

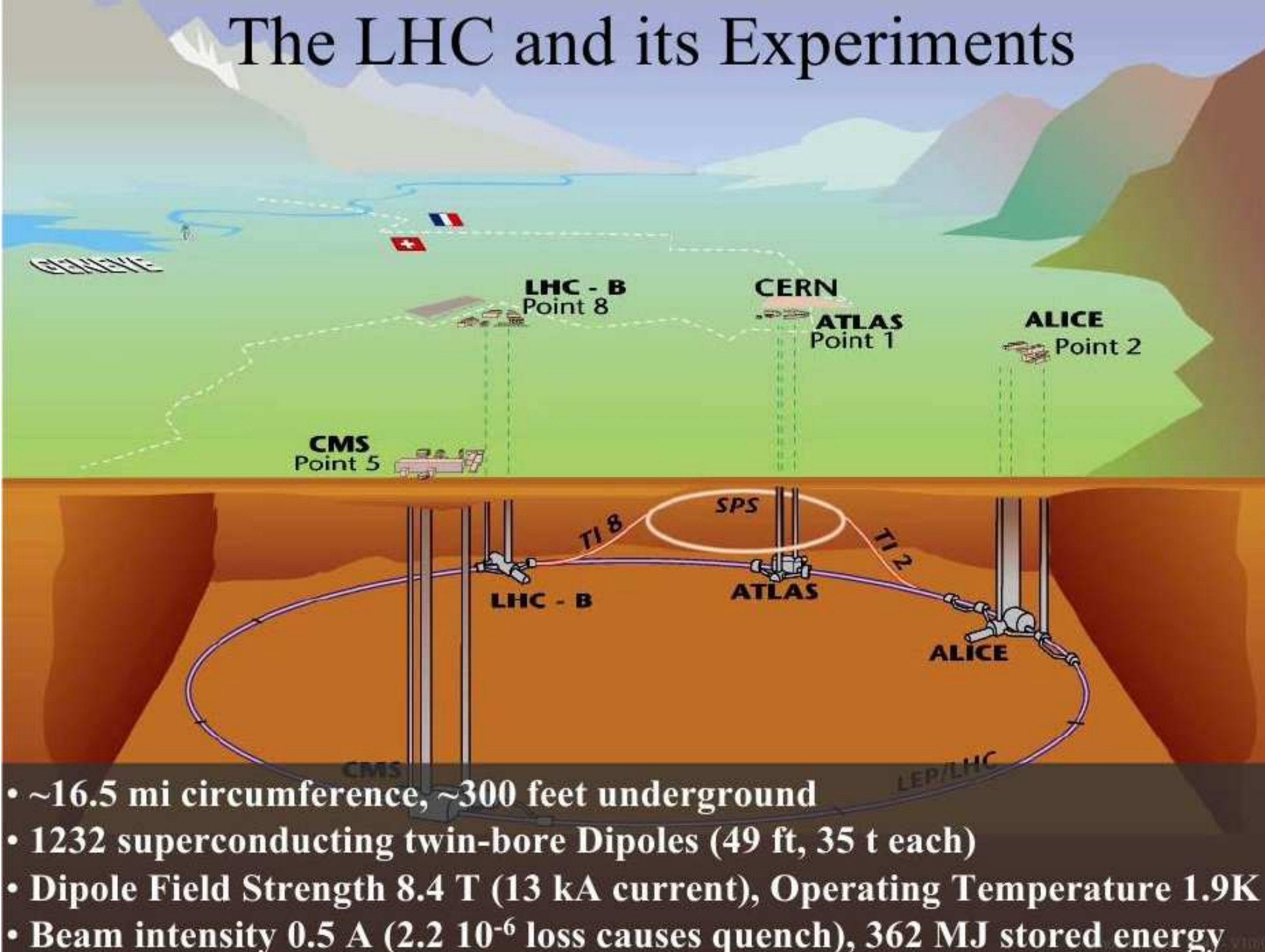
TOWARDS 1% PRECISION AT THE LHC?

Gavin Salam, CERN

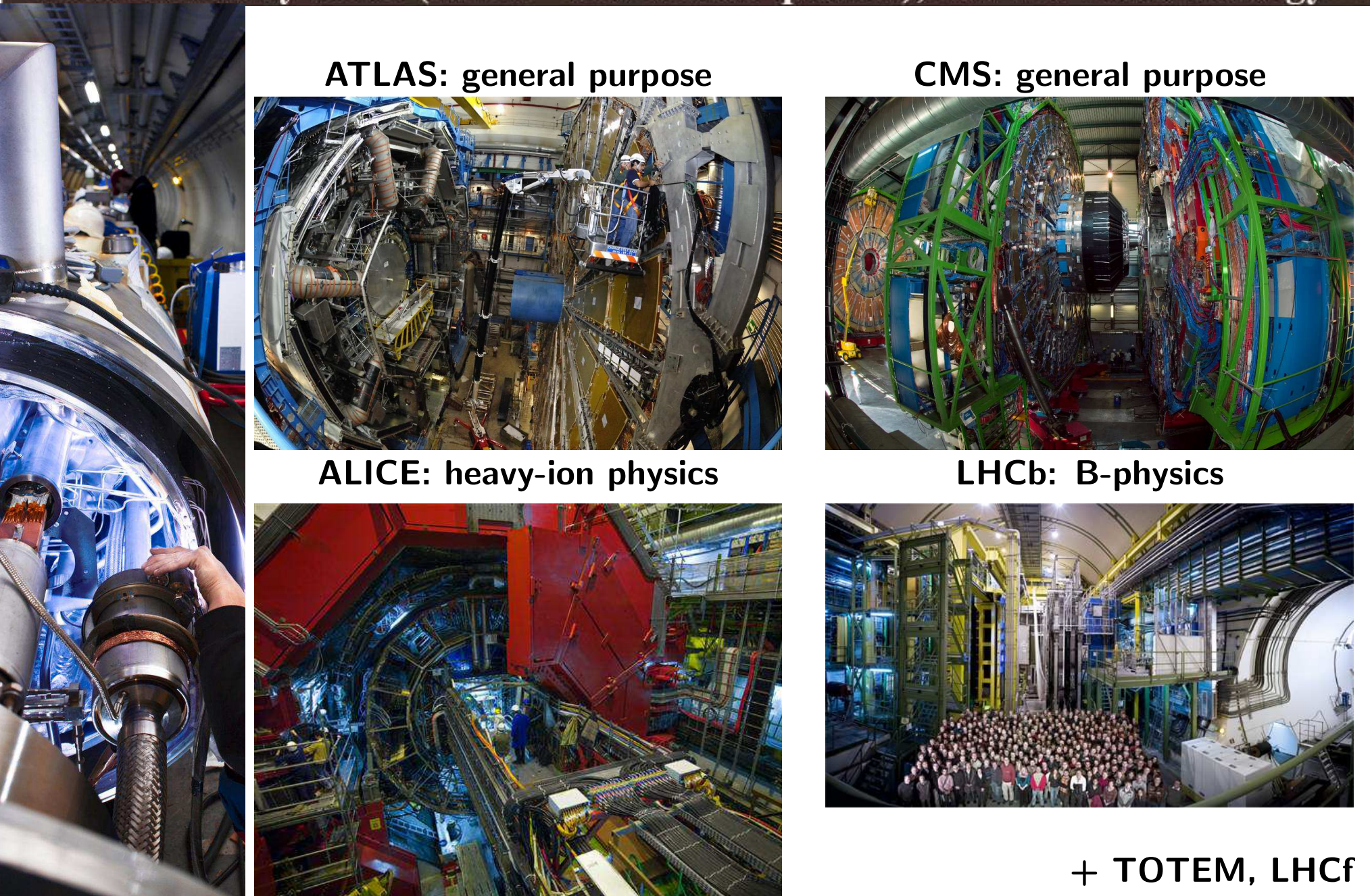
*Future challenges for precision QCD
IPPP, Durham, UK, 25–28 October 2016*

