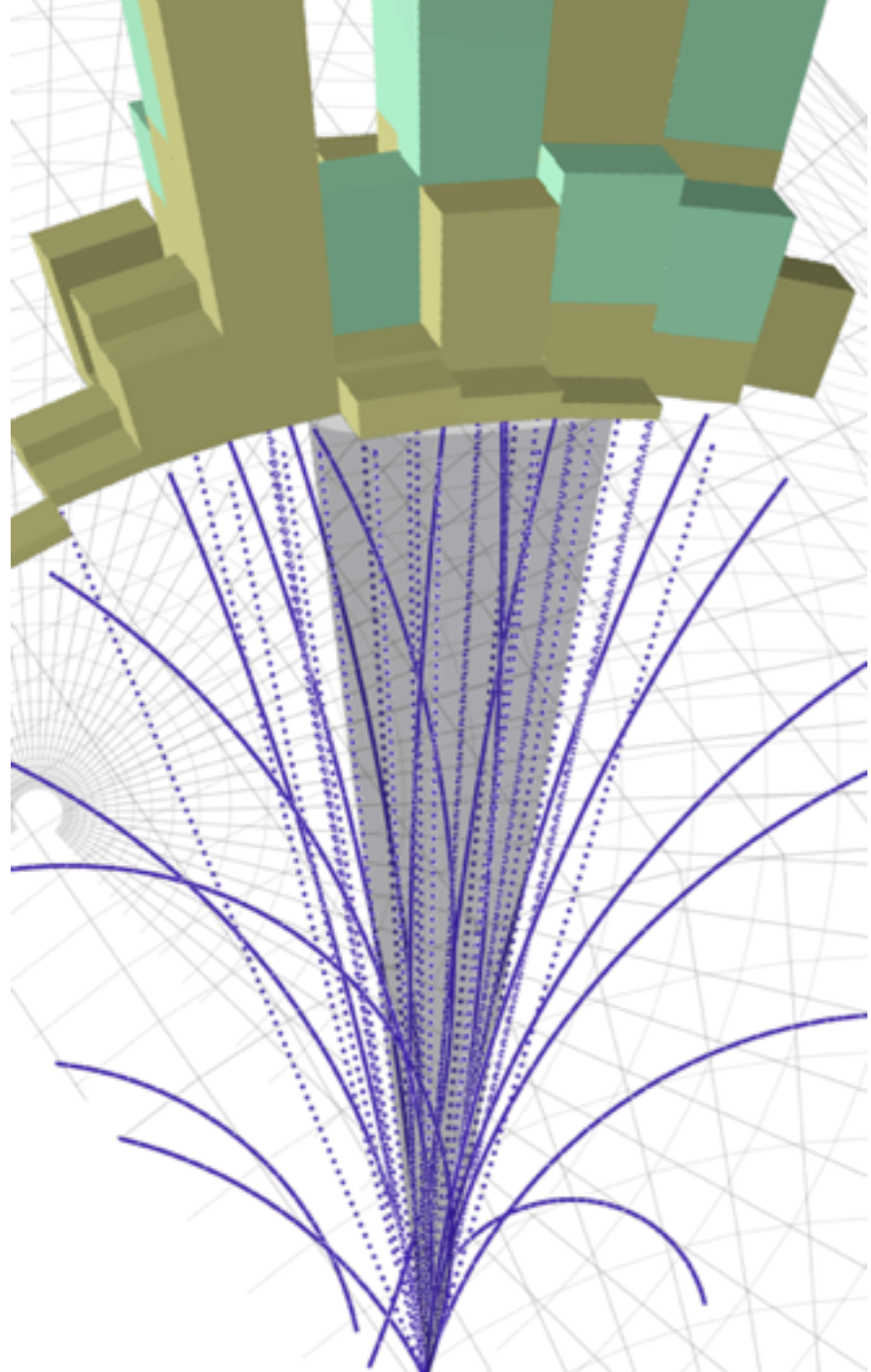


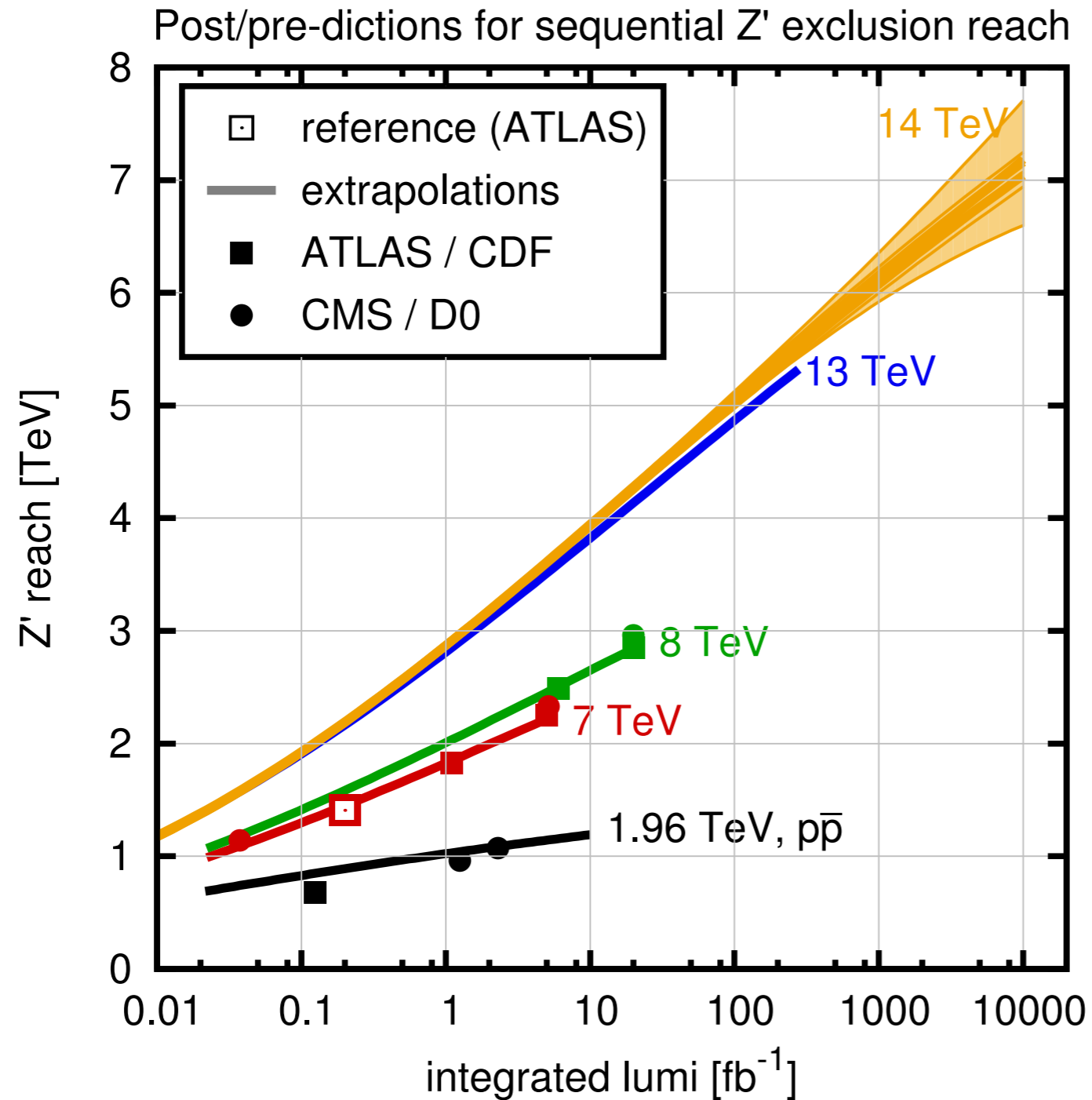
Analytics for jet substructure



Gavin Salam (CERN)
based on work with Dasgupta, Fregoso & Marzani

*Physics challenges in the face of LHC-14
Madrid, September 2014*

LHC reach v. lumi



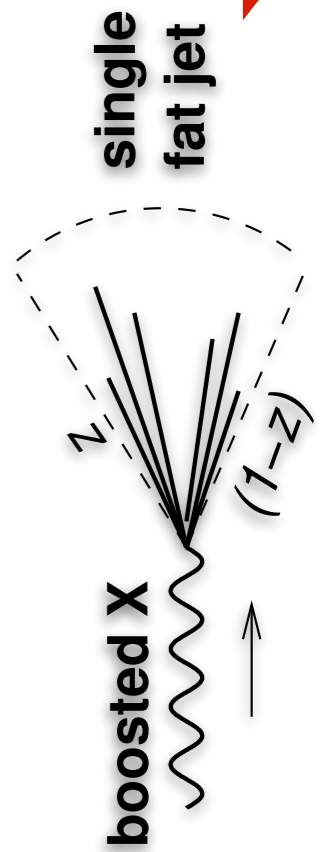
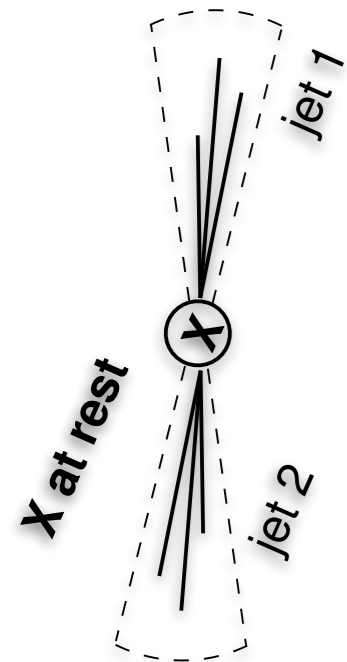
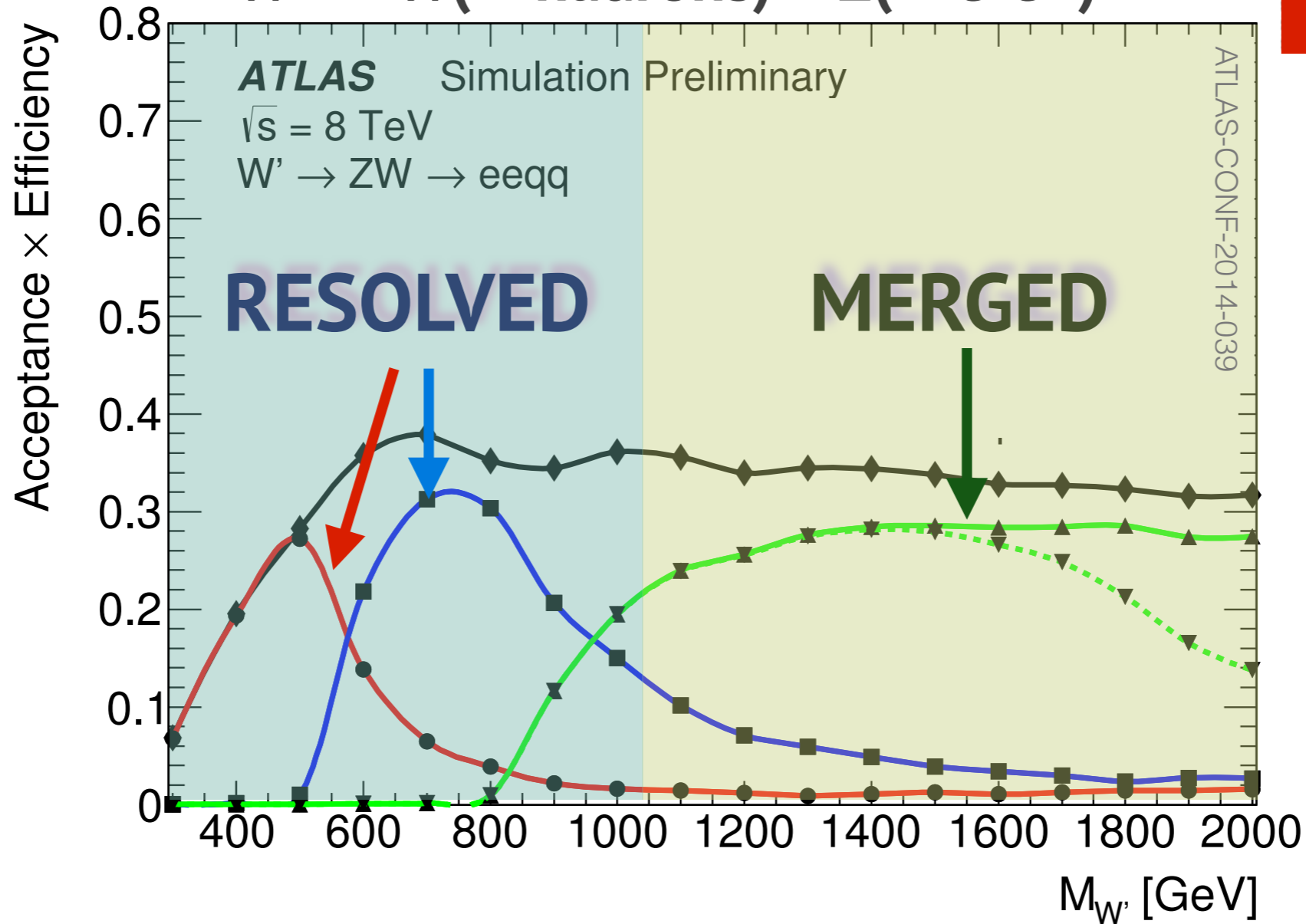
LHC8 → HL-LHC14
x ~2.2 in mass

Tevatron → LHC8
x ~3 in mass

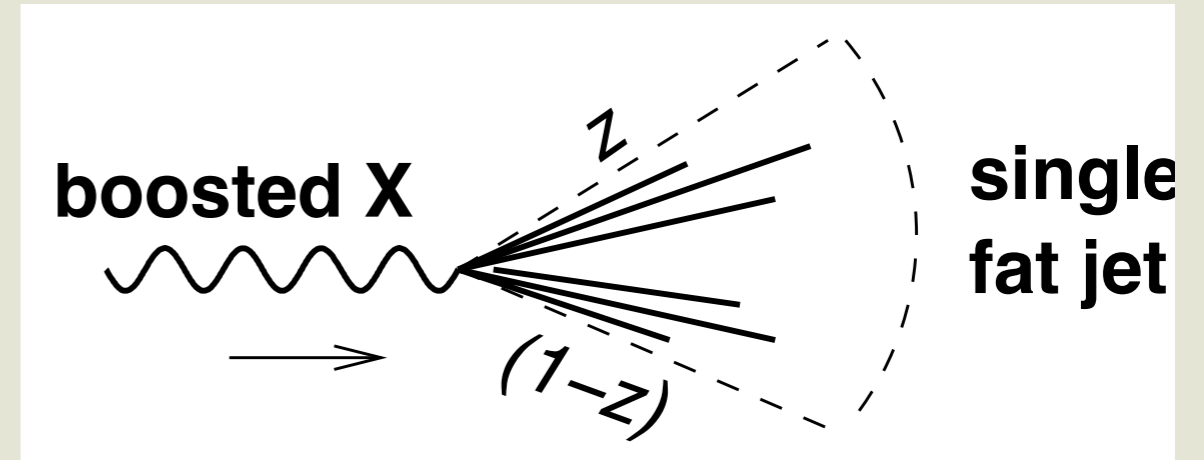
Boosted searches

LHC 13/14

$$W' \rightarrow W(\rightarrow \text{hadrons}) + Z(\rightarrow e^+e^-)$$



Most obvious way of detecting a boosted decay is through the mass of the jet

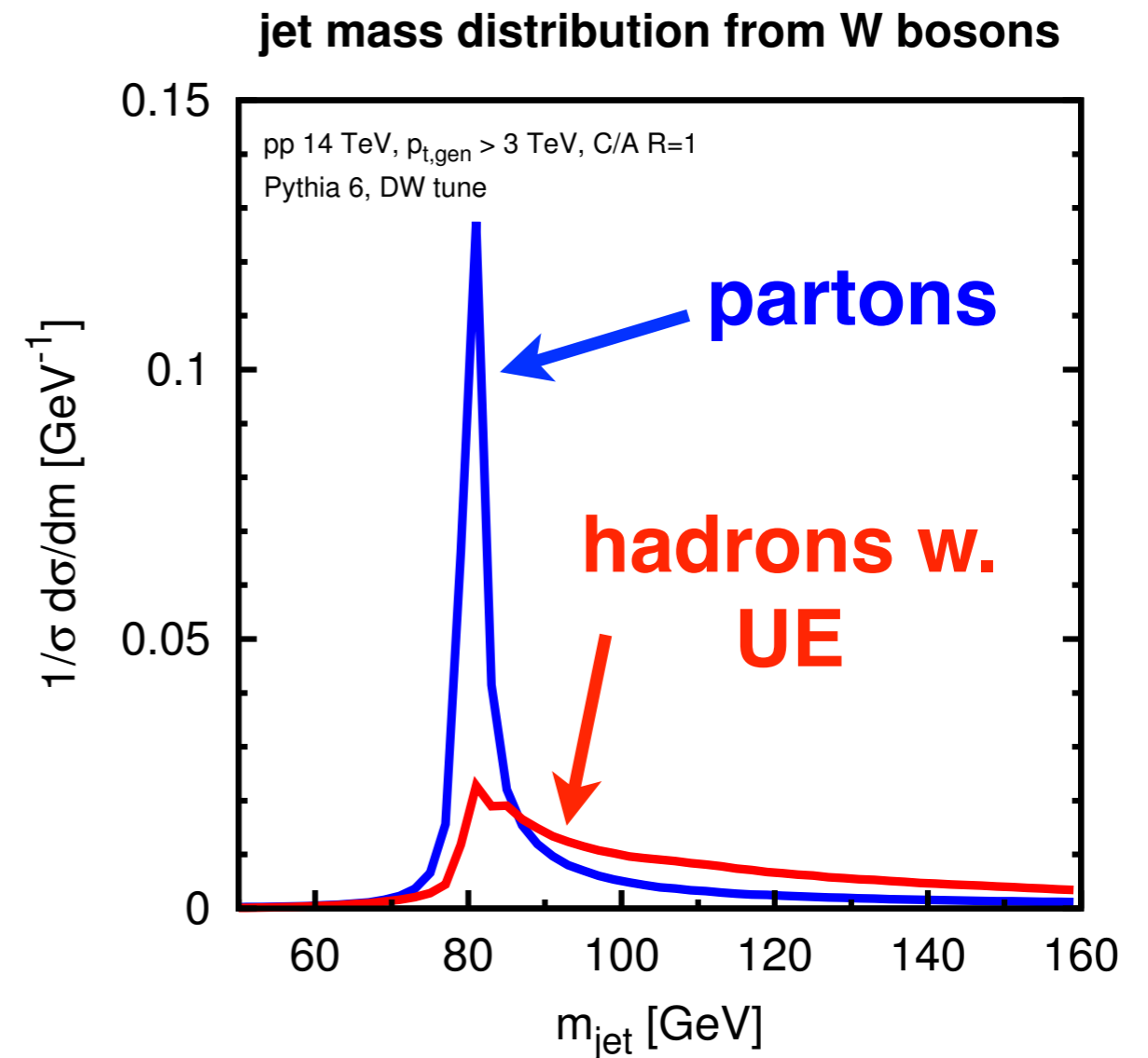


But jet mass is **poor** in practice:

e.g., narrow W resonance highly smeared by QCD radiation

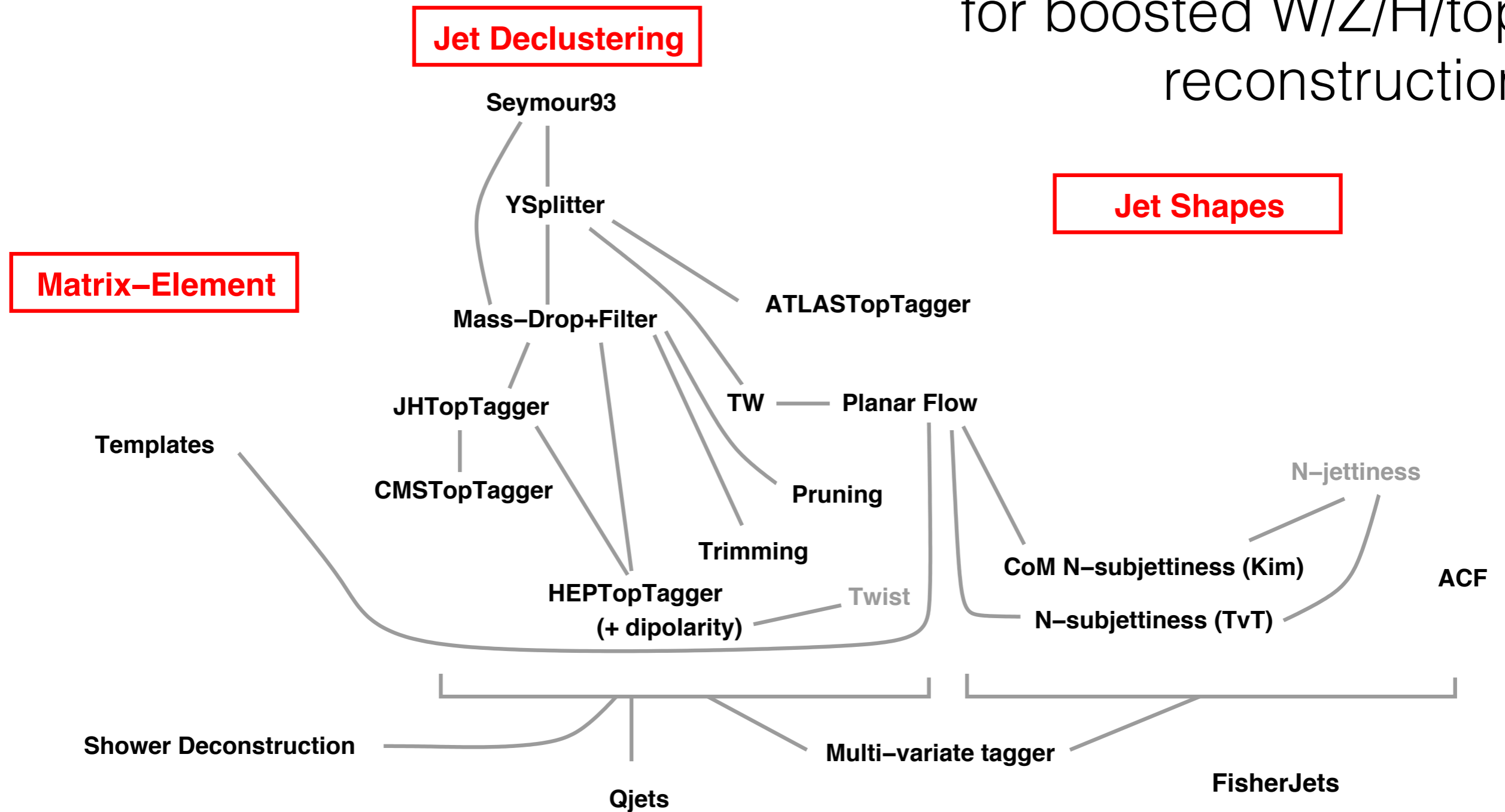
(mainly underlying event/pileup)

cf. calculations by Rubin '10



Very active research field

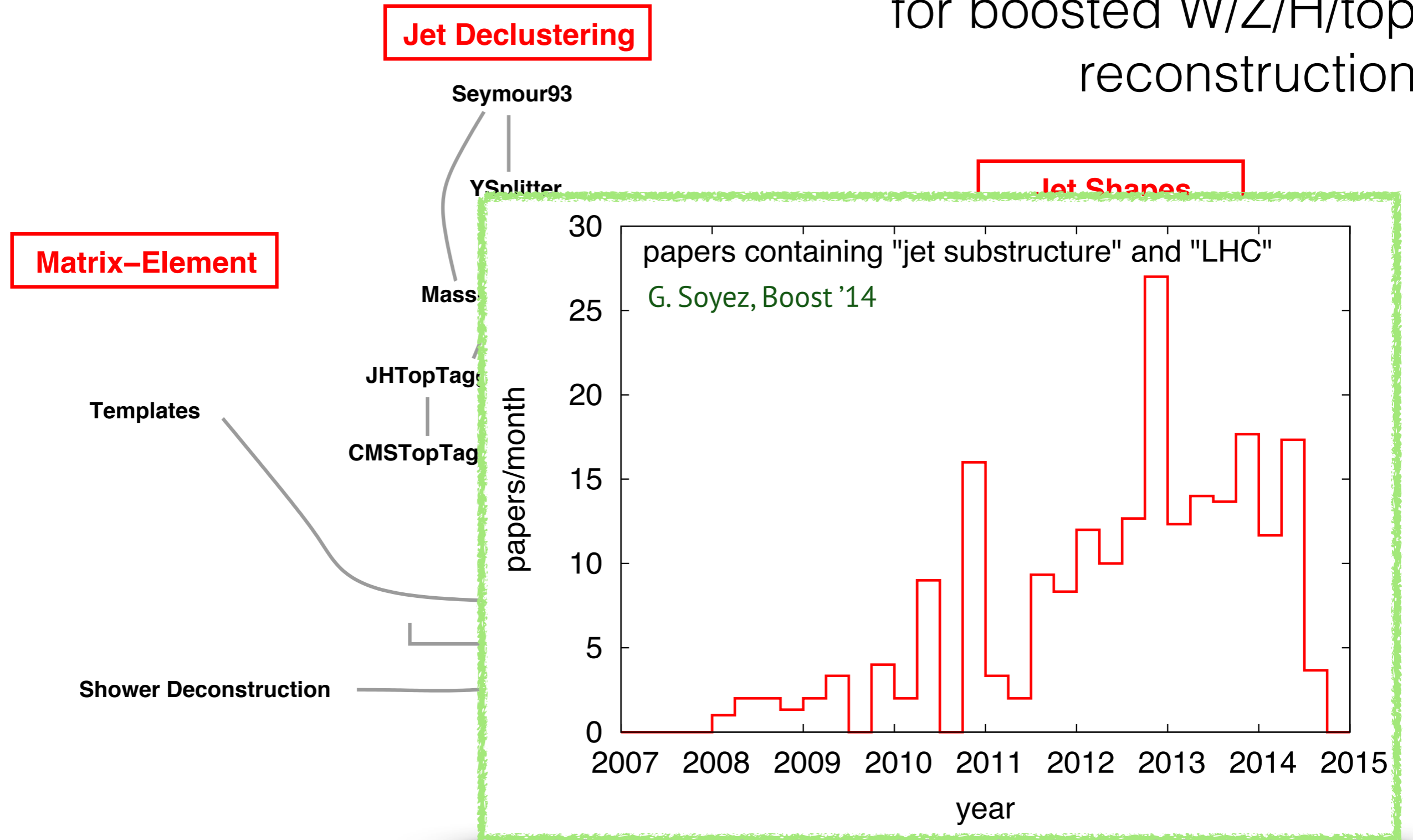
Some of the tools developed for boosted W/Z/H/top reconstruction



apologies for omitted taggers, arguable links, etc.

Very active research field

Some of the tools developed for boosted W/Z/H/top reconstruction



To fully understand “Boost” you want to study all possible signal (W/Z/H/top/...) and QCD jets.

But you need to start somewhere.

We chose the QCD jets because:

(a) they have the richest structure.

(b) once you know understand the QCD jets, the route for understanding signal jets becomes clear too.

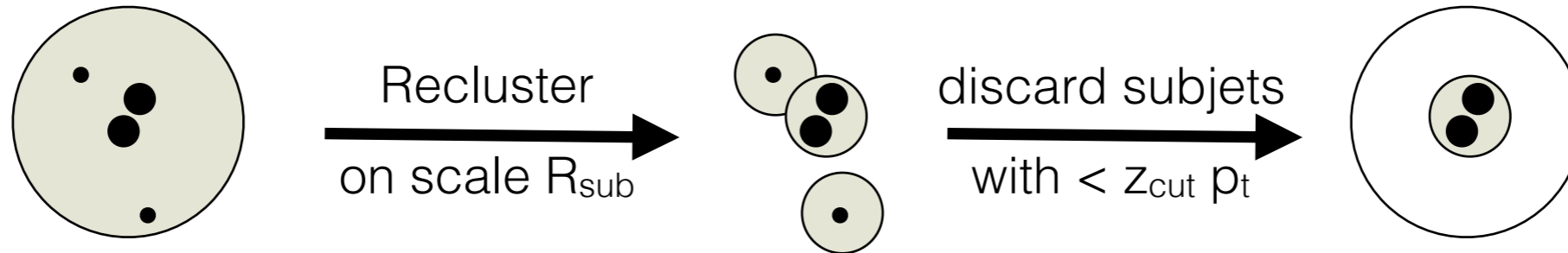
arXiv:1307.0007

Dasgupta, Fregoso, Marzani & GPS

+Dasgupta, Fregoso, Marzani & Powling, 1307.0013

Cannot possibly study all tools
These 3 are widely used

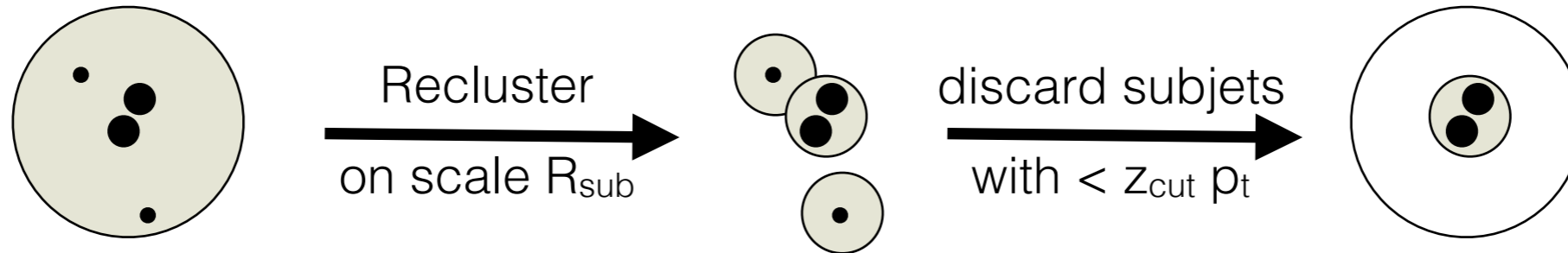
Trimming



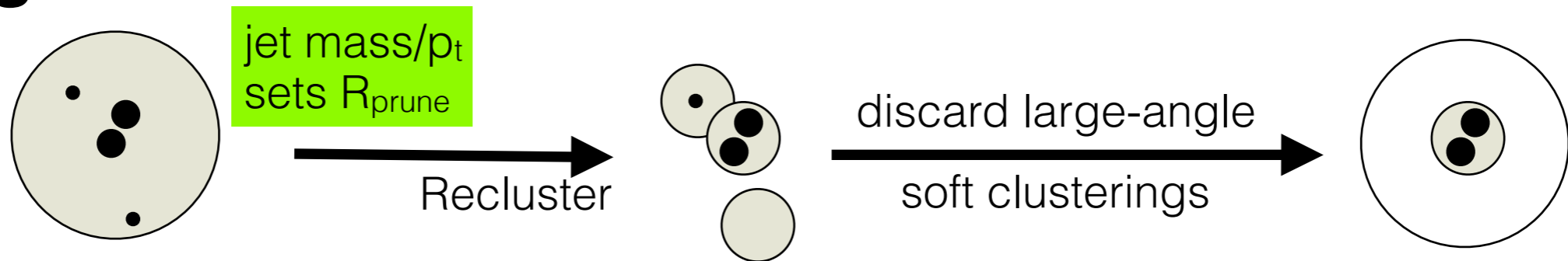
study 3 taggers/groomers

Cannot possibly study all tools
These 3 are widely used

Trimming



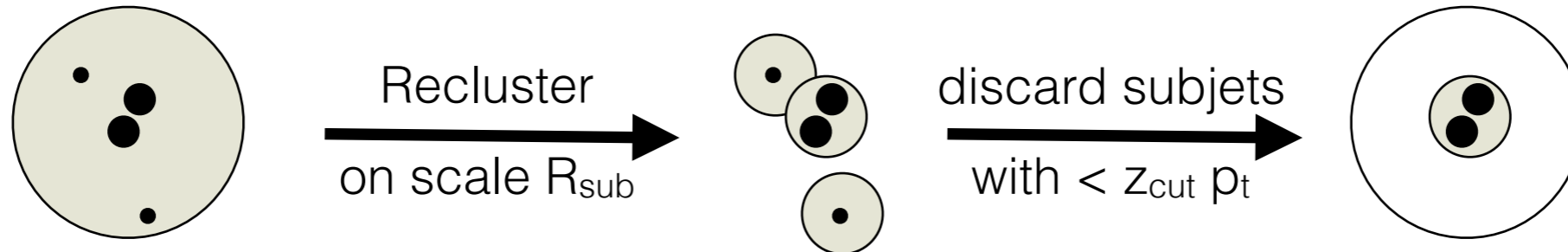
Pruning



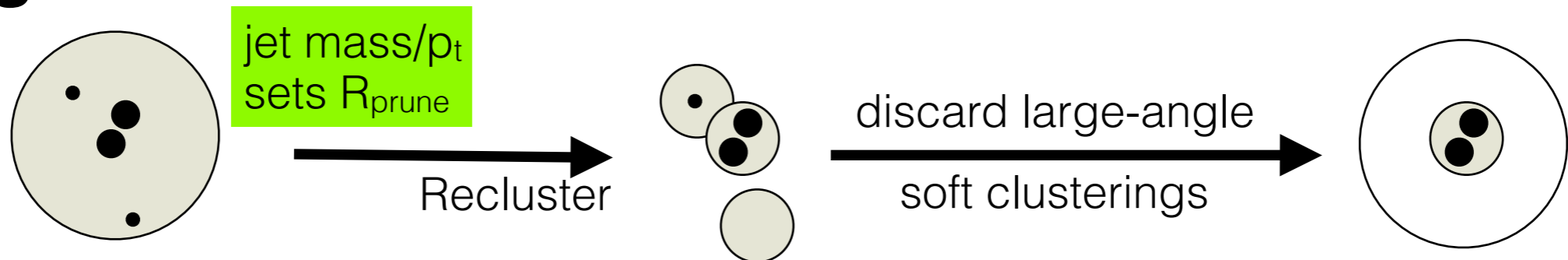
study 3 taggers/groomers

Cannot possibly study all tools
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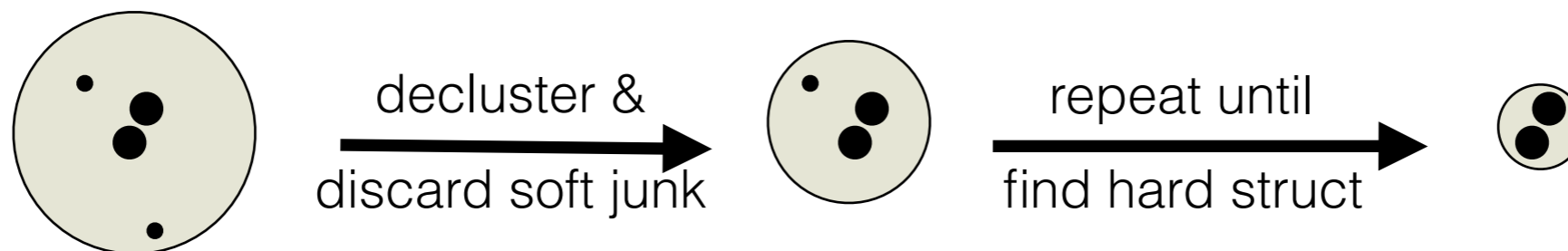
Trimming



Pruning



Mass-drop tagger (MDT, aka BDRS)



For phenomenology

Jet mass: m

*[as compared to $W/Z/H$
or top mass]*

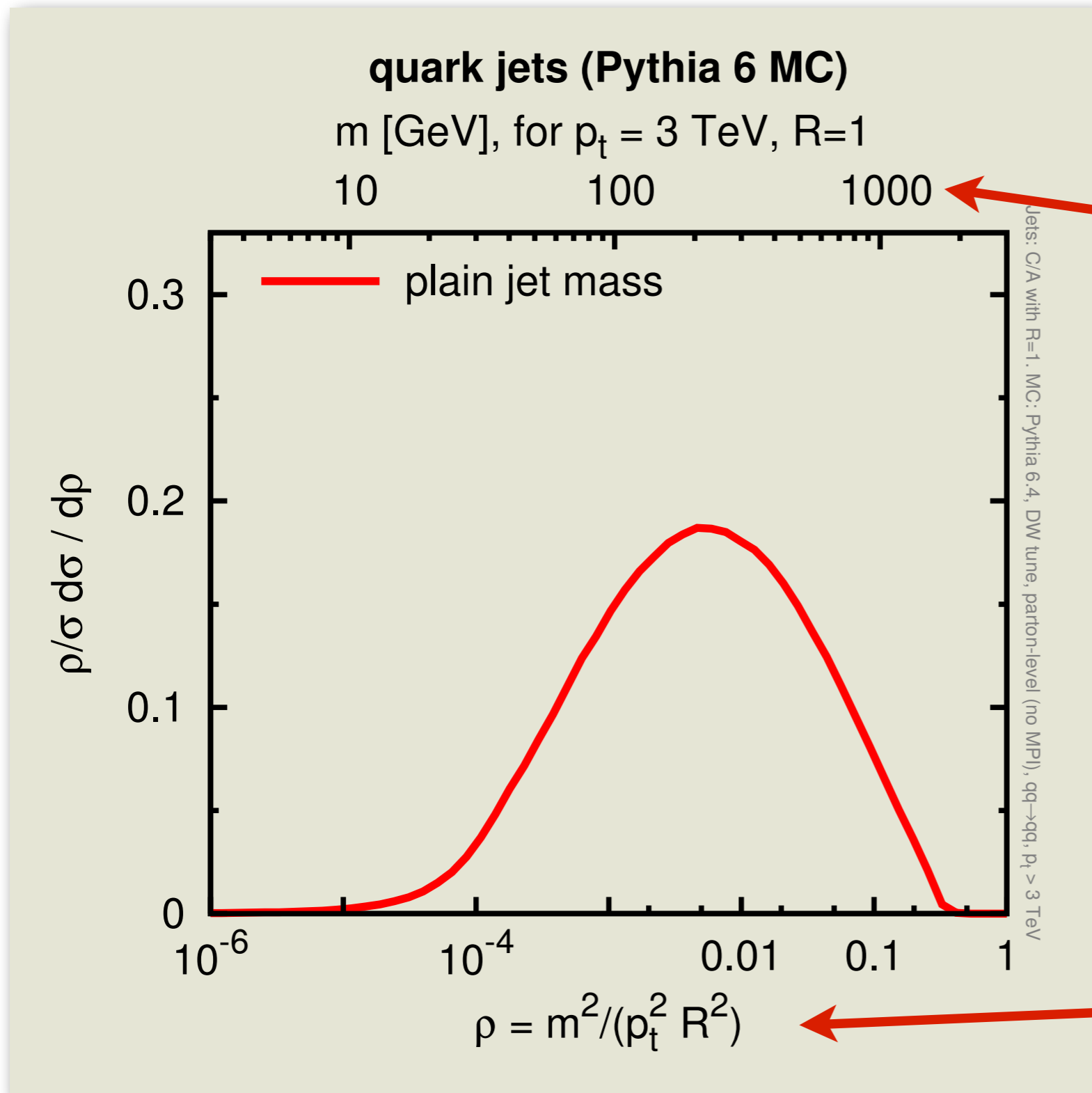
For QCD calculations

$$\rho = \frac{m^2}{p_t^2 R^2}$$

*[R is jet opening angle
– or radius]*

Because ρ is invariant under
boosts along jet direction

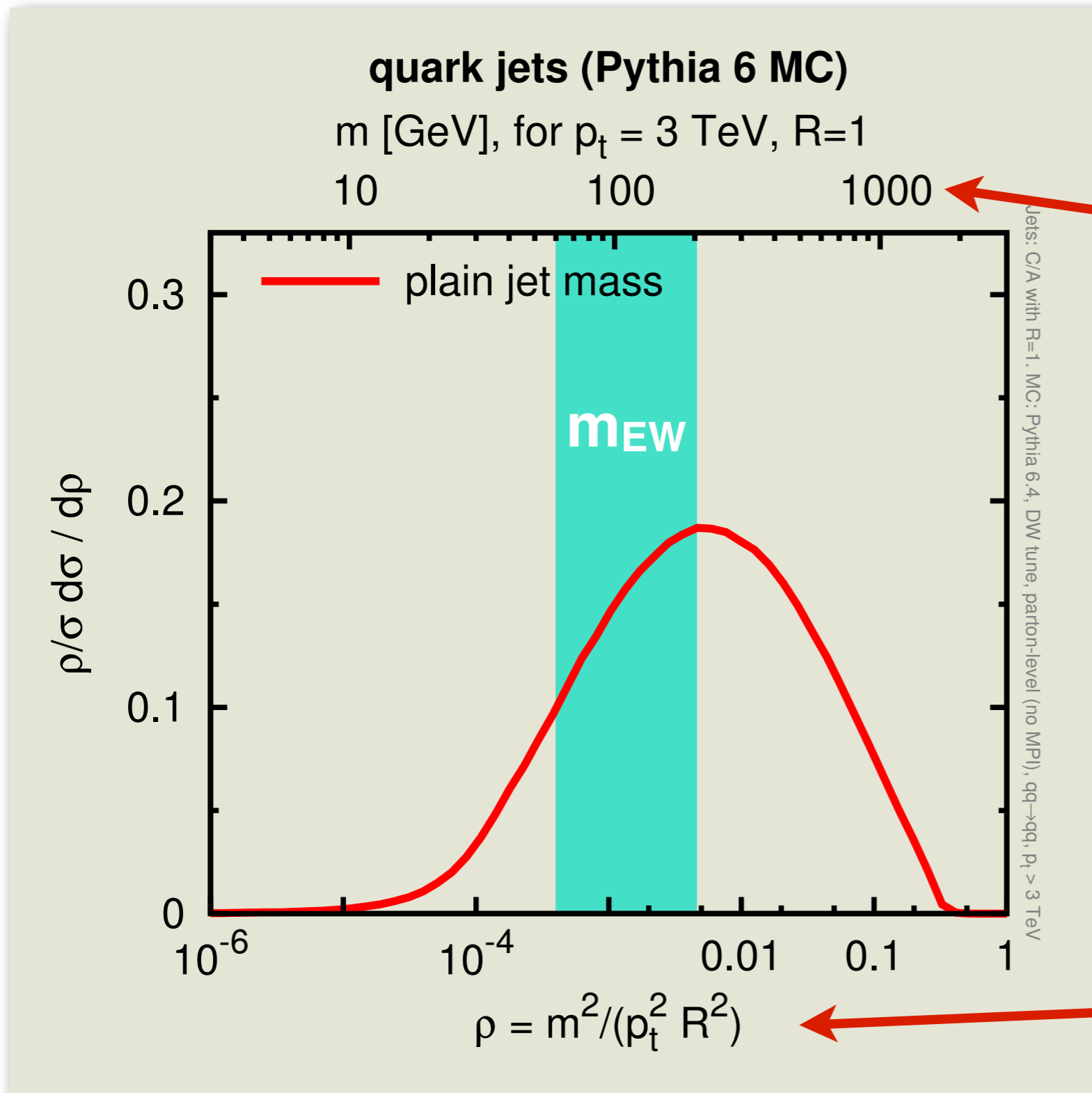
The “right” MC study can already be instructive (testing on quark [background] jets)



Physical mass for
3 TeV, $R=1$ jets

$\rho \sim$ Rescaled mass²
(i.e. the QCD variable)

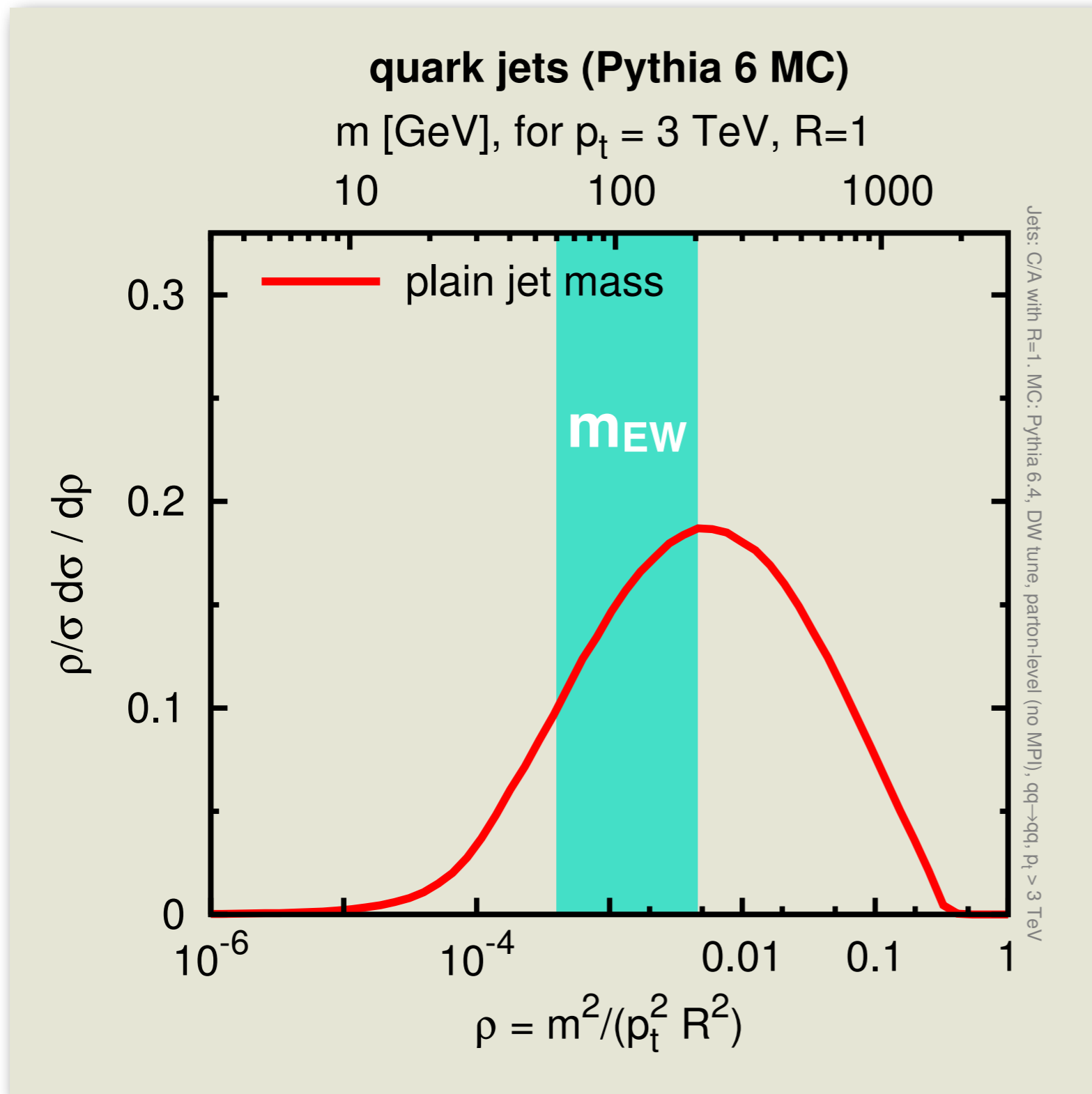
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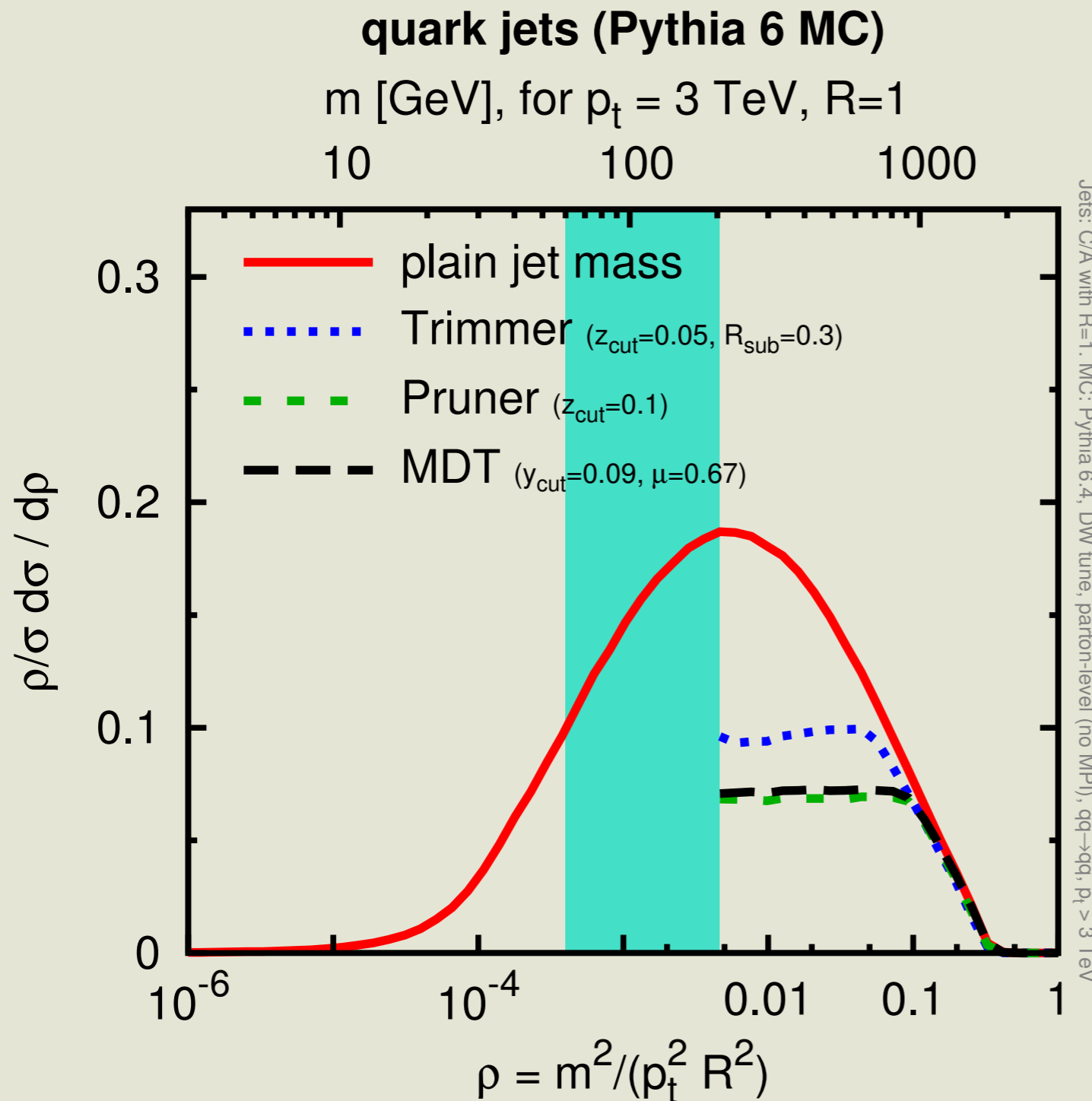
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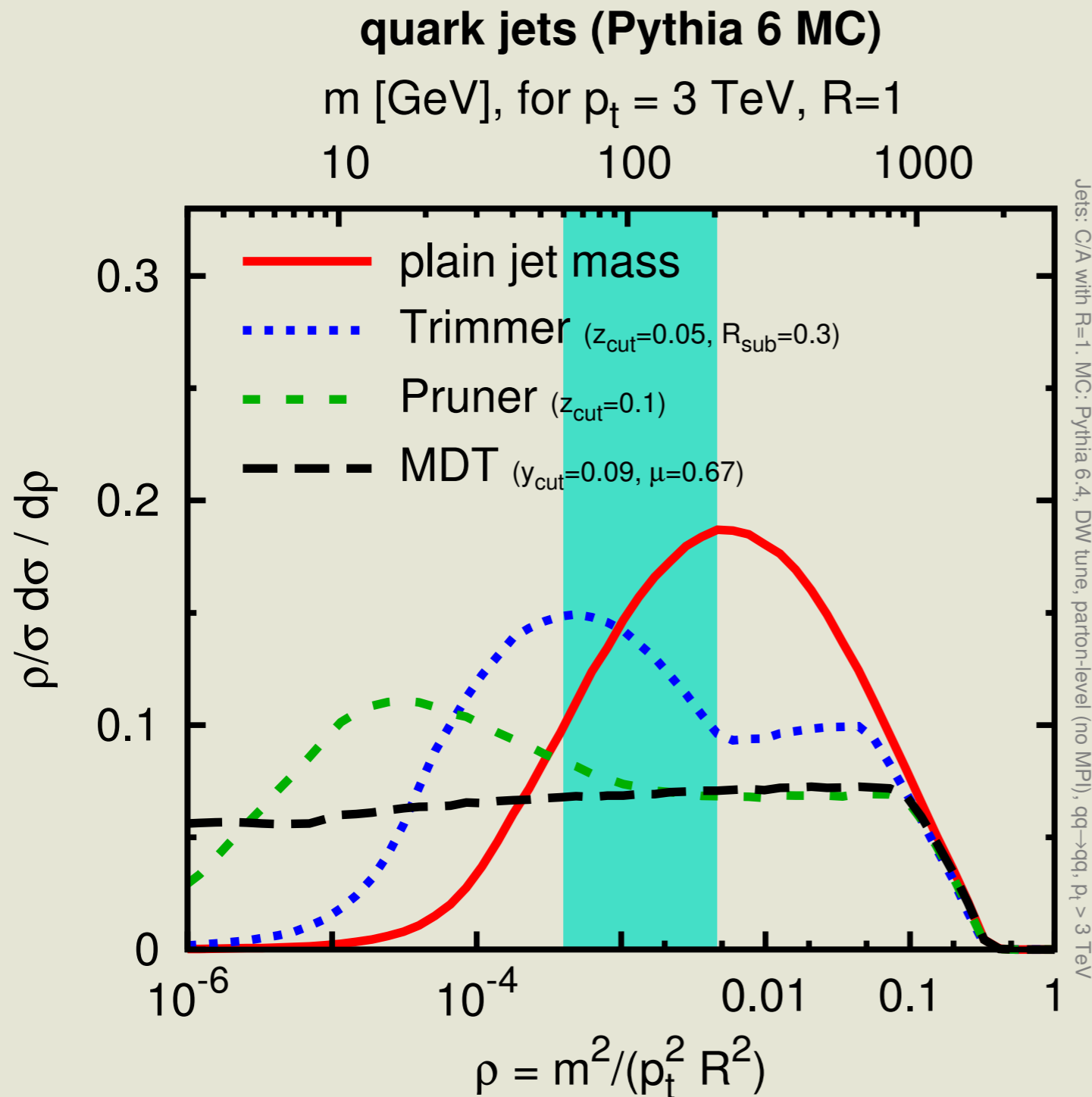


The “right” MC study can already be instructive (testing on quark [background] jets)



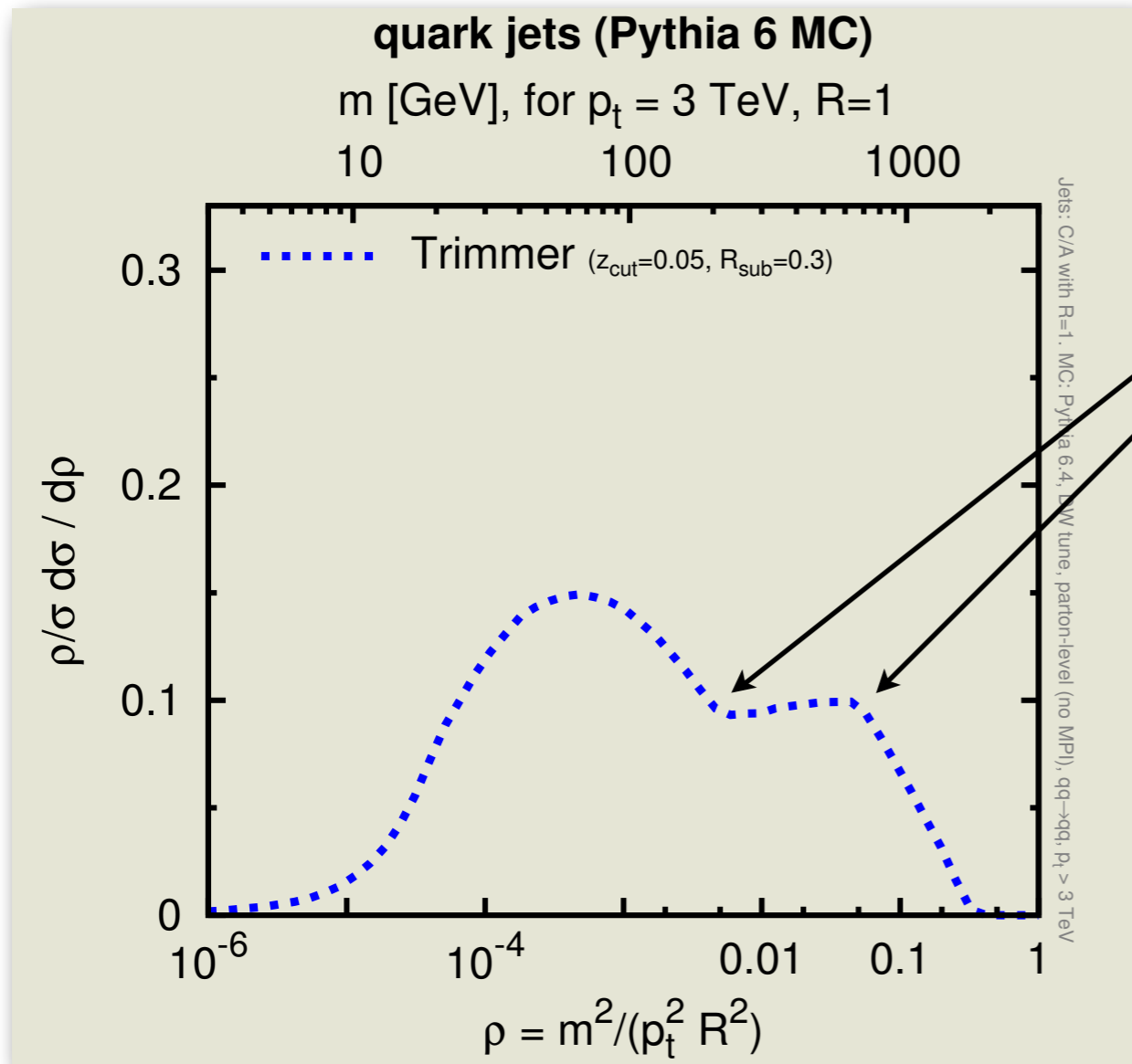
Different taggers
can be
quite similar

The “right” MC study can already be instructive (testing on quark [background] jets)



But only for a
limited range
of masses

What might we want to find out?



Where exactly are the kinks?
How do their locations depend
on $z_{\text{cut}}, R_{\text{sub}}$?

Kinks are especially
dangerous for data-
driven backgrounds

What physics is relevant in the
different regions?

Because then you have
an idea of how well you
control it

And maybe you can
make better taggers

Key calculations related to plain jet mass

- Catani, Turnock, Trentadue & Webber, '91: **heavy-jet mass in e^+e^-**
- Dasgupta & GPS, '01: **hemisphere jet mass in e^+e^-** (and DIS)
(\rightarrow non-global logs)
- Appleby & Seymour, '02; Delenda, Appleby, Dasgupta & Banfi '06: **impact of jet boundary** (\rightarrow clustering logs)
- Gehrmann, Gehrmann de Ridder, Glover '08; Weinzierl '08
Chien & Schwartz '10: **heavy-jet mass in e^+e^- to higher accuracy**
- Rubin '10: **filtering for jet masses**
- Li, Li & Yuan '12,
Dasgupta, Khelifa-Kerfa, Marzani & Spannowsky '12,
Chien & Schwartz '12,
Jouttenus, Stewart, Tackmann, Waalewijn '13:
jet masses at hadron colliders
- Hatta & Ueda '13: non-global logs beyond large- N_c limit
- Forshaw, Seymour et al '06-'12, Catani, de Florian & Rodrigo '12: factorization breaking terms (aka super-leading logs)

Jet masses are hard! Will tagging/grooming make them impossible?

Matt Schwartz @ Boost 2012



Take all particles in a jet of radius R and recluster them into subjets with a jet definition with radius

$$R_{\text{sub}} < R$$

The subjets that satisfy the condition

$$p_t^{(\text{subjet})} > z_{\text{cut}} p_t^{(\text{jet})}$$

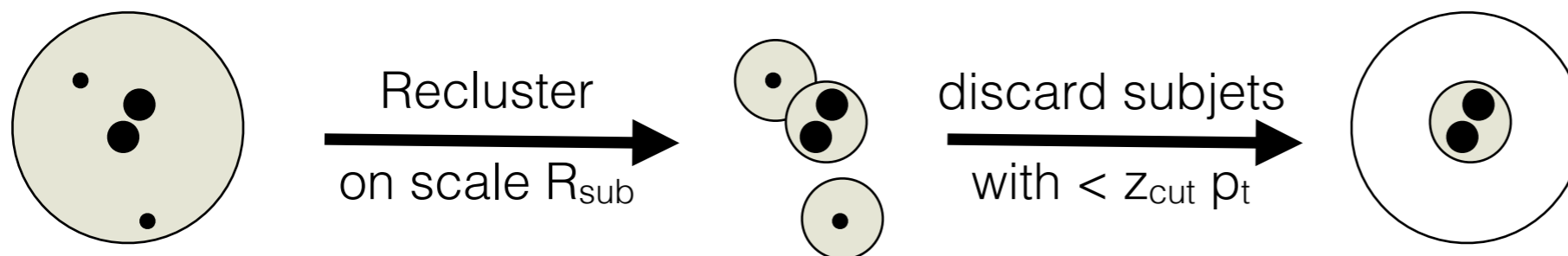
are kept and merged to form the trimmed jet.

