#### Perturbative QCD for the LHC

Gavin P. Salam LPTHE, UPMC Paris 6 & CNRS

ICHEP 2010 Paris, France, 22–28 July 2010

# As the LHC programme gets going, what is the status of our QCD tools?

Are they where we thought they might be?

Are they where we'd *like* them to be?

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Yes! With several major milestones reached in the past two years.

Are they where we'd like them to be?

There's still ample room for progress.

#### What roles for QCD at the LHC?



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Telling us what the background is, so we can see any excess



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# Monte Carlos



The most pervasive role of QCD at LHC

Every paper that comes out from the LHC pp physics programme will involve the use of one or more QCD-based parton-shower Monte Carlo event generators: Pythia, Herwig, Sherpa, ...

For simulating physics signals.

For simulating background signals.

For simulating pileup.

As input to simulating detector respone.

### Generations of generators

Original Fortran (77) Generation

Has served us well since 1980's, but now reaching end-of-life

- Herwig 6.5: 11 authors, 60k lines
- ► Pythia 6.4: 3 + N authors, 80k lines Still the most widely used
- Supplemented with Alpgen/Madgraph (tree-level ME), or MC@NLO/POWHEG (NLO)

New (C++) Generation

After 5–10 years' work, codes now entering early adulthood.

▶ HERWIG++ 2.4: 14 authors, 250k lines + ThePEG, 3 authors, 110k lines

- PYTHIA 8.1: 5 authors, 70k lines
- ▶ SHERPA 1.2: 11 authors, 250k lines

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#### Pythia 6.4 $\rightarrow$ Pythia 8.1

- New p<sub>t</sub> ordered shower (mass-ordered shower removed)
- Numerous new features for multiple interactions

```
Herwig 6.5 \rightarrow Herwig++ 2.4
```

- New angular ordered shower, including better mass treatment
- Several processes at NLO with POWHEG
- Incorporates multiple interactions model

```
[no F77 version] \rightarrow Sherpa 1.2
```

- Dipole shower
- Efficient multileg matrix-elements (COMIX), CKKW matching
- ► Now has own multiple interactions, hadronisation, etc.



All 3 show good agreement for this basic observable

### $Z p_t$ distribution v. Tevatron data



All 3 show good agreement for this basic observable

# NLO calculations



#### How accurate is perturbative QCD?

 $\sigma = c_0 + c_1 \alpha_s + c_2 \alpha_s^2 + \dots$  $\alpha_s \simeq 0.1$ That implies LO QCD (just  $c_0$ ) should be accurate to within 10% It isn't

Need NLO in order to have a good guess at normalisation and uncertainties in backgrounds



Anastasiou, Melnikov & Petriello '04 Anastasiou, Dissertori & Stöckli '07 
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## One of the motivations for NLO multijet



SUSY particles often have cascade decays  $\rightarrow$  multijet + Missing  $E_T$  + X

Signal is broad excess  $(\sim~\times5)$  over expected (LO) background

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#### Traditional

Draw all Feynman diagrams with 1 loop. Work out formulae for them.

Work hard to reduce integrals to known forms (+ tricks).



**Recursive/unitarity methods** Assemble loop-diagrams from individual tree-level diagrams.

Build trees by sticking together simpler tree-level diagrams



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Ţ	he NL	0 revo	lution					
	1980	1985	1990	1995	2000	2005	2010	



1979: NLO Drell-Yan [Altarelli, Ellis & Martinelli]



1987: NLO high- $p_t$  photoproduction [Aurenche et al] 1988: NLO  $b\bar{b}$ ,  $t\bar{t}$  [Nason et al] 1993: dijets,  $V_j$  [JETRAD, Giele, Glover & Kosower]

### The NLO revolution



```
1998: NLO Wb\bar{b} [MCFM: Ellis & Veseli]
2000: NLO Zb\bar{b} [MCFM: Campbell & Ellis]
2001: NLO 3j [NLOJet++: Nagy]
...
2007: NLO t\bar{t}j [Dittmaier, Uwer & Weinzierl '07]
...
```

### The NLO revolution





2009: NLO	W+3j [Rocket: Ellis, Melnikov & Zanderighi]	[unitarity]
2009: NLO	W+3j [BlackHat: Berger et al]	[unitarity]
2009: NLO	$t\bar{t}b\bar{b}$ [Bredenstein et al]	[traditional]
2009: NLO	$t\bar{t}b\bar{b}$ [HELAC-NLO: Bevilacqua et al]	[unitarity]
2009: NLO	$qar{q}  ightarrow bar{b}bar{b}$ [Golem: Binoth et al]	[traditional]
2010: NLO	<i>tījj</i> [HELAC-NLO: Bevilacqua et al]	[unitarity]
2010: NLO	Z+3j [BlackHat: Berger et al]	[unitarity]

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2010: NLO W+4j [BlackHat: Berger et al, preliminary]

[unitarity]



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pQCD for LHC

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#### **Automation:**

A large number of  $2 \rightarrow 3$  processes have been done manually. Only some public; e.g. MCFM, NLOJet++

For 2  $\rightarrow$  4, 2  $\rightarrow$  5, far too many processes for all to be handled manually.

