Jets, our window on partons at the LHC

Gavin P. Salam LPTHE, UPMC Paris 6 & CNRS

Torino, 23 May 2008

Basics: Cacciari (LPTHE) & Soyez (BNL) Higgs: Butterworth, Davison (ATLAS UCL) & Rubin (LPTHE) Other related work: Dasgupta (Manchester), Magnea (Turin), Rojo (LPTHE)

Jets, our window on partons (p. 2) LO. LHC

Startup approaches for $\ensuremath{\mathsf{LHC}}$







Startup approaches for LHC



2 general purpose detectors





Compared to current biggest collider (Tevatron)

- LHC energy will be 7 times higher
- Total number of collisions (over 6 years) 50 times higher

Aims are varied; Higgs discovery top priority

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 $(v+H)^2W^+W^-+\cdots$

Excitations H around v are the Higgs \equiv sign of what's going on.

Plus searches for anything NEW in this energy domain

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LHC is a parton collider

- Quarks and gluons are inevitable in initial state
- and ubiquitous in the final state

Partons — quarks and gluons — are key concepts of QCD.

- Lagrangian is in terms of quark and gluon fields
- Perturbative QCD only deals with partons

Though we often talk of quarks and gluons, we never see them

- ▶ Not an asymptotic state of the theory because of confinement
- But also even in perturbation theory

because of collinear divergences (in massless approx.)

The closest we can get to handling final-state partons is jets

1. Jets Introduction



 $\int \alpha_{\rm s} \frac{dE}{E} \frac{d\theta}{\theta} \gg 1$

At low scales:

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Parton fragmentation

quark

Gluon emission:

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Parton fragmentation



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Seeing v. defining jets



Jets are what we see. Clearly(?) 2 of them.

> 2 partons? $E_{parton} = M_z/2?$

How many jets do you see? Do you really want to ask yourself this question for 10⁸ events?



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A jet definition is a systematic procedure that **projects away the multiparticle dynamics**, so as to leave a simple picture of what happened in an event:



Jets are *as close as we can get to a physical single hard quark or gluon:* with good definitions their properties (multiplicity, energies, [flavour]) are

- finite at any order of perturbation theory
- \blacktriangleright insensitive to the parton \rightarrow hadron transition

NB: finiteness \longleftrightarrow set of jets depends on jet def.



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Jet (definitions) provide central link between expt., "theory" and theory And jets are an input to almost all analyses



QCD jets flowchart



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- Periodic key developments in jet definitions spurred by ever-increasing experimental/theoretical sophistication.
- Approach of LHC provides motivation for taking a new, fresh, systematic look at jets.
- This talk: some of the discoveries along the way







What's new for jets @ LHC?

Number of particles:

Experiment	Ν
LEP, HERA	50
Tevatron	100-400
LHC low-lumi	800
LHC high-lumi	4000
LHC PbPb	30000

- Range & complexity of signatures (jets, tt̄, tj, Wj, Hj, tt̄j, WWj, Wjj, SUSY, etc.)
- e.g. \sim 5 million $t\overline{t}$ ightarrow 6 jet events/year
- Theory investment

 \sim 100 people imes 10 years 60 - 100 million \$

Physics scales:

Experiment	Physics	Scale
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LHC	+ BSM	
	+ Pileup	

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Jets, our window on partons (p. 13) 1. Jets Intro 2. Jets at LHC

Old issues? 1990 "standards"

Snowmass Accord (1990):

FERMILAB-Conf-90/249-E [E-741/CDF]

Toward a Standardization of Jet Definitions ·

Several important properties that should be met by a jet definition are [3]:

- 1. Simple to implement in an experimental analysis;
- 2. Simple to implement in the theoretical calculation;
- 3. Defined at any order of perturbation theory;
- 4. Yields finite cross section at any order of perturbation theory;
- 5. Yields a cross section that is relatively insensitive to hadronization.