Trimming

Krohn, Thaler & Wang '09

two parameters:
 R_{sub} and z_{cut}

Use z_{cut} because signals (bkgds) tend to have large (small) z_{cut}



Take all particles in a jet of radius R and recluster them into subjets with a jet definition with radius

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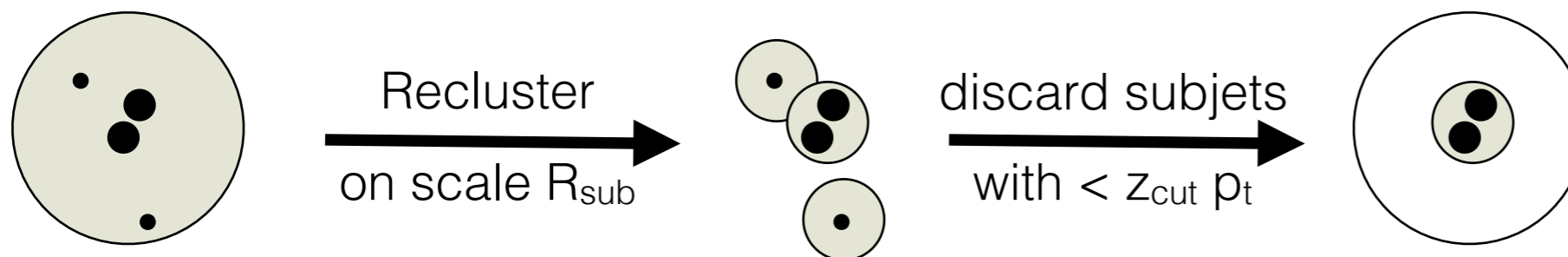
Our approximations

- $\rho \ll 1$
logs of ρ get resummed
- pretend $R \ll 1$
- $Z_{\text{cut}} \ll 1$,
but $(\log Z_{\text{cut}})$ not large

These approximations are not as “wild” as they might sound.

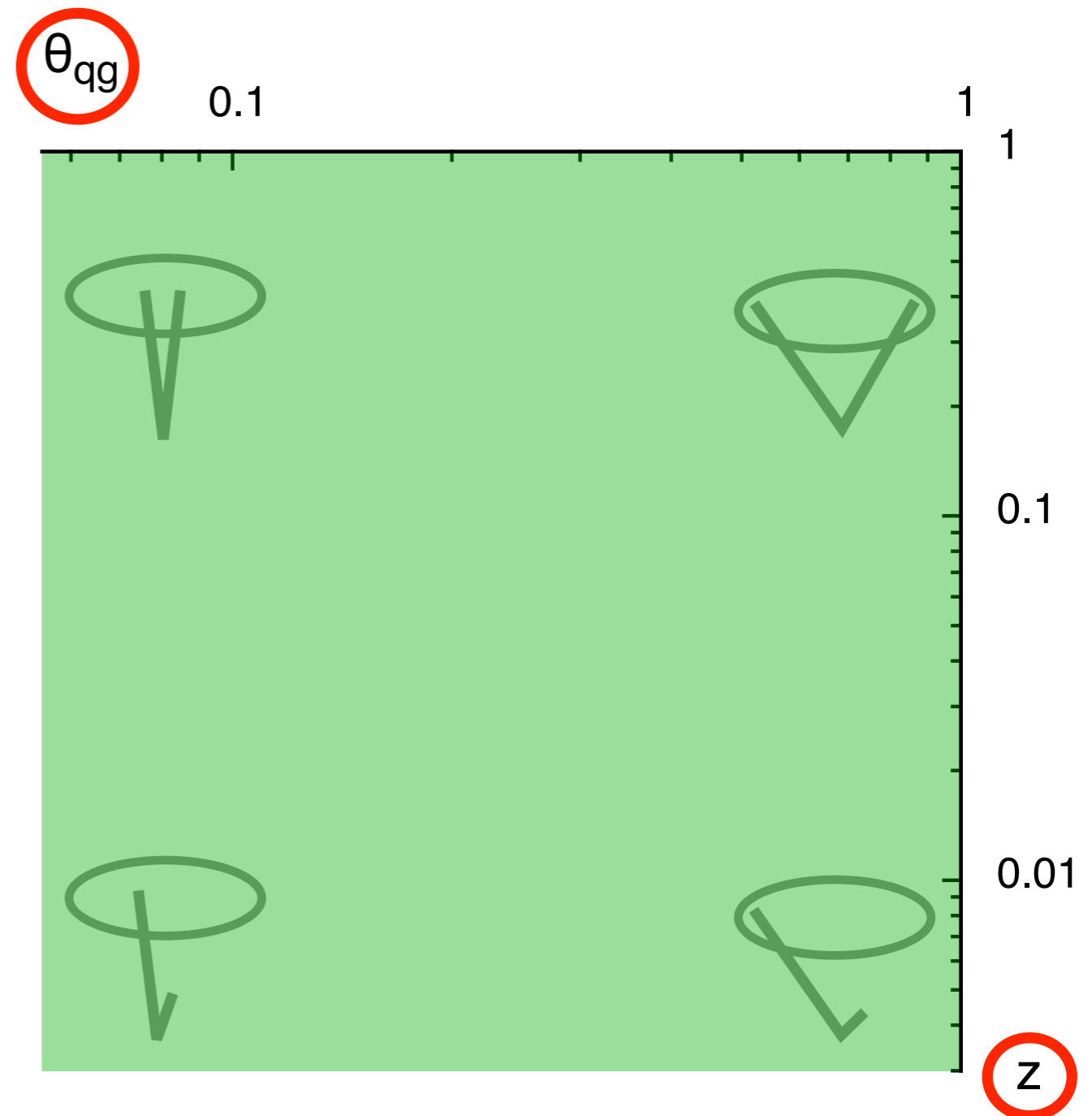
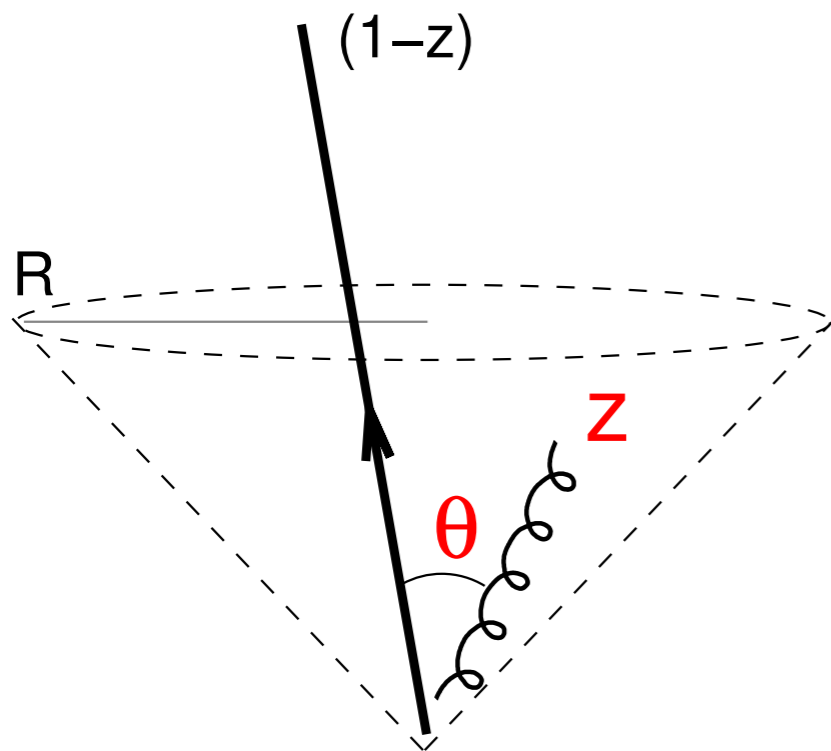
They can also be relaxed.

But our aim for now is to understand the taggers — we leave highest precision calculations till later.



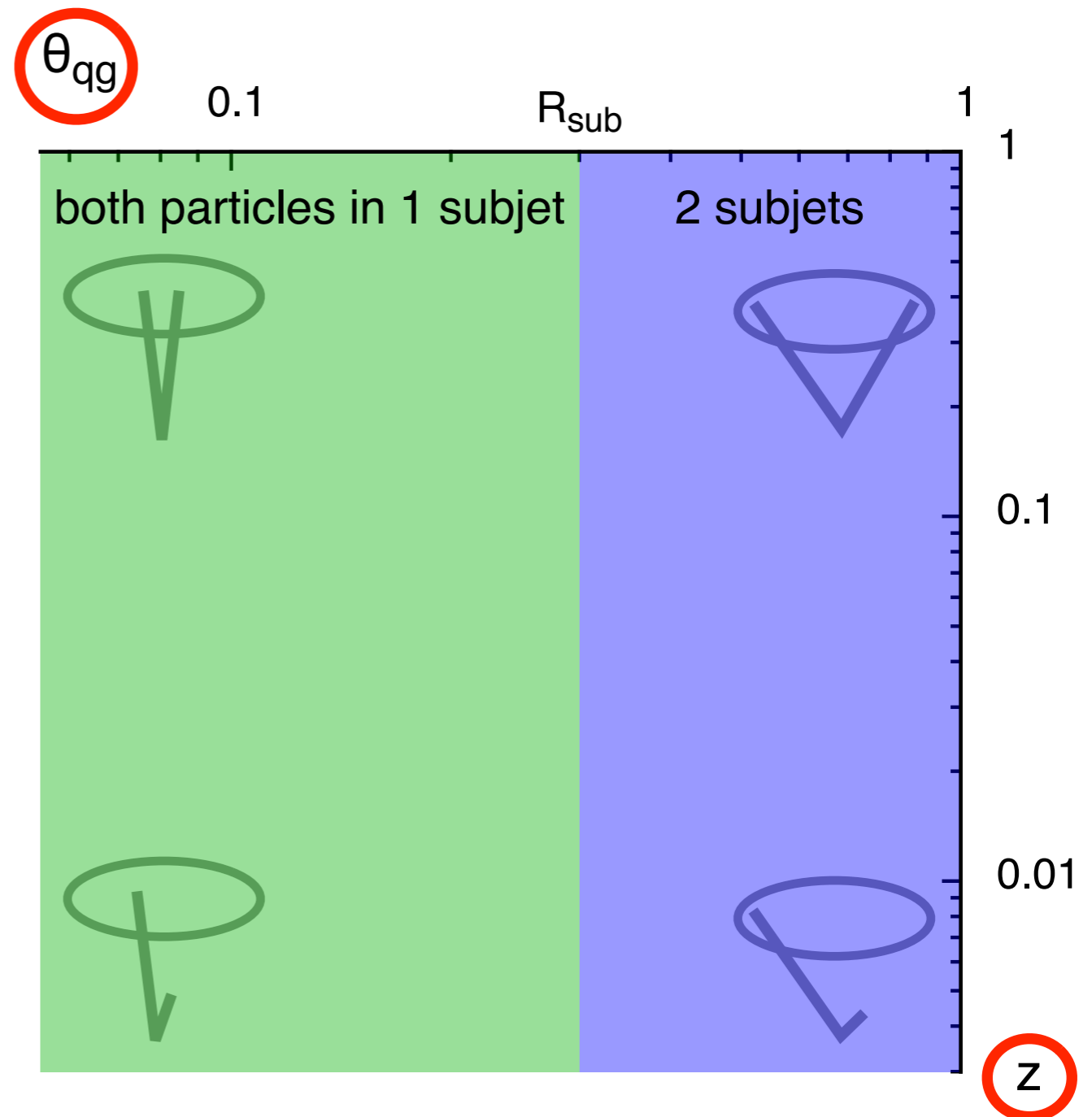
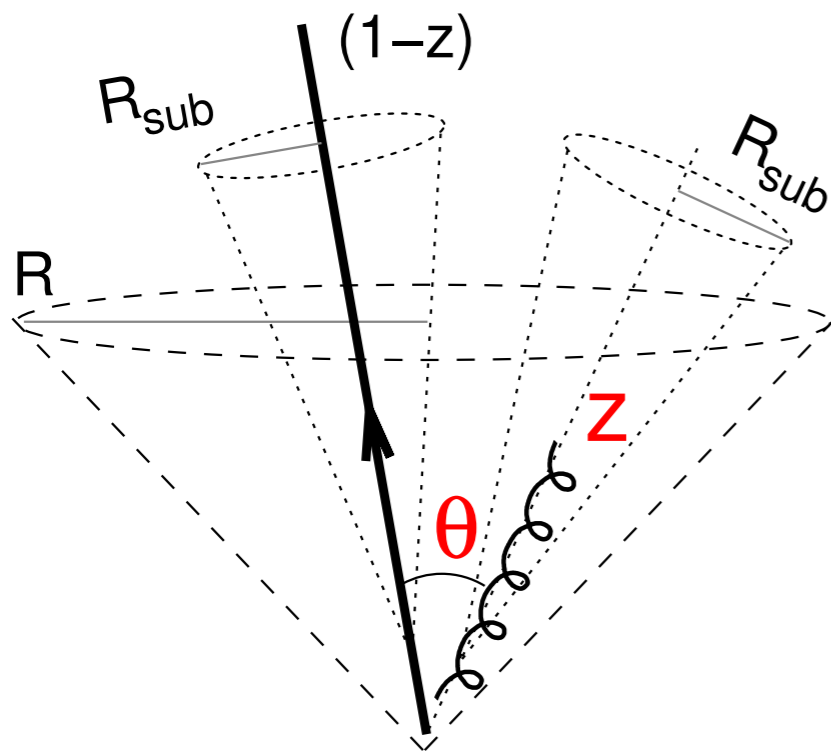
Leading Order — 2-body kinematic plane

At $O(\alpha_s)$, a quark jet emits a gluon. We study this as a function of the gluon momentum fraction z and the quark-gluon opening angle θ



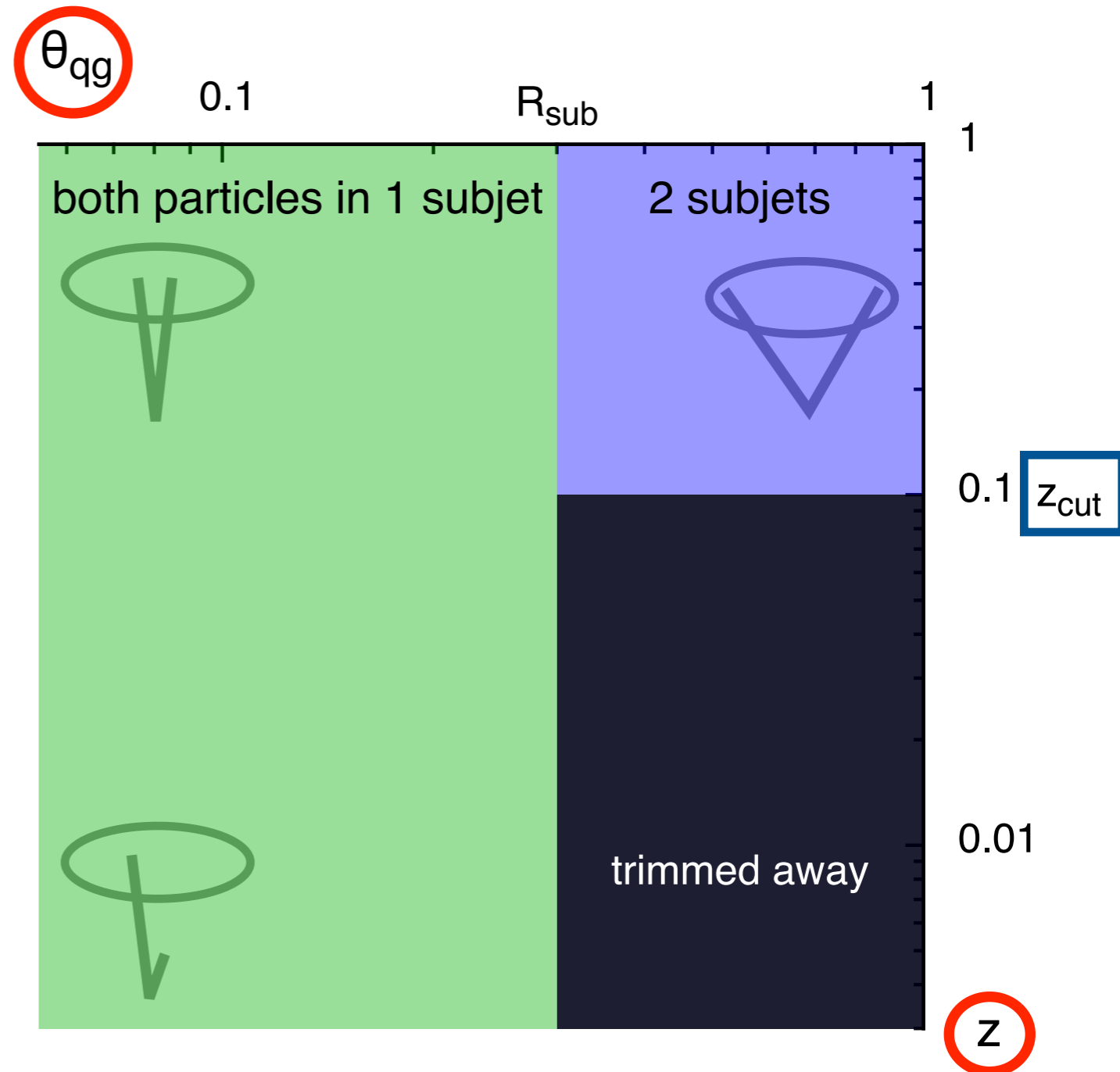
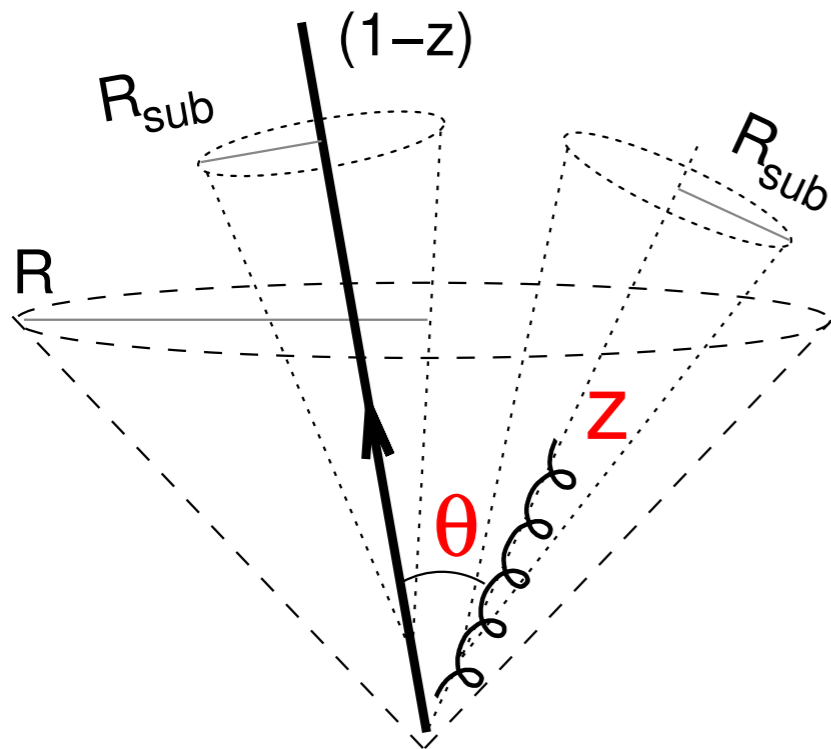
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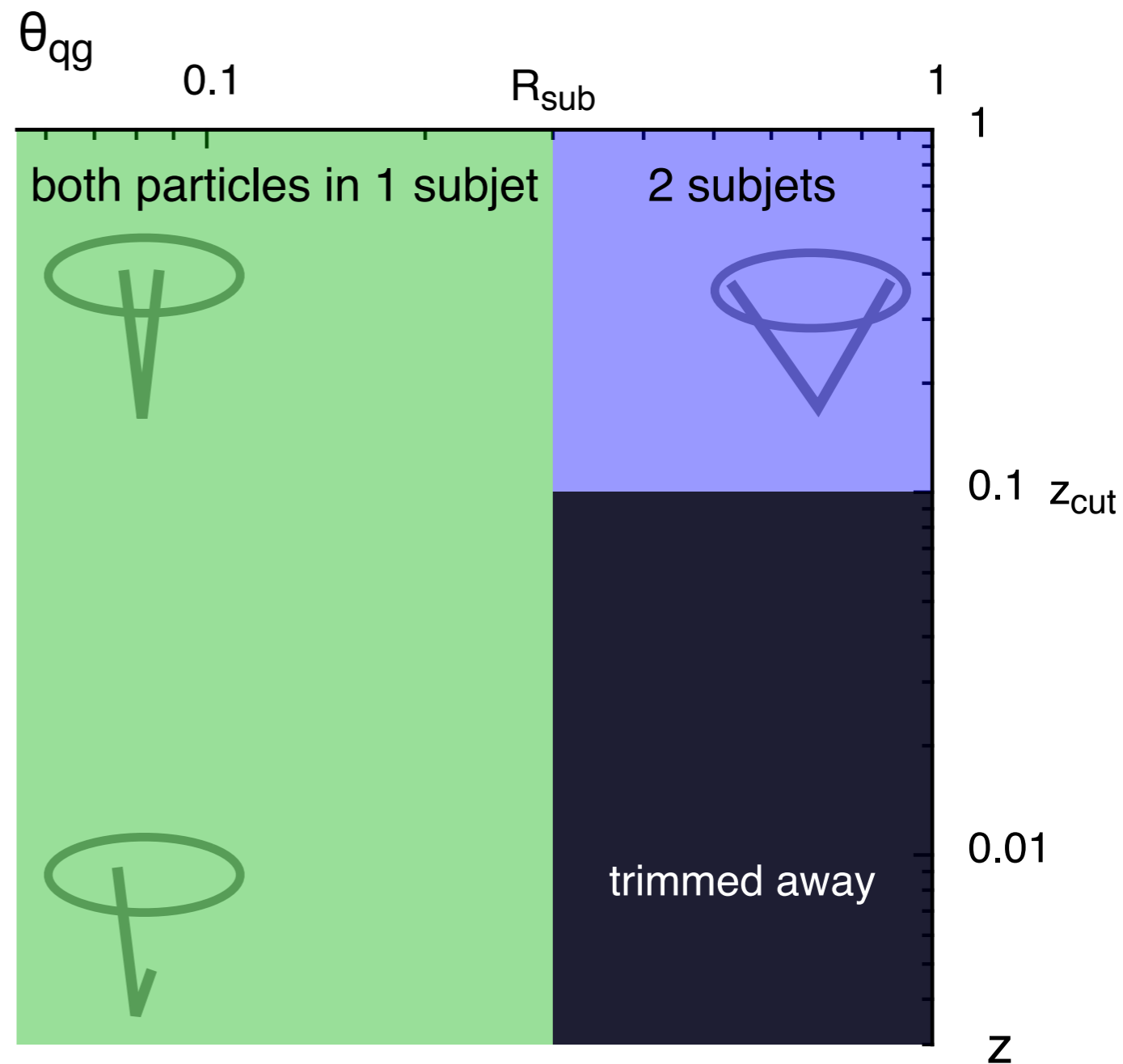
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matrix element

$$\frac{\alpha_s C_F}{\pi} \frac{d\theta^2}{\theta^2} \frac{dz}{z}$$

emission probability \sim constant
in $\log \theta - \log z$ plane



jet mass

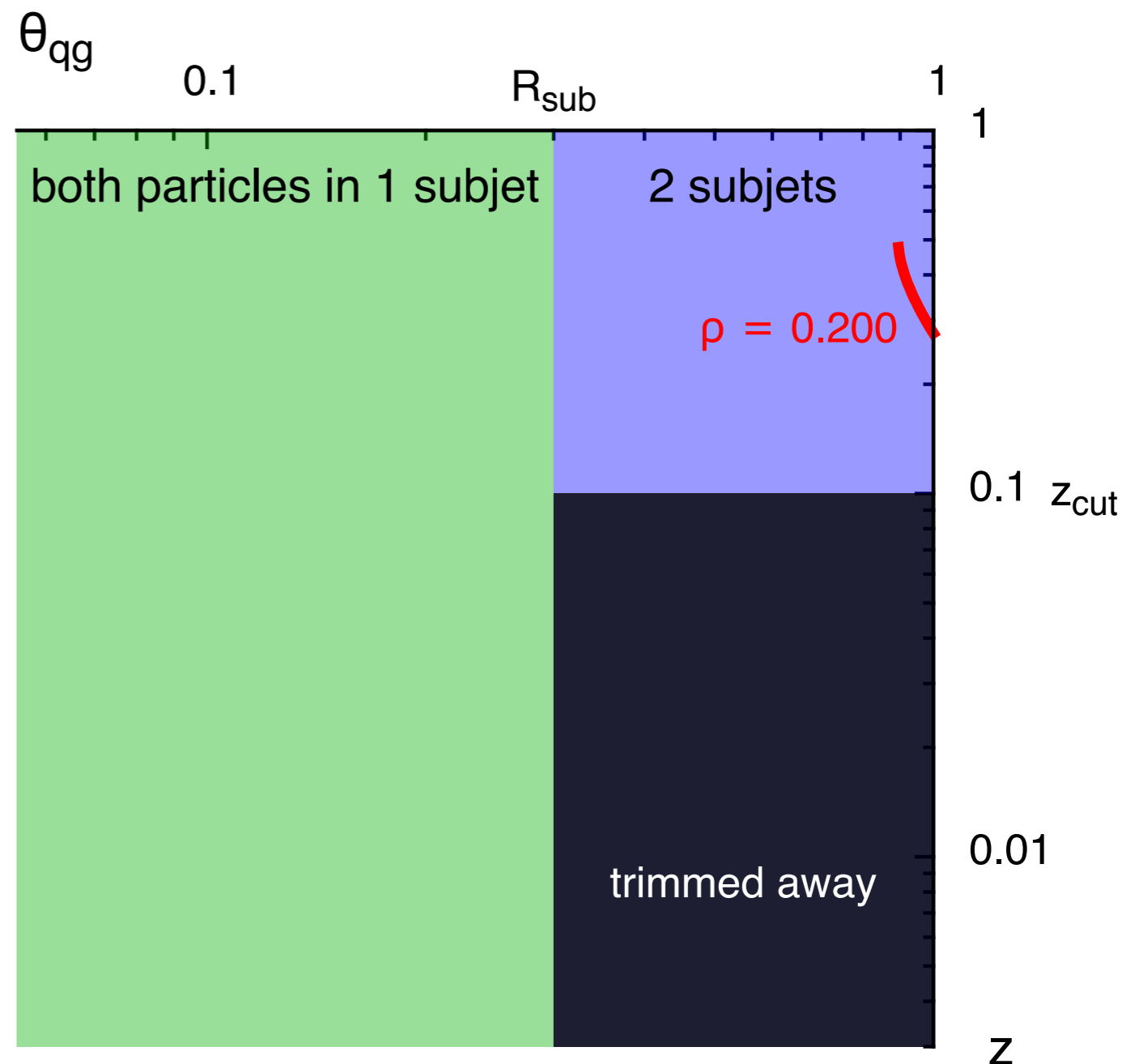
$$\rho = z(1 - z)\theta^2$$

length of **fixed- ρ contour** gives
LO differential cross section

matrix element

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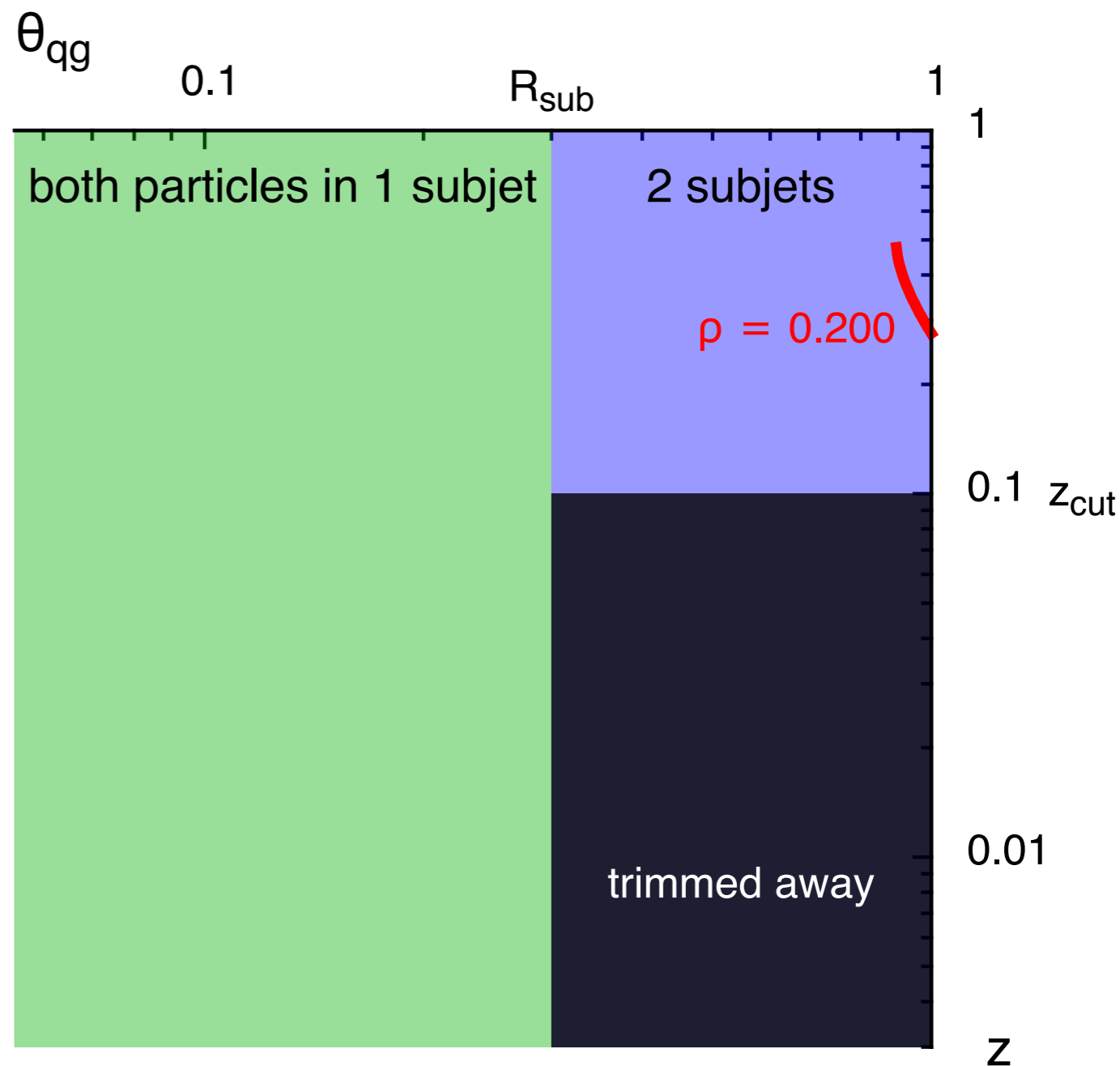
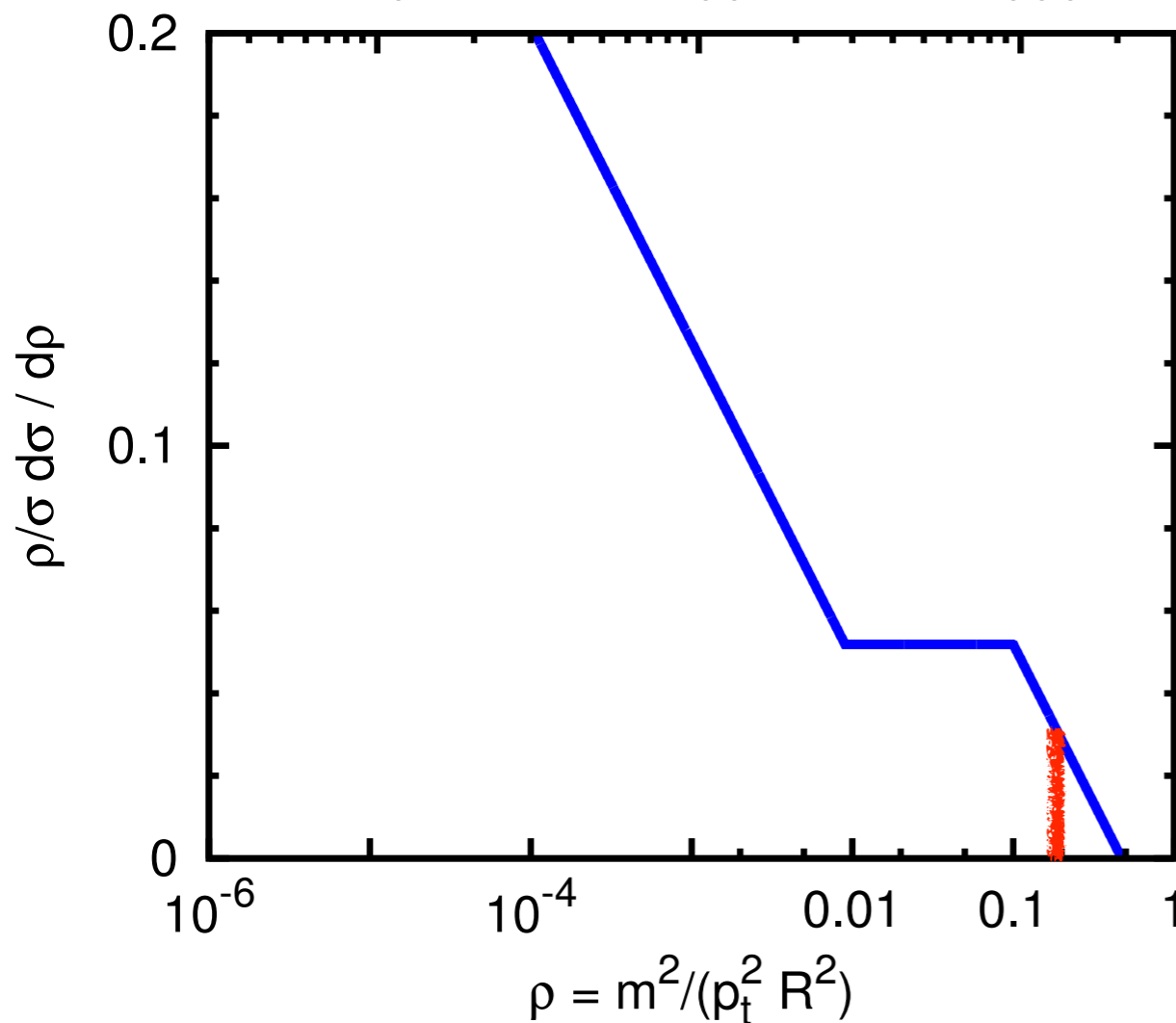
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trimmed quark jets: LO

m [GeV], for $p_t = 3$ TeV, $R=1$

10 100 1000



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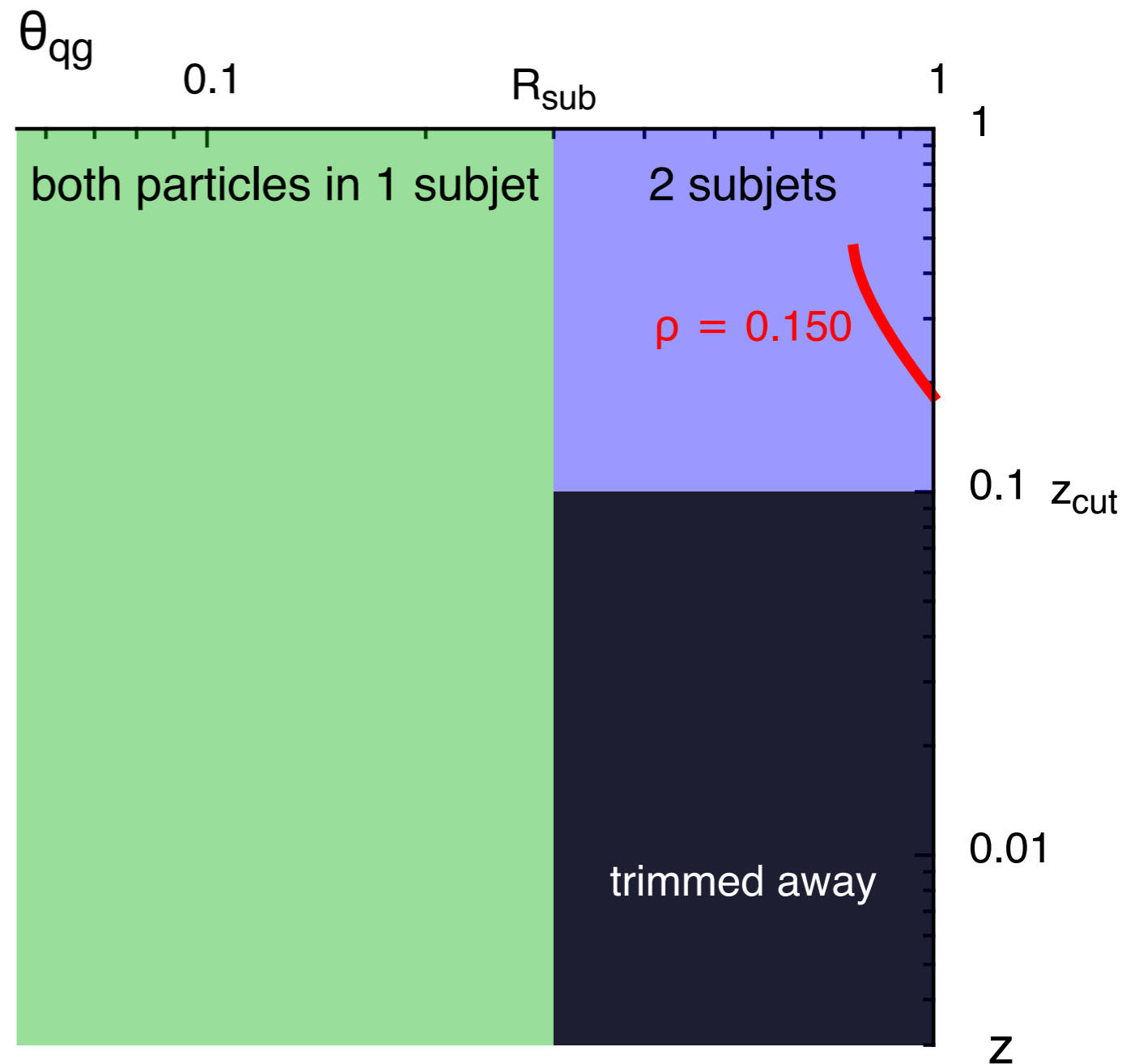
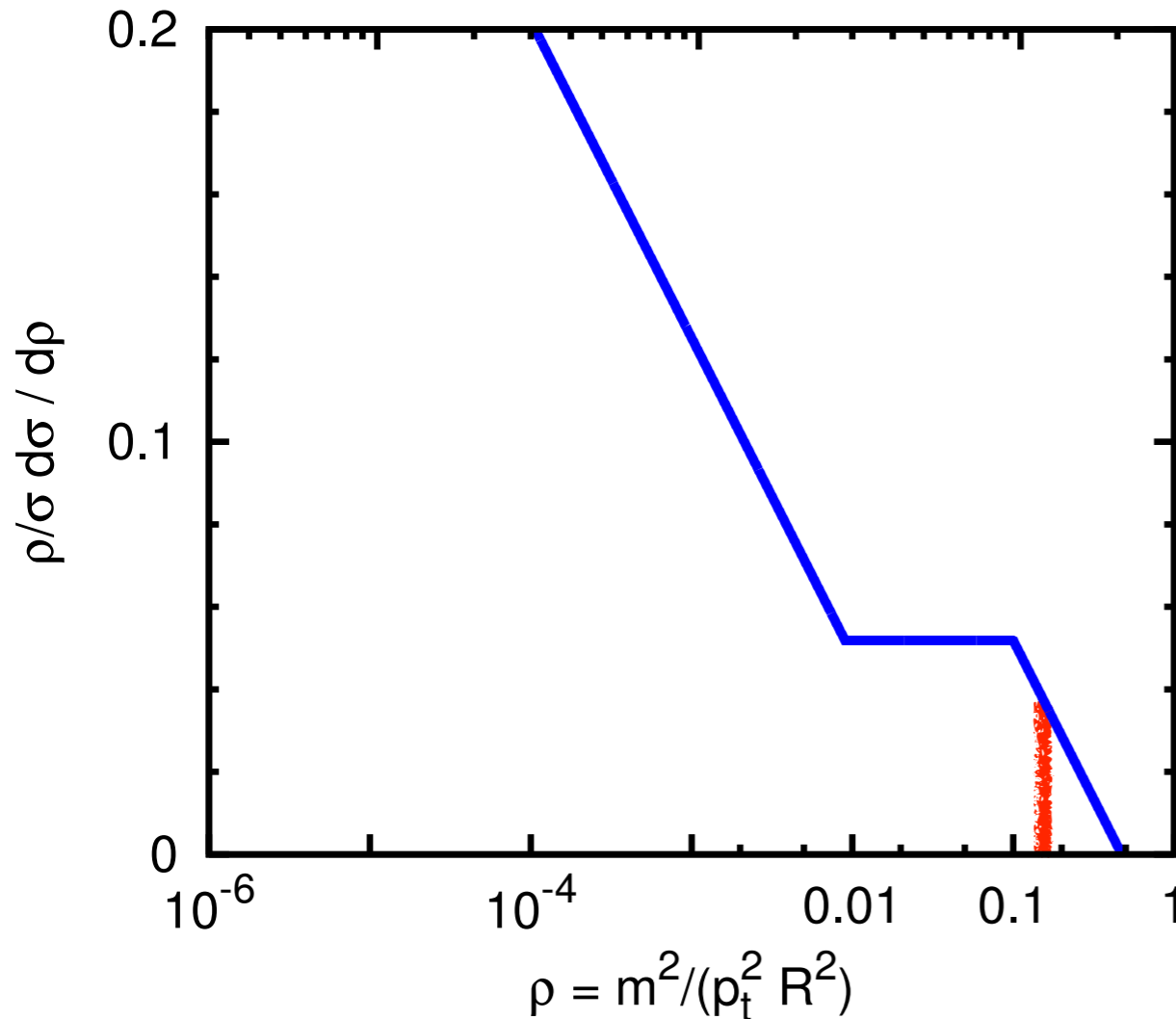
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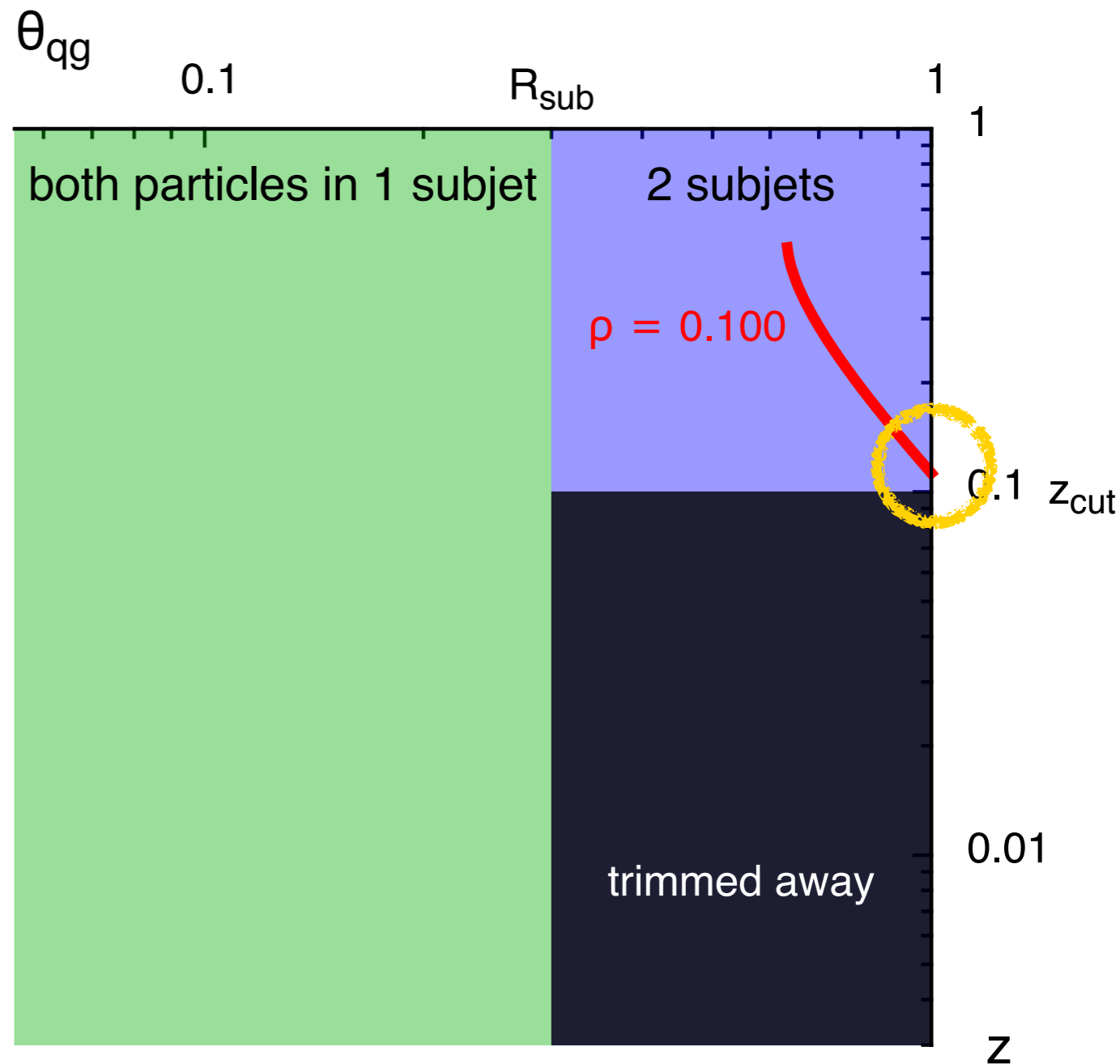
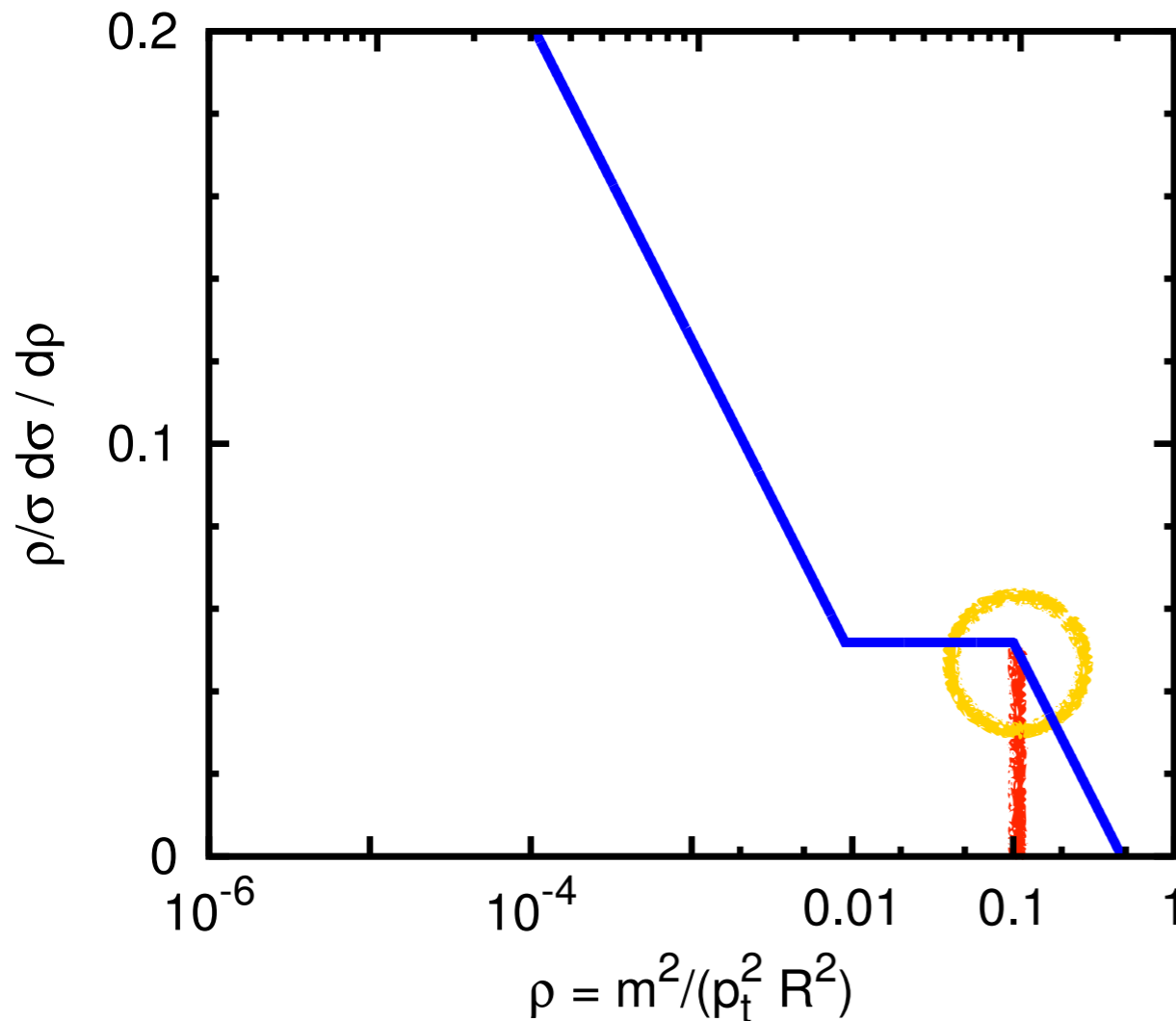
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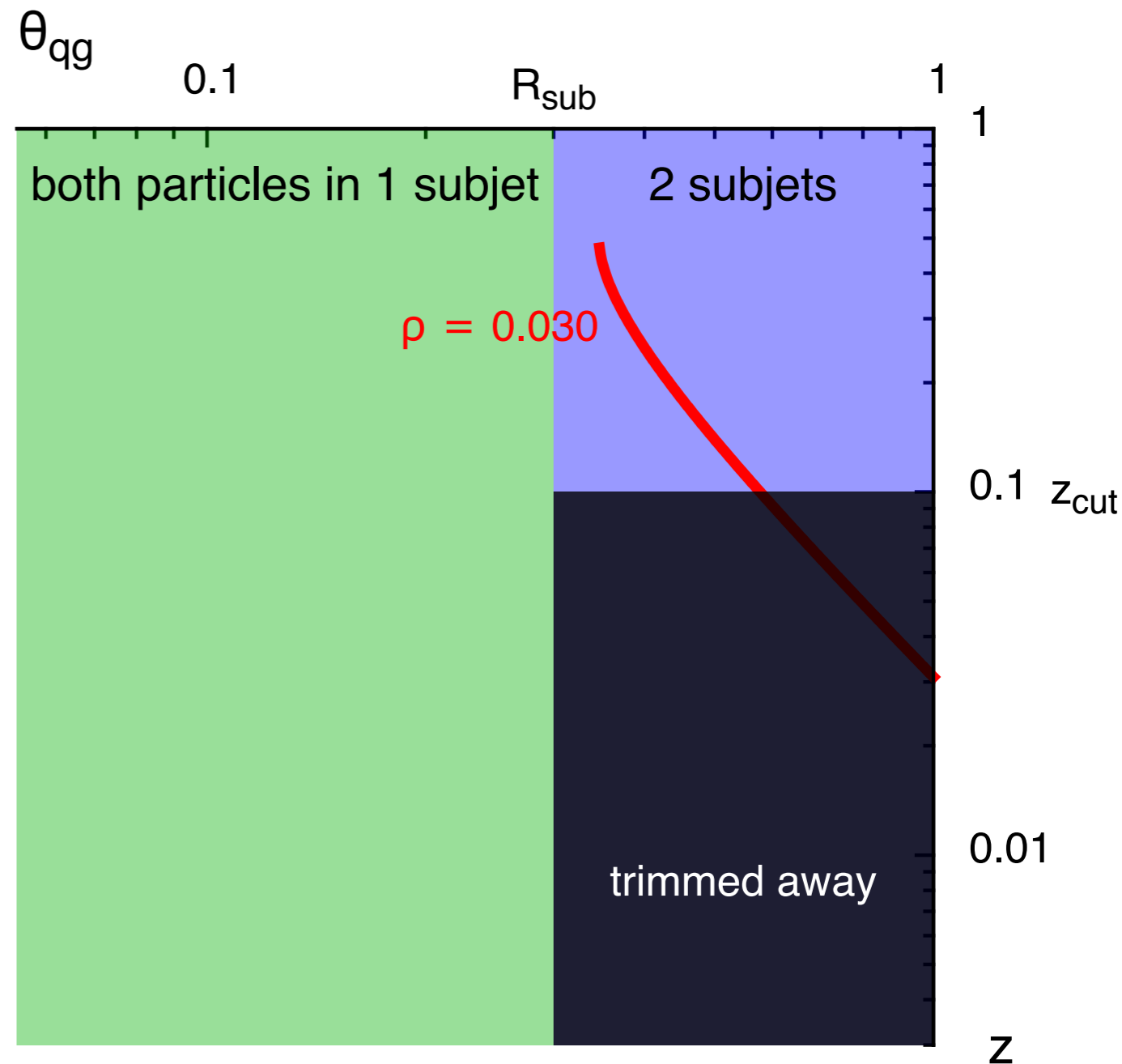
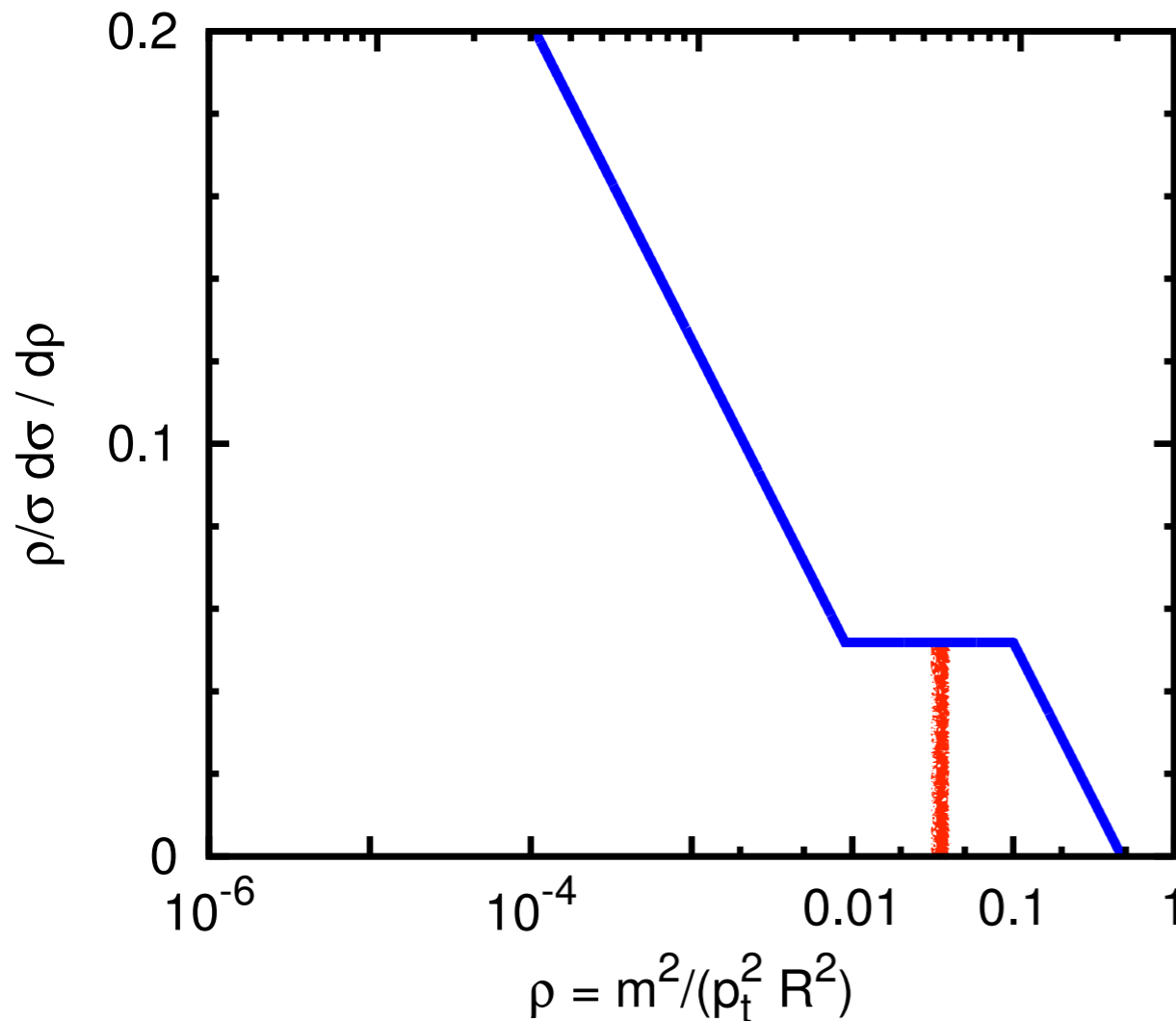
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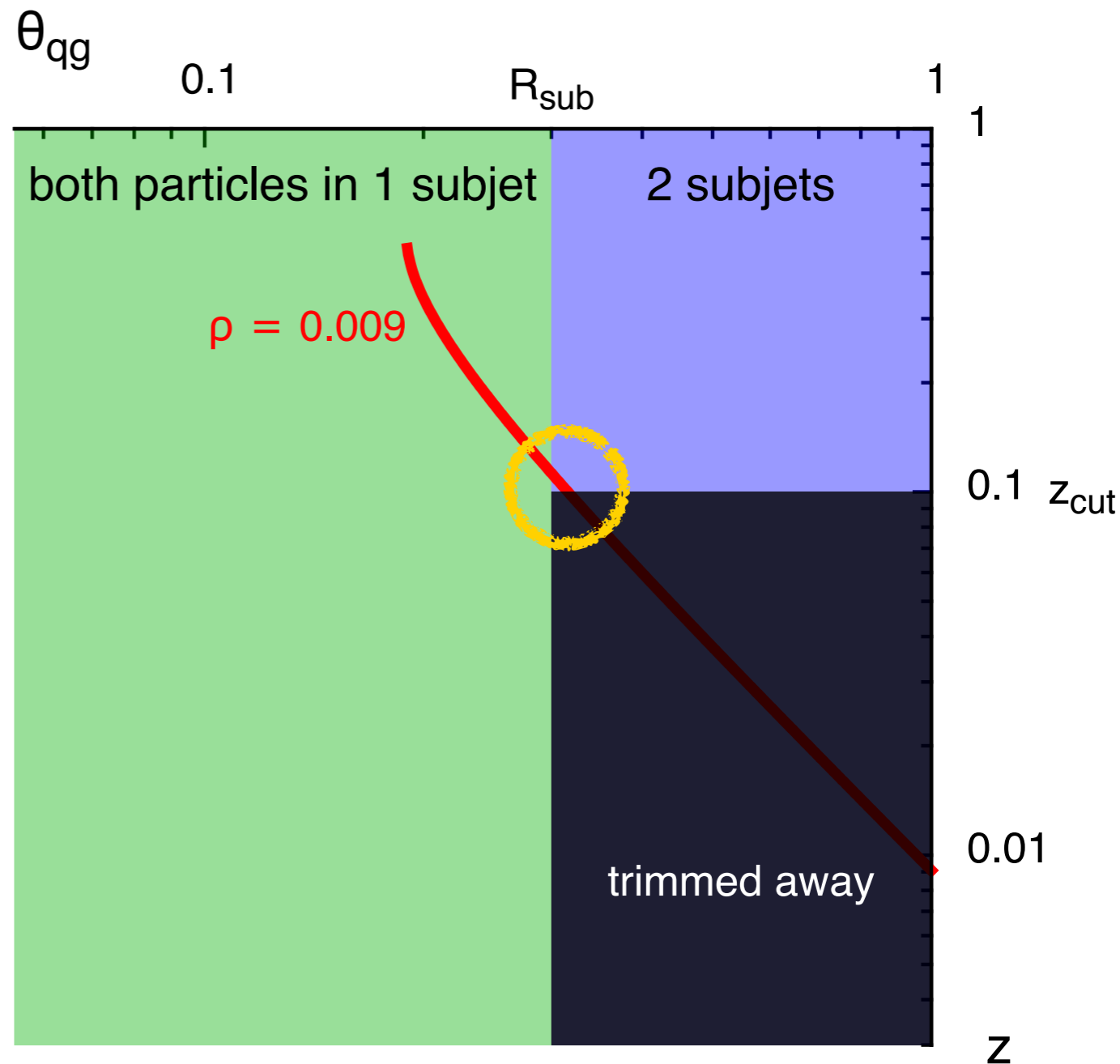
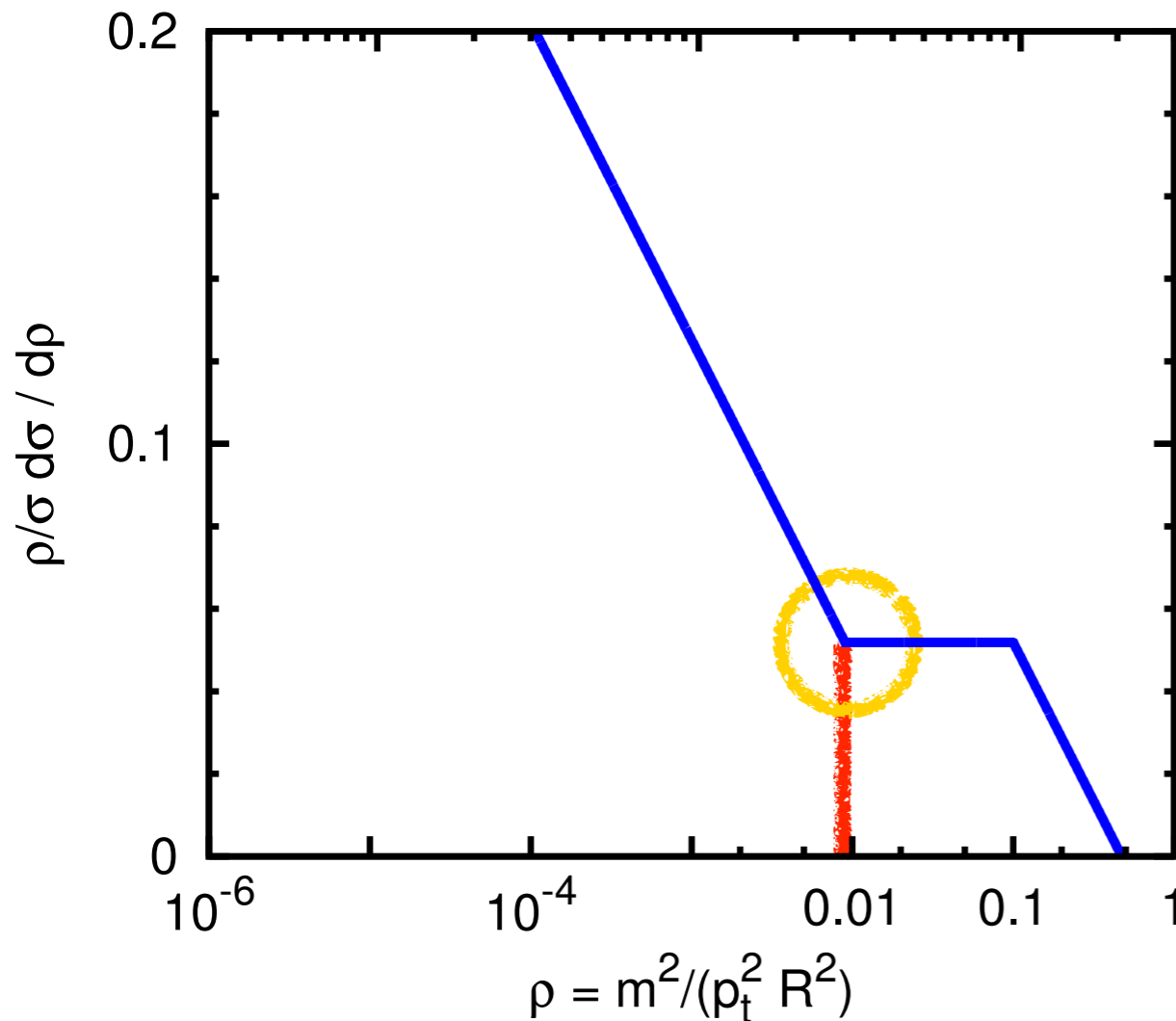
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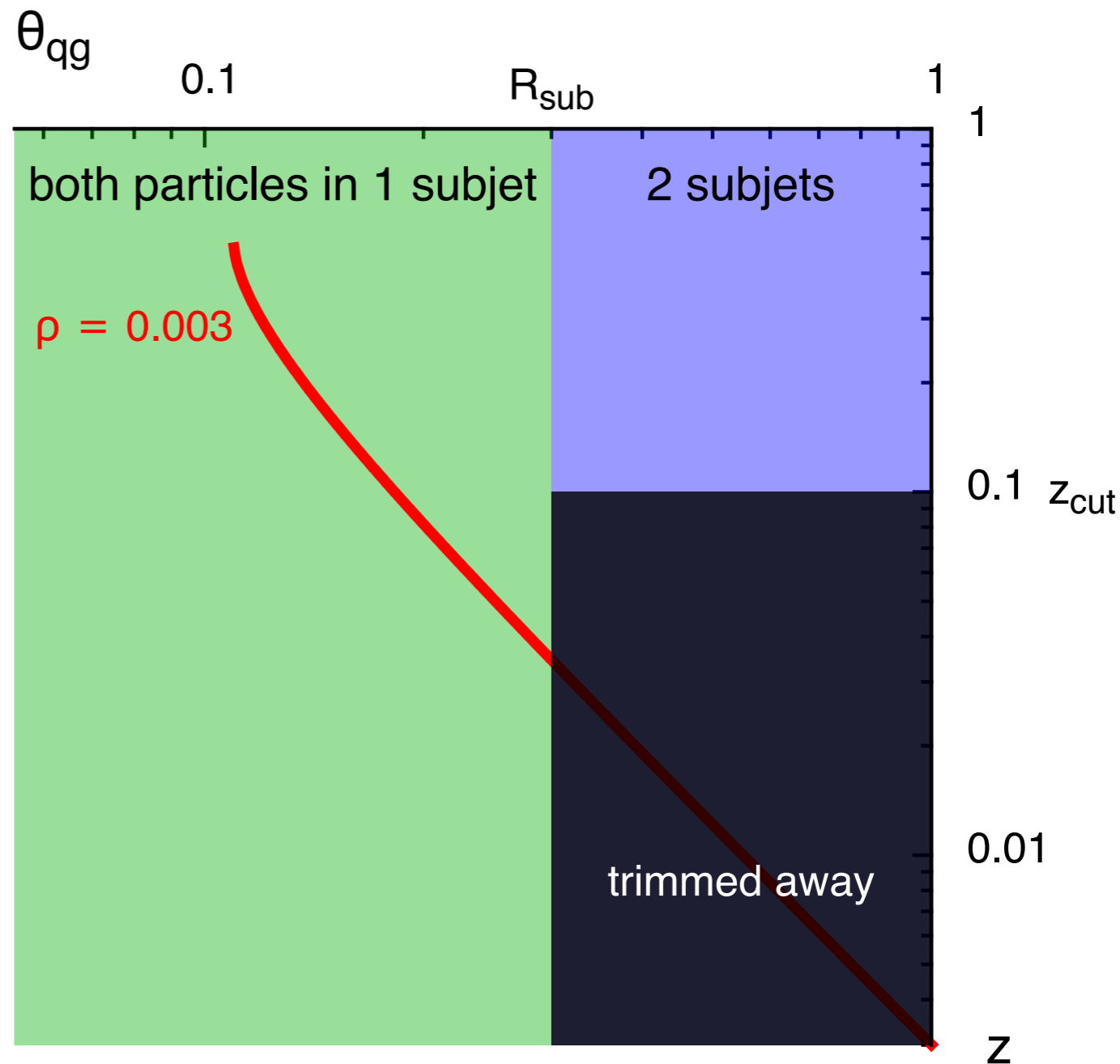
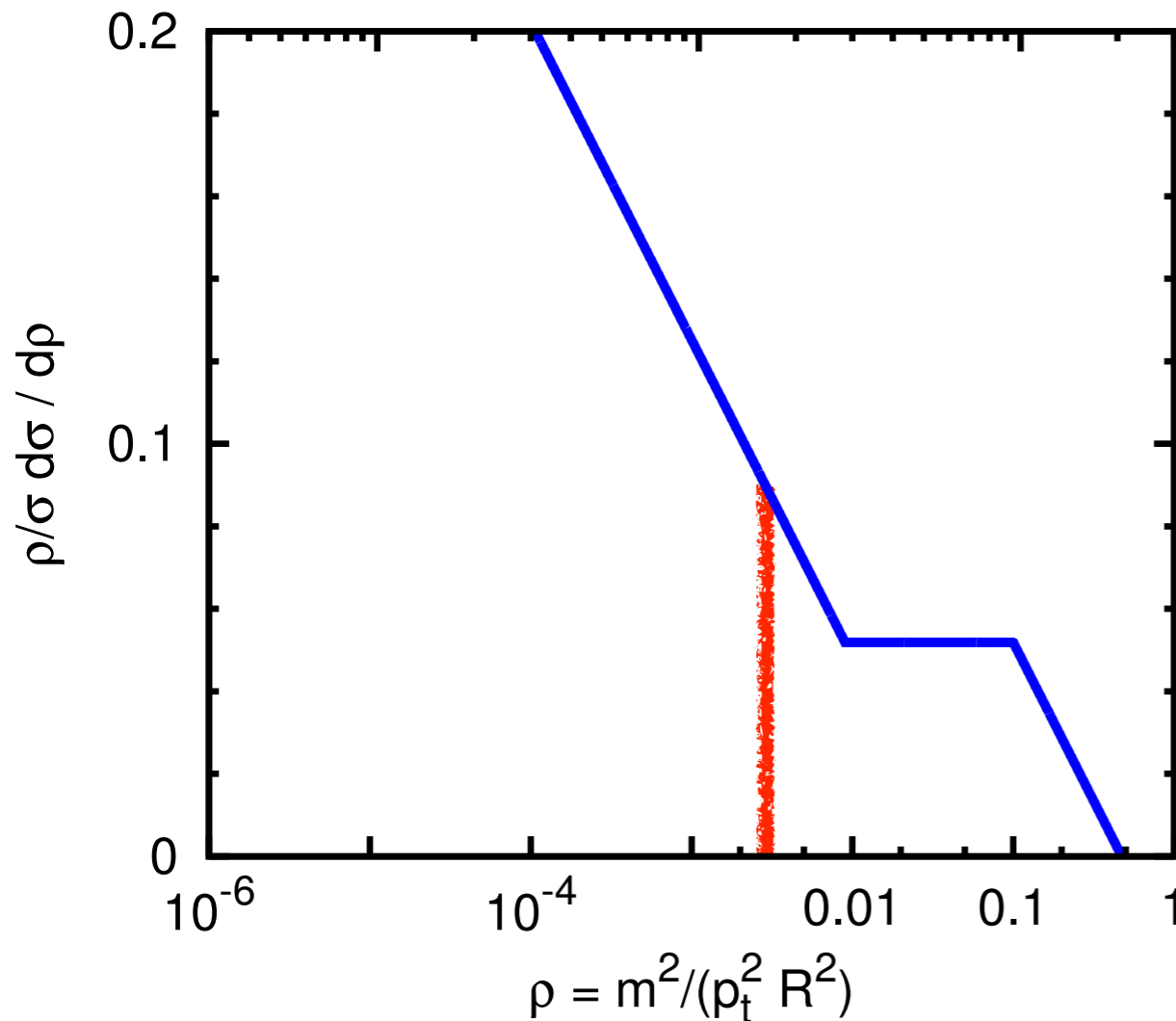
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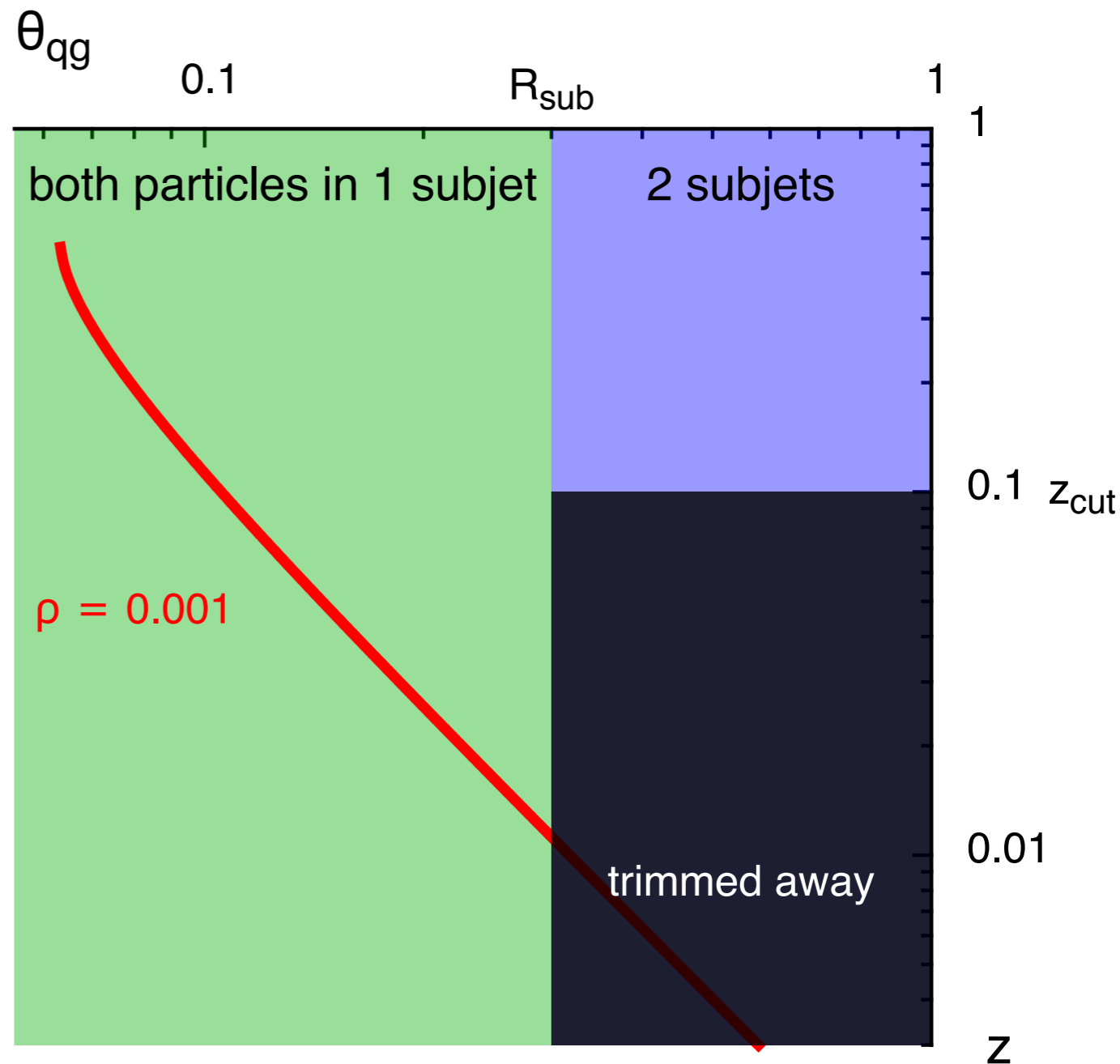
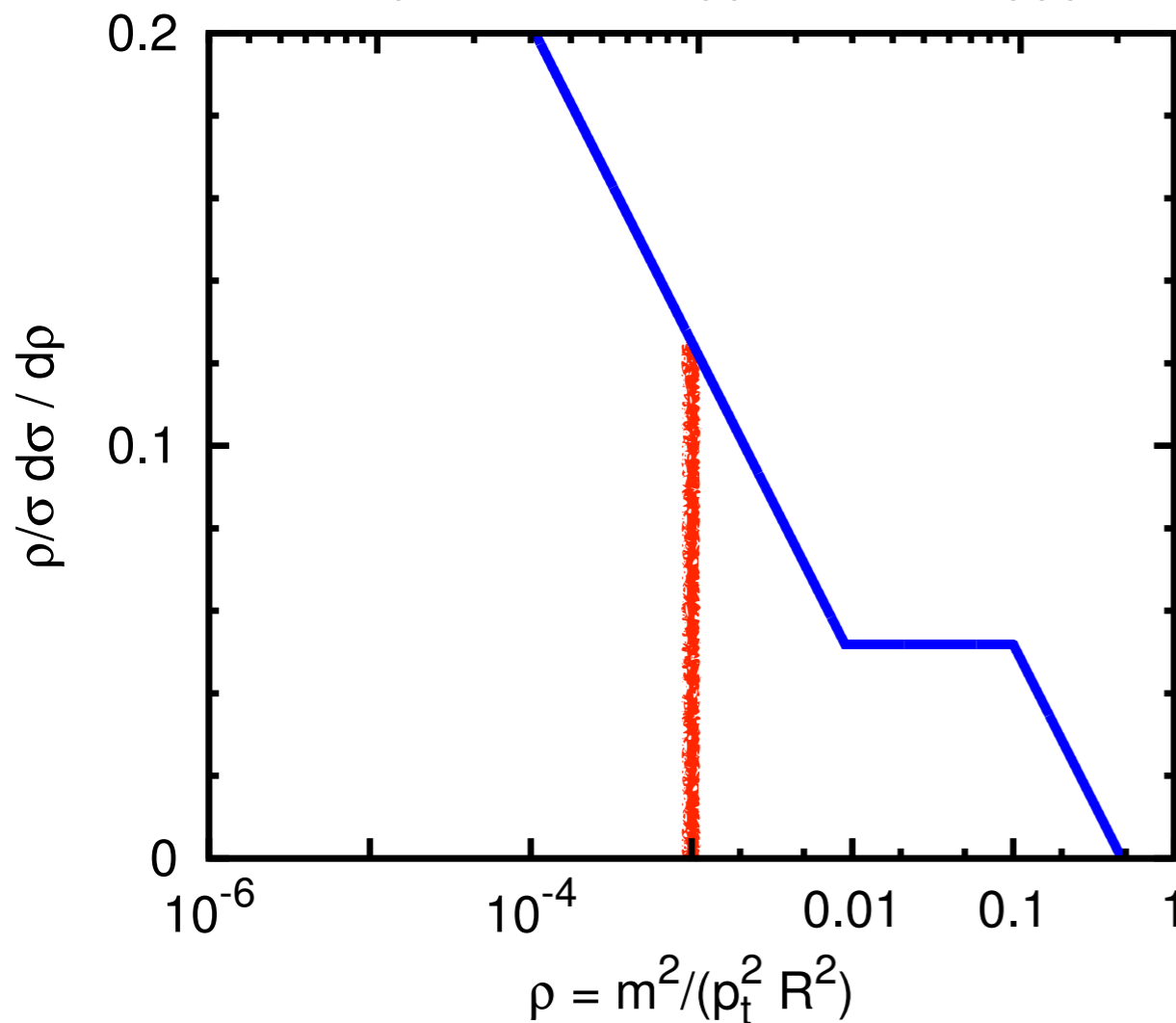
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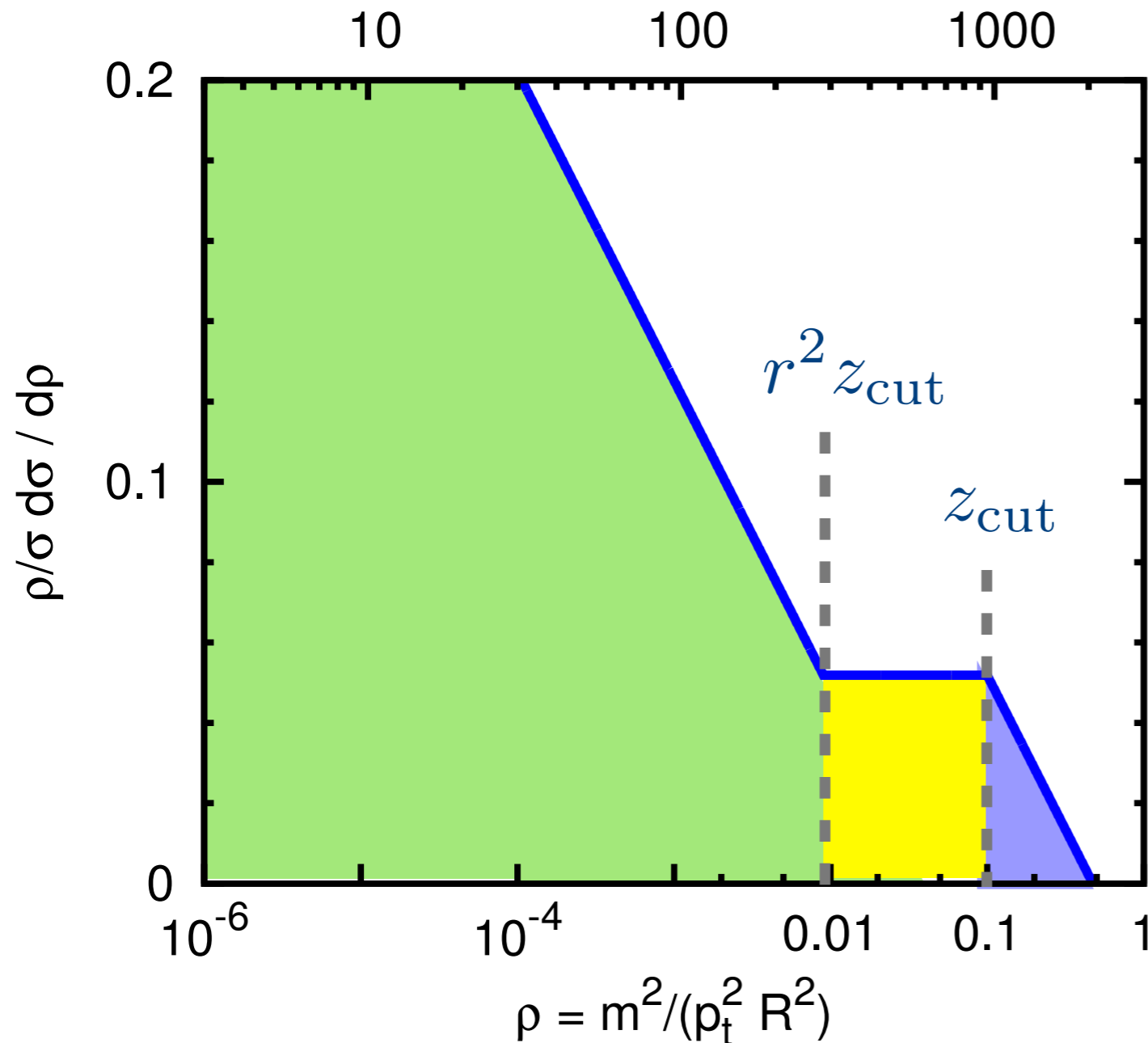
10 100 1000



