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Jets in QCD, an introduction

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Drawing on work with M. Cacciari, J. Rojo & G. Soyez

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Capacitation de Pales na Particion (nº 1024) Universitose de Cambros de Correctaie (Rowr) Jets are the most direct of all hard probes of the medium. As close as you can get to the original quark or gluon near its time of creation

What might you want to do with them?

cf. talks by Wiedemann, Arleo

Look back in time to before the parton traversed the medium And so get the parton's energy near start of fragmentation e.g. to normalise fragmentation functions

- Then scan forwards "time" to see what happened to it as it went through the medium
- And to identify "where its energy went"

<u>This talk</u>

- Some background about jets in usual collider contexts
- Some thoughts on jets in heavy-ion collisions

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Partons (quarks, gluons) are not trouble-free concepts...



- Partons split into further partons
- Jets are a a way of thinking of the 'original parton'
- A 'jet' is a fundamentally ambiguous concept (e.g. requires a resolution)

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A jet definition is a systematic procedure that **projects away the multiparticle dynamics**, so as to leave a simple picture of what happened in an event:



Jets are *as close as we can get to a physical single hard quark or gluon:* with good definitions their properties (multiplicity, energies, [flavour]) are

- finite at any order of perturbation theory
- \blacktriangleright insensitive to the parton \rightarrow hadron transition

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Two broad classes of jet algorithm

Sequential recombination (SR)	Cone
k_t , Jade, Cam/Aachen,	UA1, JetClu, Midpoint,
$\begin{array}{l} \mbox{Bottom-up:} \\ \mbox{Cluster 'closest' particles repeat-} \\ \mbox{edly until few left} \rightarrow \mbox{jets.} \end{array}$	Top-down: Find coarse regions of energy flow (cones), and call them jets.
Works because of mapping: <i>closeness</i> ⇔ <i>QCD divergence</i>	Works because <i>QCD only modifies</i> energy flow on small scales
Loved by e^+e^- , ep (& theorists)	Loved by <i>pp</i> (& fewer theorists)
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Driven by LHC's arrival [and Tevatron's mixed record]

- Let's see how each type works
- And what the issues & progress have been

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Sequential recombination (e.g. k_t) algorithms Catani et al '91-93, Ellis & Soper '93

> The favourite in e^+e^- and DIS Much loved by QCD theorists Long disfavoured in pp



Sequential recombination algorithms

k_t algorithm

- Find smallest of all $d_{ij} = \min(k_{ti}^2, k_{tj}^2) \Delta R_{ij}^2 / R^2$ and $d_{iB} = k_i^2$
- Recombine i, j (if $iB: i \rightarrow jet$)

Repeat



'Trivial' computational issue:

- ▶ for N particles: N² d_{ij} searched through N times = N³
- 4000 particles (or calo cells): 1 minute NB: often study 10⁷ - 10⁸ events



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An event clustered with k_t



Jets are irregular in shape

often quoted as a difficulty in experimental calibration \boldsymbol{X}

A consequence of hierarchical nature

Which gives window on substructure \checkmark

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CDF hep-ex/0512062 & hep-ex/0701051 inclusive-jet results show irregularity of k_t jets does not prevent a good measurement.

Jets, G. Salam (p. 9)

Algs & progress



This, and k_t 's theoretical simplicity have spurred inclusion of k_t algorithm in standard LHC experiments' "panoply" of jets

Cone algorithms

Sterman & Weinberg '77, UAx '80s, Tevatron '90s

Widely used at *pp* colliders Range from simple to very complex Plagued by infrared and collinear safety issues Much work in past years: help LHC avoid previous pp colliders' deficiencies



Historically, all practical cone algs had these problems

Because they used "seed particles"

- Cause perturbative QCD to give divergent answers \rightarrow meaningless
- Issue exarcerbated in complex environments [e.g. multijet BSM signatures]
- HIC are a complex environment too!

IR & Coll. safety are important there too

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Tevatron & ATLAS cone algs have two main steps:

- Find some/all stable cones
 - \equiv cone pointing in same direction as the momentum of its contents
- Resolve cases of overlapping stable cones





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Resolve cases of overlapping stable cones

By running a 'split-merge' procedure

How do you find the stable cones?

- Iterate from 'seed' particles
 Done originally, very IR unsafe, N² [JetClu, Atlas]
 - Iterate from 'midpoints' between cones from seeds
 Midpoint cone, less IR unsafe, N³
 - Seedless: try all subsets of particles IR safe, N2^N
 100 particles: 10¹⁷ years
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How do you find the stable cones?

