

Towards Jetography

Gavin Salam

LPTHE, CNRS and UPMC (Univ. Paris 6)

Based on work with

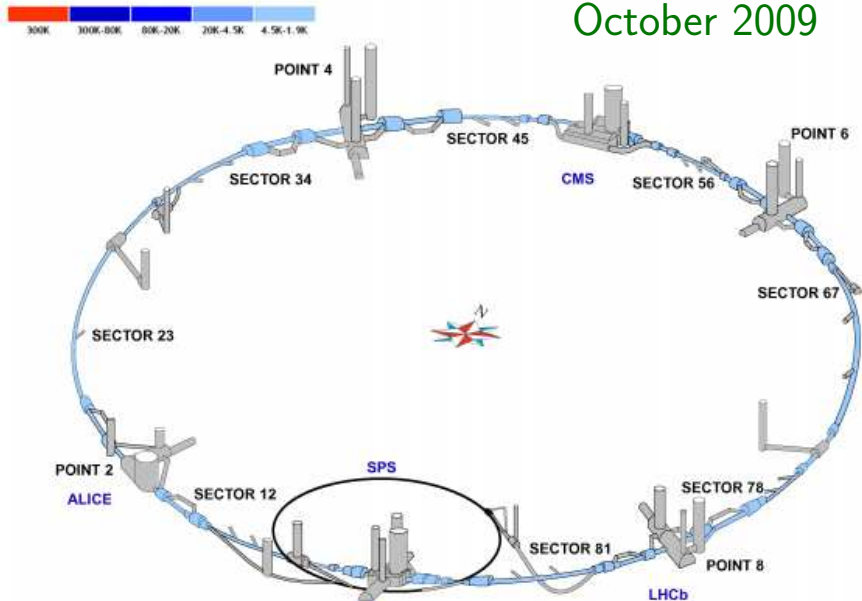
Jon Butterworth, Matteo Cacciari, Mrinal Dasgupta, Adam Davison,
Lorenzo Magnea, Juan Rojo, Mathieu Rubin & Gregory Soyez

C. N. Yang Institute for Theoretical Physics

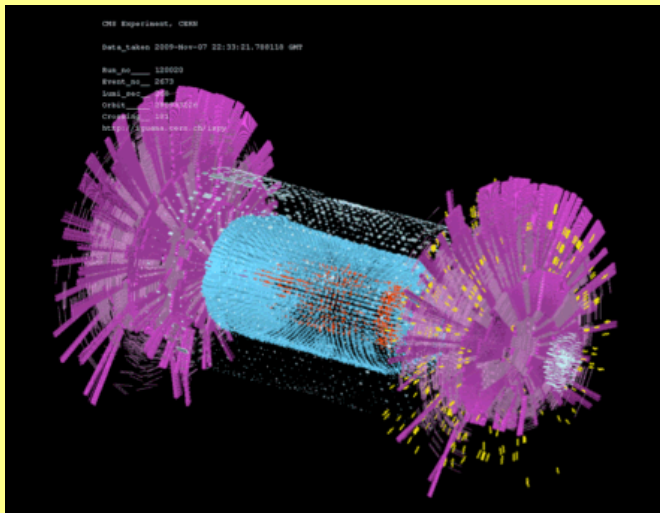
Stony Brook

9 February 2010

October 2009



7 November: first beam (picture: CMS)



T 6

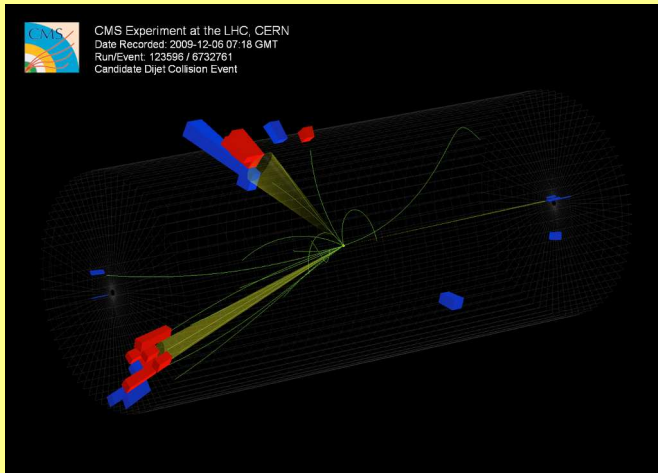
T 7

POINT
ALIC

December: 10^6 collisions at $\sqrt{s} = 900$ GeV



CMS Experiment at the LHC, CERN
Date Recorded: 2009-12-06 07:18 GMT
Run/Event: 123596 / 6732761
Candidate Dijet Collision Event



POINT
ALIC

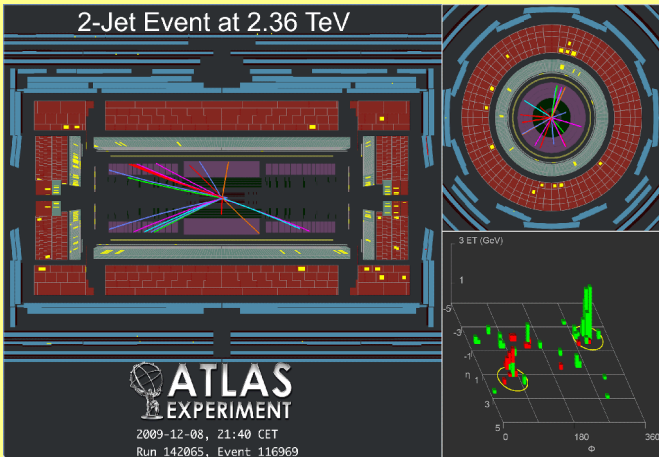
SECTOR 81

POINT 8

LHCb

December: collisions at $\sqrt{s} = 2360$ GeV

2-Jet Event at 2.36 TeV



POINT
ALIC

SECTOR 81

POINT 8

LHCb

quark



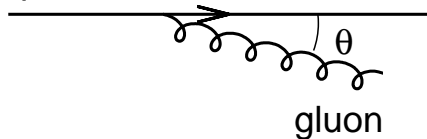
Gluon emission:

$$\int \alpha_s \frac{dE}{E} \frac{d\theta}{\theta} \gg 1$$

At low scales:

$$\alpha_s \rightarrow 1$$

quark

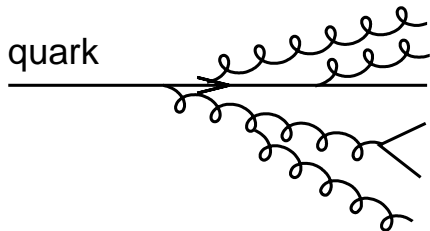


Gluon emission:

$$\int \alpha_s \frac{dE}{E} \frac{d\theta}{\theta} \gg 1$$

At low scales:

$$\alpha_s \rightarrow 1$$

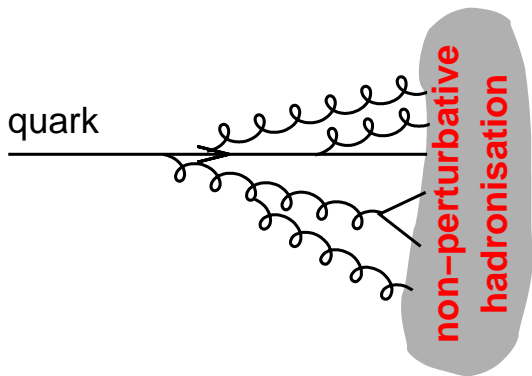


Gluon emission:

$$\int \alpha_s \frac{dE}{E} \frac{d\theta}{\theta} \gg 1$$

At low scales:

$$\alpha_s \rightarrow 1$$

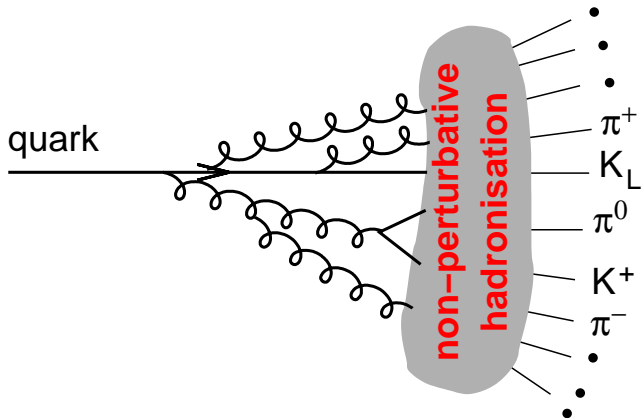


Gloun emission:

$$\int \alpha_s \frac{dE}{E} \frac{d\theta}{\theta} \gg 1$$

At low scales:

$$\alpha_s \rightarrow 1$$

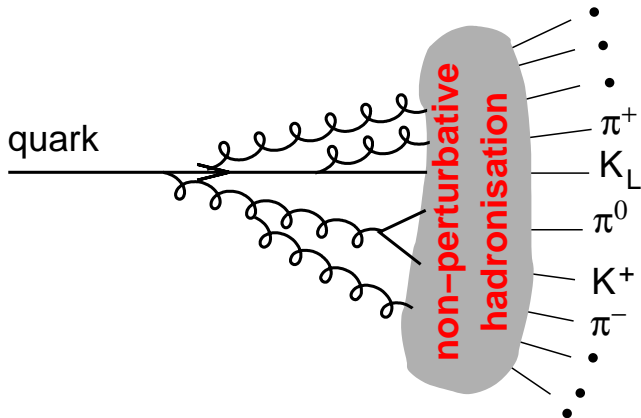


Gloun emission:

$$\int \alpha_s \frac{dE}{E} \frac{d\theta}{\theta} \gg 1$$

At low scales:

$$\alpha_s \rightarrow 1$$



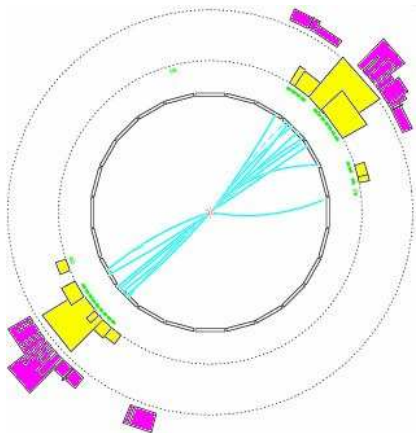
Gluon emission:

$$\int \alpha_s \frac{dE}{E} \frac{d\theta}{\theta} \gg 1$$

At low scales:

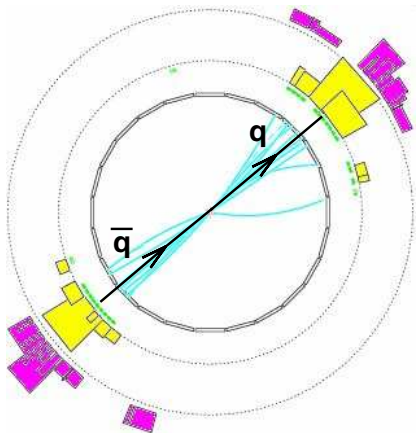
$$\alpha_s \rightarrow 1$$

This is a jet



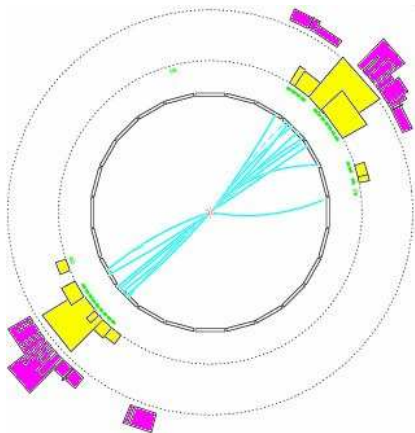
Jets are what we see.
Clearly(?) 2 jets here

How many jets do you see?
Do you really want to ask yourself
this question for 10^9 events?

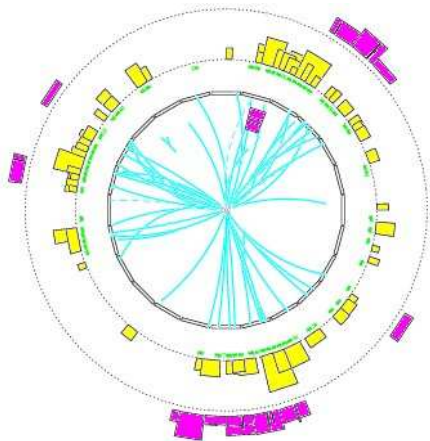


Jets are what we see.
Clearly(?) 2 jets here

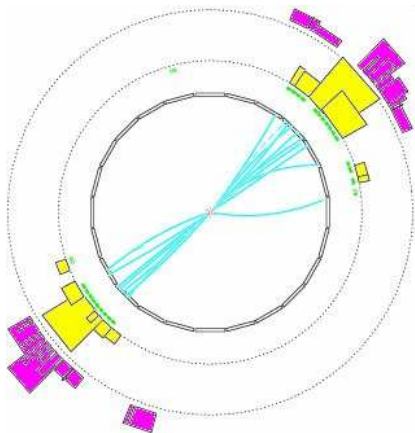
How many jets do you see?
Do you really want to ask yourself
this question for 10^9 events?



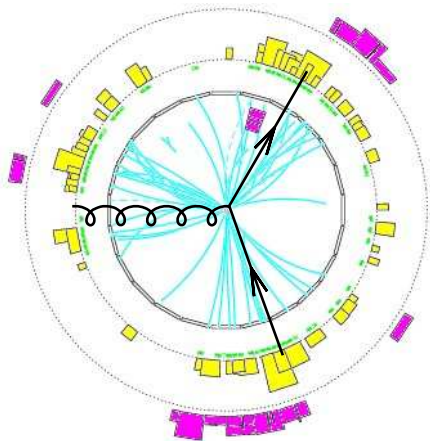
Jets are what we see.
Clearly(?) 2 jets here



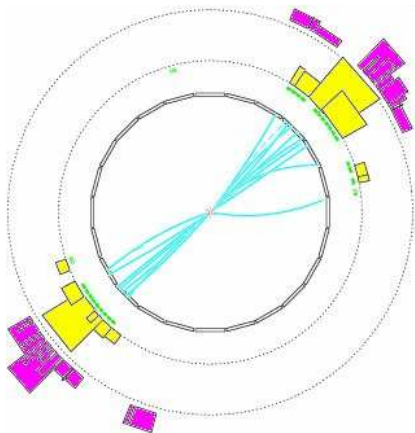
How many jets do you see?
Do you really want to ask yourself
this question for 10^9 events?



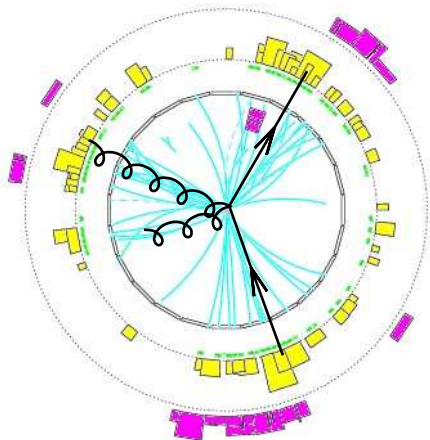
Jets are what we see.
Clearly(?) 2 jets here



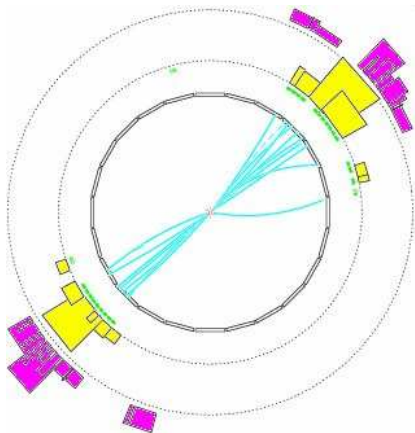
How many jets do you see?
Do you really want to ask yourself
this question for 10^9 events?



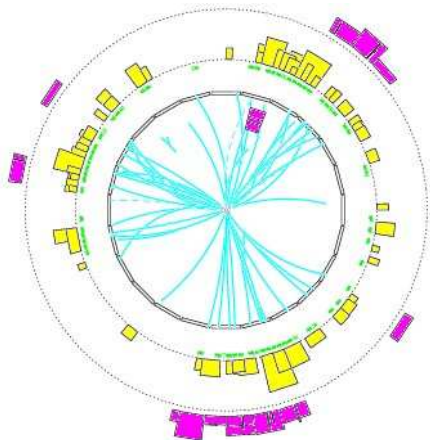
Jets are what we see.
Clearly(?) 2 jets here



How many jets do you see?
Do you really want to ask yourself
this question for 10^9 events?



Jets are what we see.
Clearly(?) 2 jets here



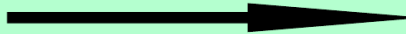
How many jets do you see?
Do you really want to ask yourself
this question for 10^9 events?

jet definition

 $\{P_i\}$

particles,
4-momenta,
calorimeter towers, ...

jet algorithm

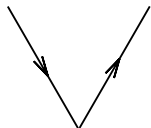
 $\{j_k\}$

jets

+ parameters (usually at least the radius R)

+ recombination scheme

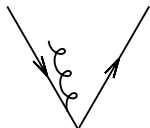
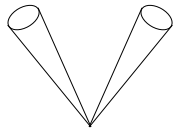
Reminder: running a jet definition gives a well defined physical observable,
which we can measure and, hopefully, calculate



LO partons

Jet ↓ Defⁿ

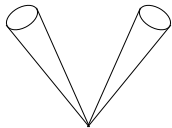
jet 1 jet 2



NLO partons

Jet ↓ Defⁿ

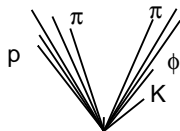
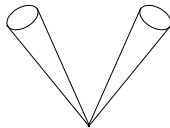
jet 1 jet 2



parton shower

Jet ↓ Defⁿ

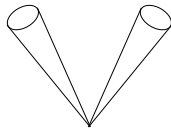
jet 1 jet 2



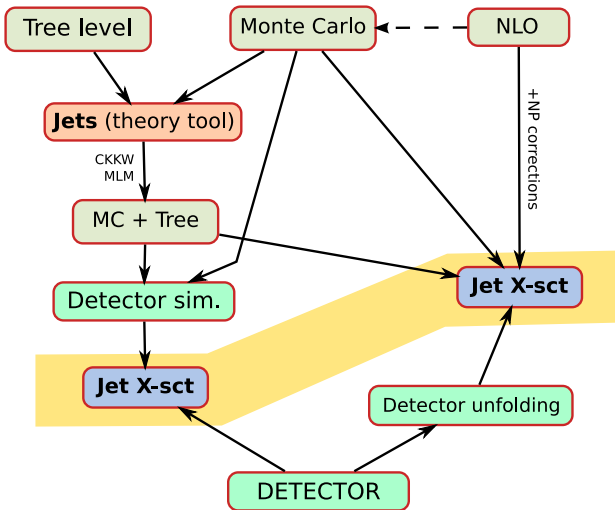
hadron level

Jet ↓ Defⁿ

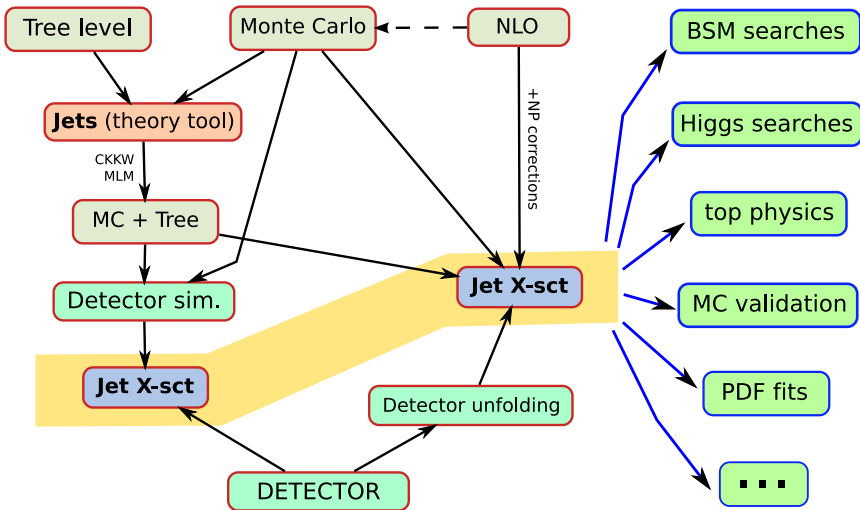
jet 1 jet 2



Projection to jets should be resilient to QCD effects



Jet (definitions) provide central link between expt., "theory" and theory
And jets are an input to almost all analyses



Jet (definitions) provide central link between expt., “theory” and theory
And jets are an input to almost all analyses

- ▶ The different kinds of jet algorithm
- ▶ The historical problems with them (“Snowmass criteria”) and some of the solutions
Speed, infrared safety
- ▶ Understanding the physics of jet algorithms
the momentum of a jet v. the momentum of a “parton”
- ▶ Doing better physics *with* jets
Dijet mass reconstruction
Low-mass Higgs-boson search

What jet algorithms are out there?