*Talk in part inspired by discussions at KITP Santa Barbara
& for ECFA HL-LHC workshop*

The LHC and its Experiments

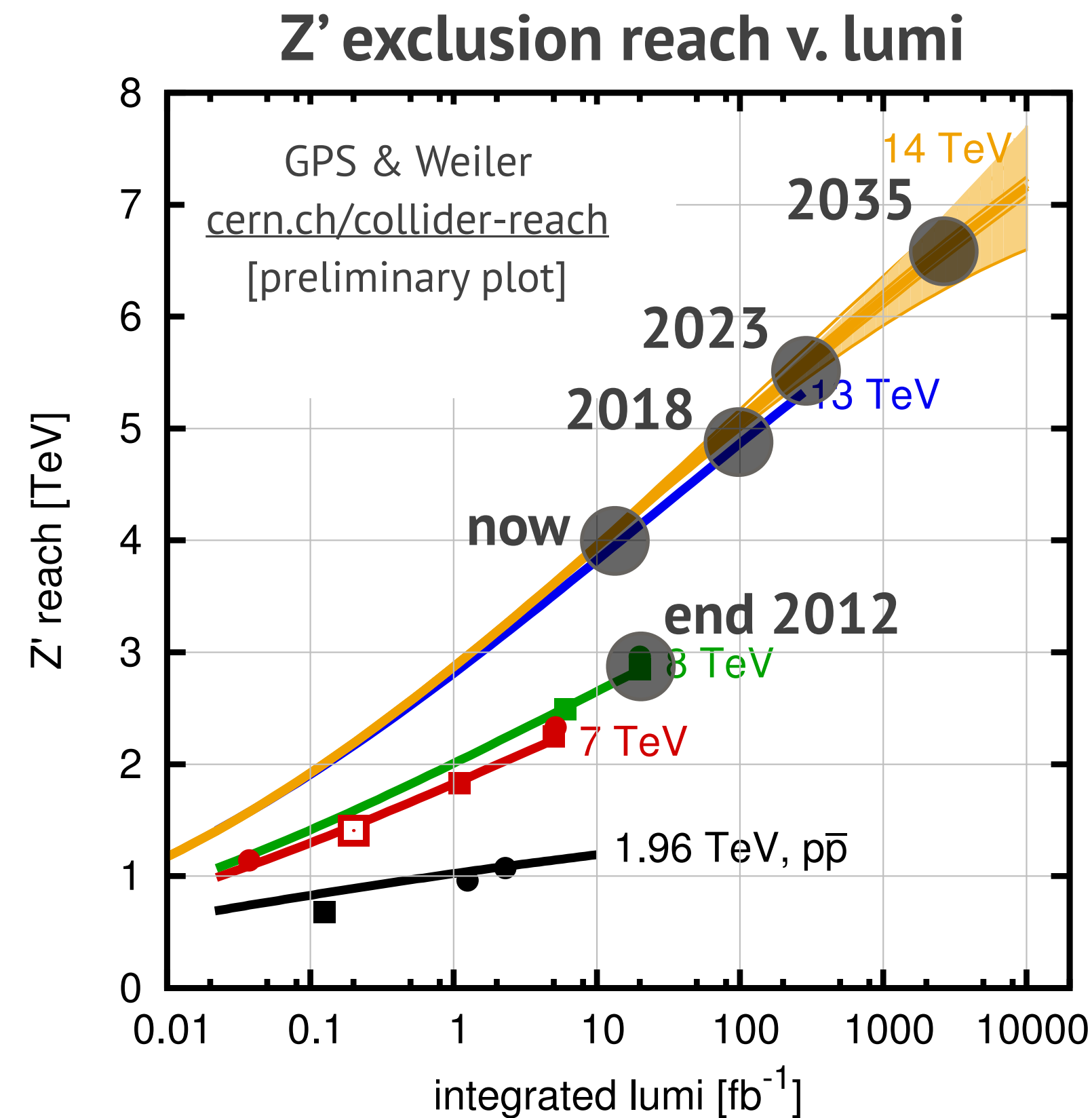


- ~16.5 mi circumference, ~300 feet underground
- 1232 superconducting twin-bore Dipoles (49 ft, 35 t each)
- Dipole Field Strength 8.4 T (13 kA current), Operating Temperature 1.9K
- Beam intensity 0.5 A ($2.2 \cdot 10^{-6}$ loss causes quench), 362 MJ stored energy



+ TOTEM, LHCf

LHC – TWO ROLES – A DISCOVERY MACHINE AND A PRECISION MACHINE



Today

- 20 fb⁻¹ @ 8 TeV
- 13 fb⁻¹ @ 13 TeV (analysed)

Future

- 2018: 100 fb⁻¹ @ 13 TeV
- 2023: 300 fb⁻¹ @ 1? TeV
- 2035: 3000 fb⁻¹ @ 14 TeV

1 fb⁻¹ = 10¹⁴ collisions

Increase in luminosity brings discovery reach and precision

PRECISION LHC PHYSICS NEEDS PRECISION THEORY

Progress on calculations has been stunning in the past years

- N3LO Higgs
- Many processes at NNLO
- NLO + PS automation
- First NNLO + PS
- NNLL Resummations
- EW + QCD, etc.

This progress is essential for LHC precision physics, but also only part of the story.

