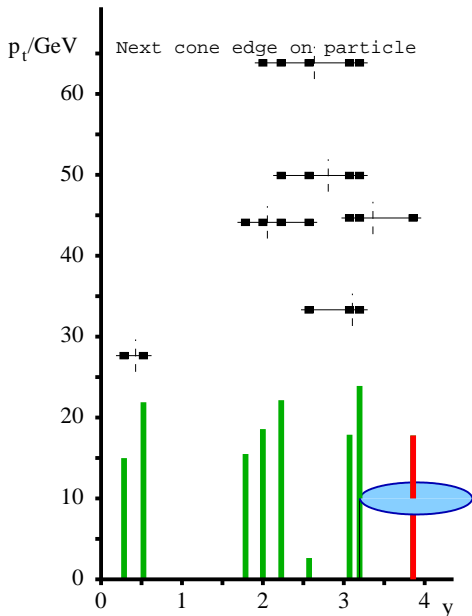
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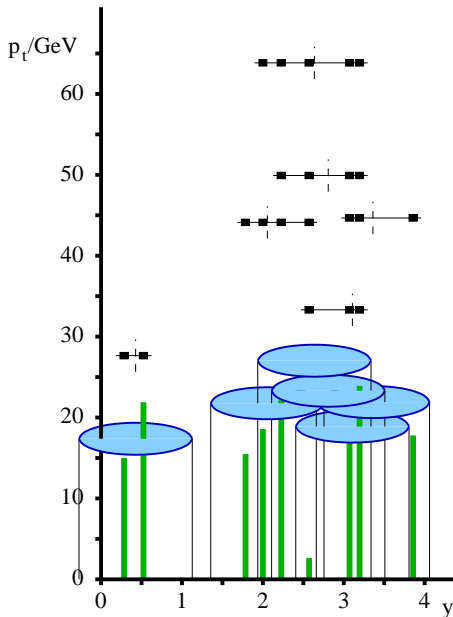
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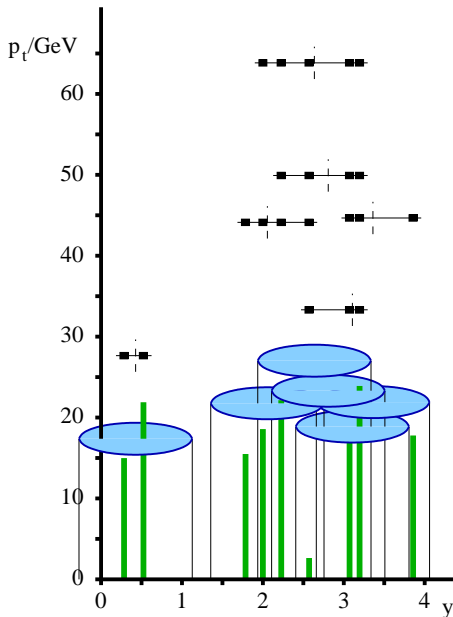
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## A full set of IRC-safe jet algorithms

Generalise inclusive-type sequential recombination with

$$d_{ij} = \min(k_{ti}^{2p}, k_{tj}^{2p}) \Delta R_{ij}^2 / R^2 \quad d_{iB} = k_{ti}^{2p}$$

	Alg. name	Comment	time
$p = 1$	$k_t$ CDOSTW '91-93; ES '93	Hierarchical in rel. $k_t$	$N \ln N$ exp.
$p = 0$	Cambridge/Aachen Dok, Leder, Moretti, Webber '97 Wengler, Wobisch '98	Hierarchical in angle Scan multiple $R$ at once ↔ QCD angular ordering	$N \ln N$
$p = -1$	anti- $k_t$ Cacciari, GPS, Soyez '08 ~ reverse- $k_t$ Delsart	Hierarchy meaningless, jets like CMS cone (IC-PR)	$N^{3/2}$
SC-SM	SISCone GPS Soyez '07 + Tevatron run II '00	Replaces JetClu, ATLAS MidPoint (xC-SM) cones	$N^2 \ln N$ exp.

**All these algorithms coded in (efficient) C++ at**  
<http://fastjet.fr/> (Cacciari, GPS & Soyez '05-08)

kt adapts to the  
jet structure

the cone gives  
nice conical jets

the cone is too  
rigid

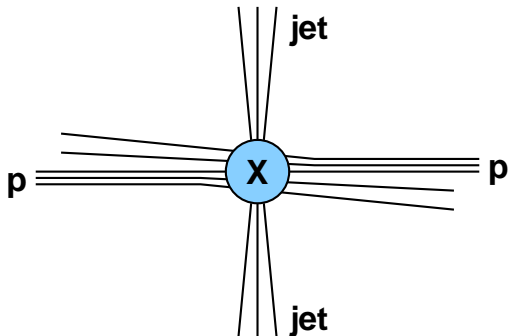
kt's a vacuum  
cleaner

cone has big  
hadronisation  
corrections

kt's too irregular  
I can't correct  
for pileup

Past jet discussions often polarised, driven by unquantified statements

Question #3:  
what do we mean by a “better” jet  
definition?



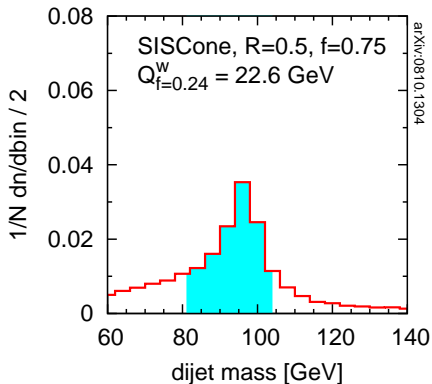
**Quality = suited to whatever you use the jets for**

Simplest application: reconstruct dijet invariant mass peak for some new particle.

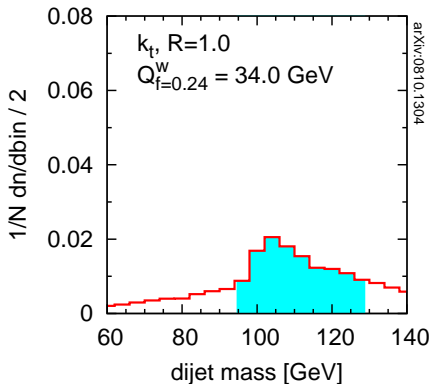
e.g.  $pp \rightarrow X \rightarrow qq \rightarrow 2 \text{ jets}$

Good jet algorithm  $\rightarrow$  better invariant mass peak.



qq,  $M = 100$  GeV

**SIScone  $R = 0.5$**   
**BETTER**

qq,  $M = 100$  GeV

**$k_t$ ,  $R = 1.0$**   
**WORSE**

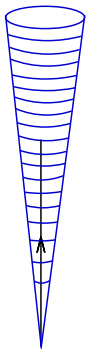
Question #4a:

What physics governs quality  
of jet definition?

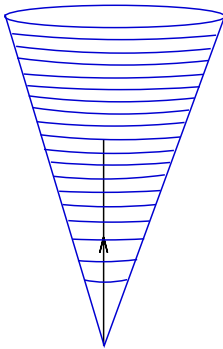
[ $R$ -dependence]

Small v. large jet radius ( $R$ )  $\equiv$  HSBC

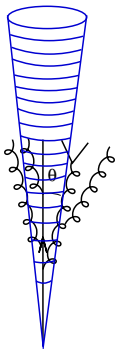
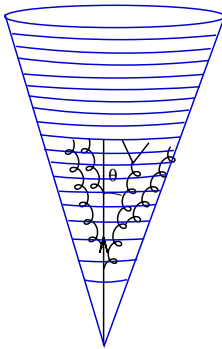
Small jet radius



Large jet radius



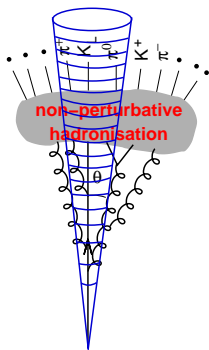
single parton @ LO: **jet radius irrelevant**

Small v. large jet radius ( $R$ )  $\equiv$  HSBC**Small jet radius****Large jet radius**

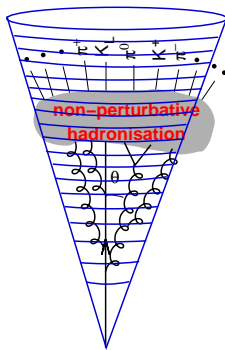
perturbative fragmentation: **large jet radius better**  
(it captures more)

Small v. large jet radius ( $R$ )  $\equiv$  HSBC

## Small jet radius

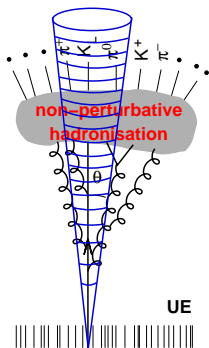


## Large jet radius

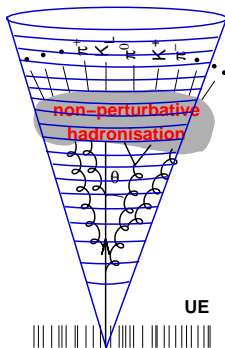


non-perturbative fragmentation: **large jet radius better**  
(it captures more)

## Small jet radius



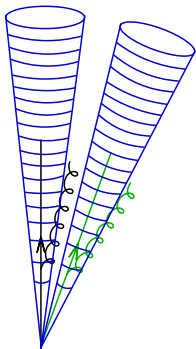
## Large jet radius



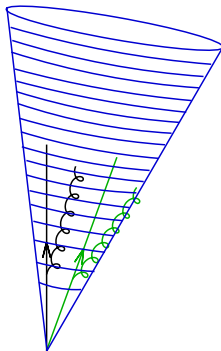
underlying ev. & pileup “noise”: **small jet radius better**  
(it captures less)

Small v. large jet radius ( $R$ )  $\equiv$  HSBC

## Small jet radius



## Large jet radius



multi-hard-parton events: **small jet radius better**  
(it resolves partons more effectively)

*4-way tension in many measurements:*

Prefer small $R$	prefer large $R$
resolve many jets (e.g. $t\bar{t}$ )	minimize QCD radiation loss
limit UE & pileup	limit hadronisation



Parton  $p_t \rightarrow$  jet  $p_t$

Ill-defined: MC “parton”

### PT radiation:

$$q : \quad \langle \Delta p_t \rangle \simeq \frac{\alpha_s C_F}{\pi} p_t \ln R$$

$$g : \quad \langle \Delta p_t \rangle \simeq \frac{\alpha_s C_A}{\pi} p_t \ln R$$

### Hadronisation:

$$q : \quad \langle \Delta p_t \rangle \simeq -\frac{C_F}{R} \cdot 0.4 \text{ GeV}$$

$$g : \quad \langle \Delta p_t \rangle \simeq -\frac{C_A}{R} \cdot 0.4 \text{ GeV}$$

### Underlying event:

$$q, g : \quad \langle \Delta p_t \rangle \simeq \frac{R^2}{2} \cdot 2.5 - 15 \text{ GeV}$$