2 broad classes:

1. sequential recombination

“bottom up”, e.g. k_t , preferred by many theorists

2. cone type

“top down”, preferred by many experimenters

k_t algorithm

Catani, Dokshitzer, Olsson, Seymour, Turnock, Webber '91-'93
Ellis, Soper '93

- ▶ Find smallest of all $d_{ij} = \min(k_{ti}^2, k_{tj}^2) \Delta R_{ij}^2 / R^2$ and $d_{iB} = k_i^2$
- ▶ Recombine
- ▶ Repeat

**Bottom-up jets:
Sequential recombination
(attempt to invert QCD branching)**

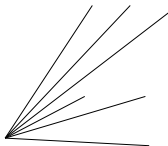


- variables
- ▶ $\Delta R_{ij} = (\phi_i - \phi_j)^2 + (y_i - y_j)^2$
 - ▶ rapidity $y_i = \frac{1}{2} \ln \frac{E_i + p_{zi}}{E_i - p_{zi}}$
 - ▶ ΔR_{ij} is boost invariant angle

k_t algorithm

Catani, Dokshitzer, Olsson, Seymour, Turnock, Webber '91-'93
Ellis, Soper '93

- ▶ Find smallest of all $d_{ij} = \min(k_{ti}^2, k_{tj}^2) \Delta R_{ij}^2 / R^2$ and $d_{iB} = k_i^2$
- ▶ Recombine i, j (if iB : $i \rightarrow \text{jet}$)
- ▶ Repeat



NB: hadron collider variables

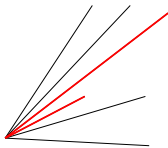
- ▶ $\Delta R_{ij}^2 = (\phi_i - \phi_j)^2 + (y_i - y_j)^2$
- ▶ rapidity $y_i = \frac{1}{2} \ln \frac{E_i + p_{zi}}{E_i - p_{zi}}$
- ▶ ΔR_{ij} is boost invariant angle

R sets minimal interjet angle

k_t algorithm

Catani, Dokshitzer, Olsson, Seymour, Turnock, Webber '91-'93
Ellis, Soper '93

- ▶ Find **smallest of all** $d_{ij} = \min(k_{ti}^2, k_{tj}^2) \Delta R_{ij}^2 / R^2$ and $d_{iB} = k_i^2$
- ▶ Recombine i, j (if iB : $i \rightarrow \text{jet}$)
- ▶ Repeat



NB: hadron collider variables

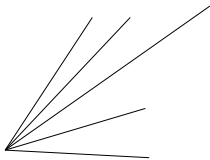
- ▶ $\Delta R_{ij}^2 = (\phi_i - \phi_j)^2 + (y_i - y_j)^2$
- ▶ rapidity $y_i = \frac{1}{2} \ln \frac{E_i + p_{zi}}{E_i - p_{zi}}$
- ▶ ΔR_{ij} is boost invariant angle

R sets minimal interjet angle

k_t algorithm

Catani, Dokshitzer, Olsson, Seymour, Turnock, Webber '91-'93
Ellis, Soper '93

- ▶ Find smallest of all $d_{ij} = \min(k_{ti}^2, k_{tj}^2) \Delta R_{ij}^2 / R^2$ and $d_{iB} = k_i^2$
- ▶ **Recombine** i, j (if iB : $i \rightarrow \text{jet}$)
- ▶ Repeat



NB: hadron collider variables

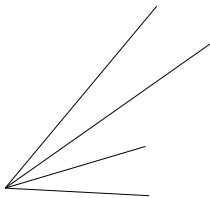
- ▶ $\Delta R_{ij}^2 = (\phi_i - \phi_j)^2 + (y_i - y_j)^2$
- ▶ rapidity $y_i = \frac{1}{2} \ln \frac{E_i + p_{zi}}{E_i - p_{zi}}$
- ▶ ΔR_{ij} is boost invariant angle

R sets minimal interjet angle

k_t algorithm

Catani, Dokshitzer, Olsson, Seymour, Turnock, Webber '91-'93
Ellis, Soper '93

- ▶ Find smallest of all $d_{ij} = \min(k_{ti}^2, k_{tj}^2) \Delta R_{ij}^2 / R^2$ and $d_{iB} = k_i^2$
- ▶ Recombine i, j (if iB : $i \rightarrow \text{jet}$)
- ▶ Repeat



NB: hadron collider variables

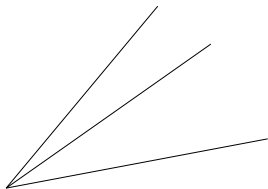
- ▶ $\Delta R_{ij}^2 = (\phi_i - \phi_j)^2 + (y_i - y_j)^2$
- ▶ rapidity $y_i = \frac{1}{2} \ln \frac{E_i + p_{zi}}{E_i - p_{zi}}$
- ▶ ΔR_{ij} is boost invariant angle

R sets minimal interjet angle

k_t algorithm

Catani, Dokshitzer, Olsson, Seymour, Turnock, Webber '91-'93
Ellis, Soper '93

- ▶ Find smallest of all $d_{ij} = \min(k_{ti}^2, k_{tj}^2) \Delta R_{ij}^2 / R^2$ and $d_{iB} = k_i^2$
- ▶ Recombine i, j (if iB : $i \rightarrow \text{jet}$)
- ▶ Repeat



NB: hadron collider variables

- ▶ $\Delta R_{ij}^2 = (\phi_i - \phi_j)^2 + (y_i - y_j)^2$
- ▶ rapidity $y_i = \frac{1}{2} \ln \frac{E_i + p_{zi}}{E_i - p_{zi}}$
- ▶ ΔR_{ij} is boost invariant angle

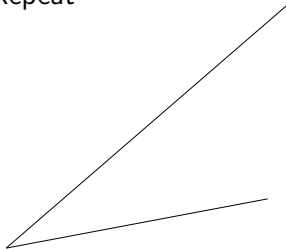
R sets minimal interjet angle

Sequential recombination algorithms

k_t algorithm

Catani, Dokshitzer, Olsson, Seymour, Turnock, Webber '91-'93
Ellis, Soper '93

- ▶ Find smallest of all $d_{ij} = \min(k_{ti}^2, k_{tj}^2) \Delta R_{ij}^2 / R^2$ and $d_{iB} = k_i^2$
- ▶ Recombine i, j (if iB : $i \rightarrow \text{jet}$)
- ▶ Repeat



NB: hadron collider variables

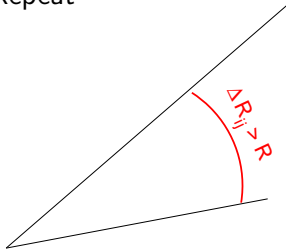
- ▶ $\Delta R_{ij}^2 = (\phi_i - \phi_j)^2 + (y_i - y_j)^2$
- ▶ rapidity $y_i = \frac{1}{2} \ln \frac{E_i + p_{zi}}{E_i - p_{zi}}$
- ▶ ΔR_{ij} is boost invariant angle

R sets minimal interjet angle

k_t algorithm

Catani, Dokshitzer, Olsson, Seymour, Turnock, Webber '91-'93
Ellis, Soper '93

- ▶ Find smallest of all $d_{ij} = \min(k_{ti}^2, k_{tj}^2) \Delta R_{ij}^2 / R^2$ and $d_{iB} = k_i^2$
- ▶ Recombine i, j (if iB : $i \rightarrow \text{jet}$)
- ▶ Repeat



NB: hadron collider variables

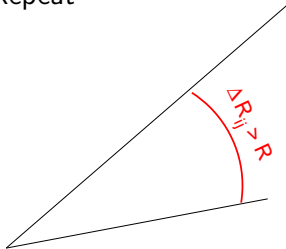
- ▶ $\Delta R_{ij}^2 = (\phi_i - \phi_j)^2 + (y_i - y_j)^2$
- ▶ rapidity $y_i = \frac{1}{2} \ln \frac{E_i + p_{zi}}{E_i - p_{zi}}$
- ▶ ΔR_{ij} is boost invariant angle

R sets minimal interjet angle

k_t algorithm

Catani, Dokshitzer, Olsson, Seymour, Turnock, Webber '91-'93
Ellis, Soper '93

- ▶ Find smallest of all $d_{ij} = \min(k_{ti}^2, k_{tj}^2) \Delta R_{ij}^2 / R^2$ and $d_{iB} = k_i^2$
- ▶ Recombine i, j (if iB : $i \rightarrow \text{jet}$)
- ▶ Repeat



NB: hadron collider variables


- ▶ $\Delta R_{ij}^2 = (\phi_i - \phi_j)^2 + (y_i - y_j)^2$
- ▶ rapidity $y_i = \frac{1}{2} \ln \frac{E_i + p_{zi}}{E_i - p_{zi}}$
- ▶ ΔR_{ij} is boost invariant angle

R sets minimal interjet angle

NB: d_{ij} distance \leftrightarrow QCD branching probability $\sim \alpha_s \frac{dk_{tj}^2 dR_{ij}^2}{d_{ij}}$

Tevatron & ATLAS cone algs have two main steps:

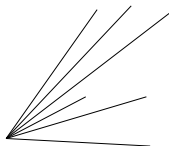
- ▶ Find some/all stable cones
 - ≡ cone pointing in same direction as the momentum of its contents
 - Found by iterating from some initial seed directions
- ▶ Resolve cases of overlapping stable cones



**Top-down jets:
cone algorithms
(energy flow conserved by QCD)**

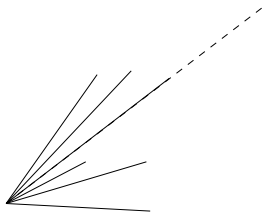
Tevatron & ATLAS cone algs have two main steps:

- ▶ Find some/all stable cones
 - ≡ cone pointing in same direction as the momentum of its contents
 - Found by iterating from some initial seed directions
- ▶ Resolve cases of overlapping stable cones
 - By running a 'split-merge' procedure



Tevatron & ATLAS cone algs have two main steps:

- ▶ Find some/all stable cones
 - ≡ cone pointing in same direction as the momentum of its contents
 - Found by iterating from some initial seed directions
- ▶ Resolve cases of overlapping stable cones
 - By running a 'split-merge' procedure



Tevatron & ATLAS cone algs have two main steps:

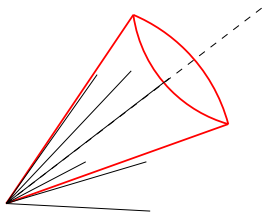
► Find some/all stable cones

≡ cone pointing in same direction as the momentum of its contents

Found by iterating from some initial seed directions

► Resolve cases of overlapping stable cones

By running a 'split-merge' procedure



Tevatron & ATLAS cone algs have two main steps:

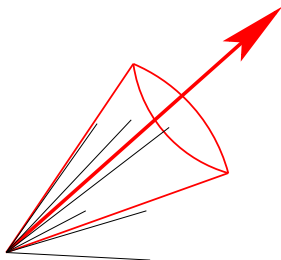
► Find some/all stable cones

≡ cone pointing in same direction as the momentum of its contents

Found by iterating from some initial seed directions

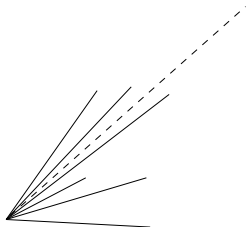
► Resolve cases of overlapping stable cones

By running a 'split-merge' procedure



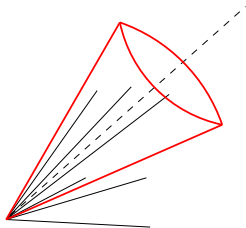
Tevatron & ATLAS cone algs have two main steps:

- ▶ Find some/all stable cones
 - ≡ cone pointing in same direction as the momentum of its contents
 - Found by iterating from some initial seed directions
- ▶ Resolve cases of overlapping stable cones
 - By running a 'split-merge' procedure



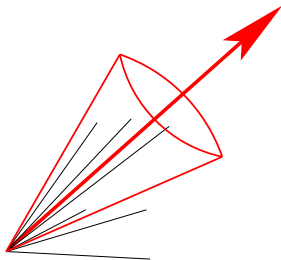
Tevatron & ATLAS cone algs have two main steps:

- ▶ Find some/all stable cones
 - ≡ cone pointing in same direction as the momentum of its contents
 - Found by iterating from some initial seed directions
- ▶ Resolve cases of overlapping stable cones
 - By running a 'split-merge' procedure



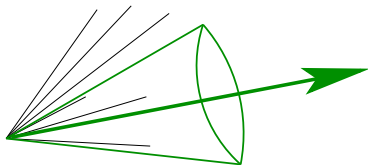
Tevatron & ATLAS cone algs have two main steps:

- ▶ Find some/all stable cones
 - ≡ cone pointing in same direction as the momentum of its contents
 - Found by iterating from some initial seed directions
- ▶ Resolve cases of overlapping stable cones
 - By running a 'split-merge' procedure



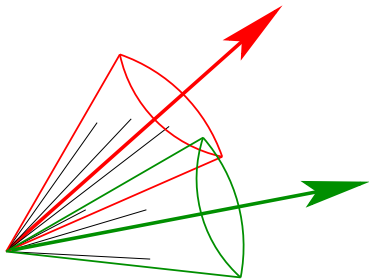
Tevatron & ATLAS cone algs have two main steps:

- ▶ Find some/all stable cones
 - ≡ cone pointing in same direction as the momentum of its contents
 - Found by iterating from some initial seed directions
- ▶ Resolve cases of overlapping stable cones
 - By running a 'split-merge' procedure



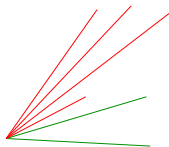
Tevatron & ATLAS cone algs have two main steps:

- ▶ Find some/all stable cones
 - ≡ cone pointing in same direction as the momentum of its contents
 - Found by iterating from some initial seed directions
- ▶ Resolve cases of overlapping stable cones
 - By running a 'split-merge' procedure



Tevatron & ATLAS cone algs have two main steps:

- ▶ Find some/all stable cones
 - ≡ cone pointing in same direction as the momentum of its contents
 - Found by iterating from some initial seed directions
- ▶ Resolve cases of overlapping stable cones
 - By running a 'split-merge' procedure

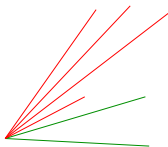


Tevatron & ATLAS cone algs have two main steps:

- ▶ Find some/all stable cones
 - ≡ cone pointing in same direction as the momentum of its contents
 - Found by iterating from some initial seed directions
- ▶ Resolve cases of overlapping stable cones
 - By running a 'split-merge' procedure

What seeds do you use?

- ▶ All particles above some threshold
 - Done originally [JetClu, Atlas]
- ▶ Additionally from 'midpoints' between stable cones
 - Midpoint cone [Tevatron Run II]

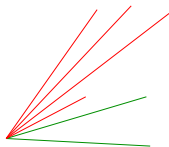


Tevatron & ATLAS cone algs have two main steps:

- ▶ Find some/all stable cones
 - ≡ cone pointing in same direction as the momentum of its contents
 - Found by iterating from some initial seed directions
- ▶ Resolve cases of overlapping stable cones
 - By running a 'split-merge' procedure

What seeds do you use?

- ▶ All particles above some threshold
 - Done originally [JetClu, Atlas]
- ▶ Additionally from 'midpoints' between stable cones
 - Midpoint cone [Tevatron Run II]



Readying jet “technology” for the LHC era

[a.k.a. satisfying Snowmass]

Snowmass Accord (1990):

FERMILAB-Conf-90/249-E
[E-741/CDF]

Toward a Standardization of Jet Definitions *

Several important properties that should be met by a jet definition are [3]:

1. Simple to implement in an experimental analysis;
2. Simple to implement in the theoretical calculation;
3. Defined at any order of perturbation theory;
4. Yields finite cross section at any order of perturbation theory;
5. Yields a cross section that is relatively insensitive to hadronization.

Snowmass Accord (1990):

FERMILAB-Conf-90/249-E
[E-741/CDF]

Toward a Standardization of Jet Definitions *

Several important properties that should be met by a jet definition are [3]:

1. Simple to implement in an experimental analysis;
2. Simple to implement in the theoretical calculation;
3. Defined at any order of perturbation theory;
4. Yields finite cross section at any order of perturbation theory;

Property 1 \Leftrightarrow speed. (+other aspects)

- ▶ LHC events may have up to $N = 4000$ particles (at high-lumi)
- ▶ Sequential recombination algs. (k_t) slow, $\sim N^3 \rightarrow 60s$ for $N = 4000$, not practical for $\mathcal{O}(10^9)$ events

Can be reduced to $N \ln N$ ($60s \rightarrow 20ms$) Cacciari & GPS '05 + CGAL

Snowmass Accord (1990):

FERMILAB-Conf-90/249-E
[E-741/CDF]

Toward a Standardization of Jet Definitions *

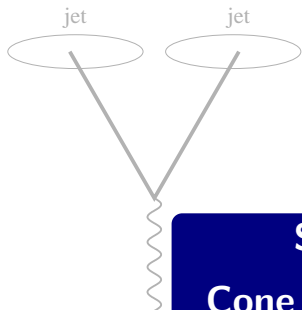
Several important properties that should be met by a jet definition are [3]:

1. Simple to implement in an experimental analysis;
2. Simple to implement in the theoretical calculation;
3. Defined at any order of perturbation theory;
4. Yields finite cross section at any order of perturbation theory;
5. Yields a cross section that is relatively insensitive to hadronization.

Property 4 \equiv Infrared and Collinear (IRC) Safety. It helps ensure:

- ▶ Soft (low-energy) emissions & collinear splittings don't change jets
- ▶ Each order of perturbation theory is smaller than previous (at high p_t)

Wasn't satisfied by the cone algorithms

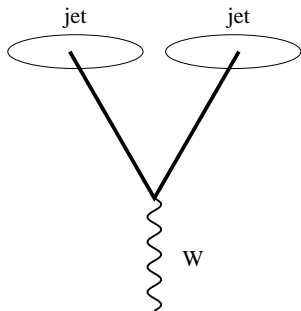


Snowmass issue #4
Cone algorithms and IR safety

1-jet $\alpha_s^2 \alpha_{EW}$
2-jet $\mathcal{O}(1)$

$\alpha_s^3 \alpha_{EW}$
 $-\infty$

$\alpha_s^3 \alpha_{EW}$
 $+\infty$
 0



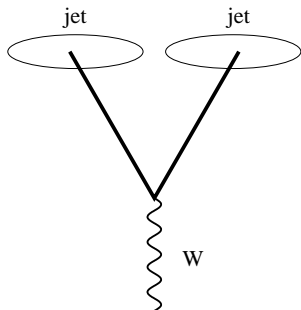
1-jet $\alpha_s^2 \alpha_{EW}$
2-jet $\mathcal{O}(1)$

$\alpha_s^3 \alpha_{EW}$
 $-\infty$

$\alpha_s^3 \alpha_{EW}$
 $+\infty$
 0

With these (& most) cone algorithms, perturbative infinities fail to cancel at some order \equiv IR unsafety

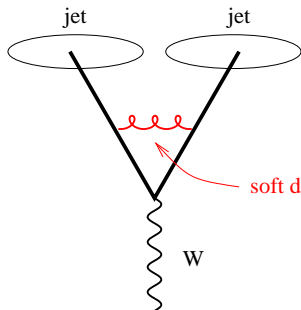
JetClu (& Atlas Cone) in Wjj @ NLO



$$\alpha_s^2 \alpha_{EW}$$

1-jet

2-jet $\mathcal{O}(1)$



$$\alpha_s^3 \alpha_{EW}$$

$-\infty$

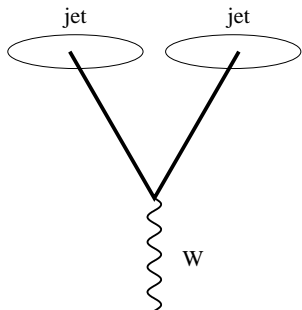
$$\alpha_s^3 \alpha_{EW}$$

$+\infty$

0

With these (& most) cone algorithms, perturbative infinities fail to cancel at some order \equiv IR unsafety

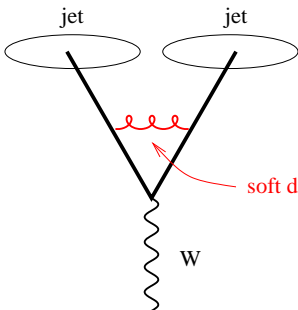
JetClu (& Atlas Cone) in Wjj @ NLO



$$\alpha_s^2 \alpha_{EW}$$

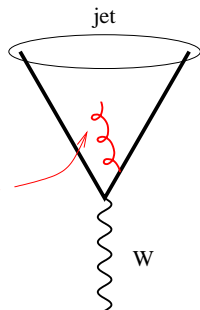
1-jet

2-jet $\mathcal{O}(1)$



$$\alpha_s^3 \alpha_{EW}$$

$-\infty$



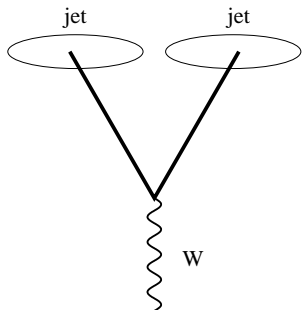
$$\alpha_s^3 \alpha_{EW}$$

$+\infty$

0

With these (& most) cone algorithms, perturbative infinities fail to cancel at some order \equiv IR unsafety

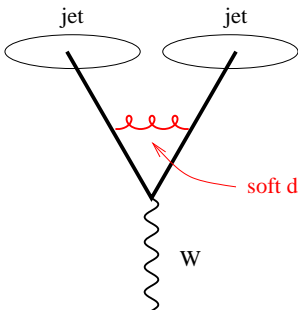
JetClu (& Atlas Cone) in Wjj @ NLO



$$\alpha_s^2 \alpha_{EW}$$

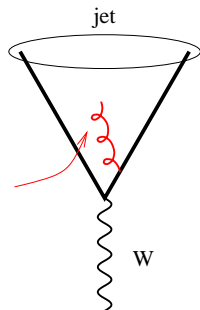
1-jet

2-jet $\mathcal{O}(1)$



$$\alpha_s^3 \alpha_{EW}$$

$-\infty$



$$\alpha_s^3 \alpha_{EW}$$

$+\infty$

0

With these (& most) cone algorithms, perturbative infinities fail to cancel at some order \equiv **IR unsafety**

Real life does not have infinities, but pert. infinity leaves a real-life trace

$$\alpha_s^2 + \alpha_s^3 + \alpha_s^4 \times \infty \rightarrow \alpha_s^2 + \alpha_s^3 + \alpha_s^4 \times \ln p_t/\Lambda \rightarrow \alpha_s^2 + \underbrace{\alpha_s^3 + \alpha_s^3}_{\text{BOTH WASTED}}$$

Among consequences of IR unsafety:

	<i>Last meaningful order</i>			Known at
	JetClu, ATLAS cone [IC-SM]	MidPoint [IC _{mp} -SM]	CMS it. cone [IC-PR]	
Inclusive jets	LO	NLO	NLO	NLO (→ NNLO)
W/Z + 1 jet	LO	NLO	NLO	NLO
3 jets	none	LO	LO	NLO [nlojet++]
W/Z + 2 jets	none	LO	LO	NLO [MCFM]
m_{jet} in $2j + X$	none	none	none	LO

NB: 50,000,000\$/£/CHF/€ investment in NLO

Multi-jet contexts much more sensitive: **ubiquitous at LHC**

And LHC will rely on QCD for background double-checks
 extraction of cross sections, extraction of parameters

Real life does not have infinities, but pert. infinity leaves a real-life trace

$$\alpha_s^2 + \alpha_s^3 + \alpha_s^4 \times \infty \rightarrow \alpha_s^2 + \alpha_s^3 + \alpha_s^4 \times \ln p_t/\Lambda \rightarrow \alpha_s^2 + \underbrace{\alpha_s^3 + \alpha_s^3}_{\text{BOTH WASTED}}$$

Among consequences of IR unsafety:

	<i>Last meaningful order</i>			Known at
	JetClu, ATLAS cone [IC-SM]	MidPoint [IC _{mp} -SM]	CMS it. cone [IC-PR]	
Inclusive jets	LO	NLO	NLO	NLO (→ NNLO)
W/Z + 1 jet	LO	NLO	NLO	NLO
3 jets	none	LO	LO	NLO [nlojet++]
W/Z + 2 jets	none	LO	LO	NLO [MCFM]
m _{jet} in 2j + X	none	none	none	LO

NB: 50,000,000\$/£/CHF/€ investment in NLO

Multi-jet contexts much more sensitive: **ubiquitous at LHC**

And LHC will rely on QCD for background double-checks
 extraction of cross sections, extraction of parameters

Real life does not have infinities, but pert. infinity leaves a real-life trace

$$\alpha_s^2 + \alpha_s^3 + \alpha_s^4 \times \infty \rightarrow \alpha_s^2 + \alpha_s^3 + \alpha_s^4 \times \ln p_t/\Lambda \rightarrow \alpha_s^2 + \underbrace{\alpha_s^3 + \alpha_s^3}_{\text{BOTH WASTED}}$$

Among consequences of IR unsafety:

	<i>Last meaningful order</i>			Known at
	JetClu, ATLAS cone [IC-SM]	MidPoint [IC _{mp} -SM]	CMS it. cone [IC-PR]	
Inclusive jets	LO	NLO	NLO	NLO (→ NNLO)
W/Z + 1 jet	LO	NLO	NLO	NLO
3 jets	none	LO	LO	NLO [nlojet++]
W/Z + 2 jets	none	LO	LO	NLO [MCFM]
m_{jet} in $2j + X$	none	none	none	LO

NB: 50,000,000\$/£/CHF/€ investment in NLO

Multi-jet contexts much more sensitive: **ubiquitous at LHC**

And LHC will rely on QCD for background double-checks
 extraction of cross sections, extraction of parameters

How do we solve
cone IR safety
problems?

Fix stable-cone finding



SISCone

GPS & Soyez '07

Same family as Tev. Run II alg

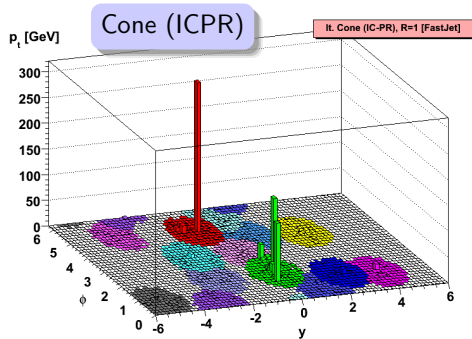
Invent "cone-like" alg.



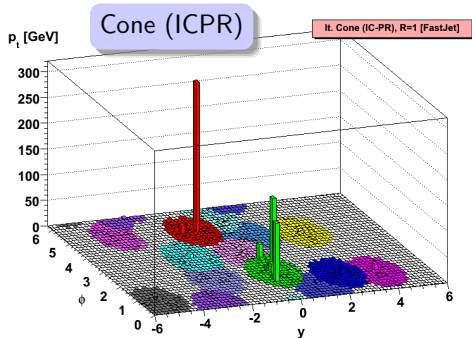
anti-kt

Cacciari, GPS & Soyez '08

Essential characteristic of cones?



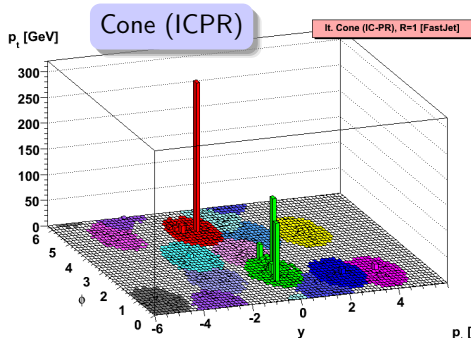
Essential characteristic of cones?