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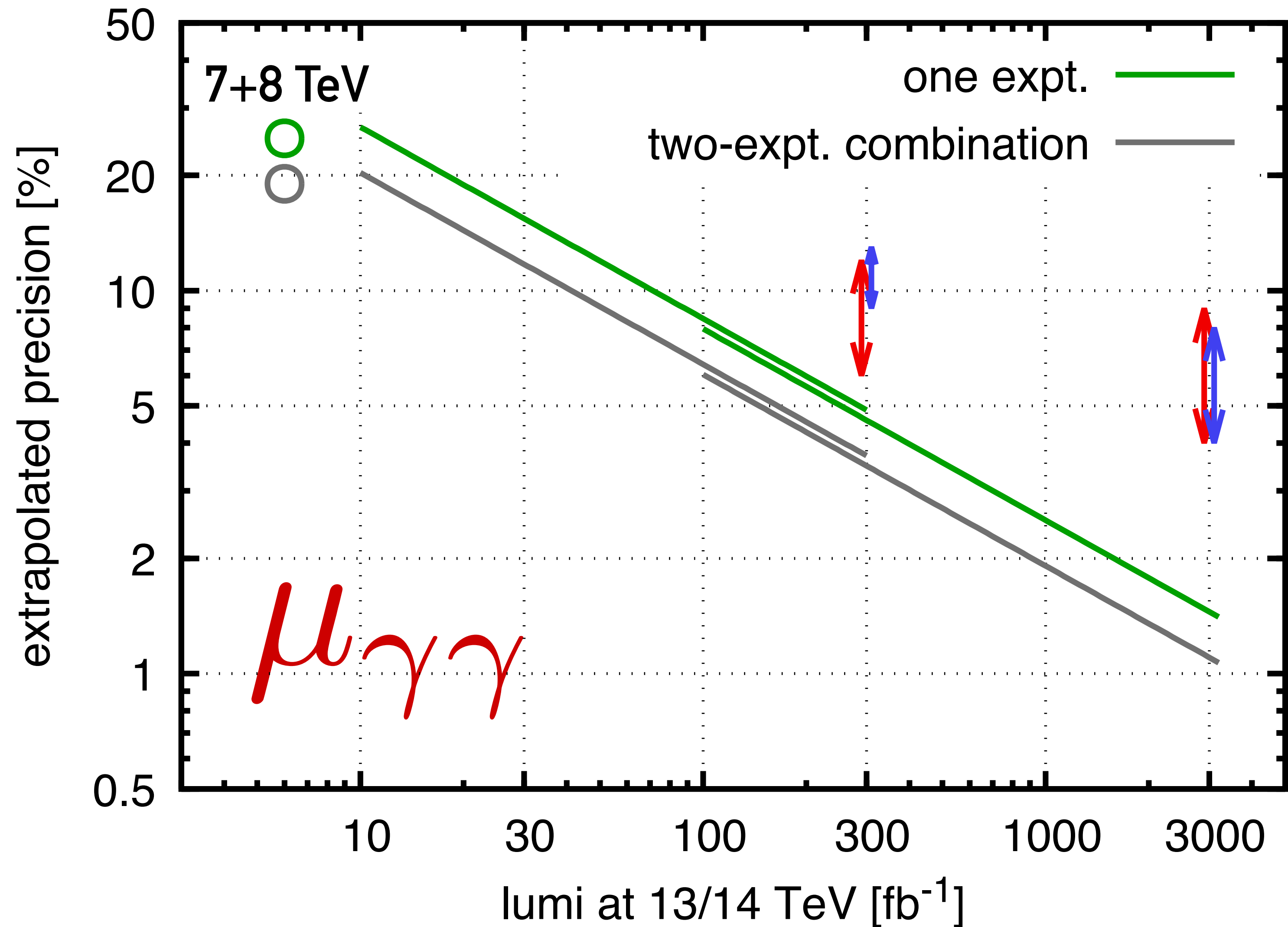
This progress is essential for LHC precision physics, but also only part of the story.

The intention with this talk?

Start asking questions about what precision goals we might set ourselves, what obstacles we will meet, what techniques and measurements might help us progress

**What precision should we
have as a target?**

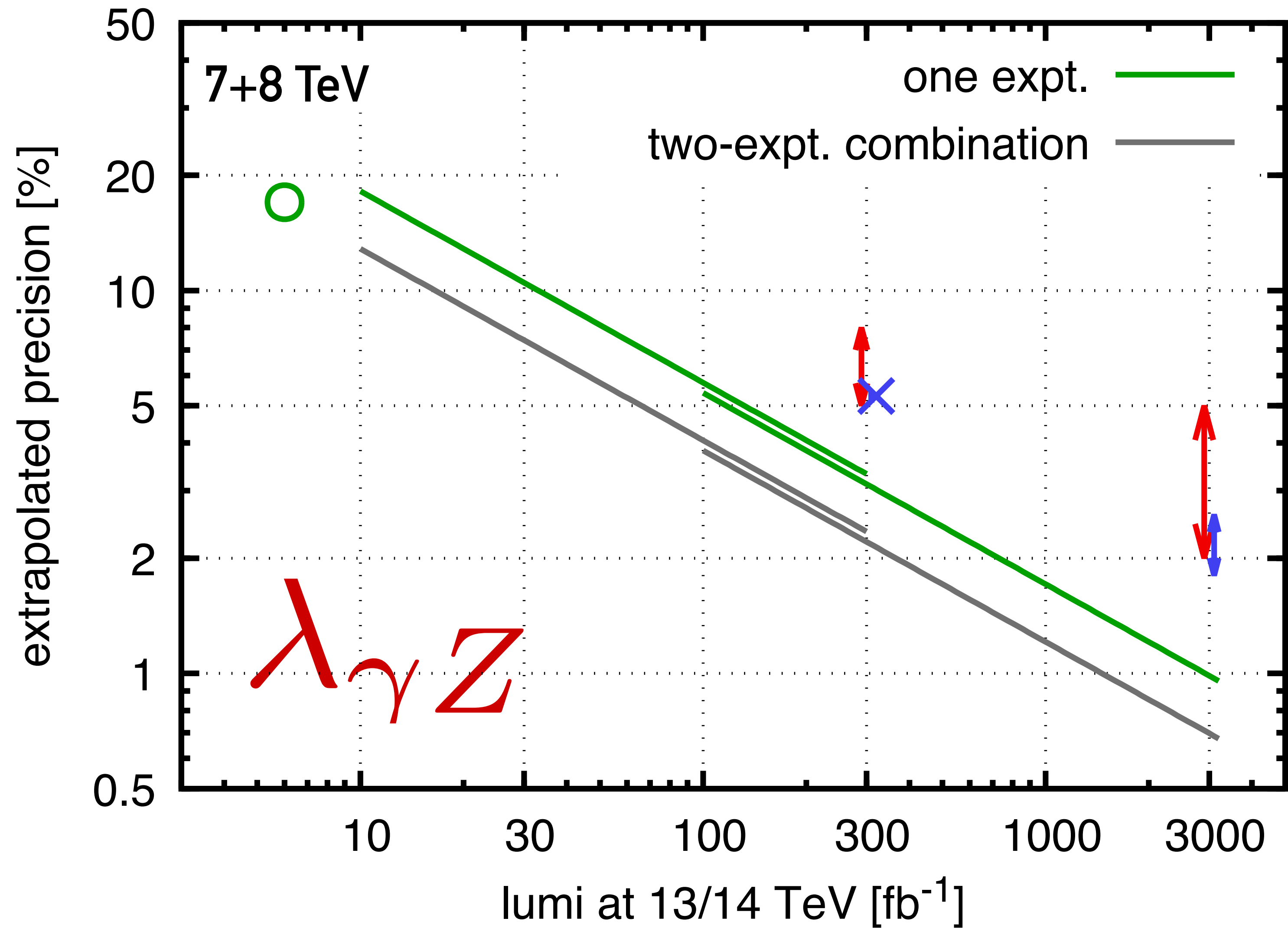
NAIVELY EXTRAPOLATE 7+8 TEV HIGGS RESULTS (based on lumi and σ)



CMS \updownarrow *today's TH syst.*
ATLAS \updownarrow *50% TH syst.*
no TH syst.