Without these, either the experiment won't use the jet-definition, or the theoretical calculations will be compromised Long satisfied in e^+e^- and DIS Satisfied in $\lesssim 10\%$ of jet work at Tevatron Hardly discussed in LHC TDRs

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2. Safe, practical jet-finding

Sequential recombination	Cone
k_t , Jade, Cam/Aachen,	UA1, JetClu, Midpoint,
Bottom-up: Cluster 'closest' particles repeat- edly until few left \rightarrow jets.	Top-down: Find coarse regions of energy flow (cones), and call them jets.
Works because of mapping: <i>closeness</i> ⇔ <i>QCD divergence</i>	Works because <i>QCD only modifies</i> energy flow on small scales
Loved by e^+e^- , ep and theorists	Loved by <i>pp</i> and few(er) theorists

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- Find smallest of all $d_{ij} = \min(k_{ti}^2, k_{tj}^2) \Delta R_{ij}^2/R^2$ and $d_{iB} = k_i^2$
- Recombine i, j (if $iB: i \rightarrow jet$)
- Repeat



- NB: hadron collider variables
- $\Delta R_{ij}^2 = (\phi_i \phi_j)^2 + (y_i y_j)^2$
- rapidity $y_i = \frac{1}{2} \ln \frac{E_i + \rho_{zi}}{E_i \rho_{zi}}$
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Why k_t ?

k_t distance measures

$$d_{ij} = \min(k_{ti}^2, k_{tj}^2) \Delta R_{ij}^2, \qquad d_{iB} = k_{ti}^2$$

are closely related to structure of divergences for QCD emissions

$$[dk_j]|M_{g \to g_i g_j}^2(k_j)| \sim \frac{\alpha_{\rm s} C_A}{2\pi} \frac{dk_{tj}}{\min(k_{ti}, k_{tj})} \frac{d\Delta R_{ij}}{\Delta R_{ij}}, \qquad (k_{tj} \ll k_{ti}, \ \Delta R_{ij} \ll 1)$$

and

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 k_t algorithm attempts approximate inversion of branching process

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*k*_t algorithm attempts approximate inversion of branching process

Computing...

'Trivial' computational issue:

- ▶ for N particles: $N^2 d_{ij}$ searched through N times = N^3
- 4000 particles (or calo cells): 1 minute NB: often study 10⁷ - 10⁸ events (20-200 CPU years)
 Heavy lons: 30000 particles: 10 hours/event

As far as possible physics choices should not be limited by computing.

Even if we're clever about repeating the full search each time, we still have $\mathcal{O}(N^2) \ d_{ij}$'s to establish

Fast Hierarchical Clustering and Other Applications of Dynamic Closest Pairs

David Eppstein UC Irvine

We develop data structures for dynamic closest pair problems with arbitrary distance functions, that do not necessarily come from any geometric structure on the objects. Based on a technique previously used by the author for Euclidean closest pairs, we show how to insert and delete objects from an n-object set, maintaining the closest pair, in $O(n \log^2 n)$ time per update and O(n) space. With quadratic space, we can instead use a quadtree-like structure to achieve an optimal time bound, O(n) per update. We apply these data structures to hierarchical clustering, greedy matching, and TSP heuristics, and discuss other potential applications in machine learning. Gröber bases, and local improvement algorithms for partition and placement problems. Experiments show our new methods to be faster in practice than previously used heuristics.

Categories and Subject Descriptors: F.2.2 [Analysis of Algorithms]: Nonnumeric Algorithms

General Terms: Closest Pair, Agglomerative Clustering

Additional Key Words and Phrases: TSP, matching, conga line data structure, quadtree, nearest neighbor heuristic

1. INTRODUCTION

Hierarchical clustering has long been a mainstay of statistical analysis, and clustering based methods have attracted attention in other fields: computational biology (reconstruction of evolutionary trees; tree-based multiple sequence alignment), scientific simulation (n-body problems), theoretical computer science (network design and nearest neighbor searching) and of course the web (hierarchical indices such as Yahoo). Many clustering methods have been devised and used in these applications, but less effort has gone into algorithmic speedups of these methods.

In this paper we identify and demonstrate speedups for a key subroutine used in several clustering algorithms, that of maintaining closest pairs in a dynamic set of objects. We also describe several other applications or potential applications of the

k_t alg. is so good it's used throughout science!

NB HEP is not only field to use bruteforce...

For general distance measures problem reduces to $\sim N^2$ (factor ~ 20 for N = 1000).