(Some) cone algorithms give **circular** jets in $y - \phi$ plane

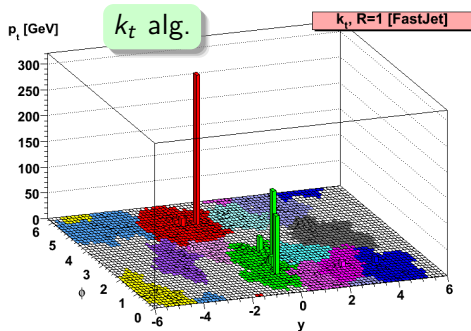
Much appreciated by experiments
e.g. for acceptance corrections

Essential characteristic of cones?

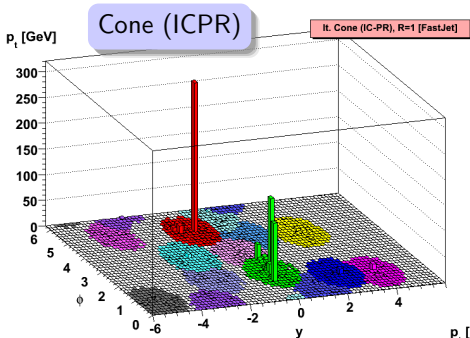


(Some) cone algorithms give **circular** jets in $y - \phi$ plane

Much appreciated by experiments
e.g. for acceptance corrections



Essential characteristic of cones?



(Some) cone algorithms give **circular** jets in $y - \phi$ plane

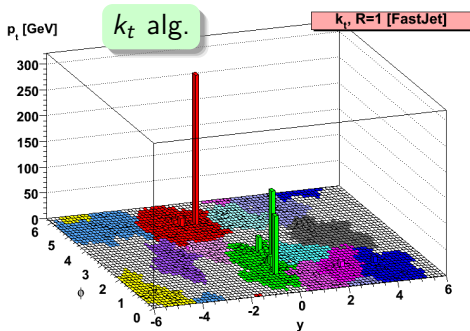
Much appreciated by experiments
e.g. for acceptance corrections

k_t jets are **irregular**

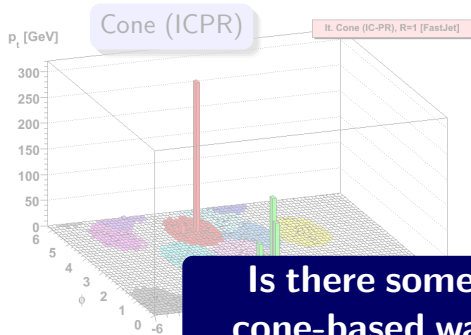
Because soft junk clusters together first:

$$d_{ij} = \min(k_{ti}^2, k_{tj}^2) \Delta R_{ij}^2$$

Regularly held against k_t



Essential characteristic of cones?



(Some) cone algorithms give **circular** jets in $y - \phi$ plane

Much appreciated by experiments e.g. for acceptance corrections

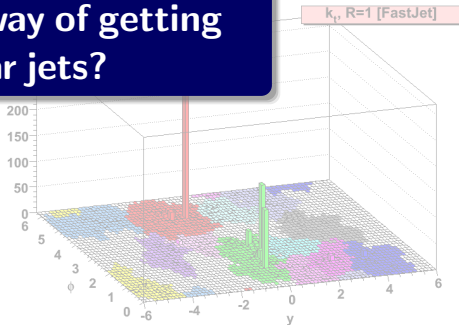
Is there some other, non cone-based way of getting circular jets?

k_t jets are **regularly held**

Because soft junk clusters together first:

$$d_{ij} = \min(k_{ti}^2, k_{tj}^2) \Delta R_{ij}^2$$

Regularly held against k_t



Soft stuff clusters with nearest neighbour

$$k_t: d_{ij} = \min(k_{ti}^2, k_{tj}^2) \Delta R_{ij}^2 \longrightarrow \text{anti-}k_t: d_{ij} = \frac{\Delta R_{ij}^2}{\max(k_{ti}^2, k_{tj}^2)}$$

Hard stuff clusters with nearest neighbour
Privilege collinear divergence over soft divergence
Cacciari, GPS & Soyez '08

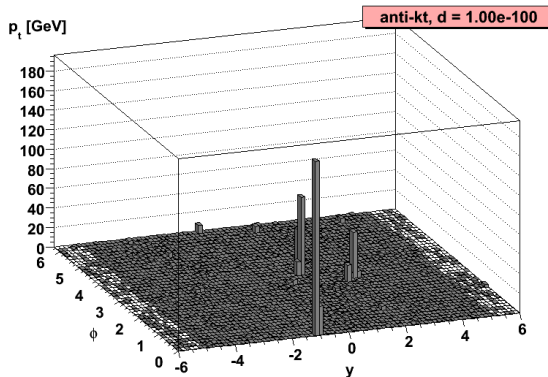
Soft stuff clusters with nearest neighbour

$$k_t: d_{ij} = \min(k_{ti}^2, k_{tj}^2) \Delta R_{ij}^2 \longrightarrow \text{anti-}k_t: d_{ij} = \frac{\Delta R_{ij}^2}{\max(k_{ti}^2, k_{tj}^2)}$$

Hard stuff clusters with nearest neighbour

Privilege collinear divergence over soft divergence

Cacciari, GPS & Soyez '08



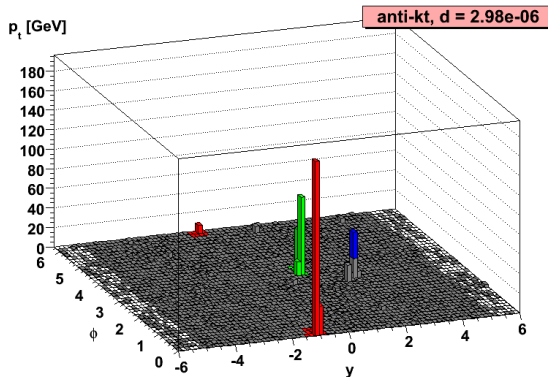
Soft stuff clusters with nearest neighbour

$$k_t: d_{ij} = \min(k_{ti}^2, k_{tj}^2) \Delta R_{ij}^2 \longrightarrow \text{anti-}k_t: d_{ij} = \frac{\Delta R_{ij}^2}{\max(k_{ti}^2, k_{tj}^2)}$$

Hard stuff clusters with nearest neighbour

Privilege collinear divergence over soft divergence

Cacciari, GPS & Soyez '08



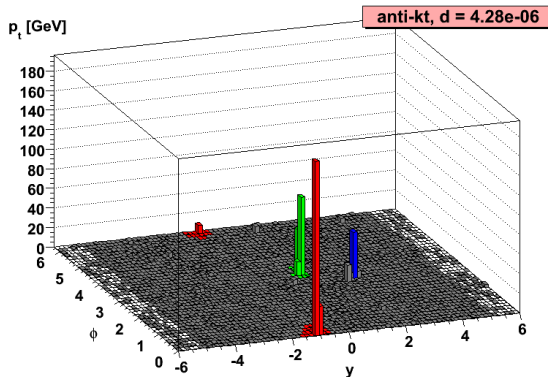
Soft stuff clusters with nearest neighbour

$$k_t: d_{ij} = \min(k_{ti}^2, k_{tj}^2) \Delta R_{ij}^2 \longrightarrow \text{anti-}k_t: d_{ij} = \frac{\Delta R_{ij}^2}{\max(k_{ti}^2, k_{tj}^2)}$$

Hard stuff clusters with nearest neighbour

Privilege collinear divergence over soft divergence

Cacciari, GPS & Soyez '08



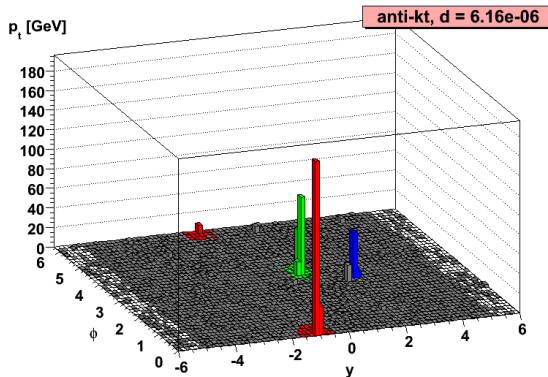
Soft stuff clusters with nearest neighbour

$$k_t: d_{ij} = \min(k_{ti}^2, k_{tj}^2) \Delta R_{ij}^2 \longrightarrow \text{anti-}k_t: d_{ij} = \frac{\Delta R_{ij}^2}{\max(k_{ti}^2, k_{tj}^2)}$$

Hard stuff clusters with nearest neighbour

Privilege collinear divergence over soft divergence

Cacciari, GPS & Soyez '08



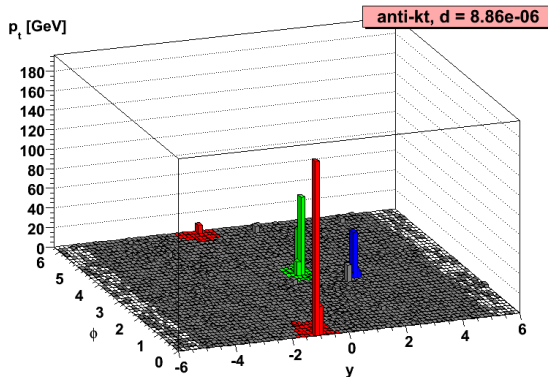
Soft stuff clusters with nearest neighbour

$$k_t: d_{ij} = \min(k_{ti}^2, k_{tj}^2) \Delta R_{ij}^2 \longrightarrow \text{anti-}k_t: d_{ij} = \frac{\Delta R_{ij}^2}{\max(k_{ti}^2, k_{tj}^2)}$$

Hard stuff clusters with nearest neighbour

Privilege collinear divergence over soft divergence

Cacciari, GPS & Soyez '08



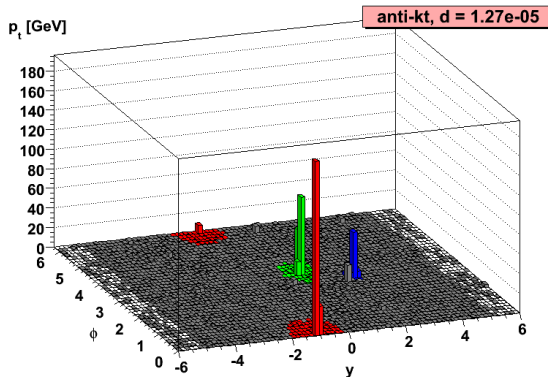
Soft stuff clusters with nearest neighbour

$$k_t: d_{ij} = \min(k_{ti}^2, k_{tj}^2) \Delta R_{ij}^2 \longrightarrow \text{anti-}k_t: d_{ij} = \frac{\Delta R_{ij}^2}{\max(k_{ti}^2, k_{tj}^2)}$$

Hard stuff clusters with nearest neighbour

Privilege collinear divergence over soft divergence

Cacciari, GPS & Soyez '08



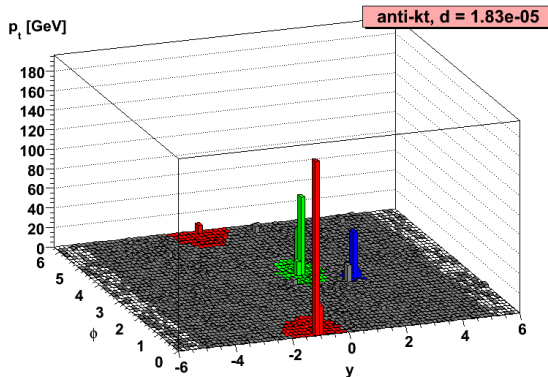
Soft stuff clusters with nearest neighbour

$$k_t: d_{ij} = \min(k_{ti}^2, k_{tj}^2) \Delta R_{ij}^2 \longrightarrow \text{anti-}k_t: d_{ij} = \frac{\Delta R_{ij}^2}{\max(k_{ti}^2, k_{tj}^2)}$$

Hard stuff clusters with nearest neighbour

Privilege collinear divergence over soft divergence

Cacciari, GPS & Soyez '08



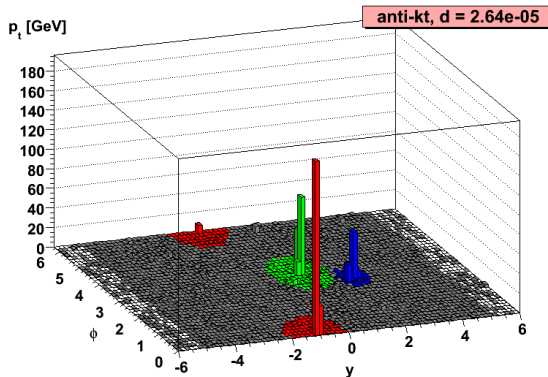
Soft stuff clusters with nearest neighbour

$$k_t: d_{ij} = \min(k_{ti}^2, k_{tj}^2) \Delta R_{ij}^2 \longrightarrow \text{anti-}k_t: d_{ij} = \frac{\Delta R_{ij}^2}{\max(k_{ti}^2, k_{tj}^2)}$$

Hard stuff clusters with nearest neighbour

Privilege collinear divergence over soft divergence

Cacciari, GPS & Soyez '08



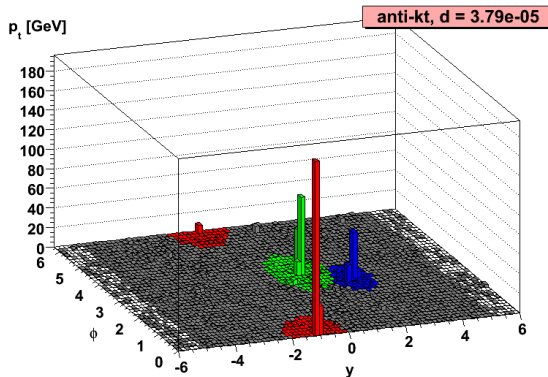
Soft stuff clusters with nearest neighbour

$$k_t: d_{ij} = \min(k_{ti}^2, k_{tj}^2) \Delta R_{ij}^2 \longrightarrow \text{anti-}k_t: d_{ij} = \frac{\Delta R_{ij}^2}{\max(k_{ti}^2, k_{tj}^2)}$$

Hard stuff clusters with nearest neighbour

Privilege collinear divergence over soft divergence

Cacciari, GPS & Soyez '08



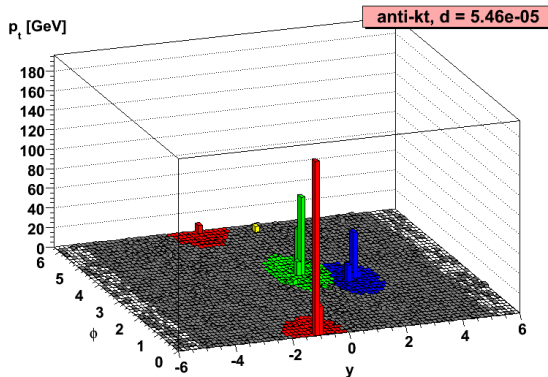
Soft stuff clusters with nearest neighbour

$$k_t: d_{ij} = \min(k_{ti}^2, k_{tj}^2) \Delta R_{ij}^2 \longrightarrow \text{anti-}k_t: d_{ij} = \frac{\Delta R_{ij}^2}{\max(k_{ti}^2, k_{tj}^2)}$$

Hard stuff clusters with nearest neighbour

Privilege collinear divergence over soft divergence

Cacciari, GPS & Soyez '08



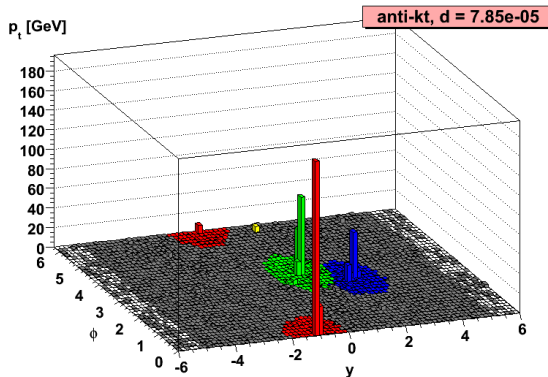
Soft stuff clusters with nearest neighbour

$$k_t: d_{ij} = \min(k_{ti}^2, k_{tj}^2) \Delta R_{ij}^2 \longrightarrow \text{anti-}k_t: d_{ij} = \frac{\Delta R_{ij}^2}{\max(k_{ti}^2, k_{tj}^2)}$$

Hard stuff clusters with nearest neighbour

Privilege collinear divergence over soft divergence

Cacciari, GPS & Soyez '08



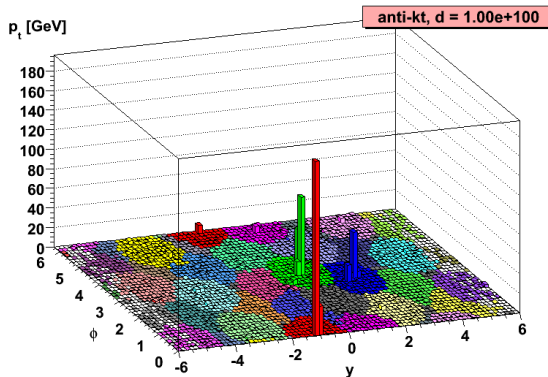
Soft stuff clusters with nearest neighbour

$$k_t: d_{ij} = \min(k_{ti}^2, k_{tj}^2) \Delta R_{ij}^2 \longrightarrow \text{anti-}k_t: d_{ij} = \frac{\Delta R_{ij}^2}{\max(k_{ti}^2, k_{tj}^2)}$$

Hard stuff clusters with nearest neighbour

Privilege collinear divergence over soft divergence

Cacciari, GPS & Soyez '08



anti- k_t gives
cone-like jets
without using stable
cones

Generalise inclusive-type sequential recombination with

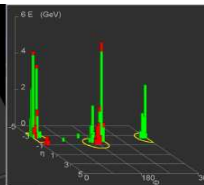
$$d_{ij} = \min(k_{ti}^{2p}, k_{tj}^{2p}) \Delta R_{ij}^2 / R^2 \quad d_{iB} = k_{ti}^{2p}$$

	Alg. name	Comment	time
$p = 1$	k_t CDOSTW '91-93; ES '93	Hierarchical in rel. k_t	$N \ln N$ exp.
$p = 0$	Cambridge/Aachen Dok, Leder, Moretti, Webber '97 Wengler, Wobisch '98	Hierarchical in angle Scan multiple R at once ↔ QCD angular ordering	$N \ln N$
$p = -1$	anti- k_t Cacciari, GPS, Soyez '08 ~ reverse- k_t Delsart	Hierarchy meaningless, jets like CMS cone (IC-PR)	$N^{3/2}$
SC-SM	SISCone GPS Soyez '07 + Tevatron run II '00	Replaces JetClu, ATLAS MidPoint (xC-SM) cones	$N^2 \ln N$ exp.

All these algorithms [& much more] coded in (efficient) C++ at
<http://fastjet.fr/> (Cacciari, GPS & Soyez '05-'09)

ATLAS: first dijet event, with anti- k_t

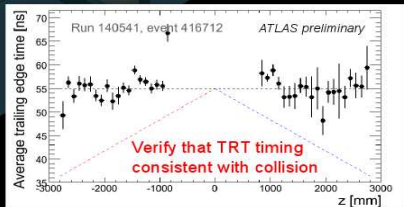
A di-jet candidate



Run 140541
Event 416712

Two jets back-to-back in ϕ , both with (uncalibrated) $E_T \sim 10$ GeV, η of 1.3 and 2.5, \sim no missing E_T

Triggered by MBTS A/B in time, several hits
Also triggered by L1Calo EM3



CMS: first dijet event, with anti- k_t

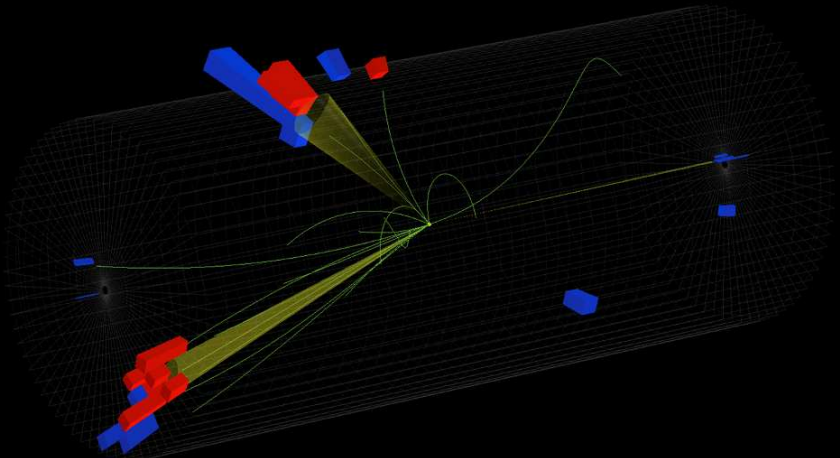


CMS Experiment at the LHC, CERN

Date Recorded: 2009-12-06 07:18 GMT

Run/Event: 123596 / 6732761

Candidate Dijet Collision Event



Snowmass is solved

But it was a problem from the 1990s

What are the problems we *should* be
trying to solve for LHC?

Which jet definition(s) for LHC?

Choice of algorithm (k_t , SISCone, ...)

Choice of parameters (R , ...)

Can we address this question scientifically?

Jetography

Which jet definition(s) for LHC?

Choice of algorithm (k_t , SISCone, ...)

Choice of parameters (R , ...)

Can we address this question scientifically?

Jetography

Jet definitions differ mainly in:

alg + R

1. How close two particles must be to end up in same jet
[discussed in the '90s, e.g. Ellis & Soper]
2. How much perturbative radiation is lost from a jet
[indirectly discussed in the '90s (analytic NLO for inclusive jets)]
3. How much non-perturbative contamination
(hadronisation, UE, pileup) a jet receives
[partially discussed in '90s — Korchemsky & Sterman '95, Seymour '97]

Jet definitions differ mainly in:

$$\text{alg} + R$$

1. How close two particles must be to end up in same jet
[discussed in the '90s, e.g. Ellis & Soper]
2. How much perturbative radiation is lost from a jet
[indirectly discussed in the '90s (analytic NLO for inclusive jets)]
3. How much non-perturbative contamination
(hadronisation, UE, pileup) a jet receives
[partially discussed in '90s — Korchemsky & Sterman '95, Seymour '97]

Jet definitions differ mainly in:

$$\text{alg} + R$$

1. How close two particles must be to end up in same jet
[discussed in the '90s, e.g. Ellis & Soper]
2. How much perturbative radiation is lost from a jet
[indirectly discussed in the '90s (analytic NLO for inclusive jets)]
3. How much non-perturbative contamination
(hadronisation, UE, pileup) a jet receives
[partially discussed in '90s — Korchemsky & Sterman '95, Seymour '97]

The question's dangerous: a "parton" is an ambiguous concept

Three limits can help you:

- ▶ Threshold limit e.g. de Florian & Vogelsang '07
- ▶ Parton from color-neutral object decay (Z')
- ▶ Small- R (radius) limit for jet

One simple result

$$\frac{\langle p_{t,jet} - p_{t,parton} \rangle}{p_t} = \frac{\alpha_s}{\pi} \ln R \times \begin{cases} 1.01 C_F & \text{quarks} \\ 0.94 C_A + 0.07 n_f & \text{gluons} \end{cases} + \mathcal{O}(\alpha_s)$$

only $\mathcal{O}(\alpha_s)$ depends on algorithm & process
cf. Dasgupta, Magnea & GPS '07

Hadronisation: the “parton-shower” \rightarrow hadrons transitionMethod:

- ▶ “infrared finite α_s ” à la Dokshitzer & Webber '95
- ▶ **prediction** based on e^+e^- event shape data
- ▶ could have been deduced from old work Korchensky & Sterman '95
Seymour '97

Main result

$$\langle p_{t,jet} - p_{t,parton-shower} \rangle \simeq -\frac{0.4 \text{ GeV}}{R} \times \begin{cases} C_F & \text{quarks} \\ C_A & \text{gluons} \end{cases}$$

cf. Dasgupta, Magnea & GPS '07
coefficient holds for anti- k_t ; see Dasgupta & Delenda '09 for k_t alg.