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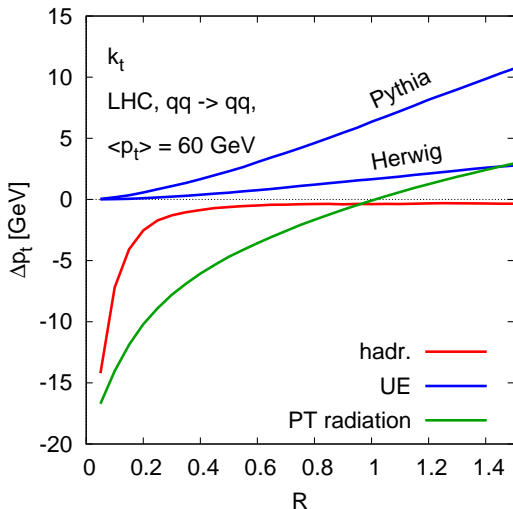
### Hadronisation:

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Dasgupta, Magnea & GPS '07

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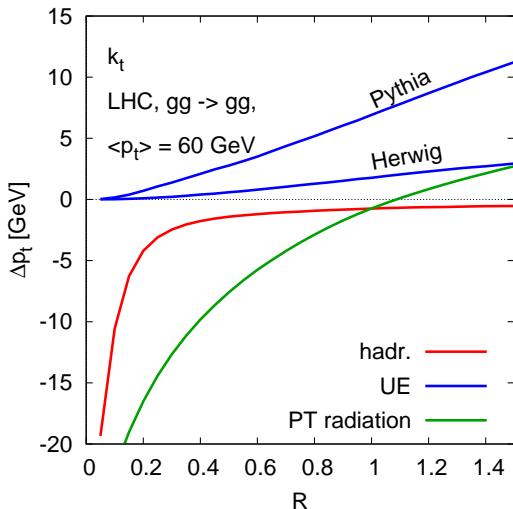
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Dasgupta, Magnea & GPS '07

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$$g : \quad \langle \Delta p_t \rangle \simeq \frac{\alpha_s C_A}{\pi} p_t \ln R$$

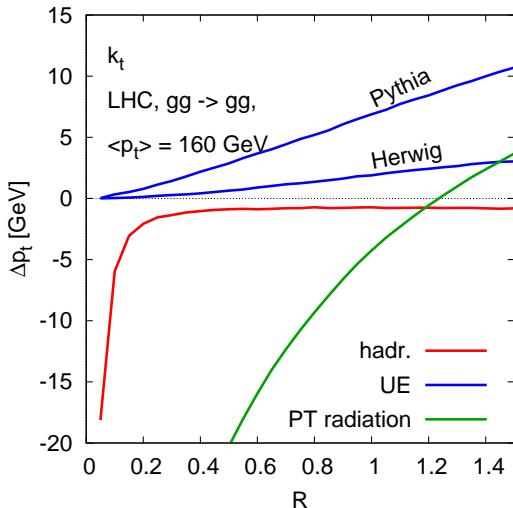
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$$q : \quad \langle \Delta p_t \rangle \simeq -\frac{C_F}{R} \cdot 0.4 \text{ GeV}$$

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### Underlying event:

$$q, g : \quad \langle \Delta p_t \rangle \simeq \frac{R^2}{2} \cdot 2.5 - 15 \text{ GeV}$$



Dasgupta, Magnea & GPS '07

Best jet quality  $\Leftrightarrow$  least dispersion between “parton”  $p_t$  and jet  $p_t$ .

NB: “parton” not well-defined

### Simplifying assumption:

$$\langle \Delta p_t^2 \rangle \simeq \langle \Delta p_t \rangle^2$$

$\langle \Delta p_t \rangle^2$  from perturbative, hadronisation and UE effects

- ▶ low- $p_t$  jet  $\rightarrow$  prefer small  $R$   
UE matters a lot
- ▶ high- $p_t$  jet  $\rightarrow$  prefer large  $R$   
pert matters most

Best jet quality  $\Leftrightarrow$  least dispersion between “parton”  $p_t$  and jet  $p_t$ .

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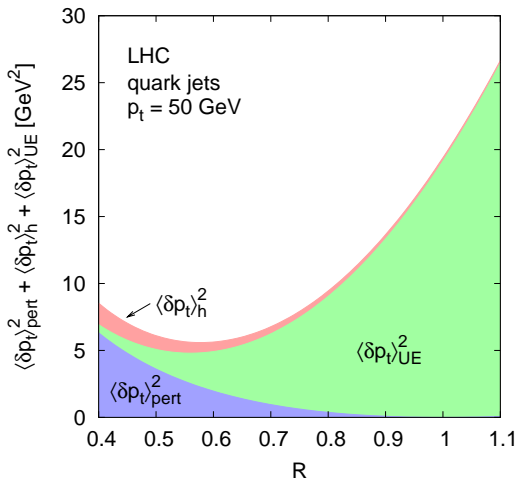
**Simplifying assumption:**

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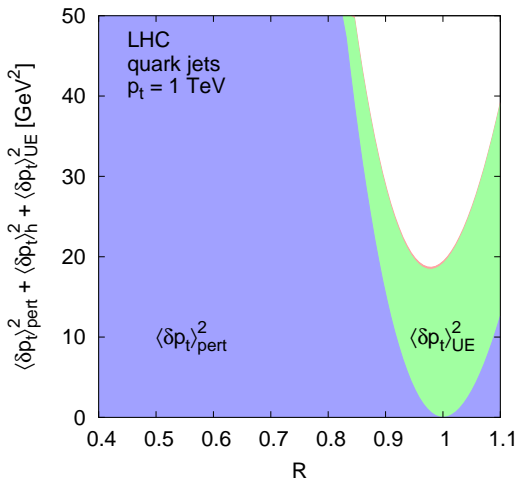
NB: “parton” not well-defined

**Simplifying assumption:**

$$\langle \Delta p_t^2 \rangle \simeq \langle \Delta p_t \rangle^2$$

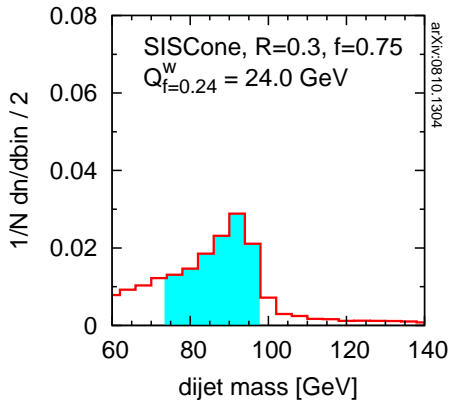
$\langle \Delta p_t \rangle^2$  from perturbative, hadronisation and UE effects

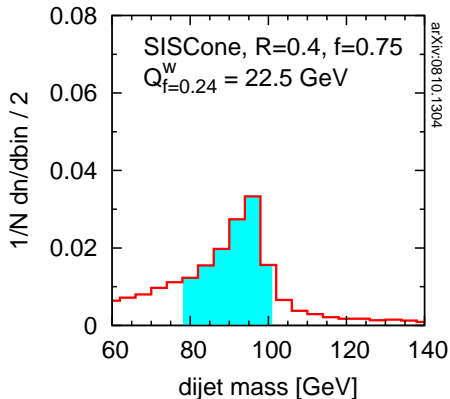
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- ▶ high- $p_t$  jet  $\rightarrow$  prefer large  $R$   
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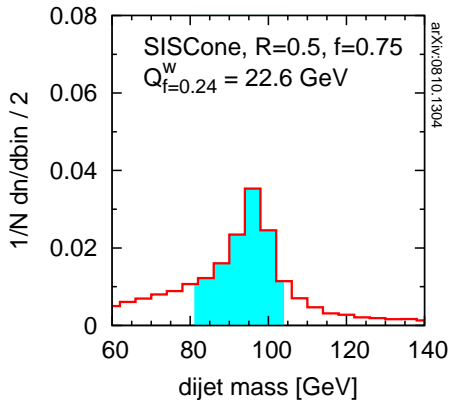


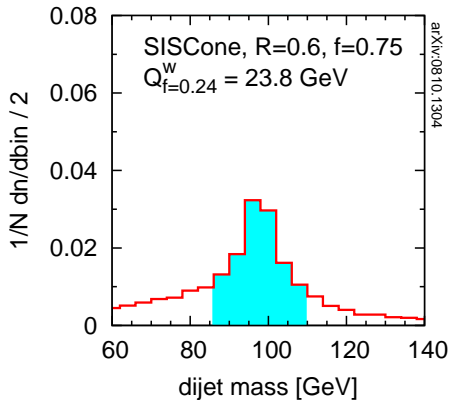
Does this match what one sees in  
Monte Carlo simulation?