Extrapolation suggests that we get “precision” value from full lumi only if we aim for $O(1\%)$ or better precision

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DI-HIGGS PRODUCTION AT HL-LHC ($HH \rightarrow 4b, 3ab^{-1}$)

Behr, Bortoletto, Frost, Hartland, Issever & Rojo, 1512.08928

Category		signal	background		$S/\sqrt{B_{\text{tot}}}$	$S/\sqrt{B_{4b}}$	S/B_{tot}	S/B_{4b}
		N_{ev}	$N_{\text{ev}}^{\text{tot}}$	N_{ev}^{4b}				
Boosted	no PU	290	$1.2 \cdot 10^4$	$8.0 \cdot 10^3$	2.7	3.2	0.03	0.04
	PU80+SK+Trim	290	$3.7 \cdot 10^4$	$1.2 \cdot 10^4$	1.5	2.7	0.01	0.02
Intermediate	no PU	130	$3.1 \cdot 10^3$	$1.5 \cdot 10^3$	2.3	3.3	0.04	0.08
	PU80+SK+Trim	140	$5.6 \cdot 10^3$	$2.4 \cdot 10^3$	1.9	2.9	0.03	0.06
Resolved	no PU	630	$1.1 \cdot 10^5$	$5.8 \cdot 10^4$	1.9	2.7	0.01	0.01
	PU80+SK	640	$1.0 \cdot 10^5$	$7.0 \cdot 10^4$	2.0	2.6	0.01	0.01
Combined	no PU				4.0	5.3		
	PU80+SK+Trim				3.1	4.7		

Key signal channels will need ~1% control of complex bkgds

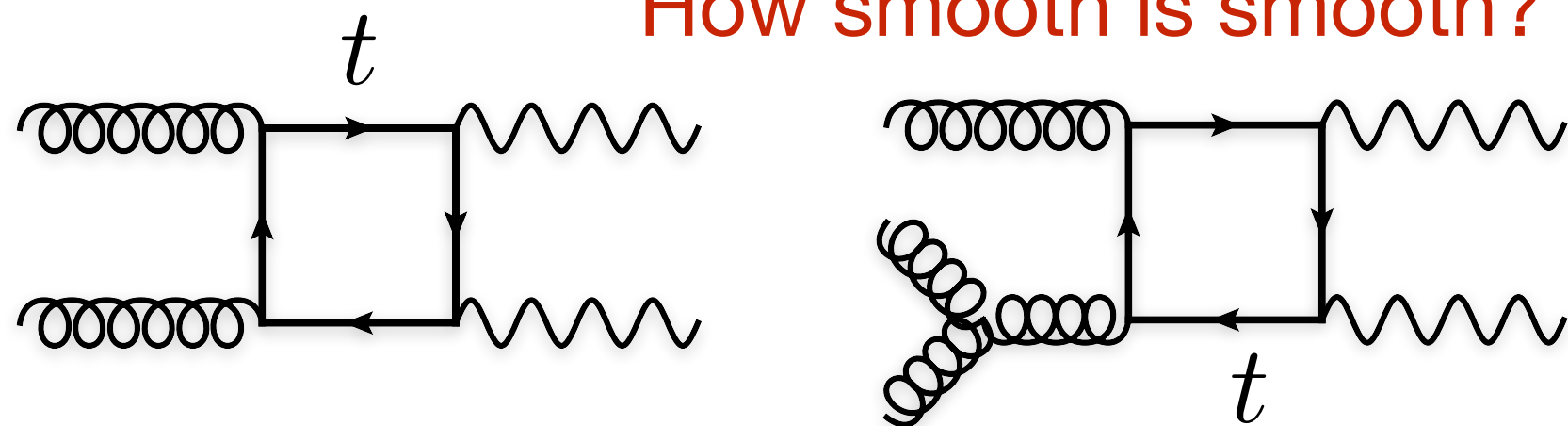
DATA-DRIVEN BKGD ESTIMATES: NON-SMOOTHNESS AT 1% LEVEL



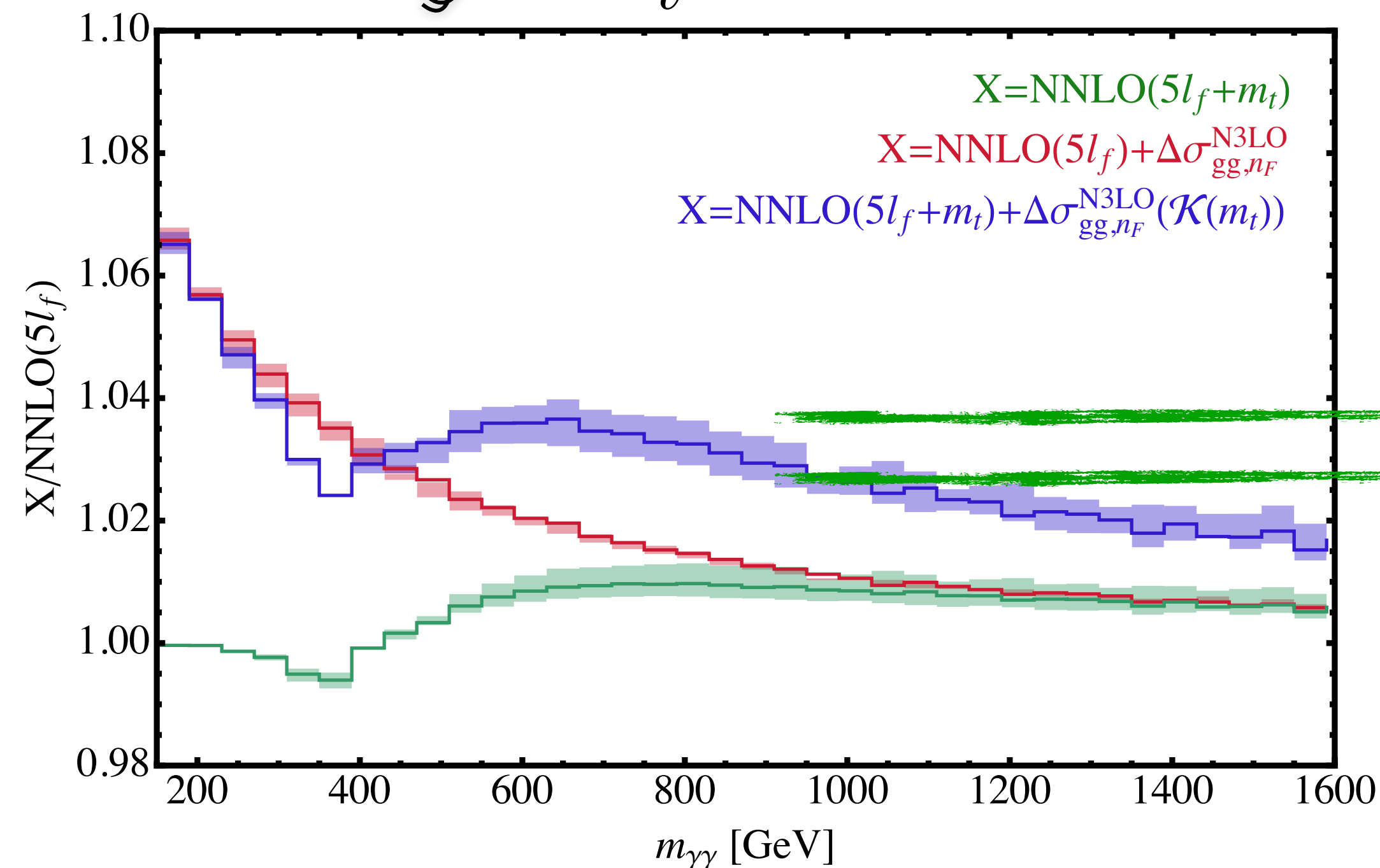
Predictions at high invariant masses.