Among the challenges, efficiency, which becomes limiting factor as complexity increases 1 histogram  $\sim O(100)$  CPU days

- because you need to integrate over "more" phase space
- because the amplitudes themselves take longer to evaluate

Or get efficiency gain from graphics cards? Hagiwara et al '09 Giele, Stavenga & Winter '09-10

# Exclusive (hadron-level) quality of Monte Carlo and accuracy of NLO together?

like MC@NLO, POWHEG



# Exclusive (hadron-level) quality of Monte Carlo and accuracy of NLO together?

#### like MC@NLO. POWHEG



MENLOPS: e.g. NLO:Z, LO:Z+1/2/3/... + parton shower Hamilton & Nason '10; + work in progress SHERPA

simultaneously NLO:Z & NLO:Z+j + parton shower

Alioli et al, prelim

Generalising this is the current frontier

pQCD for LHC

# Precision QCD (NNLO, etc.)



# To get precision for the fundamental particles we're studying:

- To better study top, W/Z [Higgs]
- Extract their masses, couplings,

etc.

#### For cases where NLO seems crazy

- As can occur for  $p_t \gg m_{EW}$  (LHC!)
- In general, with large ratios of scales

#### Rubin, GPS & Sapeta '10

#### Here, concentrate on first case, specifically top

Vector Boson Fusion @ NNLO: Bolzoni et al '10

[For more detailed review, see talk by Gehrmann de Ridder]

#### [NNLO etc.]

# Why NNLO / resummation / etc.?



In general, with large ratios of scales

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[NNLO etc.] └[Top] Top production

#### "The most interesting known unknown" in someone's slides (or blog?) — tell me if they were yours

- [Won't talk about:] forward-backward asymmetry, single top
- Mass: nice ideas for a well-defined extraction (because MC extractions give ~ pole mass, but not obvious how exactly)

From NLO distribution, Biswas, Melnikov, Schulze '10 From  $\sigma_{t\bar{t}}$ , proposal @ Moriond '08; + Moch & Uwer '09

Huge effort to calculate cross section accurately

[NNLO etc.] └[Top] Top production

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# Towards a high precision $t\bar{t}$ cross section

#### NNLO

- Two-loop diagrams
  - high-energy limit:
  - Czakon, Mitov & Moch '07 numerical  $q\bar{q} \rightarrow t\bar{t}$ , Czakon '08 analytical  $q\bar{q} \rightarrow t\bar{t}$  (part): Bonciani et al '08–'09 all two-loop poles: Ferroglia et al '09
- One-loop squared
  Körner et al '08, Anastasiou & Aybat '08
- ► 1-loop tītj and real tītjj Dittmaier, Uwer & Weinzierl '07 Bevilacqua et al '10, Melnikov & Schulze '10
- Learning how to combine terms
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Alternatively, identify physically relevant contributions:

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Alternatively, identify physically relevant contributions:

Soft  $2 \rightarrow 2$  structure (massless) Soft  $2 \rightarrow 2$  structure (massive) Expansion to NNLO

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Alternatively, identify physically relevant contributions:

#### NNLL (threshold logs)

- Soft  $2 \rightarrow 2$  structure (massless)
  - Mert Aybat, Dixon & Sterman '06
    - Becher & Neubert '09
      - Gardi & Magnea '09
- Soft  $2 \rightarrow 2$  structure (massive)
  - Kidonakis '09
  - Mitov, Sterman & Sung '09
    - Becher & Neubert '09
  - Beneke, Falgari & Schwinn '09
  - Czakon, Mitov & Sterman '09
- Expansion to NNLO

Beneke et al '09

### $t\bar{t}$ cross sections



Uncertainties shown are theory (scale) only; no PDF uncertainties

The kinds of differences that are present:

Ahrens et al '10, NNLL+NLO: threshold around  $m_{t\bar{t}}$ Aliev et al '10 (Hathor), NNLO approx: threshold around  $2m_t$ Procedures for scale dependence and estimating unknown NNLO terms

### $t\bar{t}$ cross sections



LHC 7 TeV



Uncertainties shown are theory (scale) only; no PDF uncertainties



An aside (not directly LHC): NNLO event shapes in  $e^+e^-$ 



Big theory progress and much activity for  $e^+e^-$  event shapes

- NNLO Gehrmann, Gehrmann de Ridder, Glover & Heinrich '07; Weinzierl '08
- ▶ N<sup>3</sup>LL (thrust, heavy-jet mass) Becher & Schwartz '08, Chien & Schwartz '10





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Is non-perturbative QCD the biggest systematic?