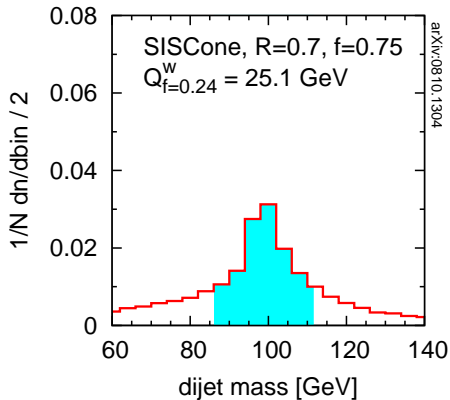


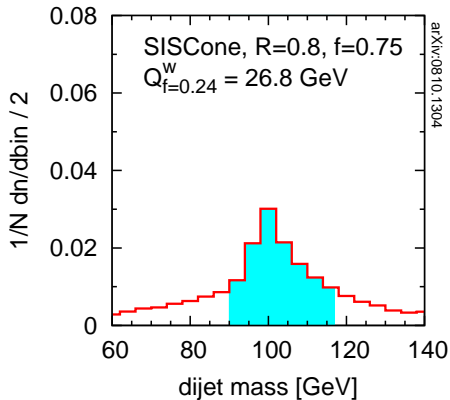
**$R = 0.3$** qq,  $M = 100$  GeV

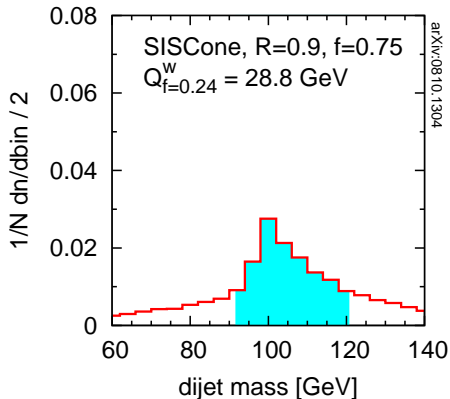
$R = 0.4$ qq,  $M = 100$  GeV

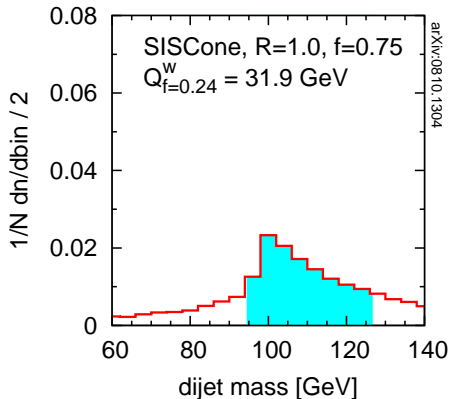
**$R = 0.5$** qq,  $M = 100$  GeV

**$R = 0.6$** qq,  $M = 100$  GeV

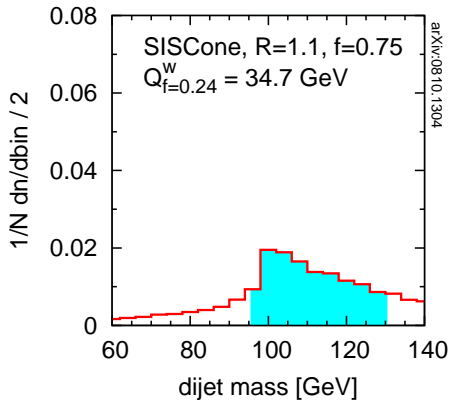
**$R = 0.7$** qq,  $M = 100$  GeV

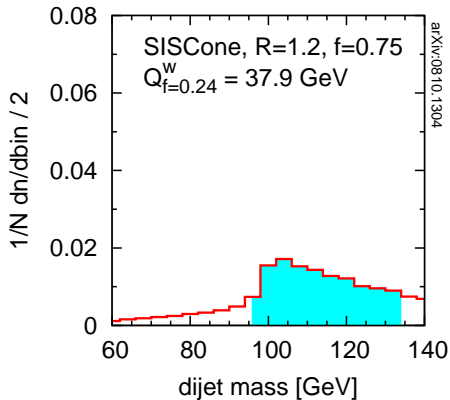
**$R = 0.8$** qq,  $M = 100$  GeV

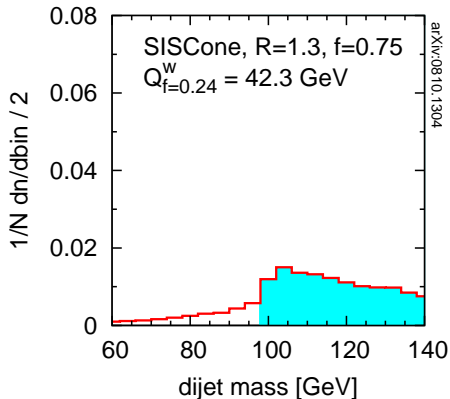
$R = 0.9$ qq,  $M = 100$  GeV

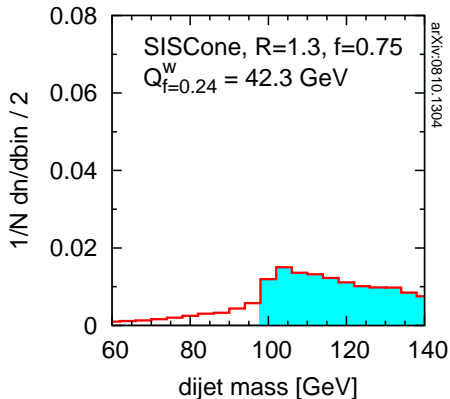
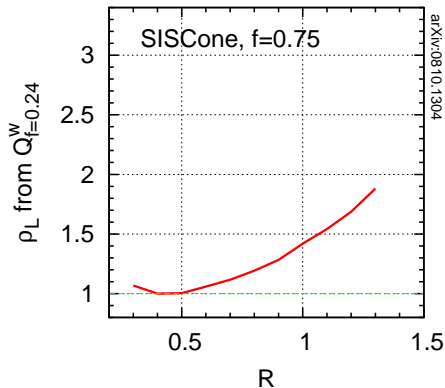
**$R = 1.0$** qq,  $M = 100$  GeV



$R = 1.1$ qq,  $M = 100$  GeV

$R = 1.2$ qq,  $M = 100$  GeV

**$R = 1.3$** qq,  $M = 100$  GeV

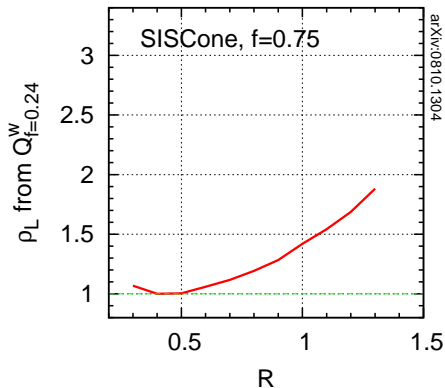
**$R = 1.3$** qq,  $M = 100$  GeVqq,  $M = 100$  GeV

**After scanning, summarise “quality” v.  $R$ . Minimum  $\equiv$  BEST**  
 picture not so different from crude analytical estimate

Scan through  $qq$  mass values

$$m_{qq} = 100 \text{ GeV}$$

$$qq, M = 100 \text{ GeV}$$



Best  $R$  is at minimum of curve

- ▶ Best  $R$  depends strongly on mass of system
- ▶ Increases with mass, just like crude analytical prediction
- NB: current analytics too crude

BUT: so far, LHC's plans involve running with fixed smallish  $R$  values

e.g. CMS arXiv:0807.4961

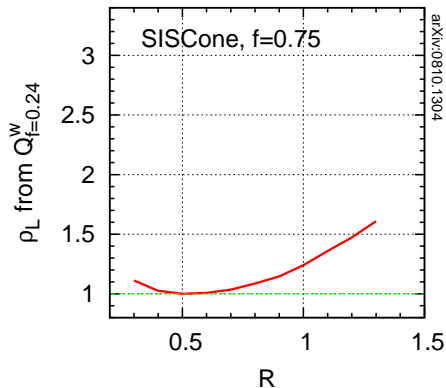
NB: 100,000 plots for various jet algorithms, narrow  $qq$  and  $gg$  resonances from <http://quality.fastjet.fr>

Cacciari, Rojo, GPS & Soyez '08

Scan through  $qq$  mass values

$$m_{qq} = 150 \text{ GeV}$$

$$qq, M = 150 \text{ GeV}$$



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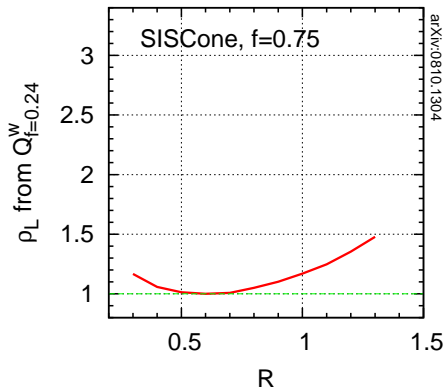
NB: 100,000 plots for various jet algorithms, narrow  $qq$  and  $gg$  resonances from <http://quality.fastjet.fr>

Cacciari, Rojo, GPS & Soyez '08

Scan through  $qq$  mass values

$$m_{qq} = 200 \text{ GeV}$$

$$qq, M = 200 \text{ GeV}$$



Best  $R$  is at minimum of curve

- Best  $R$  depends strongly on mass of system
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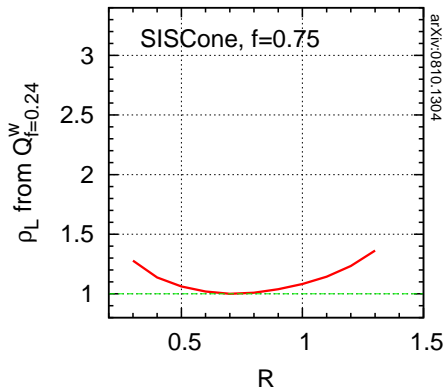
e.g. CMS arXiv:0807.4961

NB: 100,000 plots for various jet algorithms, narrow  $qq$  and  $gg$  resonances from <http://quality.fastjet.fr>

Cacciari, Rojo, GPS & Soyez '08

$$m_{qq} = 300 \text{ GeV}$$

$$qq, M = 300 \text{ GeV}$$



Best  $R$  is at minimum of curve

- ▶ Best  $R$  depends strongly on mass of system
- ▶ Increases with mass, just like crude analytical prediction
- NB: current analytics too crude

BUT: so far, LHC's plans involve running with fixed smallish  $R$  values

e.g. CMS arXiv:0807.4961

NB: 100,000 plots for various jet algorithms, narrow  $qq$  and  $gg$  resonances from <http://quality.fastjet.fr>

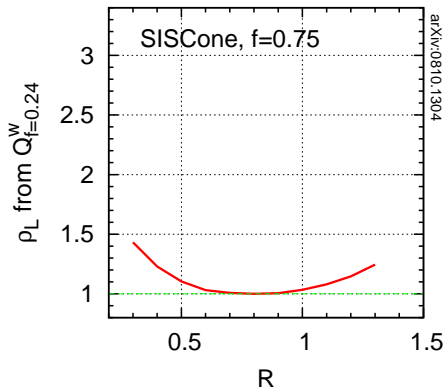
Cacciari, Rojo, GPS & Soyez '08



Scan through  $qq$  mass values

$$m_{qq} = 500 \text{ GeV}$$

$$qq, M = 500 \text{ GeV}$$



Best  $R$  is at minimum of curve

- Best  $R$  depends strongly on mass of system
- Increases with mass, just like crude analytical prediction
- NB: current analytics too crude

BUT: so far, LHC's plans involve running with fixed smallish  $R$  values

e.g. CMS arXiv:0807.4961

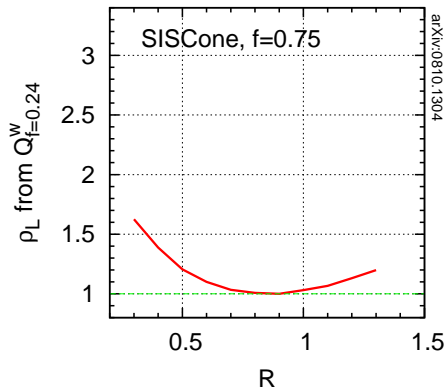
NB: 100,000 plots for various jet algorithms, narrow  $qq$  and  $gg$  resonances from <http://quality.fastjet.fr>

Cacciari, Rojo, GPS & Soyez '08

Scan through  $qq$  mass values

$$m_{qq} = 700 \text{ GeV}$$

$$qq, M = 700 \text{ GeV}$$



Best  $R$  is at minimum of curve

- ▶ Best  $R$  depends strongly on mass of system
- ▶ Increases with mass, just like crude analytical prediction
  - NB: current analytics too crude

BUT: so far, LHC's plans involve running with fixed smallish  $R$  values

e.g. CMS arXiv:0807.4961

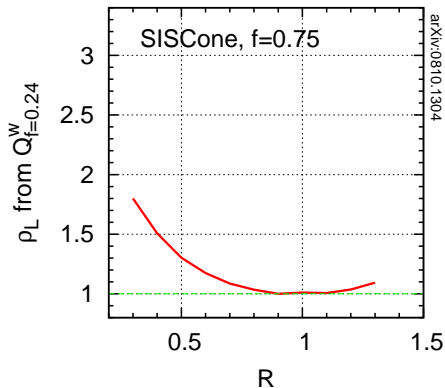
NB: 100,000 plots for various jet algorithms, narrow  $qq$  and  $gg$  resonances from <http://quality.fastjet.fr>