Eppstein '99 Cardinal '03 Fast Hierarchical Clustering and Other Applications of Dynamic Closest Pairs

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Of these naive methods, brute force recomputation may be most commonly used, due to its low space requirements and ease of implementation. Three hierarchical clustering codes we examined, Zupan's [Zupan 1982], CLUSTAL W [Thompson et al. 1994], and PHYLIP [Felsenstein 1995] use brute force. (Indeed, they do not even save space by doing so, since they all store the distance matrix.) Pazzani's learning code [Pazzani 1997] also uses brute force (M. Pazzani, personal communication), as does *Mathematica*'s Gröbner basis code (D. Lichtblau, personal communication). *k*_t alg. is so good it's used throughout science!

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Eppstein '99 + Cardinal '03 There are N(N-1)/2 distances d_{ij} — surely we have to calculate them all in order to find smallest?

k_t distance measure is partly geometrical:

$$\begin{split} \min_{i,j} d_{ij} &\equiv \min_{i,j} (\min\{k_{ti}^2, k_{tj}^2\} \Delta_{ij}^2) \\ &= \min_{i,j} (k_{ti}^2 \Delta_{ij}^2) \\ &= \min_i (k_{ti}^2 \min_j \Delta_{ij}^2) \end{split}$$

In words: if i, j form smallest d_{ij} then j is geometrical nearest neighbour (GNN) of i.

 k_t distance need only be calculated between GNNs

Each point has 1 GNN \rightarrow need only calculate N d_{ij} 's

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Finding Geom Nearest Neighbours



Given a set of vertices on plane (1...10) a *Voronoi diagram* partitions plane into cells containing all points closest to each vertex Dirichlet '1850. Voronoi '1908

A vertex's nearest other vertex is always in an adjacent cell.

E.g. GNN of point 7 will be found among 1,4,2,8,3 (it turns out to be 3)

Construction of Voronoi diagram for *N* points: *N* In *N* time Fortune '88 Update of 1 point in Voronoi diagram: In *N* time Devillers '99 [+ related work by other authors]

Convenient C++ package available: CGAL http://www.cgal.org Assemble with other comp. science methods: FastJet Cacciari & GPS, hep-ph/0512210 http://www.lpthe.jussieu.fr/~salam/fastjet/



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FastJet performance



NB: for $N < 10^4$, FastJet switches to a related geometrical N^2 alg. Conclusion: speed issues for k_t resolved



Jet discussions: often polarised, driven by unquantified statements



Rigorous approach is to quantify similarities & differences
 Dasgupta, Magnea & GPS '07; Cacciari, GPS & Soyez '08

Bottom line: grains of truth in the qualitative statements
 So want good cone algorithms too [NB: two varieties, IC-SM & IC-PR]

Jets, our window on partons (p. 24) 2. Safe, practical jet-finding 2. Cone algorithms





► Find one stable cone

By iterating from hardest seed particle





Find one stable cone

By iterating from hardest seed particle





Find one stable cone

By iterating from hardest seed particle





Iterative Cone [with progressive removal]

Procedure:

Find one stable cone

By iterating from hardest seed particle





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By iterating from hardest seed particle





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Iterative Cone with Progressive Removal

Call it a jet; remove its particles from the event; repeat

(IC-PR)

e.g. CMS it. cone, [Pythia Cone, GetJet], ...
NB: not same type of algorithm as Atlas Cone, MidPoint, SISCone







ICPR iteration issue


















Jets, our window on partons (p. 26) 2. Safe, practical jet-finding 2. Cone algorithms







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Jets, our window on partons (p. 27) 2. Safe, practical jet-finding 2. Cone algorithms



For everything to fit together all of Snowmass criteria needed.

Given need to compromise, the IRC safety usually goes first.

This breaks connection between different parts of QCD.

 $\sim 90\%$ of Tevatron and LHC work based on IRC unsafe algs — a pervasive problem.

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What we want: something that behaves like a cone algorithm (circular jets), but that is IRC safe.