“Naive” prediction (UE \simeq colour dipole between pp):

$$\Delta p_t \simeq 0.4 \text{ GeV} \times \frac{R^2}{2} \times \begin{cases} C_F & q\bar{q} \text{ dipole} \\ C_A & \text{gluon dipole} \end{cases}$$

DWT Pythia tune or ATLAS Jimmy tune tell you:

$$\Delta p_t \simeq \mathbf{10 - 15 \text{ GeV}} \times \frac{R^2}{2}$$

This big coefficient motivates special effort to understand interplay between jet algorithm and UE: “jet areas”

How does coefficient depend on algorithm?

How does it depend on jet p_t ? How does it fluctuate?

cf. Cacciari, GPS & Soyez '08

“Naive” prediction (UE \simeq colour dipole between pp):

$$\Delta p_t \simeq 0.4 \text{ GeV} \times \frac{R^2}{2} \times \begin{cases} C_F & q\bar{q} \text{ dipole} \\ C_A & \text{gluon dipole} \end{cases}$$

DWT Pythia tune or ATLAS Jimmy tune tell you:

$$\Delta p_t \simeq \mathbf{10 - 15 \text{ GeV}} \times \frac{R^2}{2}$$

This big coefficient motivates special effort to understand interplay between jet algorithm and UE: “jet areas”

How does coefficient depend on algorithm?

How does it depend on jet p_t ? How does it fluctuate?

cf. Cacciari, GPS & Soyez '08

Jet algorithm properties: summary

	k_t	Cam/Aachen	anti- k_t	SISCone
reach	R	R	R	$(1 + \frac{p_{t2}}{p_{t1}})R$
$\Delta p_{t,PT} \simeq \frac{\alpha_s C_i}{\pi} \times$	$\ln R$	$\ln R$	$\ln R$	$\ln 1.35R$
$\Delta p_{t,hadr} \simeq -\frac{0.4 \text{ GeV} C_i}{R} \times$	0.7	?	1	?
area = $\pi R^2 \times$	0.81 ± 0.28	0.81 ± 0.26	1	0.25
$+ \pi R^2 \frac{C_i}{\pi b_0} \ln \frac{\alpha_s(Q_0)}{\alpha_s(Rp_t)} \times$	0.52 ± 0.41	0.08 ± 0.19	0	0.12 ± 0.07

In words:

- ▶ k_t : area fluctuates a lot, depends on p_t (bad for UE)
- ▶ Cam/Aachen: area fluctuates somewhat, depends less on p_t
- ▶ anti- k_t : area is constant (circular jets)
- ▶ SISCone: reaches far for hard radiation (good for resolution, bad for multijets), area is smaller (good for UE)

Can we benefit from this
understanding in our use of jets?

Jet momentum significantly affected by R

So what R should we choose?

*Examine this in context of reconstruction
of dijet resonance*

What R is best for an isolated jet?

E.g. to reconstruct $m_X \sim (p_{tq} + p_{t\bar{q}})$

PT radiation:

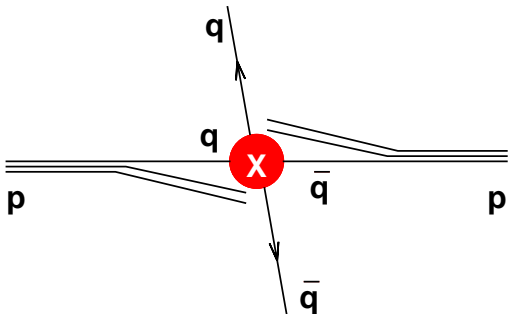
$$q : \langle \Delta p_t \rangle \simeq \frac{\alpha_s C_F}{\pi} p_t \ln R$$

Hadronisation:

$$q : \langle \Delta p_t \rangle \simeq -\frac{C_F}{R} \cdot 0.4 \text{ GeV}$$

Underlying event:

$$q, g : \langle \Delta p_t \rangle \simeq \frac{R^2}{2} \cdot 2.5 - 15 \text{ GeV}$$



Minimise fluctuations in p_t

Use crude approximation:

$$\langle \Delta p_t^2 \rangle \simeq \langle \Delta p_t \rangle^2$$

in small- R limit (!)
 cf. Dasgupta, Magnea & GPS '07

What R is best for an isolated jet?

PT radiation:

$$q : \langle \Delta p_t \rangle \simeq \frac{\alpha_s C_F}{\pi} p_t \ln R$$

Hadronisation:

$$q : \langle \Delta p_t \rangle \simeq -\frac{C_F}{R} \cdot 0.4 \text{ GeV}$$

Underlying event:

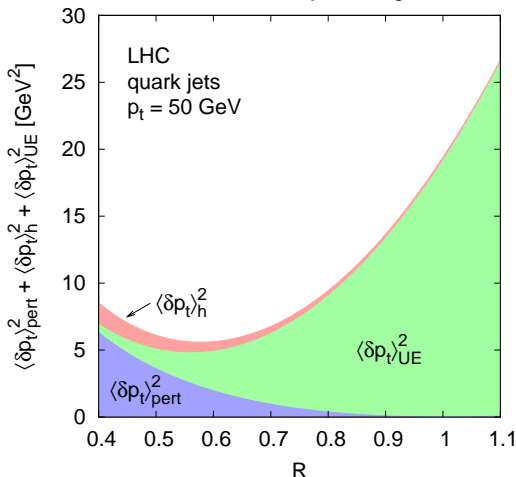
$$q, g : \langle \Delta p_t \rangle \simeq \frac{R^2}{2} \cdot 2.5 - 15 \text{ GeV}$$

Minimise fluctuations in p_t

Use crude approximation:

$$\langle \Delta p_t^2 \rangle \simeq \langle \Delta p_t \rangle^2$$

50 GeV quark jet



in small- R limit (!)

cf. Dasgupta, Magnea & GPS '07

What R is best for an isolated jet?

PT radiation:

$$q : \quad \langle \Delta p_t \rangle \simeq \frac{\alpha_s C_F}{\pi} p_t \ln R$$

Hadronisation:

$$q : \quad \langle \Delta p_t \rangle \simeq -\frac{C_F}{R} \cdot 0.4 \text{ GeV}$$

Underlying event:

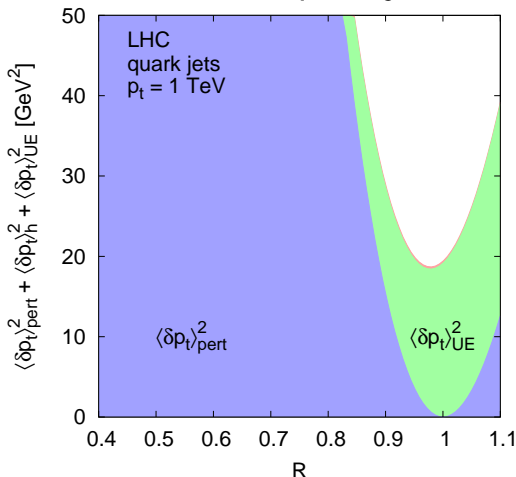
$$q, g : \quad \langle \Delta p_t \rangle \simeq \frac{R^2}{2} \cdot 2.5 - 15 \text{ GeV}$$

Minimise fluctuations in p_t

Use crude approximation:

$$\langle \Delta p_t^2 \rangle \simeq \langle \Delta p_t \rangle^2$$

1 TeV quark jet



in small- R limit (!)

cf. Dasgupta, Magnea & GPS '07

What R is best for an isolated jet?

PT radiation:

$$q : \langle \Delta p_t \rangle \simeq \frac{\alpha_s C_F}{\pi} p_t \ln R$$

Hadronization:

$q :$

At low p_t , small R limits relative impact of UE
At high p_t , perturbative effects dominate over non-perturbative $\rightarrow R_{best} \sim 1$.

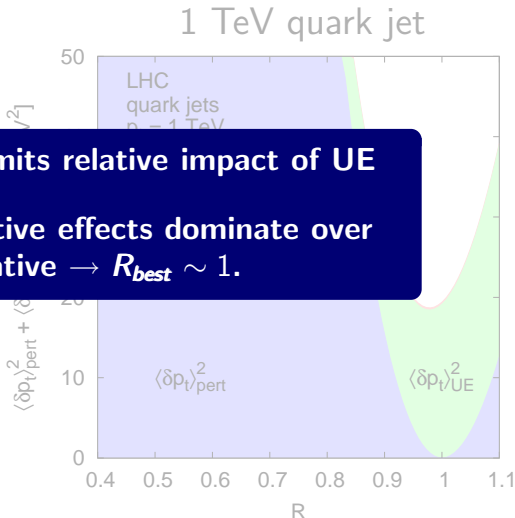
Underlying event:

$$q, g : \langle \Delta p_t \rangle \simeq \frac{R^2}{2} \cdot 2.5 - 15 \text{ GeV}$$

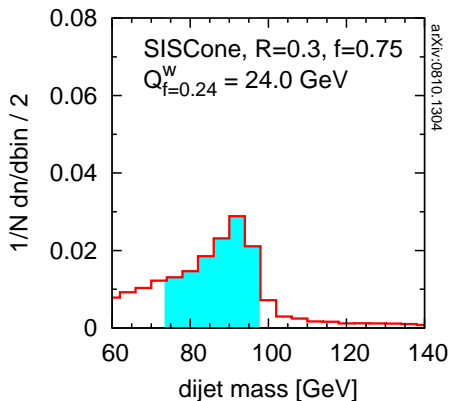
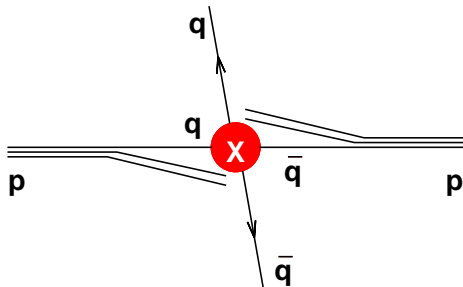
Minimise fluctuations in p_t

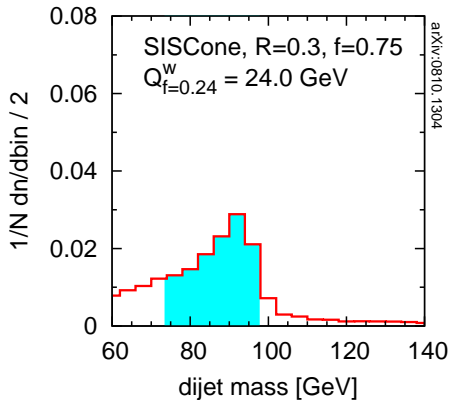
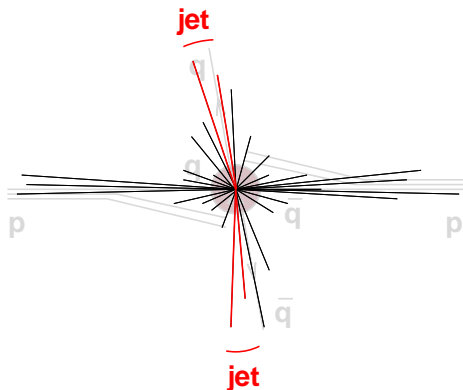
Use crude approximation:

$$\langle \Delta p_t^2 \rangle \simeq \langle \Delta p_t \rangle^2$$



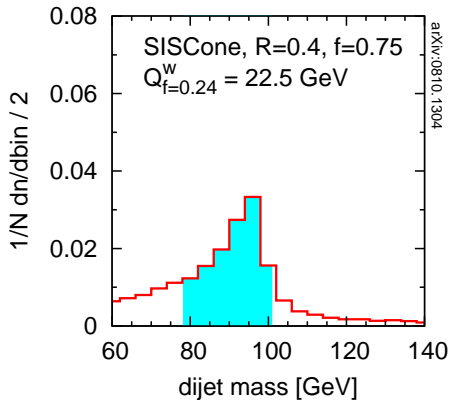
in small- R limit (!)
 cf. Dasgupta, Magnea & GPS '07

$R = 0.3$ $qq, M = 100 \text{ GeV}$ Resonance $X \rightarrow$ dijets

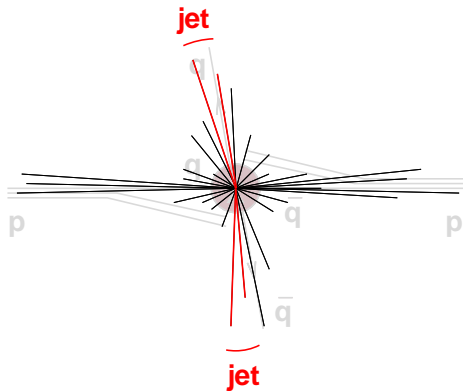
$R = 0.3$ qq, $M = 100$ GeVResonance X \rightarrow dijets

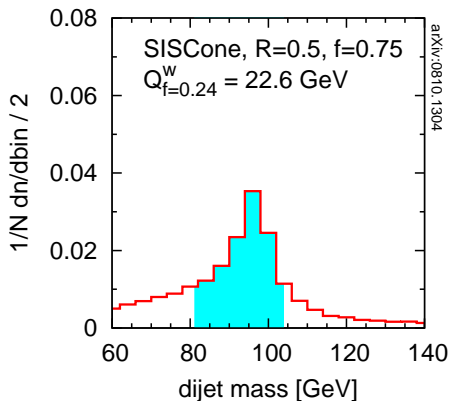
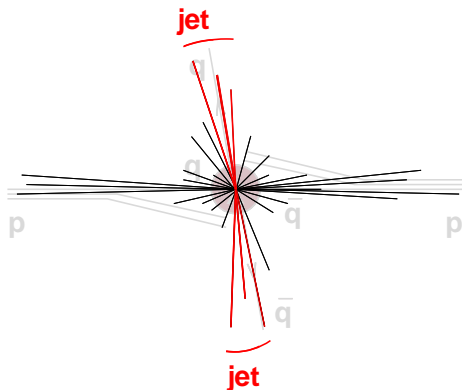
$R = 0.4$

qq , $M = 100$ GeV



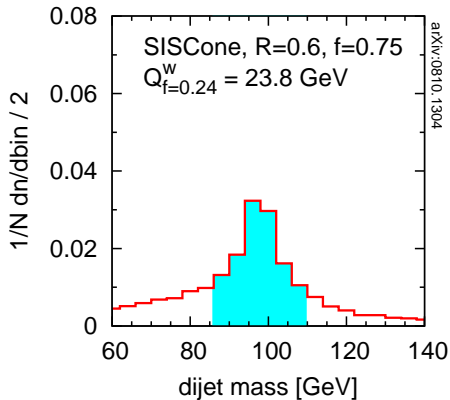
Resonance X \rightarrow dijets



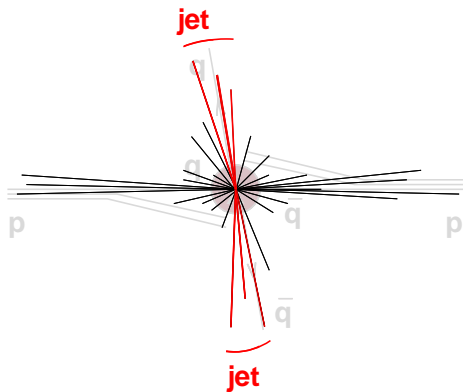
$R = 0.5$ qq, $M = 100$ GeVResonance X \rightarrow dijets

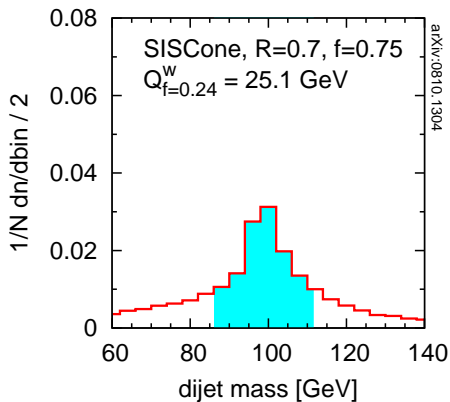
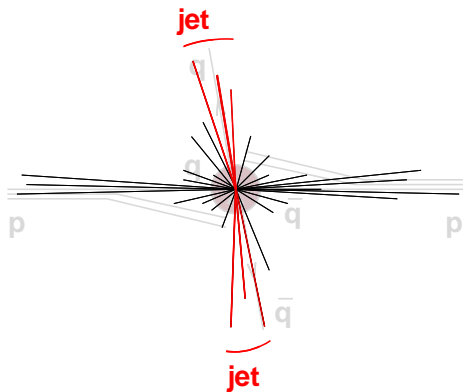
$R = 0.6$

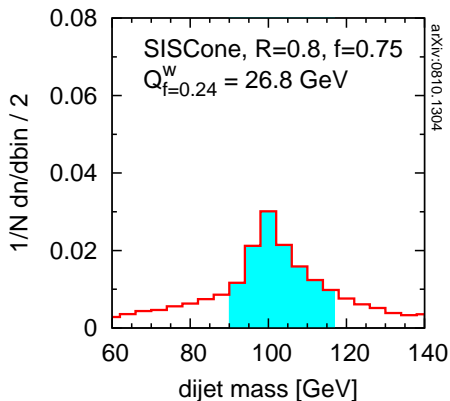
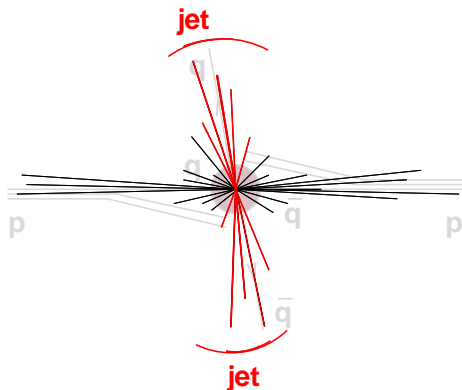
qq, $M = 100$ GeV

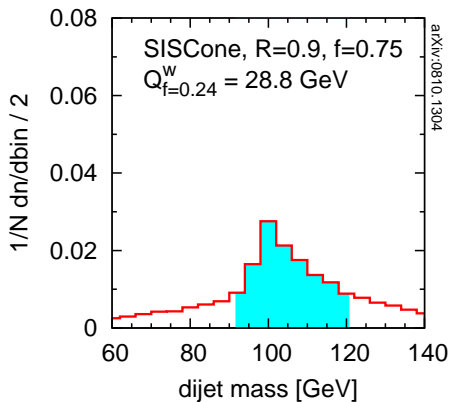
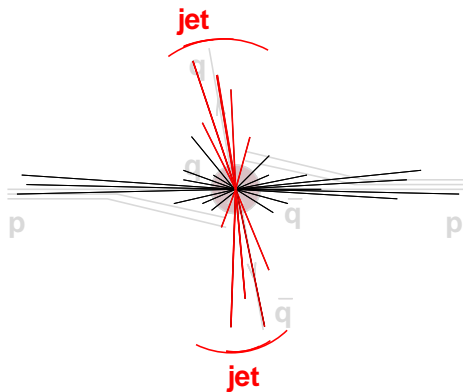


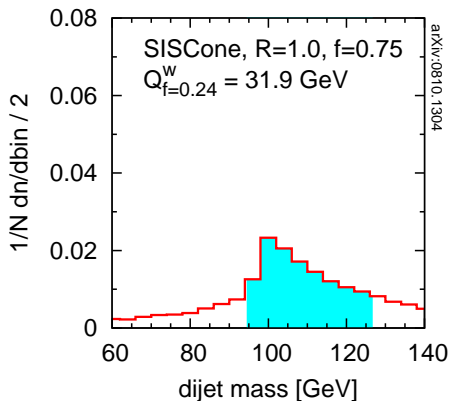
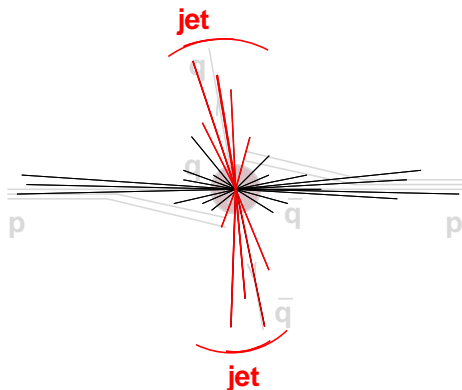
Resonance X \rightarrow dijets

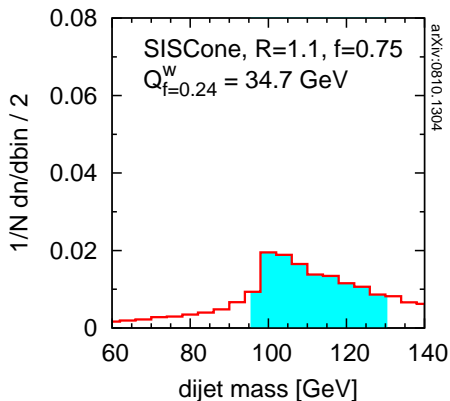
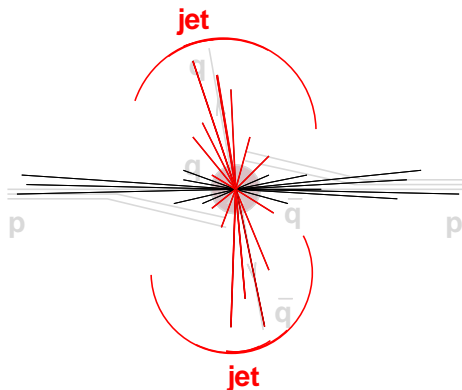


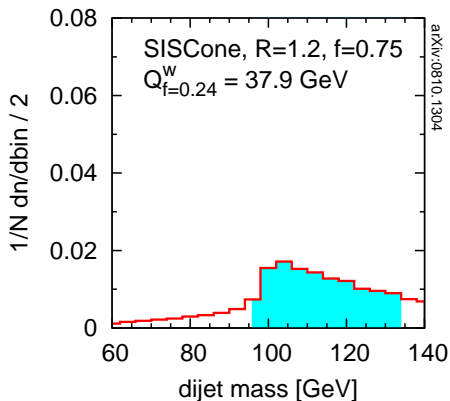
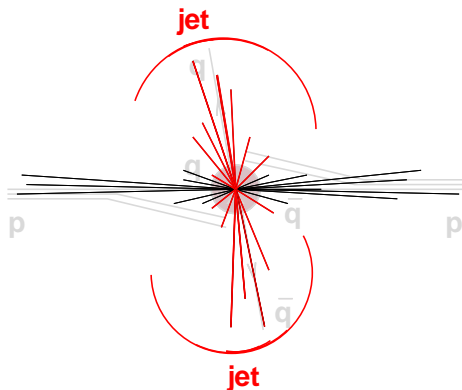
$R = 0.7$ qq, $M = 100$ GeVResonance X \rightarrow dijets

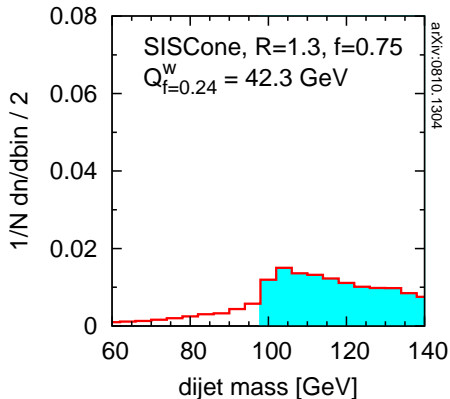
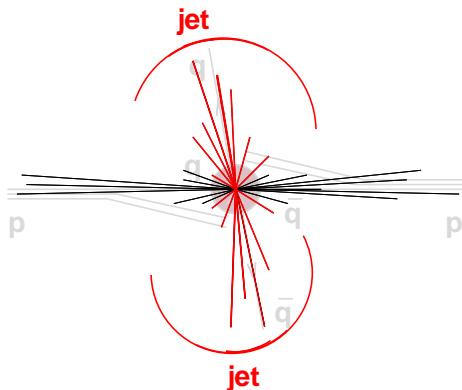
$R = 0.8$ qq, $M = 100$ GeVResonance X \rightarrow dijets