Trimming at LO in α_s

trimmed quark jets: LO

m [GeV], for $p_t = 3$ TeV, $R=1$



$$\frac{\rho}{\sigma} \frac{d\sigma^{(\text{trim,LO})}}{d\rho} =$$

$$\frac{\alpha_s C_F}{\pi} \left(\ln \frac{r^2}{\rho} - \frac{3}{4} \right)$$

$$\frac{\alpha_s C_F}{\pi} \left(\ln \frac{1}{z_{\text{cut}}} - \frac{3}{4} \right)$$

$$\frac{\alpha_s C_F}{\pi} \left(\ln \frac{1}{\rho} - \frac{3}{4} \right)$$

$$r = \frac{R_{\text{sub}}}{R}$$

continue with all-order
resummation of terms

$$\alpha_s^n \ln^m \rho$$

Inputs

QCD pattern
of multiple
soft/collinear
emission

Analysis of
taggers'
behaviour for
1, 2, 3, ... n,
emissions

Establish which
simplifying
approximations
to use for
tagger & matrix
elements

Output

approx.
formula for
tagger's mass
distribution for
 $\rho \ll 1$

$$\frac{\rho}{\sigma} \frac{d\sigma}{d\rho} =$$

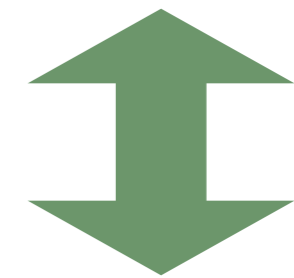
$$\sum_{n=1}^{\infty} c_{nm} \alpha_s^n \ln^m \rho$$

keeping only terms with
largest powers of $\ln \rho$,
e.g. $m = 2n, 2n-1$

Trimming

$$\rho^{\text{trim}}(k_1, k_2, \dots, k_n) \simeq \sum_i^n \rho^{\text{trim}}(k_i) \\ \sim \max_i \{ \rho^{\text{trim}}(k_i) \}$$

**Trimmed jet reduces
(\sim) to sum of
trimmed emissions**



Matrix element

$$\sum_n \frac{1}{n!} \prod_i^n \frac{d\theta_i^2}{\theta_i^2} \frac{dz_i}{z_i} \frac{\alpha_s(\theta_i z_i p_t^{\text{jet}}) C_F}{\pi}$$

**can use QED-like
independent
emissions, as if
gluons don't split**

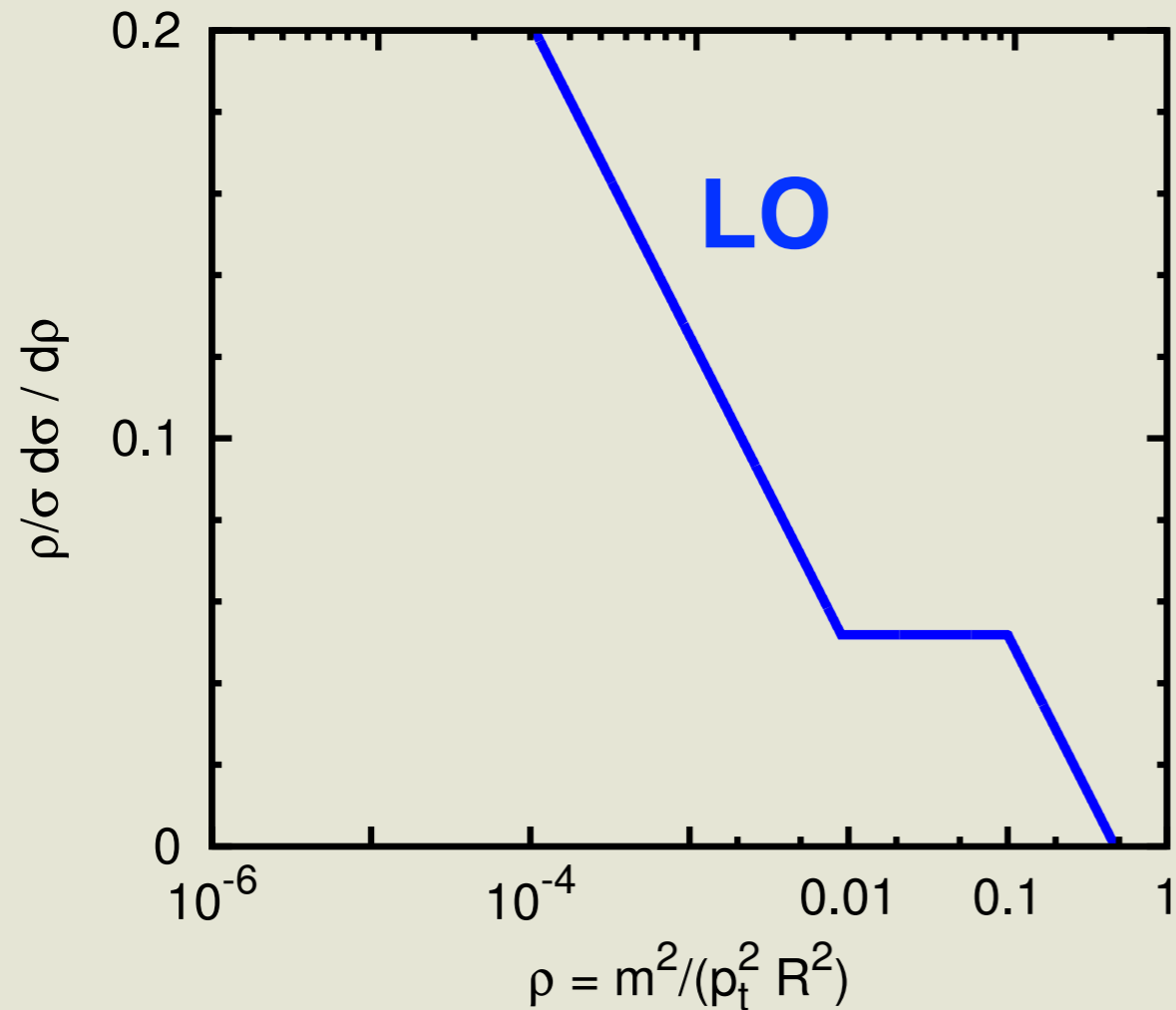
+ virtual corrections, essentially from unitarity

$$\frac{d\sigma^{\text{trim,resum}}}{d\rho} = \frac{d\sigma^{\text{trim,LO}}}{d\rho}$$

trimmed quark jets: LO

m [GeV], for $p_t = 3$ TeV, $R=1$

10 100 1000



Trimming at all orders

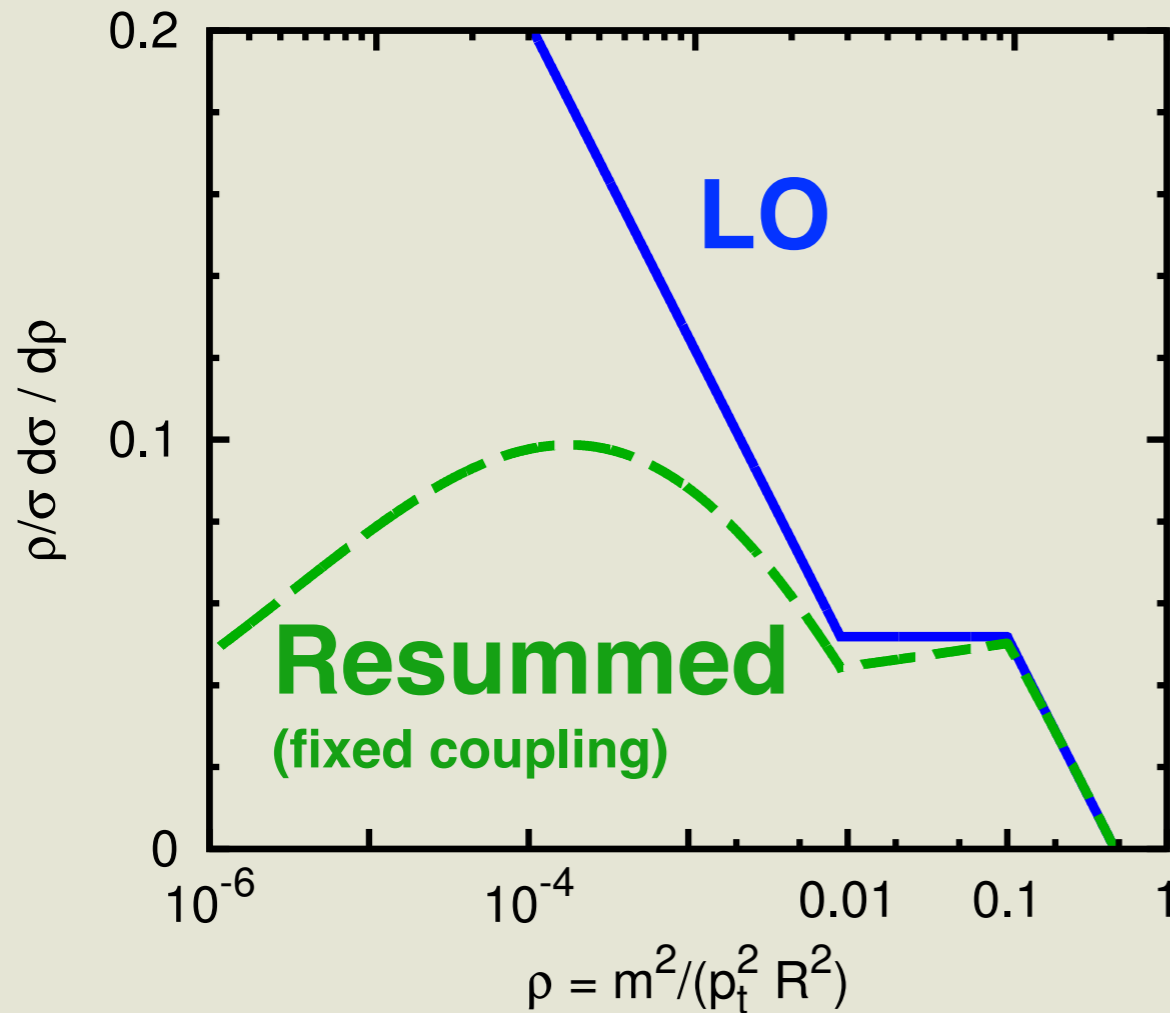
$$\frac{d\sigma^{\text{trim,resum}}}{d\rho} = \frac{d\sigma^{\text{trim,LO}}}{d\rho}$$

$$\exp \left[- \int_{\rho} d\rho' \frac{1}{\sigma} \frac{d\sigma^{\text{trim,LO}}}{d\rho'} \right]$$

trimmed quark jets

m [GeV], for $p_t = 3$ TeV, $R=1$

10 100 1000

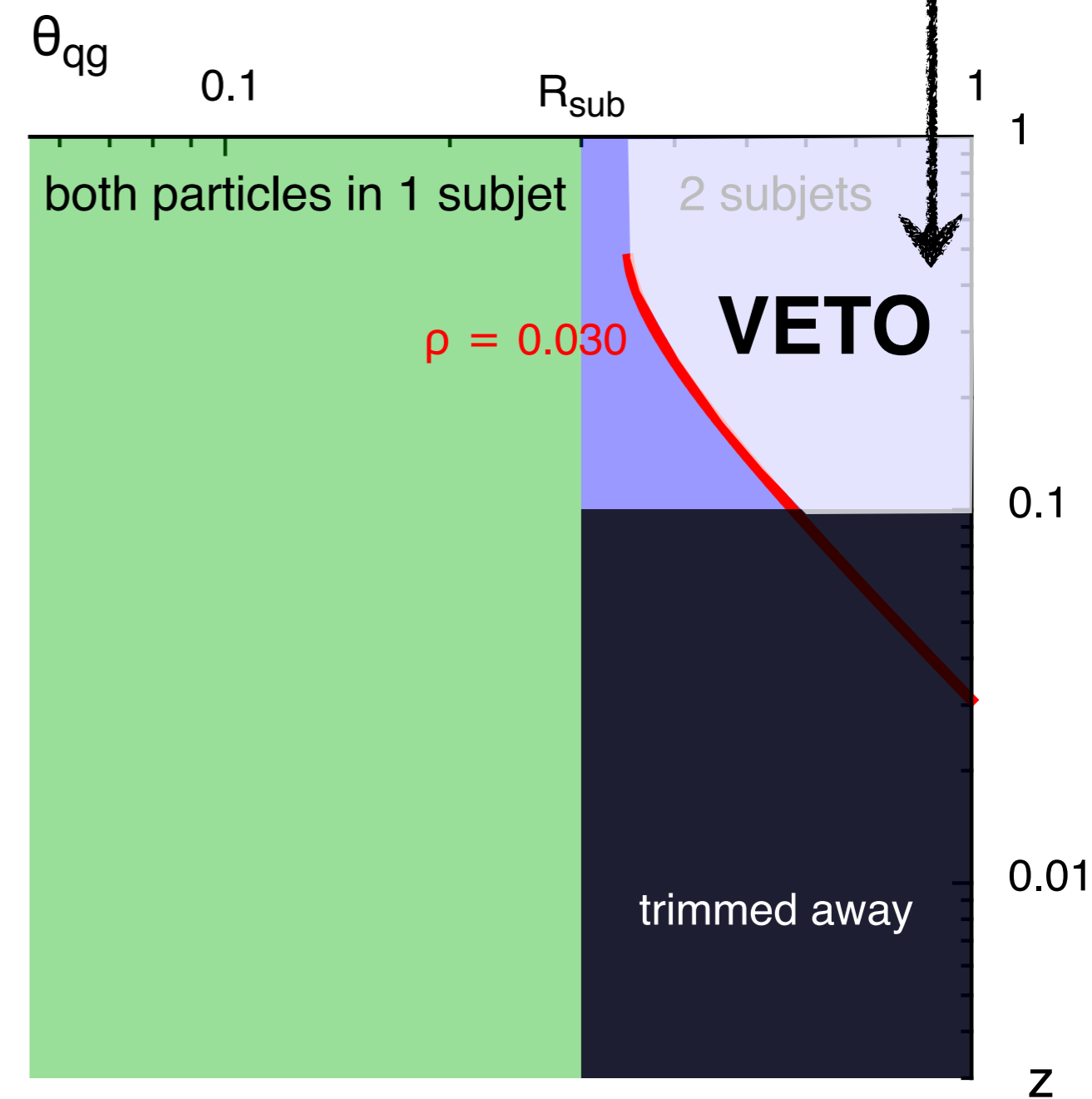
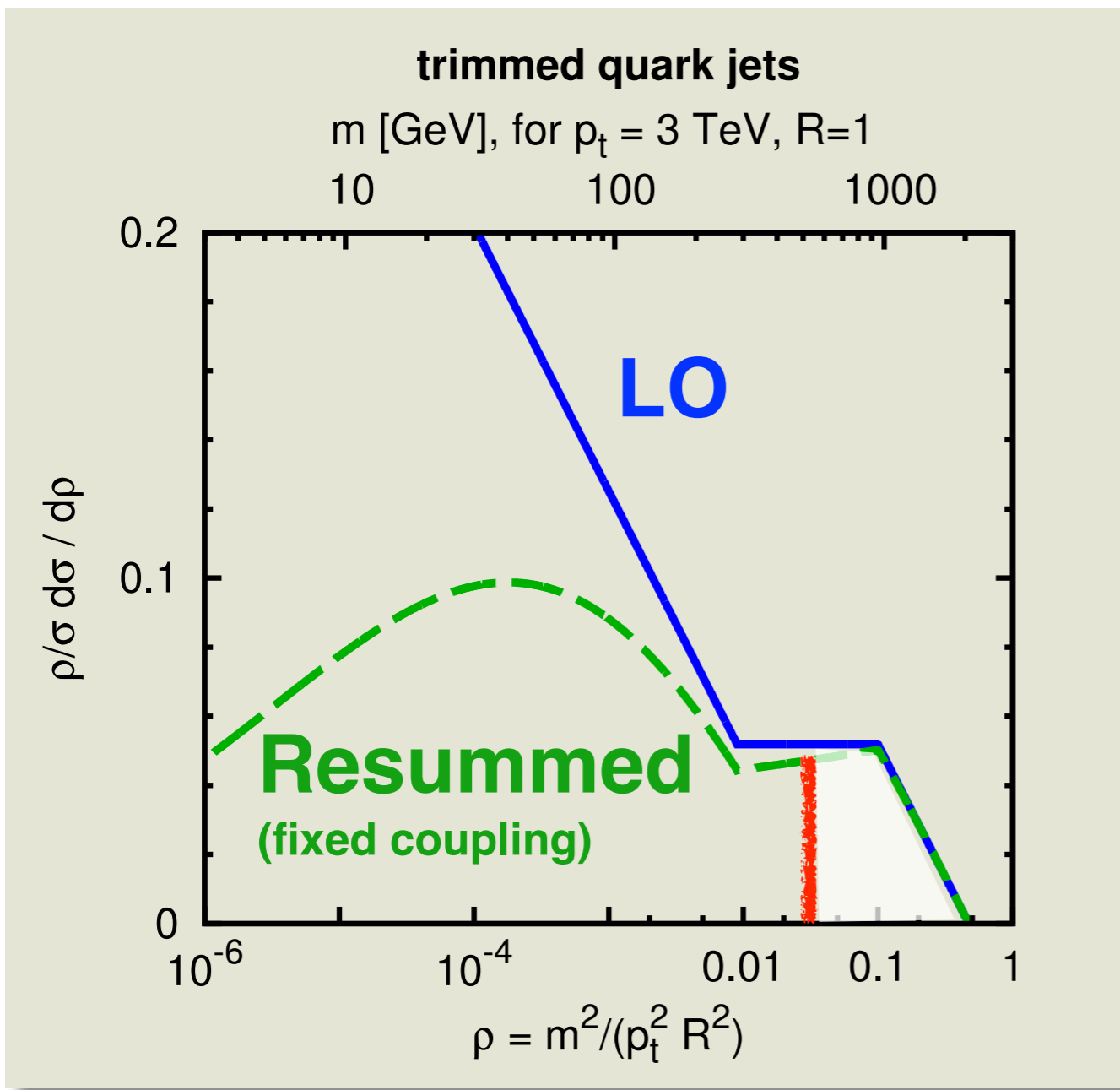


Trimming at all orders

$$\frac{d\sigma^{\text{trim, resum}}}{d\rho} = \frac{d\sigma^{\text{trim, LO}}}{d\rho}$$

$$\exp \left[- \int_{\rho} d\rho' \frac{1}{\sigma} \frac{d\sigma^{\text{trim, LO}}}{d\rho'} \right]$$

Sudakov

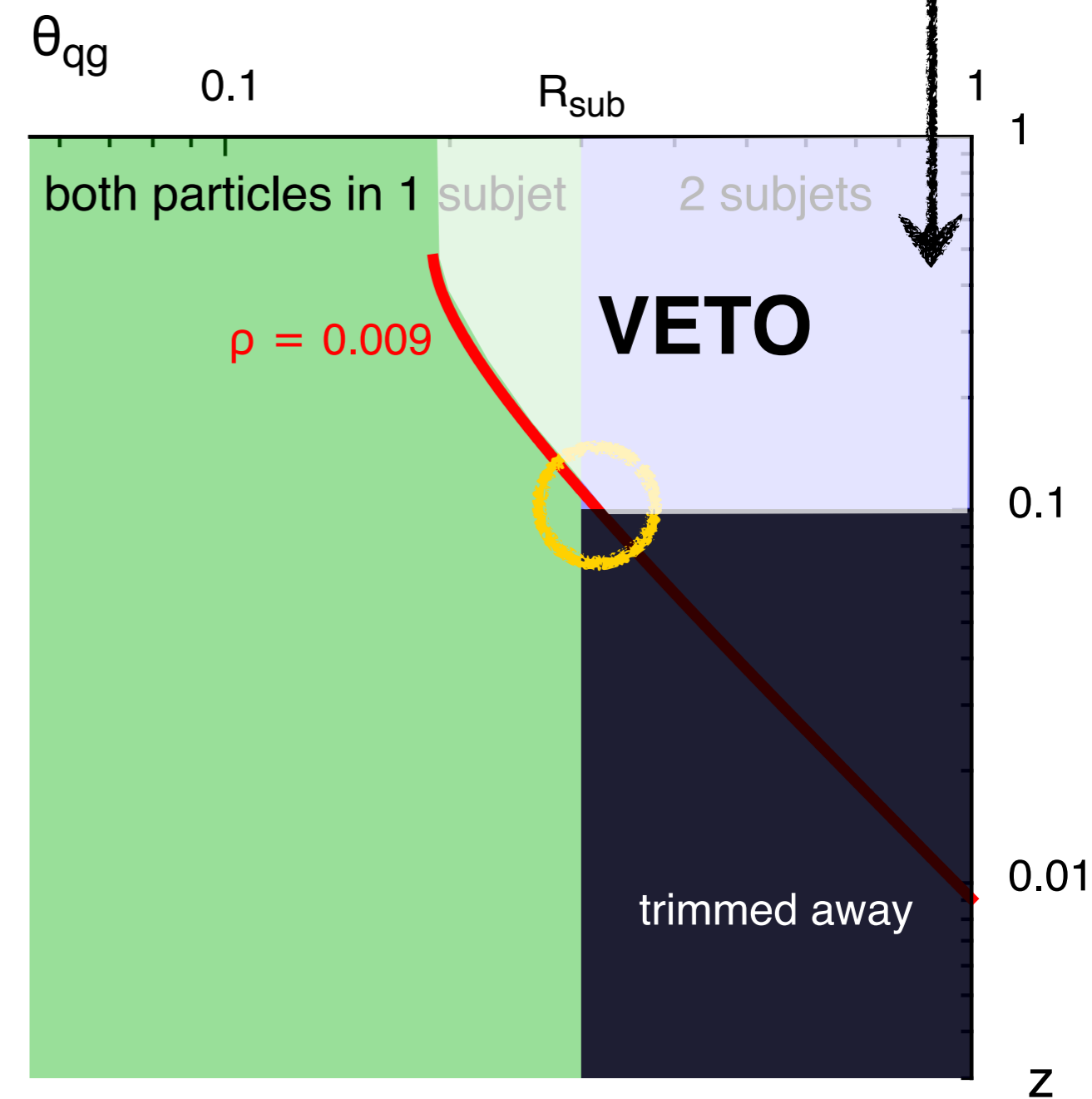
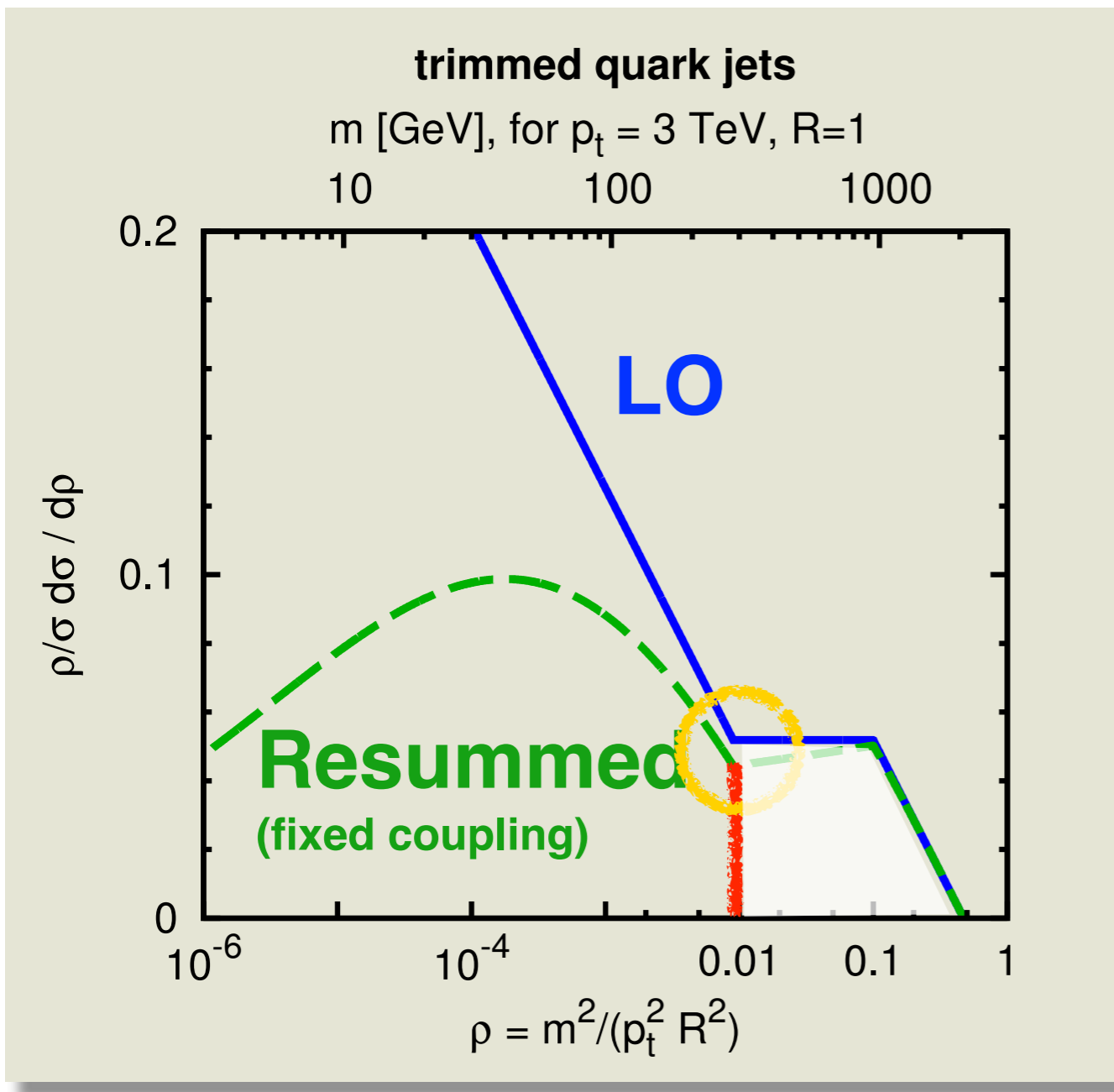


Trimming at all orders

$$\frac{d\sigma^{\text{trim, resum}}}{d\rho} = \frac{d\sigma^{\text{trim, LO}}}{d\rho}$$

$$\exp \left[- \int_{\rho} d\rho' \frac{1}{\sigma} \frac{d\sigma^{\text{trim, LO}}}{d\rho'} \right]$$

Sudakov

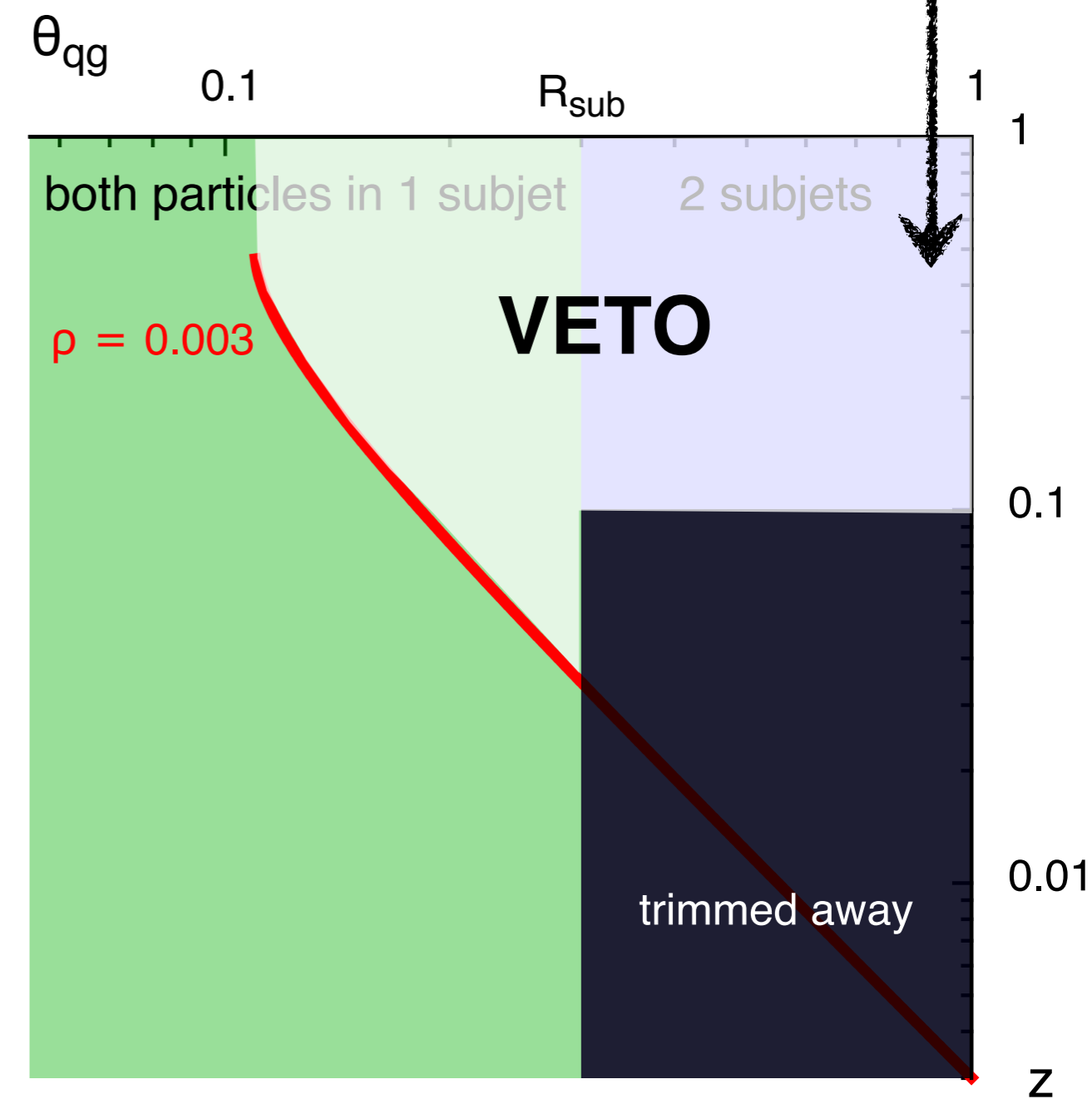
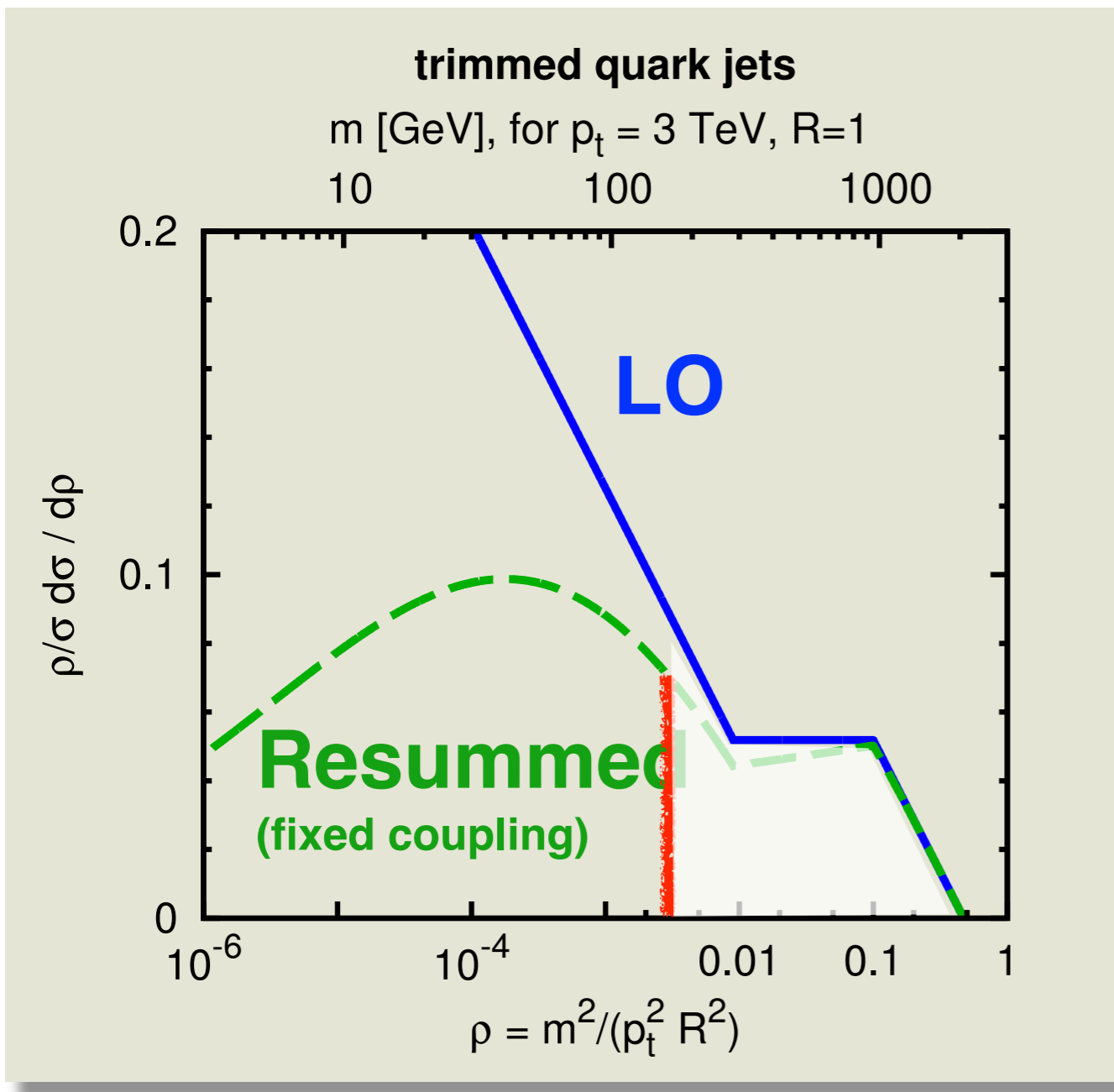


Trimming at all orders

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Sudakov

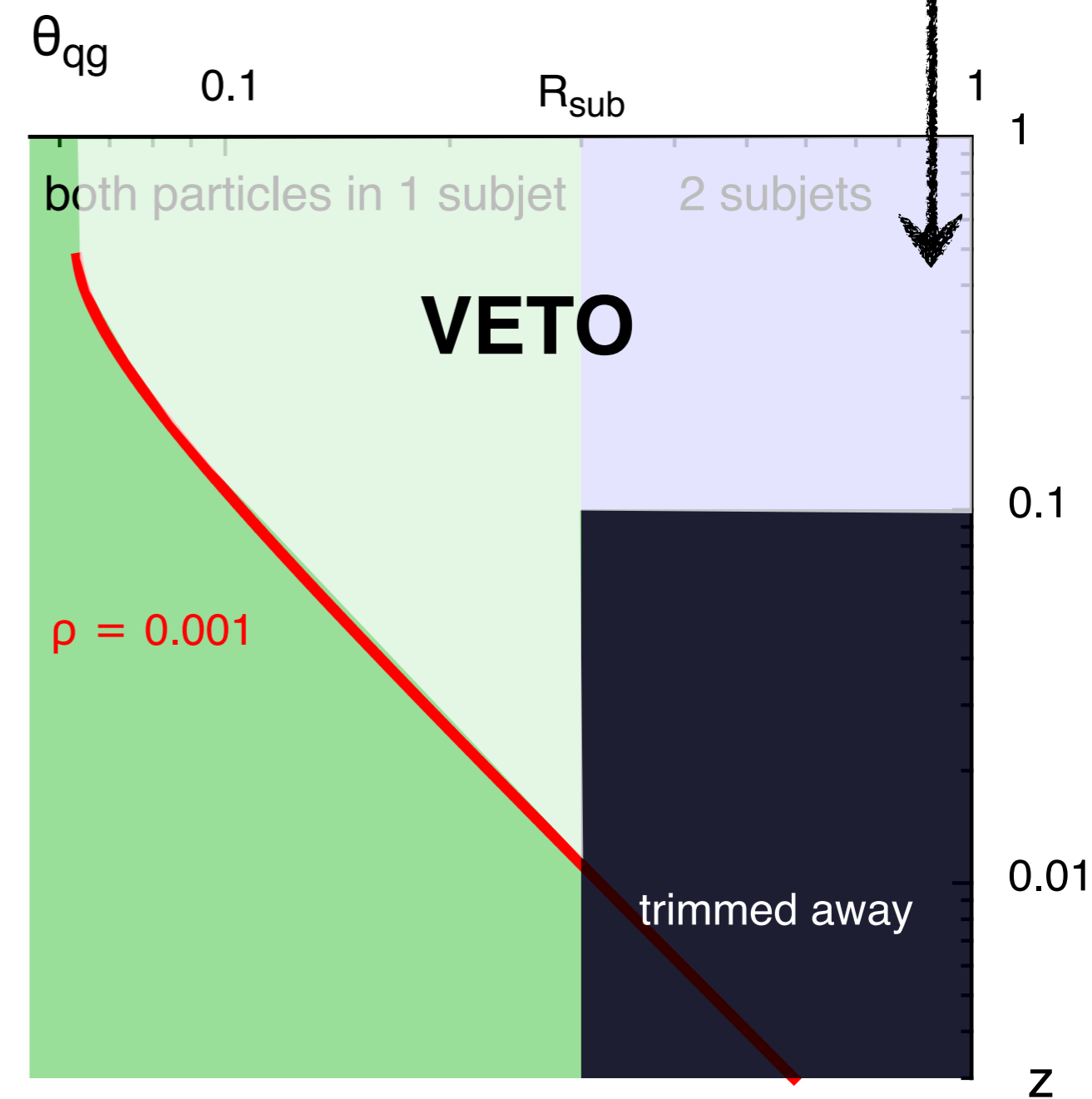
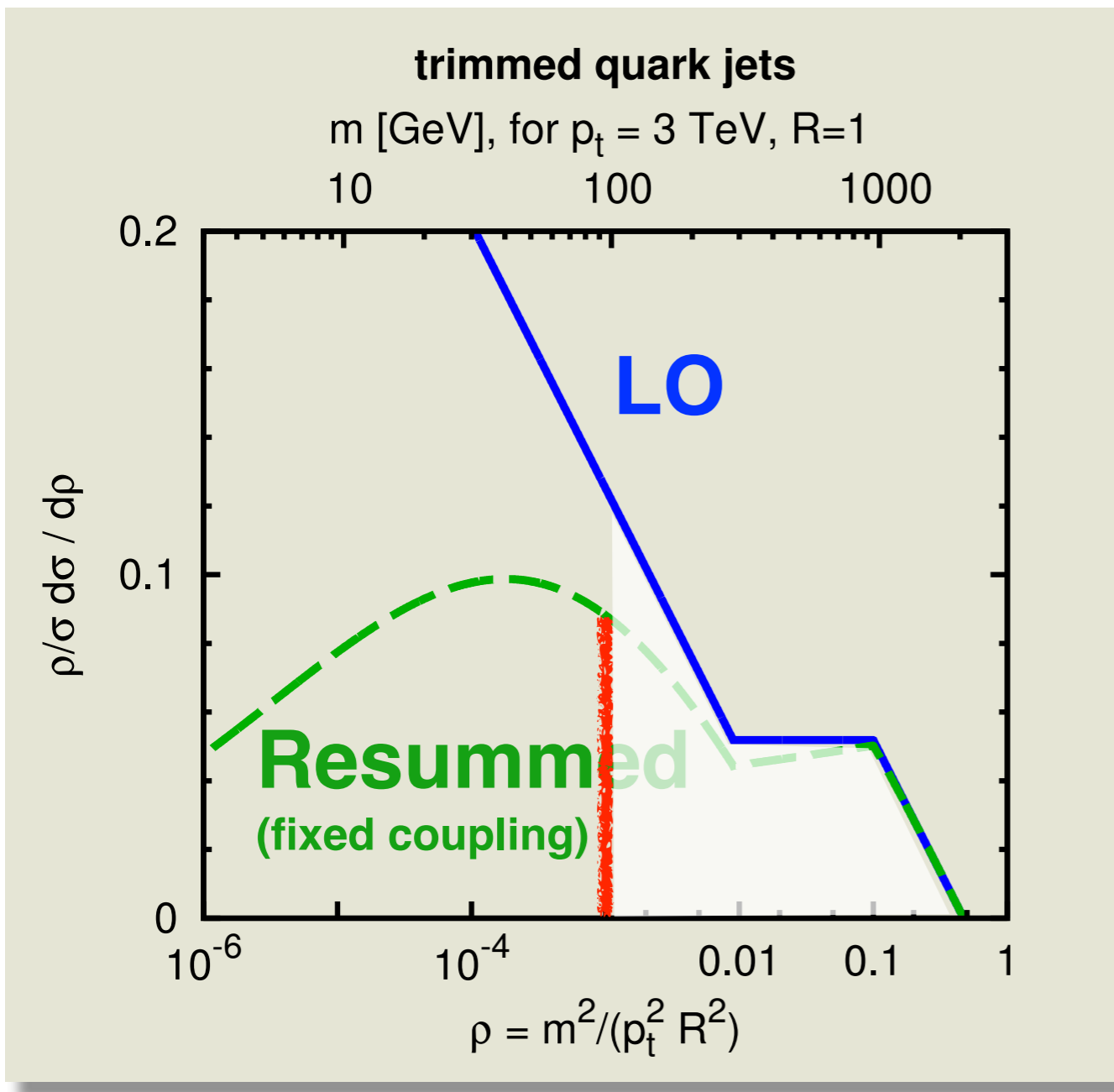


Trimming at all orders

$$\frac{d\sigma^{\text{trim, resum}}}{d\rho} = \frac{d\sigma^{\text{trim, LO}}}{d\rho}$$

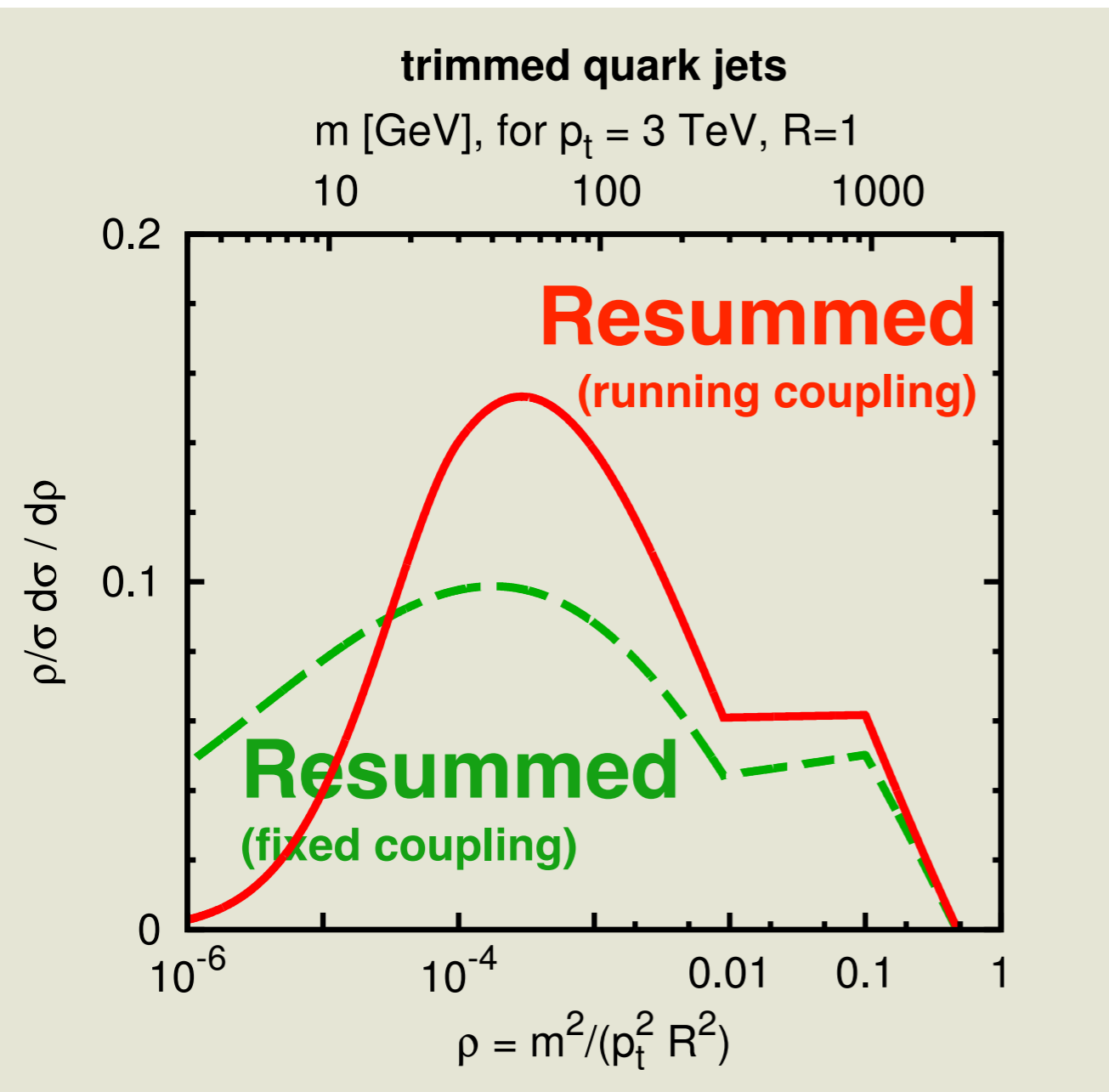
$$\exp \left[- \int_{\rho} d\rho' \frac{1}{\sigma} \frac{d\sigma^{\text{trim, LO}}}{d\rho'} \right]$$

Sudakov



Trimming at all orders

$$\frac{d\sigma^{\text{trim, resum}}}{d\rho} = \frac{d\sigma^{\text{trim, LO}}}{d\rho} \exp \left[- \int_{\rho} d\rho' \frac{1}{\sigma} \frac{d\sigma^{\text{trim, LO}}}{d\rho'} \right]$$



Full resummation also needs treatment of running coupling

What logs, what accuracy?