As we all know, bump hunts in the diphoton system assume a smooth function which can be fitted to the data. Begging the question,

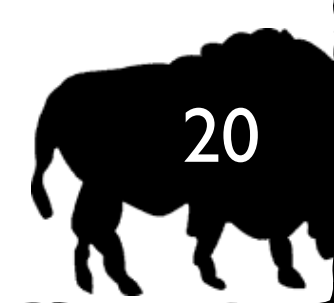
How smooth is smooth? :-)



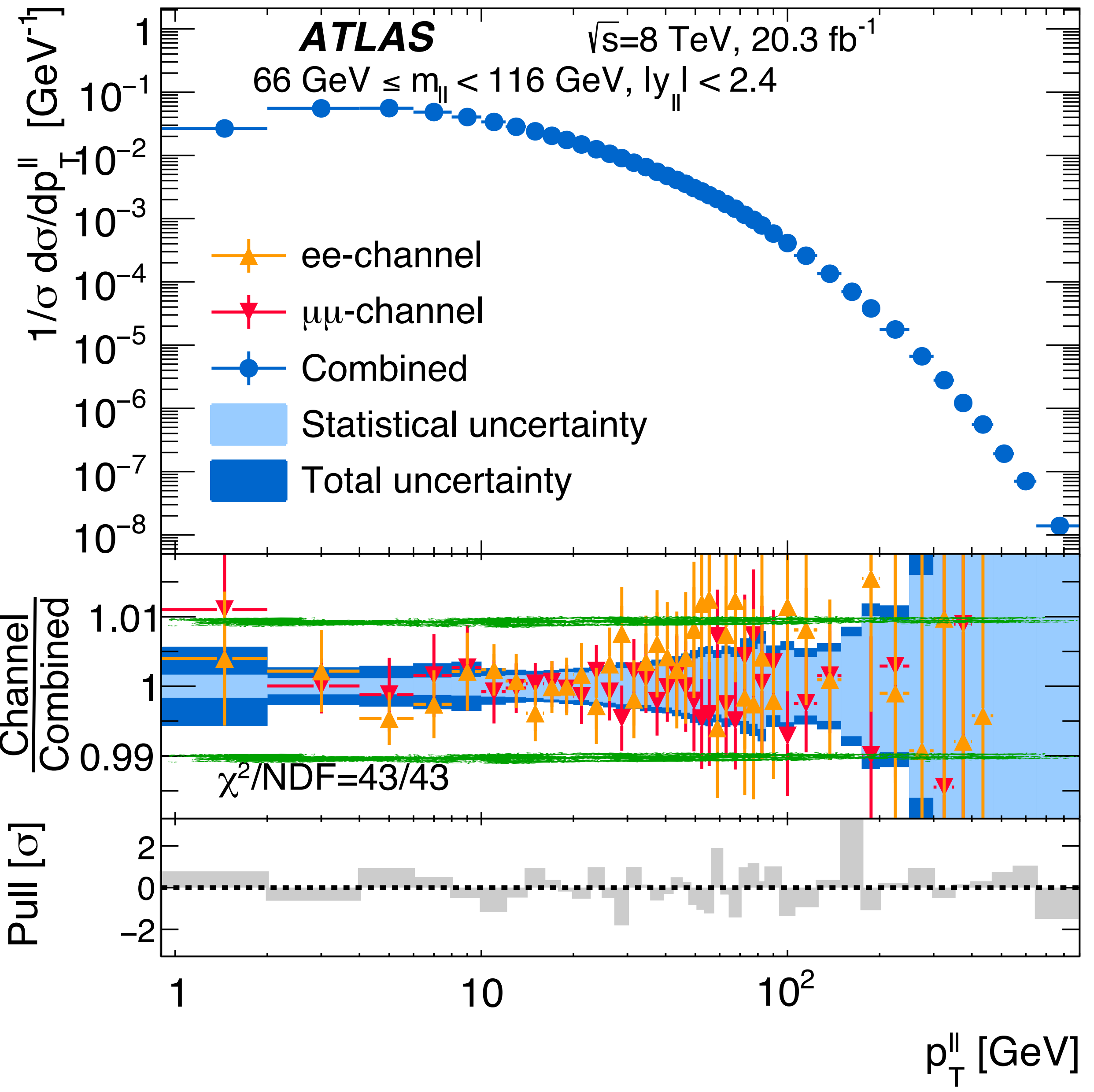
*C. Williams
Moriond QCD '16*



1%



Standard experimental techniques, like data-driven bkgd estimates, can be skewed by 0(1%) theoretical subtleties.



WHAT'S POSSIBLE EXPERIMENTALLY?