Are there lessons for precision pp/pp physics?

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# Jets



#### Jets as projections



Projection to jets provides "universal" view of event





Hard stuff clusters with nearest neighbour Cacciari, GPS & Soyez '08 [included in FastJet]

repeatedly recombine pair

of objects with smallest





[Jets]





[Jets]







[Jets]













ATLAS and CMS have shown all jet results with an infrared and collinear safe jet finder,  $anti-k_t$ ;



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# soft junk doesn't change hard jets NLO calculations are finite



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### Jets & boosted searches: X with $p_{tX} \gtrsim m_X$



#### 1) WH, $H \rightarrow b\bar{b}$ , ATLAS TDR;
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1) WH,  $H \rightarrow b\bar{b}$ , ATLAS TDR; 2) WH,  $H \rightarrow b\bar{b}$ , Butterworth et al '08 & ATLAS '09; 3) Buried Higgs, Falkowski et al '10; 4)  $\tilde{\chi}^0 \rightarrow qqq$ , Butterworth et al '09; 5)  $t\bar{t}H$ ,  $H \rightarrow b\bar{b}$ , Plen et al '09; 6) Buried Higgs, Chen et al '10; and many more...

[Jets]

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## Conclusions

- ► The C++ event generators: Herwig++, Sherpa and Pythia 8
- NNPDF global fit with robust error estimates

### **Breakthroughs:**

- ▶ NLO calculations, first  $2 \rightarrow 5$  results (W+4j) Next step: automation
- Jet finding IR safety; pulling out hadronic signals previously thought impossible

High accuracy:

► Much work on NNLO *t*t and (NNLL) approximations

And several other processes, e.g. Z/W/H,  $\gamma j$ , j j, V j

Open questions: estimation of uncertainties; impact of hadronisation

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With thanks for comments, suggestions, conversations and information:

Matteo Cacciari, Aude Gehrmann de Ridder, Gudrun Heinrich, Nikolaos Kidonakis, Giulia Zanderighi

# **EXTRAS**





\* up-to-date decay data and LO PDF sets

#### Sjöstrand @ MC4LHC Readiness Workshop, March '10

[Extras]

L[MC]

## Herwig++

- The new Herwig++ program now provides a full simulation of lepton-lepton, lepton-hadron and hadron-hadron collisions with many improvements over its FORTRAN predecessor:
  - New angular ordered parton shower with better theoretical control and mass treatment;
  - Many processes at NLO in the POWHEG approach;
  - Multiple scattering model of the underlying event;
  - Better treatment of BSM physics models;
  - Improved simulation of tau and hadron decays.

CERN 29th March

6

#### Richardson @ MC4LHC Readiness Workshop, March '10

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[Extras

L[MC]

pQCD for LHC

### The three MC++'s



L[MC]





A trend towards more elements included **exactly** in Monte Carlo

PS: the original

► ME+PS Ideas from mid '90's CKKW '01, MLM

NLO+PS MC@NLO '02, POWHEG '04

What's new?

ME + NLO + PS (MENLOPS)
Hamilton & Nason '10

What's still unsolved?

 $\cdot$  NLO + NLO + (...) + PS

pecific implementations: Lavesson & Lonnblad '08 (  $e^+e^-$ 





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Alioli et al [prelim, Z&Z+j]

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pQCD for LHC





pQCD for LHC

# Parton Distribution Functions (PDFs)



PDFs go into every LHC prediction and calculation, from Monte Carlo event generation, through to precision studies.

Protons are the initial state; quarks and gluons interact

Of several groups, so far CTEQ and MSTW have dominated the Global Fit Industry, albeit with a decade-old worry about their procedures:

How well-founded are their uncertainty estimates? ( $\delta\chi^2$  choice, parametrisations, ...)

The barrier to entry for new players is high:

PDF evolution

- Calculation of cross sections for many DIS and pp observables
- > Proper statistical treatment of all (correlated) experimental errors
- Fitting a couple of thousand data points, from myriad sources



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Statistical treatment is transparent Generate 'replica' datasets. For each one, fit a replica PDF Sample over ensemble of PDFs to get error on cross section.

[Extras]

L[PDFs]

Neural networks provide flexible parametrisation of the PDFs Avoid biases from manual choice of functional form

Genetic algorithms to handle fits with large numbers of parameters





### Provides significant added confidence in our understanding of PDF uncertainties



## **Theory uncertainties**

For a wide range of experimentally well-measured observables, theory uncertainties are limiting factor in extracting parameters of the theory (masses, couplings, etc.).

Theory uncertainties are currently being left out from global PDF fits I would be surprised if NLO theory uncertainties ≪ exp. ones Maybe not a problem at NNLO? Only MSTW have NNLO right now

This should (in my opinion) become a high priority for PDF fits.