Express accuracy for
“cumulative distⁿ” $\Sigma(\rho)$:

$$\Sigma(\rho) = \int_0^\rho d\rho' \frac{1}{\sigma} \frac{d\sigma}{d\rho'}$$

Use shorthand $L = \log 1/\rho$

Trimming's **leading logs** (LL, in Σ) are:

$$\alpha_s L^2, \alpha_s^2 L^4, \dots \text{ I.e. } \alpha_s^n L^{2n}$$

Just like the
jet mass

We also have **next-to-leading logs** (NLL): $\alpha_s^n L^{2n-1}$

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Just like the
jet mass

We also have **next-to-leading logs** (NLL): $\alpha_s^n L^{2n-1}$

Could we do better? Yes: NLL in $\ln \Sigma$:

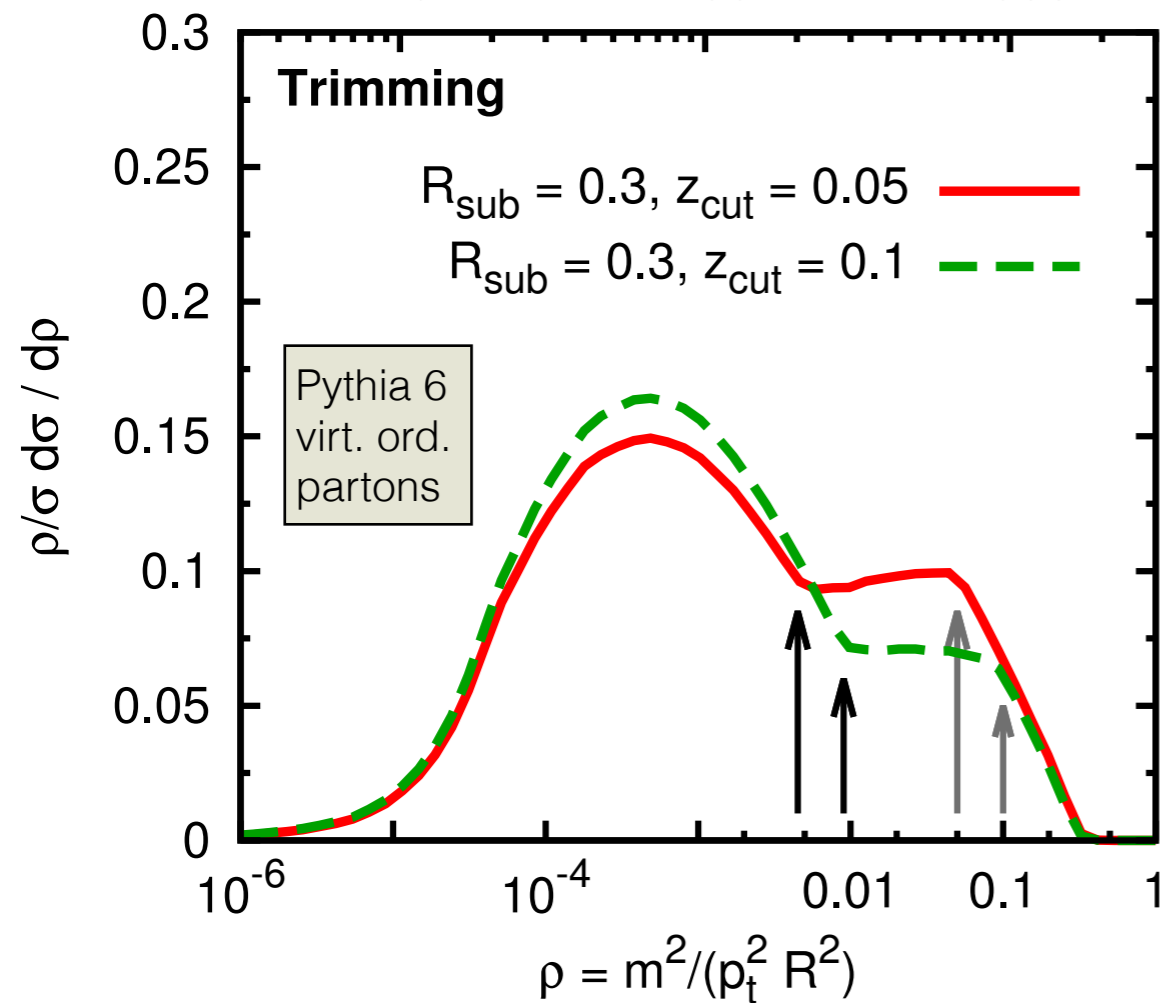
$$\ln \Sigma: \alpha_s^n L^{n+1} \text{ and } \alpha_s^n L^n$$

Trimmed mass is like plain jet mass (with $R \rightarrow R_{\text{sub}}$), and this accuracy involves **non-global logs, clustering logs**

Monte Carlo

m [GeV], for $p_t = 3$ TeV, $R = 1$

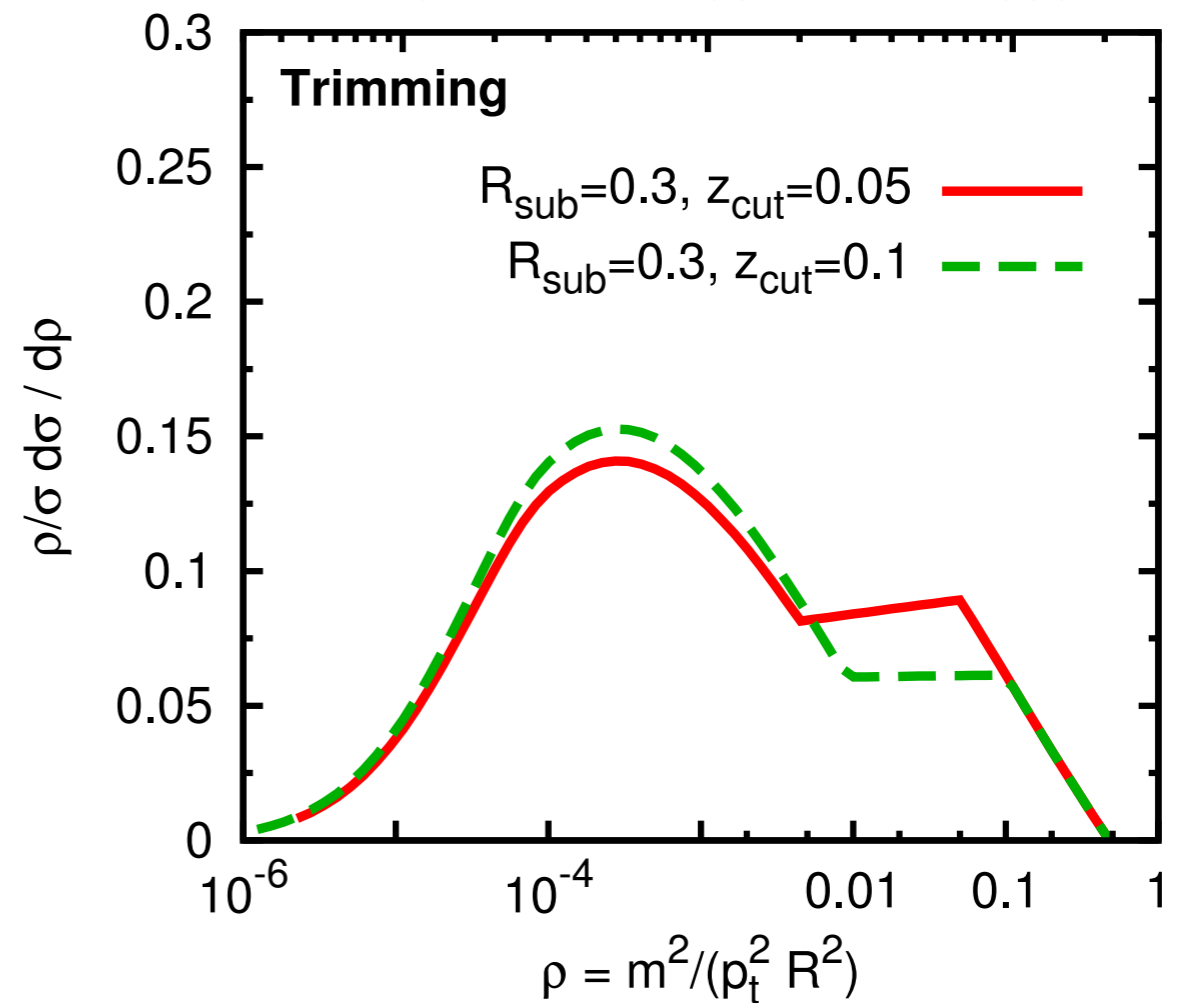
10 100 1000



Analytic

m [GeV], for $p_t = 3$ TeV, $R = 1$

10 100 1000

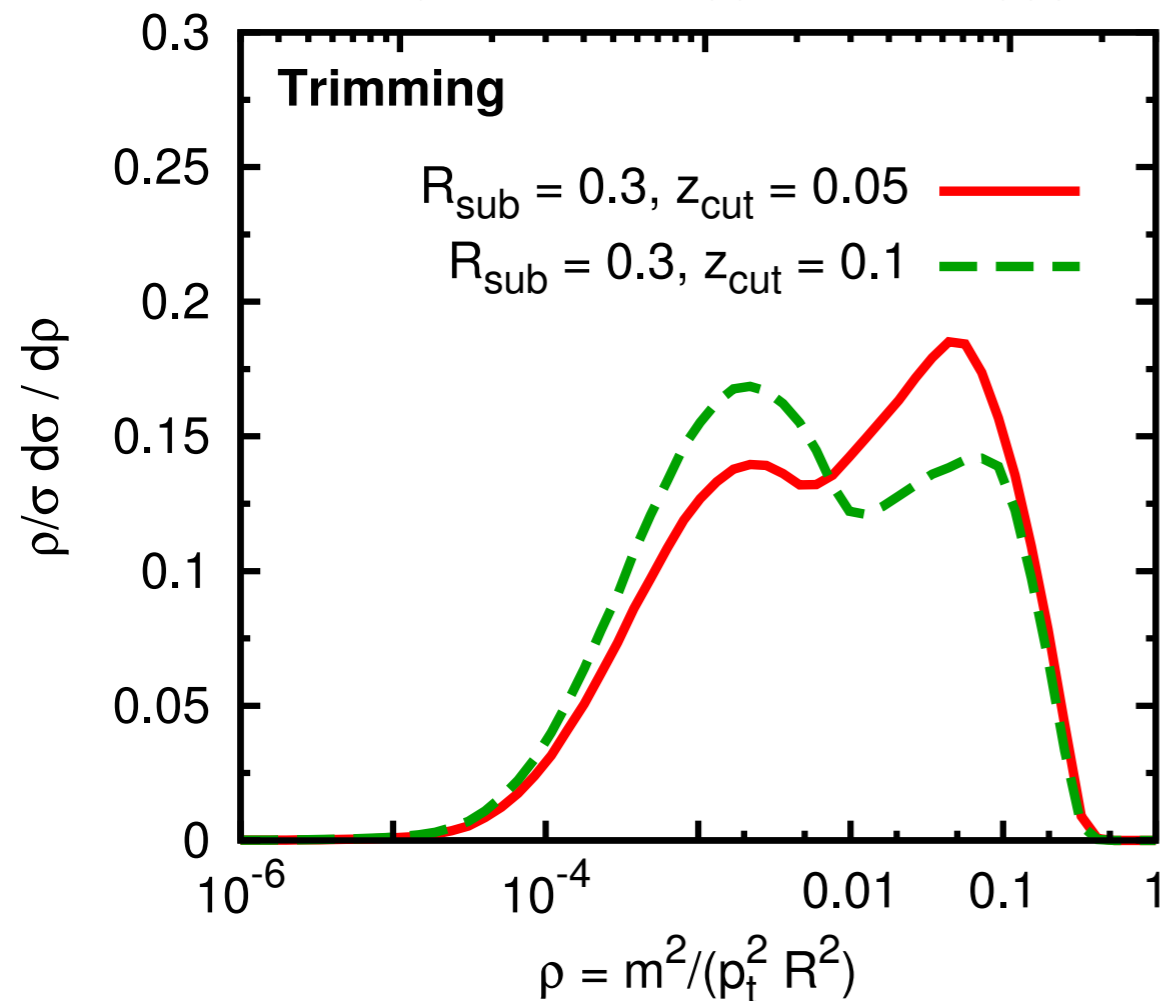


Non-trivial agreement!
(also for dependence on parameters)

Monte Carlo

m [GeV], for $p_t = 3$ TeV, $R = 1$

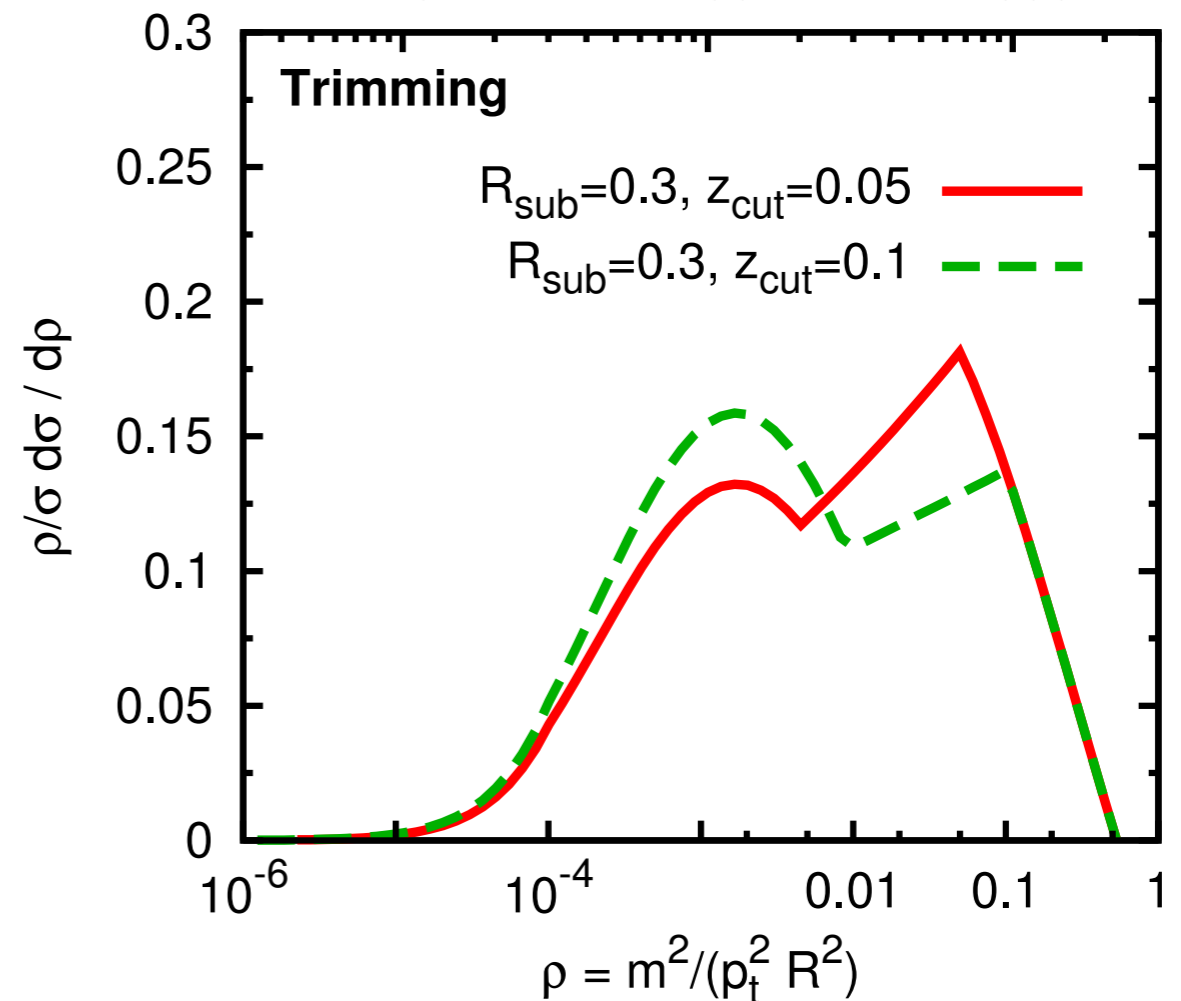
10 100 1000



Analytic

m [GeV], for $p_t = 3$ TeV, $R = 1$

10 100 1000



Non-trivial agreement!
(also for dependence on parameters)

For a jet clustered with C/A:

1. undo last clustering step to break jet (mass m) into two subjets with $m_1 > m_2$
2. If significant mass-drop ($m_1 < \mu m$) and subjet energy-sharing not too asymmetric

$$\min(p_{t1}^2, p_{t2}^2) \Delta R_{12}^2 < y_{\text{cut}} m^2$$

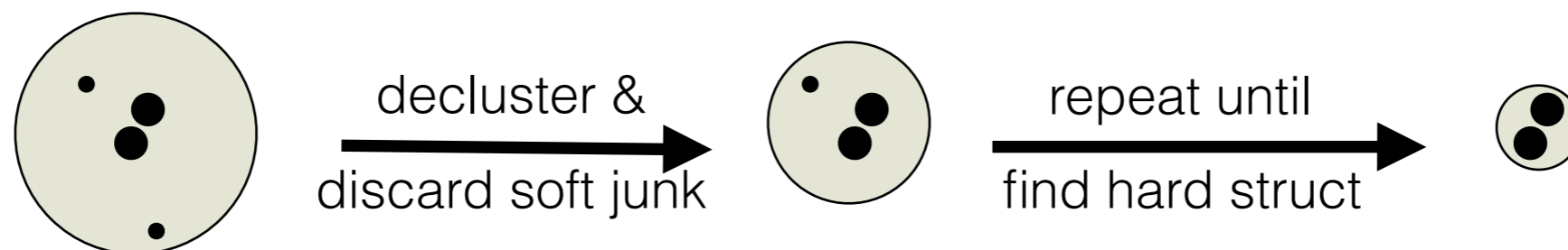
jet is **tagged**.

3. Otherwise discard subjet 2, and go to step 1 with jet \rightarrow subjet 1.

Mass-Drop Tagger

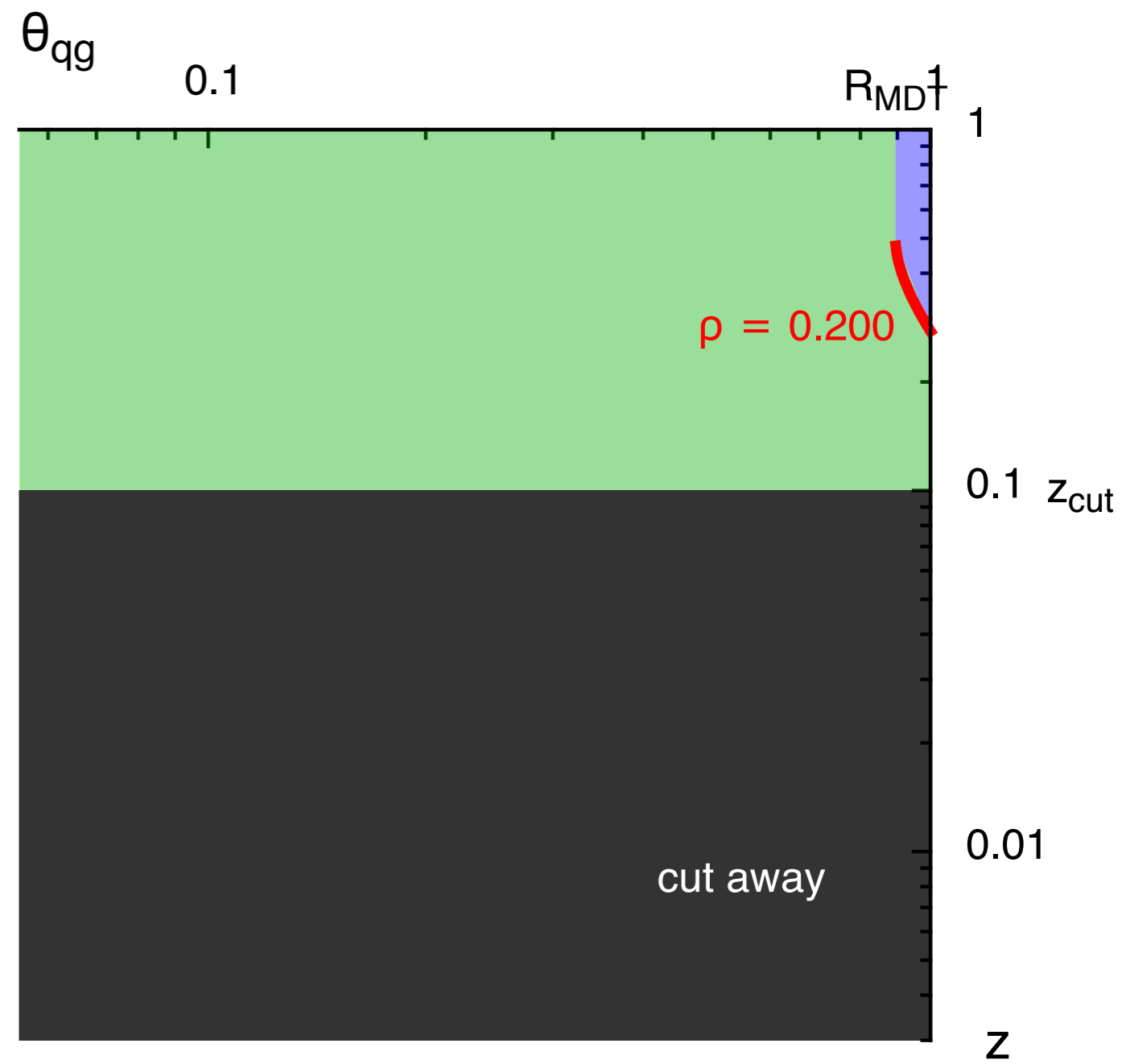
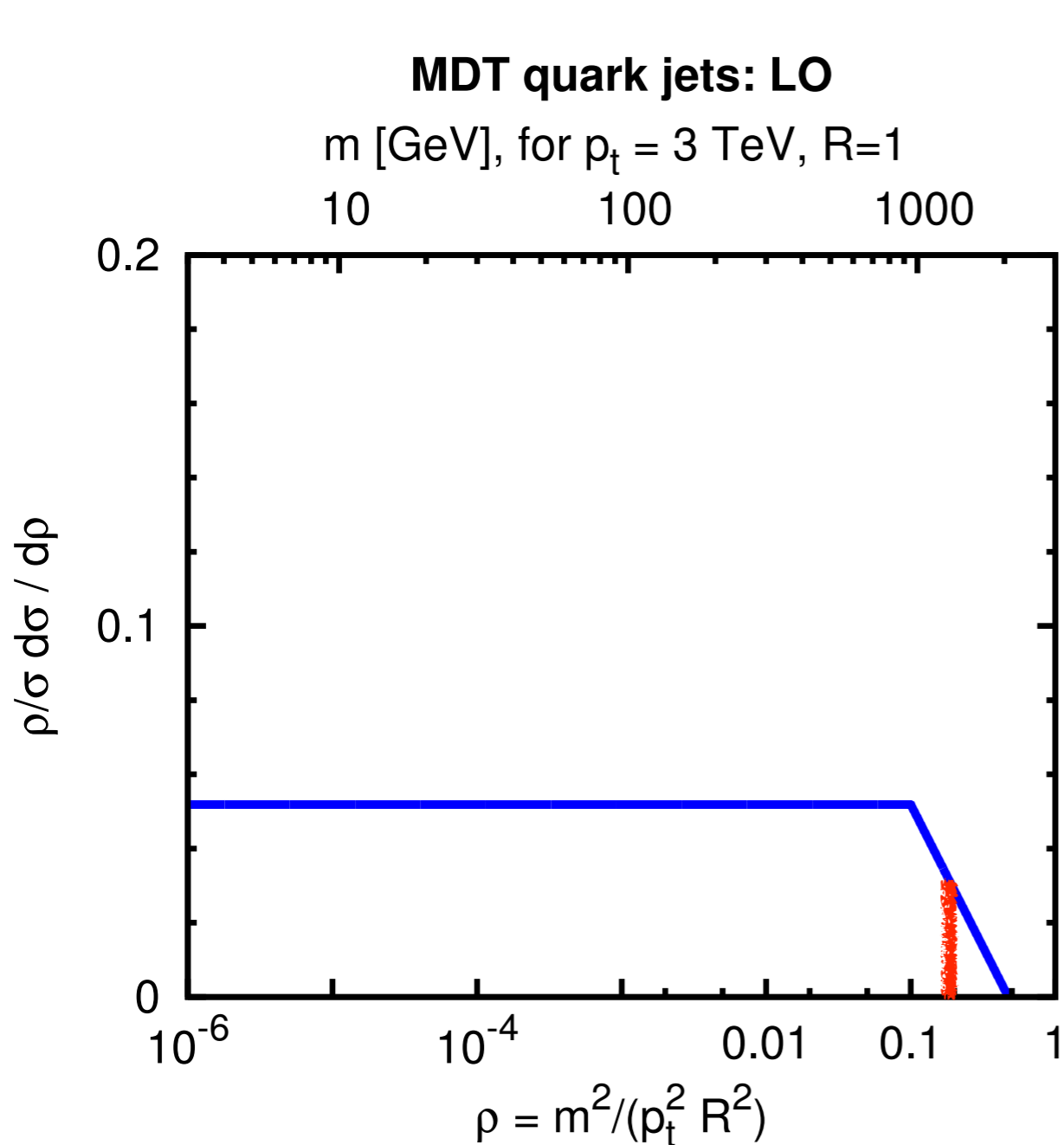
Butterworth, Davison,
Rubin & GPS '08

two parameters:
 μ and y_{cut} ($\sim z_{\text{cut}}$)



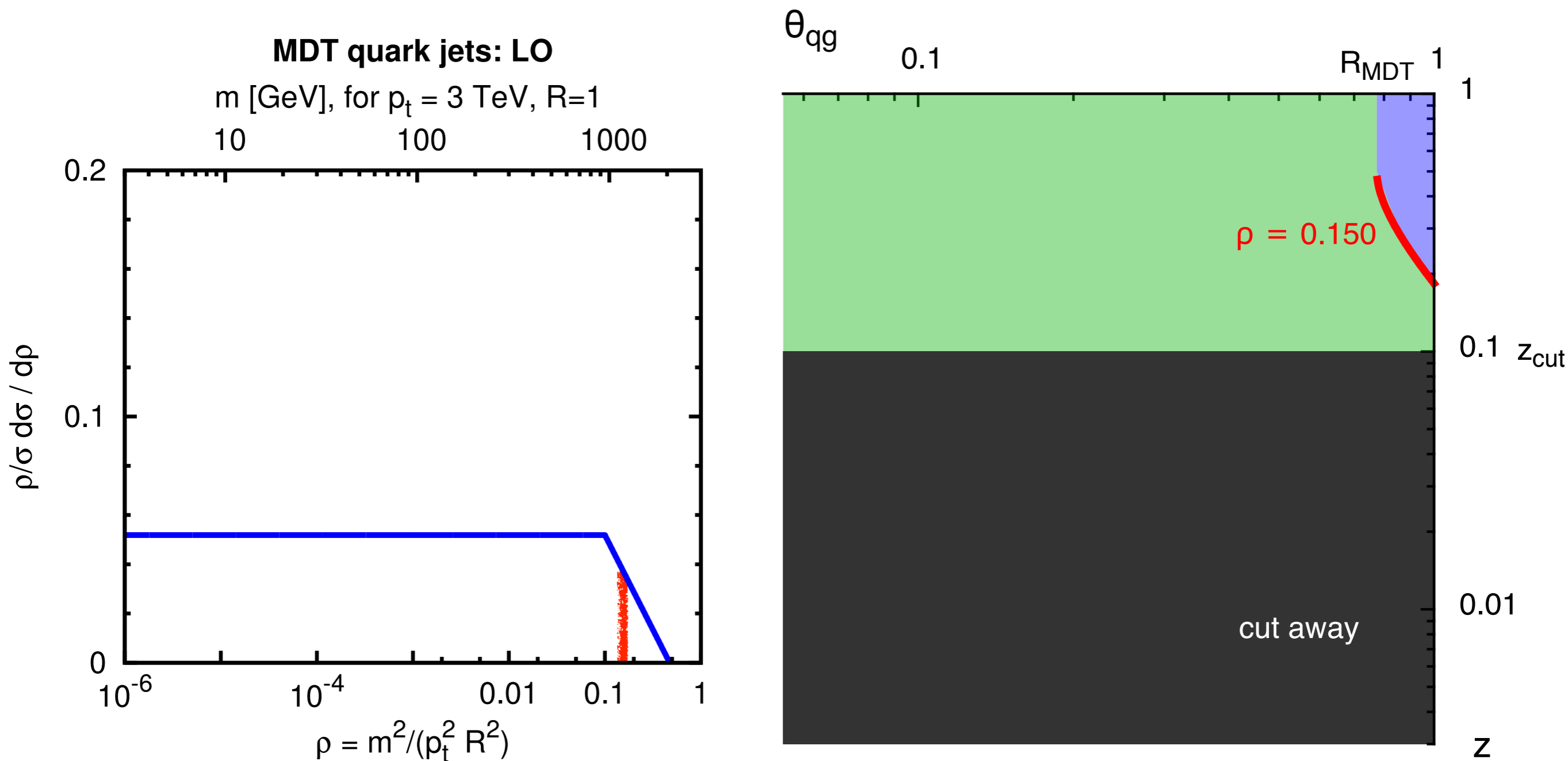
Mass-Drop Tagger at LO

Jet is always split to give two subjets, and so y_{cut} ($\sim z_{\text{cut}}$) is always applied.



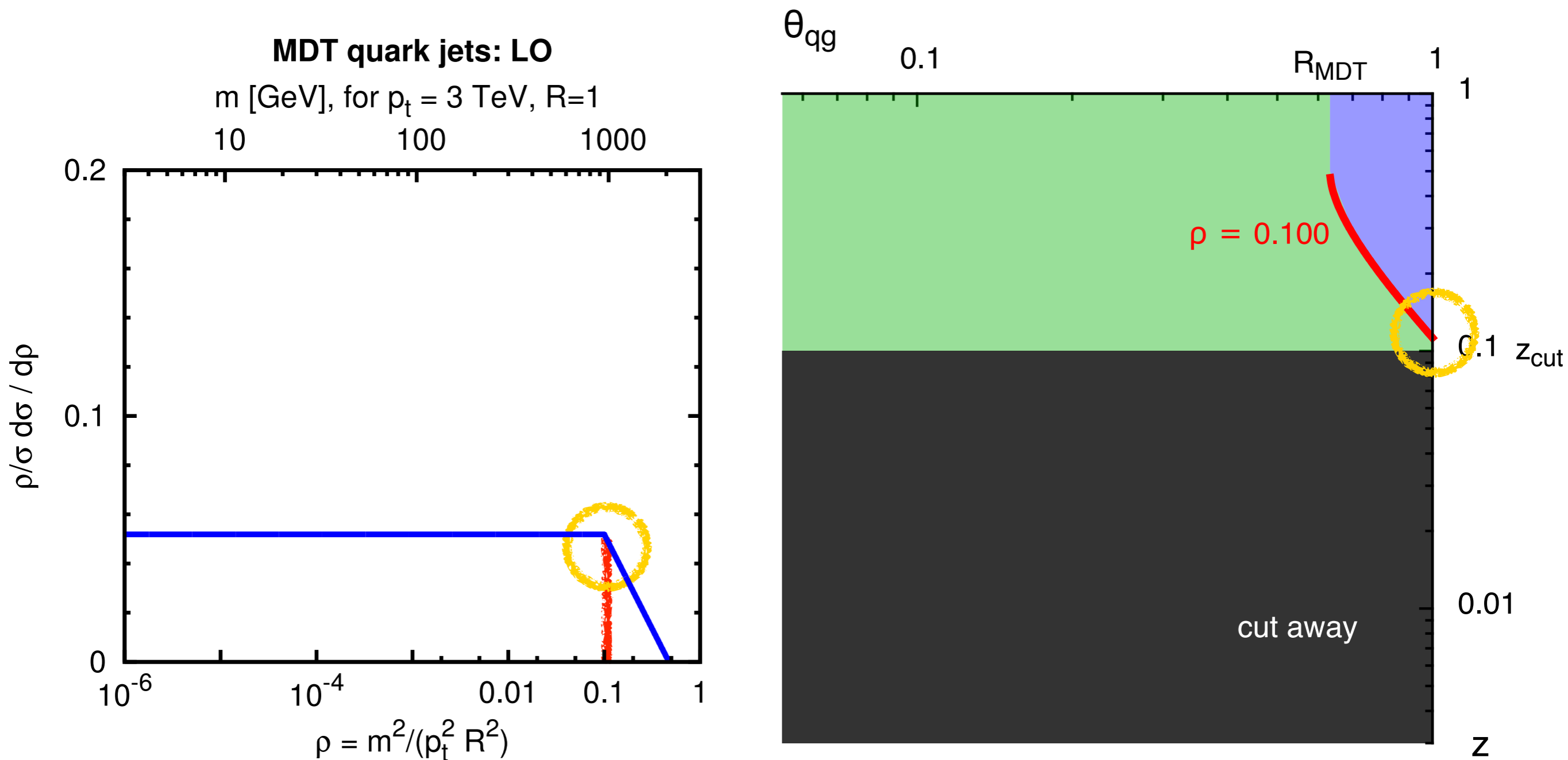
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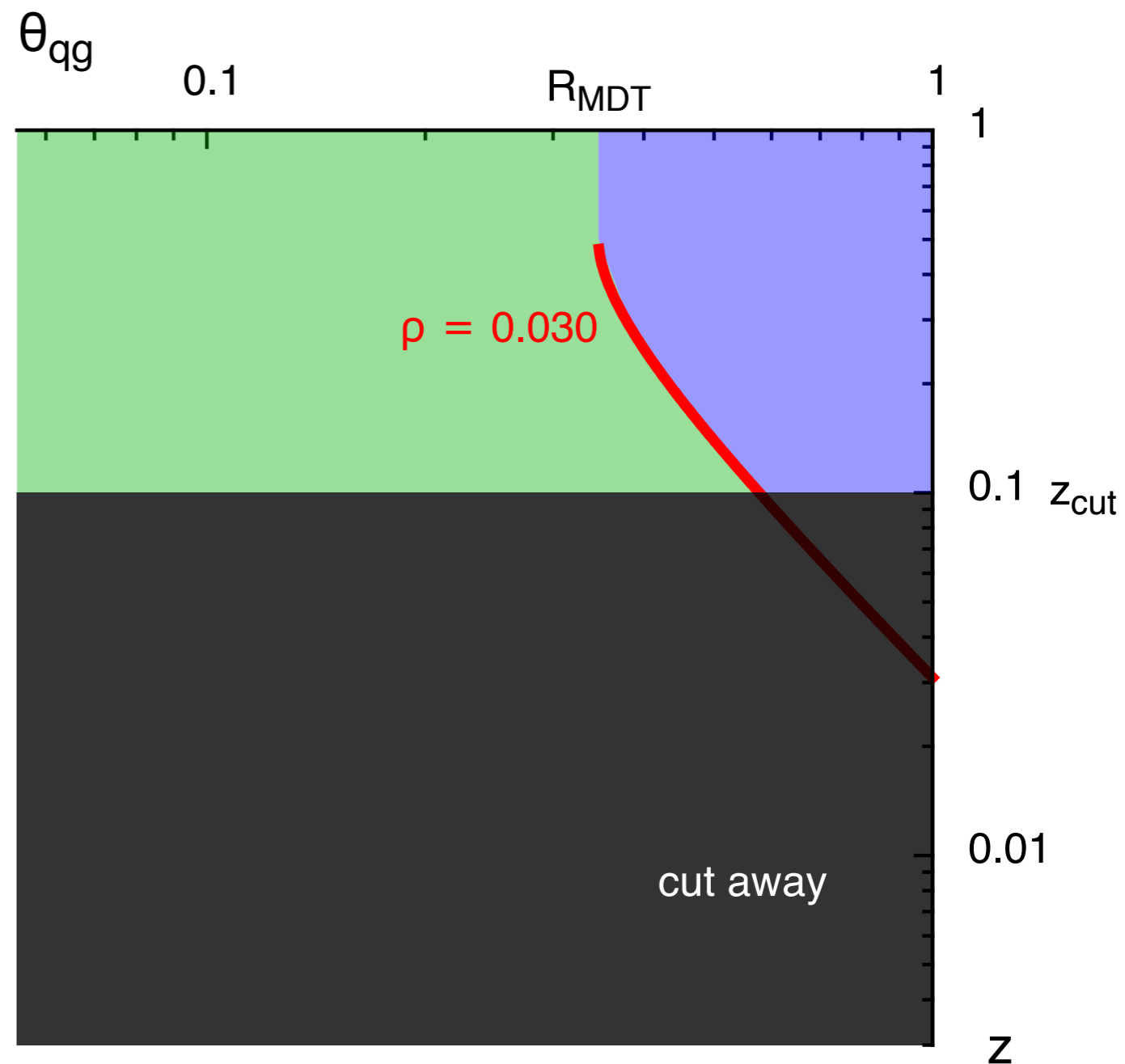
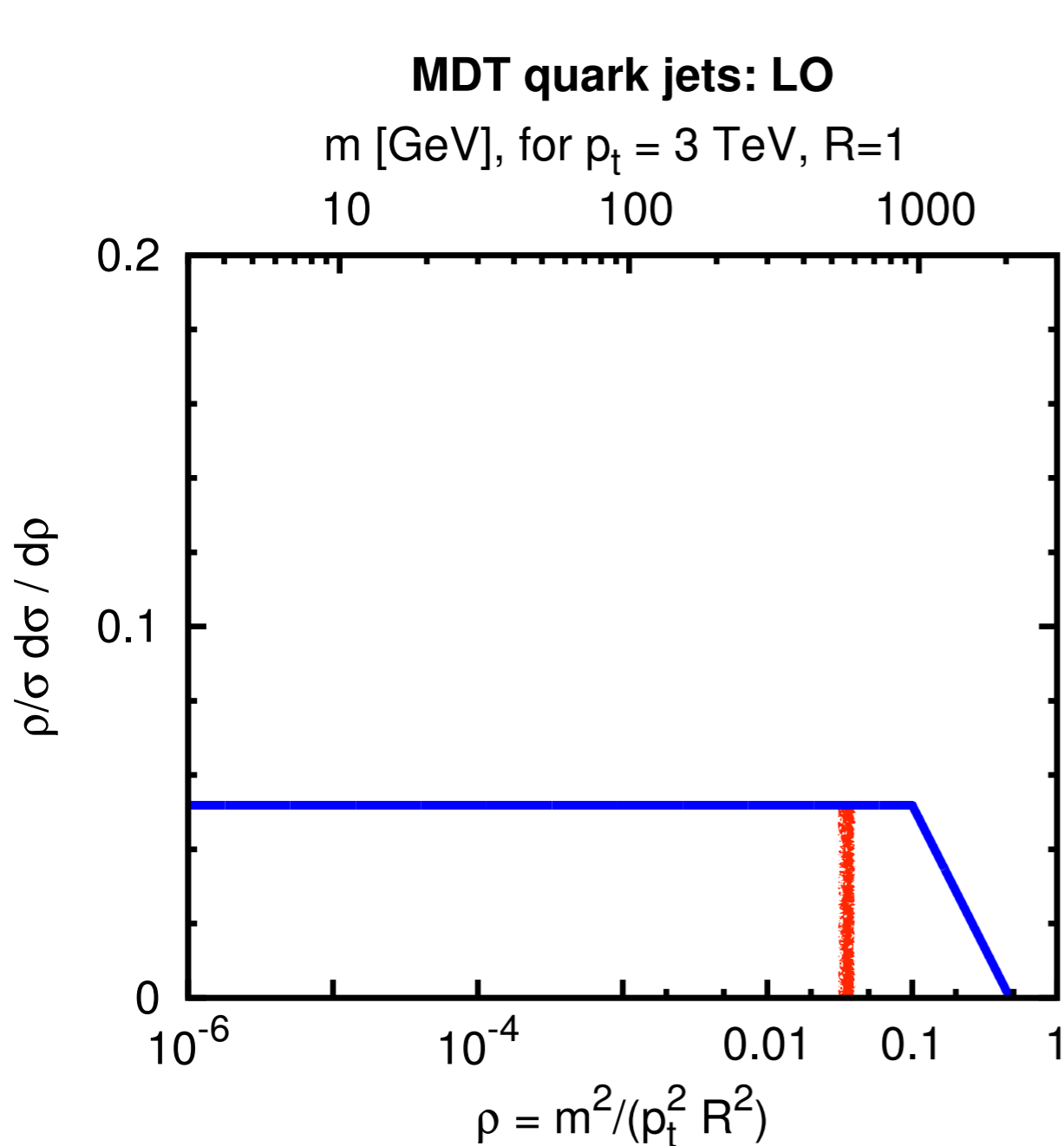
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Jet is always split to give two subjets, and so y_{cut} ($\sim z_{\text{cut}}$) is always applied.



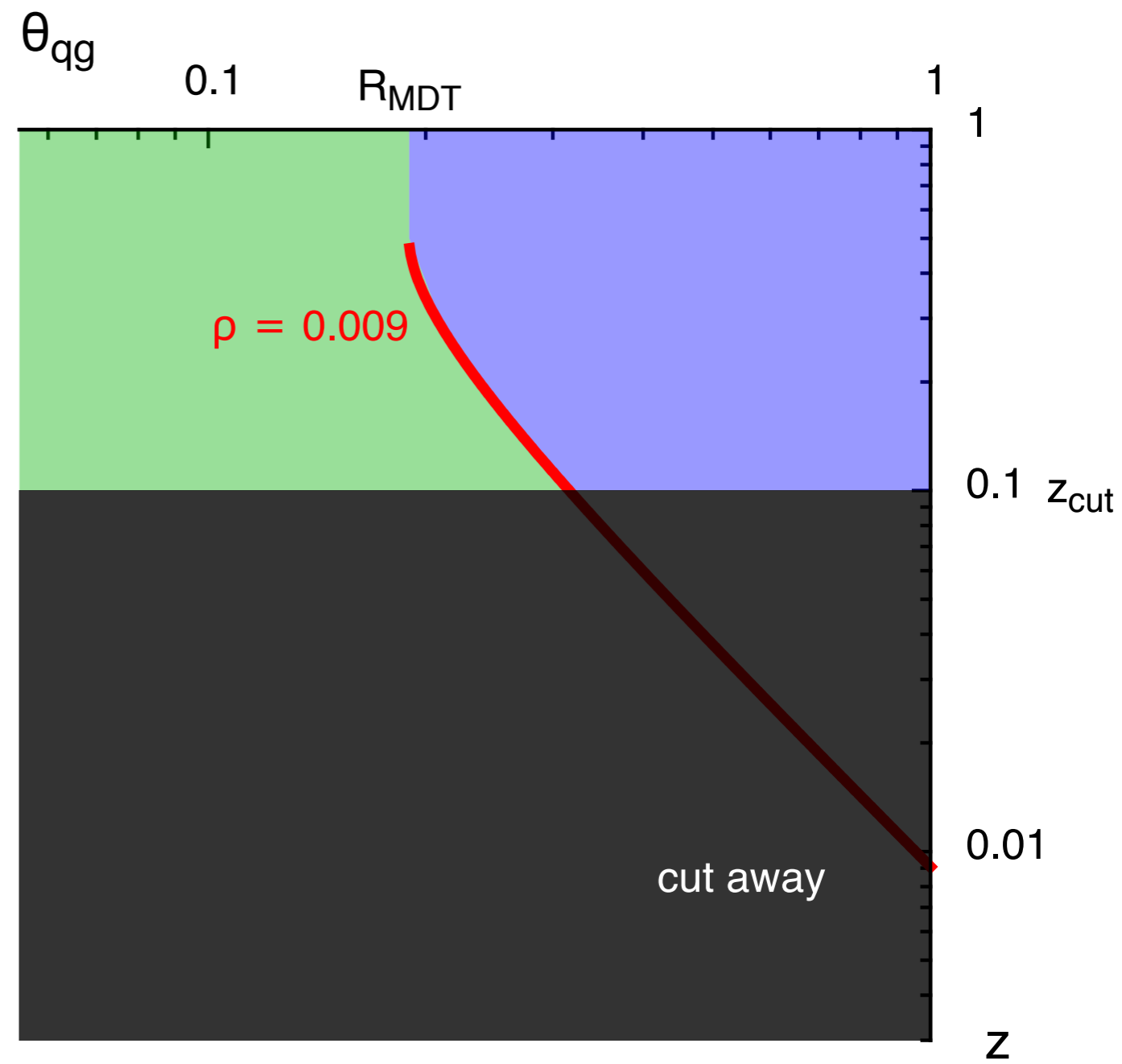
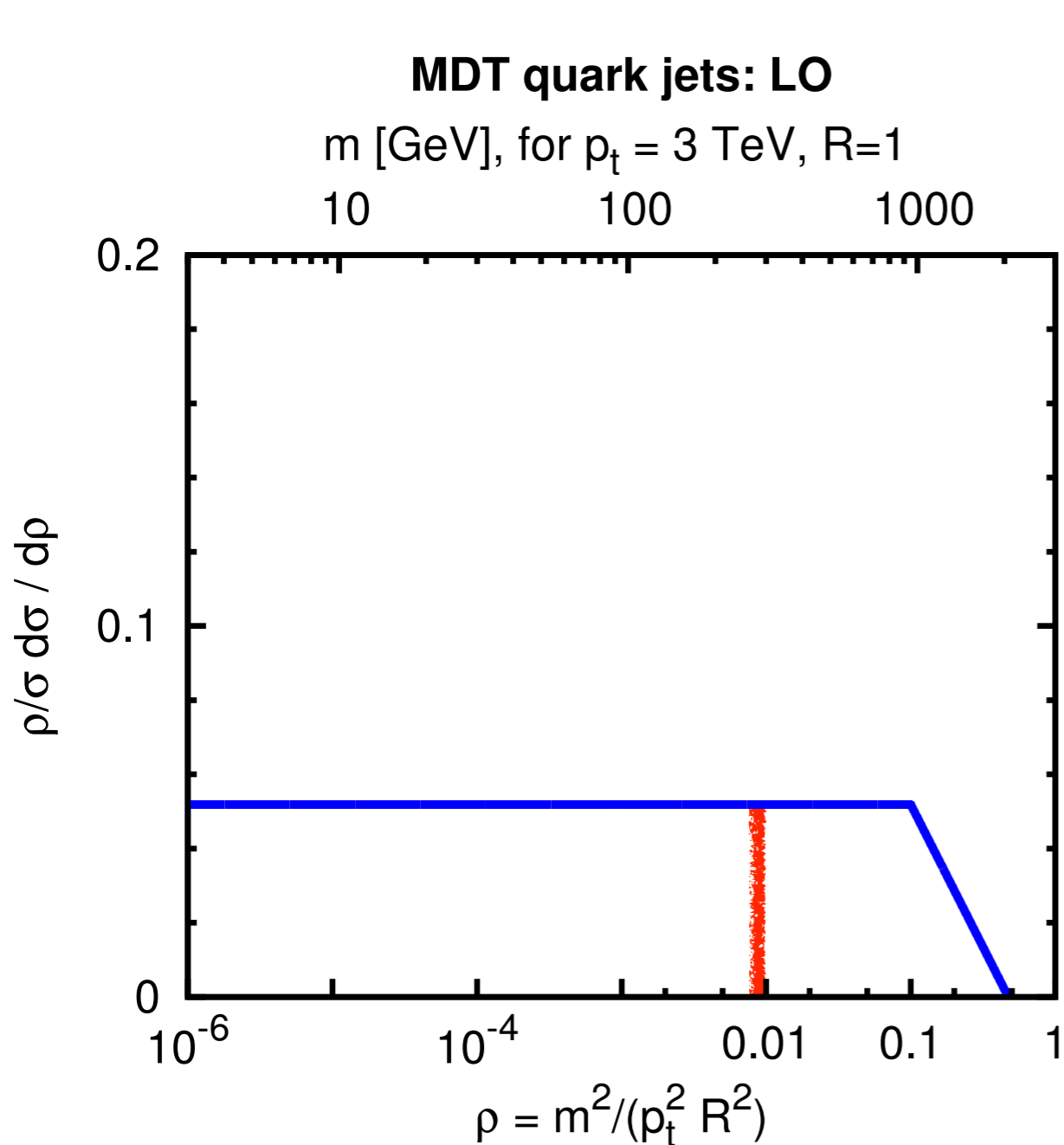
Mass-Drop Tagger at LO

Jet is always split to give two subjets, and so y_{cut} ($\sim z_{\text{cut}}$) is always applied.



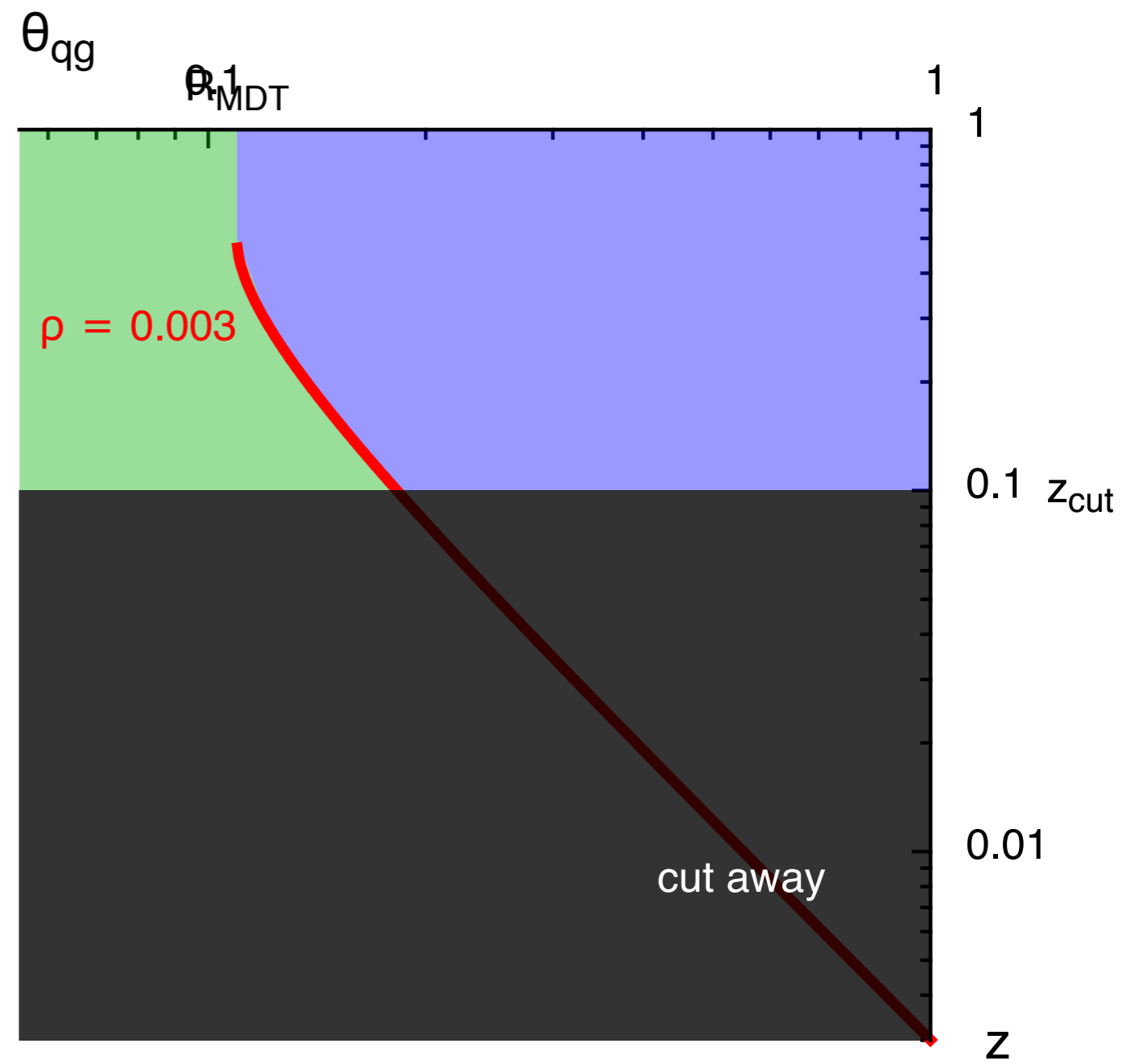
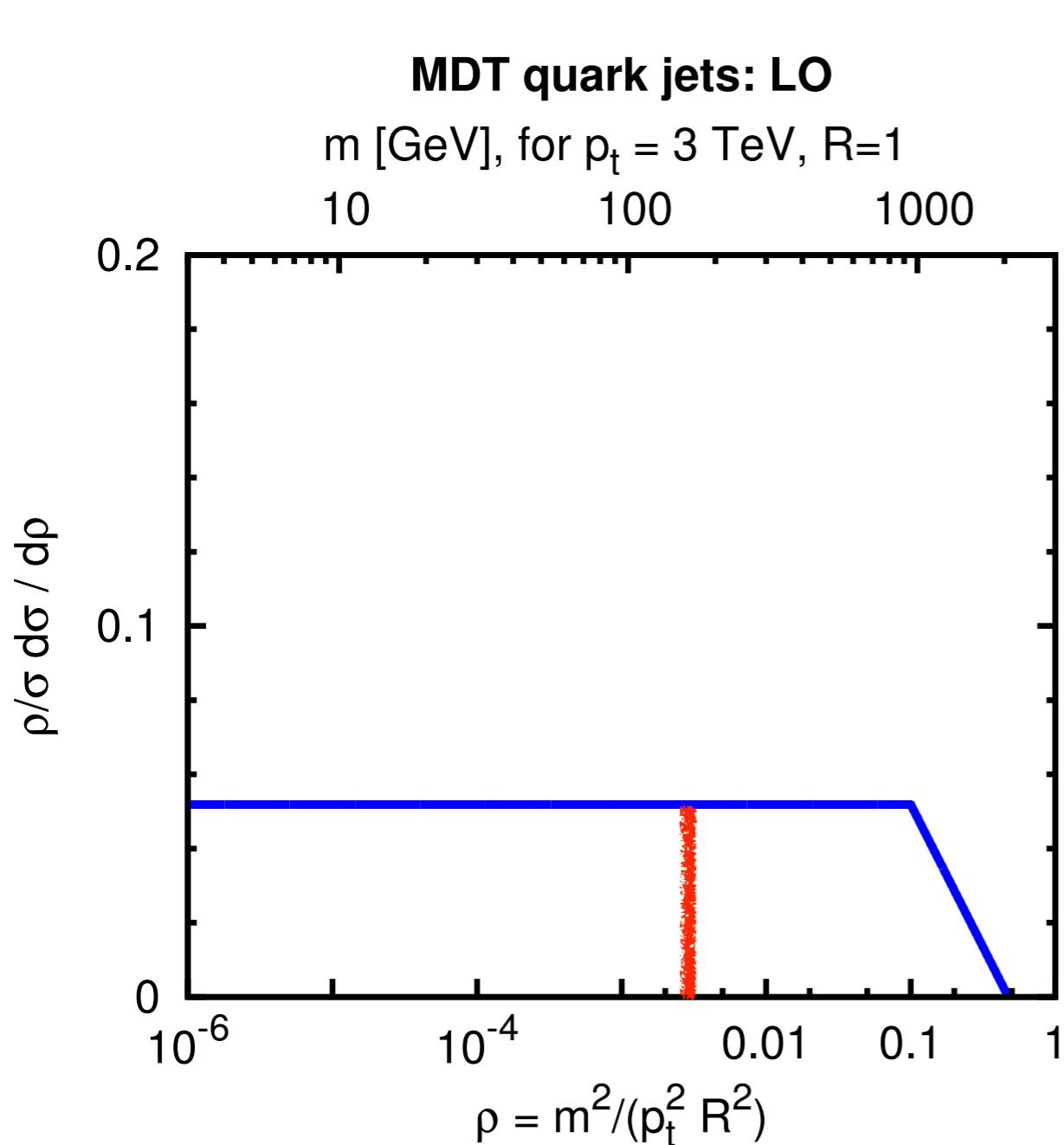
Mass-Drop Tagger at LO

Jet is always split to give two subjets, and so y_{cut} ($\sim z_{\text{cut}}$) is always applied.