Today's most precise results are perhaps for the Z transverse momentum

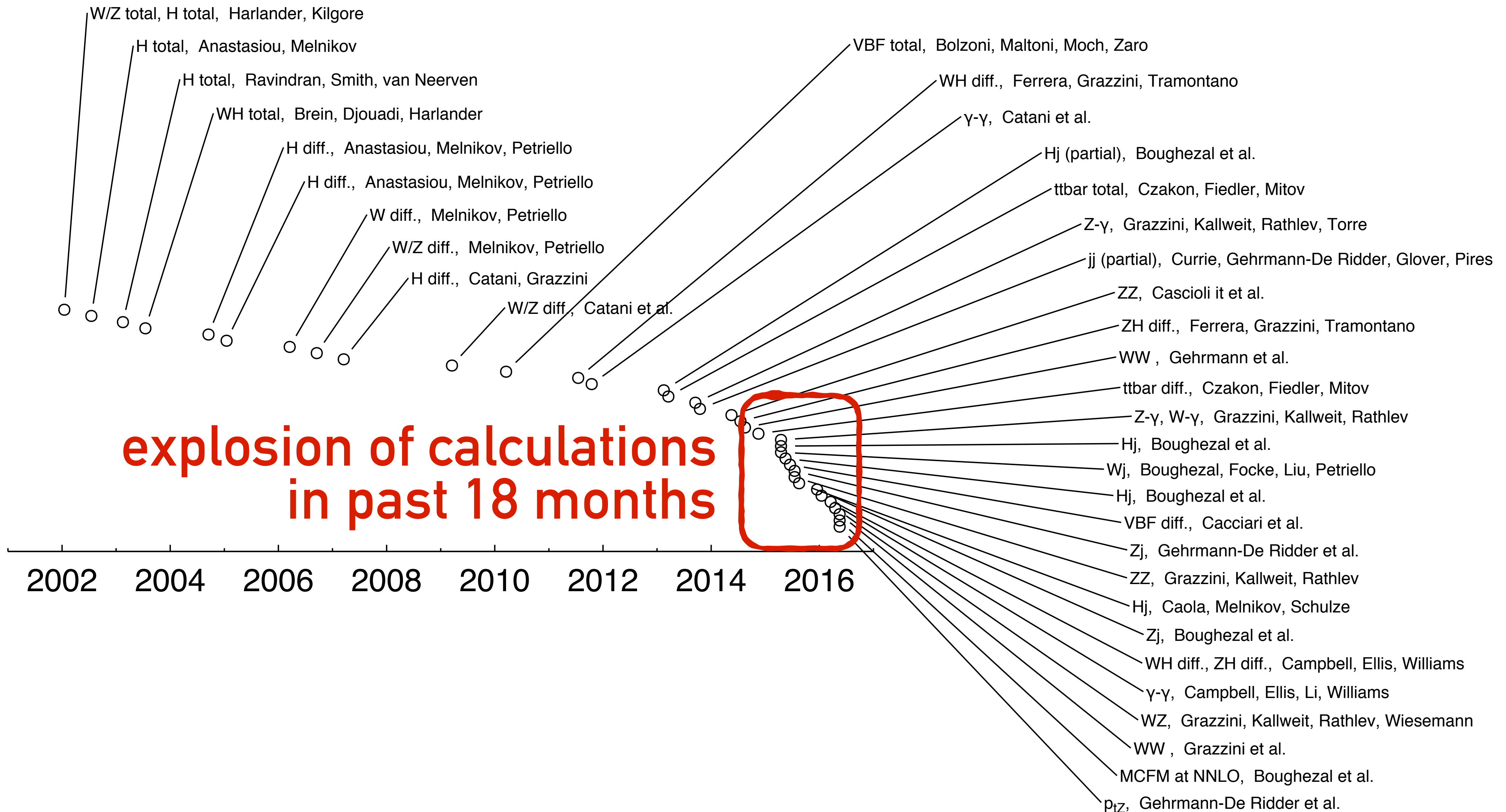
- normalised to Z fiducal σ
- achieves $<1\%$, from $p_T = 1$ to 200 GeV

$\pm 1\%$

Ratio to total cross section cancels lumi & some lepton-efficiency systematics.

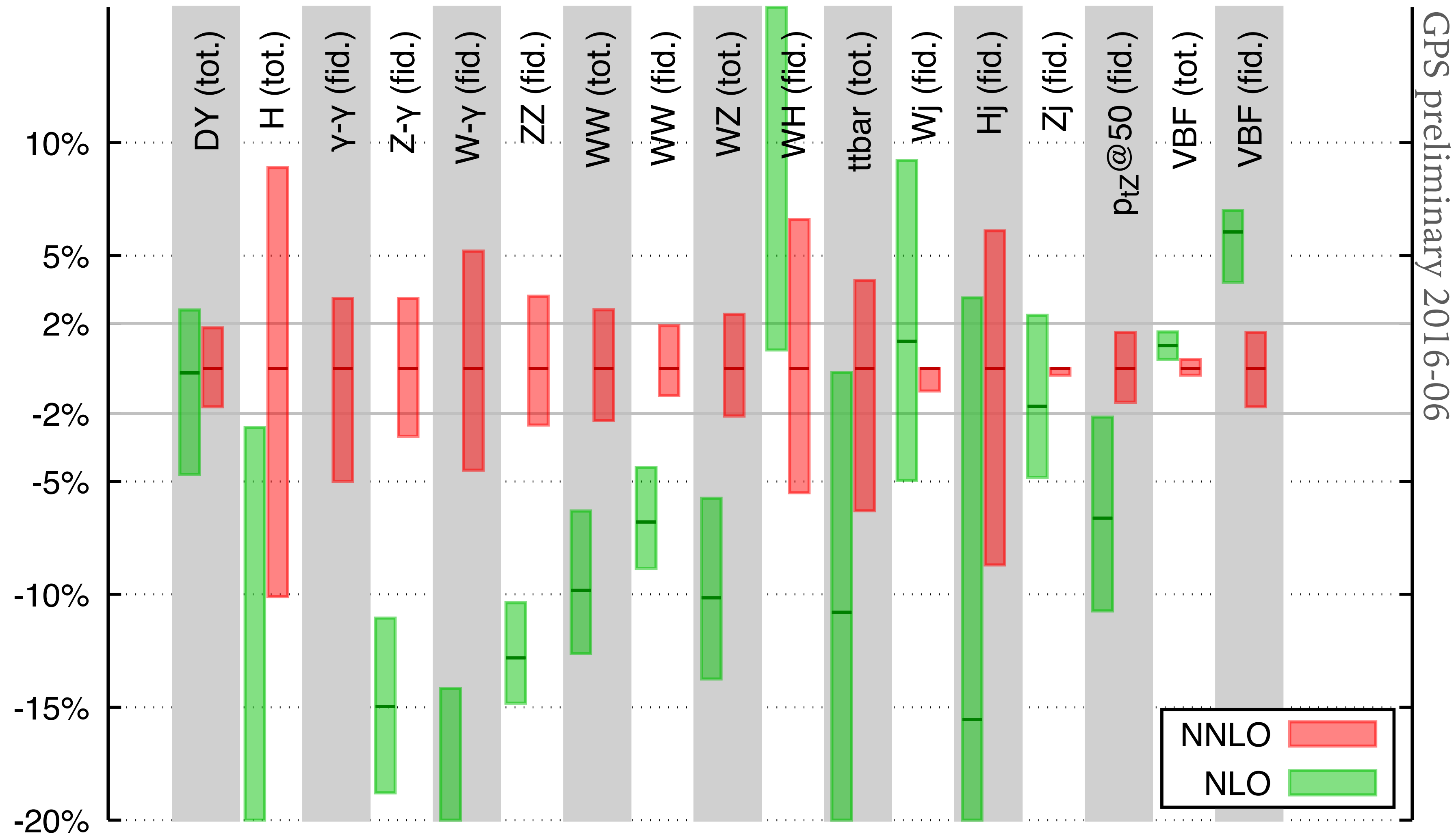
NNLO hadron-collider calculations v. time