 Iterate from 'seed' particles Done originally, very IR unsafe, N² [JetClu, Atlas]
 Advance #2: IR safe seedless cone (SM) separate mom. and geometry New comp. geometry techniques: 2D all distinct circular enclosures Then for each check whether → stable cone
 Time reduced from N2^N to N² In N: 6s for N=4000. GPS & Soyez '07 "SISCone"

- ► Find one stable cone E.g. by iterating from hardest seed particle
- Call it a jet; remove its particles from the event; repeat



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 - This is not the same algorithm
 - Many physics aspects differ

Iterative Cone with Progressive Removal (IC-PR) Collinear unsafe [← hardest seed] e.g. CMS it. cone, [Pythia Cone, GetJet]



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Advance #3: anti- k_t algorithm

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 Call it a jet;remove its particles from the event; repeat
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Iterative Cone with Progressive Removal (IC-PR) Collinear unsafe [← hardest seed]

GPS, Cacciari & Soyez '08

Seq. Rec.: find smallest of d_{ij} , d_{iB} : $d_{ij} = \min(p_{ti}^{-2}, p_{tj}^{-2})\Delta R_{ij}^2/R^2$, $d_{iB} = p_{ti}^{-2}$

- Grows outwards from hard "seeds," but in collinear safe way
- Has circular jet "area," just like IC-PR & same @ NLO (incl.jets)
- ▶ Fast: *Nn* or *Nn*^{1/2}, 25ms for 4000 particles



ICPR has circular jets But collinear unsafe

- So does anti-k_t safe from theory point of view
- Cones with split-merge (SISCone) shrink to remove soft junk



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A set of 4 jet algorithms

k_t SR, $d_{ij} = \min(k_{ti}^2,k_{tj}^2)\Delta R_{ij}^2/R^2$ hierarchical in rel \perp momenta	Cambridge/Aachen SR, $d_{ij} = \Delta R_{ij}^2/R^2$ hierarchical in angle
anti- k_t	SISCone
SR, $d_{ij} = \min(k_{ti}^{-2}, k_{tj}^{-2}) \Delta R_{ij}^2/R^2$	Seedless Infrared Safe cone +SM
gives perfectly conical jets	gives "economical" jets

All share 1 main parameter: R, the angular reach differ in details of shape, substructure, NLO corrections [and all accessible through FastJet: Cacciari, GPS & Soyez, '05-08]

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Jets in HIC



so dangerous to place p_t cutoffs?

- \blacktriangleright Huge soft background in each event $~~\sim$ 200 GeV per unit area in ϕ,η
- Modelling very uncertain; we're not too sure how medium affects
 - distribution of hadron momenta
 - multiplicities
 - angular distribution of energy flow

so want to study different angular scales

- Full programme of what we/you want to do with jets in HIC not yet clear?
 - provide reference momentum, e.g. to get hadron fragementation functions
 - look inside them, to learn about how medium changes energy flow
- Technical issues: multiplicity of 30k particles [without cutoff] Solved for all algs, except SISCone (but could pre-cluster)

Guiding principles

Be detector independent, as far as possible

Enable direct comparisons between collaborations

- Ensure continuity with pp pp has "underlying event" noise, & will have much pileup at LHC
- Be aware of inherent systematics in the procedure & quantify them All methods have some systematics

1. Estimate the transverse momentum density from the collective flow



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2. Subtract the collective flow from jets (either before or after clustering)



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Subtraction in action



the inclusive jet spectrum — a basic measurement [here shown unquenched] Jets, G. Salam (p. 22) Jets in HIC



Jets, G. Salam (p. 22) Jets in HIC



10

Jnderstand systematics of "noise" $\langle \Delta p_t^2 \rangle \simeq \langle A_{JA,R} \rangle \langle \sigma^2 \rangle + \langle \Delta p_t^2 \rangle_{BR}$ Low jet-areas good; Back-reaction Jets, G. Salam (p. 22) Jets in HIC



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Low jet-areas good; Back-reaction? Better understanding \rightarrow better algs

Jets, G. Salam (p. 22) Lets in HIC



cf. STAR talk? But quenching can change pt dis-



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 $\langle \Delta p_t^2 \rangle \simeq \langle A_{IABB} \rangle \langle \sigma^2 \rangle + \langle \Delta p_t^2 \rangle_{BBB}$

Low jet-areas good; Back-reaction? Better understanding \rightarrow better algs

Events are noisy. One approach: cf. STAR talk? But quenching can change pt dis-

tribution of particles in jets



"Background" may not be uniform

- Ridge
- Mach cone

When estimating background (globally, locally), are you affected by this? Importance of using complementary methods within each experiment

Are these structures part of background, or part of jet? What goes into the jet is ultimately your choice ➡Should jet algorithms be designed to include them? Jets are just now becoming a reality in Heavy-Ion Collisions $${\rm STAR},\&$ in not so long LHC}$

It's important to start on a good footing

Infrared & Collinear safe algorithms

E.g.: k_t , Cam/Aachen, anti- k_t & SISCone [all in FastJet]

Exciting new territory, in terms of how we study it... Exploit flexibility in approaches to separating jets & background and in how we use the jets

And in terms of what it will teach us!

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EXTRAS
Jets, G. Salam (p. 26) Extras



Start with a hard dijet event

Jets, G. Salam (p. 26) Extras

Background subtraction in HI event



Same event on a different scale



Embed it into a central Hydjet Pb Pb event



Look at $P_t/Area$ for each jet

Background subtraction in HI event



Fit the background $\rho(y)$ [NB: more general functional form needs investigating]



Subtract $\rho(y)$ from P_t /Area for each jet



Look at resulting corrected $P_t = P_{t,orig} - \rho(y) \times \text{Area}$ Hard jets with roughly correct P_t and y emerge clearly!

Background subtraction in HI event



Try with Cambridge/Aachen instead of k_t to check robustness!