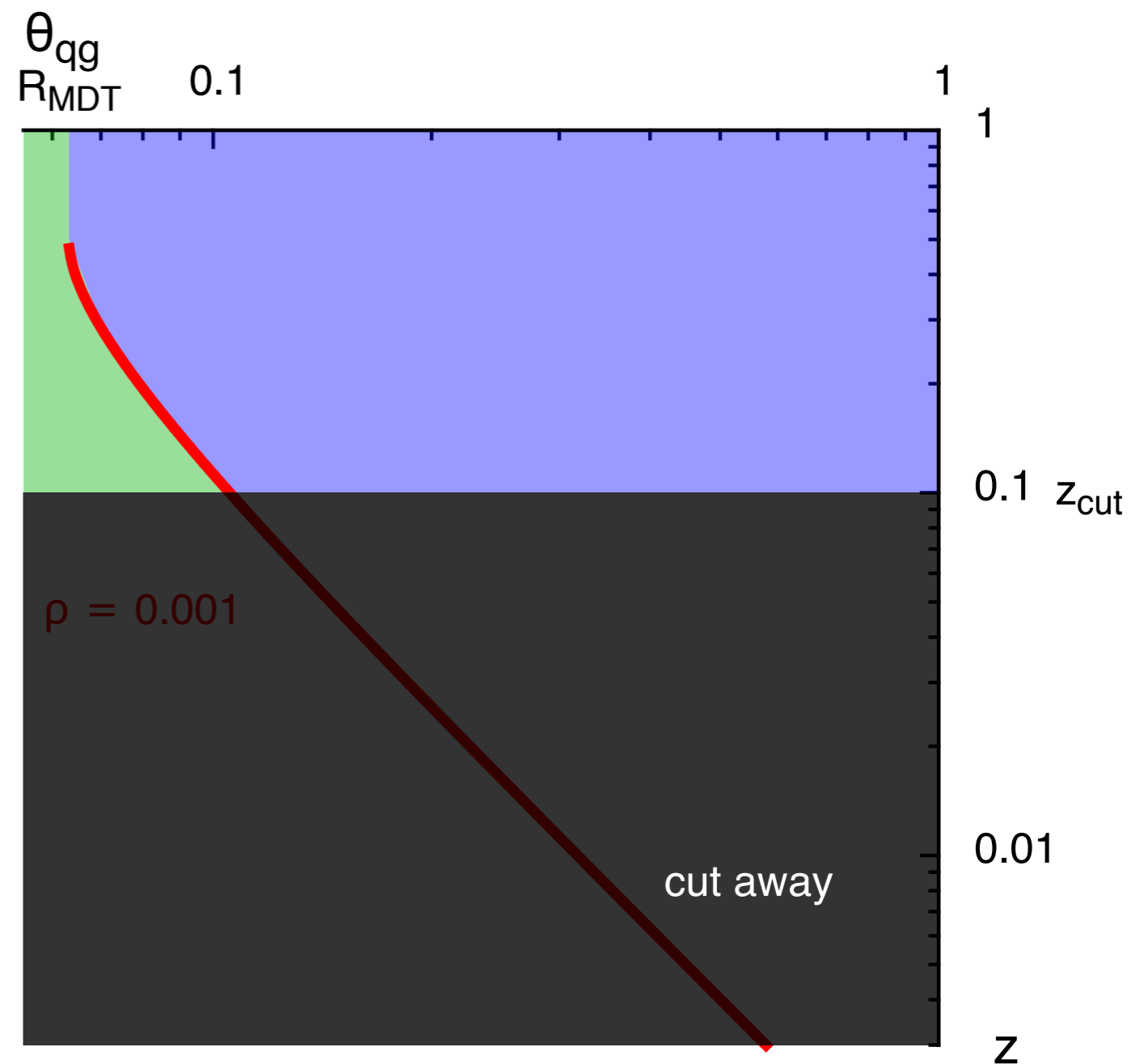
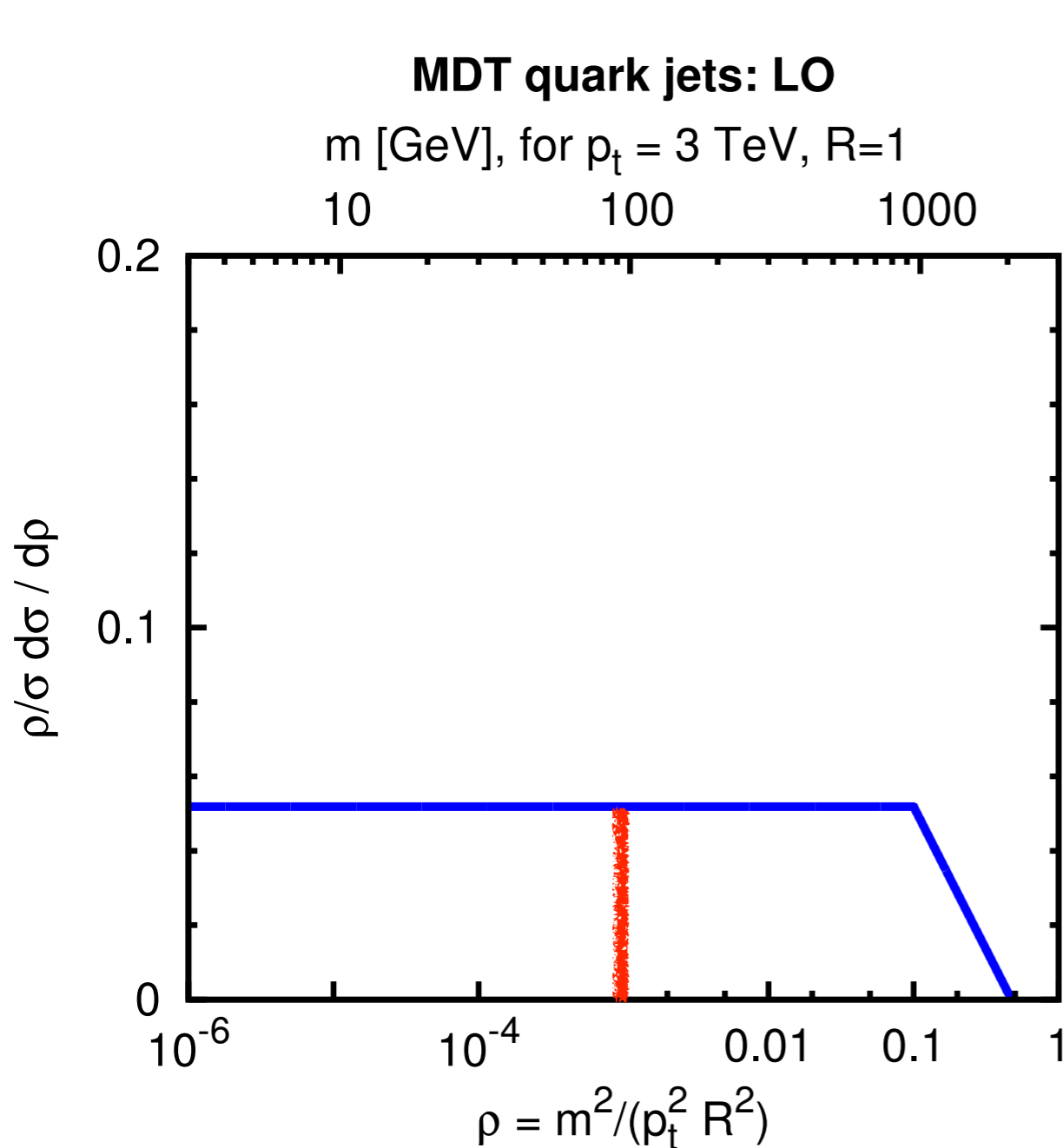
Mass-Drop Tagger at LO

Jet is always split to give two subjets, and so y_{cut} ($\sim z_{\text{cut}}$) is always applied.



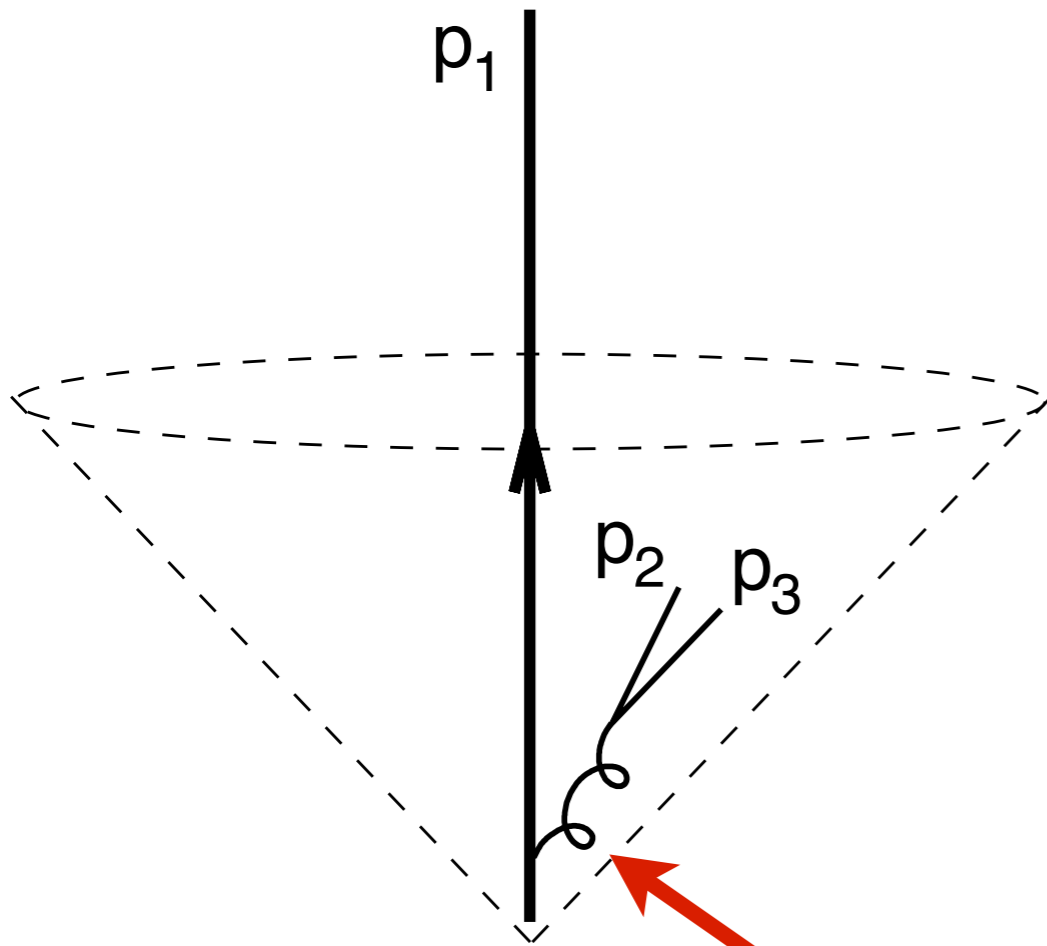
Mass-Drop Tagger at LO

Jet is always split to give two subjets, and so y_{cut} ($\sim z_{\text{cut}}$) is always applied.



What MDT does wrong beyond LO:

Follows a soft branch ($p_2 + p_3 < y_{\text{cut}} p_{\text{jet}}$) with “accidental” small mass, when the “right” answer was that the (massless) hard branch had no substructure



Subjet is soft, but has more substructure than hard subjet

MDT's leading logs (LL, in Σ) are:

$$\alpha_s L, \alpha_s^2 L^3, \dots \text{ I.e. } \alpha_s^n L^{2n-1}$$

quite complicated to evaluate

A simple fix: “**modified**” Mass Drop Tagger:

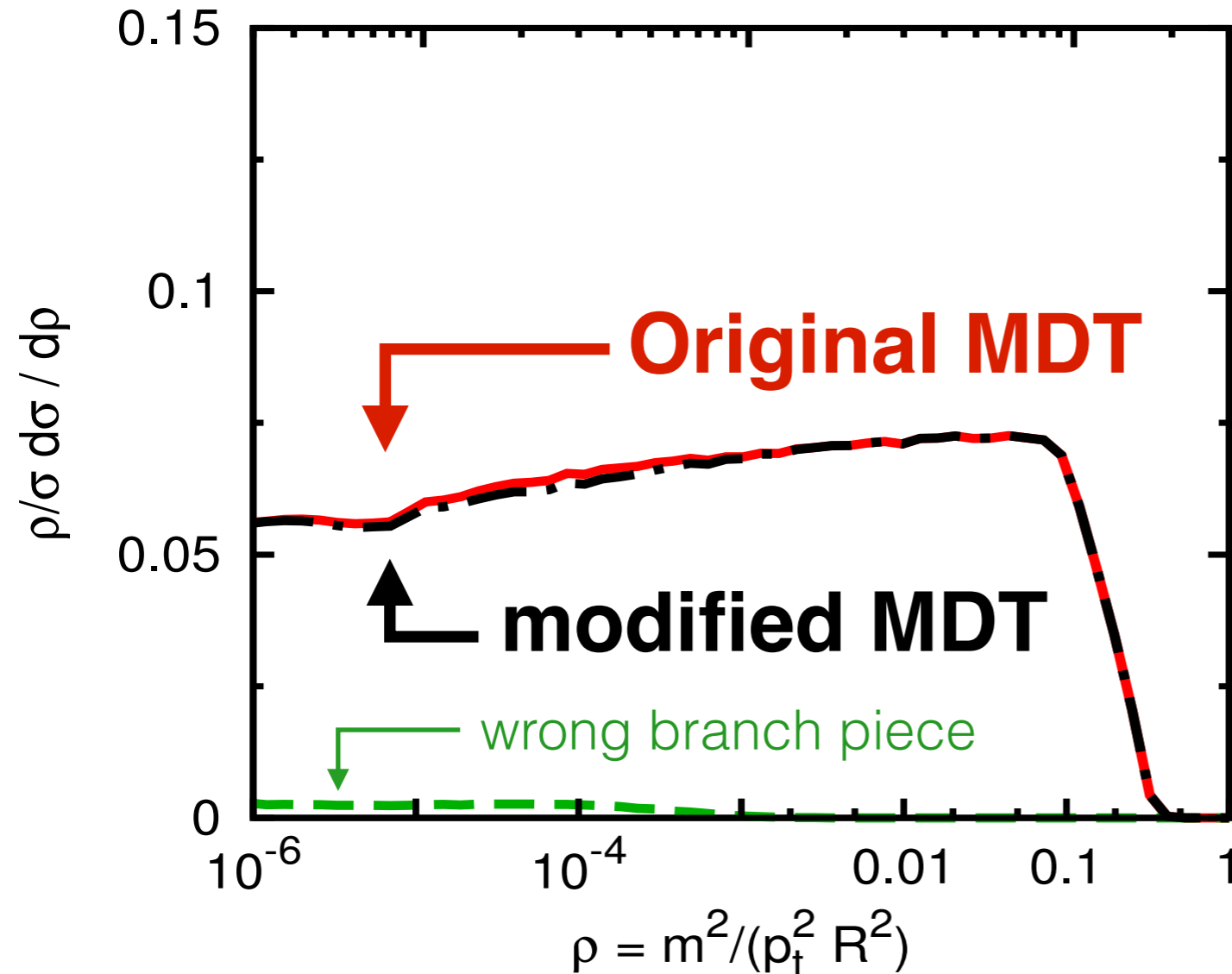
When recursing, **follow branch with larger $(m^2+p_t^2)$**

(rather than the one with larger m)

Pythia 6 MC: quark jets

m [GeV], for $p_t = 3$ TeV, $R = 1$

10 100 1000



Modification has almost no phenomenological impact, but big analytical consequences...

modified Mass Drop Tagger

At most “single logs”, at all orders, i.e.

$$\alpha_s L, \alpha_s^2 L^2, \dots \text{ I.e. } \alpha_s^n L^n$$

Logs exclusively collinear – much simpler than jet mass

➔ no non-global logs

➔ no clustering logs

➔ no super-leading (factorization-breaking) logs

First time anything like this has been seen

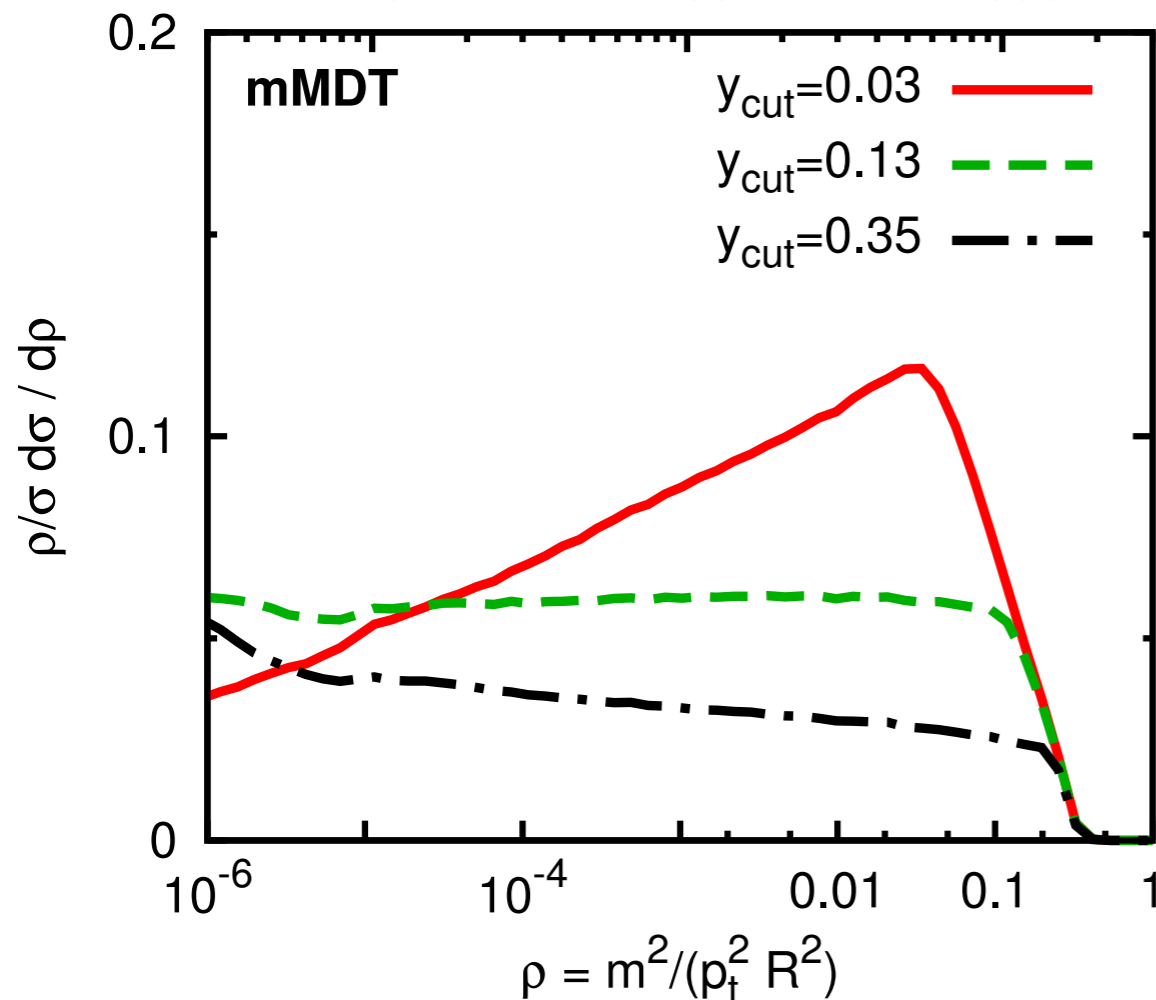
Fairly simple formulae; e.g. [fixed-coupling]

$$\Sigma^{(\text{mMDT})}(\rho) = \exp \left[-\frac{\alpha_s C_F}{\pi} \left(\ln \frac{y_{\text{cut}}}{\rho} \ln \frac{1}{y_{\text{cut}}} - \frac{3}{4} \ln \frac{1}{\rho} + \frac{1}{2} \ln^2 \frac{1}{y_{\text{cut}}} \right) \right]$$

Monte Carlo

m [GeV], for $p_t = 3$ TeV, $R = 1$

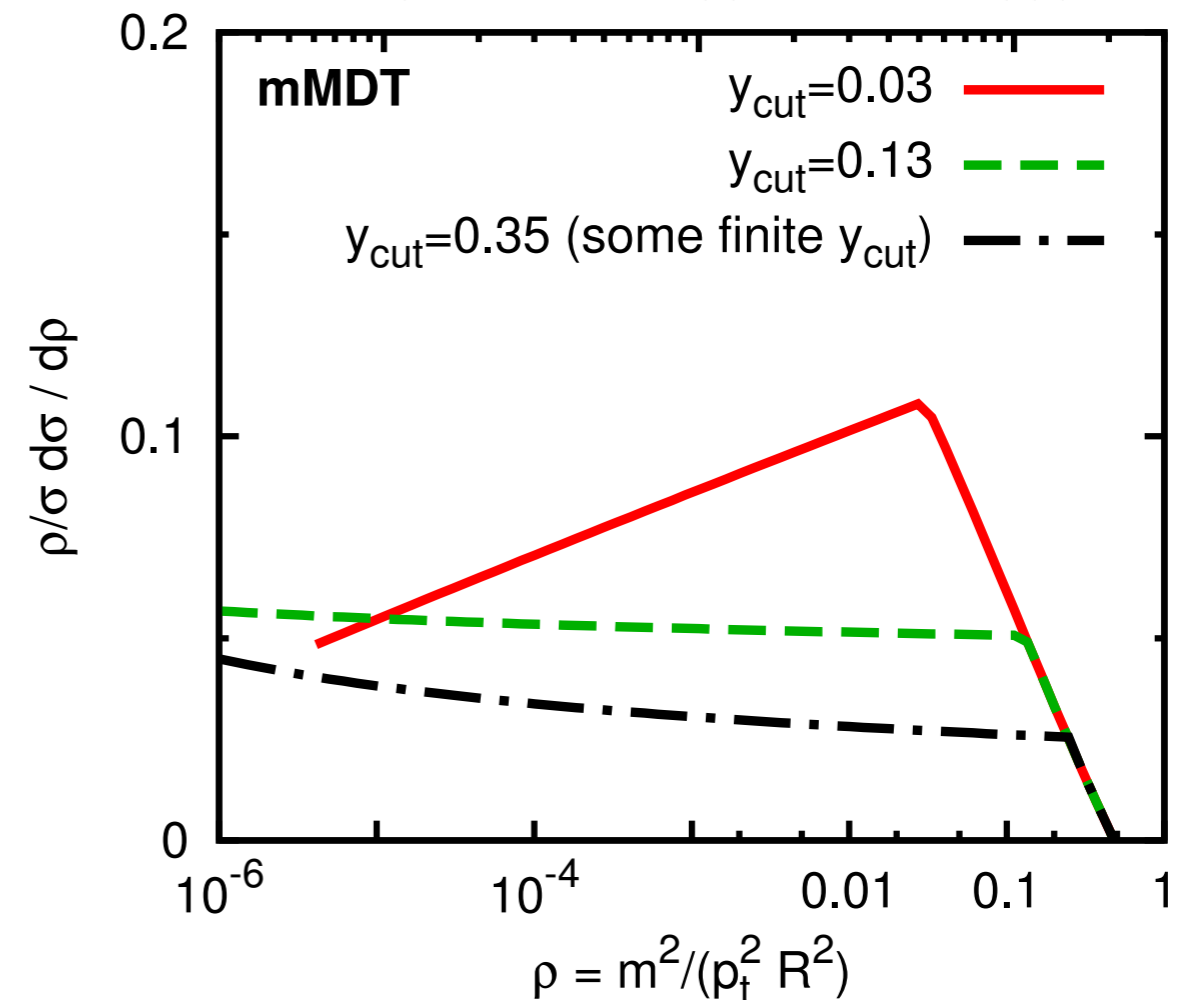
10 100 1000



Analytic

m [GeV], for $p_t = 3$ TeV, $R = 1$

10 100 1000

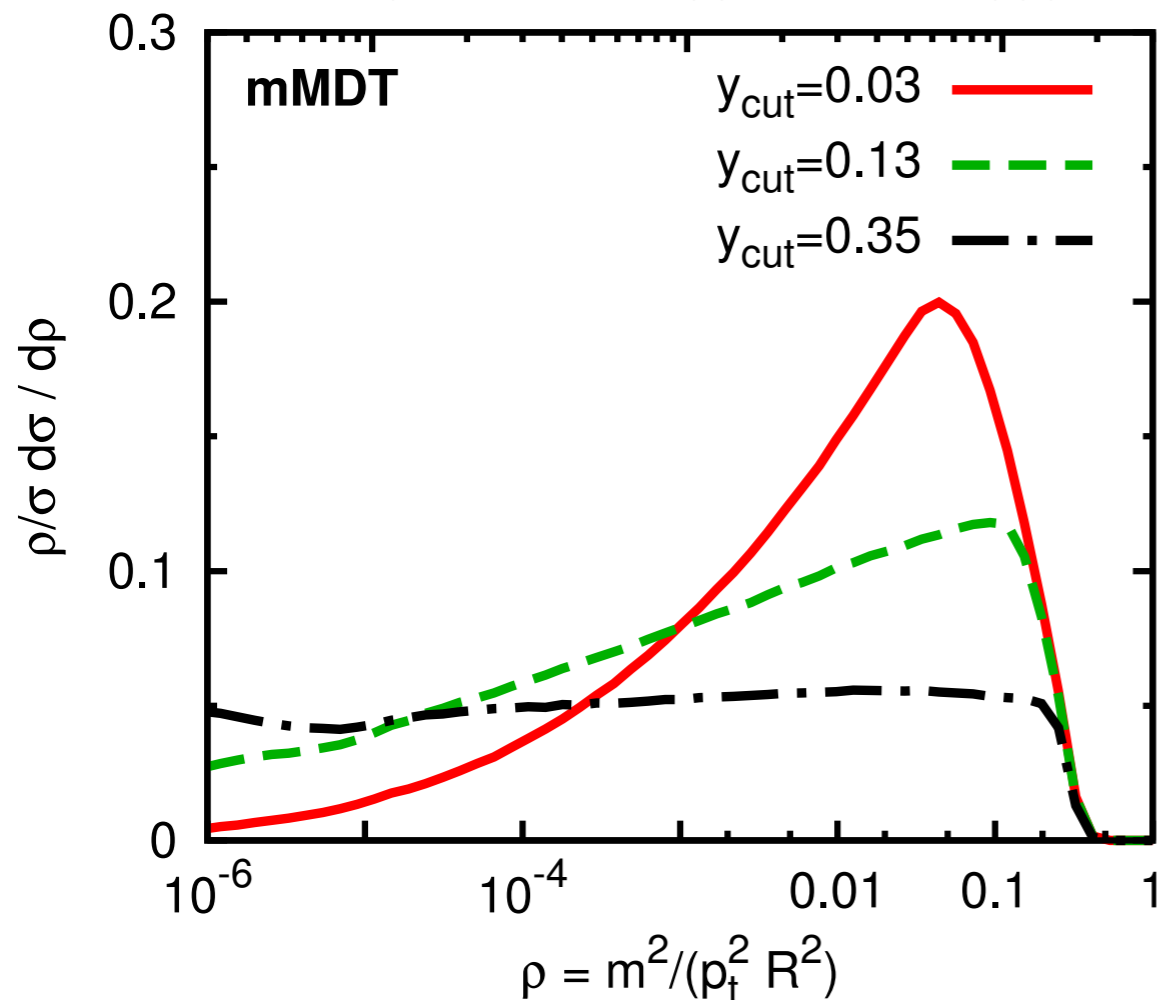


[mMDT is closest we have to a scale-invariant tagger, though exact behaviour depends on q/g fractions]

Monte Carlo

m [GeV], for $p_t = 3$ TeV, $R = 1$

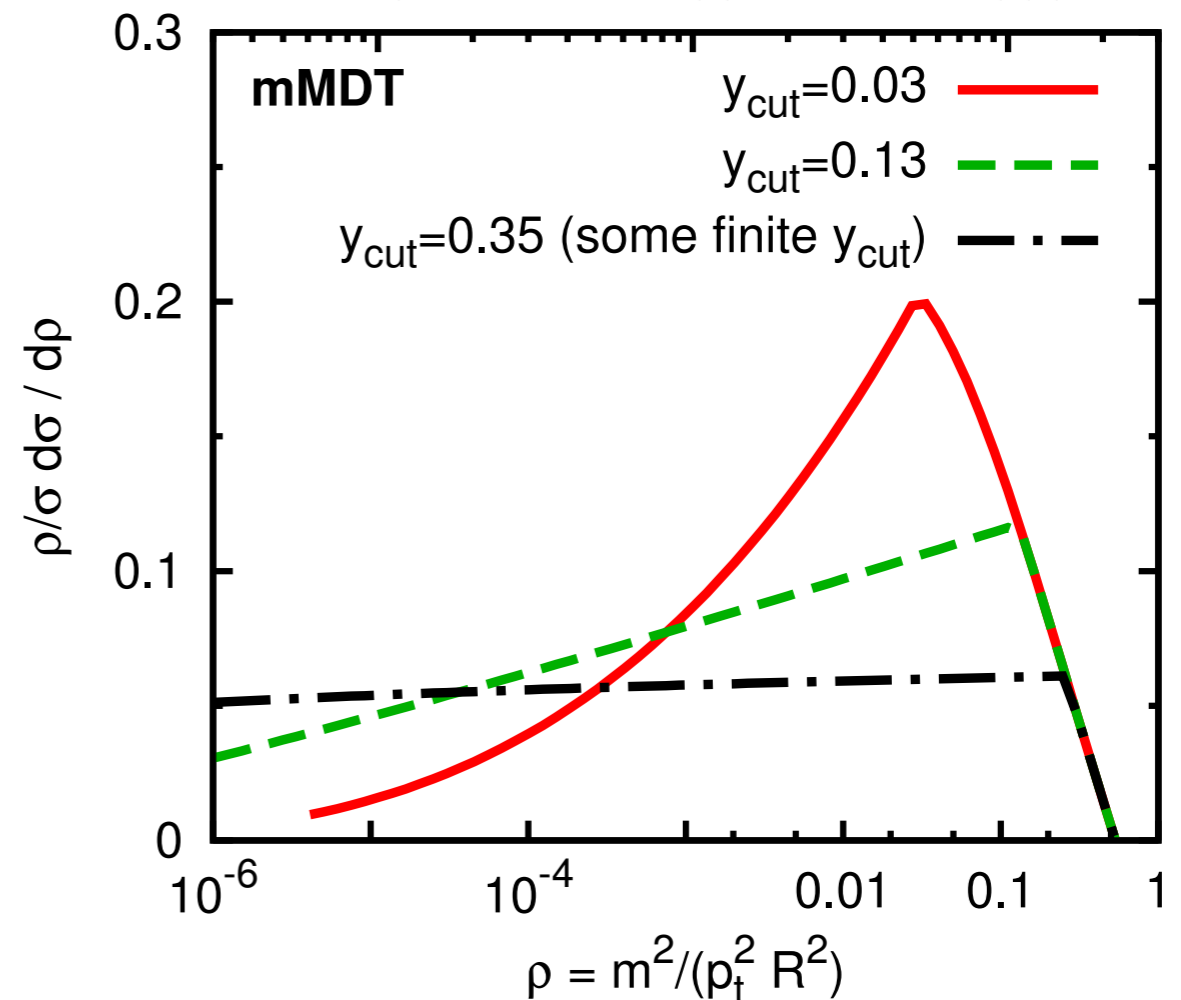
10 100 1000



Analytic

m [GeV], for $p_t = 3$ TeV, $R = 1$

10 100 1000



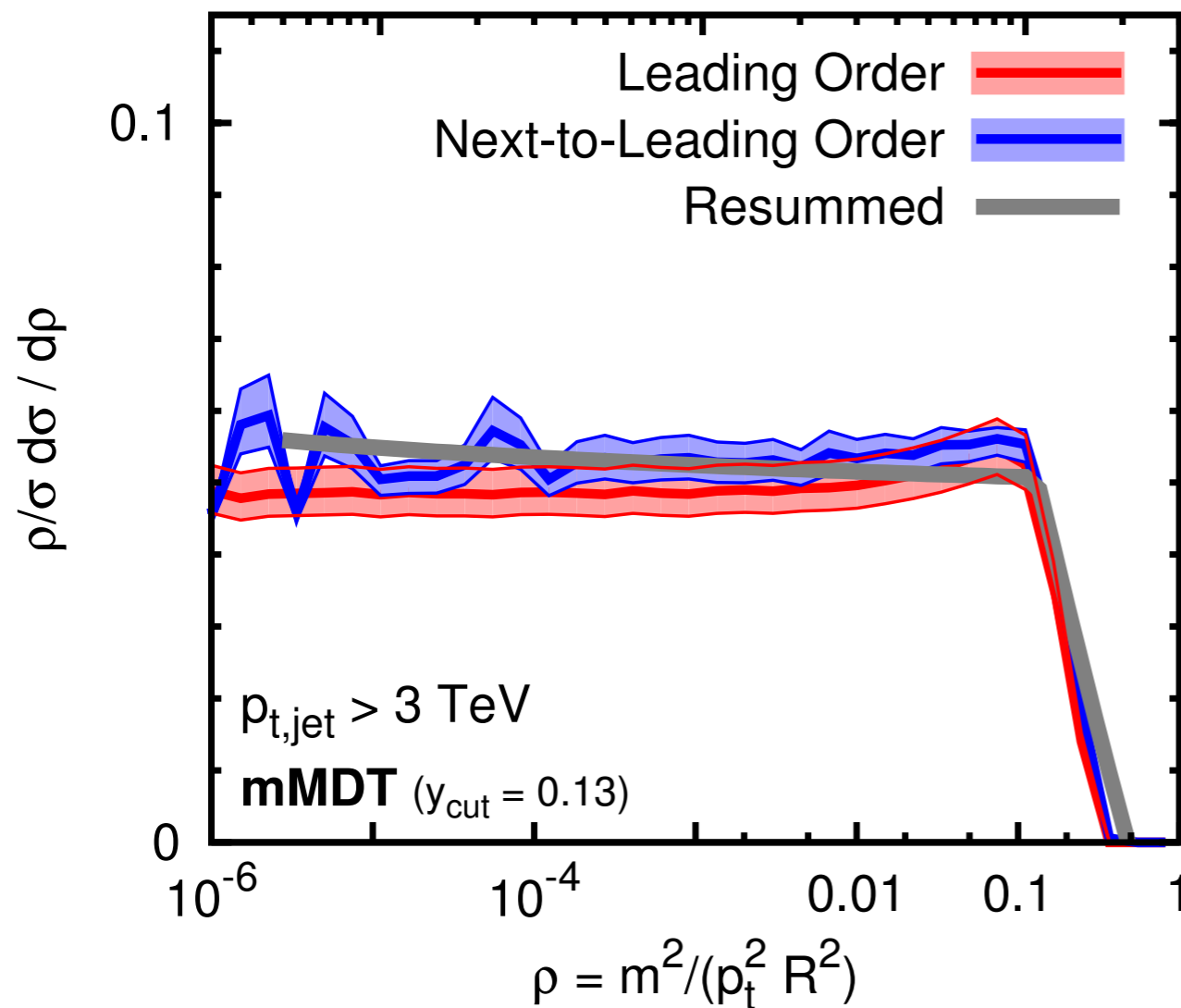
[mMDT is closest we have to a scale-invariant tagger, though exact behaviour depends on q/g fractions]

mMDT resummation v. fixed order

LO v. NLO v. resummation (quark jets)

m [GeV], for $p_t = 3$ TeV, $R = 1$

10 100 1000



NLO from NLOJet++

Because we only have single logs, fixed-order is valid over a broader than usual range of scales

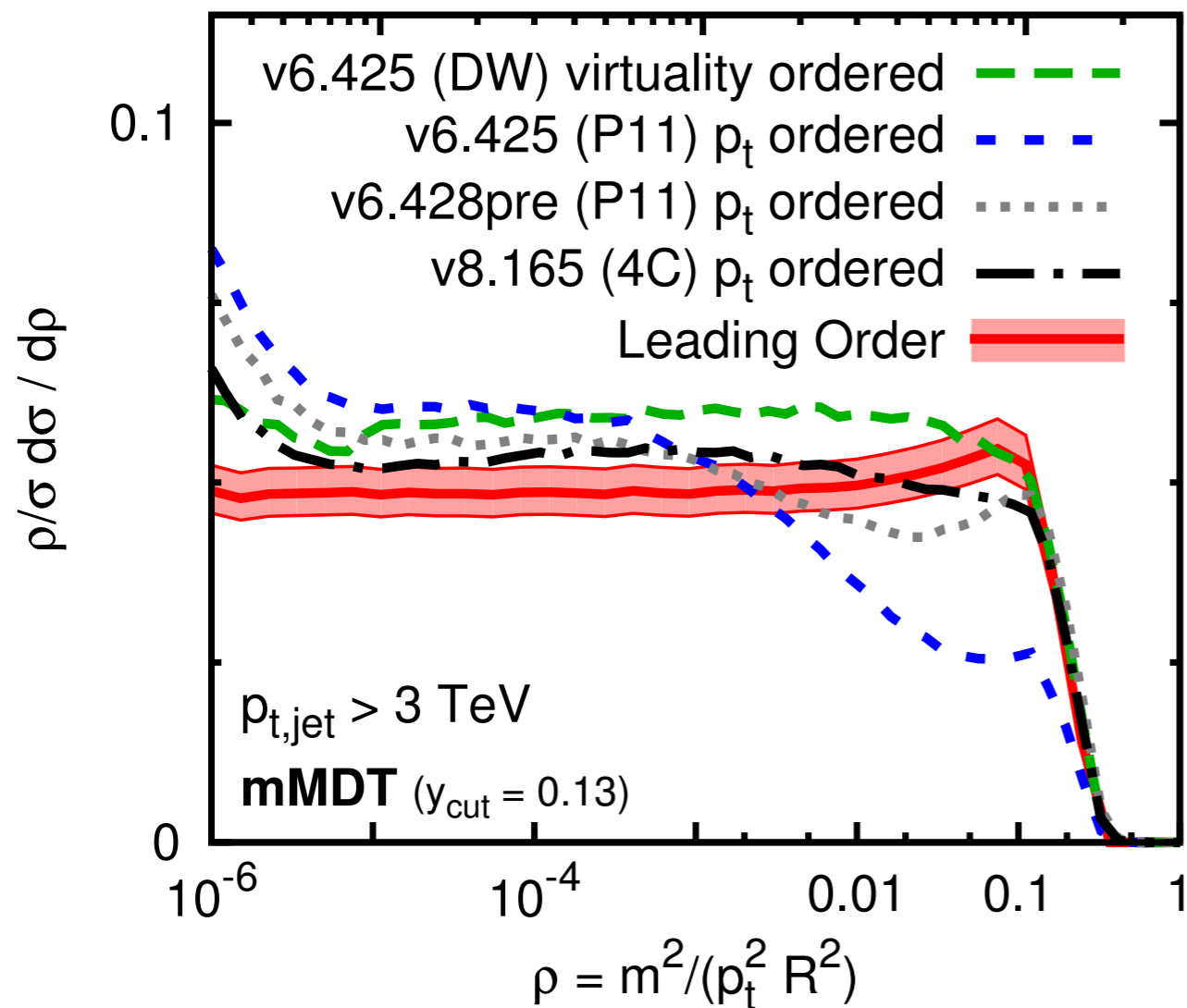
(helped by fortuitous cancellation between running coupling and single-log Sudakov)

mMDT: comparing many showers

LO v. Pythia showers (quark jets)

m [GeV], for $p_{t,jet} = 3$ TeV, $R = 1$

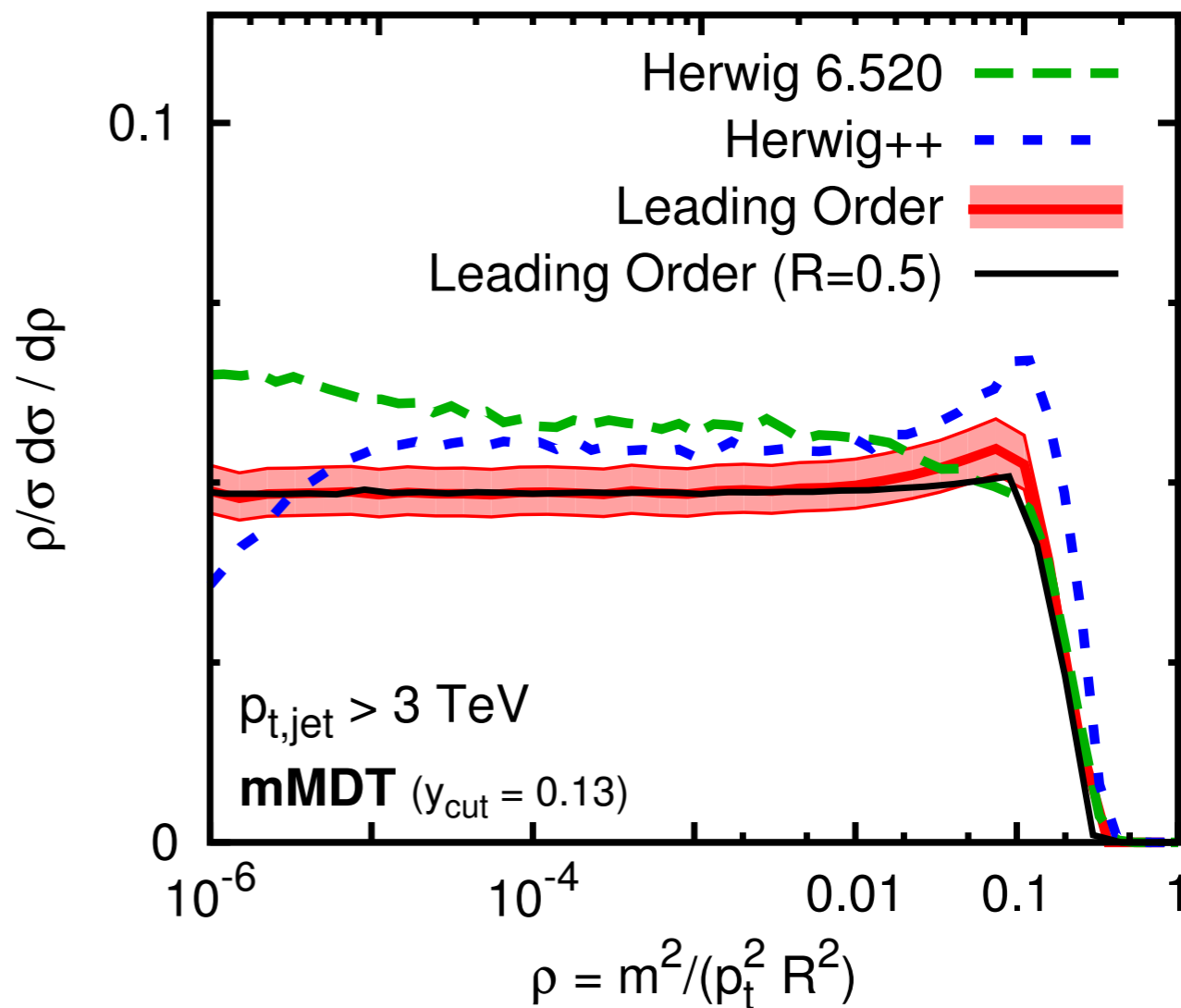
10 100 1000



LO v. Herwig showers (quark jets)

m [GeV], for $p_{t,jet} = 3$ TeV, $R = 1$

10 100 1000

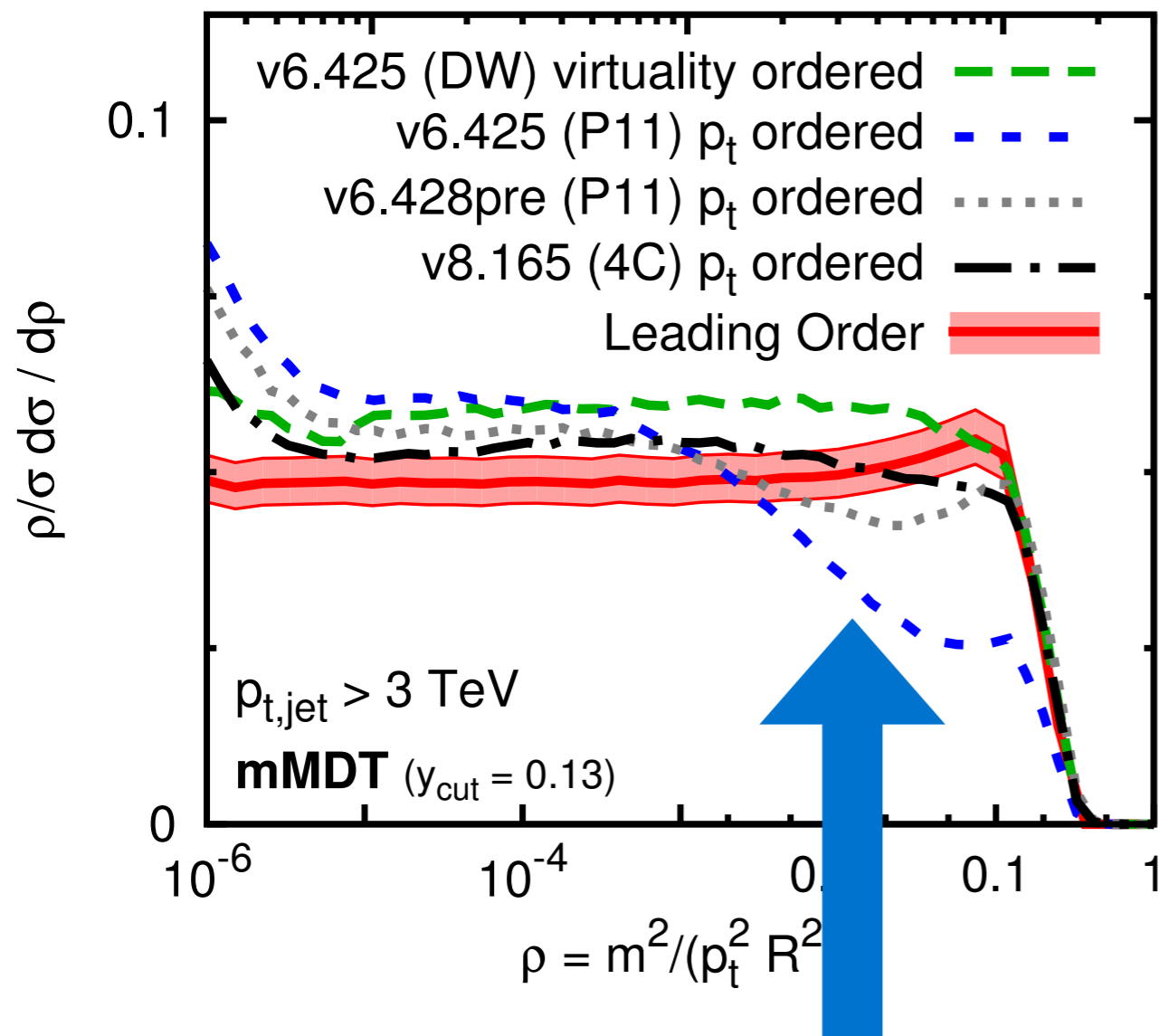


mMDT: comparing many showers

LO v. Pythia showers (quark jets)

m [GeV], for $p_{t,jet} = 3$ TeV, $R = 1$

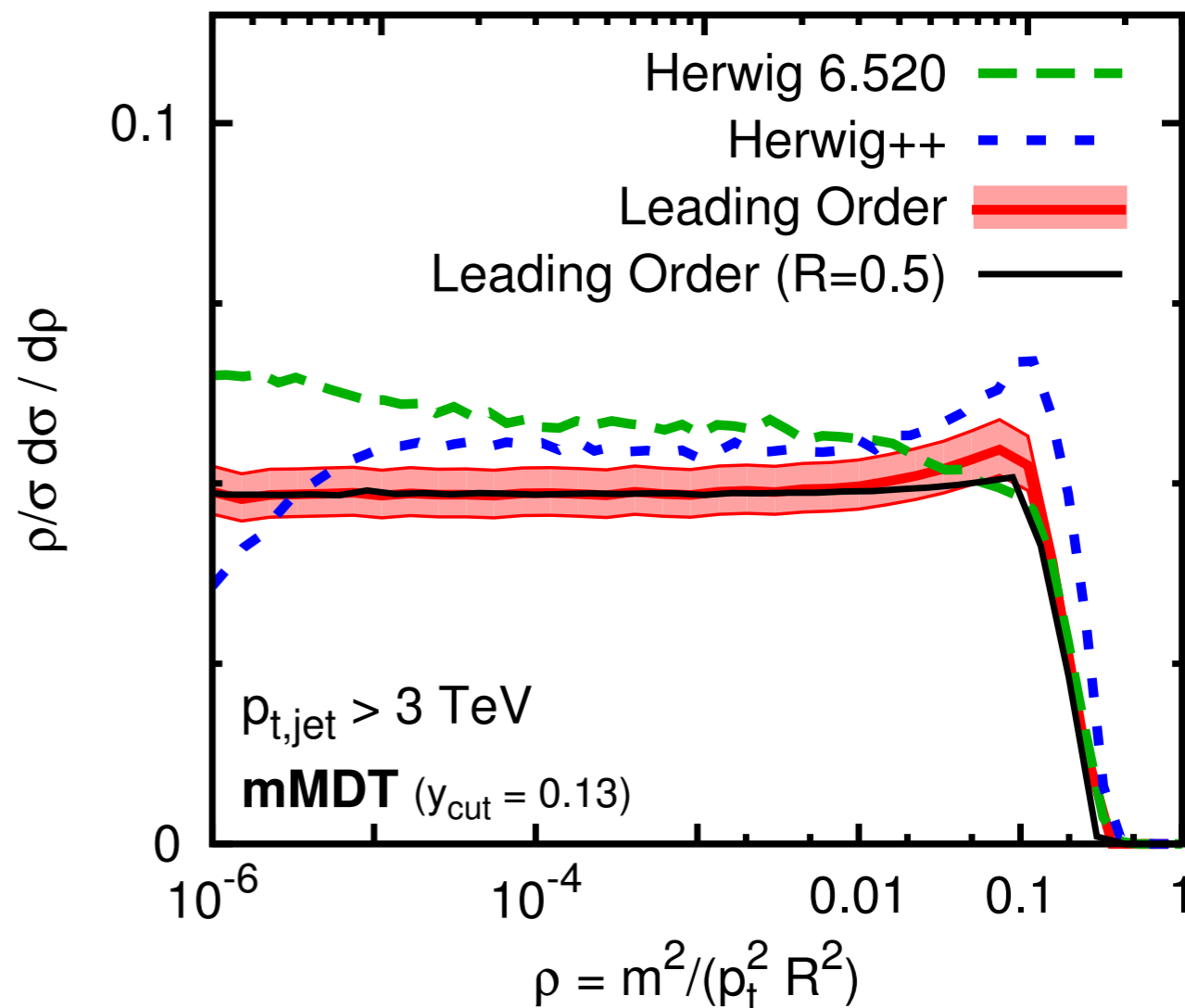
10 100 1000



LO v. Herwig showers (quark jets)

m [GeV], for $p_{t,jet} = 3$ TeV, $R = 1$

10 100 1000



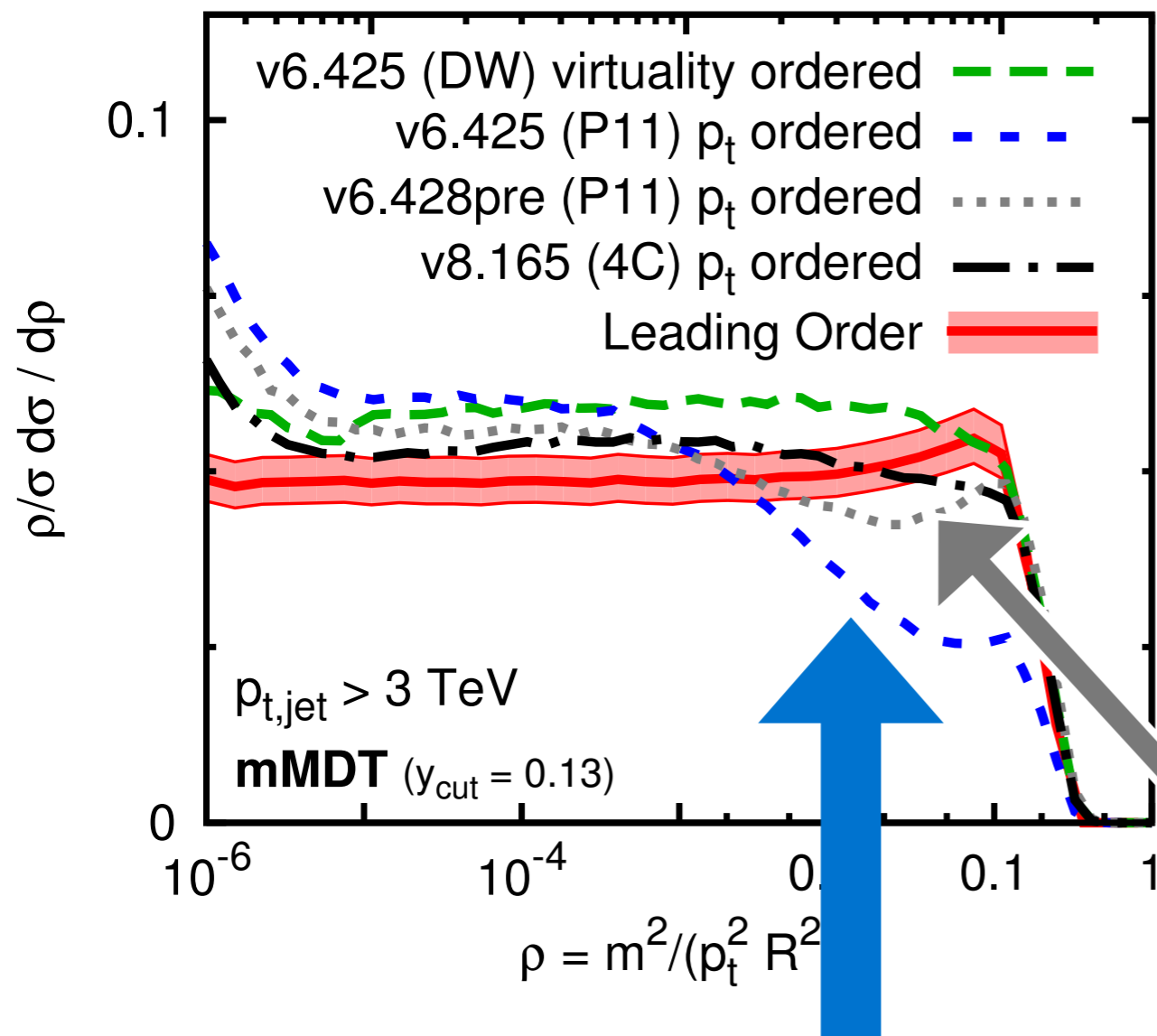
Issue found in Pythia 6 p_t -ordered shower → promptly identified and fixed by Pythia authors!

mMDT: comparing many showers

LO v. Pythia showers (quark jets)

m [GeV], for $p_t = 3$ TeV, $R = 1$

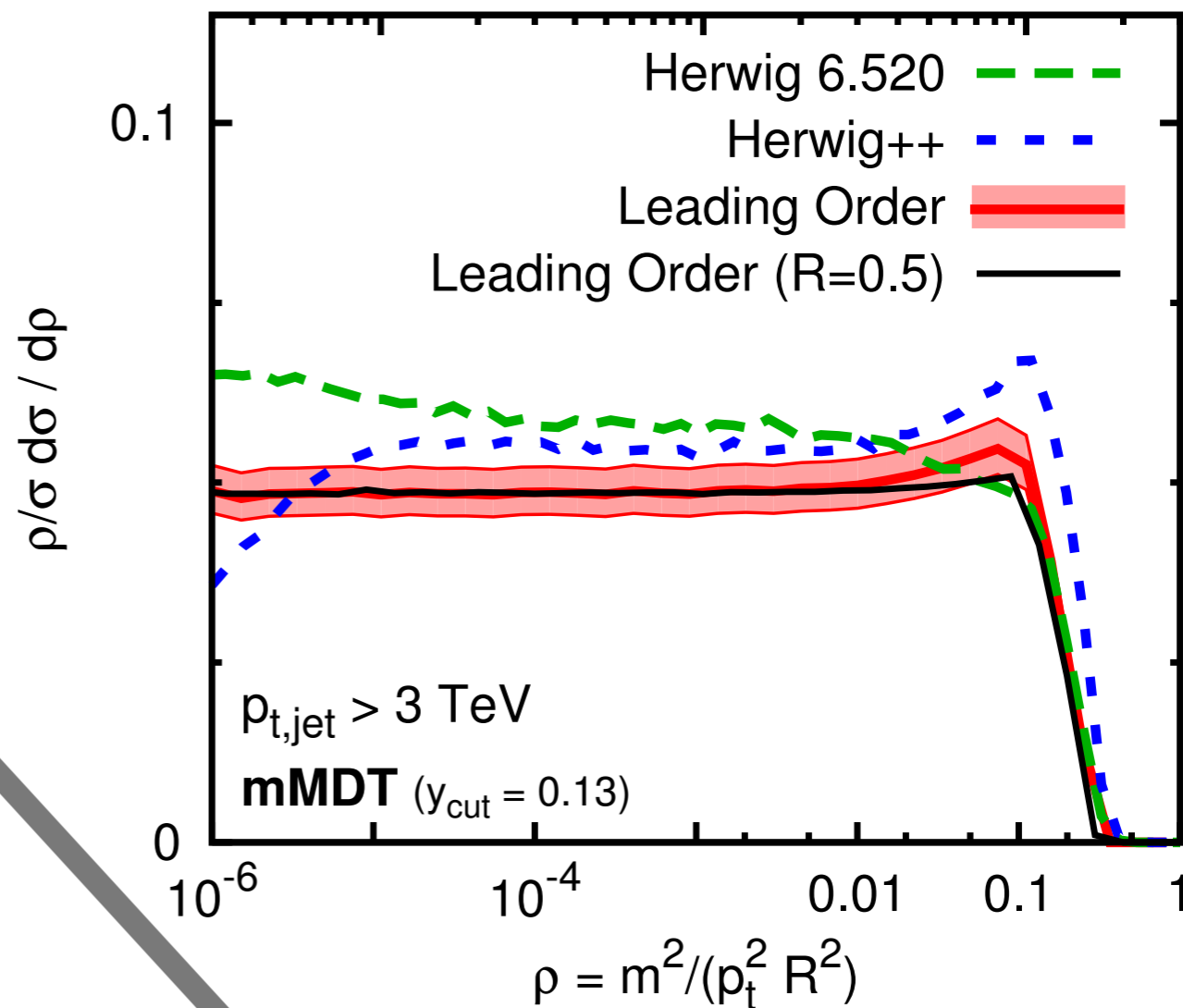
10 100 1000



LO v. Herwig showers (quark jets)

m [GeV], for $p_t = 3$ TeV, $R = 1$

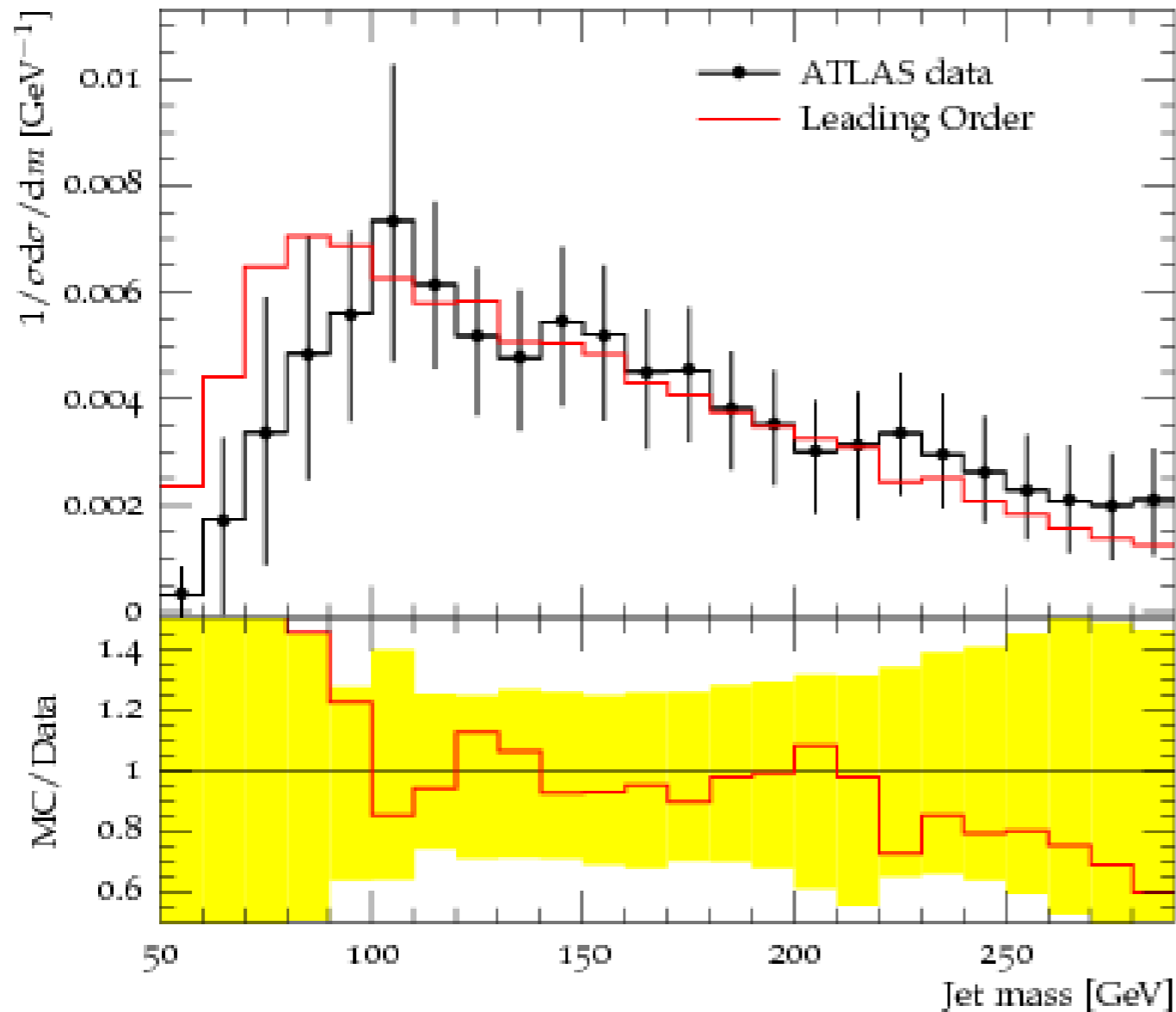
10 100 1000



Issue found in Pythia 6 p_t -ordered shower → promptly identified and fixed by Pythia authors!