Cacciari, Rojo, GPS & Soyez '08

Scan through  $qq$  mass values

$$m_{qq} = 1000 \text{ GeV}$$

$$qq, M = 1000 \text{ GeV}$$



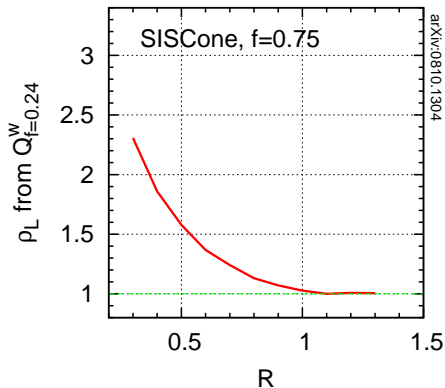
Best  $R$  is at minimum of curve

- ▶ Best  $R$  depends strongly on mass of system
- ▶ Increases with mass, just like crude analytical prediction
  - NB: current analytics too crude

**BUT:** so far, LHC's plans involve running with fixed smallish  $R$  values

e.g. CMS arXiv:0807.4961

NB: 100,000 plots for various jet algorithms, narrow  $qq$  and  $gg$  resonances from <http://quality.fastjet.fr> Cacciari, Rojo, GPS & Soyez '08

$m_{qq} = 2000 \text{ GeV}$  $qq, M = 2000 \text{ GeV}$ Best  $R$  is at minimum of curve

- ▶ Best  $R$  depends strongly on mass of system
- ▶ Increases with mass, just like crude analytical prediction
  - NB: current analytics too crude

**BUT:** so far, LHC's plans involve running with fixed smallish  $R$  values

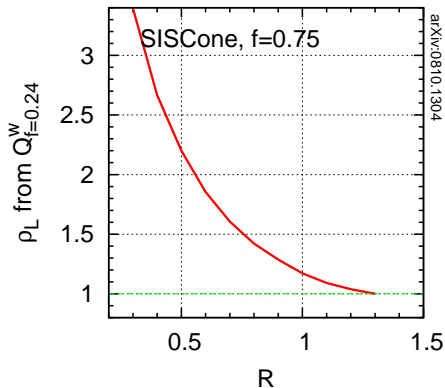
e.g. CMS arXiv:0807.4961

NB: 100,000 plots for various jet algorithms, narrow  $qq$  and  $gg$  resonances from <http://quality.fastjet.fr> Cacciari, Rojo, GPS & Soyez '08

Scan through  $qq$  mass values

$$m_{qq} = 4000 \text{ GeV}$$

$$qq, M = 4000 \text{ GeV}$$



Best  $R$  is at minimum of curve

- ▶ Best  $R$  depends strongly on mass of system
- ▶ Increases with mass, just like crude analytical prediction

NB: current analytics too crude

**BUT:** so far, LHC's plans involve running with fixed smallish  $R$  values

e.g. CMS arXiv:0807.4961

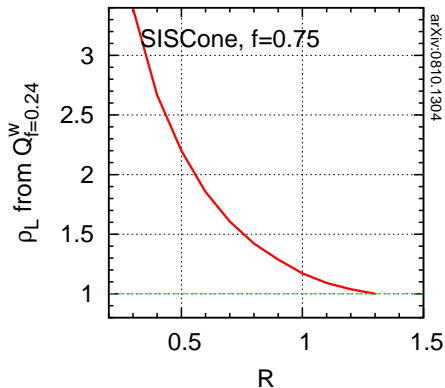
NB: 100,000 plots for various jet algorithms, narrow  $qq$  and  $gg$  resonances from <http://quality.fastjet.fr>

Cacciari, Rojo, GPS & Soyez '08

Scan through  $qq$  mass values

$$m_{qq} = 4000 \text{ GeV}$$

$$qq, M = 4000 \text{ GeV}$$



Best  $R$  is at minimum of curve

- ▶ Best  $R$  depends strongly on mass of system
- ▶ Increases with mass, just like crude analytical prediction

NB: current analytics too crude

**BUT: so far, LHC's plans involve running with fixed smallish  $R$  values**

e.g. CMS arXiv:0807.4961

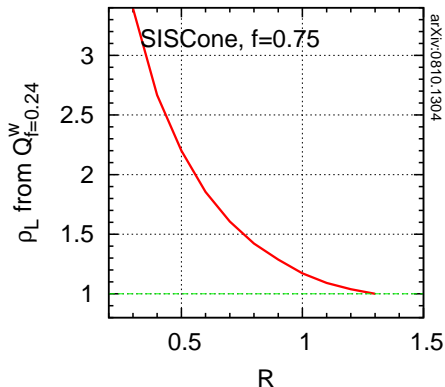
NB: 100,000 plots for various jet algorithms, narrow  $qq$  and  $gg$  resonances from <http://quality.fastjet.fr>

Cacciari, Rojo, GPS & Soyez '08

Scan through  $qq$  mass values

$$m_{qq} = 4000 \text{ GeV}$$

$$qq, M = 4000 \text{ GeV}$$



Best  $R$  is at minimum of curve

- ▶ Best  $R$  depends strongly on mass of system
- ▶ Increases with mass, just like crude analytical prediction

NB: current analytics too crude

**BUT: so far, LHC's plans involve running with fixed smallish  $R$  values**

e.g. CMS arXiv:0807.4961

NB: 100,000 plots for various jet algorithms, narrow  $qq$  and  $gg$  resonances from <http://quality.fastjet.fr>

Cacciari, Rojo, GPS & Soyez '08

## 1) 'Best' jet definition depends strongly on context

## 2) Key element is interplay between

- ▶ Loss of perturbative radiation from partons
- ▶ "Noise" contamination from underlying event (and pileup)

## 3) We've not discussed choice of jet algorithm

- ▶ But it's relevant too

Relates to "jet areas"  
= analytic study of UE contamination  
also being looked at by H1



Question #5:

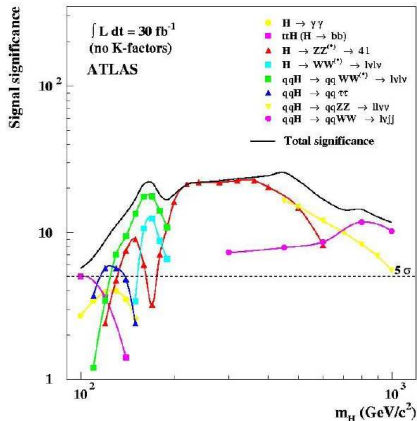
Can we apply understanding  
somewhere new?

An example: light Higgs search

As example, a Higgs-boson search illustrates two things:

- ▶ Using LHC scale hierarchy  $\sqrt{s} \gg M_{EW}$  to our advantage
- ▶ Using QCD to help us extract cleaner signals

taken from Butterworth, Davison, Rubin & GPS '08



## Low-mass Higgs search @ LHC:

complex because dominant decay channel,  $H \rightarrow bb$ , often swamped by backgrounds.

Various production processes

- ▶  $gg \rightarrow H (\rightarrow \gamma\gamma)$  feasible
- ▶  $WW \rightarrow H \rightarrow \dots$  feasible
- ▶  $gg \rightarrow t\bar{t}H$  v. hard
- ▶  $q\bar{q} \rightarrow WH, ZH$

small; but gives access to

$WH$  and  $ZH$  couplings

Currently considered impossible

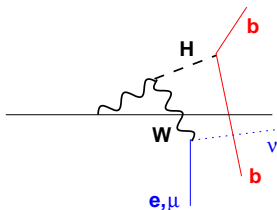
## WH/ZH search channel @ LHC

- ▶ Signal is  $W \rightarrow \ell\nu$ ,  $H \rightarrow b\bar{b}$ .
- ▶ Backgrounds include  $Wb\bar{b}$ ,  $t\bar{t} \rightarrow \ell\nu b\bar{b}jj$ , ...

Studied e.g. in ATLAS TDR

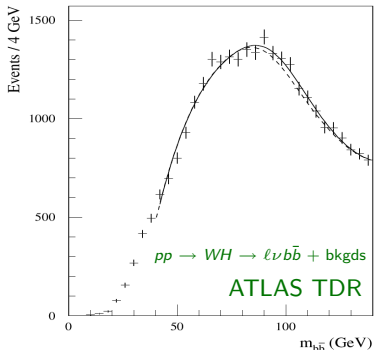
Difficulties, e.g.

- ▶ Poor acceptance ( $\sim 12\%$ )  
Easily lose 1 of 4 decay products
- ▶  $p_t$  cuts introduce intrinsic bkgd mass scale;
- ▶  $gg \rightarrow t\bar{t} \rightarrow \ell\nu b\bar{b}[jj]$  has similar scale
- ▶ small S/B
- ▶ Need exquisite control of bkgd shape



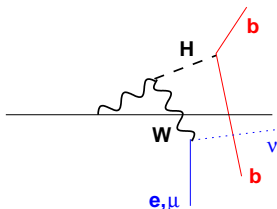
- ▶ Signal is  $W \rightarrow \ell\nu$ ,  $H \rightarrow b\bar{b}$ .
- ▶ Backgrounds include  $Wb\bar{b}$ ,  $t\bar{t} \rightarrow \ell\nu b\bar{b}jj$ , ...

Studied e.g. in ATLAS TDR



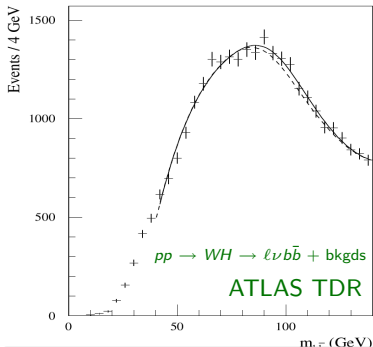
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- ▶ small S/B
- ▶ Need exquisite control of bkgd shape



- ▶ Signal is  $W \rightarrow \ell\nu, H \rightarrow b\bar{b}$ .
- ▶ Backgrounds include  $Wb\bar{b}, t\bar{t} \rightarrow \ell\nu b\bar{b}jj, \dots$

Studied e.g. in ATLAS TDR

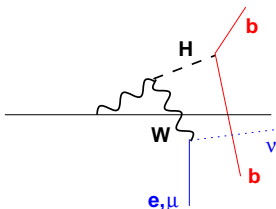


## Difficulties, e.g.

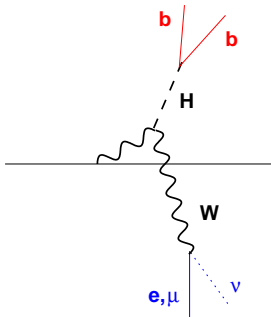
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- ▶  $p_t$  cuts introduce intrinsic bkgd mass scale;
- ▶  $gg \rightarrow t\bar{t} \rightarrow \ell\nu b\bar{b}[jj]$  has similar scale
- ▶ small S/B
- ▶ Need exquisite control of bkgd shape

## Conclusion (ATLAS TDR):

*“The extraction of a signal from  $H \rightarrow b\bar{b}$  decays in the WH channel will be very difficult at the LHC, even under the most optimistic assumptions [...]”*