$R = 0.9$ qq, $M = 100$ GeVResonance X \rightarrow dijets

Dijet mass: scan over R [Pythia 6.4] $R = 1.0$ $qq, M = 100 \text{ GeV}$ Resonance X \rightarrow dijets

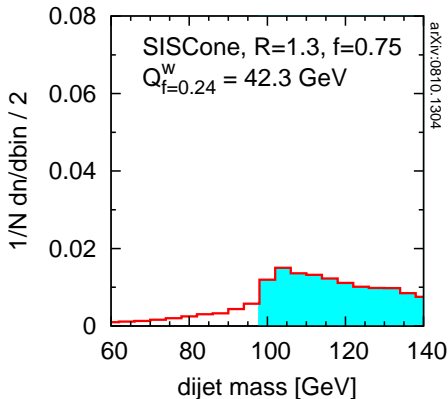
Dijet mass: scan over R [Pythia 6.4] $R = 1.1$ $qq, M = 100 \text{ GeV}$ Resonance X \rightarrow dijets

Dijet mass: scan over R [Pythia 6.4] $R = 1.2$ $qq, M = 100 \text{ GeV}$ Resonance X \rightarrow dijets

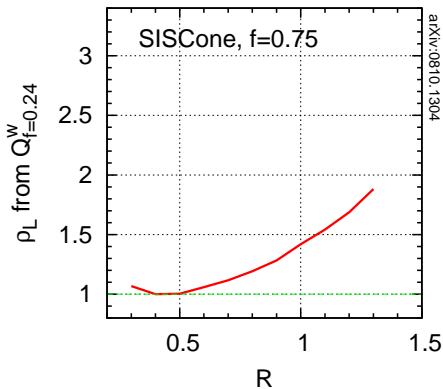
Dijet mass: scan over R [Pythia 6.4] $R = 1.3$ qq, $M = 100$ GeVResonance X \rightarrow dijets

$R = 1.3$

qq, $M = 100$ GeV



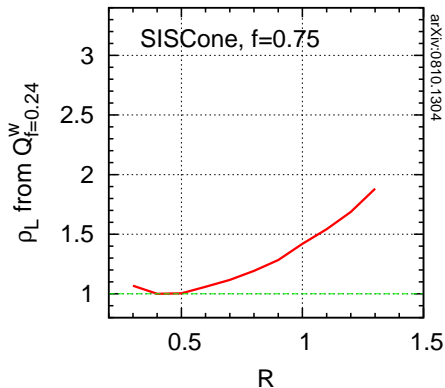
qq, $M = 100$ GeV



After scanning, summarise “quality” v. R . Minimum \equiv BEST
picture not so different from crude analytical estimate

$m_{qq} = 100 \text{ GeV}$

$qq, M = 100 \text{ GeV}$



Best R is at minimum of curve

- ▶ Best R depends strongly on mass of system
- ▶ Increases with mass, just like crude analytical prediction
- NB: current analytics too crude

BUT: so far, LHC's plans involve running with fixed smallish R values

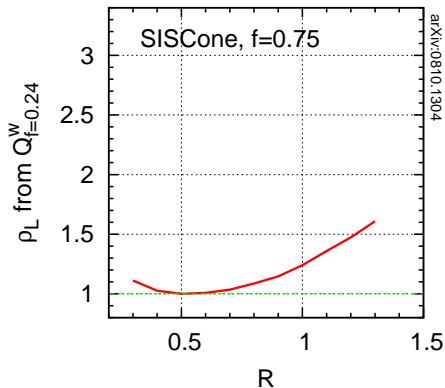
e.g. CMS arXiv:0807.4961

NB: 100,000 plots for various jet algorithms, narrow $q\bar{q}$ and $g\bar{g}$ resonances from <http://quality.fastjet.fr>

Cacciari, Rojo, GPS & Soyez '08

$m_{qq} = 150 \text{ GeV}$

$qq, M = 150 \text{ GeV}$



Best R is at minimum of curve

- Best R depends strongly on mass of system
- Increases with mass, just like crude analytical prediction
NB: current analytics too crude

BUT: so far, LHC's plans involve running with fixed smallish R values

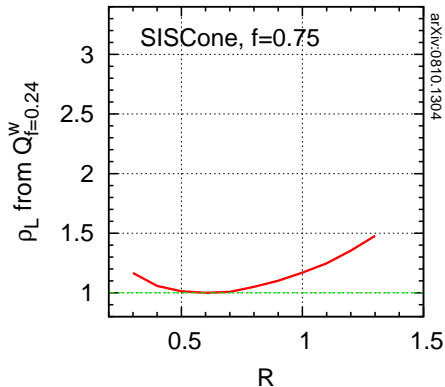
e.g. CMS arXiv:0807.4961

NB: 100,000 plots for various jet algorithms, narrow $q\bar{q}$ and $g\bar{g}$ resonances from <http://quality.fastjet.fr>

Cacciari, Rojo, GPS & Soyez '08

$$m_{qq} = 200 \text{ GeV}$$

$$qq, M = 200 \text{ GeV}$$



Best R is at minimum of curve

- ▶ Best R depends strongly on mass of system
- ▶ Increases with mass, just like crude analytical prediction
- NB: current analytics too crude

BUT: so far, LHC's plans involve running with fixed smallish R values

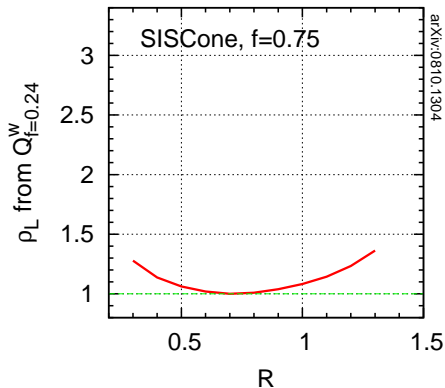
e.g. CMS arXiv:0807.4961

NB: 100,000 plots for various jet algorithms, narrow $q\bar{q}$ and $g\bar{g}$ resonances from <http://quality.fastjet.fr>

Cacciari, Rojo, GPS & Soyez '08

$$m_{qq} = 300 \text{ GeV}$$

$$qq, M = 300 \text{ GeV}$$



Best R is at minimum of curve

- ▶ Best R depends strongly on mass of system
- ▶ Increases with mass, just like crude analytical prediction
- NB: current analytics too crude

BUT: so far, LHC's plans involve running with fixed smallish R values

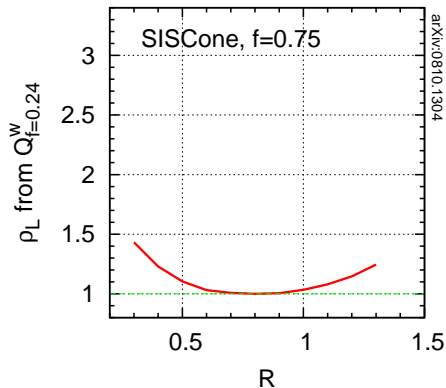
e.g. CMS arXiv:0807.4961

NB: 100,000 plots for various jet algorithms, narrow $q\bar{q}$ and $g\bar{g}$ resonances from <http://quality.fastjet.fr>

Cacciari, Rojo, GPS & Soyez '08

$$m_{qq} = 500 \text{ GeV}$$

$$qq, M = 500 \text{ GeV}$$



Best R is at minimum of curve

- ▶ Best R depends strongly on mass of system
- ▶ Increases with mass, just like crude analytical prediction
- NB: current analytics too crude

BUT: so far, LHC's plans involve running with fixed smallish R values

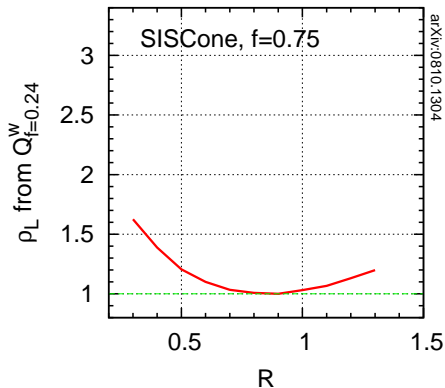
e.g. CMS arXiv:0807.4961

NB: 100,000 plots for various jet algorithms, narrow $q\bar{q}$ and $g\bar{g}$ resonances from <http://quality.fastjet.fr>

Cacciari, Rojo, GPS & Soyez '08

$$m_{qq} = 700 \text{ GeV}$$

$$qq, M = 700 \text{ GeV}$$



Best R is at minimum of curve

- ▶ Best R depends strongly on mass of system
- ▶ Increases with mass, just like crude analytical prediction
NB: current analytics too crude

BUT: so far, LHC's plans involve running with fixed smallish R values

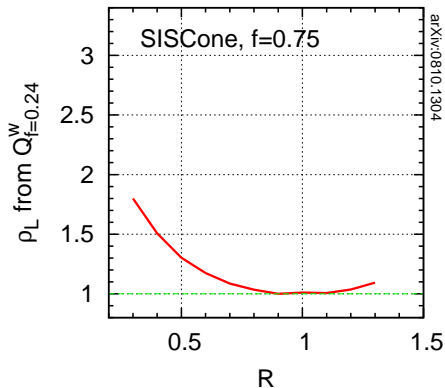
e.g. CMS arXiv:0807.4961

NB: 100,000 plots for various jet algorithms, narrow $q\bar{q}$ and $g\bar{g}$ resonances from <http://quality.fastjet.fr>

Cacciari, Rojo, GPS & Soyez '08

$m_{q\bar{q}} = 1000 \text{ GeV}$

$q\bar{q}, M = 1000 \text{ GeV}$



Best R is at minimum of curve

- ▶ Best R depends strongly on mass of system
- ▶ Increases with mass, just like crude analytical prediction
NB: current analytics too crude

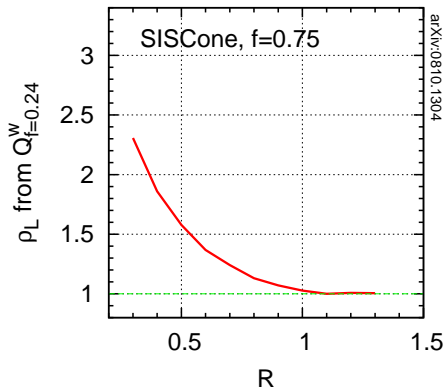
BUT: so far, LHC's plans involve running with fixed smallish R values

e.g. CMS arXiv:0807.4961

NB: 100,000 plots for various jet algorithms, narrow $q\bar{q}$ and $g\bar{g}$ resonances from <http://quality.fastjet.fr> Cacciari, Rojo, GPS & Soyez '08

$m_{q\bar{q}} = 2000 \text{ GeV}$

$q\bar{q}, M = 2000 \text{ GeV}$



Best R is at minimum of curve

- ▶ Best R depends strongly on mass of system
- ▶ Increases with mass, just like crude analytical prediction
NB: current analytics too crude

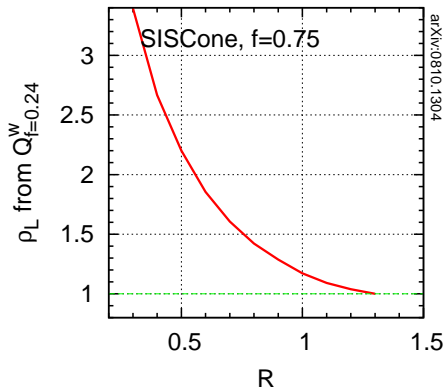
BUT: so far, LHC's plans involve running with fixed smallish R values

e.g. CMS arXiv:0807.4961

NB: 100,000 plots for various jet algorithms, narrow $q\bar{q}$ and $g\bar{g}$ resonances
from <http://quality.fastjet.fr> Cacciari, Rojo, GPS & Soyez '08

$m_{q\bar{q}} = 4000 \text{ GeV}$

$q\bar{q}, M = 4000 \text{ GeV}$



Best R is at minimum of curve

- ▶ Best R depends strongly on mass of system
- ▶ Increases with mass, just like crude analytical prediction

NB: current analytics too crude

BUT: so far, LHC's plans involve running with fixed smallish R values

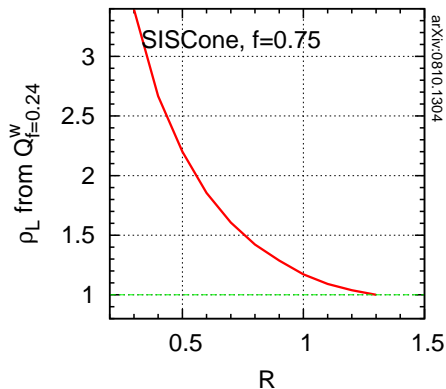
e.g. CMS arXiv:0807.4961

NB: 100,000 plots for various jet algorithms, narrow $q\bar{q}$ and $g\bar{g}$ resonances from <http://quality.fastjet.fr>

Cacciari, Rojo, GPS & Soyez '08

$m_{q\bar{q}} = 4000 \text{ GeV}$

$q\bar{q}, M = 4000 \text{ GeV}$



Best R is at minimum of curve

- ▶ Best R depends strongly on mass of system
- ▶ Increases with mass, just like crude analytical prediction

NB: current analytics too crude

BUT: so far, LHC's plans involve running with fixed smallish R values

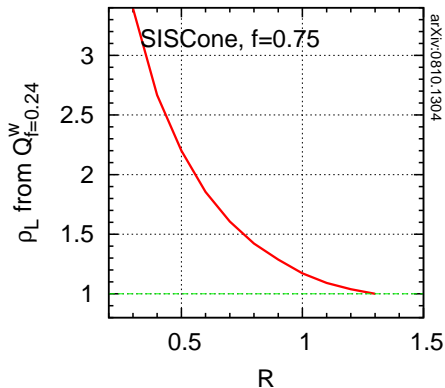
e.g. CMS arXiv:0807.4961

NB: 100,000 plots for various jet algorithms, narrow $q\bar{q}$ and $g\bar{g}$ resonances from <http://quality.fastjet.fr>

Cacciari, Rojo, GPS & Soyez '08

$m_{q\bar{q}} = 4000 \text{ GeV}$

$q\bar{q}, M = 4000 \text{ GeV}$



Best R is at minimum of curve

- ▶ Best R depends strongly on mass of system
- ▶ Increases with mass, just like crude analytical prediction

NB: current analytics too crude

BUT: so far, LHC's plans involve running with fixed smallish R values

e.g. CMS arXiv:0807.4961

NB: 100,000 plots for various jet algorithms, narrow $q\bar{q}$ and $g\bar{g}$ resonances from <http://quality.fastjet.fr>

Cacciari, Rojo, GPS & Soyez '08

File Edit View History Bookmarks Tools Help

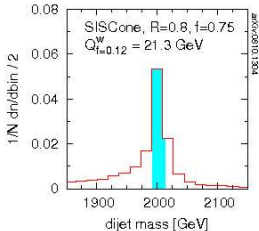
http://www.lpthe.jussieu.fr/~salam/jet-quality/

Testing jet definitions: qq & gg c...

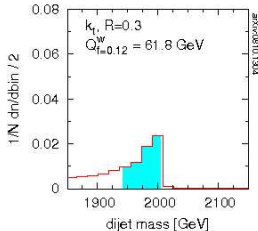
Testing jet definitions: qq & gg cases

by M. Cacciari, J. Rojo, G.P. Salam and G. Soyez, arXiv:0810.1304

qq, M = 2000 GeV



qq, M = 2000 GeV


 k_t C/A anti- k_t SIScone C/A-filt

 R = 0.8
 $Q_{f=z}^W$ $Q_{f=x\gamma M}^W$ x 2

 rebin = 2
 qq gg

 mass = 2000

 pileup: none 0.05 0.25 mb^{-1}/ev

 subtraction:
 k_t C/A anti- k_t SIScone C/A-filt

 R = 0.3
 $Q_{f=z}^W$ $Q_{f=x\gamma M}^W$ x 2

 rebin = 2
 qq gg

 mass = 2000

 pileup: none 0.05 0.25 mb^{-1}/ev

 subtraction:

This page is intended to help visualize how the choice of jet definition impacts a dijet invariant mass reconstruction at LHC.

The controls fall into 4 groups:

- the jet definition
- the binning and quality measures
- the jet-type (quark, gluon) and mass scale
- pileup and subtraction

The events were simulated with Pythia 6.4 (DWT tune) and reconstructed with FastJet 2.3.

For more information, view and listen to the **flash demo**, or click on individual terms.

This page has been tested with Firefox v2 and v3, IE7, Safari v3, Opera v9.5, Chrome 0.2.

The dijet mass is a classic jets analysis.

But LHC also opens up characteristically new kinematic regions, because $\sqrt{s} \gg m_{EW}$.

We can and should make use of this

Illustrated in next slides, for Higgs search with
 $m_H = 115 \text{ GeV}, H \rightarrow b\bar{b}$

- ▶ Signal is $W \rightarrow \ell\nu$, $H \rightarrow b\bar{b}$.
- ▶ Backgrounds include $Wb\bar{b}$, $t\bar{t} \rightarrow \ell\nu b\bar{b}jj$, ...

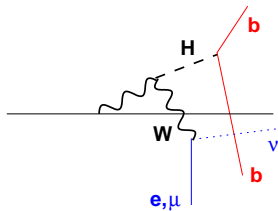
Studied e.g. in ATLAS TDR

Difficulties, e.g.

- ▶ $gg \rightarrow t\bar{t}$ has $\ell\nu b\bar{b}$ with **same intrinsic mass scale**, but much higher partonic luminosity
- ▶ Need exquisite control of bkgd shape

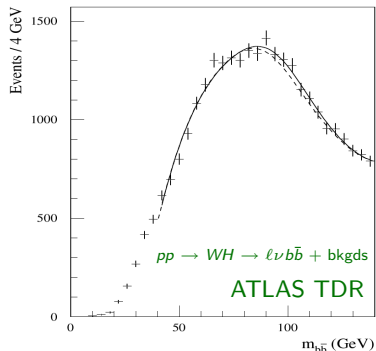
Try a long shot?

- ▶ Go to high p_t ($p_{tH}, p_{tV} > 200$ GeV)
- ▶ Lose 95% of signal, but more efficient?
- ▶ Maybe kill $t\bar{t}$ & gain clarity?



- ▶ Signal is $W \rightarrow \ell\nu, H \rightarrow b\bar{b}$.
- ▶ Backgrounds include $Wb\bar{b}, t\bar{t} \rightarrow \ell\nu b\bar{b}jj, \dots$

Studied e.g. in ATLAS TDR

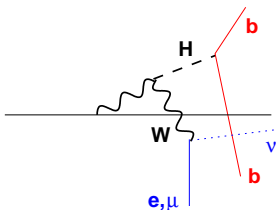


Difficulties, e.g.

- ▶ $gg \rightarrow t\bar{t}$ has $\ell\nu b\bar{b}$ with **same intrinsic mass scale**, but much higher partonic luminosity
- ▶ Need exquisite control of bkgd shape

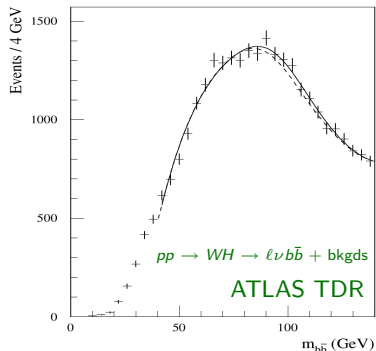
Try a long shot?

- ▶ Go to high p_t ($p_{tH}, p_{tV} > 200$ GeV)
- ▶ Lose 95% of signal, but more efficient?
- ▶ Maybe kill $t\bar{t}$ & gain clarity?



- ▶ Signal is $W \rightarrow \ell\nu, H \rightarrow b\bar{b}$.
- ▶ Backgrounds include $Wb\bar{b}, t\bar{t} \rightarrow \ell\nu b\bar{b}jj, \dots$

Studied e.g. in ATLAS TDR

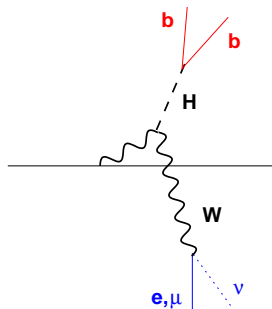


Difficulties, e.g.

- ▶ $gg \rightarrow t\bar{t}$ has $\ell\nu b\bar{b}$ with **same intrinsic mass scale**, but much higher partonic luminosity
- ▶ Need exquisite control of bkgd shape

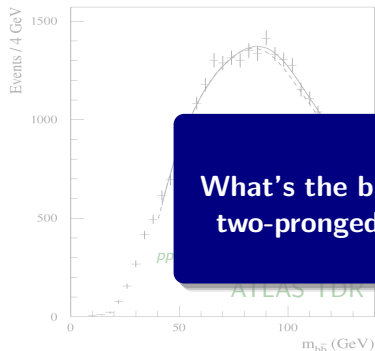
Try a long shot?

- ▶ Go to high p_t ($p_{tH}, p_{tV} > 200$ GeV)
- ▶ Lose 95% of signal, but more efficient?
- ▶ Maybe kill $t\bar{t}$ & gain clarity?



- ▶ Signal is $W \rightarrow \ell\nu, H \rightarrow b\bar{b}$.
- ▶ Backgrounds include $Wb\bar{b}, t\bar{t} \rightarrow \ell\nu b\bar{b}jj, \dots$

Studied e.g. in ATLAS TDR



Difficulties, e.g.

- ▶ $gg \rightarrow t\bar{t}$ has $\ell\nu b\bar{b}$ with **same intrinsic** partonic

Question:
 What's the best strategy to identify the two-pronged structure of the boosted Higgs decay?



- Try a long shot?**
- ▶ Go to high p_t ($p_{tH}, p_{tV} > 200$ GeV)
 - ▶ Lose 95% of signal, but more efficient?
 - ▶ Maybe kill $t\bar{t}$ & gain clarity?

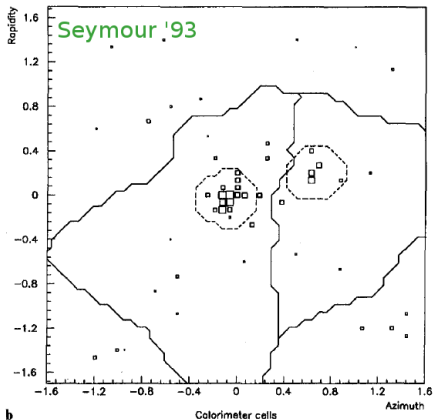
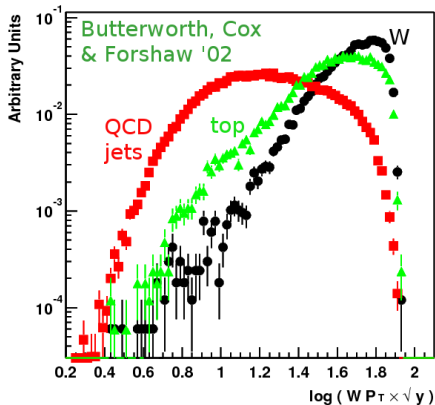


Fig. 2. A hadronic W decay, as seen at calorimeter level, **a** without, and **b** with, particles from the underlying event. Box sizes are logarithmic in the cell energy, lines show the borders of the sub-jets for infinitely soft emission according to the cluster (solid) and cone (dashed) algorithms

Use k_t jet-algorithm's hierarchy to split the jets



Use k_t alg.'s distance measure (rel. trans. mom.) to cut out QCD bkgd:

$$d_{ij}^{k_t} = \min(p_{ti}^2, p_{tj}^2) \Delta R_{ij}^2$$

Y-splitter

only partially correlated with mass

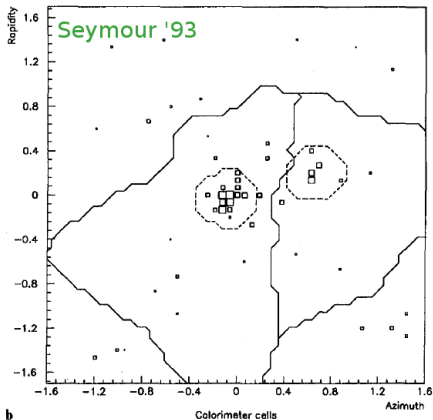
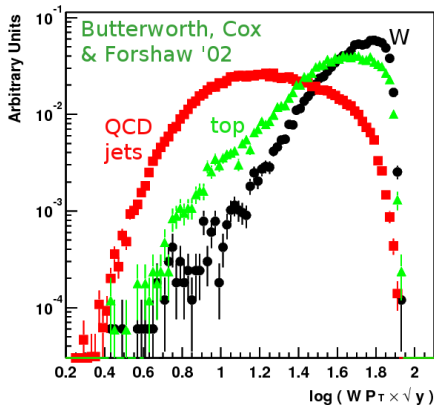


Fig. 2. A hadronic W decay, as seen at calorimeter level, **a** without, and **b** with, particles from the underlying event. Box sizes are logarithmic in the cell energy, lines show the borders of the sub-jets for infinitely soft emission according to the cluster (solid) and cone (dashed) algorithms

Use k_t jet-algorithm's hierarchy to split the jets



Use k_t alg.'s distance measure (rel. trans. mom.) to cut out QCD bkgd:

$$d_{ij}^{k_t} = \min(p_{ti}^2, p_{tj}^2) \Delta R_{ij}^2$$

Y-splitter

only partially correlated with mass

The Cambridge/Aachen jet alg.