LO results (njet+Sherpa) ATLAS MDT 500 < pT < 600 GeV

Cambridge-Aachen filtered jets, R=1.2, 500 GeV < p_⊥ < 600 GeV



Since LO quite close to full resummation, you can try comparing LO directly to data.

Remarkable agreement!
[see backup for non-pert effects]

Dasgupta, Siodmok & Powling, in prep.

Looking beyond

mMDT has a single-logarithmic (pure collinear) distribution that's free of non-global logs

A generalisation is **Soft Drop**

Uncluster C/A jets as with mMDT, but stop only if

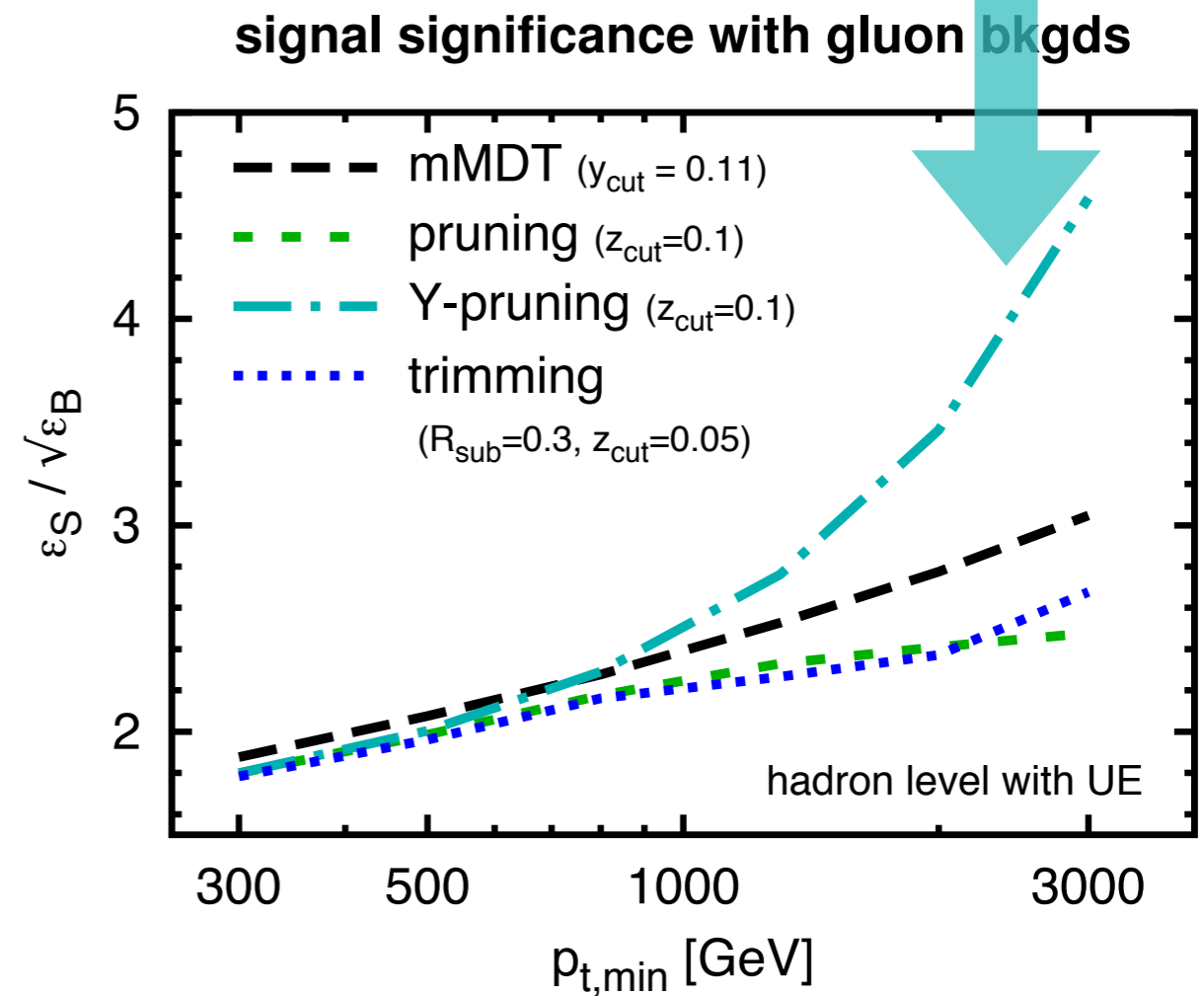
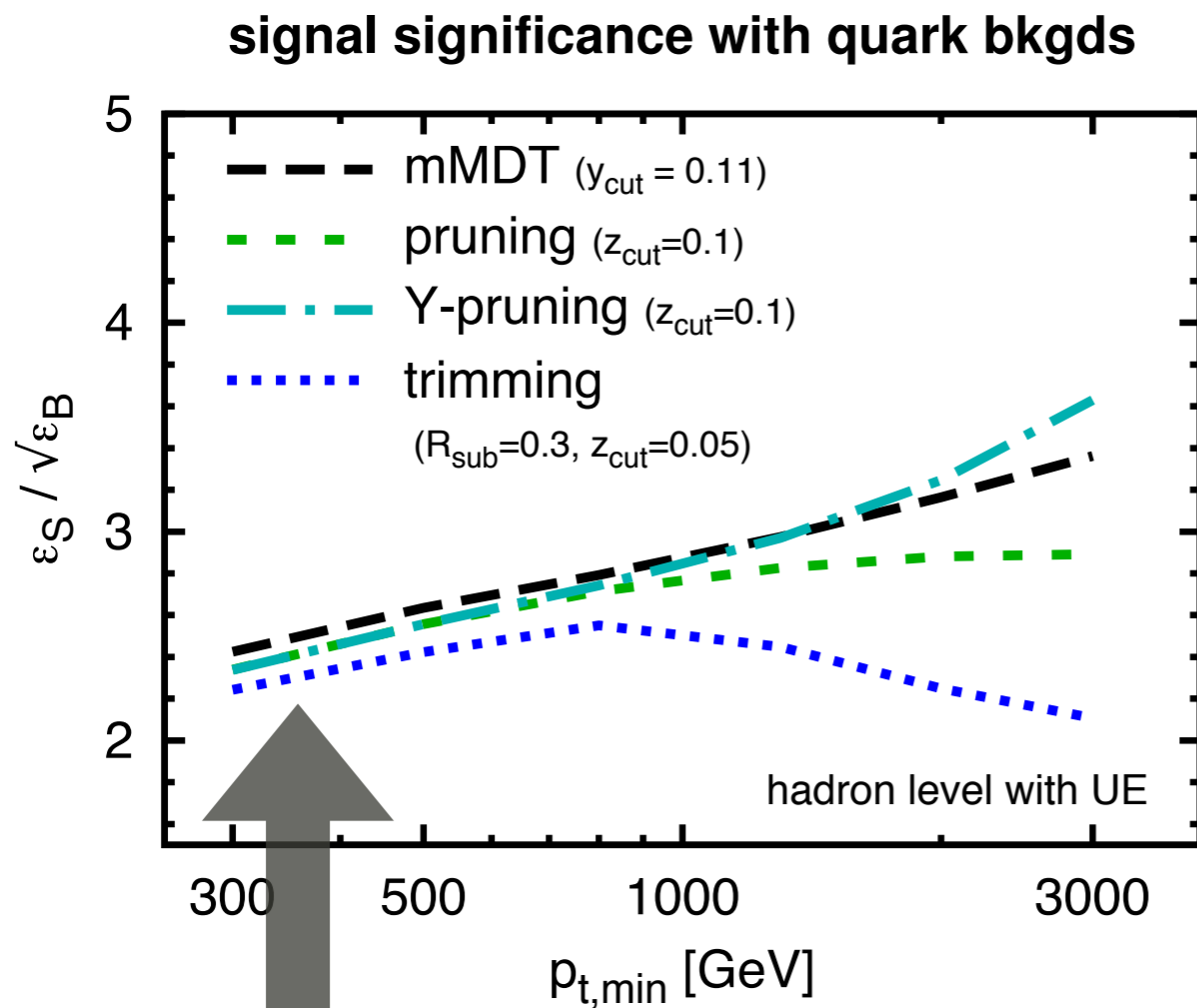
$$\frac{\min(p_{t1}, p_{t2})}{p_t} > z_{\text{cut}} \left(\frac{\Delta R_{12}}{R} \right)^\beta$$

For $\beta > 0$, get double-log distⁿ without NG logs
[mMDT corresponds to $\beta = 1$]

Larkoski, Marzani, Soyez, Thaler '14

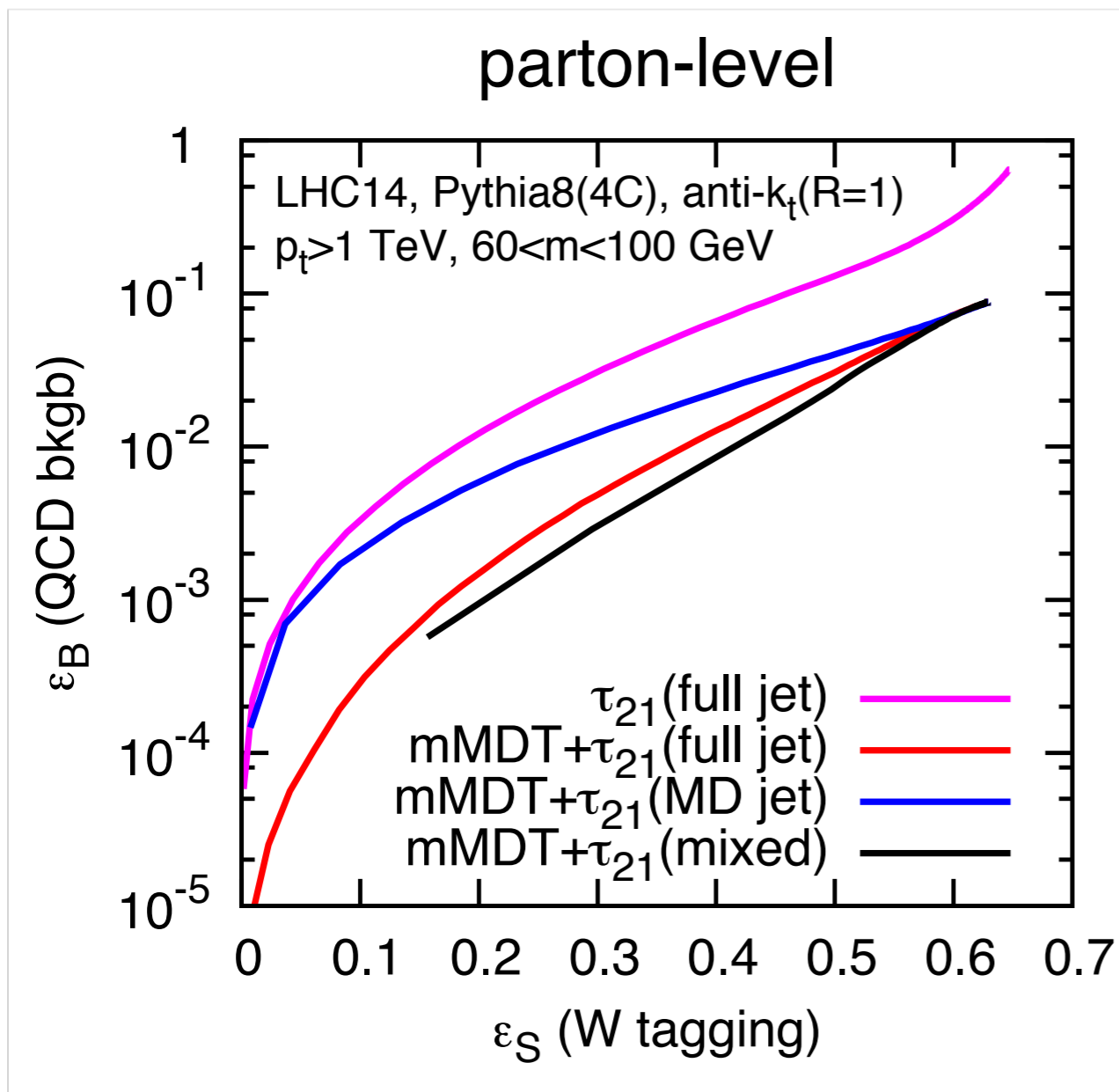
Performance for finding signals (S/\sqrt{B})

At high p_t , substantial gains from new Y-pruning
(probably just indicative of potential for doing better)



At low p_t (moderate m/p_t), all taggers quite similar

Combining variables



Experiments often combine [trimming/pruning/MDT/etc.] with a shape cut, typically N-subjettiness,

$$\tau_{21} = \tau_2 / \tau_1$$

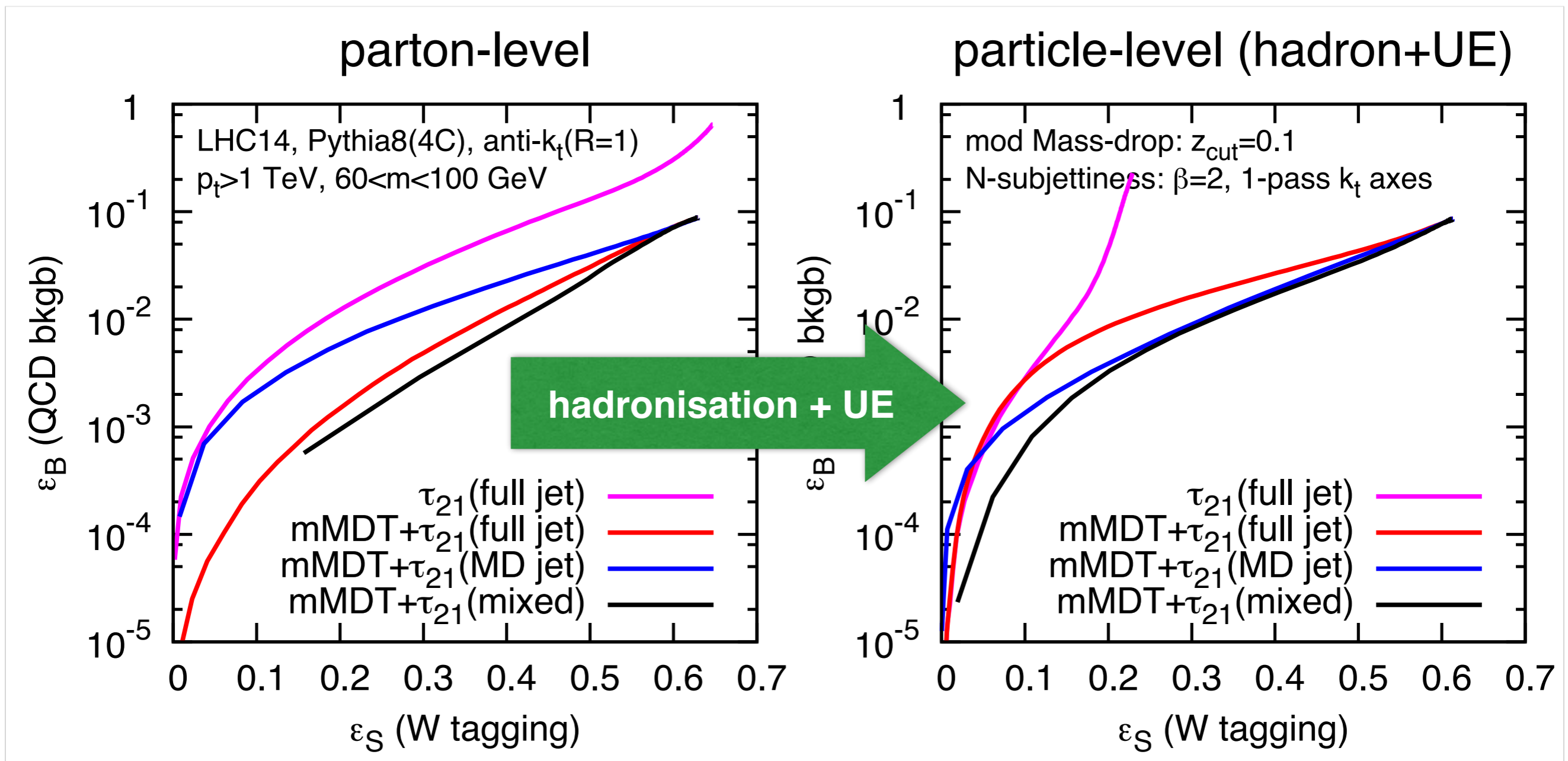
Next: understand τ_{21} .

Qu.: apply before or after MMDT?

Prelim. answer: take τ_2 from full jet, τ_1 from mMDT jet

Work in progress, Dasgupta, GPS, Soyez & Sarem-Schunk

But: non-pert effects change picture



Work in progress, Dasgupta, GPS, Soyez & Sarem-Schunk

- Taggers may be quite simple to write, but potentially involved to understand.
- Contrast this with p_t cuts for standard jet analyses – (mostly) simple
- Still, many taggers/groomers are within calculational reach.
- Calculations help put the field on solid ground & potentially open road to new, better tools

Summary table

	highest logs	transition(s)	Sudakov peak	NGLs
plain mass	$\alpha_s^n L^{2n}$	—	$L \simeq 1/\sqrt{\bar{\alpha}_s}$	yes
trimming	$\alpha_s^n L^{2n}$	$z_{\text{cut}}, r^2 z_{\text{cut}}$	$L \simeq 1/\sqrt{\bar{\alpha}_s} - 2 \ln r$	yes
pruning	$\alpha_s^n L^{2n}$	$z_{\text{cut}}, z_{\text{cut}}^2$	$L \simeq 2.3/\sqrt{\bar{\alpha}_s}$	yes
MDT	$\alpha_s^n L^{2n-1}$	$y_{\text{cut}}, \frac{1}{4}y_{\text{cut}}^2, y_{\text{cut}}^3$	—	yes
Y-pruning	$\alpha_s^n L^{2n-1}$	z_{cut}	(Sudakov tail)	yes
mMDT	$\alpha_s^n L^n$	y_{cut}	—	no

NEW

Special: only single logarithms ($L = \ln \rho$)
 → more accurately calculable

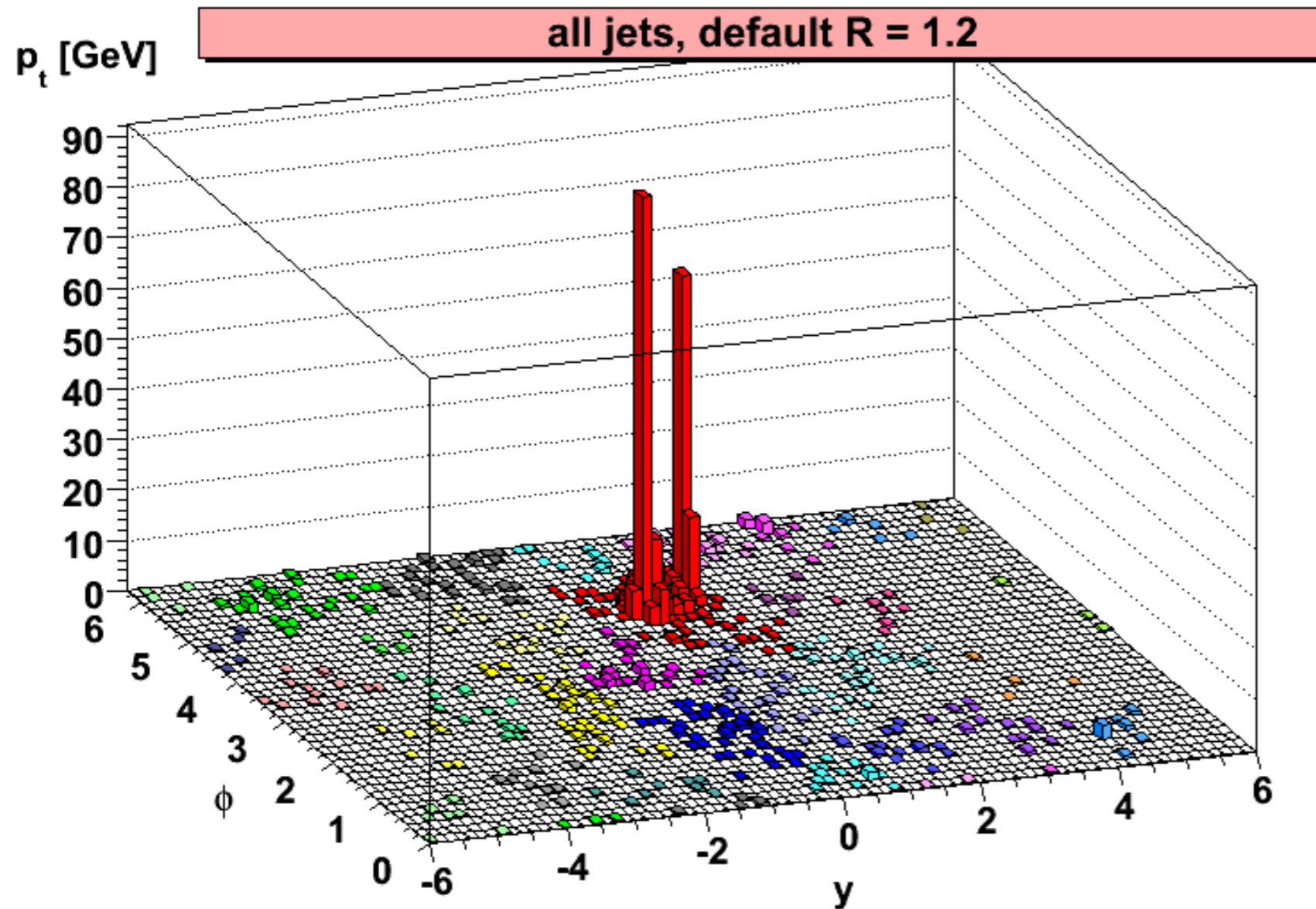
Special: better exploits signal/bkgd differences

EXTRAS

$pp \rightarrow ZH \rightarrow \nu\bar{\nu}b\bar{b}$, @14 TeV, $m_H = 115$ GeV

SIGNAL

Herwig 6.510 + Jimmy 4.31 + FastJet 2.3



Zbb BACKGROUND

Cluster event, C/A, R=1.2

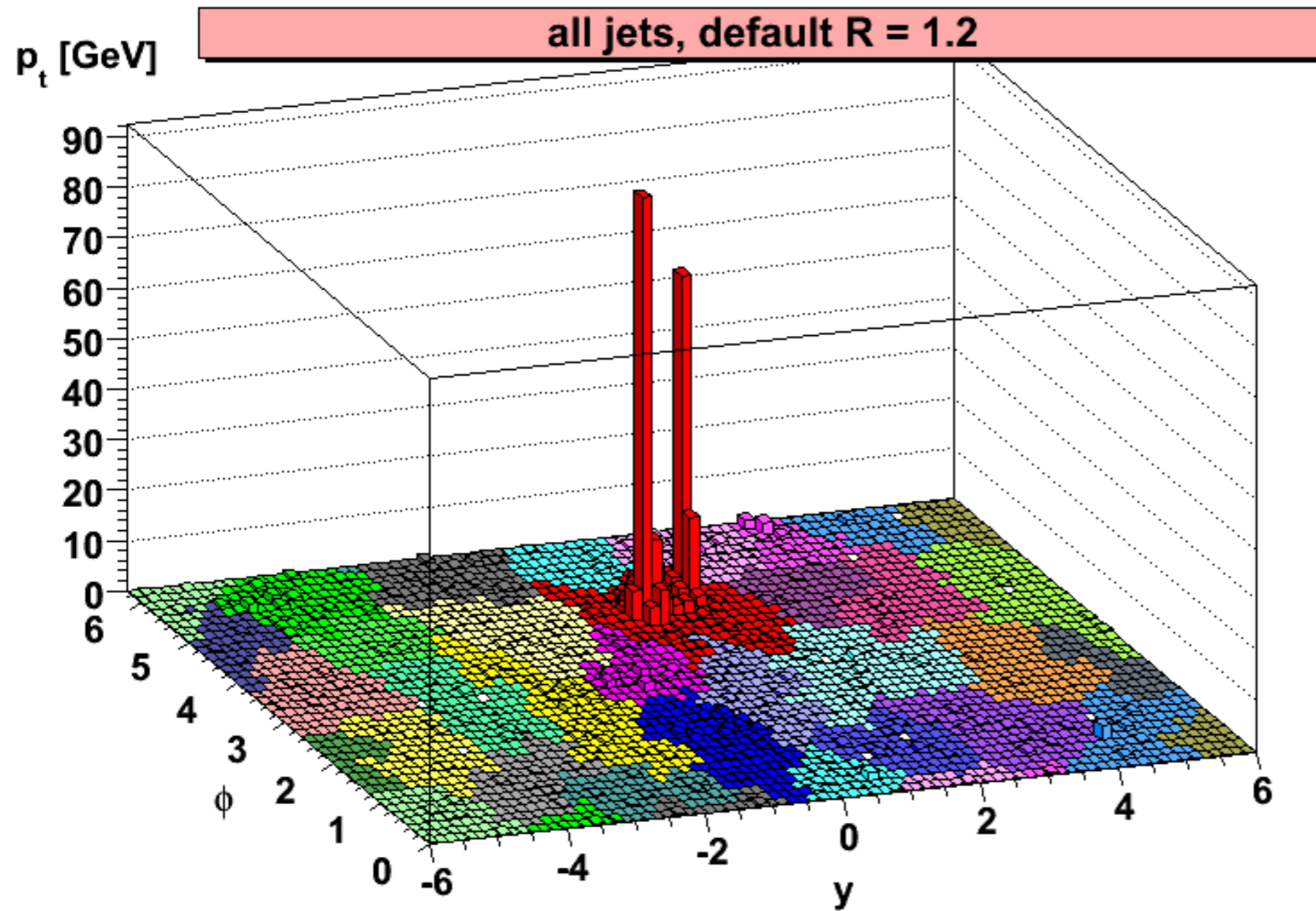
Butterworth, Davison, Rubin & GPS '08

arbitrary norm

$pp \rightarrow ZH \rightarrow \nu\bar{\nu}b\bar{b}$, @14 TeV, $m_H = 115$ GeV

SIGNAL

Herwig 6.510 + Jimmy 4.31 + FastJet 2.3



Zbb BACKGROUND

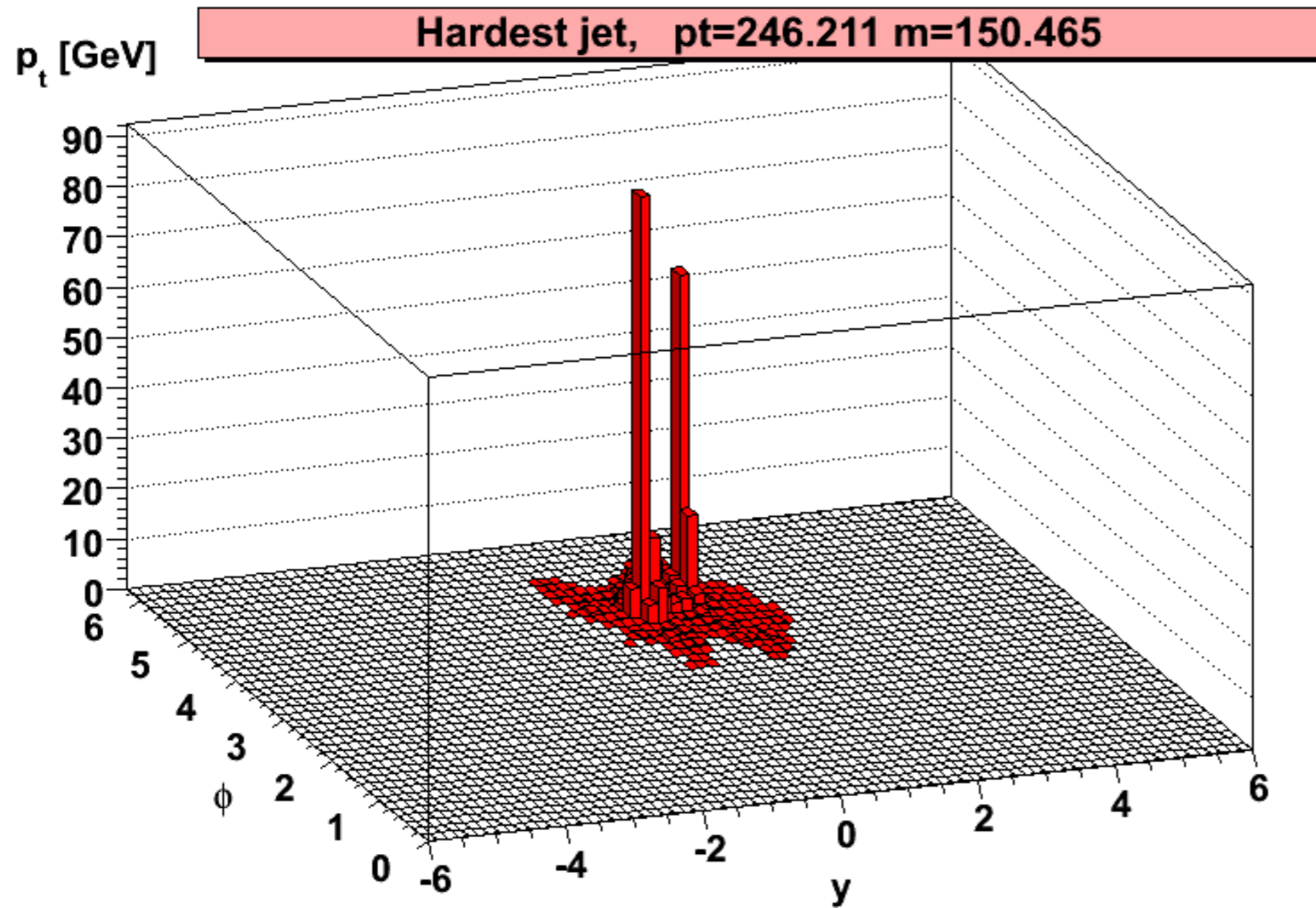
Fill it in, \rightarrow show jets more clearly

Butterworth, Davison, Rubin & GPS '08

arbitrary norm
68

$$pp \rightarrow ZH \rightarrow \nu\bar{\nu}b\bar{b}, @14\text{TeV}, m_H = 115\text{ GeV}$$

Herwig 6.510 + Jimmy 4.31 + FastJet 2.3

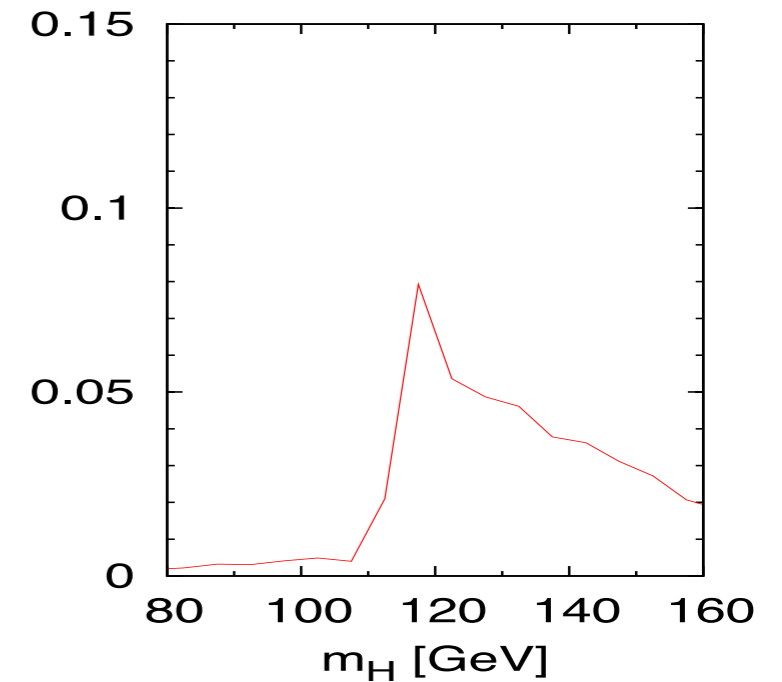


Consider hardest jet, $m = 150$ GeV

Butterworth, Davison, Rubin & GPS '08

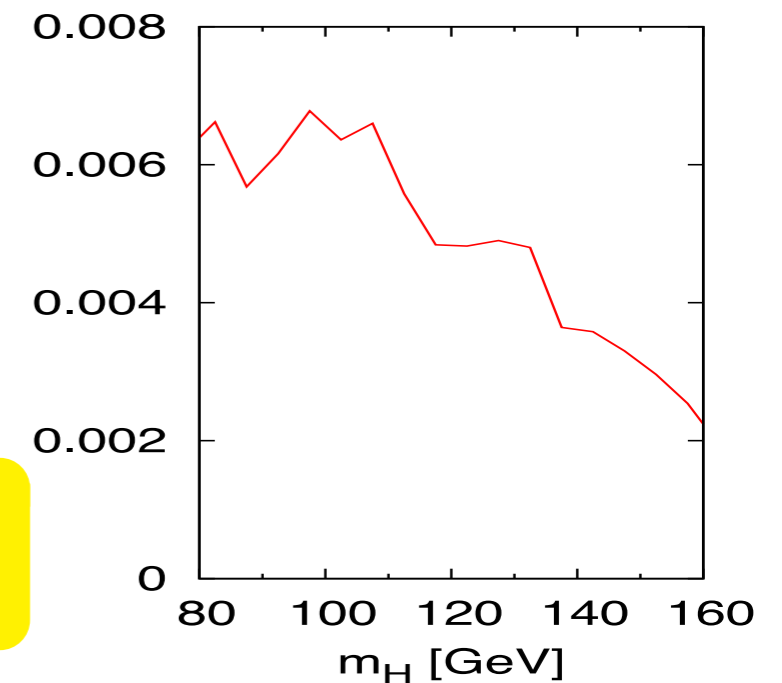
SIGNAL

$200 < p_{tZ} < 250$ GeV



Zbb BACKGROUND

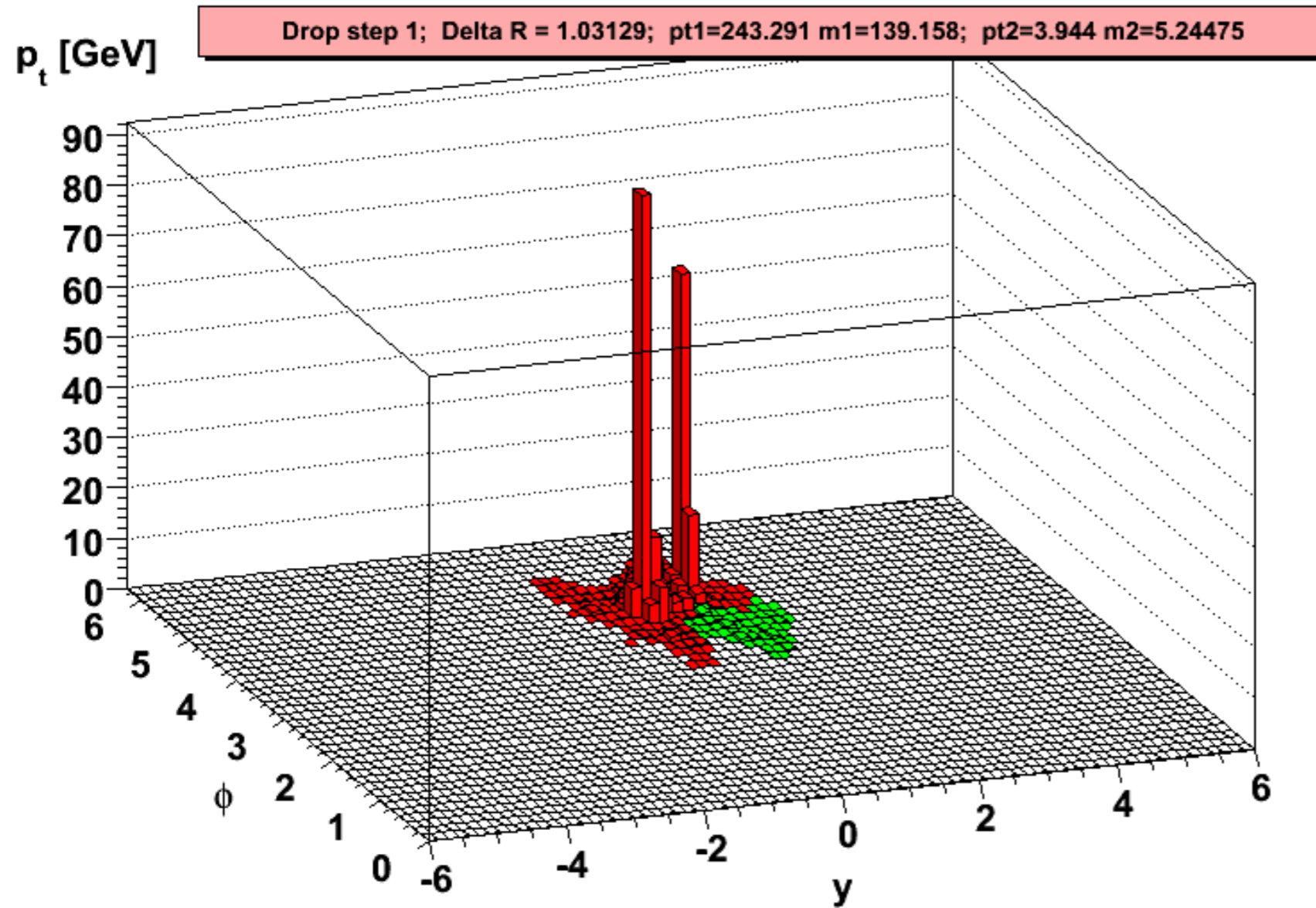
$200 < p_{tZ} < 250$ GeV



arbitrary norm.
69

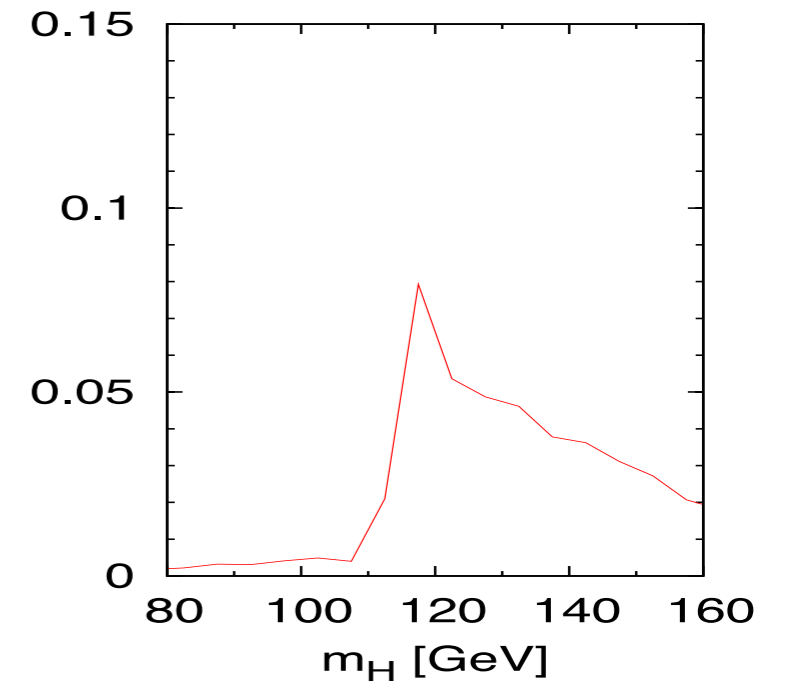
$pp \rightarrow ZH \rightarrow \nu\bar{\nu}b\bar{b}$, @14 TeV, $m_H = 115$ GeV

Herwig 6.510 + Jimmy 4.31 + FastJet 2.3



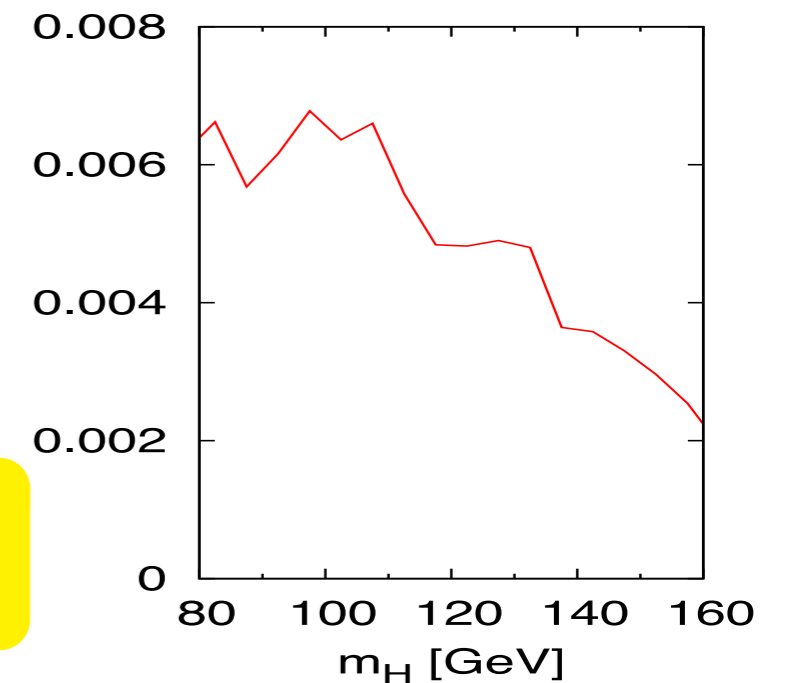
SIGNAL

$200 < p_{tZ} < 250$ GeV



Zbb BACKGROUND

$200 < p_{tZ} < 250$ GeV



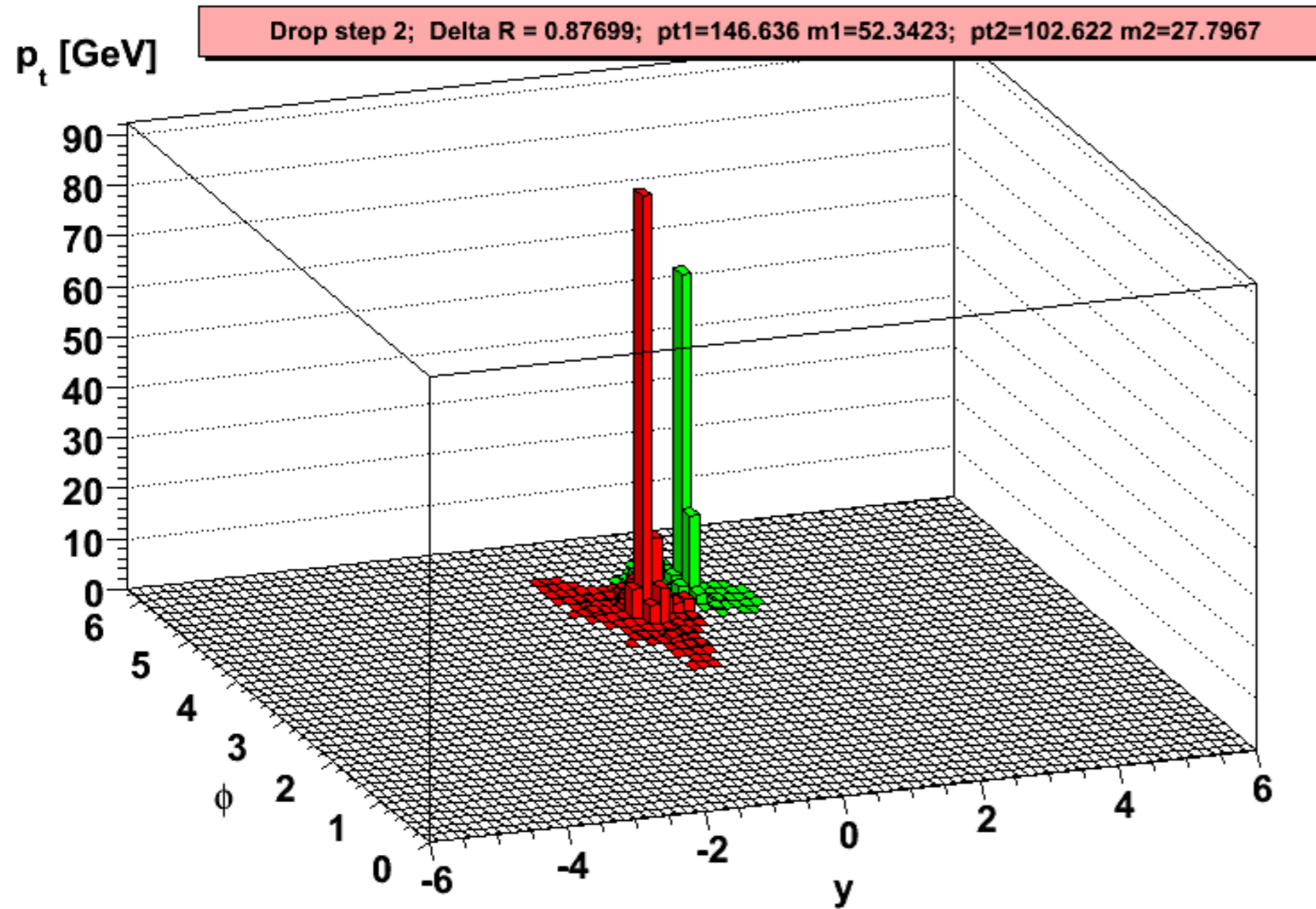
split: $m = 150$ GeV, $\frac{\max(m_1, m_2)}{m} = 0.92 \rightarrow$ repeat

Butterworth, Davison, Rubin & GPS '08

arbitrary norm.
70

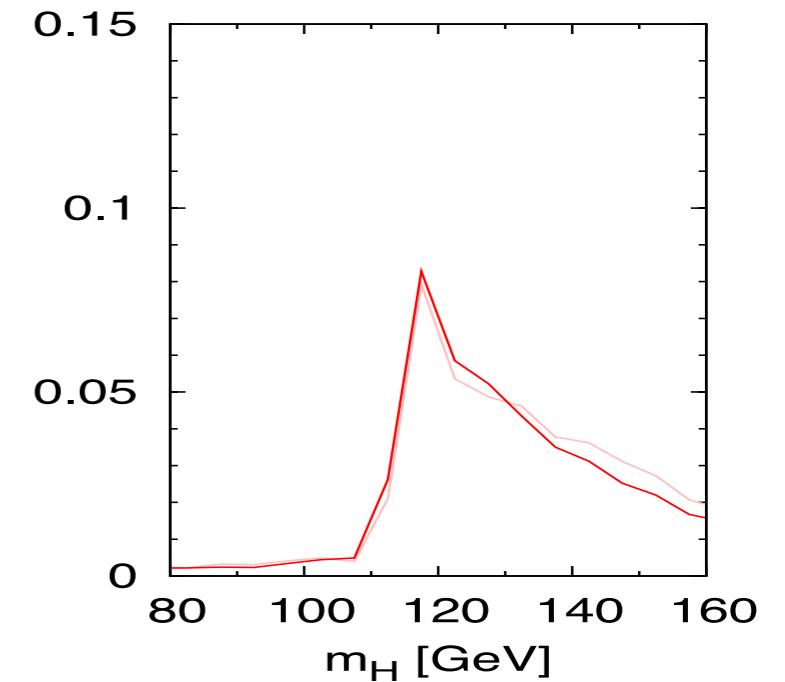
$pp \rightarrow ZH \rightarrow \nu\bar{\nu}b\bar{b}$, @14 TeV, $m_H = 115$ GeV

Herwig 6.510 + Jimmy 4.31 + FastJet 2.3



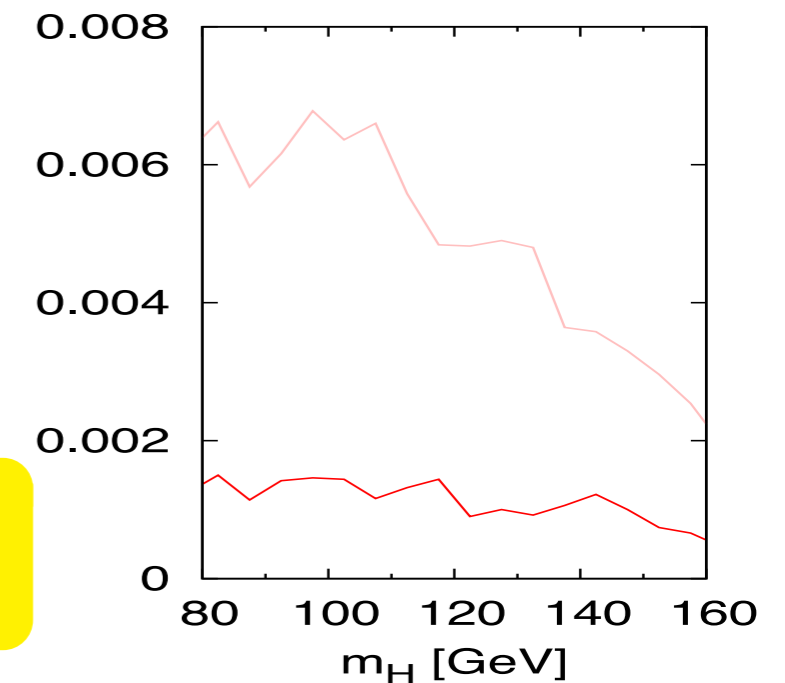
SIGNAL

$200 < p_{tZ} < 250$ GeV



Zbb BACKGROUND

$200 < p_{tZ} < 250$ GeV



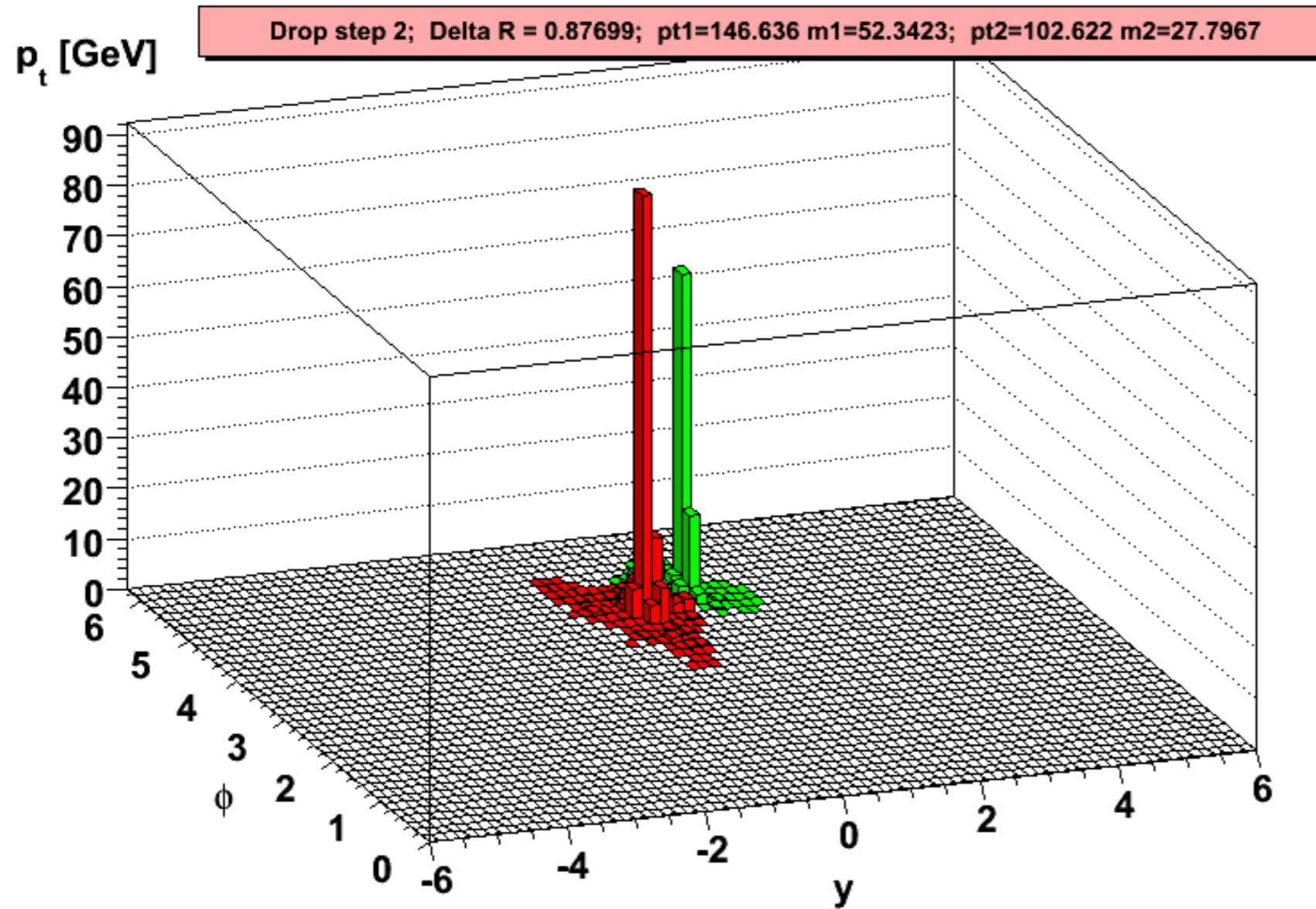
split: $m = 139$ GeV, $\frac{\max(m_1, m_2)}{m} = 0.37 \rightarrow$ mass drop

Butterworth, Davison, Rubin & GPS '08

arbitrary norm₇₁

$pp \rightarrow ZH \rightarrow \nu\bar{\nu}b\bar{b}$, @14 TeV, $m_H = 115$ GeV

Herwig 6.510 + Jimmy 4.31 + FastJet 2.3

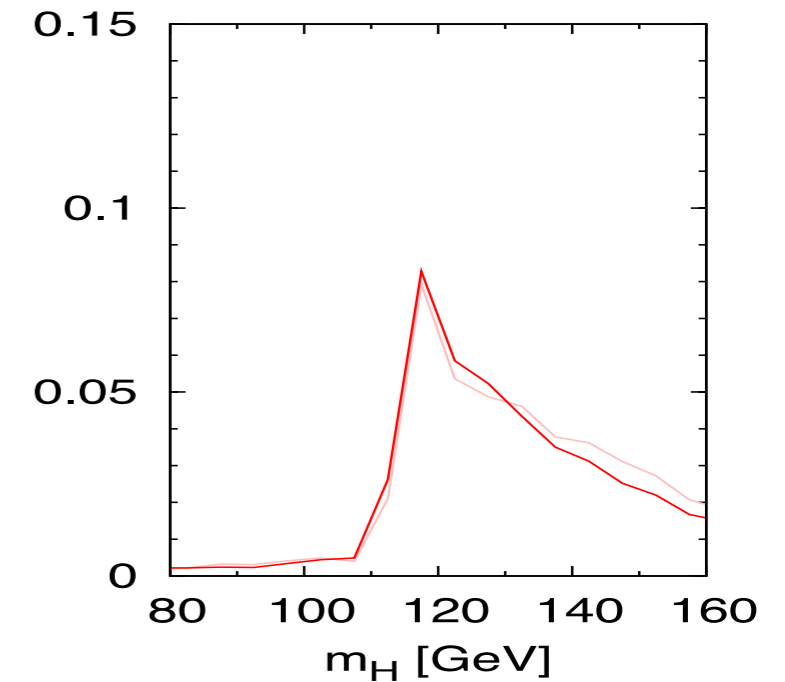


check: $y_{12} \simeq \frac{p_{t2}}{p_{t1}} \simeq 0.7 \rightarrow \text{OK} + 2 \text{ } b\text{-tags (anti-QCD)}$