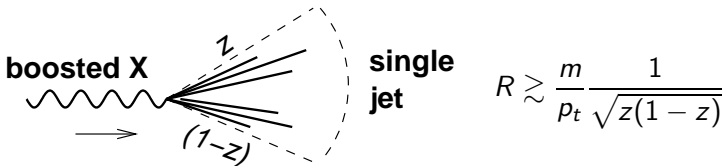
Take advantage of the fact that  $\sqrt{s} \gg M_H, m_t, \dots$



Go to high  $p_t$ :

- ✓ Higgs and W/Z more likely to be central
- ✓ high- $p_t$   $Z \rightarrow \nu\bar{\nu}$  becomes visible
- ✓ Fairly collimated decays: high- $p_t$   $\ell^\pm, \nu, b$   
Good detector acceptance
- ✓ Backgrounds lose cut-induced scale
- ✓  $t\bar{t}$  kinematics cannot simulate bkgd  
Gain clarity and S/B
- ✗ Cross section will drop dramatically  
By a factor of 20 for  $p_{tH} > 200$  GeV  
**Will the benefits outweigh this?**

## Hadronically decaying Higgs boson at high $p_t =$ single massive jet?

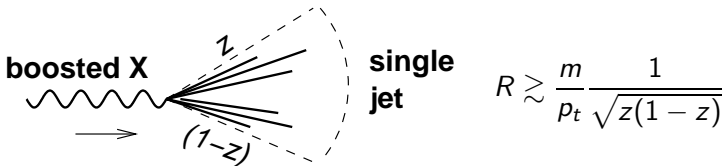


discussion of this & related problems: Seymour '93; Butterworth, Cox & Forshaw '02; Butterworth, Ellis & Raklev '07; Skiba & Tucker-Smith '07; Holdom '07; Baur '07; Agashe et al. '07; Lillie, Randall & Wang '07; Contino & Servant '08; Brooijmans '08; Thaler & Wang '08; Kaplan et al '08; Almeida et al '08; [...]

What does QCD tell us about how to deal with this?

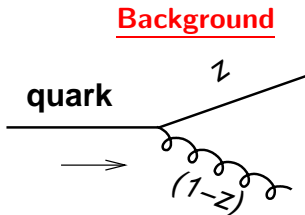
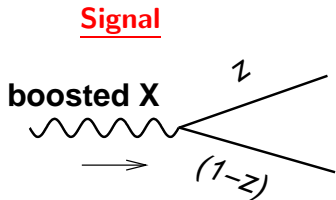


## Hadronically decaying Higgs boson at high $p_t =$ single massive jet?



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What does QCD tell us about how to deal with this?



Splitting probability for Higgs:

$$P(z) \propto 1$$

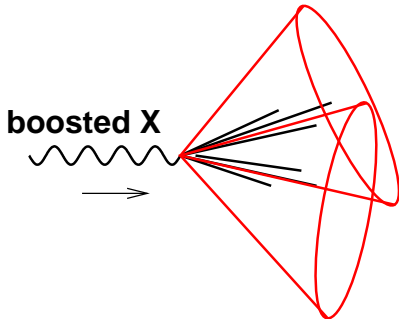
Splitting probability for quark:

$$P(z) \propto \frac{1+z^2}{1-z}$$

$1/(1-z)$  divergence enhances background

Remove divergence in bkdg with cut on  $z$   
Can choose cut analytically so as to maximise  $S/\sqrt{B}$

Originally: ad-hoc cut on (related)  $k_t$ -distance  
Seymour '93; Butterworth, Cox & Forshaw '02



Given a color-singlet  $q\bar{q}$  pair of opening angle  $R_{bb}$ :

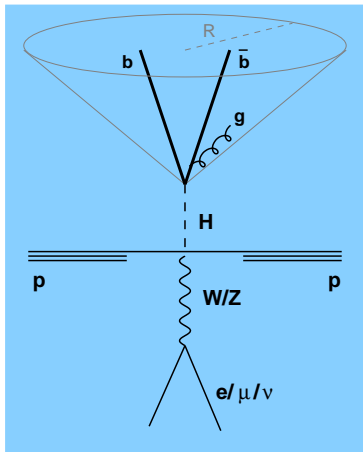
*Nearly all the radiation from the pair is contained in two cones of opening angle  $R_{bb}$ , one centred on each quark.*

Standard result also in QED

Use this to capture just the radiation from the  $q\bar{q} \Rightarrow$  good mass resol<sup>n</sup>

High- $p_t$  light Higgs decays to  $b\bar{b}$  inside a single jet. Can this be seen?

Butterworth, Davison, Rubin & GPS '08



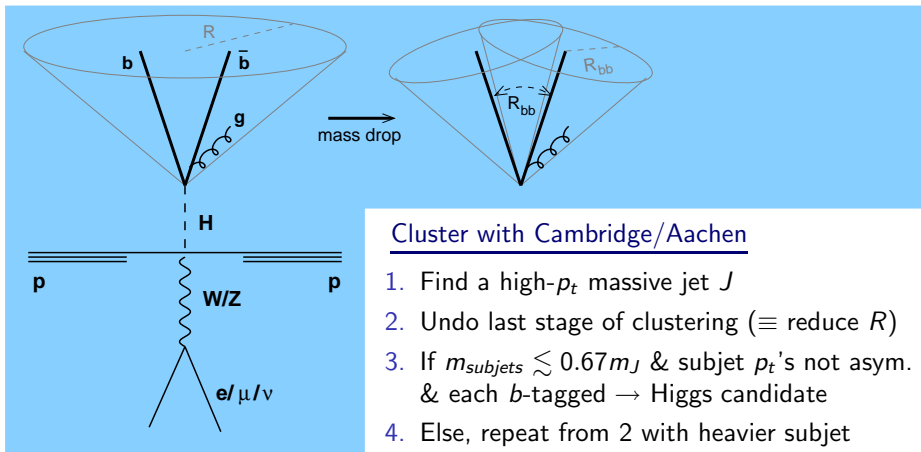
## Cluster with Cambridge/Aachen

1. Find a high- $p_t$  massive jet  $J$
2. Undo last stage of clustering ( $\equiv$  reduce  $R$ )
3. If  $m_{\text{subjects}} \lesssim 0.67m_J$  & subjet  $p_t$ 's not asym. & each  $b$ -tagged  $\rightarrow$  Higgs candidate
4. Else, repeat from 2 with heavier subjet

Then on the Higgs-candidate: *filter* away UE/pileup by reducing  $R \rightarrow R_{\text{filt}}$ , take *three hardest subjects* (keep LO gluon rad<sup>n</sup>) + require  $b$ -tags on two hardest.

High- $p_t$  light Higgs decays to  $b\bar{b}$  inside a single jet. Can this be seen?

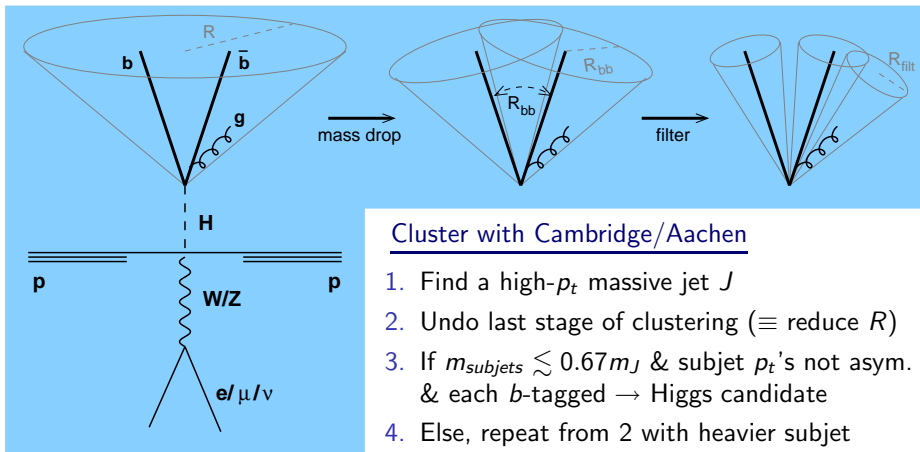
Butterworth, Davison, Rubin & GPS '08



Then on the Higgs-candidate: *filter* away UE/pileup by reducing  $R \rightarrow R_{\text{filt}}$ , take *three hardest subjets* (keep LO gluon rad<sup>n</sup>) + require  $b$ -tags on two hardest.

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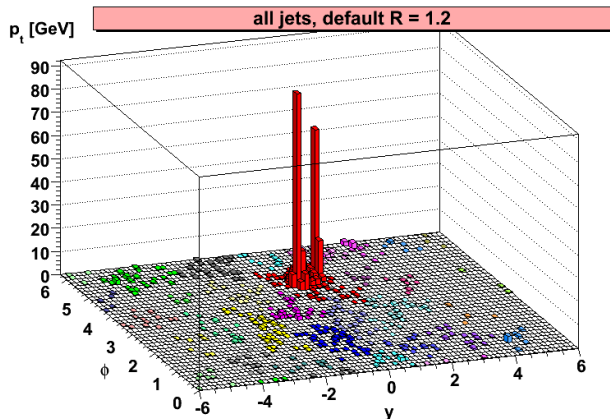
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Then on the Higgs-candidate: *filter* away UE/pileup by reducing  $R \rightarrow R_{filt}$ , take *three hardest subjects* (keep LO gluon rad<sup>n</sup>) + require  $b$ -tags on two hardest.

SIGNAL

Herwig 6.510 + Jimmy 4.31 + FastJet 2.3



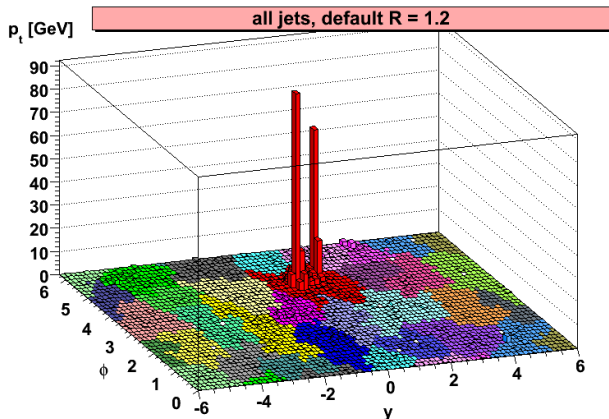
Zbb BACKGROUND

Cluster event, C/A, R=1.2

arbitrary norm.

SIGNAL

Herwig 6.510 + Jimmy 4.31 + FastJet 2.3



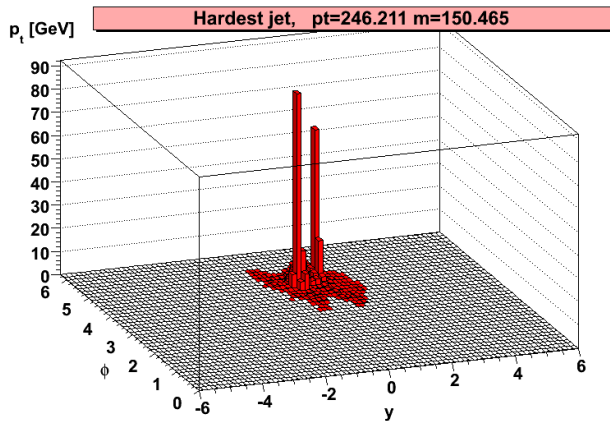
Zbb BACKGROUND

Fill it in,  $\rightarrow$  show jets more clearly

arbitrary norm.