Approach: drop the "cone" in definition, but design an algorithm that still acts like a cone: $anti-k_t$

- 1. Find smallest of d_{ij} , d_{iB} : $d_{ij} = \min(k_{ti}^{-2}, k_{tj}^{-2})\Delta R_{ij}^2/R^2$, $d_{iB} = k_{ti}^{-2}$
- 2. if ij, recombine them; if iB, call i a jet, and remove from list of particles
- 3. repeat from step 1 until no particles left.

Cacciari, GPS & Soyez '08

Looks like k_t but momentum in *denominator* causes d_{ij} to involve largest $k_t \rightarrow$ jets grows outward from hard "seeds".



anti- k_t v. Cone (ICPR) jets





Complementary set of IR/Collinear safe jet algs \longrightarrow flexbility in studying complex events.

Consider families of jet algs: e.g. sequential recombination with

 $d_{ij} = \min(k_{ti}^{2p}, k_{tj}^{2p}) \Delta R_{ij}^2 / R^2$

	Alg. name	Comp. Geometry problem	time
p = 1	k _t	Dynamic Nearest Neighbour	
	CDOSTW '91-93; ES '93	CGAL (Devillers et al)	NIn N exp.
p = 0	Cambridge/Aachen	Dynamic Closest Pair	
	Dok, Leder, Moretti, Webber '97	T. Chan '02	N In N
	Wengler, Wobisch '98		
p = -1	anti- <i>k</i> t (cone-like)	Dynamic Nearest Neighbour	
	Cacciari, GPS, Soyez, in prep.	CGAL (worst case)	№ ^{3/2}
cone	SISCone	All circular enclosures	
	GPS Soyez '07 + Tevatron run II '00	previously unconsidered	$N^2 \ln N$ exp.

All accessible in FastJet

FastJet in software of all (4) LHC collaborations

3. An example: boosted Higgs search

Illustrate LHC challenges with a recently widely discussed class of problems:

Can you identify hadronically decaying EW bosons when they're produced at high pt?



Significant discussion over years: heavy new things decay to EW states

- Seymour '94 [Higgs $\rightarrow WW \rightarrow \nu \ell$ jets]
- ▶ Butterworth, Cox & Forshaw '02 [$WW \rightarrow WW \rightarrow \nu \ell$ jets]
- Butterworth, Ellis & Raklev '07 [SUSY decay chains $\rightarrow W, H$]
- Skiba & Tucker-Smith '07 [vector quarks]
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Most obvious method: look at the jet mass, but

- QCD jets can be massive too
- Non-pert mass resol^{*n*} $\sim \delta M \sim R^4 \Lambda_{UE} \frac{p_t}{M}$ Dasg

 \rightarrow large backgrounds

Dasgupta, Magnea & GPS '07

<u>Natural idea:</u> use hierarchical structure of k_t alg to resolve structure Seymour '93; Butterworth, Cox & Forshaw '02 [Ysplitter]

- ▶ You can cut on d_{ij} (rel. \perp mom.²), correl. with mass helps reject bkgds
- **•** But not ideal: k_t intrinsic mass resolution often poor

What you really want:

- Stay with hierarchical-type alg: study two subjets
- Dynamically choose R based on $p_t \& M \rightarrow \text{best mass resolution}$
- → Cambridge/Aachen algorithm

Repeatedly cluster pair of objects closest in angle until all separated by $\geq R$ [Can then undo clustering & look at jet on a range of angular scales]

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E.g.: WH/ZH search channel @ LHC

• Signal is $W \to \ell \nu$, $H \to b \overline{b}$.

• Backgrounds include $Wb\bar{b}$, $t\bar{t} \rightarrow \ell \nu b\bar{b} j j$, ...

Studied e.g. in ATLAS TDR

Difficulties, e.g.

- ▶ $gg \rightarrow t\bar{t}$ has $\ell \nu b\bar{b}$ with same intrinsic mass scale, but much higher partonic luminosity
- Need exquisite control of bkgd shape



- Go to high p_t ($p_{tH}, p_{tV} > 200$ GeV)
- Lose 95% of signal, but more efficient?
- Maybe kill $t\bar{t}$ & gain clarity?



Jets, our window on partons (p. 34) 3. Example: Higgs search

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Searching for high- p_t HW/HZ?