Butterworth, Davison, Rubin & GPS '08

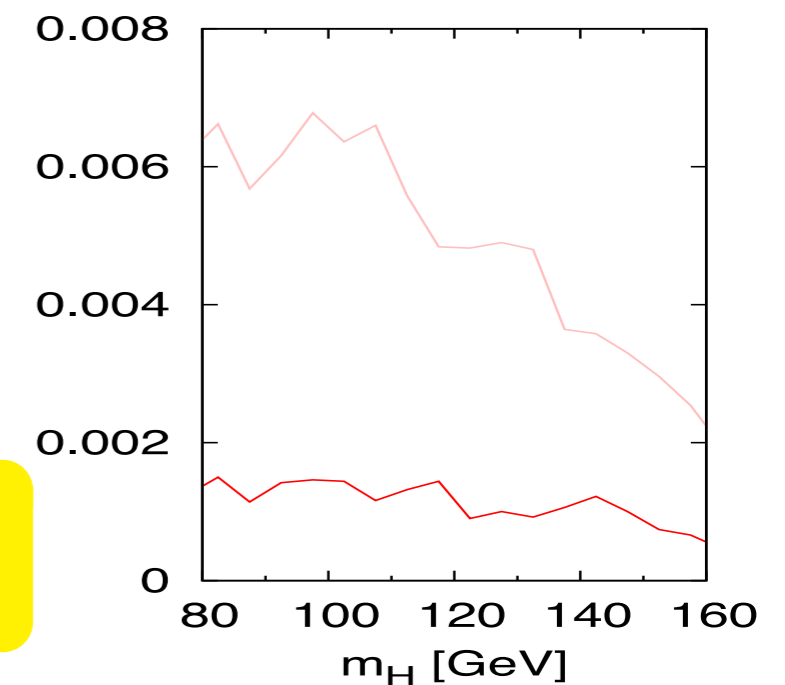
SIGNAL

$200 < p_{tZ} < 250$ GeV



Zbb BACKGROUND

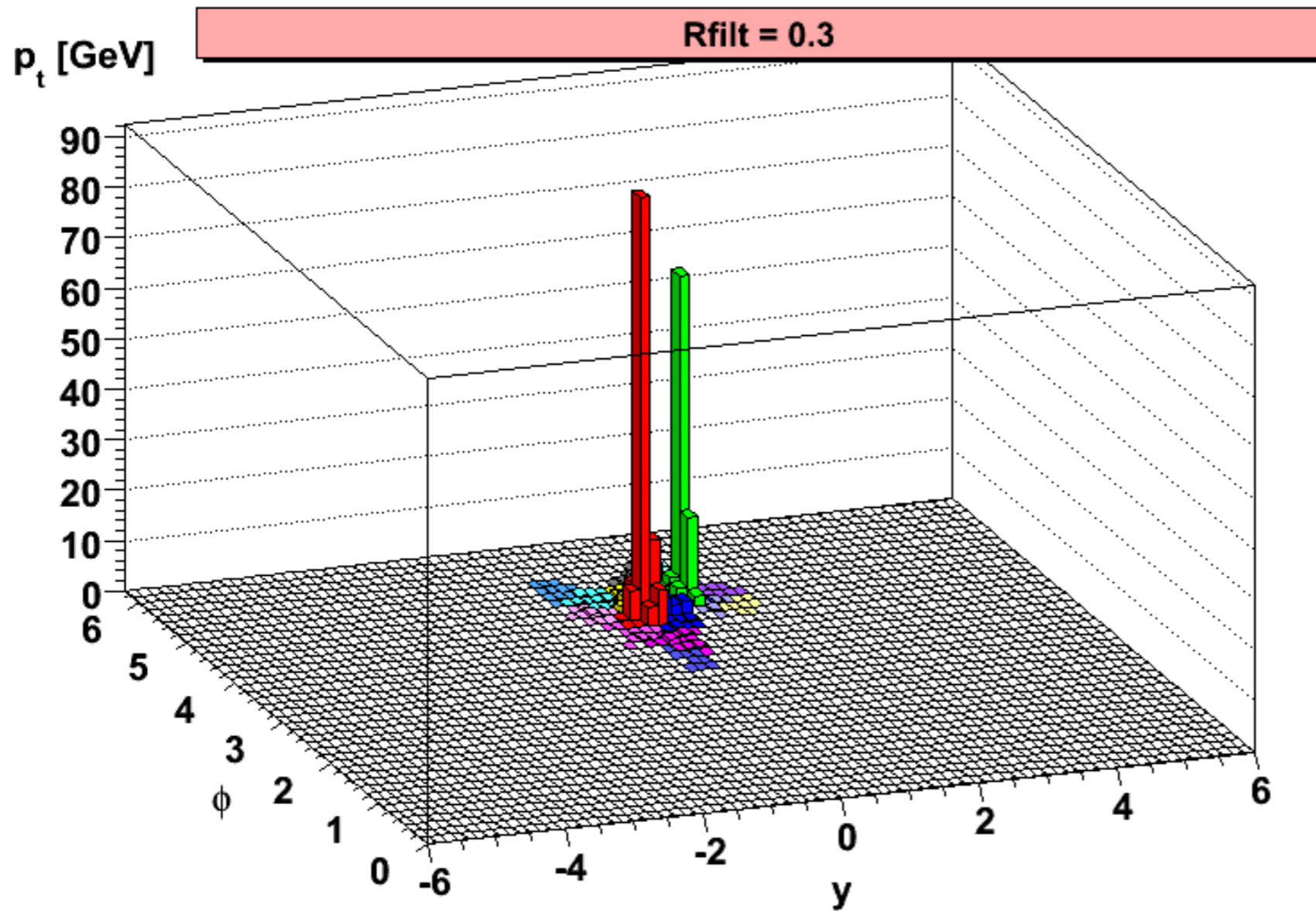
$200 < p_{tZ} < 250$ GeV



arbitrary norm₇₂

$pp \rightarrow ZH \rightarrow \nu\bar{\nu}b\bar{b}$, @14 TeV, $m_H = 115$ GeV

Herwig 6.510 + Jimmy 4.31 + FastJet 2.3

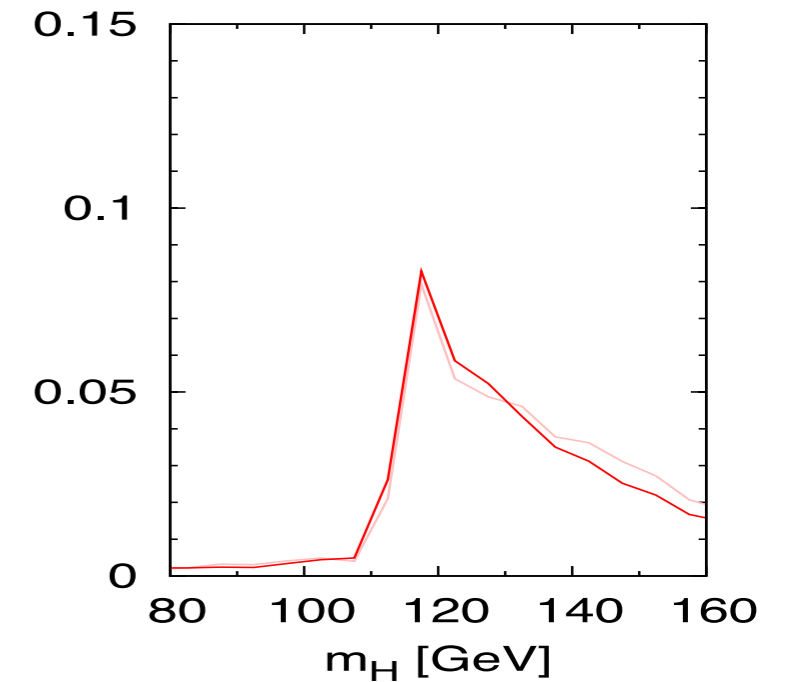


$R_{filt} = 0.3$

Butterworth, Davison, Rubin & GPS '08

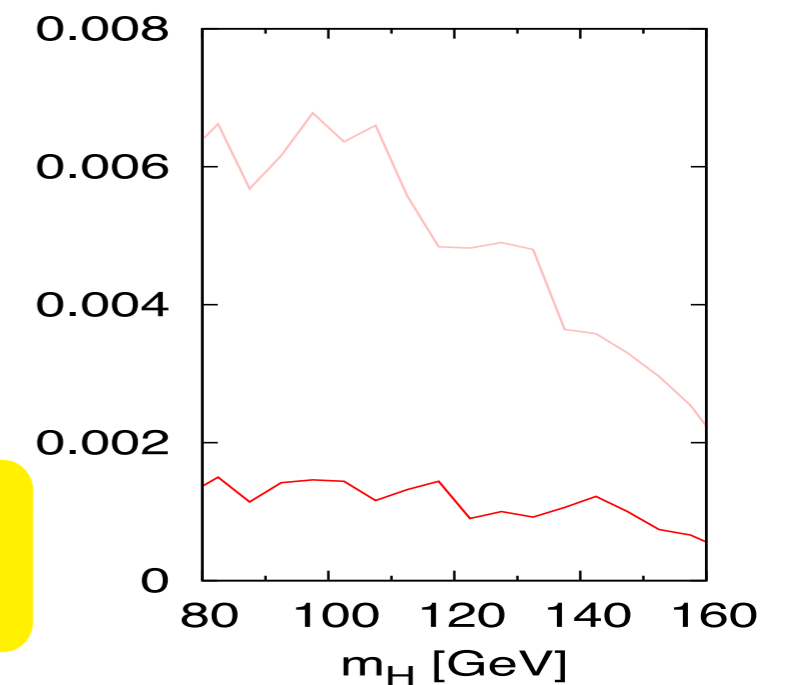
SIGNAL

$200 < p_{tZ} < 250$ GeV



Zbb BACKGROUND

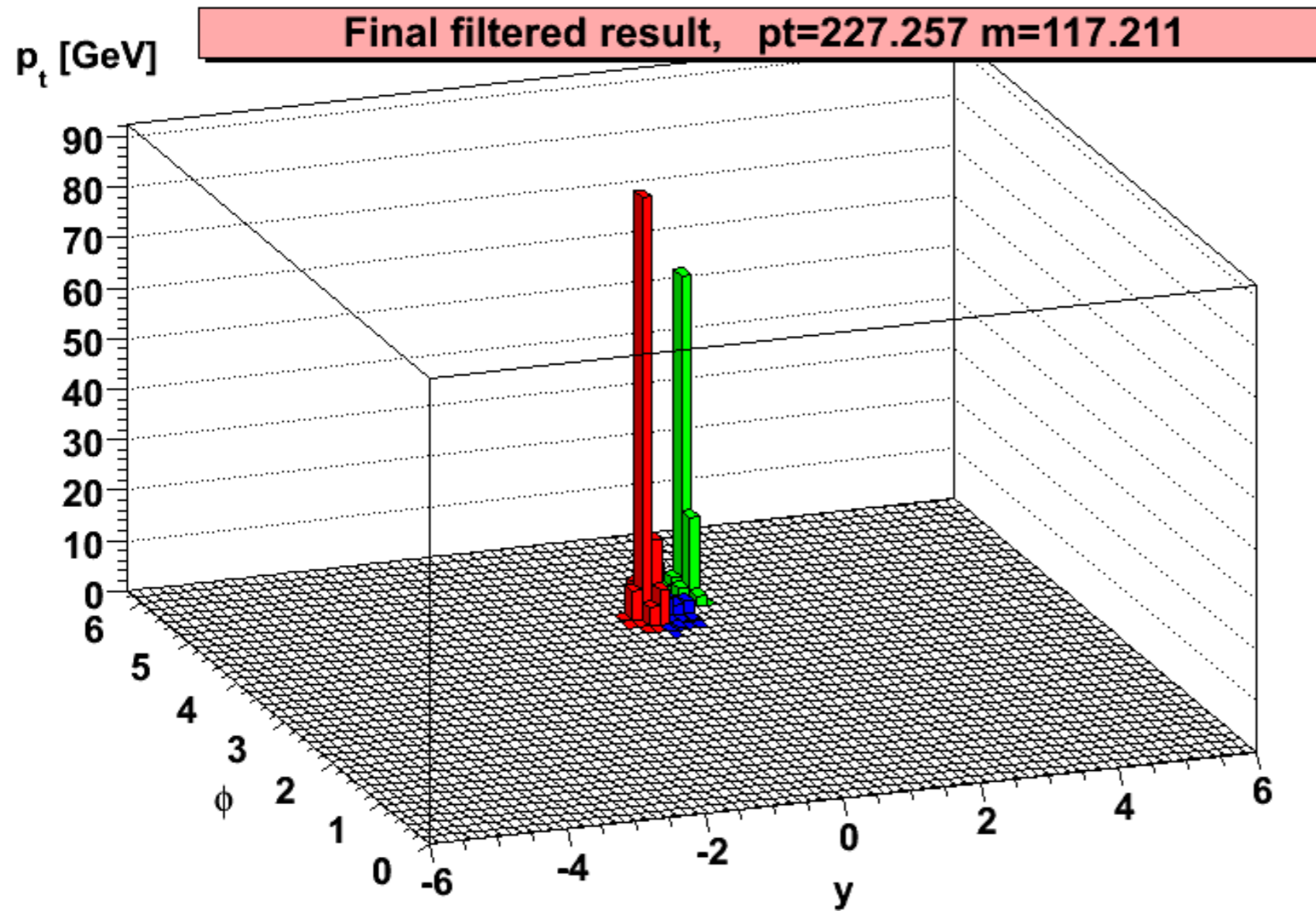
$200 < p_{tZ} < 250$ GeV



arbitrary norm.₇₃

$pp \rightarrow ZH \rightarrow \nu\bar{\nu}b\bar{b}$, @14 TeV, $m_H = 115$ GeV

Herwig 6.510 + Jimmy 4.31 + FastJet 2.3

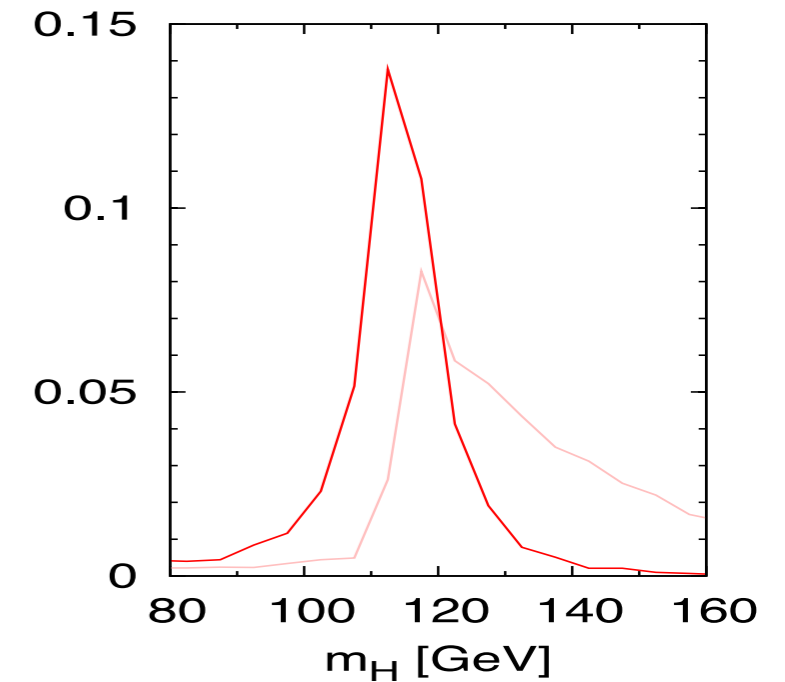


$R_{filt} = 0.3$: take 3 hardest, $m = 117$ GeV

Butterworth, Davison, Rubin & GPS '08

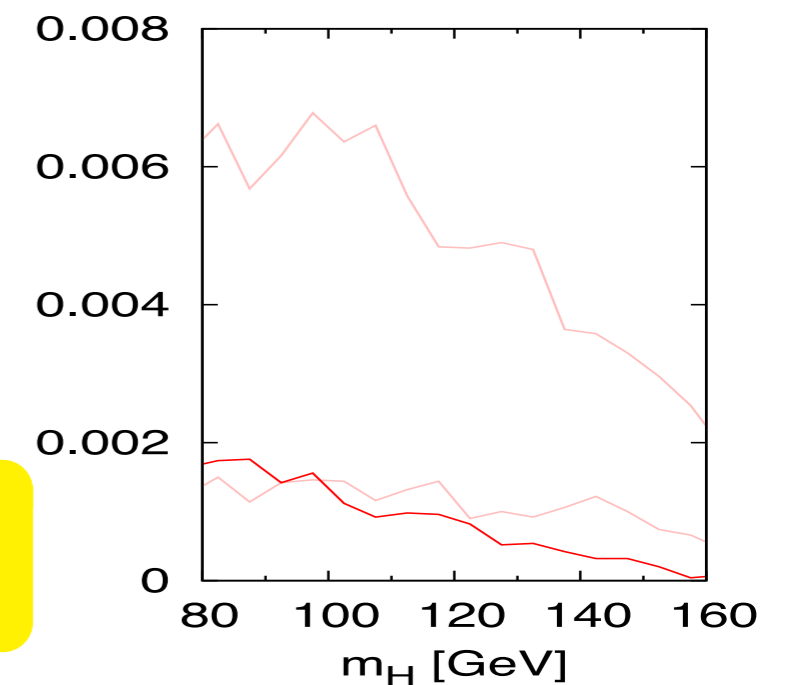
SIGNAL

$200 < p_{tZ} < 250$ GeV



Zbb BACKGROUND

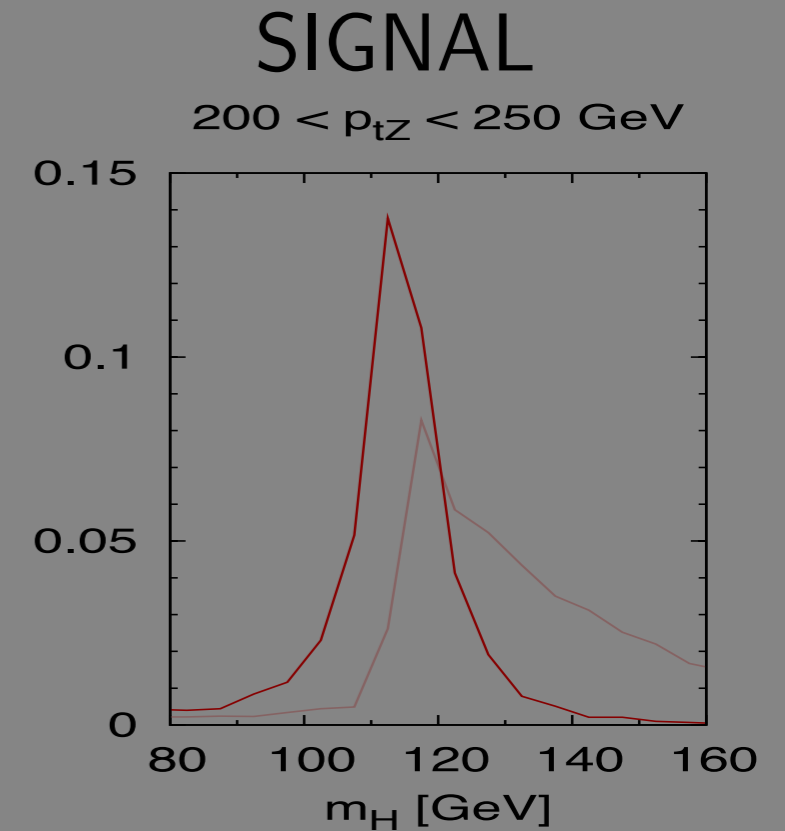
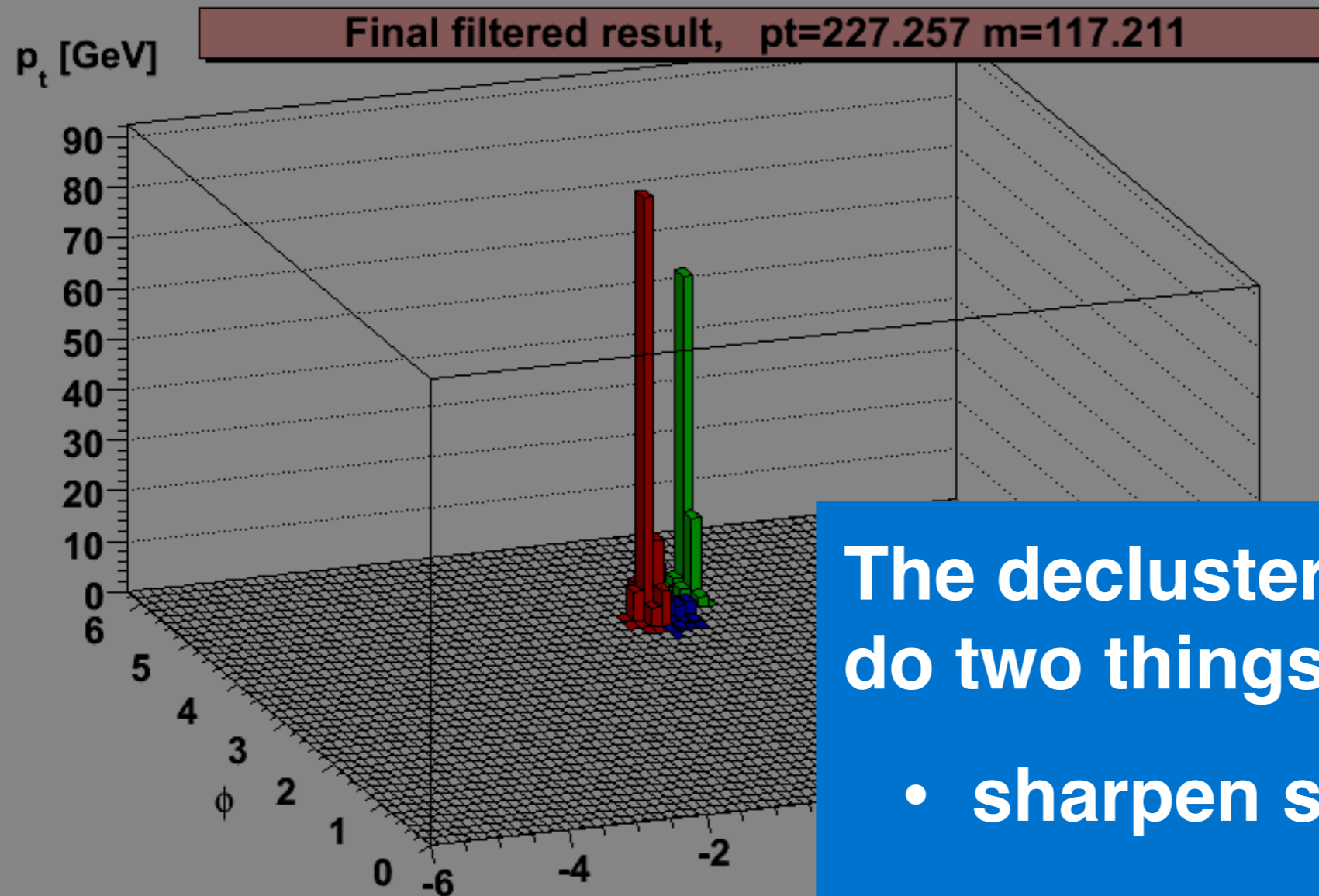
$200 < p_{tZ} < 250$ GeV



arbitrary norm₇₄

$$pp \rightarrow ZH \rightarrow \nu\bar{\nu}b\bar{b}, @14\text{ TeV}, m_H = 115\text{ GeV}$$

Herwig 6.510 + Jimmy 4.31 + FastJet 2.3



The declustering and cuts do two things

- sharpen signals
- reduce backgrounds

$R_{filt} = 0.3$: take 3 hardest, $m =$

Butterworth, Davison, Rubin & GPS '08

arbitrary norm.

What about
non-perturbative effects?

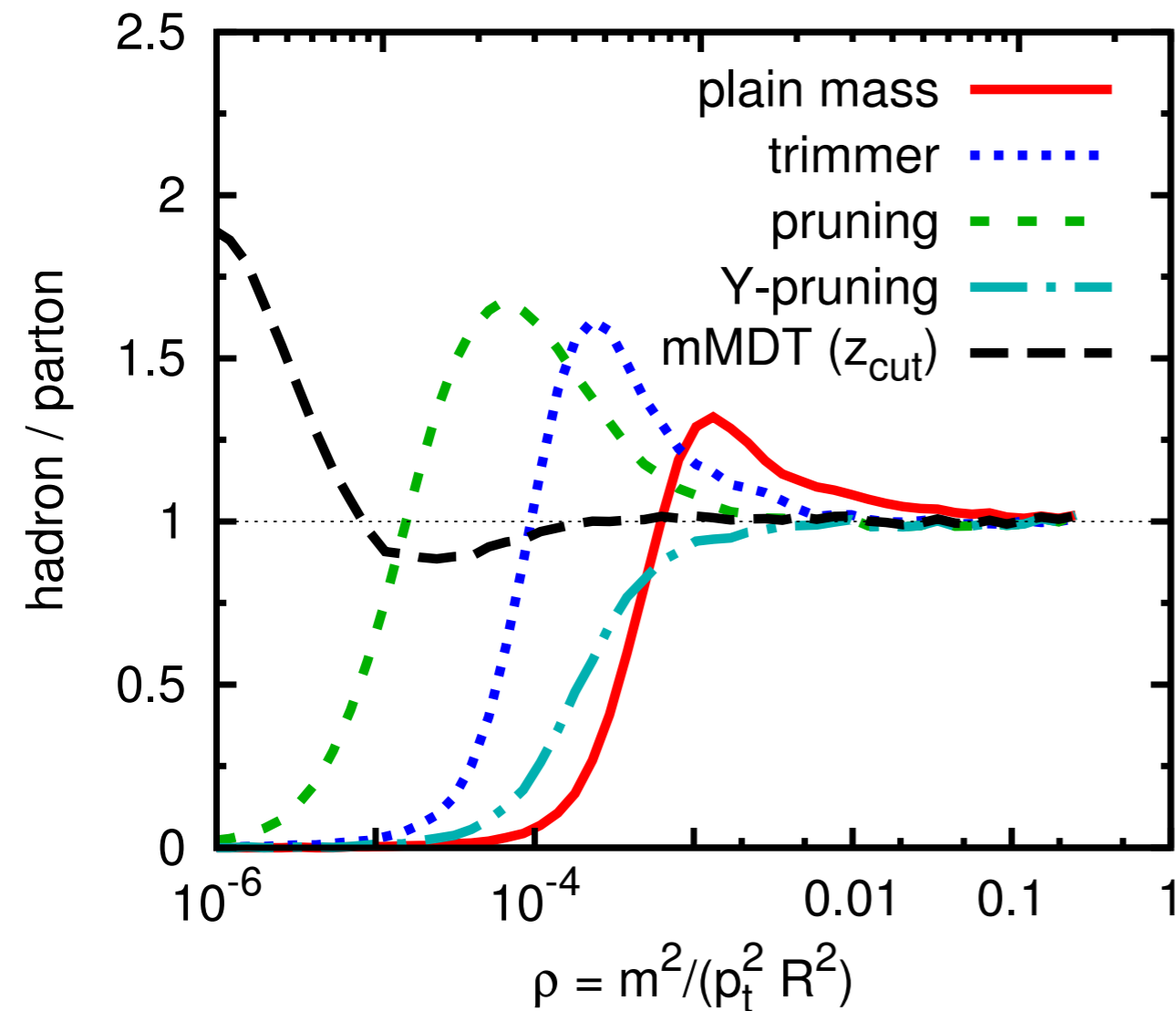
[on 3 TeV jets?!]

Hadronisation effects

hadronisation summary (quark jets)

m [GeV], for $p_t = 3$ TeV, $R = 1$

10 100 1000



Nearly all taggers have
large hadronisation
effects:

15 – 60%

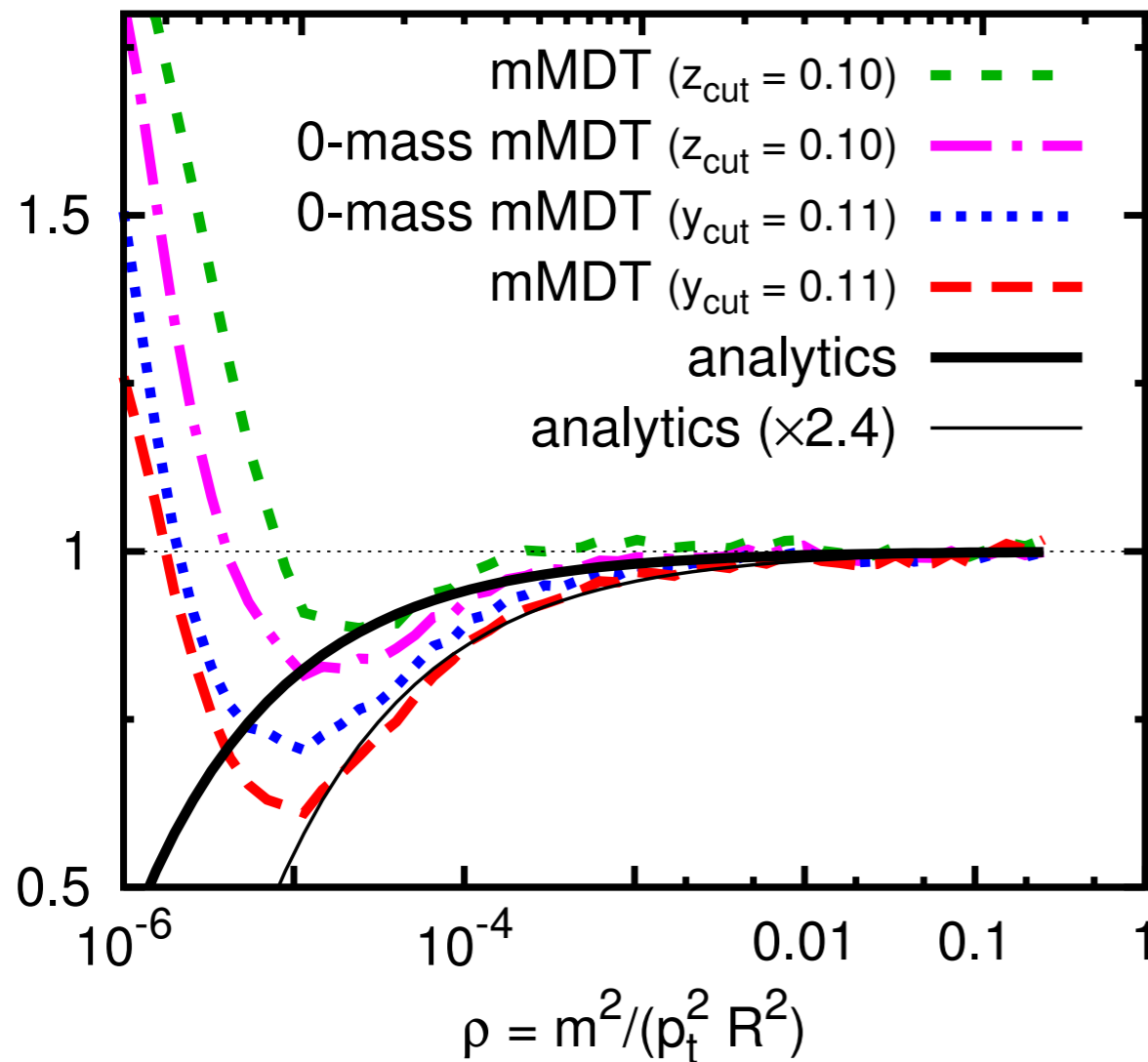
for $m = 30 - 100$ GeV

Hadronisation effects

hadronisation v. analytics (quark jets)

m [GeV], for $p_t = 3$ TeV, $R = 1$

10 100 1000



Exception is (m)MDT.

In some cases
just few % effect.

m -dependence of
hadronisation even
understood analytically!

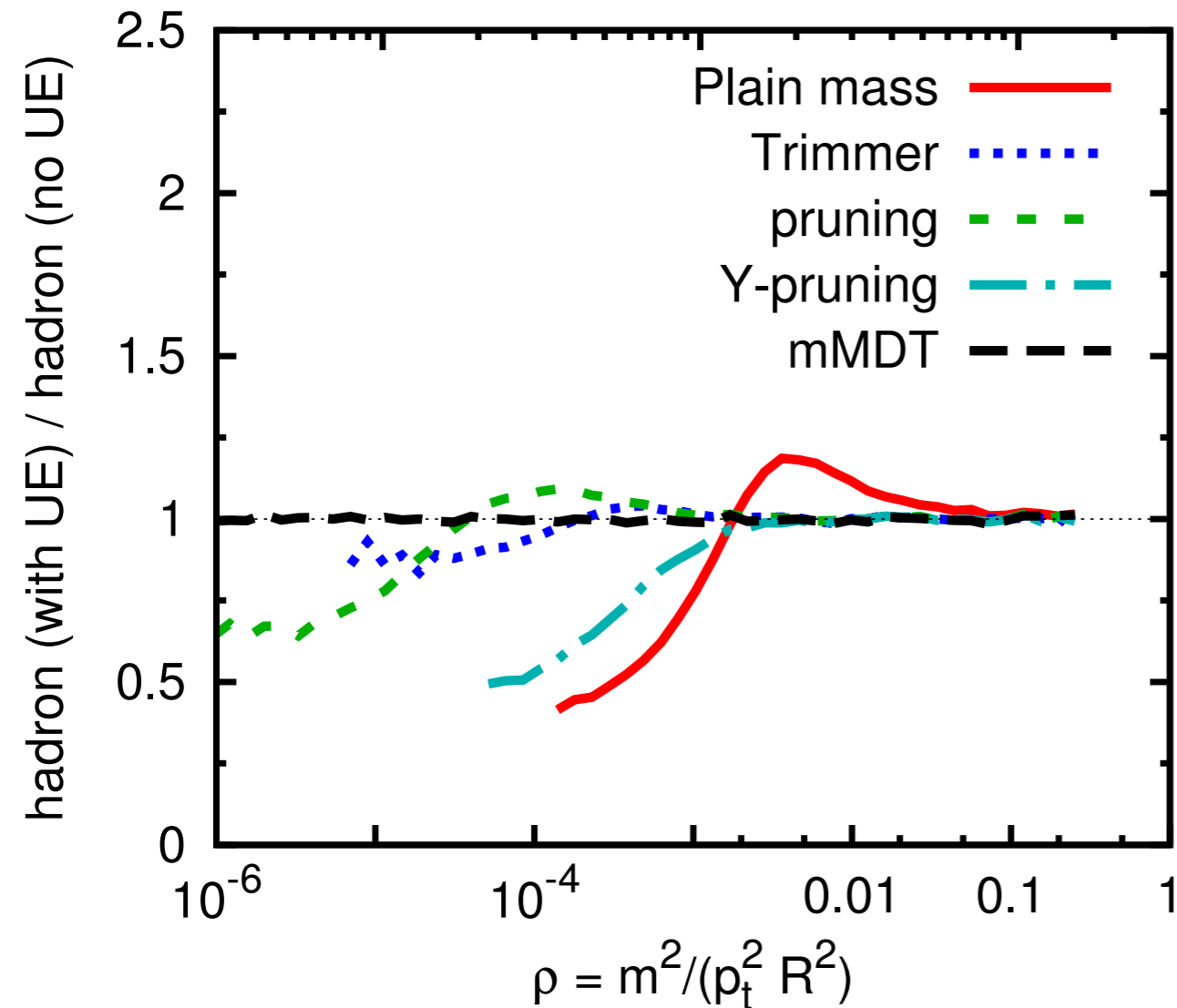
$$\frac{d\sigma}{dm}^{\text{hadron}} \approx \frac{d\sigma}{dm}^{\text{parton}} \left(1 - c \frac{\Lambda}{m} \right)$$

Underlying Event (UE)

UE summary (quark jets)

m [GeV], for $p_t = 3$ TeV, $R = 1$

10 100 1000



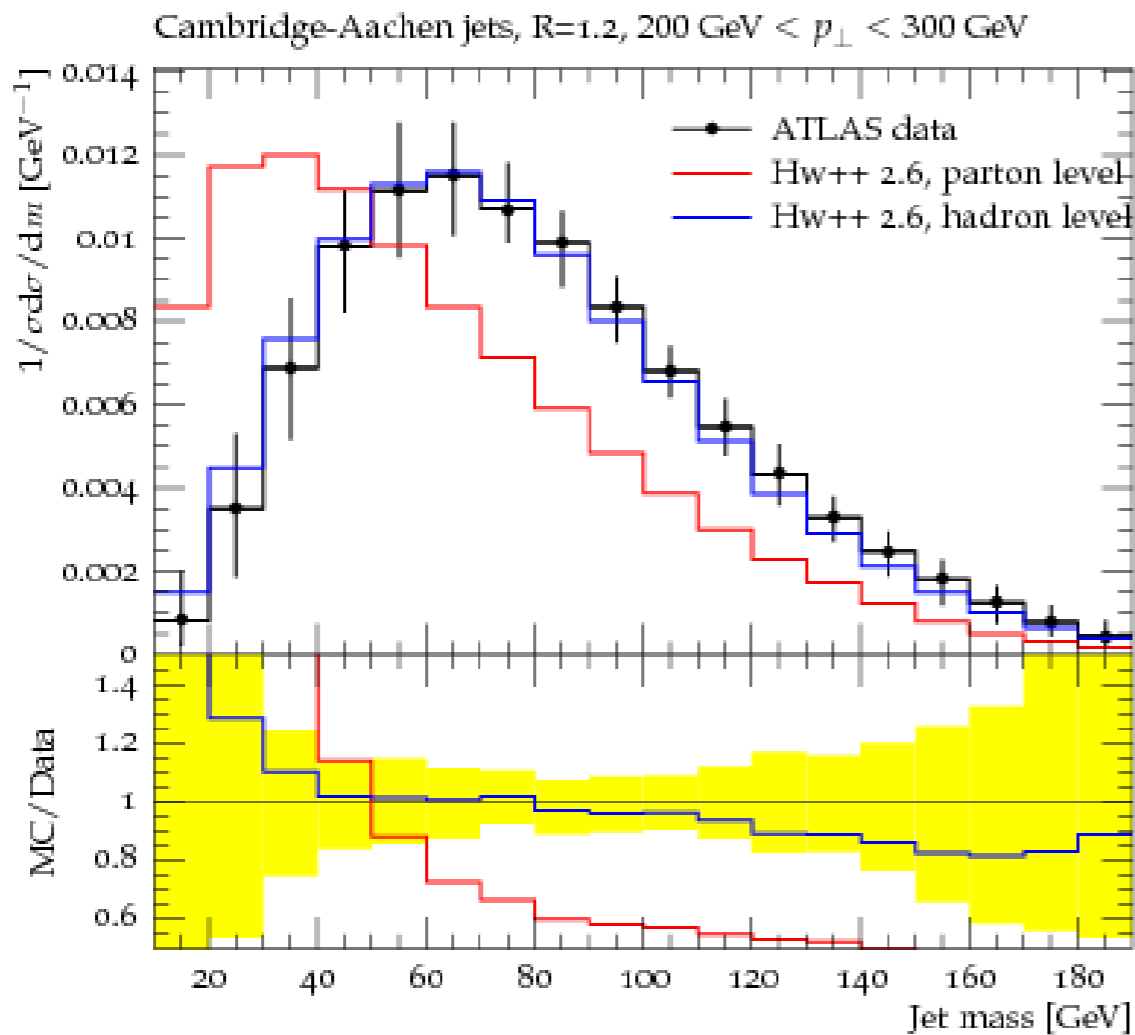
Underlying event impact
much reduced relative to
jet mass

Almost zero for mMDT
(this depends on jet p_t)

mMDT phenomenology

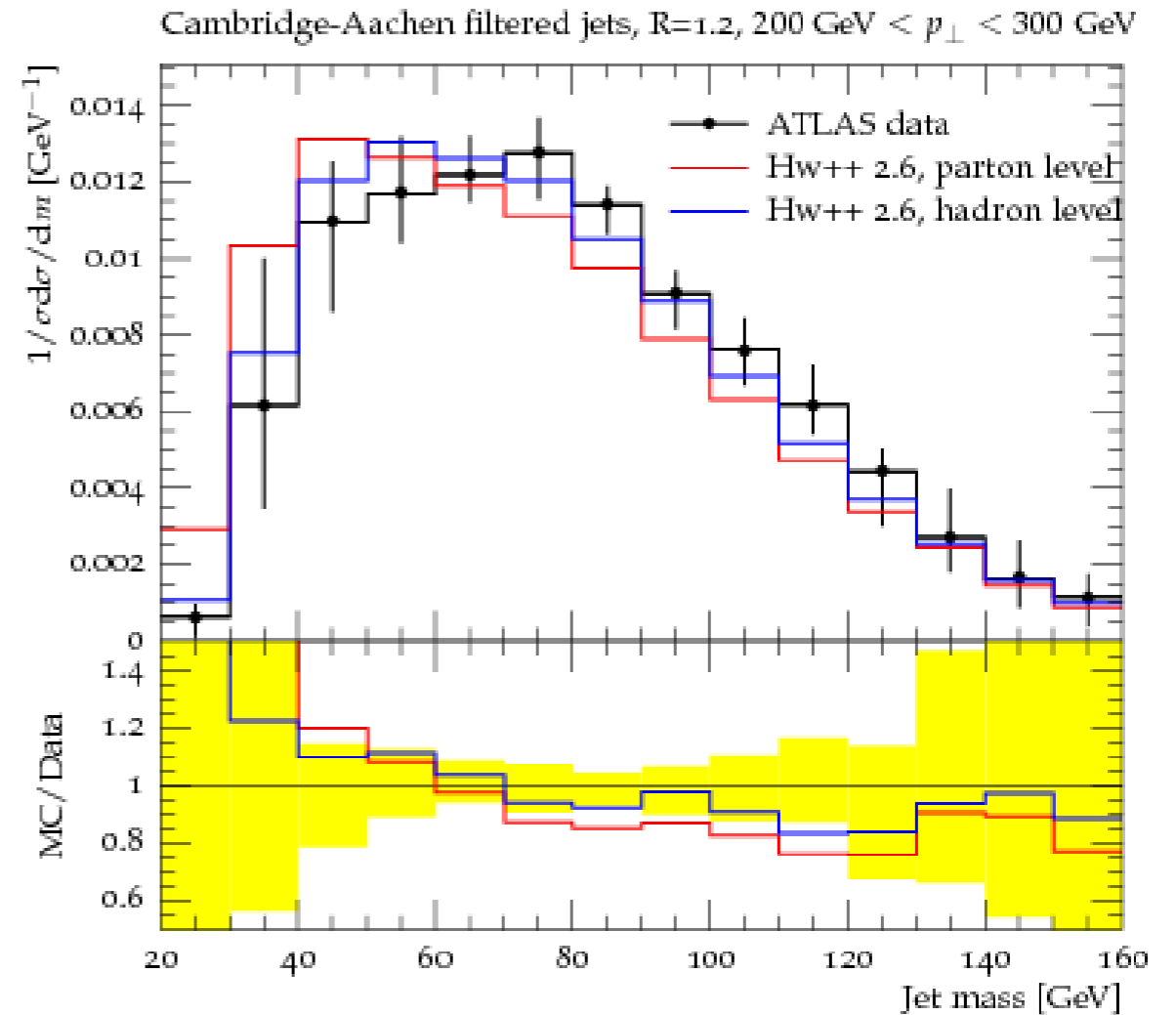
ATLAS measurement of the jet mass with MDT [JHEP 1205 (2012)]

Hadronization + MPI effects Plain Mass ATLAS MDT



significant effects

red line – parton level
blue line – hadron level

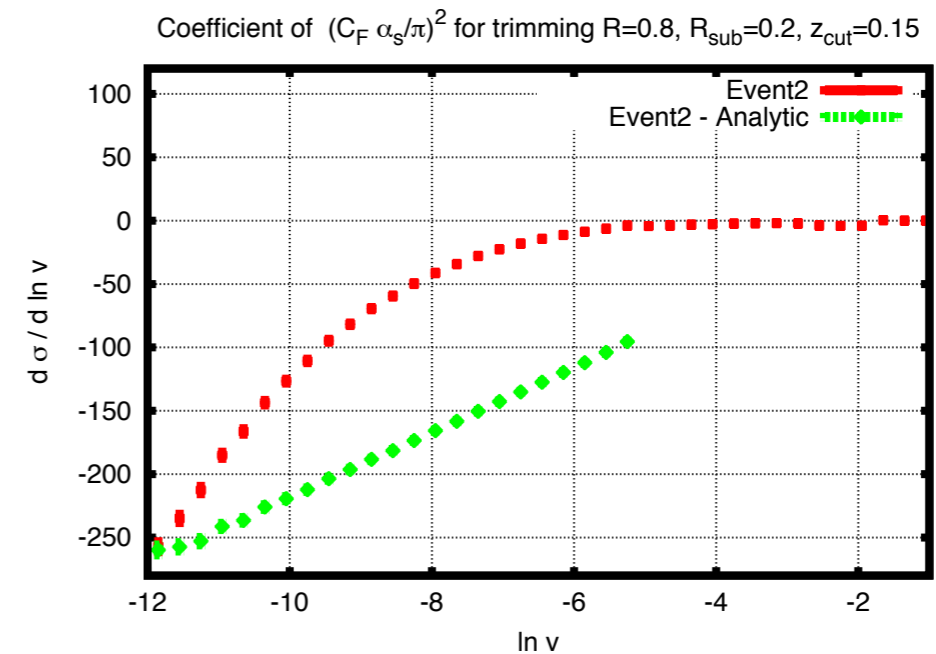
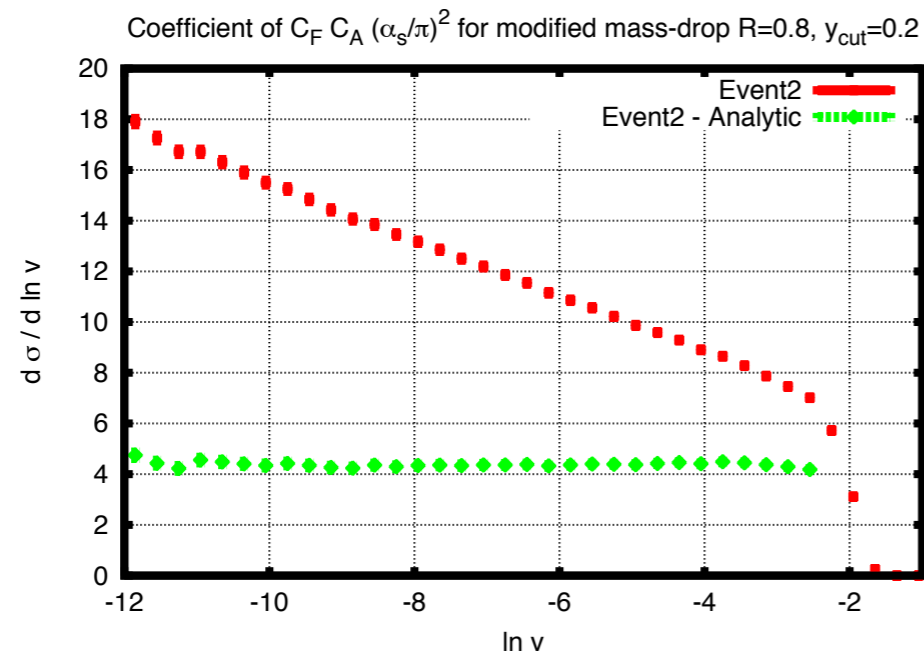
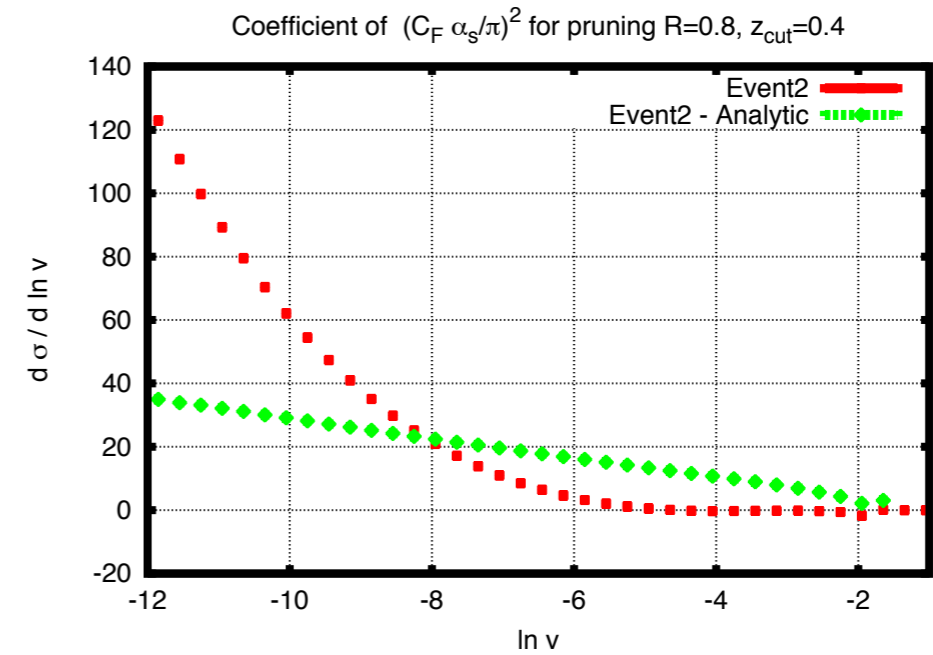
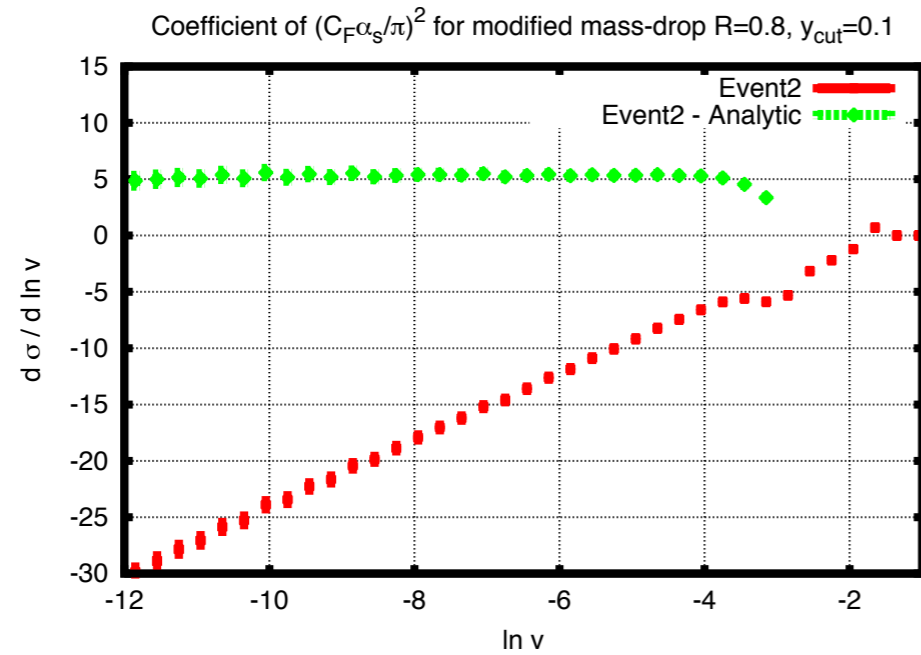


visible effects (small m)

mMDT – not very sensitive to hadronization!

Dasgupta, Siodmok & Powling, in prep.

Examples of NLO checks

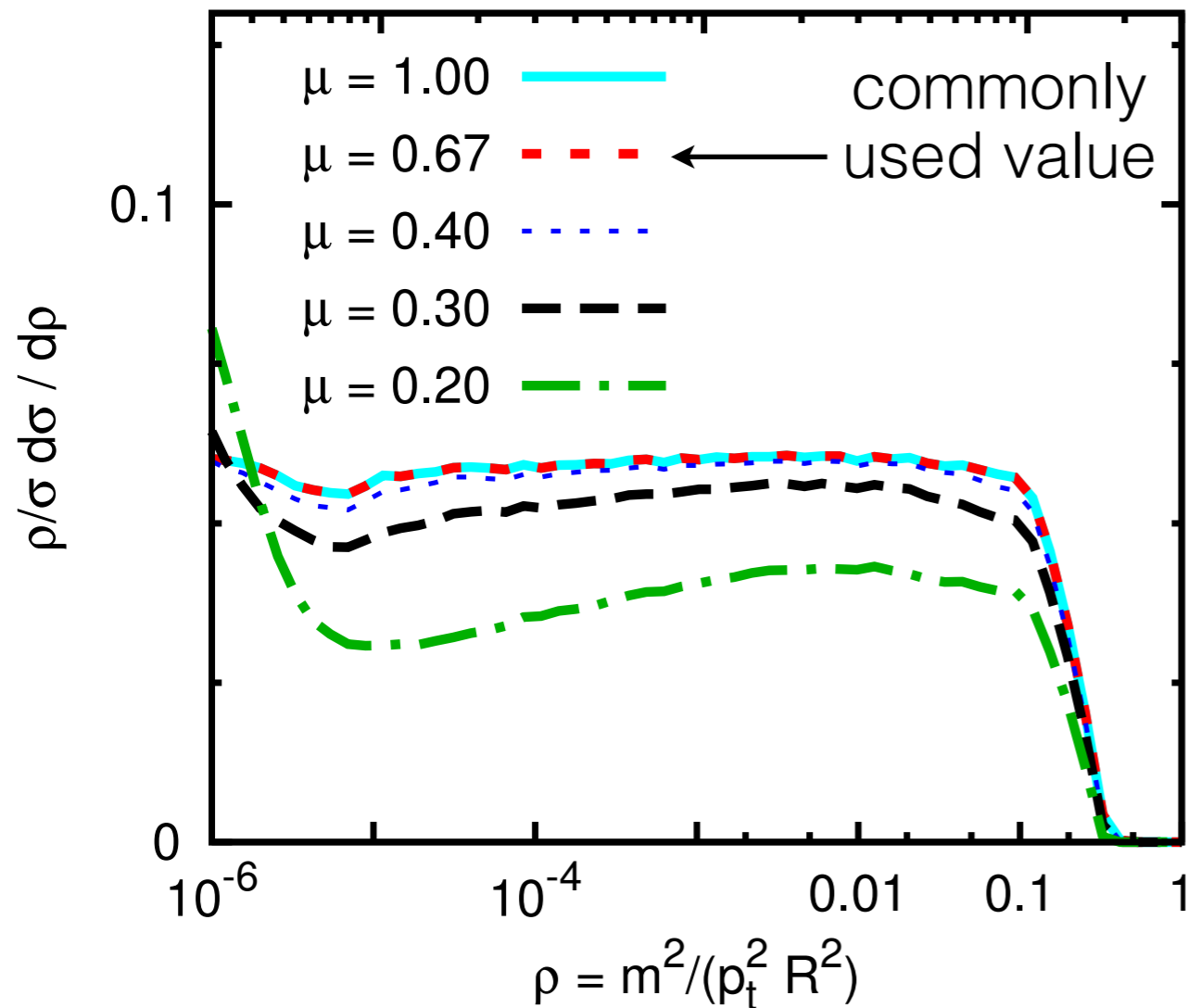


mMDT: impact of μ and of filtering

Effect of μ parameter: quark jets

m [GeV], for $p_t = 3$ TeV, $R = 1$

10 100 1000

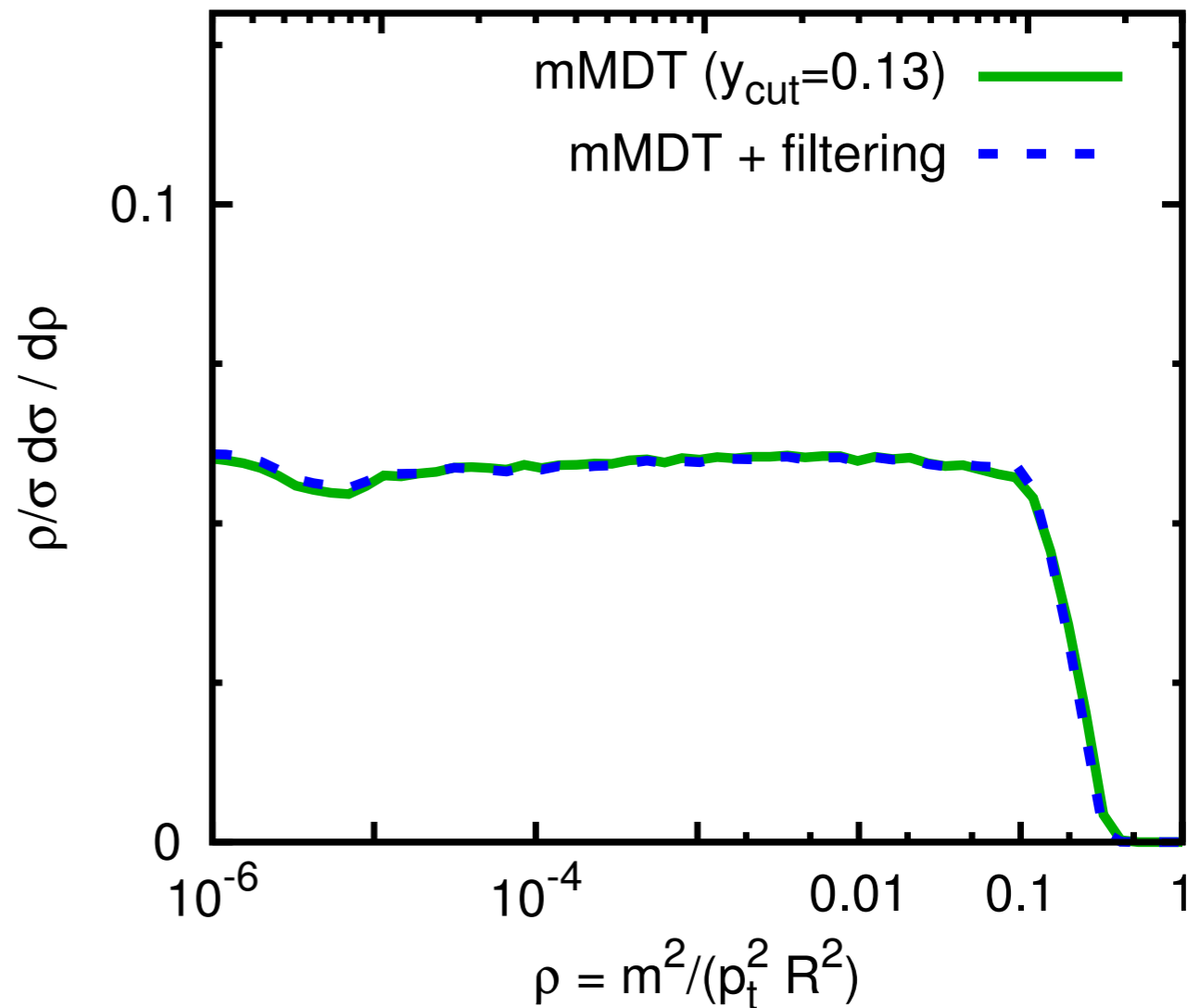


μ parameter basically irrelevant
(simpler tagger discards it)

Effect of filtering: quark jets

m [GeV], for $p_t = 3$ TeV, $R = 1$

10 100 1000

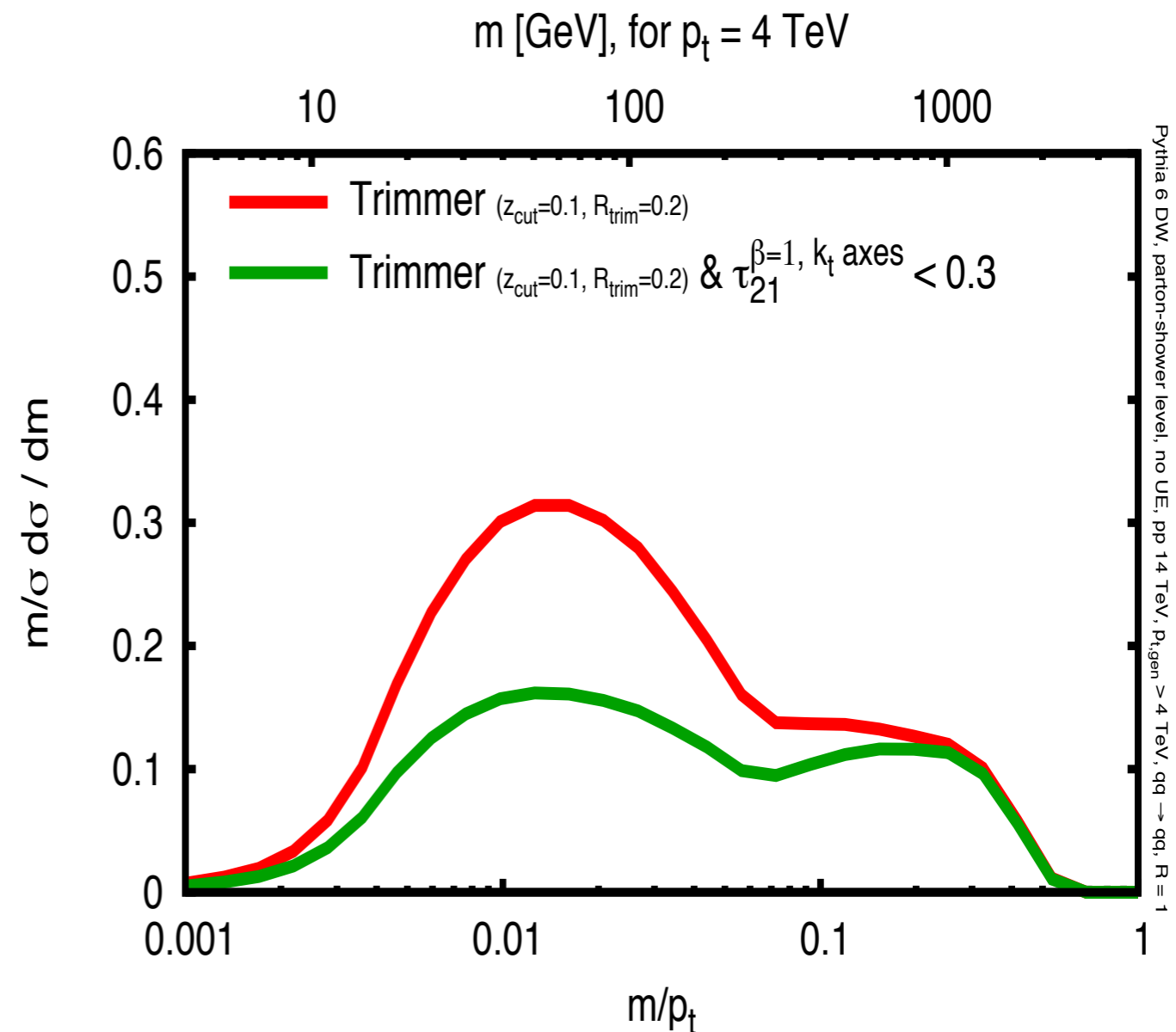


filtering leaves results
unchanged (up to and incl. NNLL)

What about cuts on shapes/radiation

E.g. cuts on N-subjettiness, tight mass drop, etc.?

- These cuts are nearly always for a jet whose mass is somehow groomed. All the structure from the grooming persists.
- So tagging & shape must probably be calculated together



Take a jet and define

$$R_{\text{prune}} = m / p_t$$

Recluster with k_t or C/A alg.
At each $i+j$ clustering step, if

$$p_{t_i} \text{ or } p_{t_j} < \mathbf{Z_{cut}} p_{t(i+j)}$$

$$\Delta R_{ij} > R_{\text{prune}}$$

discard softer prong.