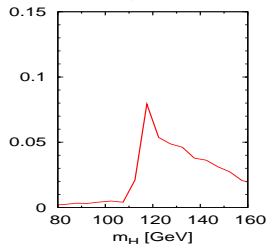
Herwig 6.510 + Jimmy 4.31 + FastJet 2.3



Consider hardest jet,  $m = 150$  GeV

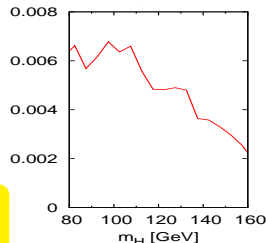
SIGNAL

$200 < p_{tZ} < 250$  GeV



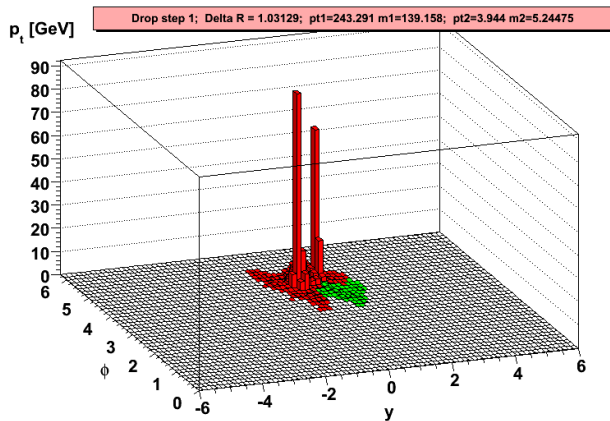
Zbb BACKGROUND

$200 < p_{tZ} < 250$  GeV



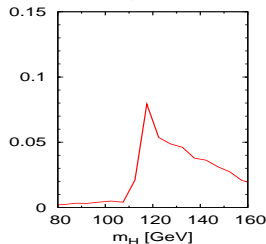
arbitrary norm.

Herwig 6.510 + Jimmy 4.31 + FastJet 2.3



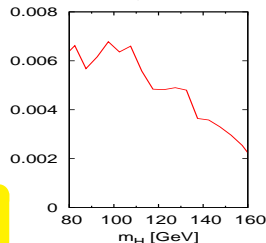
### SIGNAL

$200 < p_{tZ} < 250$  GeV



### Zbb BACKGROUND

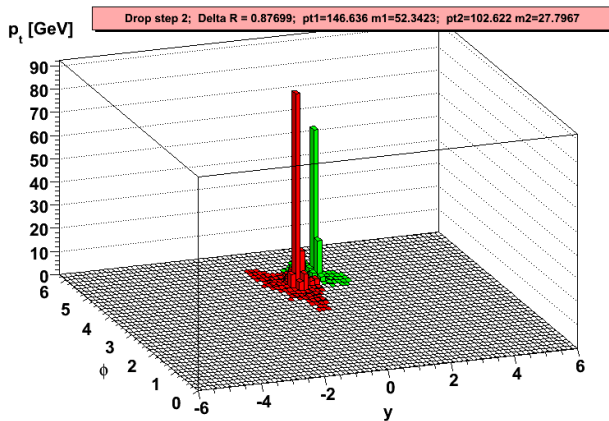
$200 < p_{tZ} < 250$  GeV



split:  $m = 150$  GeV,  $\frac{\max(m_1, m_2)}{m} = 0.92 \rightarrow$  repeat

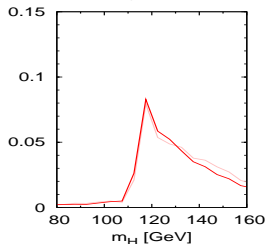
arbitrary norm.

Herwig 6.510 + Jimmy 4.31 + FastJet 2.3



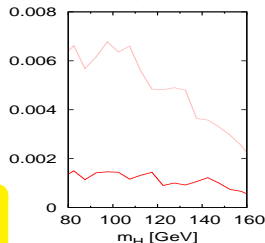
SIGNAL

$200 < p_{tZ} < 250$  GeV



Zbb BACKGROUND

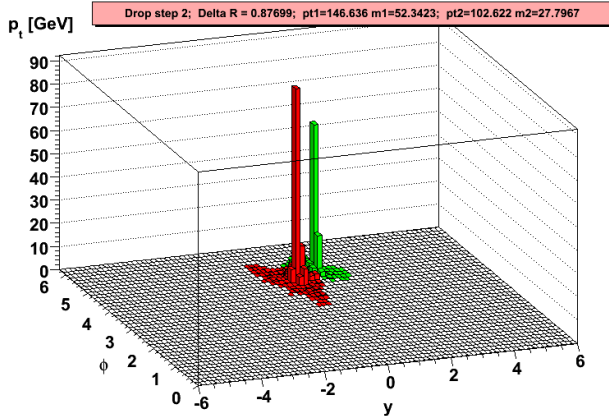
$200 < p_{tZ} < 250$  GeV



split:  $m = 139$  GeV,  $\frac{\max(m_1, m_2)}{m} = 0.37 \rightarrow$  mass drop

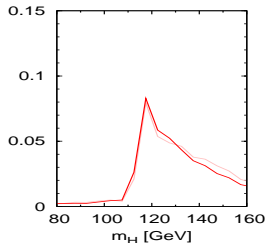
arbitrary norm.

Herwig 6.510 + Jimmy 4.31 + FastJet 2.3



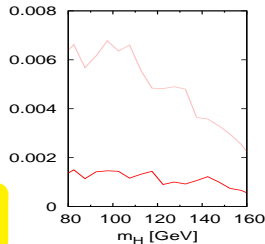
### SIGNAL

$200 < p_{tZ} < 250$  GeV



### Zbb BACKGROUND

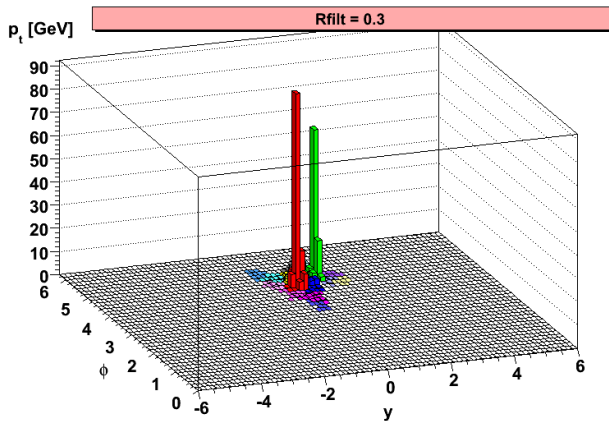
$200 < p_{tZ} < 250$  GeV



check:  $y_{12} \simeq \frac{p_{t2}}{p_{t1}} \simeq 0.7 \rightarrow \text{OK} + 2 \text{ } b\text{-tags (anti-QCD)}$

arbitrary norm.

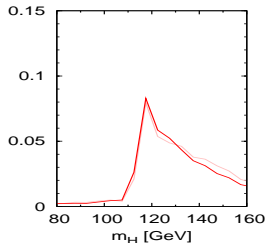
Herwig 6.510 + Jimmy 4.31 + FastJet 2.3



$R_{filt} = 0.3$

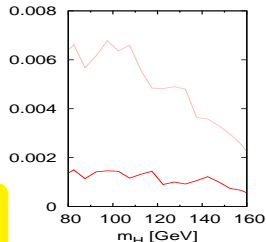
SIGNAL

$200 < p_{tZ} < 250$  GeV



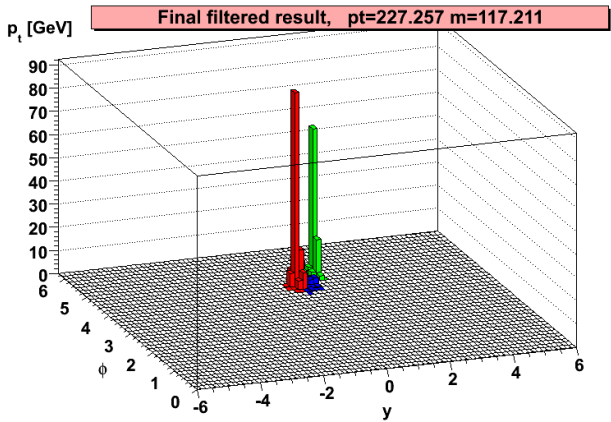
Zbb BACKGROUND

$200 < p_{tZ} < 250$  GeV



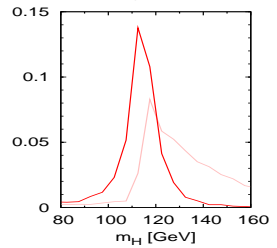
arbitrary norm.

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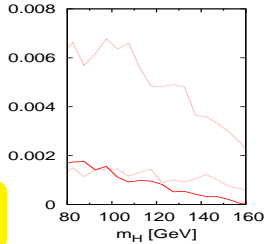
SIGNAL

$200 < p_{tZ} < 250$  GeV



Zbb BACKGROUND

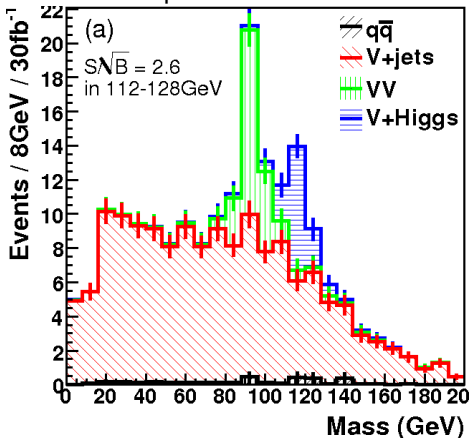
$200 < p_{tZ} < 250$  GeV



$R_{filt} = 0.3$ : take 3 hardest,  $m = 117$  GeV

arbitrary norm.