Dokshitzer et al '97
Wengler & Wobisch '98

Work out $\Delta R_{ij}^2 = \Delta y_{ij}^2 + \Delta \phi_{ij}^2$ between all pairs of objects i, j ;

Recombine the closest pair;

Repeat until all objects separated by $\Delta R_{ij} > R$.

[in FastJet]

Gives “hierarchical” view of the event; work through it backwards to analyse jet

The Cambridge/Aachen jet alg.

Dokshitzer et al '97
Wengler & Wobisch '98

Work out $\Delta R_{ij}^2 = \Delta y_{ij}^2 + \Delta \phi_{ij}^2$ between all pairs of objects i, j ;

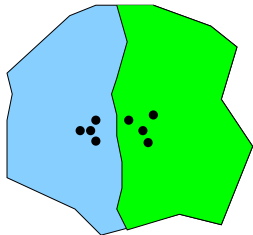
Recombine the closest pair;

Repeat until all objects separated by $\Delta R_{ij} > R$.

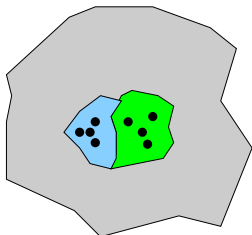
[in FastJet]

Gives “hierarchical” view of the event; work through it backwards to analyse jet

k_t algorithm



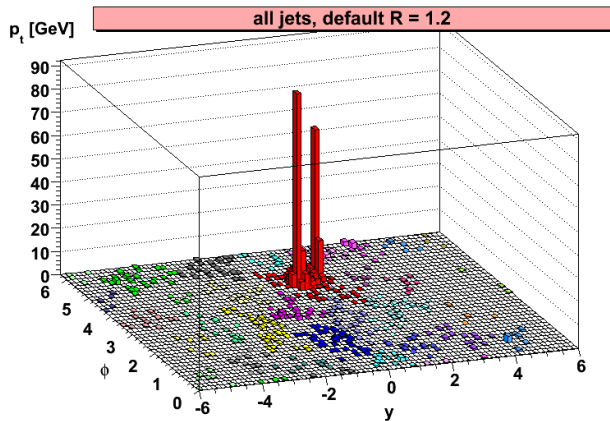
Cam/Aachen algorithm



Allows you to “dial” the correct R to keep perturbative radiation, but throw out UE

Herwig 6.510 + Jimmy 4.31 + FastJet 2.3

SIGNAL



Zbb BACKGROUND

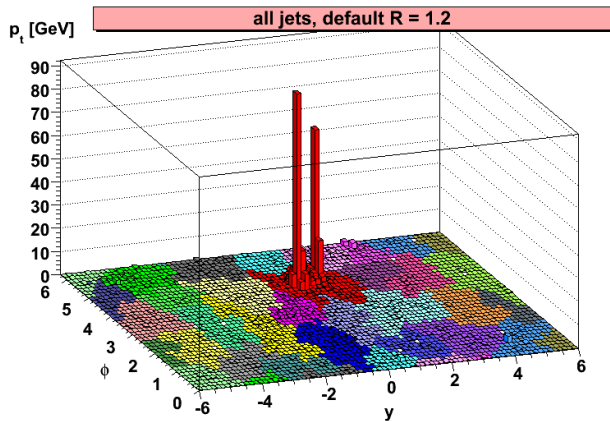
Cluster event, C/A, R=1.2

Butterworth, Davison, Rubin & GPS '08

arbitrary norm.

Herwig 6.510 + Jimmy 4.31 + FastJet 2.3

SIGNAL



Zbb BACKGROUND

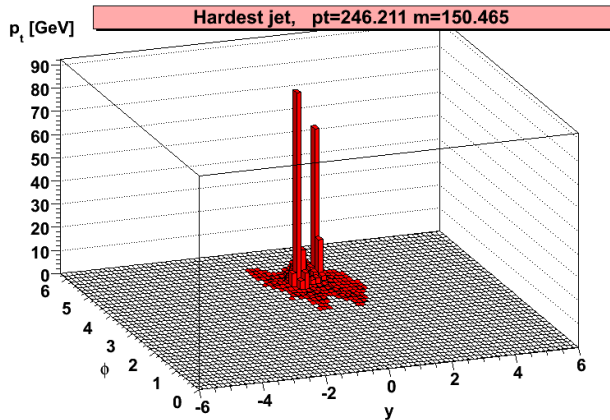
Fill it in, → show jets more clearly

Butterworth, Davison, Rubin & GPS '08

arbitrary norm.

$$pp \rightarrow ZH \rightarrow \nu\bar{\nu}b\bar{b}, @14\text{ TeV}, m_H = 115\text{ GeV}$$

Herwig 6.510 + Jimmy 4.31 + FastJet 2.3

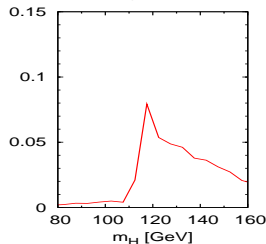


Consider hardest jet, $m = 150$ GeV

Butterworth, Davison, Rubin & GPS '08

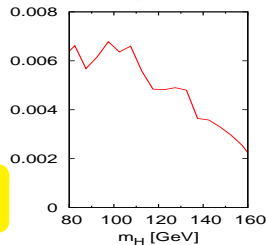
SIGNAL

$200 < p_{tZ} < 250$ GeV



Zbb BACKGROUND

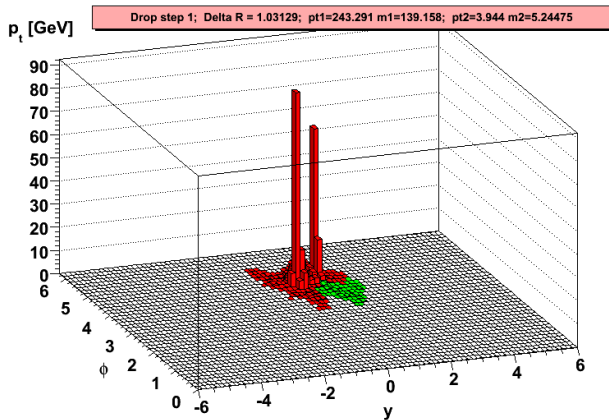
$200 < p_{tZ} < 250$ GeV



arbitrary norm.

$$pp \rightarrow ZH \rightarrow \nu\bar{\nu}b\bar{b}, @14\text{ TeV}, m_H = 115\text{ GeV}$$

Herwig 6.510 + Jimmy 4.31 + FastJet 2.3

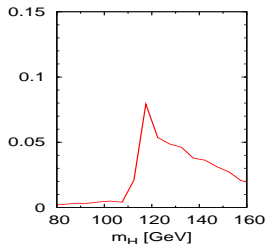


split: $m = 150\text{ GeV}$, $\frac{\max(m_1, m_2)}{m} = 0.92 \rightarrow \text{repeat}$

Butterworth, Davison, Rubin & GPS '08

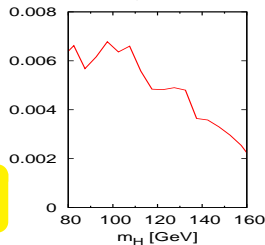
SIGNAL

$200 < p_{tZ} < 250\text{ GeV}$



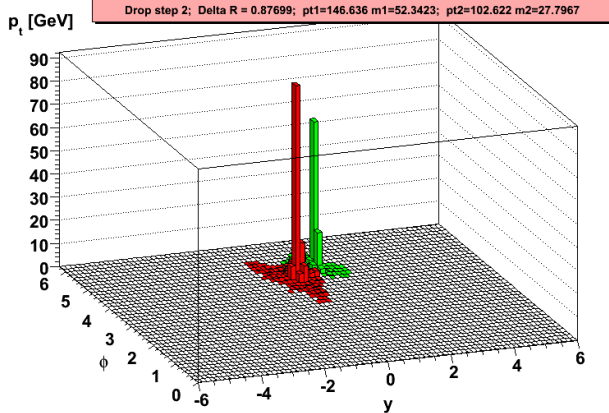
Zbb BACKGROUND

$200 < p_{tZ} < 250\text{ GeV}$



arbitrary norm.

Herwig 6.510 + Jimmy 4.31 + FastJet 2.3

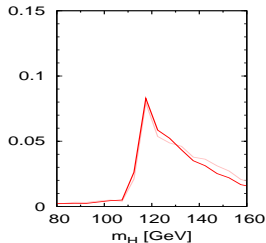


split: $m = 139$ GeV, $\frac{\max(m_1, m_2)}{m} = 0.37 \rightarrow$ mass drop

Butterworth, Davison, Rubin & GPS '08

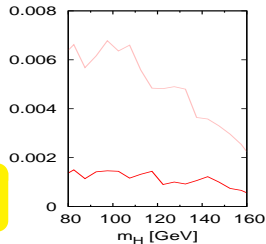
SIGNAL

$200 < p_{tZ} < 250$ GeV



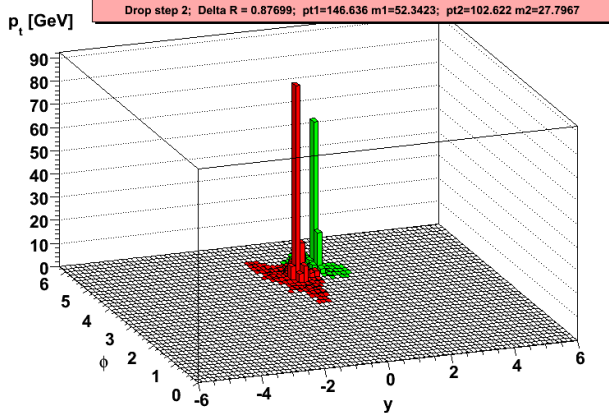
Zbb BACKGROUND

$200 < p_{tZ} < 250$ GeV



arbitrary norm.

Herwig 6.510 + Jimmy 4.31 + FastJet 2.3

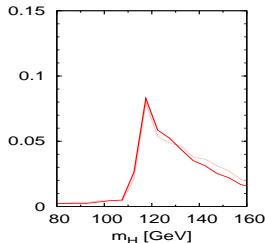


check: $y_{12} \simeq \frac{p_{t2}}{p_{t1}} \simeq 0.7 \rightarrow \text{OK} + 2 \text{ } b\text{-tags (anti-QCD)}$

Butterworth, Davison, Rubin & GPS '08

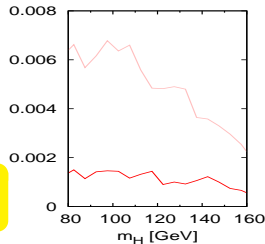
SIGNAL

$200 < p_{tZ} < 250$ GeV



Zbb BACKGROUND

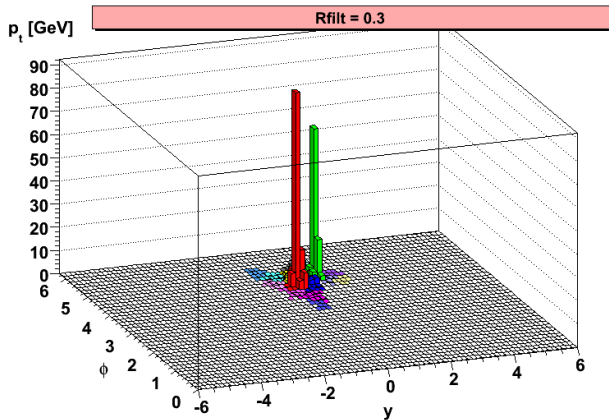
$200 < p_{tZ} < 250$ GeV



arbitrary norm.

$$pp \rightarrow ZH \rightarrow \nu\bar{\nu}b\bar{b}, @14\text{ TeV}, m_H = 115\text{ GeV}$$

Herwig 6.510 + Jimmy 4.31 + FastJet 2.3

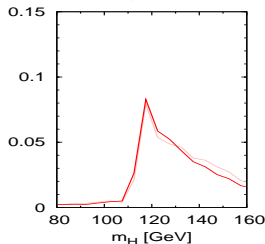


$$R_{filt} = 0.3$$

Butterworth, Davison, Rubin & GPS '08

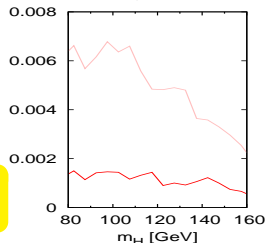
SIGNAL

$200 < p_{tZ} < 250\text{ GeV}$



Zbb BACKGROUND

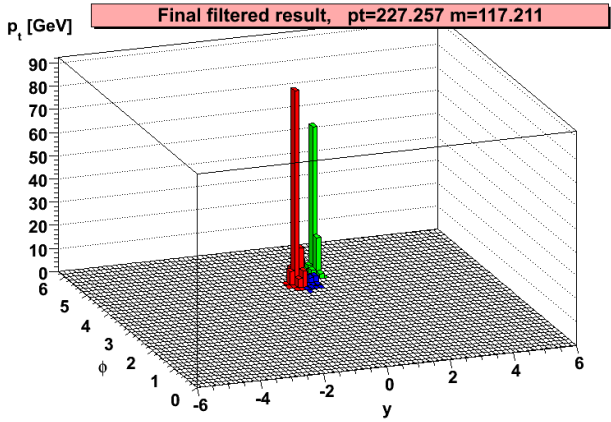
$200 < p_{tZ} < 250\text{ GeV}$



arbitrary norm.

$$pp \rightarrow ZH \rightarrow \nu\bar{\nu}b\bar{b}, @14\text{ TeV}, m_H = 115\text{ GeV}$$

Herwig 6.510 + Jimmy 4.31 + FastJet 2.3

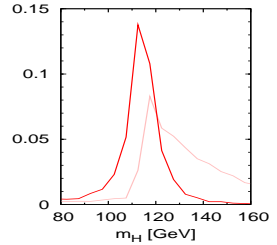


$R_{filt} = 0.3$: take 3 hardest, $m = 117\text{ GeV}$

Butterworth, Davison, Rubin & GPS '08

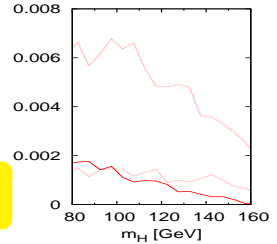
SIGNAL

$200 < p_{tZ} < 250\text{ GeV}$

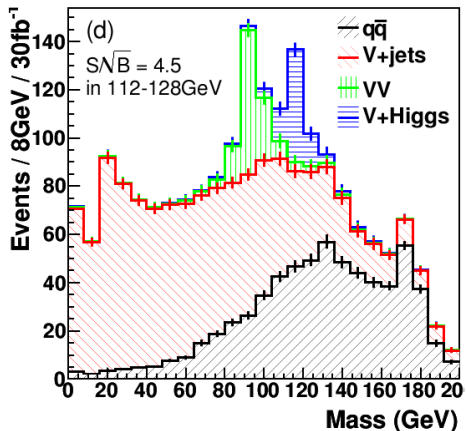


Zbb BACKGROUND

$200 < p_{tZ} < 250\text{ GeV}$



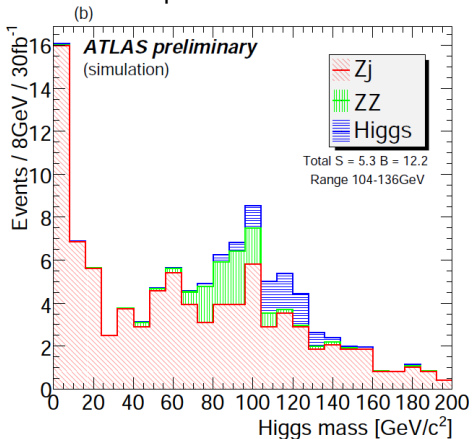
arbitrary norm.

combine HZ and HW, $p_t > 200$ GeV

- ▶ Take $Z \rightarrow \ell^+ \ell^-$, $Z \rightarrow \nu \bar{\nu}$,
 $W \rightarrow \ell \nu$ $\ell = e, \mu$
- ▶ $p_{tV}, p_{tH} > 200$ GeV
- ▶ $|\eta_V|, |\eta_H| < 2.5$
- ▶ Assume real/fake b -tag rates of 0.6/0.02.
- ▶ Some extra cuts in HW channels to reject $t\bar{t}$.
- ▶ Assume $m_H = 115$ GeV.

At $\sim 5\sigma$ for 30 fb^{-1} this looks like a competitive channel for light Higgs discovery. **A powerful method!**

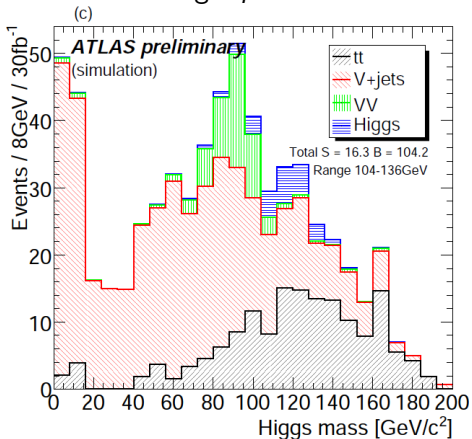
Leptonic channel



What changes compared to particle-level analysis?

$\sim 1.5\sigma$ as compared to 2.1σ

Expected given larger mass window

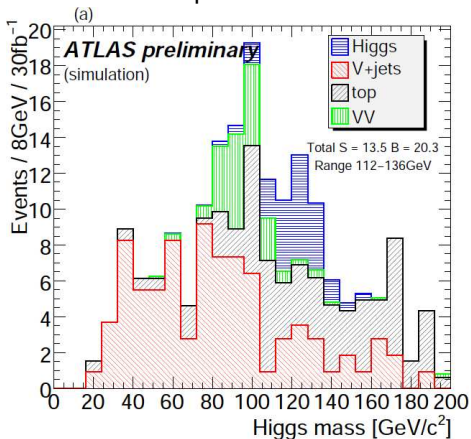
Missing E_T channel

What changes compared to particle-level analysis?

$\sim 1.5\sigma$ as compared to 3σ

Suffers: some events redistributed to semi-leptonic channel

Semi-leptonic channel



What changes compared to particle-level analysis?

$\sim 3\sigma$ as compared to 3σ

Benefits: some events redistributed from missing E_T channel

Likelihood-based analysis of all three channels together gives signal significance of

3.7σ for 30 fb^{-1}

To be compared with 4.2σ in hadron-level analysis for $m_H = 120 \text{ GeV}$
K-factors not included: don't affect significance (~ 1.5 for VH , $2 - 2.5$ for Vbb)

With 5% (20%) background uncertainty, ATLAS result becomes 3.5σ (2.8σ)

Comparison to other channels at ATLAS ($m_H = 120, 30 \text{ fb}^{-1}$):

$gg \rightarrow H \rightarrow \gamma\gamma$	$WW \rightarrow H \rightarrow \tau\tau$	$gg \rightarrow H \rightarrow ZZ^*$
4.2σ	4.9σ	2.6σ

Extracted from 0901.0512

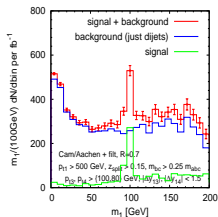
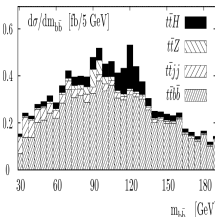
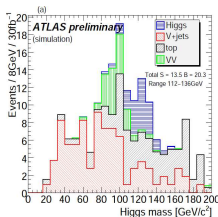
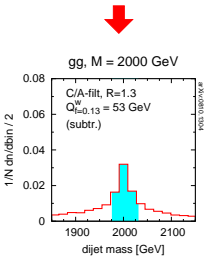
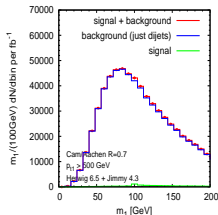
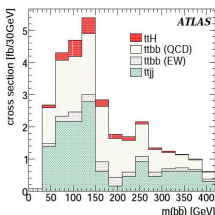
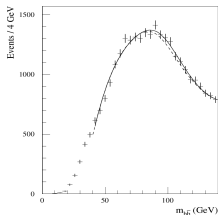
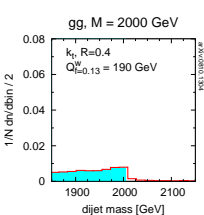
The potential of better jet finding

$$X \rightarrow gg$$

$$VH, H \rightarrow b\bar{b}$$

$$ttH, H \rightarrow b\bar{b}$$

$$\text{RPV } \tilde{\chi}_1^0 \rightarrow qq\bar{q}$$



- 1) Cacciari, Rojo, GPS & Soyez '08;
- 2) Butterworth, Davison, Rubin & GPS '08;
- 3) Plehn, GPS & Spannowsky '09;
- 4) Butterworth, Ellis, Raklev & GPS '09.