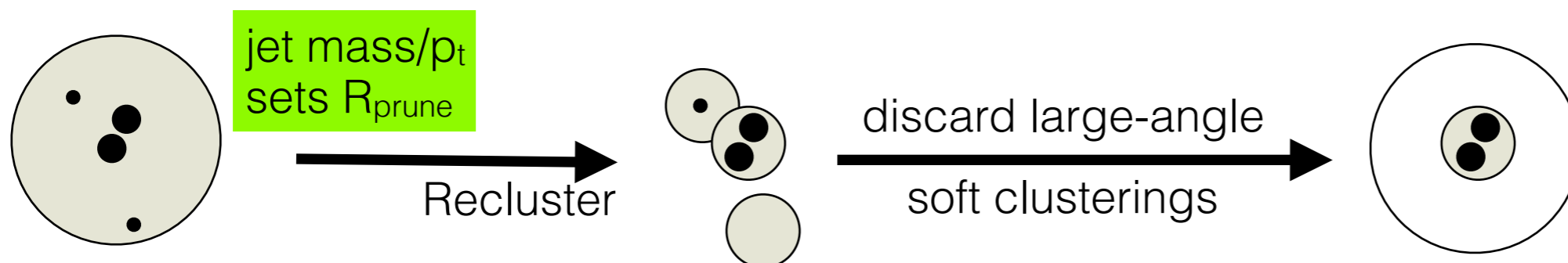
Acts similarly to filtering, but
with **dynamic subjet radius**

Pruning

Ellis, Vermillion & Walsh '09

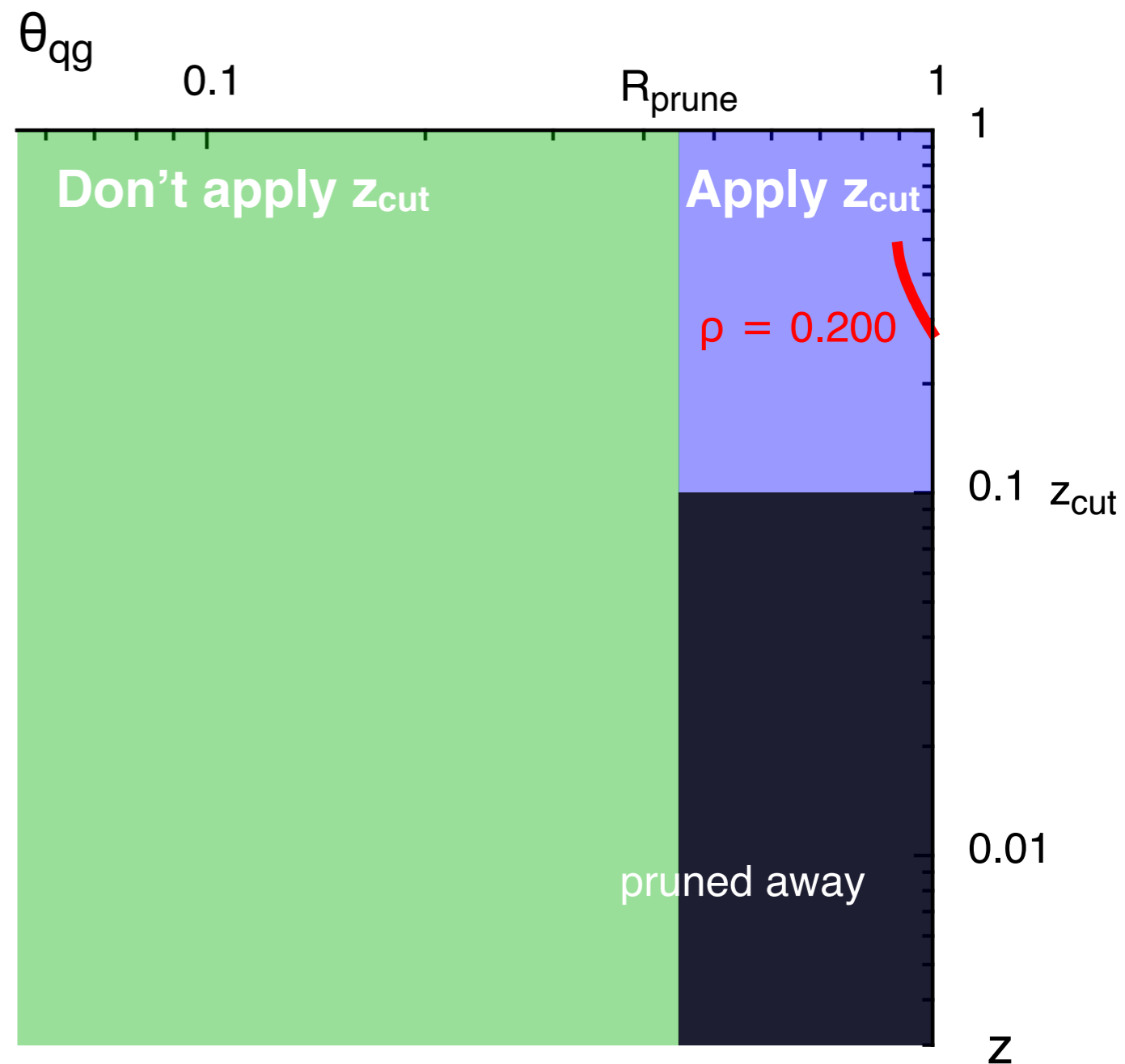
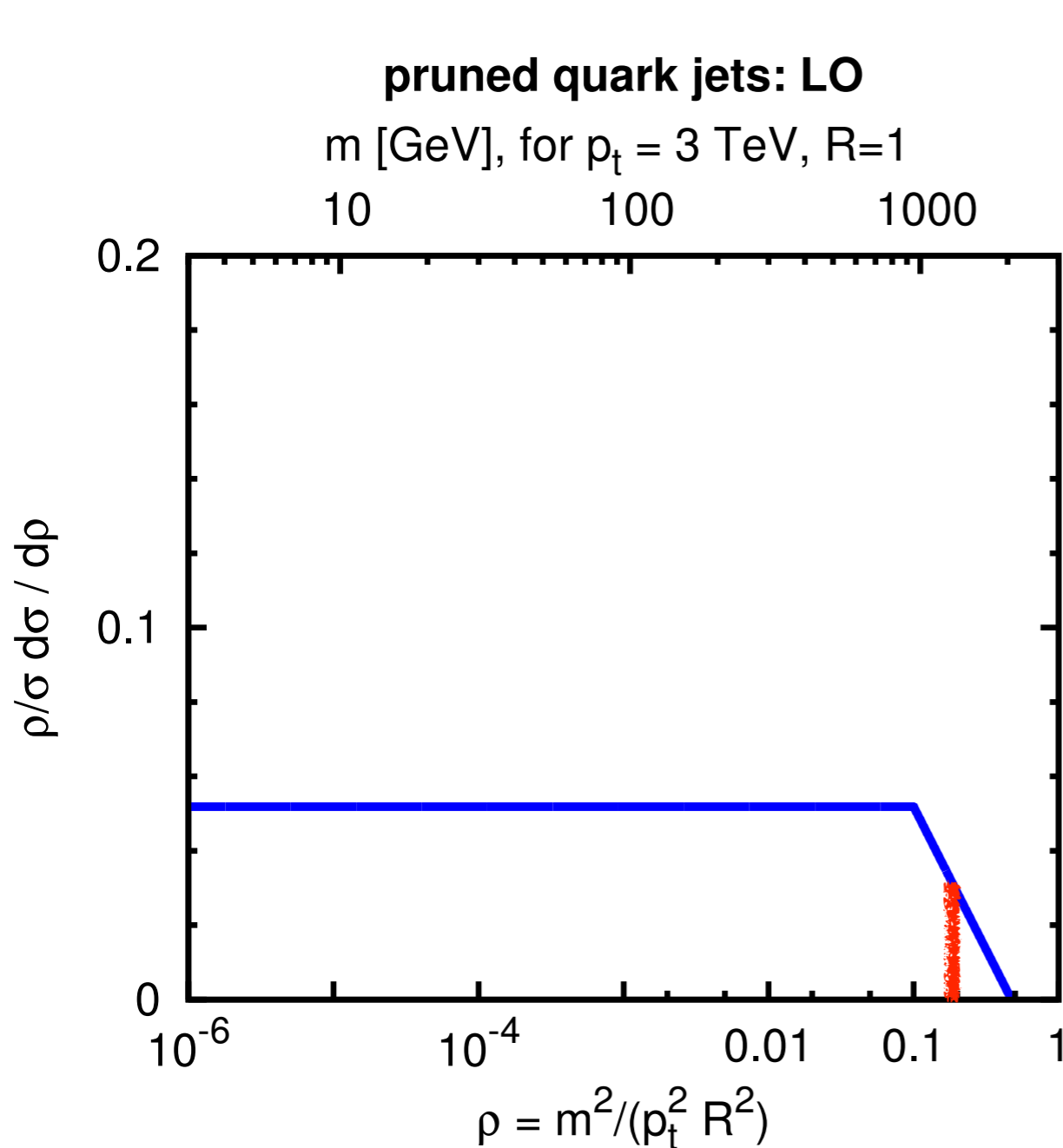
one (main) parameter: Z_{cut}

we'll study variant with C/A
reclustering



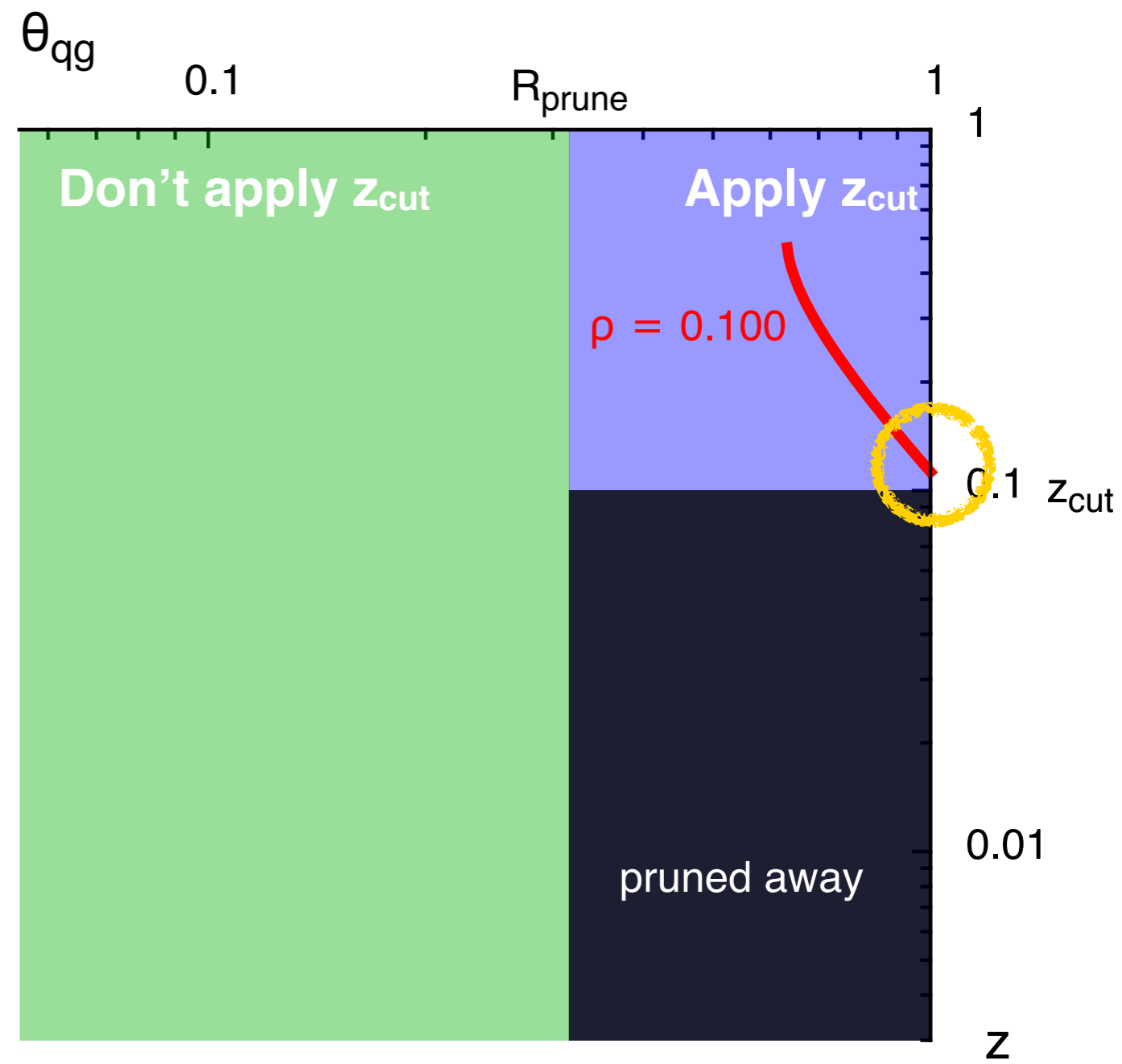
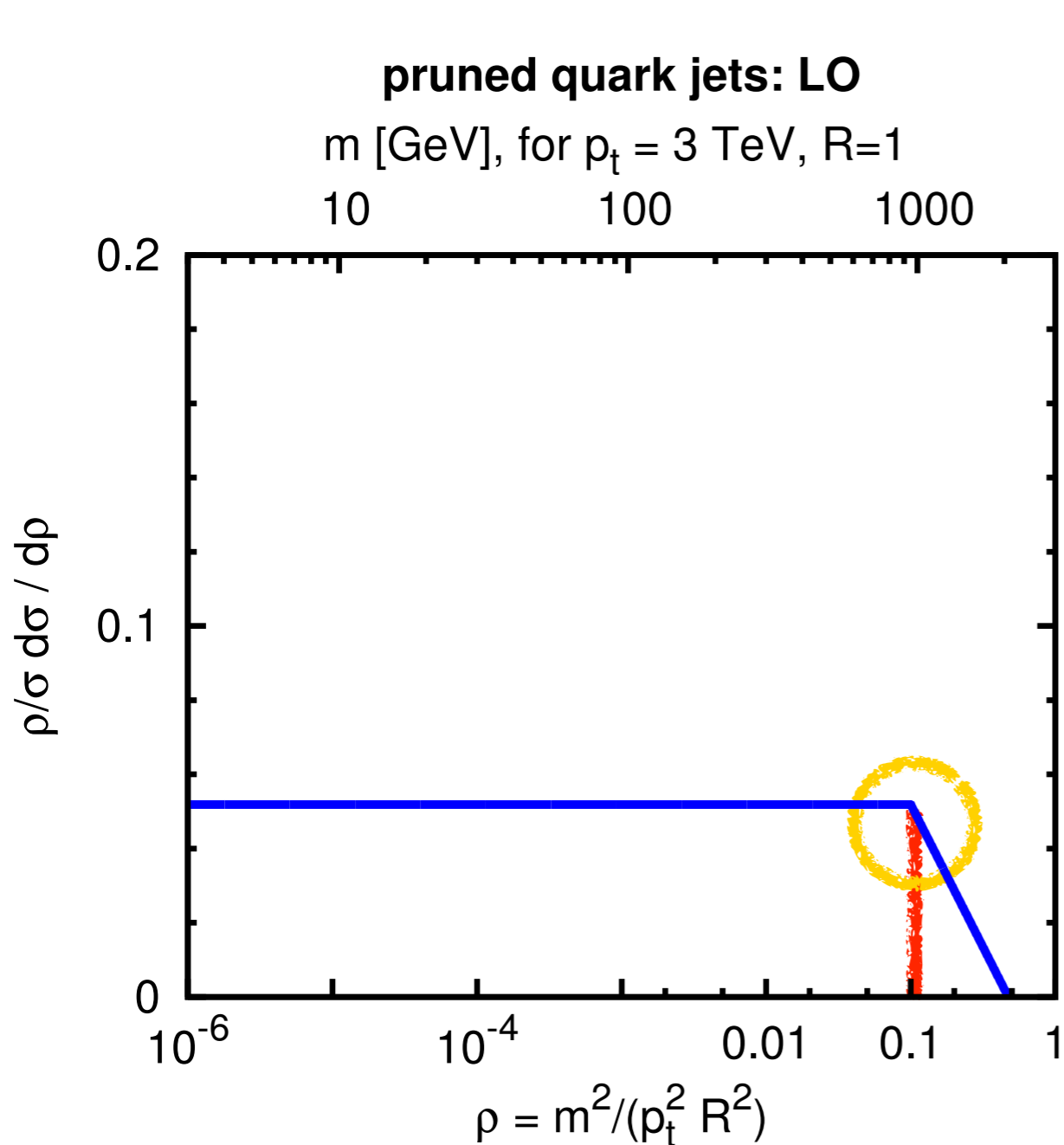
Pruning at LO

Dynamical choice of R_{prune} means that two prongs are always separated by $> R_{\text{prune}}$. So, unlike trimming, z_{cut} always applied.



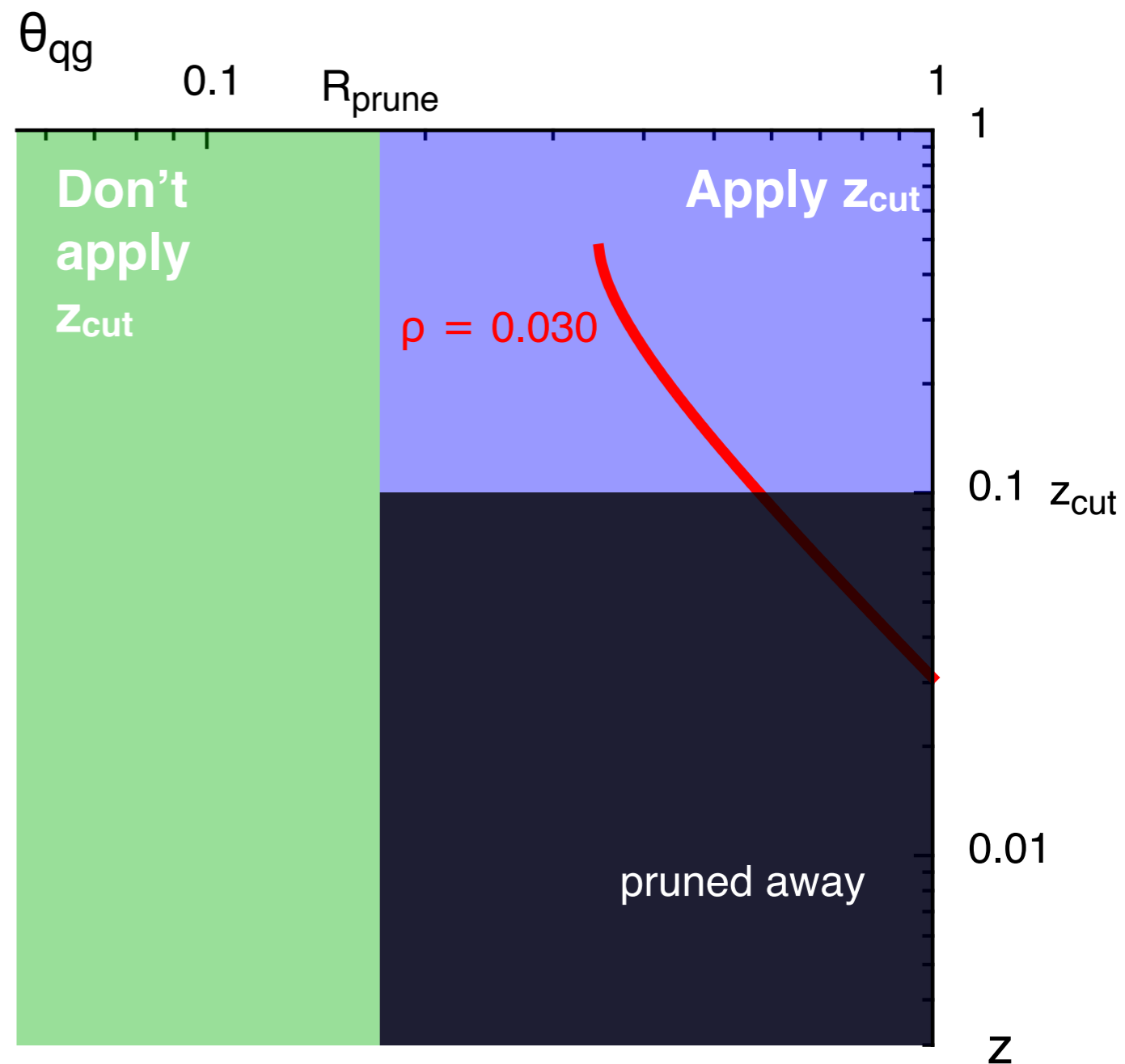
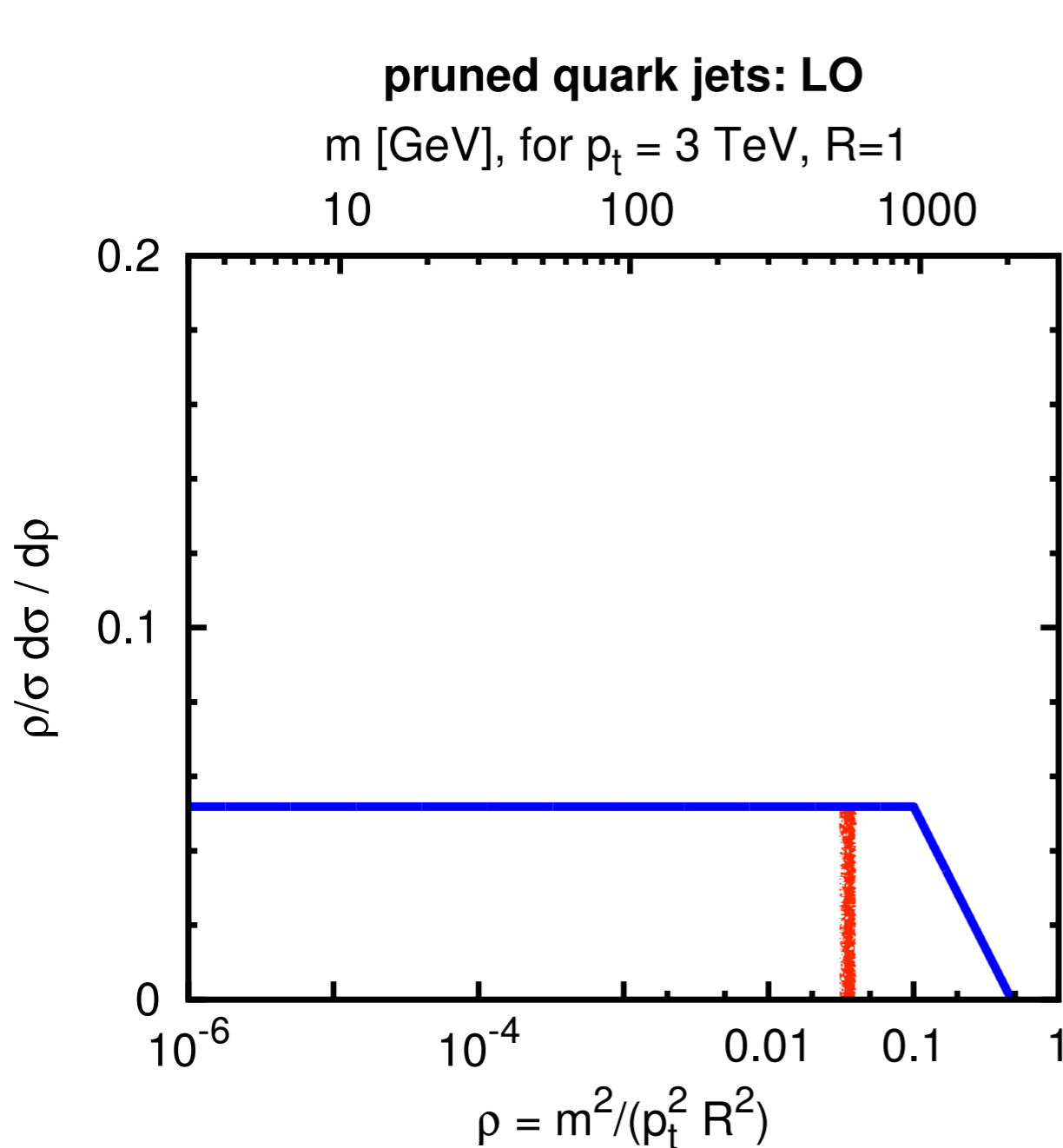
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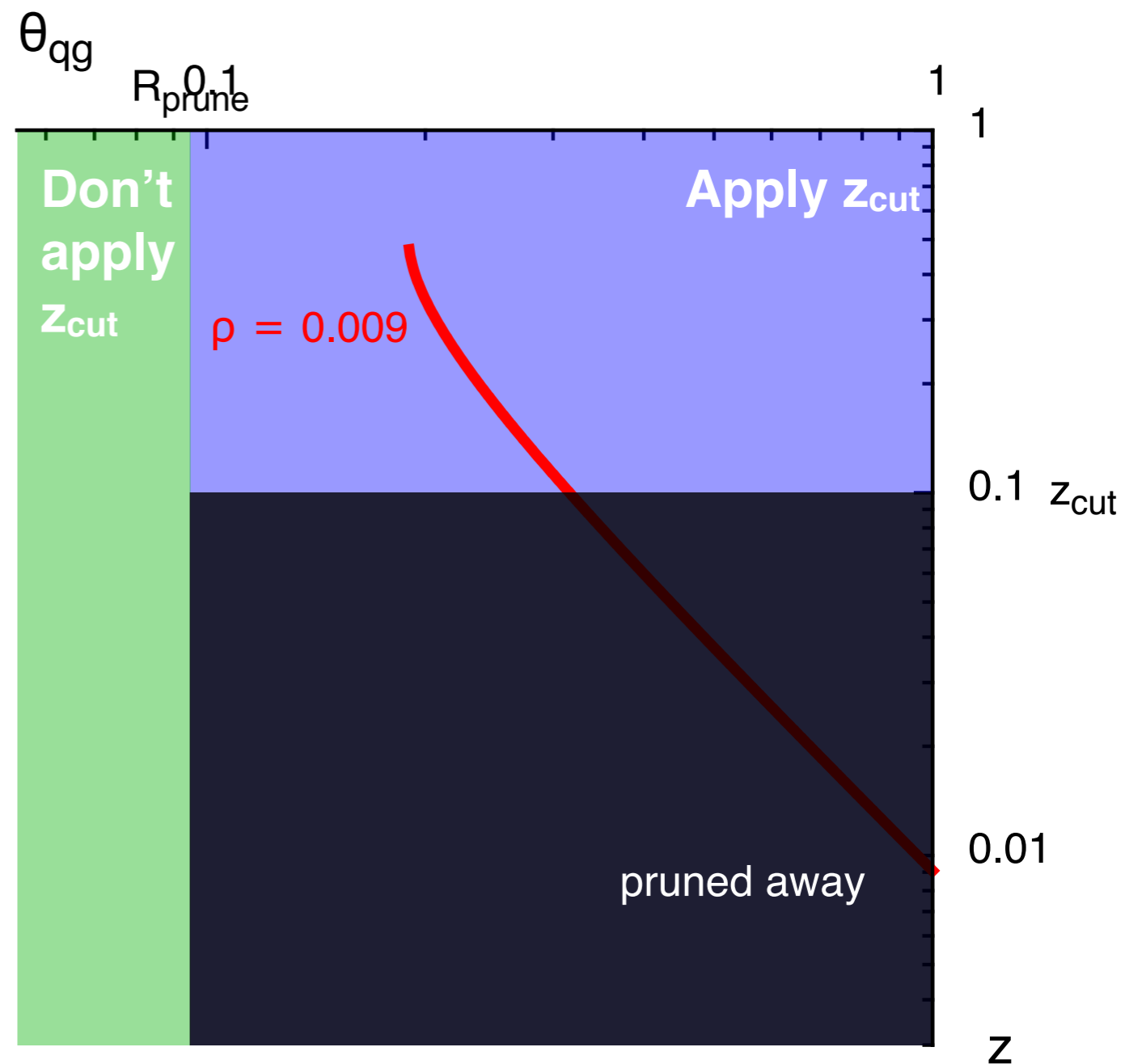
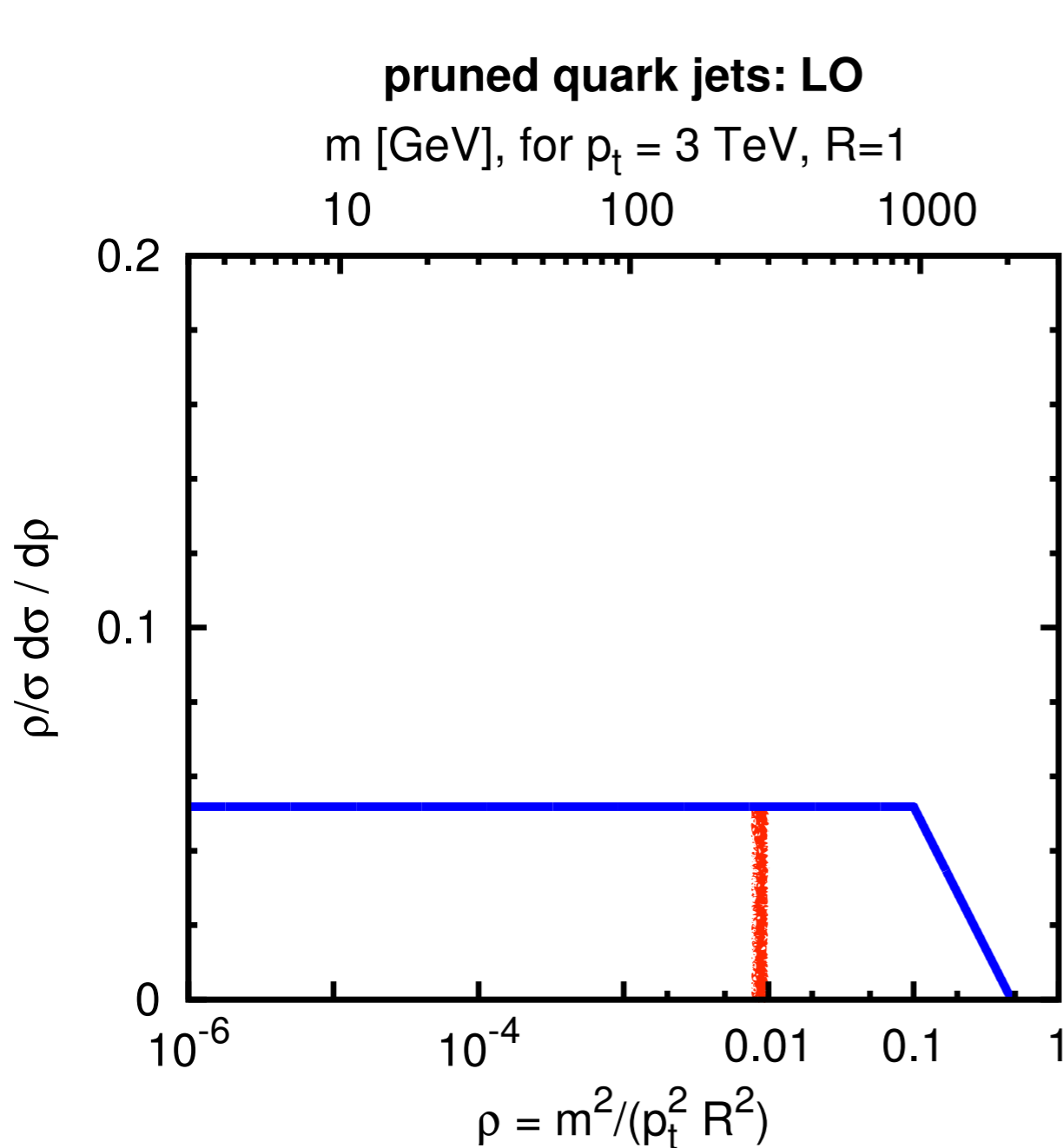
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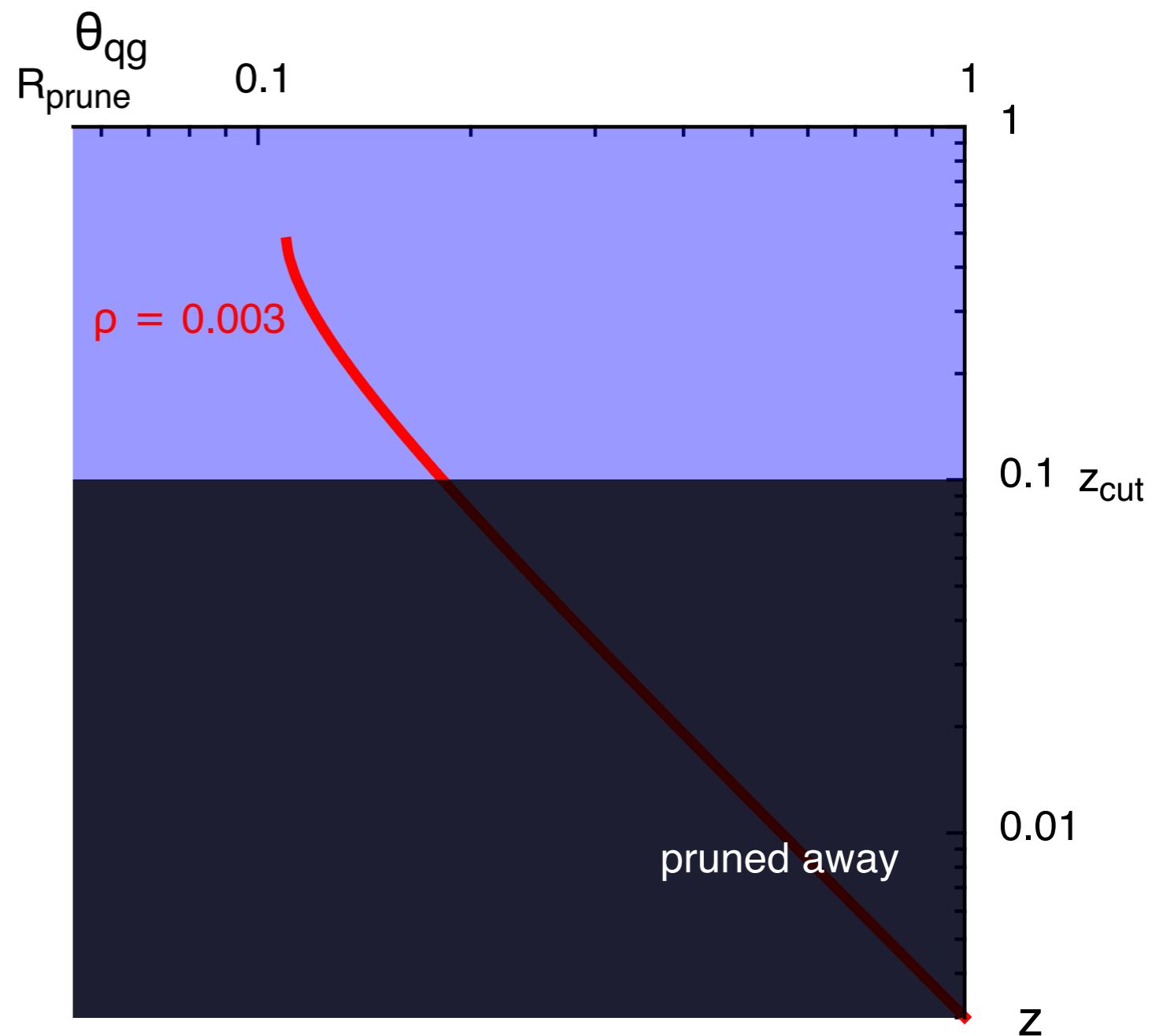
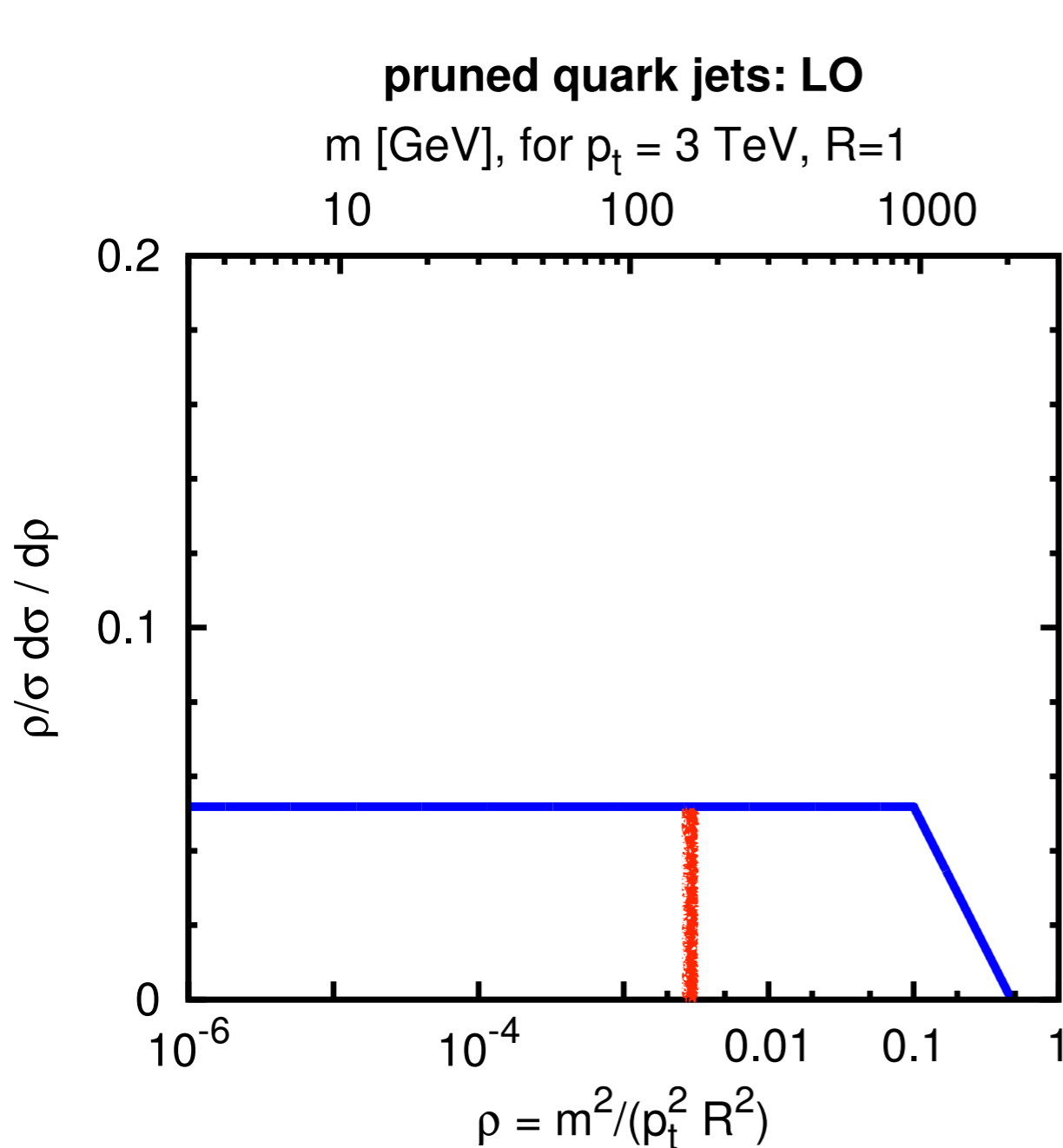
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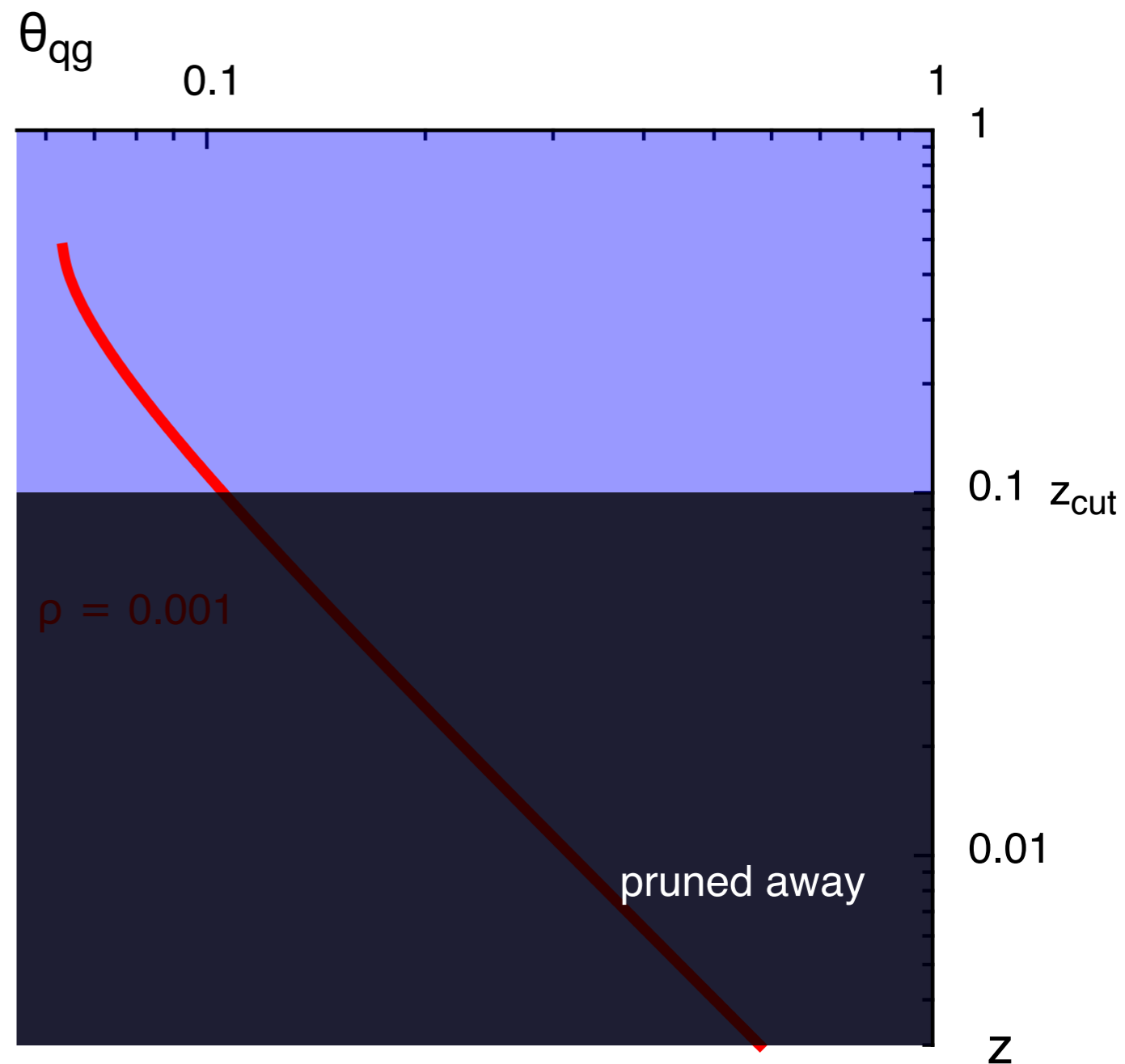
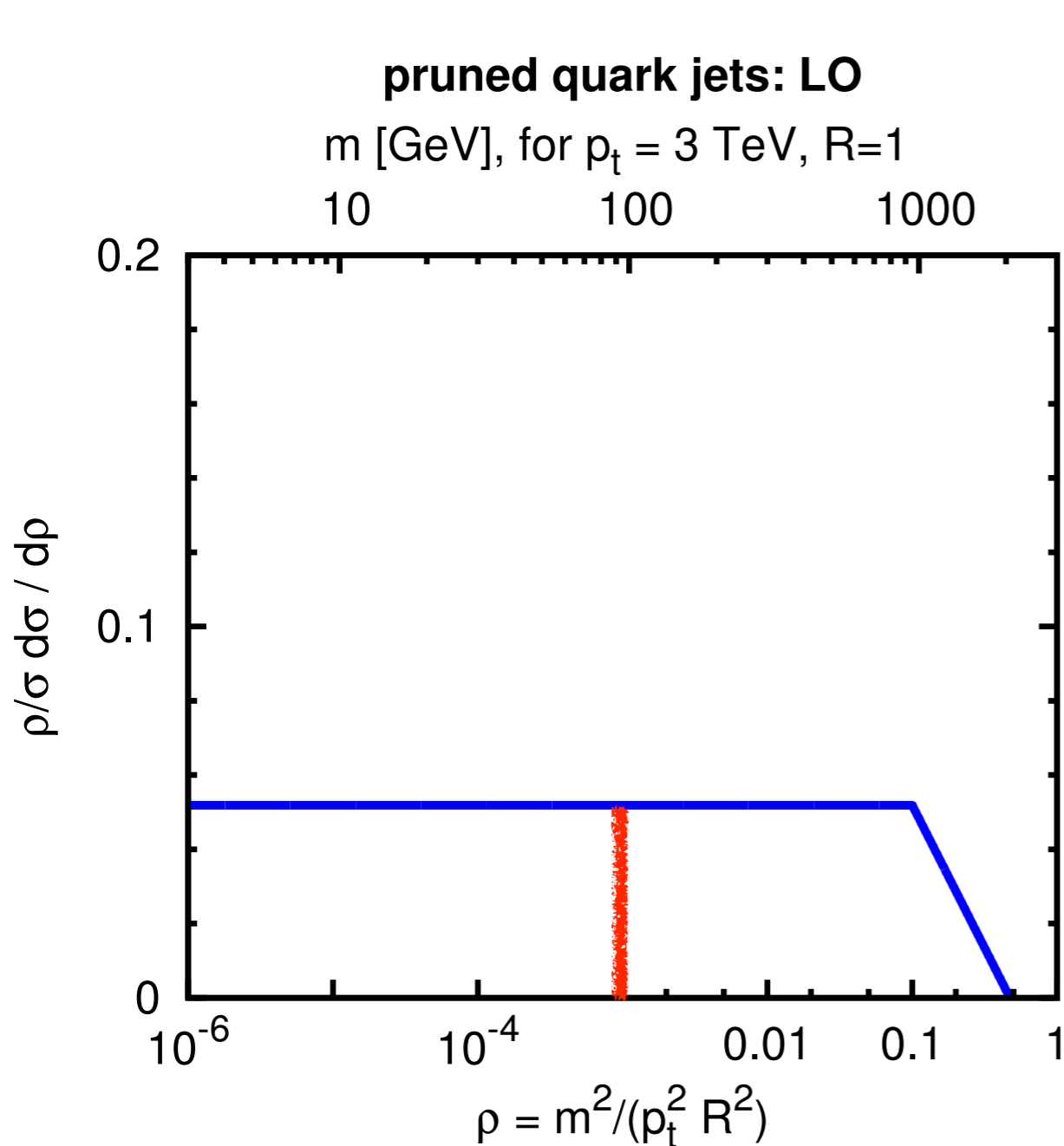
Pruning at LO

Dynamical choice of R_{prune} means that two prongs are always separated by $> R_{\text{prune}}$. So, unlike trimming, z_{cut} always applied.



Pruning at LO

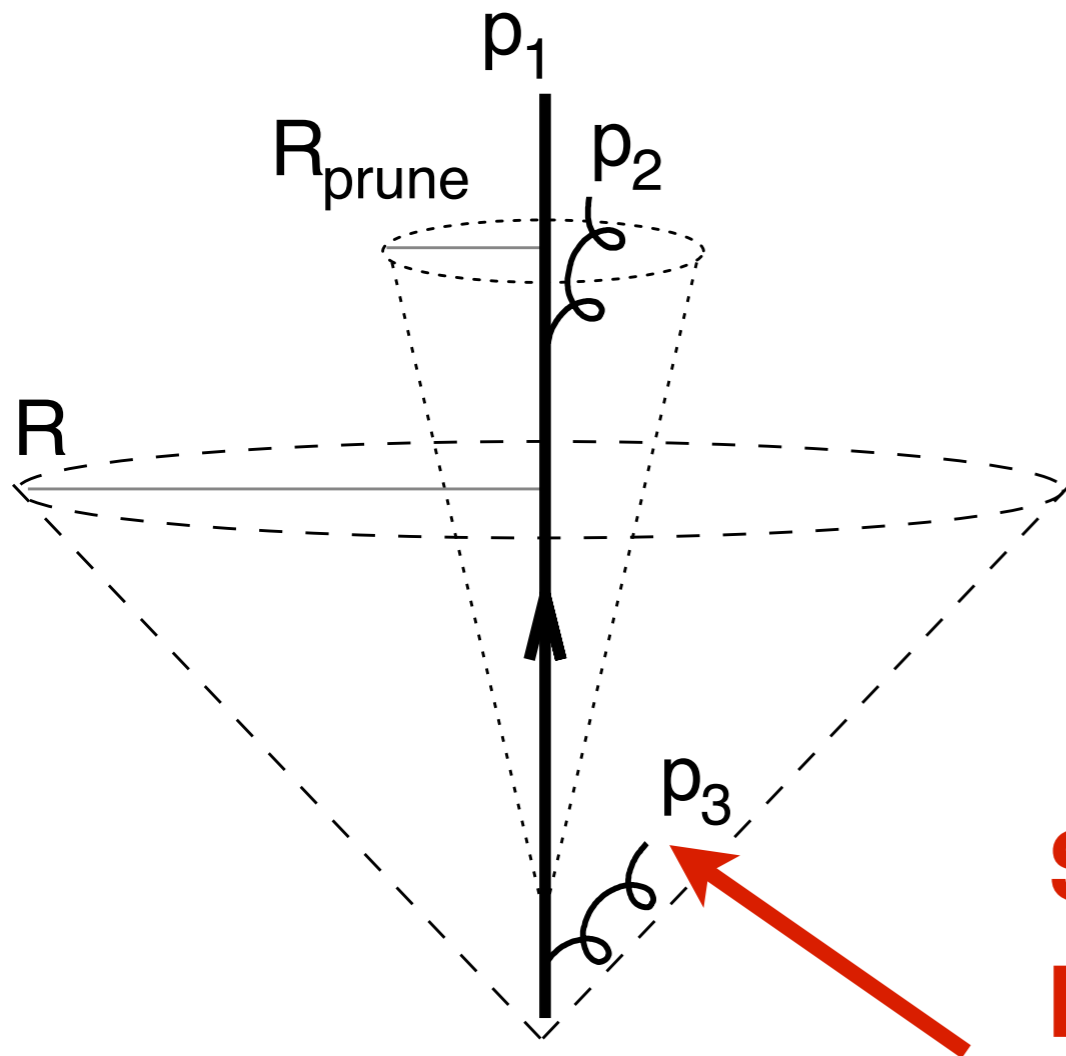
Dynamical choice of R_{prune} means that two prongs are always separated by $> R_{\text{prune}}$. So, unlike trimming, z_{cut} always applied.



pruning beyond 1st order: consider multiple emissions

What pruning sometimes does

Chooses R_{prune} based on a soft p_3 (dominates total jet mass), and leads to a single narrow subjet whose mass is also dominated by a soft emission (p_2 , within R_{prune} of p_1 , so not pruned away).



Sets pruning radius, but gets pruned away → “wrong” pruning radius → makes this ~ trimming

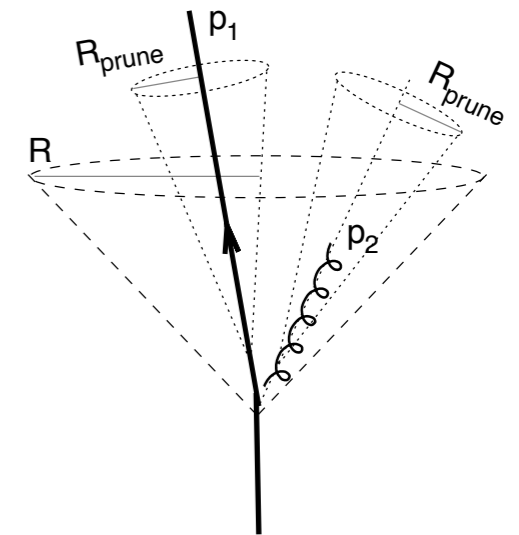
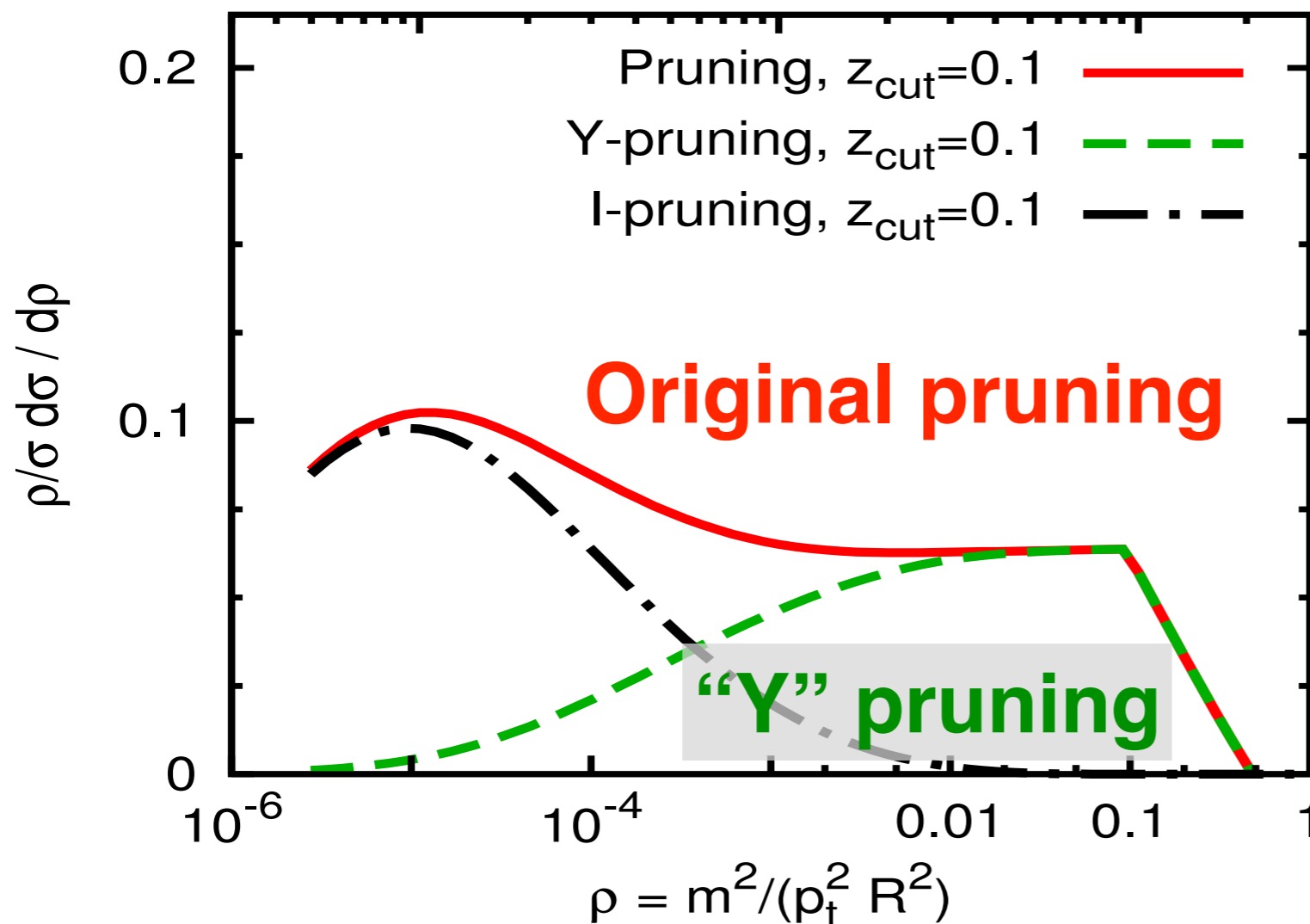
A simple fix: “Y” pruning

Require at least one successful merging with $\Delta R > R_{\text{prune}}$ and $z > z_{\text{cut}}$ — forces 2-pronged (“Y”) configurations

Analytic Calculation: quark jets

m [GeV], for $p_t = 3$ TeV, $R = 1$

10 100 1000



“Y” pruning ~ an isolation cut on radiation around the tagged object — **exploits W/Z/H colour singlet**

What logs, what accuracy?

At leading order pruning (\equiv Y-pruning): **no double logs!**

$$\alpha_s L, \text{ but no } \alpha_s L^2$$

Full Pruning's leading logs (LL, in Σ) are:

$$\alpha_s L, \alpha_s^2 L^4, \dots \text{ I.e. } \alpha_s^n L^{2n}$$

we also have NLL

Y-Pruning's leading logs (LL, in Σ) are:

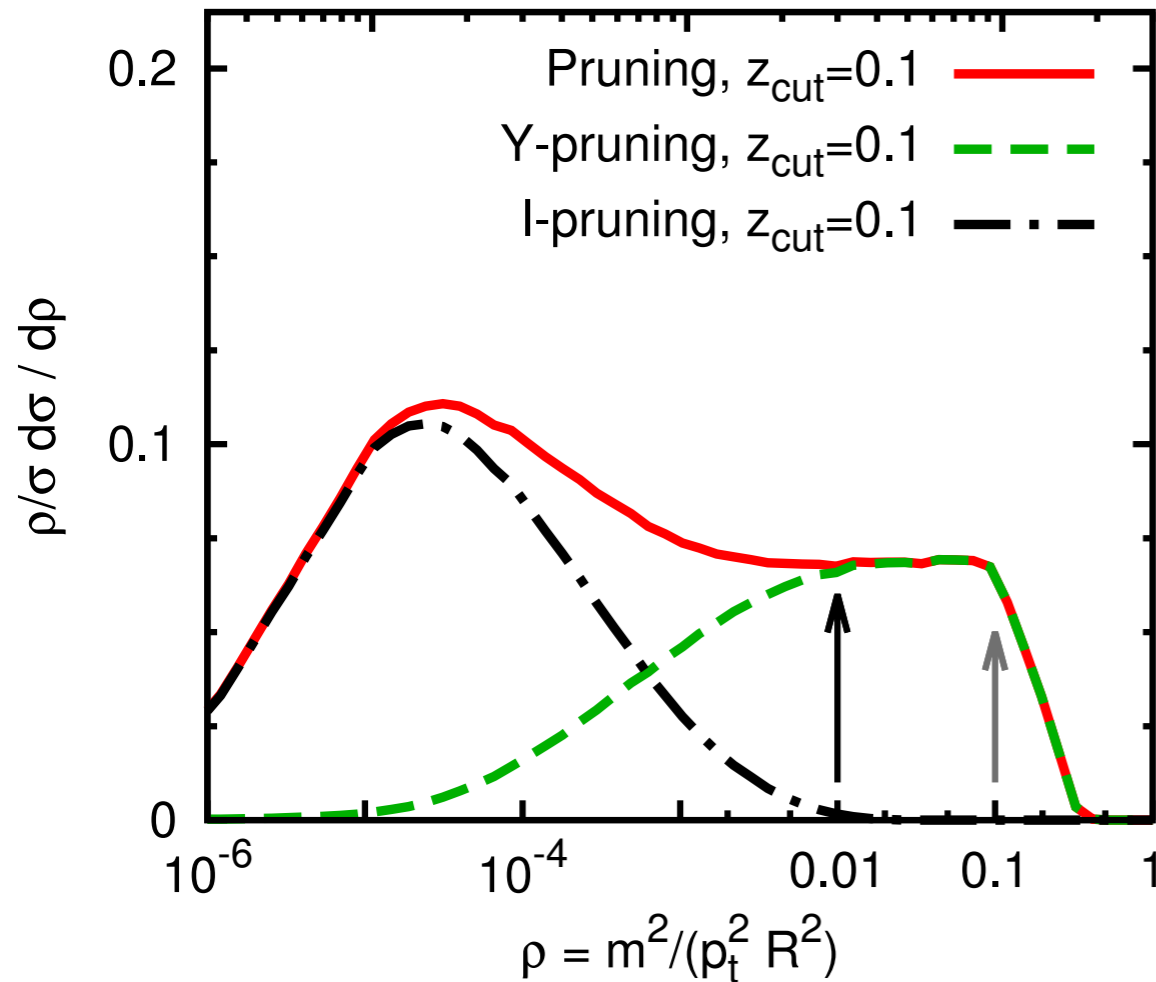
$$\alpha_s L, \alpha_s^2 L^3, \dots \text{ I.e. } \alpha_s^n L^{2n-1}$$

we also have NLL

Could we do better? Yes: NLL in $\ln \Sigma$, but involves **non-global logs, clustering logs**

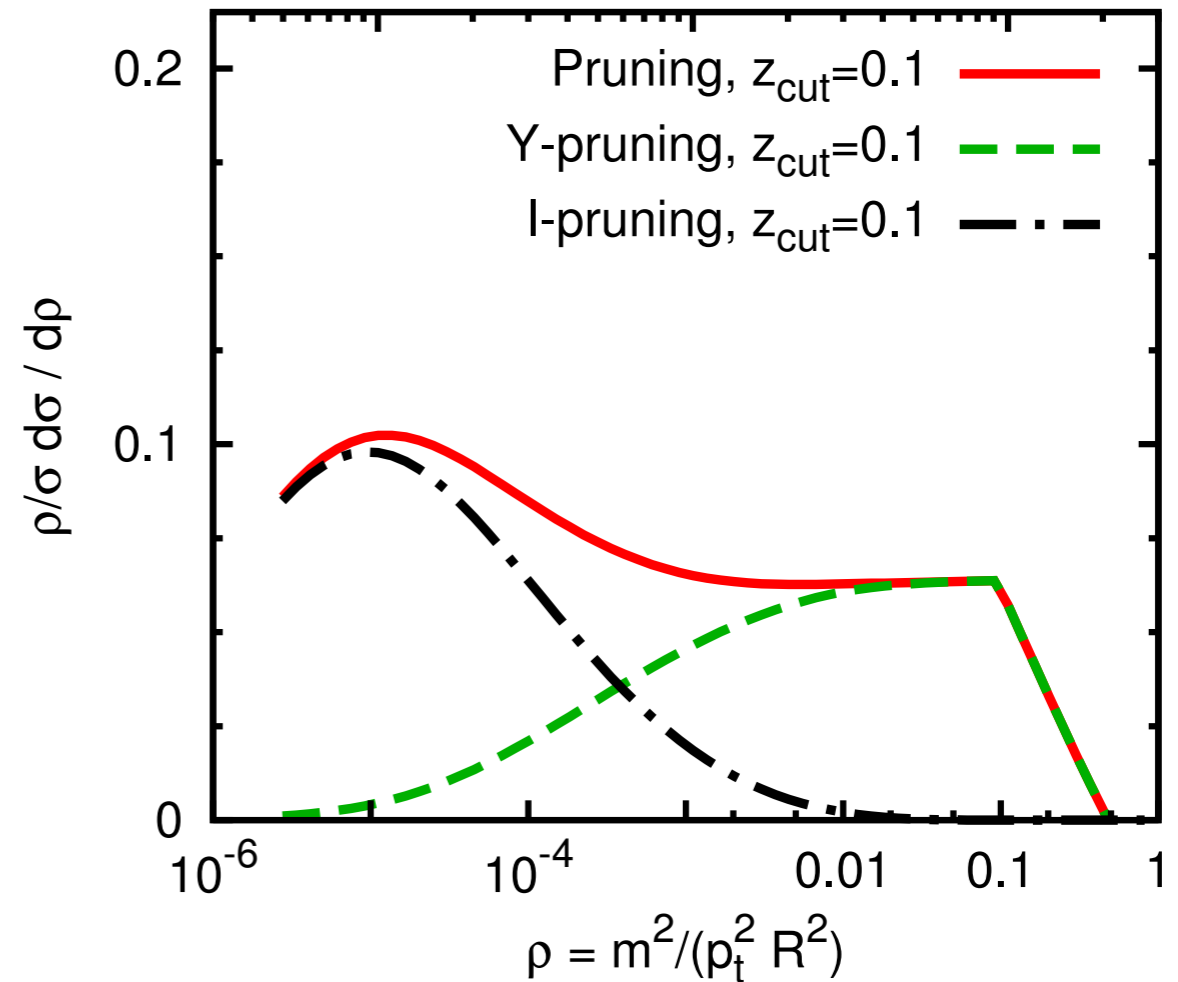
Monte Carlo

m [GeV], for $p_t = 3$ TeV, $R = 1$
 10 100 1000



Analytic

m [GeV], for $p_t = 3$ TeV, $R = 1$
 10 100 1000



Non-trivial agreement!
 (also for dependence on parameters)