### Leptonic channel



### Common cuts

- ▶  $p_{tV}, p_{tH} > 200$  GeV
- ▶  $|\eta_H| < 2.5$
- ▶  $[p_{t,\ell} > 30$  GeV,  $|\eta_\ell| < 2.5]$
- ▶ No extra  $\ell$ ,  $b$ 's with  $|\eta| < 2.5$
- ▶ Real/fake  $b$ -tag rates: 0.7/0.01
- ▶  $S/\sqrt{B}$  from 16 GeV window

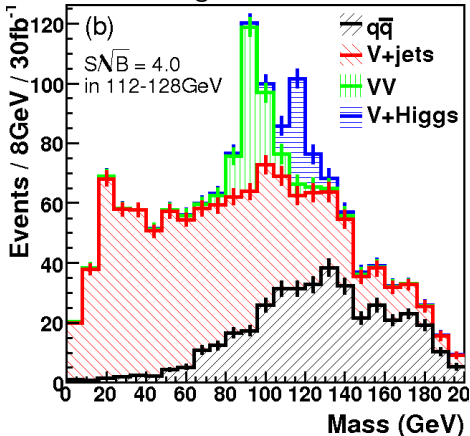
### Leptonic channel

$$Z \rightarrow \mu^+\mu^-, e^+e^-$$

- ▶  $80 < m_{\ell\ell} < 100$  GeV

At  $5.9\sigma$  for  $30 \text{ fb}^{-1}$  this looks like a possible new channel for light Higgs discovery. *Deserves serious exp. study!*

Missing  $E_T$  channel



Common cuts

- ▶  $p_{tV}, p_{tH} > 200$  GeV
- ▶  $|\eta_H| < 2.5$
- ▶  $[p_{t,\ell} > 30$  GeV,  $|\eta_\ell| < 2.5]$
- ▶ No extra  $\ell$ ,  $b$ 's with  $|\eta| < 2.5$
- ▶ Real/fake  $b$ -tag rates: 0.7/0.01
- ▶  $S/\sqrt{B}$  from 16 GeV window

Missing- $E_t$  channel

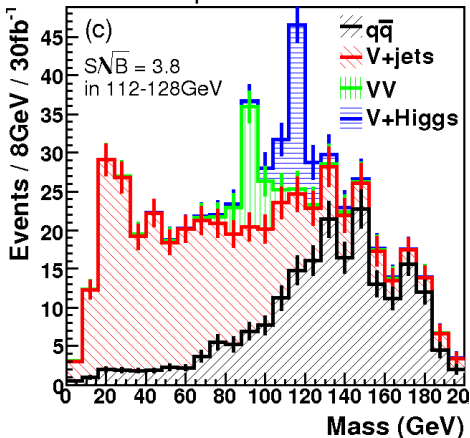
$$Z \rightarrow \nu\bar{\nu}, W \rightarrow \nu[\ell]$$

- ▶  $\cancel{E}_T > 200$  GeV

At  $5.9\sigma$  for  $30 \text{ fb}^{-1}$  this looks like a possible new channel for light Higgs discovery. **Deserves serious exp. study!**



### Semi-leptonic channel



### Common cuts

- ▶  $p_{tV}, p_{tH} > 200$  GeV
- ▶  $|\eta_H| < 2.5$
- ▶  $[p_{t,\ell} > 30$  GeV,  $|\eta_\ell| < 2.5]$
- ▶ No extra  $\ell$ ,  $b$ 's with  $|\eta| < 2.5$
- ▶ Real/fake  $b$ -tag rates: 0.7/0.01
- ▶  $S/\sqrt{B}$  from 16 GeV window

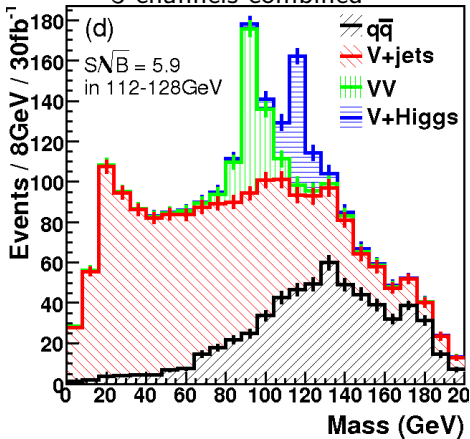
### Semi-leptonic channel

$W \rightarrow \nu\ell$

- ▶  $\cancel{E}_T > 30$  GeV (& consistent  $W$ .)
- ▶ no extra jets  $|\eta| < 3, p_t > 30$

At  $5.9\sigma$  for  $30 \text{ fb}^{-1}$  this looks like a possible new channel for light Higgs discovery. **Deserves serious exp. study!**

3 channels combined



Common cuts

- ▶  $p_{tV}, p_{tH} > 200$  GeV
- ▶  $|\eta_H| < 2.5$
- ▶  $[p_{t,\ell} > 30$  GeV,  $|\eta_\ell| < 2.5]$
- ▶ No extra  $\ell$ ,  $b$ 's with  $|\eta| < 2.5$
- ▶ Real/fake  $b$ -tag rates: 0.7/0.01
- ▶  $S/\sqrt{B}$  from 16 GeV window

3 channels combined

Note excellent  $VZ$ ,  $Z \rightarrow b\bar{b}$   
 peak for calibration  
 NB:  $q\bar{q}$  is mostly  $t\bar{t}$

At  $5.9\sigma$  for  $30 \text{ fb}^{-1}$  this looks like a possible new channel for light Higgs discovery. **Deserves serious exp. study!**

## Not just about Higgs discovery

Higgs physics means establishing whether it has the expected SM couplings.

Crucial part of that is seeing WH and ZH cleanly and separately from each other.

This channel seems to be the only good way of doing that for a light Higgs.

Alternative  $WW$  fusion: but mixes with  $ZZ$  fusion,  $gg$  fusion

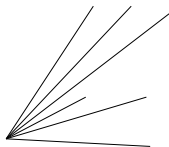
# Outlook

- ▶ There seem to be clear benefits to be had from well-chosen jet-definitions
- ▶ No single jet-definition fits all physics tasks
- ▶ Unlike photography we don't yet have "autofocus, auto-exposure" jet finders
- ▶ But we're starting to understand the issues
  - Enough to qualitatively guide our choices
  - e.g. choice of  $R$  in dijet resonance searches
  - e.g. boosted EW bosons, cf. low-mass Higgs search
- ▶ What's the next goal? **Systematic, optimised jetography?**

# Extras

$k_t$  algorithm

- ▶ Find smallest of all  $d_{ij} = \min(k_{ti}^2, k_{tj}^2) \Delta R_{ij}^2 / R^2$  and  $d_{iB} = k_i^2$
- ▶ Recombine  $i, j$  (if  $iB$ :  $i \rightarrow \text{jet}$ )
- ▶ Repeat



'Trivial' computational issue:

- ▶ for  $N$  particles:  $N^2$   $d_{ij}$  searched through  $N$  times =  $N^3$
- ▶ 4000 particles (or calo cells): 1 minute  
NB: often study  $10^7 - 10^8$  events

Advance #1: factorise momentum and geometry

Borrow methods & tools from Computational Geometry:

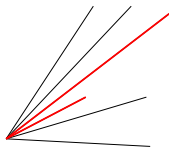
Bucketing, dynamic Voronoi diagrams, CGAL, Chan CP

Time reduced to  $Nn$  or  $N \ln N$ : 25ms for  $N=4000$ .

Cacciari & GPS '05

$k_t$  algorithm

- ▶ Find **smallest of all**  $d_{ij} = \min(k_{ti}^2, k_{tj}^2) \Delta R_{ij}^2 / R^2$  and  $d_{iB} = k_i^2$
- ▶ Recombine  $i, j$  (if  $iB$ :  $i \rightarrow \text{jet}$ )
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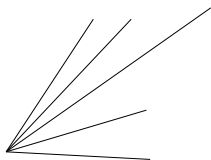
Time reduced to  $Nn$  or  $N \ln N$ : 25ms for  $N=4000$ .

Cacciari & GPS '05



$k_t$  algorithm

- ▶ Find smallest of all  $d_{ij} = \min(k_{ti}^2, k_{tj}^2) \Delta R_{ij}^2 / R^2$  and  $d_{iB} = k_i^2$
- ▶ **Recombine**  $i, j$  (if  $iB$ :  $i \rightarrow \text{jet}$ )
- ▶ Repeat



'Trivial' computational issue:

- ▶ for  $N$  particles:  $N^2$   $d_{ij}$  searched through  $N$  times =  $N^3$
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NB: often study  $10^7 - 10^8$  events

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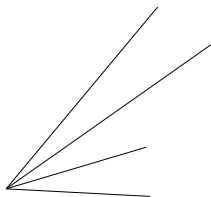
Bucketing, dynamic Voronoi diagrams, CGAL, Chan CP

Time reduced to  $Nn$  or  $N \ln N$ : 25ms for  $N=4000$ .

Cacciari & GPS '05

$k_t$  algorithm

- ▶ Find smallest of all  $d_{ij} = \min(k_{ti}^2, k_{tj}^2) \Delta R_{ij}^2 / R^2$  and  $d_{iB} = k_i^2$
- ▶ Recombine  $i, j$  (if  $iB$ :  $i \rightarrow \text{jet}$ )
- ▶ Repeat



'Trivial' computational issue:

- ▶ for  $N$  particles:  $N^2$   $d_{ij}$  searched through  $N$  times =  $N^3$
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NB: often study  $10^7 - 10^8$  events

Advance #1: factorise momentum and geometry

Borrow methods & tools from Computational Geometry:

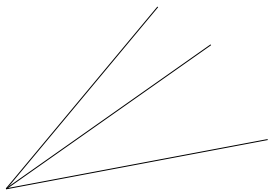
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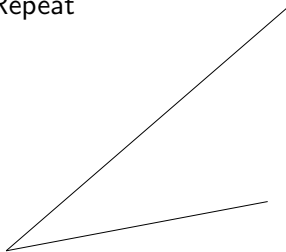
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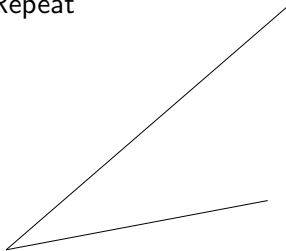
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Cacciari & GPS '05

# Sequential recombination algorithms

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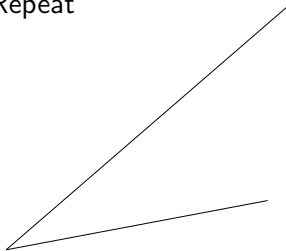
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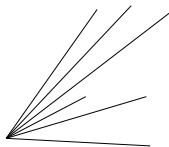
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Cacciari & GPS '05

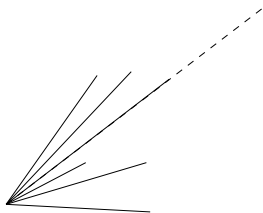
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- ▶ Find some/all stable cones  
≡ cone pointing in same direction as the momentum of its contents
- ▶ Resolve cases of overlapping stable cones  
By running a 'split-merge' procedure



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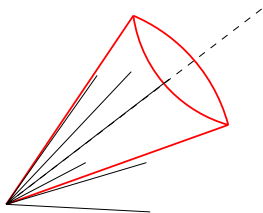
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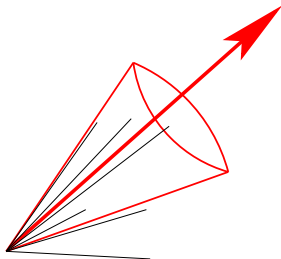
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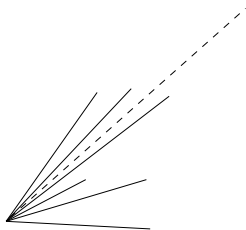
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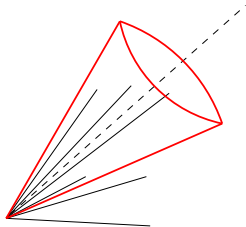
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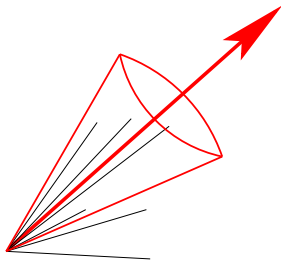
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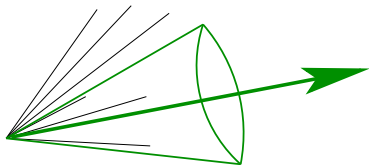
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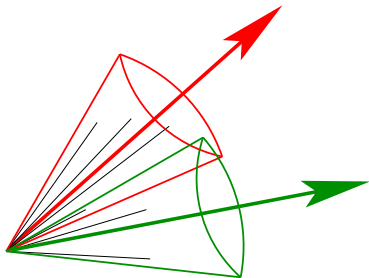
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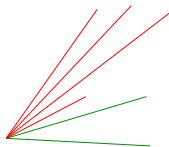
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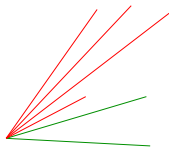


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## How do you find the stable cones?