Conclusions

- ▶ There are no longer any valid reasons for using jet algorithms that are incompatible with the Snowmass criteria.
 - LHC experiments are adopting the new tools
 - Individual analyses need to follow suit
- ▶ It's time to move forwards with the question of how best to use jets in searches
- ▶ Examples here show two things:
 - ▶ Good jet-finding brings significant gains
 - ▶ There's room for serious QCD theory input into optimising jet use
 - Not the *only* way of doing things
 - But brings more insight than trial & error MC

This opens the road towards *Jetography*, QCD-based autofocus for jets

EXTRAS

There are $N(N - 1)/2$ distances d_{ij} — surely we have to calculate them all in order to find smallest?

k_t distance measure is partly *geometrical*:

$$\begin{aligned} \min_{i,j} d_{ij} &\equiv \min_{i,j} (\min\{k_{ti}^2, k_{tj}^2\} \Delta R_{ij}^2) \\ &= \min_{i,j} (k_{ti}^2 \Delta R_{ij}^2) \\ &= \min_i (k_{ti}^2 \min_j \Delta R_{ij}^2) \end{aligned}$$

In words: for each i look only at the k_t distance to its 2D geometrical nearest neighbour (GNN).

k_t distance need only be calculated between GNNs

Each point has 1 GNN \rightarrow need only calculate N d_{ij} 's

There are $N(N - 1)/2$ distances d_{ij} — surely we have to calculate them all in order to find smallest?

k_t distance measure is partly *geometrical*:

$$\begin{aligned} \min_{i,j} d_{ij} &\equiv \min_{i,j} (\min\{k_{ti}^2, k_{tj}^2\} \Delta R_{ij}^2) \\ &= \min_{i,j} (k_{ti}^2 \Delta R_{ij}^2) \\ &= \min_i (k_{ti}^2 \min_j \Delta R_{ij}^2) \end{aligned}$$

In words: for each i look only at the k_t distance to its 2D geometrical nearest neighbour (GNN).

k_t distance need only be calculated between GNNs

Each point has 1 GNN \rightarrow need only calculate N d_{ij} 's
Cacciari & GPS, '05

There are $N(N - 1)/2$ distances d_{ij} — surely we have to calculate them all in order to find smallest?

k_t distance measure is partly *geometrical*:

$$\begin{aligned}
 \min_{i,j} d_{ij} &\equiv \min_{i,j} (\min\{k_{ti}^2, k_{tj}^2\} \Delta R_{ij}^2) \\
 &= \min_{i,j} (k_{ti}^2 \Delta R_{ij}^2) \\
 &= \min_i (k_{ti}^2 \min_j \Delta R_{ij}^2)
 \end{aligned}$$

↗ 2D dist. on rap., ϕ cylinder

In words: for each i look only at the k_t distance to its 2D geometrical nearest neighbour (GNN).

k_t distance need only be calculated between GNNs

Each point has 1 GNN → need only calculate N d_{ij} 's
Cacciari & GPS, '05

There are $N(N - 1)/2$ distances d_{ij} — surely we have to calculate them all in order to find smallest?

k_t distance measure is partly *geometrical*:

$$\begin{aligned}\min_{i,j} d_{ij} &\equiv \min_{i,j} (\min\{k_{ti}^2, k_{tj}^2\} \Delta R_{ij}^2) \\ &= \min_{i,j} (k_{ti}^2 \Delta R_{ij}^2) \\ &= \min_i (k_{ti}^2 \min_j \Delta R_{ij}^2)\end{aligned}$$

↙ 2D dist. on rap., ϕ cylinder

In words: for each i look only at the k_t distance to its 2D geometrical nearest neighbour (GNN).

k_t distance need only be calculated between GNNs

Each point has 1 GNN → need only calculate N d_{ij} 's
Cacciari & GPS, '05

There are $N(N - 1)/2$ distances d_{ij} — surely we have to calculate them all in order to find smallest?

k_t distance measure is partly *geometrical*:

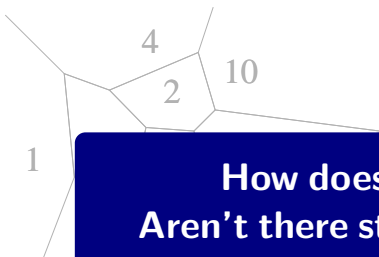
$$\begin{aligned} \min_{i,j} d_{ij} &\equiv \min_{i,j} (\min\{k_{ti}^2, k_{tj}^2\} \Delta R_{ij}^2) \\ &= \min_{i,j} (k_{ti}^2 \Delta R_{ij}^2) \\ &= \min_i (k_{ti}^2 \min_j \Delta R_{ij}^2) \end{aligned}$$

↙ 2D dist. on rap., ϕ cylinder

In words: for each i look only at the k_t distance to its 2D geometrical nearest neighbour (GNN).

k_t distance need only be calculated between GNNs

Each point has 1 GNN → need only calculate N d_{ij} 's
Cacciari & GPS, '05



Given a set of vertices on plane (1...10) a *Voronoi diagram* partitions plane into cells containing all points closest to each vertex.

How does use of GNN help?
Aren't there still $\frac{N^2}{2} \Delta R_{ij}^2$ to check... ?

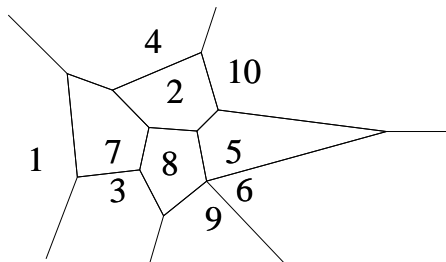
Geometrical nearest neighbour finding is a classic problem in the field of Computational Geometry

Devillers '99 [+ related work by other authors]
 Convenient C++ package available: CGAL, <http://www.cgal.org>

With help of CGAL, clustering can be done in $N \ln N$ time.

Coded in the FastJet package (v1), Cacciari & GPS '05

2d nearest-neighbours



Given a set of vertices on plane (1...10) a *Voronoi diagram* partitions plane into cells containing all points closest to each vertex

Dirichlet '1850, Voronoi '1908

A vertex's nearest other vertex is always in an adjacent cell.

E.g. GNN of point 7 must be among 1,4,2,8,3 (it is 3)

Construction of Voronoi diagram for N points: $N \ln N$ time Fortune '88

Update of 1 point in Voronoi diagram: expected $\ln N$ time

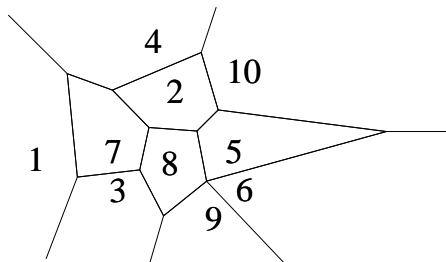
Devillers '99 [+ related work by other authors]

Convenient C++ package available: CGAL, <http://www.cgal.org>

with help of CGAL, k_t clustering can be done in $N \ln N$ time

Coded in the FastJet package (v1), Cacciari & GPS '06

2d nearest-neighbours



Given a set of vertices on plane (1...10) a *Voronoi diagram* partitions plane into cells containing all points closest to each vertex

Dirichlet '1850, Voronoi '1908

A vertex's nearest other vertex is always in an adjacent cell.

E.g. GNN of point 7 must be among 1,4,2,8,3 (it is 3)

Construction of Voronoi diagram for N points: $N \ln N$ time Fortune '88

Update of 1 point in Voronoi diagram: expected $\ln N$ time

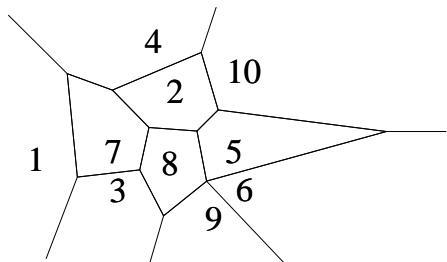
Devillers '99 [+ related work by other authors]

Convenient C++ package available: CGAL, <http://www.cgal.org>

with help of CGAL, k_t clustering can be done in $N \ln N$ time

Coded in the FastJet package (v1), Cacciari & GPS '06

2d nearest-neighbours



Given a set of vertices on plane (1...10) a *Voronoi diagram* partitions plane into cells containing all points closest to each vertex

Dirichlet '1850, Voronoi '1908

A vertex's nearest other vertex is always in an adjacent cell.

E.g. GNN of point 7 must be among 1,4,2,8,3 (it is 3)

Construction of Voronoi diagram for N points: $N \ln N$ time Fortune '88

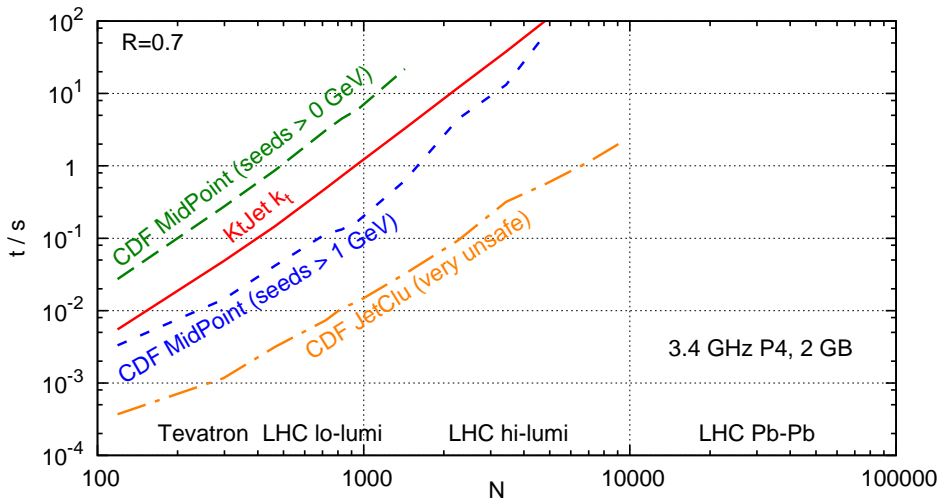
Update of 1 point in Voronoi diagram: expected $\ln N$ time

Devillers '99 [+ related work by other authors]

Convenient C++ package available: CGAL, <http://www.cgal.org>

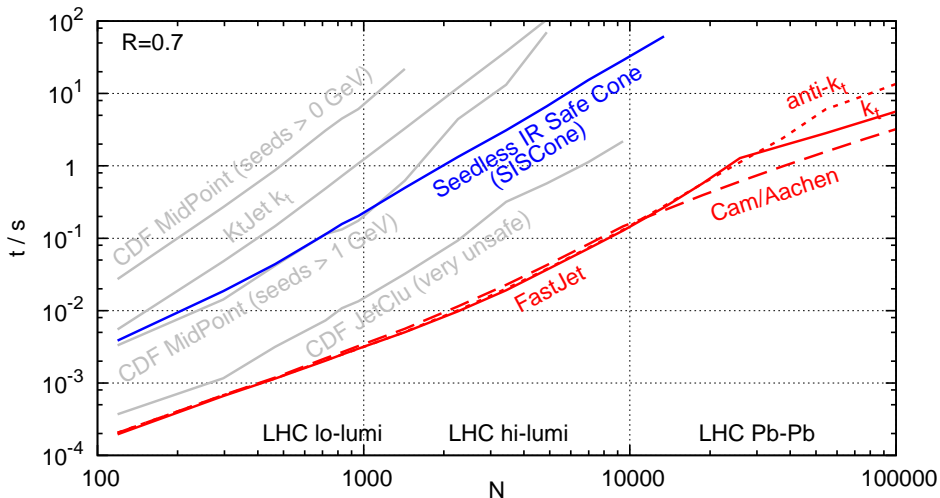
with help of CGAL, k_t clustering can be done in $N \ln N$ time

Coded in the FastJet package (v1), Cacciari & GPS '06



FastJet (v2.x), codes all developments, natively (k_t , Cam/Aachen, anti- k_t) or as plugins (SIScone): Cacciari, GPS & Soyez '05–09

<http://fastjet.fr/>

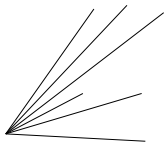


FastJet (v2.x), codes all developments, natively (k_t , Cam/Aachen, anti- k_t) or as plugins (SIScone): Cacciari, GPS & Soyez '05–09

<http://fastjet.fr/>

Procedure:

- ▶ Find one stable cone By iterating from hardest seed particle
- ▶ Call it a jet; remove its particles from the event; repeat

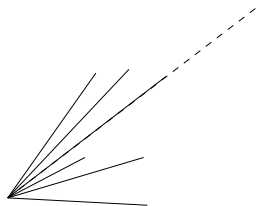


Procedure:

- ▶ Find one stable cone

By iterating from hardest seed particle

- ▶ Call it a jet; remove its particles from the event; repeat

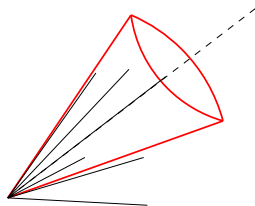


Procedure:

- ▶ Find one stable cone

By iterating from hardest seed particle

- ▶ Call it a jet; remove its particles from the event; repeat

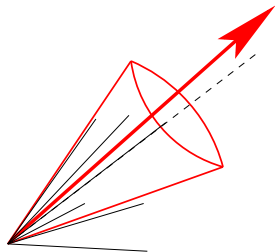


Procedure:

- ▶ Find one stable cone

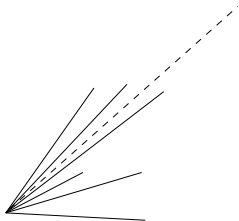
By iterating from hardest seed particle

- ▶ Call it a jet; remove its particles from the event; repeat



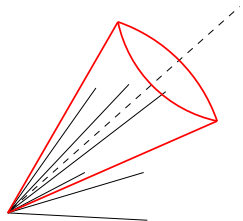
Procedure:

- ▶ Find one stable cone By iterating from hardest seed particle
- ▶ Call it a jet; remove its particles from the event; repeat



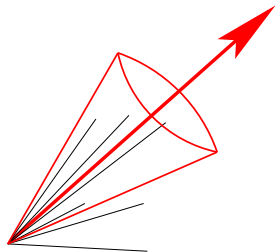
Procedure:

- ▶ Find one stable cone By iterating from hardest seed particle
- ▶ Call it a jet; remove its particles from the event; repeat



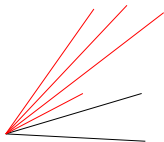
Procedure:

- ▶ Find one stable cone By iterating from hardest seed particle
- ▶ Call it a jet; remove its particles from the event; repeat



Procedure:

- ▶ Find one stable cone By iterating from hardest seed particle
- ▶ Call it a jet; remove its particles from the event; repeat



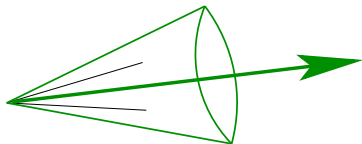
Procedure:

- ▶ Find one stable cone By iterating from hardest seed particle
- ▶ Call it a jet; remove its particles from the event; repeat



Procedure:

- ▶ Find one stable cone By iterating from hardest seed particle
- ▶ Call it a jet; remove its particles from the event; repeat



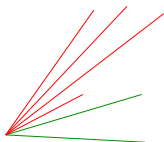
Procedure:

- ▶ Find one stable cone By iterating from hardest seed particle
- ▶ Call it a jet; remove its particles from the event; repeat



Procedure:

- ▶ Find one stable cone By iterating from hardest seed particle
- ▶ Call it a jet; remove its particles from the event; repeat



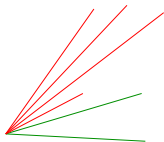
Procedure:

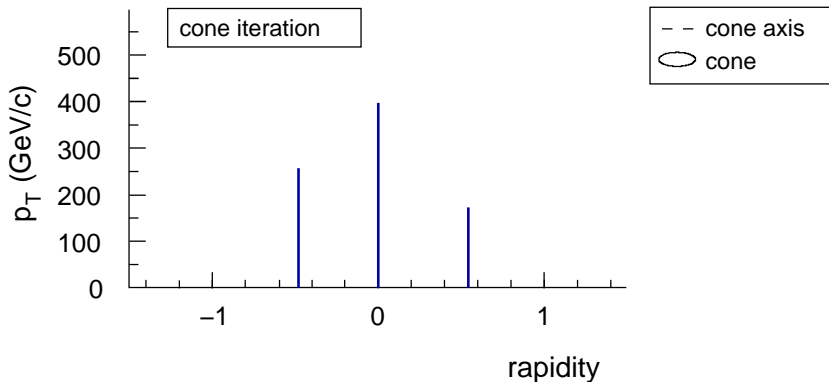
- ▶ Find one stable cone By iterating from hardest seed particle
- ▶ Call it a jet; remove its particles from the event; repeat

Iterative Cone with Progressive Removal (IC-PR)

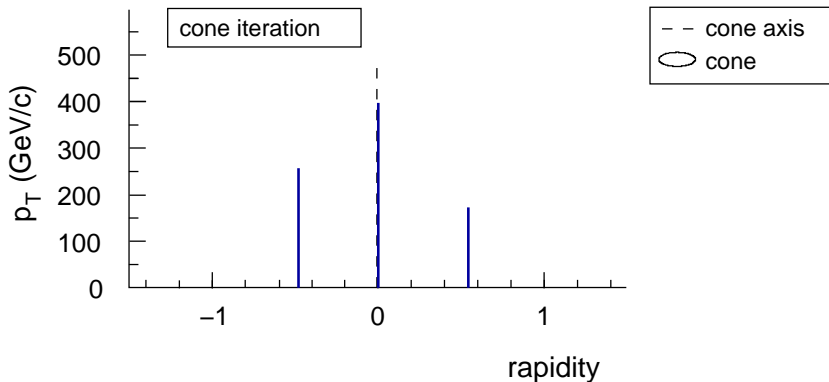
e.g. CMS it. cone, [Pythia Cone, GetJet], ...

- ▶ NB: not same type of algorithm as Atlas Cone, MidPoint, SIScone

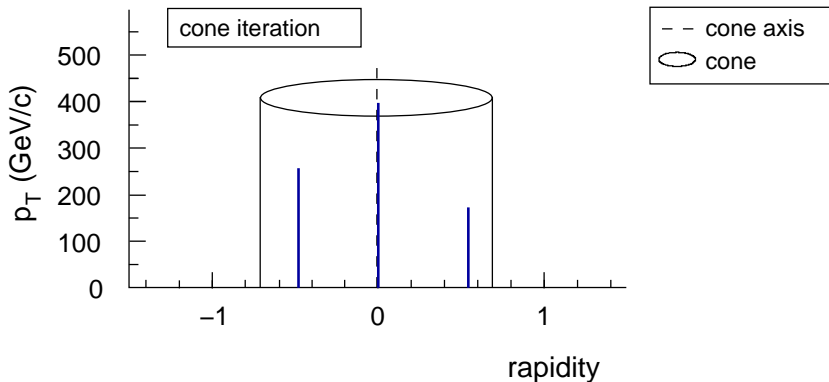




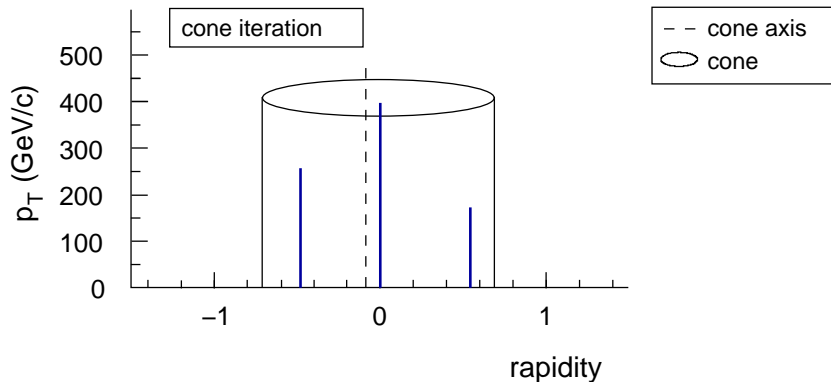
Collinear splitting can modify the hard jets: ICPR algorithms are
collinear unsafe \implies perturbative calculations give ∞



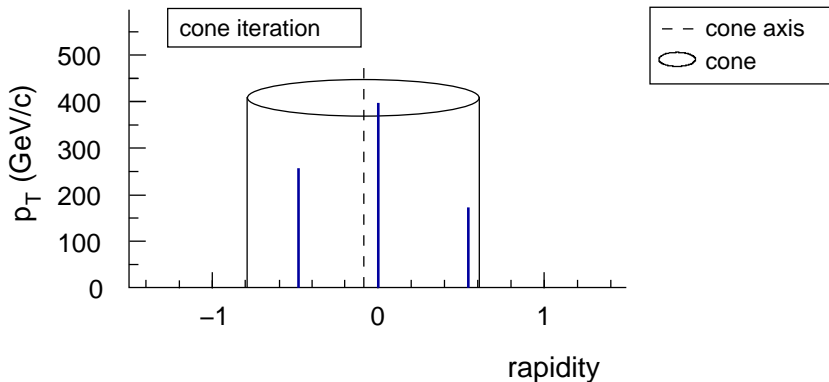
Collinear splitting can modify the hard jets: ICPR algorithms are collinear unsafe \implies perturbative calculations give ∞



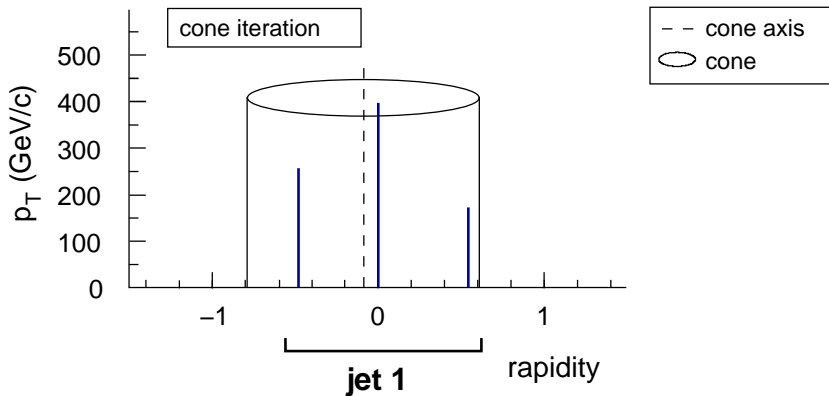
Collinear splitting can modify the hard jets: ICPR algorithms are collinear unsafe \implies perturbative calculations give ∞



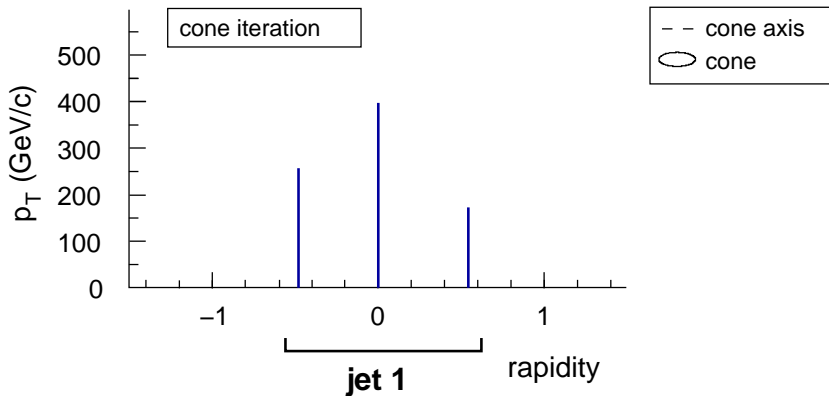
Collinear splitting can modify the hard jets: ICPR algorithms are collinear unsafe \implies perturbative calculations give ∞



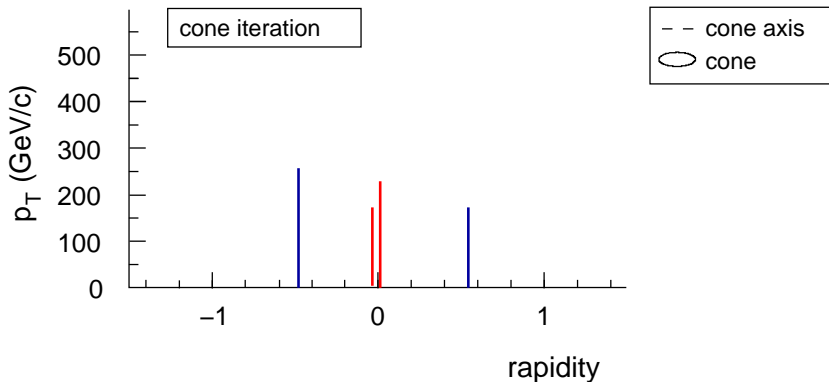
Collinear splitting can modify the hard jets: ICPR algorithms are collinear unsafe \implies perturbative calculations give ∞



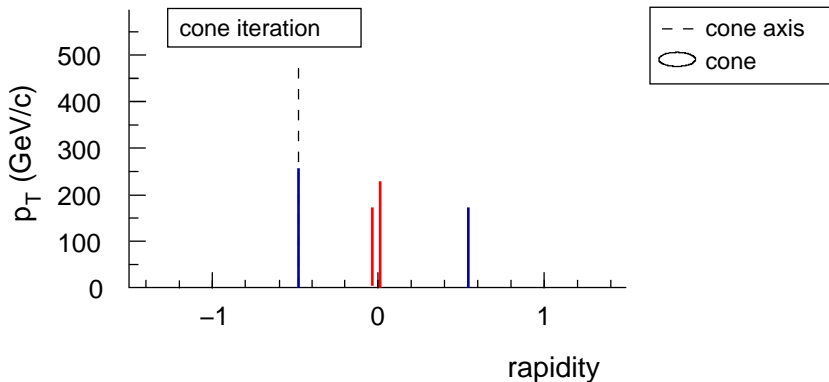
Collinear splitting can modify the hard jets: ICPR algorithms are collinear unsafe \implies perturbative calculations give ∞



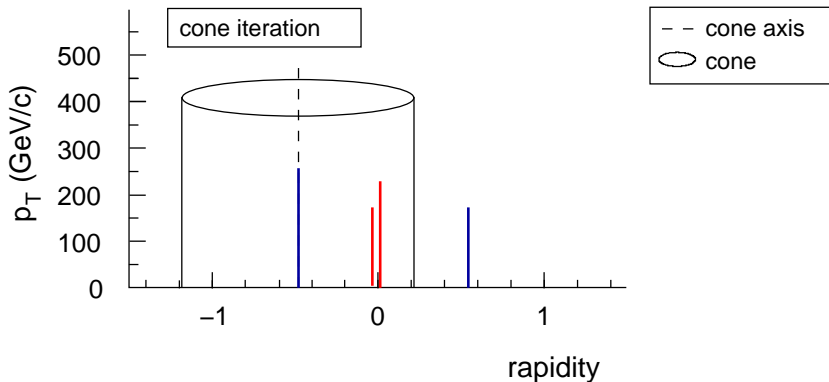
Collinear splitting can modify the hard jets: ICPR algorithms are
collinear unsafe \implies perturbative calculations give ∞