High- p_t light Higgs decays to $b\bar{b}$ inside a single jet. Can this be seen? Butterworth, Davison, Rubin & GPS '08



Then on the Higgs-candidate: *filter* away UE/pileup by reducing $R \rightarrow R_{filt}$, take *three hardest subjets* (keep LO gluon radⁿ) + require *b*-tags on two hardest.

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SIGNAL



Zbb BACKGROUND

arbitrary norm.

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Jets, our window on partons (p. 37) 3. Example: Higgs search

Compare with "standard" algorithms

Check mass spectra in HZ channel, $H \rightarrow b\bar{b}$, $Z \rightarrow \ell^+ \ell^-$



Cambridge/Aachen (C/A) with mass-drop and filtering (MD/F) works best

Jets, our window on partons (p. 38) 3. Example: Higgs search

combine HZ and HW, $p_t > 200 \text{ GeV}$



Common cuts

- ▶ p_{tV}, p_{tH} > 200 GeV
- ▶ |η_H| < 2.5</p>
- $[p_{t,\ell} > 30 \text{ GeV}, |\eta_\ell| < 2.5]$
- \blacktriangleright No extra ℓ , *b*'s with $|\eta| < 2.5$
- Real/fake b-tag rates: 0.7/0.01

• S/\sqrt{B} from 18 GeV window

Leptonic channel

$$Z
ightarrow \mu^+ \mu^-, e^+ e^-$$

▶ 80
$$< m_{\ell^+\ell^-} <$$
 100 GeV

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Semi-leptonic channel

 $W \to \nu \ell$

- $\not\!\!E_T > 30 \text{ GeV}$ (& consistent W.)
- no extra jets $|\eta| < 3, p_t > 30$

combine HZ and HW, $p_t > 200 \text{ GeV}$



Common cuts

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- $[p_{t,\ell} > 30 \text{ GeV}, |\eta_\ell| < 2.5]$
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3 channels combined

combine HZ and HW, $p_t > 200 \text{ GeV}$



Closing

Jets are the closest we can get to seeing and giving meaning to partons

- Play a pivotal role in experimental analyses, comparisons to QCD calculations
- Significant progress in past 2 years towards making them *consistent* (IR/Collinear safe) and *practical* Link with computational geometry All tools are made public: http://www.lpthe.jussieu.fr/~salam/fastjet/
- The physics of how jets behave in a hadron-collider environment is a rich subject — much to be understood, and potential for significant impact in how jets are used at LHC
 E.g. Boosted higgs search

EXTRA SLIDES

Real life does not have infinities, but pert. infinity leaves a real-life trace

$$\alpha_{\rm s}^2 + \alpha_{\rm s}^3 + \alpha_{\rm s}^4 \times \infty \to \alpha_{\rm s}^2 + \alpha_{\rm s}^3 + \alpha_{\rm s}^4 \times \ln p_t / \Lambda \to \alpha_{\rm s}^2 + \underbrace{\alpha_{\rm s}^3 + \alpha_{\rm s}^3}_{\text{BOTH WASTED}}$$

Among consequences of IR unsafety:

	Last i			
	JetClu, ATLAS	MidPoint	CMS it. cone	Known at
	LO	NLO	NLO	NLO (\rightarrow NNLO)
W/Z + 1 jet	LO	NLO	NLO	NLO
		LO	LO	NLO [nlojet++]
W/Z + 2 jets		LO	LO	NLO [MCFM]

NB: \$30 – 50M investment in NLO

Multi-jet contexts much more sensitive: **ubiquitous at LHC** And LHC will rely on QCD for background double-checks extraction of cross sections, extraction of parameters Real life does not have infinities, but pert. infinity leaves a real-life trace

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W/Z+1 jet	LO	NLO	NLO	NLO
3 jets	none	LO	LO	NLO [nlojet++]
W/Z + 2 jets	none	LO	LO	NLO [MCFM]
$m_{ m jet}$ in $2j + X$	none	none	none	LO

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Impact of *b*-tagging, Higgs mass



Most scenarios above 3σ ; still much work to be done, notably on verification of experimental resolution.

Regardless of final outcome, illustrates value of choosing appropriate "jet-methods," and of potential for progress with new ideas.

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