- ▶ Iterate from 'seed' particles
  - Done originally, very IR unsafe,  $N^2$  [JetClu, Atlas]
- ▶ Iterate from 'midpoints' between cones from seeds
  - Midpoint cone, less IR unsafe,  $N^3$
- ▶ Seedless: try all subsets of particles IR safe,  $N2^N$ 
  - 100 particles:  $10^{17}$  years

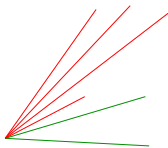


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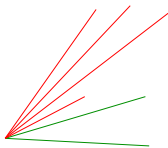


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**Advance #2: IR safe seedless cone (SM)** separate mom. and geometry

New comp. geometry techniques: 2D all distinct circular enclosures

Then for each check whether → stable cone

Time reduced from  $N^2$  to  $N^2 \ln N$ : 6s for  $N=4000$ .

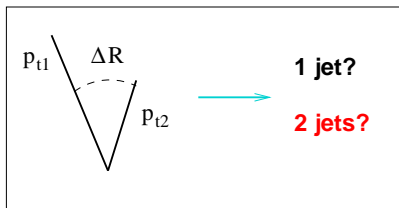
GPS & Soyez '07

**"SISCone"**

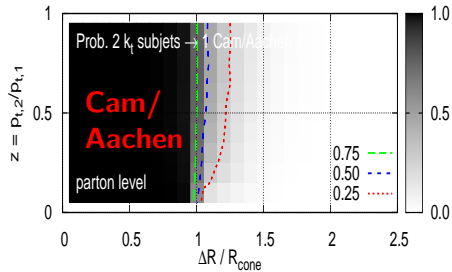
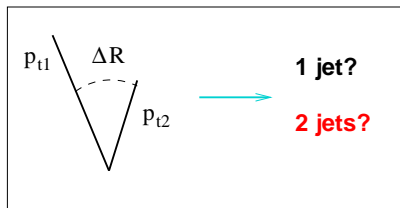
Question #4b:

What physics governs quality  
of jet definition?

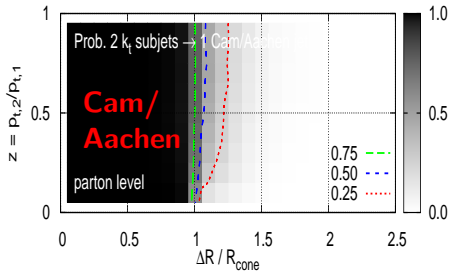
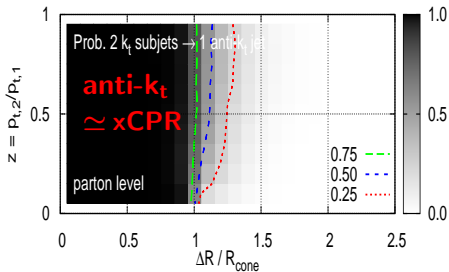
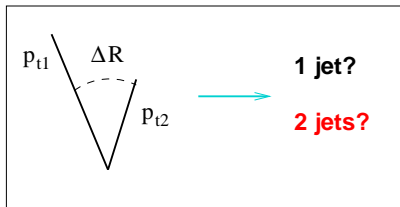
[jet algorithm dependence]



SISCone (xC-SM) reaches further for hard radiation than other algs

the *reach* of jet algorithms

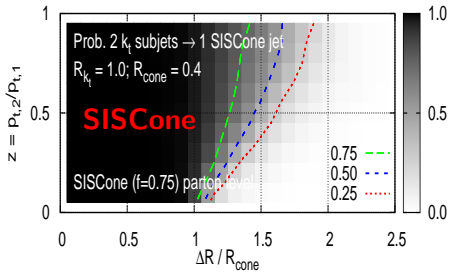
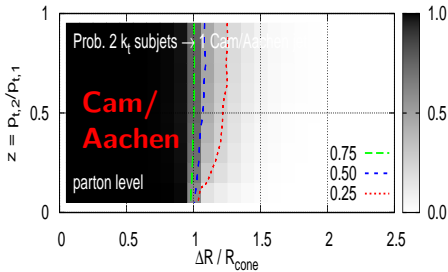
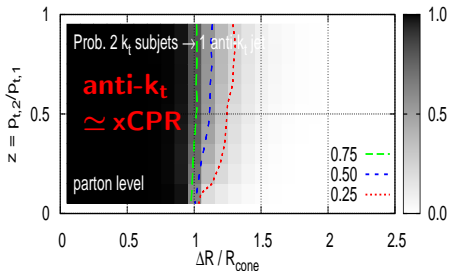
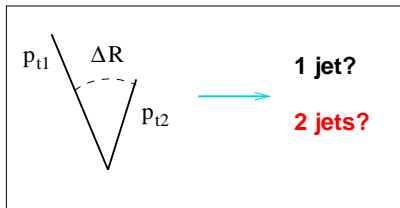
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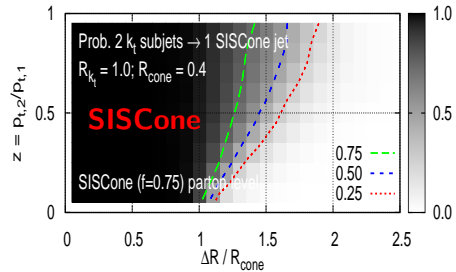
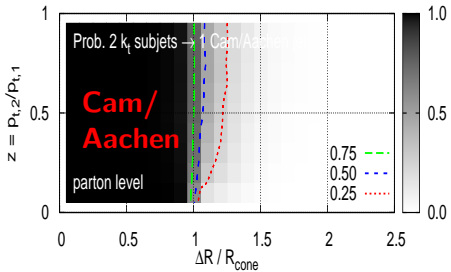
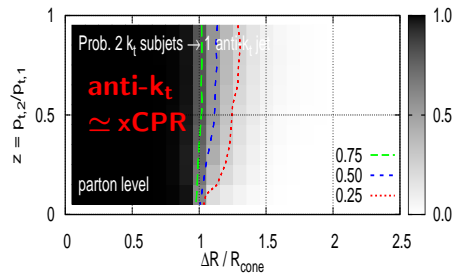
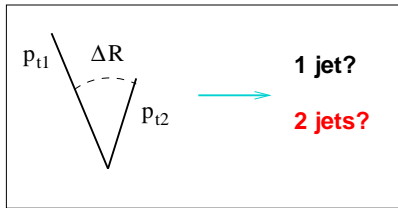


# the reach of jet algorithms



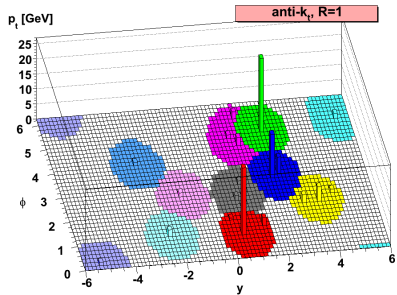
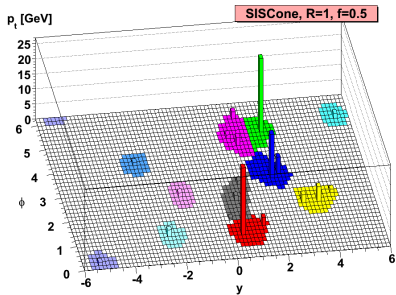
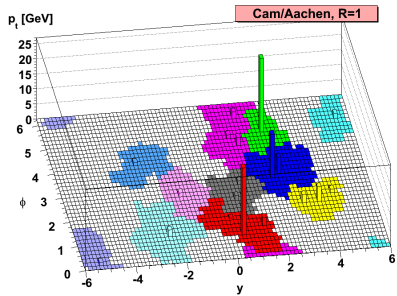
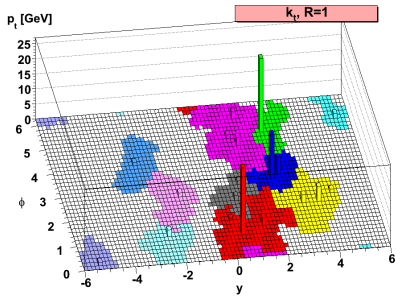
SISCone ( $\times \text{C-SM}$ ) reaches further for hard radiation than other algs

# the reach of jet algorithms



**SISCone (xC-SM) reaches further for hard radiation than other algs**

## Jet contours – visualised



Can show that jet area goes as:

$$A = A_0 + D \frac{C_{F/A}}{\pi b_0} \ln \frac{\alpha_s(Q_0)}{\alpha_s(Rp_t)} + \mathcal{O}(\alpha_s^2 \ln p_t^2)$$

Cacciari, GPS & Soyez '08  
 measurements in progress in H1

**Passive area:** suscept. to **point-like** radiation:

	$A_0/\pi R^2$	$D/\pi R^2$
$k_t$	1	0.56
Cam/Aachen	1	0.08
SISCone	1	-0.06

- ▶ Analytical calcs capture main MC features
- ▶  $k_t$  has larger area than cone, neither is  $\pi R^2$
- ▶ **SISCone has small areas**

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Cacciari, GPS & Soyez '08  
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**Active area:** suscept. to **diffuse** radiation:

	$A_0/\pi R^2$	$D/\pi R^2$
$k_t$	1 → 0.81	0.56 → 0.52
Cam/Aachen	1 → 0.81	0.08 → 0.08
SISCone	1 → 0.25	-0.06 → 0.12

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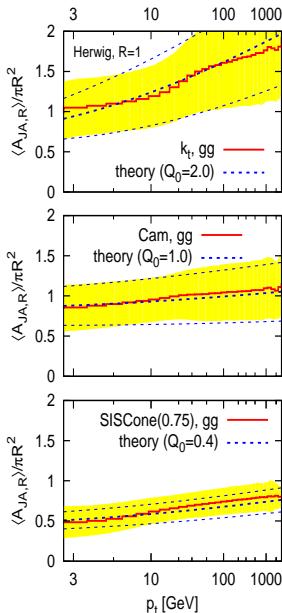
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**MISSING:**

**SISCone worked well because  
of small area and wider  
perturbative reach (NB latter  
good for dijets, bad for  
multijets)**