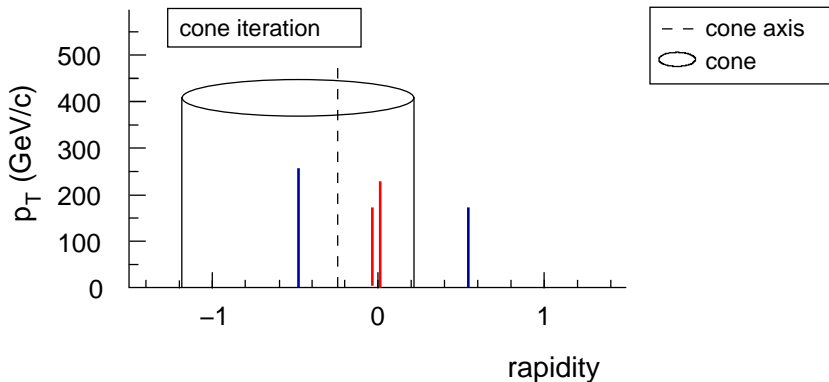
Collinear splitting can modify the hard jets: ICPR algorithms are
collinear unsafe \implies perturbative calculations give ∞



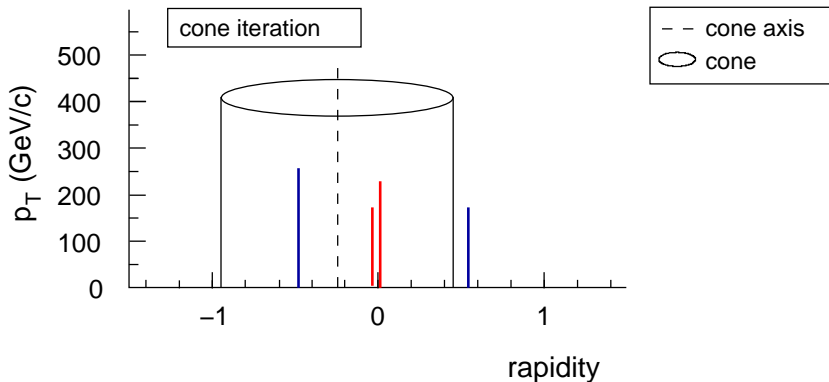
Collinear splitting can modify the hard jets: ICPR algorithms are
collinear unsafe \implies perturbative calculations give ∞



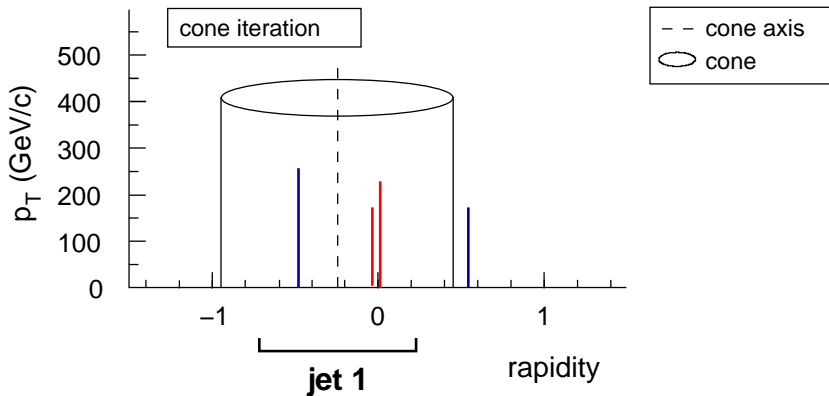
Collinear splitting can modify the hard jets: ICPR algorithms are collinear unsafe \implies perturbative calculations give ∞



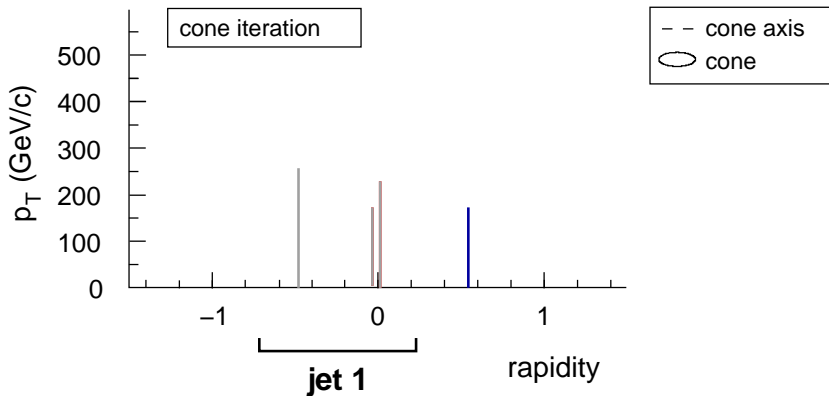
Collinear splitting can modify the hard jets: ICPR algorithms are collinear unsafe \implies perturbative calculations give ∞



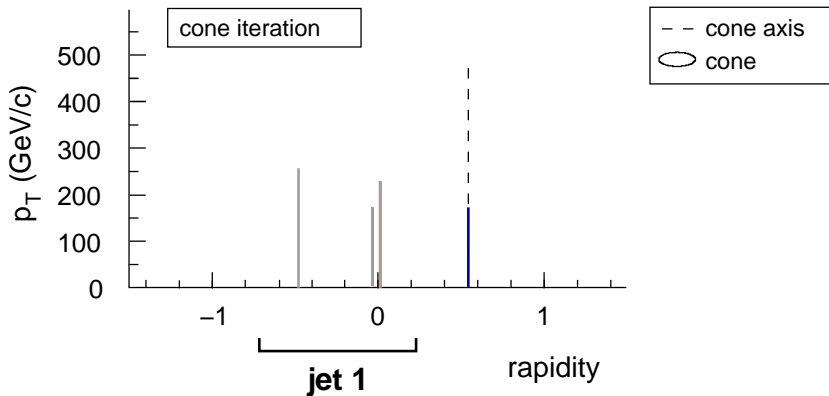
Collinear splitting can modify the hard jets: ICPR algorithms are collinear unsafe \Rightarrow perturbative calculations give ∞



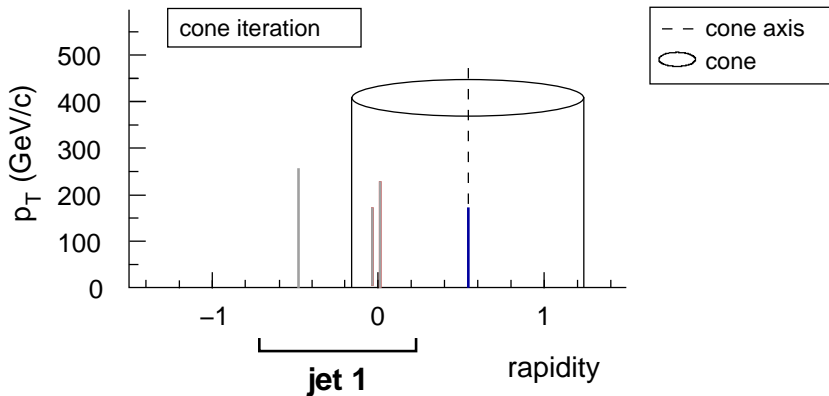
Collinear splitting can modify the hard jets: ICPR algorithms are collinear unsafe \implies perturbative calculations give ∞



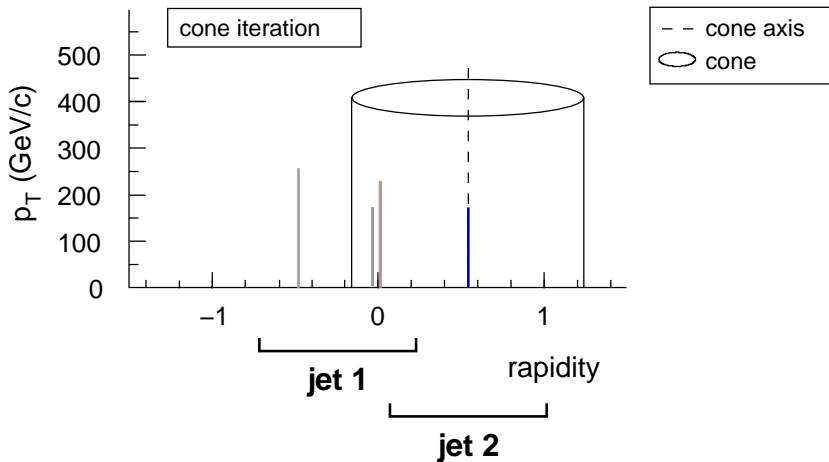
Collinear splitting can modify the hard jets: ICPR algorithms are collinear unsafe \implies perturbative calculations give ∞



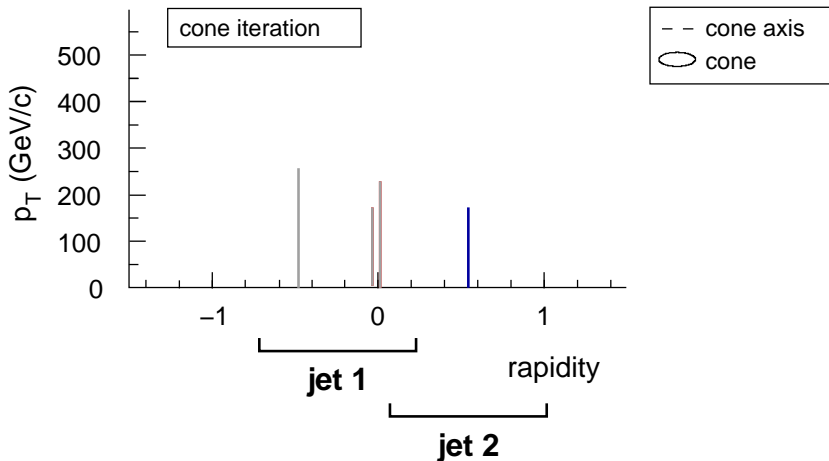
Collinear splitting can modify the hard jets: ICPR algorithms are collinear unsafe \implies perturbative calculations give ∞



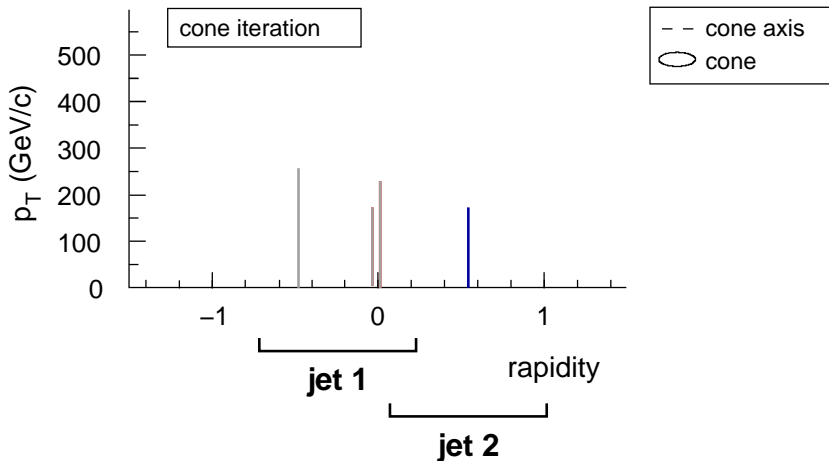
Collinear splitting can modify the hard jets: ICPR algorithms are collinear unsafe \implies perturbative calculations give ∞



Collinear splitting can modify the hard jets: ICPR algorithms are collinear unsafe \implies perturbative calculations give ∞

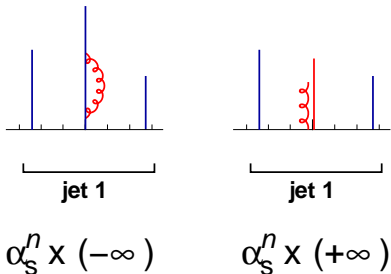


Collinear splitting can modify the hard jets: ICPR algorithms are collinear unsafe \implies perturbative calculations give ∞



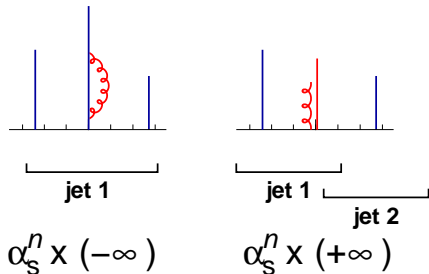
Collinear splitting can modify the hard jets: ICPR algorithms are collinear unsafe \implies perturbative calculations give ∞

Collinear Safe



Infinites cancel

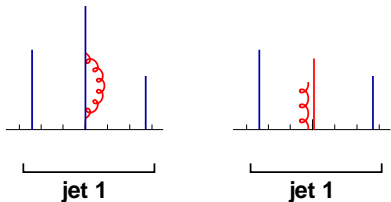
Collinear Unsafe



Infinites do not cancel

Invalidates perturbation theory

Collinear Safe

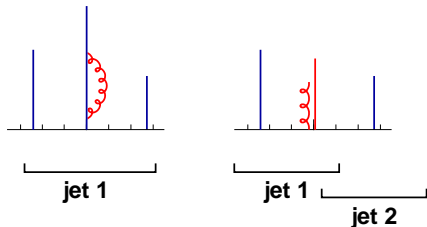


$$\alpha_S^n \times (-\infty)$$

$$\alpha_S^n \times (+\infty)$$

Infinites cancel

Collinear Unsafe



$$\alpha_S^n \times (-\infty)$$

$$\alpha_S^n \times (+\infty)$$

Infinites do not cancel

Invalidates perturbation theory

CDF have measured $W+3\text{jet}$ X-section with JetClu (IR_{2+1} unsafe).

NLO calculation with JetClu would diverge [for zero seed threshold]

Strategy for theory: use 2 algs for theory prediction, SISCone & anti- k_t ;
difference between them is IRC unsafety “systematic”.

With CDF cuts and R choice, difference is $\mathcal{O}(20\%)$

10% @ NLO: Ellis, Melnikov
& Zanderighi '09
 $\sim 20\%$ exp. systematics

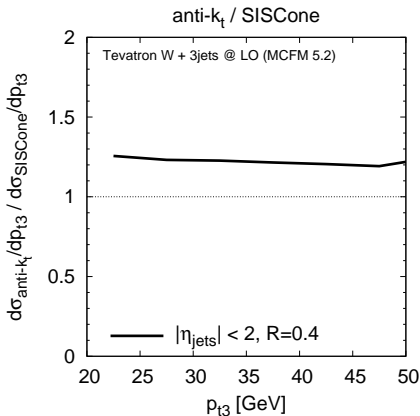
CDF have measured $W+3\text{jet}$ X-section with JetClu (IR_{2+1} unsafe).

NLO calculation with JetClu would diverge [for zero seed threshold]

Strategy for theory: use 2 algs for theory prediction, SISCone & anti- k_t ;
 difference between them is IRC unsafety “systematic”.

With CDF cuts and R choice, difference is $\mathcal{O}(20\%)$

10% @ NLO: Ellis, Melnikov
 & Zanderighi '09
 ~ 20% exp. systematics



CDF have measured $W+3\text{jet}$ X-section with JetClu (IR_{2+1} unsafe).

NLO calculation with JetClu would diverge [for zero seed threshold]

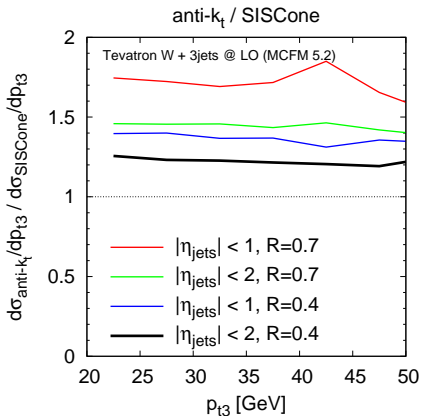
Strategy for theory: use 2 algs for theory prediction, SISCone & anti- k_t ;
difference between them is IRC unsafety “systematic”.

With CDF cuts and R choice, difference is $\mathcal{O}(20\%)$

10% @ NLO: Ellis, Melnikov
& Zanderighi '09
 $\sim 20\%$ exp. systematics

**With other cuts and R choice,
IRC systematic can be up to
75%**

Future measurements deserve
to be done with IRC safe algs...



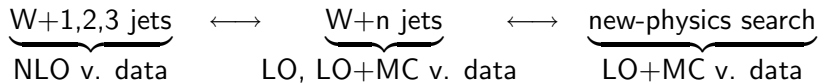
I do searches, not QCD. Why should I care about IRC safety?

- ▶ Are you looking for a mass-peak? ➡ you needn't care much
- ▶ Are you looking for an excess over bkgd? ➡ you need control samples, validated against QCD



I do searches, not QCD. Why should I care about IRC safety?

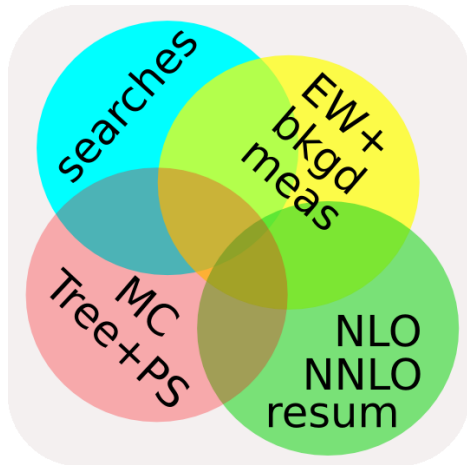
- ▶ Are you looking for a mass-peak? ➔ you needn't care much
- ▶ Are you looking for an excess over bkgd? ➔ you need control samples, validated against QCD



Does lack of IRC safety matter?

I do searches, not QCD. Why should I care about IRC safety?

- ▶ Are you looking for a mass-peak? → you needn't care much
- ▶ Are you looking for an excess over bkgd? → you need control samples, validated against QCD



$W+1,2,3$ jets
 NLO v. data
 IR safe alg.

↔

$W+n$ jets
 LO, LO+MC v. data
 IR safe alg.

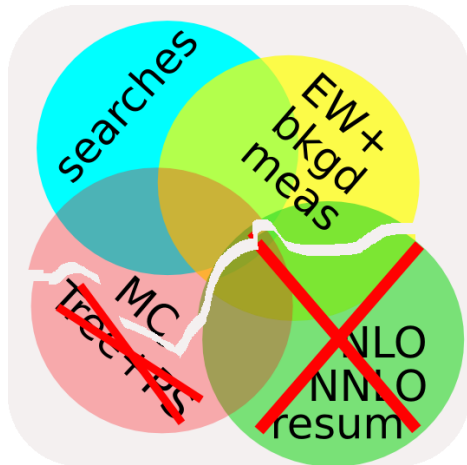
↔

new-physics search
 LO+MC v. data
 IR safe alg.

Does lack of IRC safety matter?

I do searches, not QCD. Why should I care about IRC safety?

- ▶ Are you looking for a mass-peak?
 - ➔ you needn't care much
- ▶ Are you looking for an excess over bkgd?
 - ➔ you need control samples, validated against QCD



$W+1,2,3$ jets
 NLO v. data
 IR safe alg.

↔

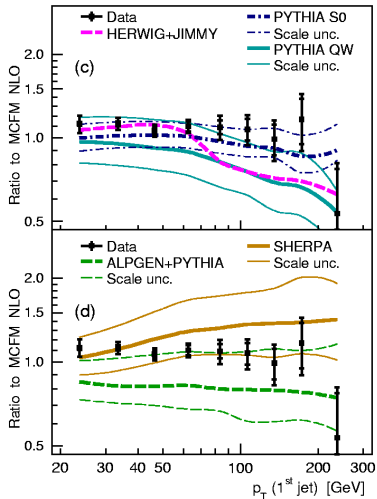
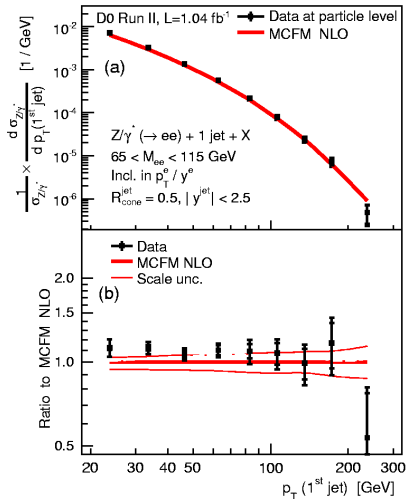
$W+n$ jets
 LO, LO+MC v. data
 IR safe alg.

↔

new-physics search
 LO+MC v. data
 IR **unsafe** alg.

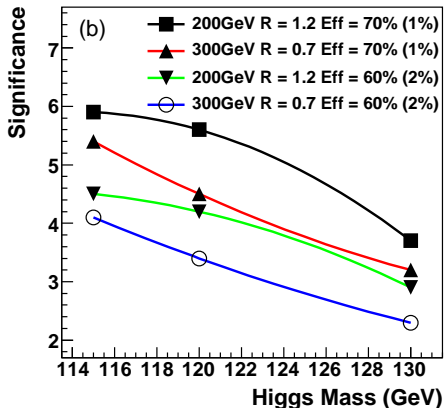
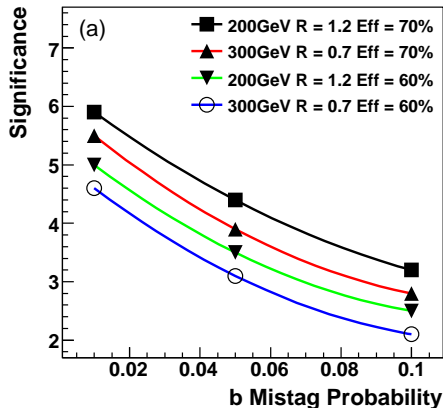
NLO

LO+PS



Cross section for signal and the Z +jets background in the leptonic Z channel for $200 < p_{TZ}/\text{GeV} < 600$ and $110 < m_J/\text{GeV} < 125$, with perfect b -tagging; shown for our jet definition (C/A MD-F), and other standard ones close to their optimal R values.

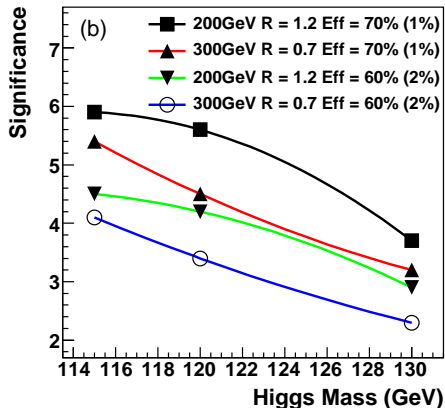
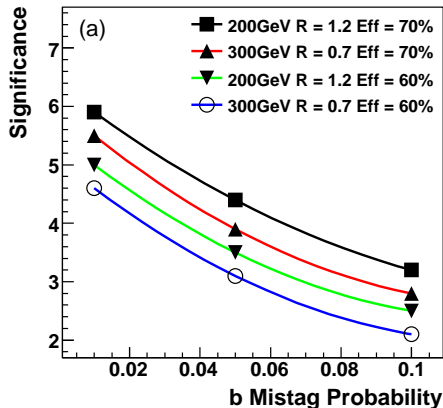
Jet definition	σ_S/fb	σ_B/fb	$S/\sqrt{B \cdot \text{fb}}$
C/A, $R = 1.2$, MD-F	0.57	0.51	0.80
k_t , $R = 1.0$, y_{cut}	0.19	0.74	0.22
SISCone, $R = 0.8$	0.49	1.33	0.42
anti- k_t , $R = 0.8$	0.22	1.06	0.21



Most scenarios above 3σ

For it to be a significant discovery channel requires decent b -tagging, lowish mass Higgs [and good experimental resolution]

In nearly all cases, looks feasible for extracting WH , ZH couplings



Most scenarios above 3σ

For it to be a significant discovery channel requires decent b -tagging, lowish mass Higgs [and good experimental resolution]

In nearly all cases, looks feasible for extracting WH , ZH couplings