as of mid June



**explosion of calculations
in past 18 months**

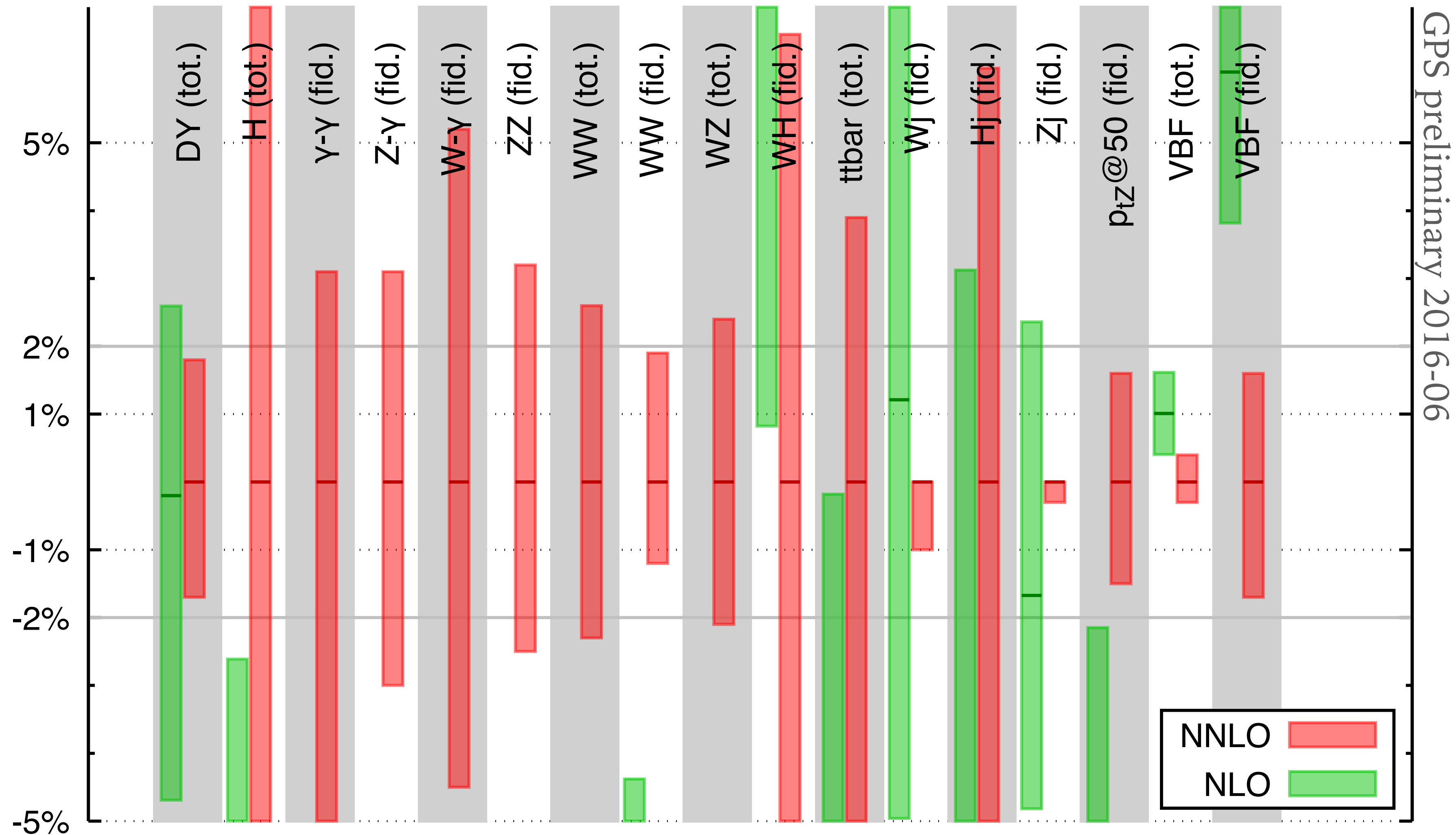
WHAT PRECISION AT NNLO?



For many processes NNLO scale band is $\sim \pm 2\%$

Though only in 3/17 cases is NNLO (central) within NLO scale band...

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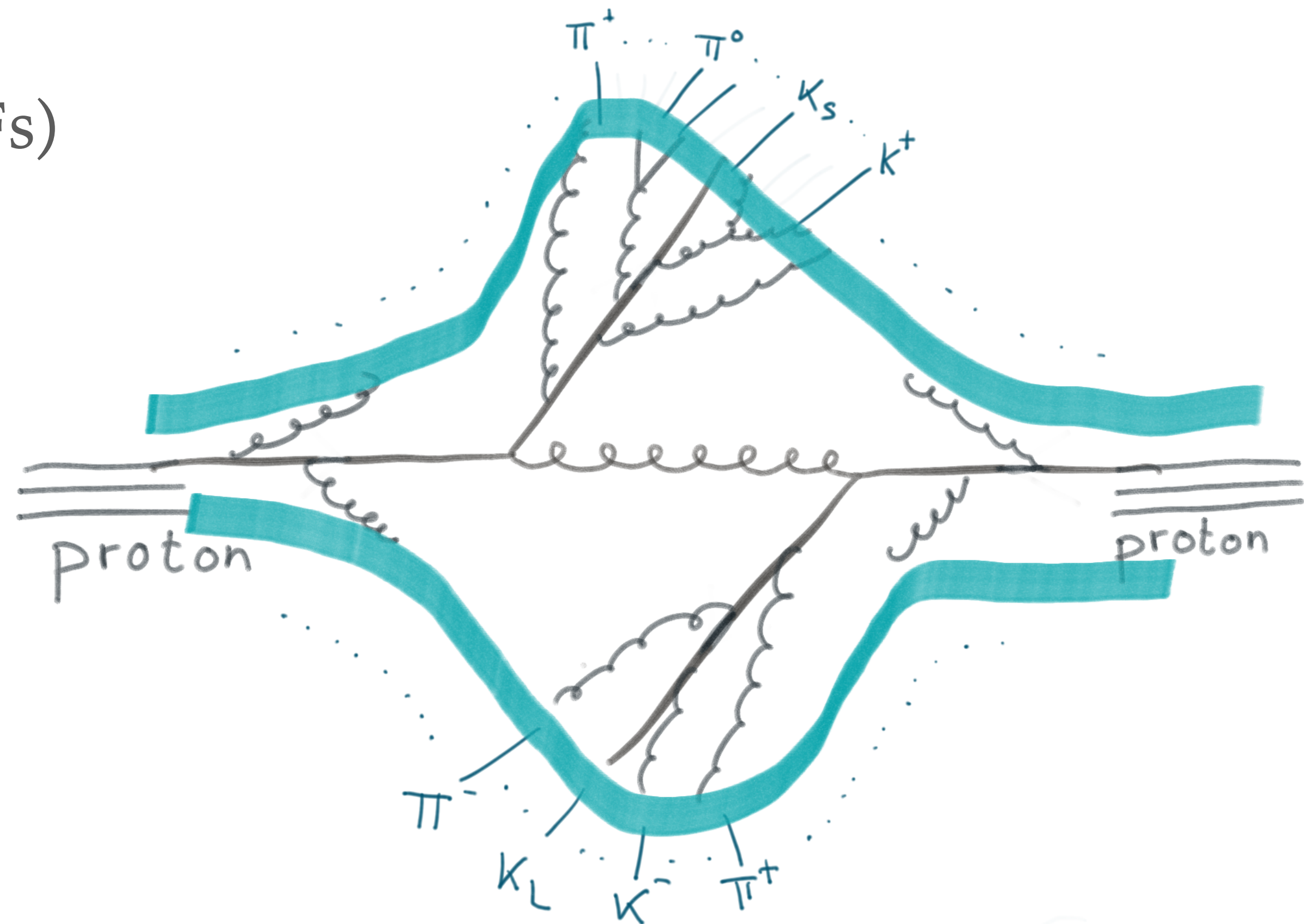
OVERALL, 1% SEEMS AN INTERESTING FIGURE TO HAVE IN MIND

To start thinking about getting there, let's work through the **"inputs"**:

- the strong coupling
- parton distribution functions (PDFs)

And the **types of process**:

- inclusive / purely leptonic
- processes with jets



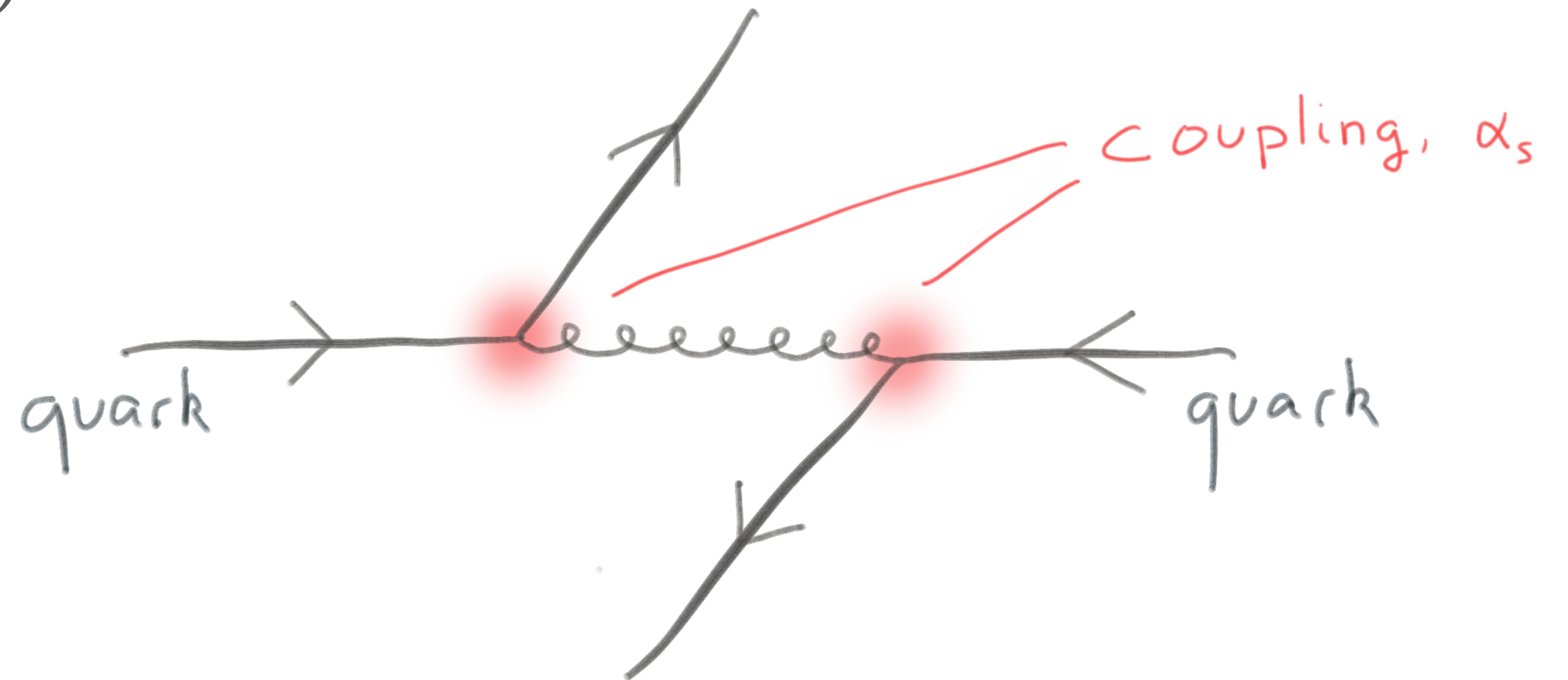
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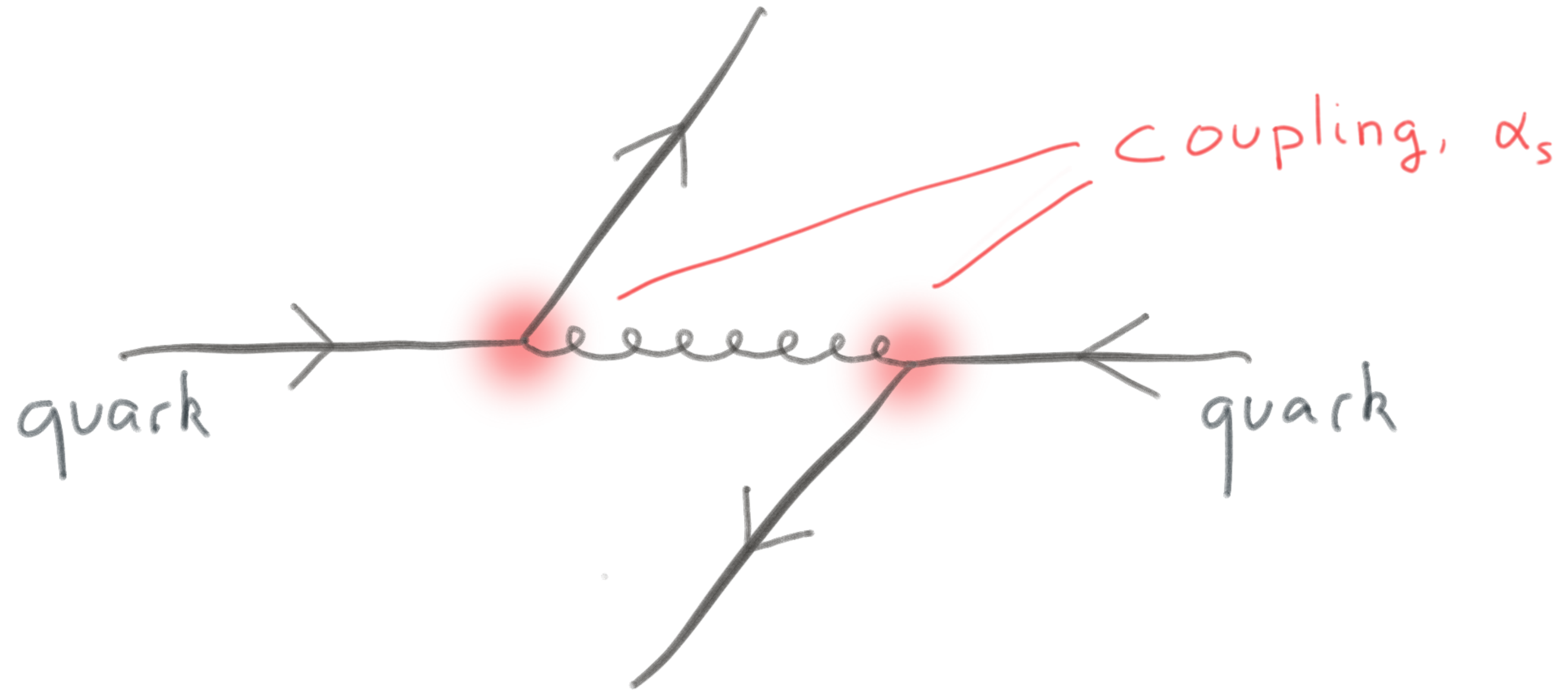
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The strong coupling: α_s

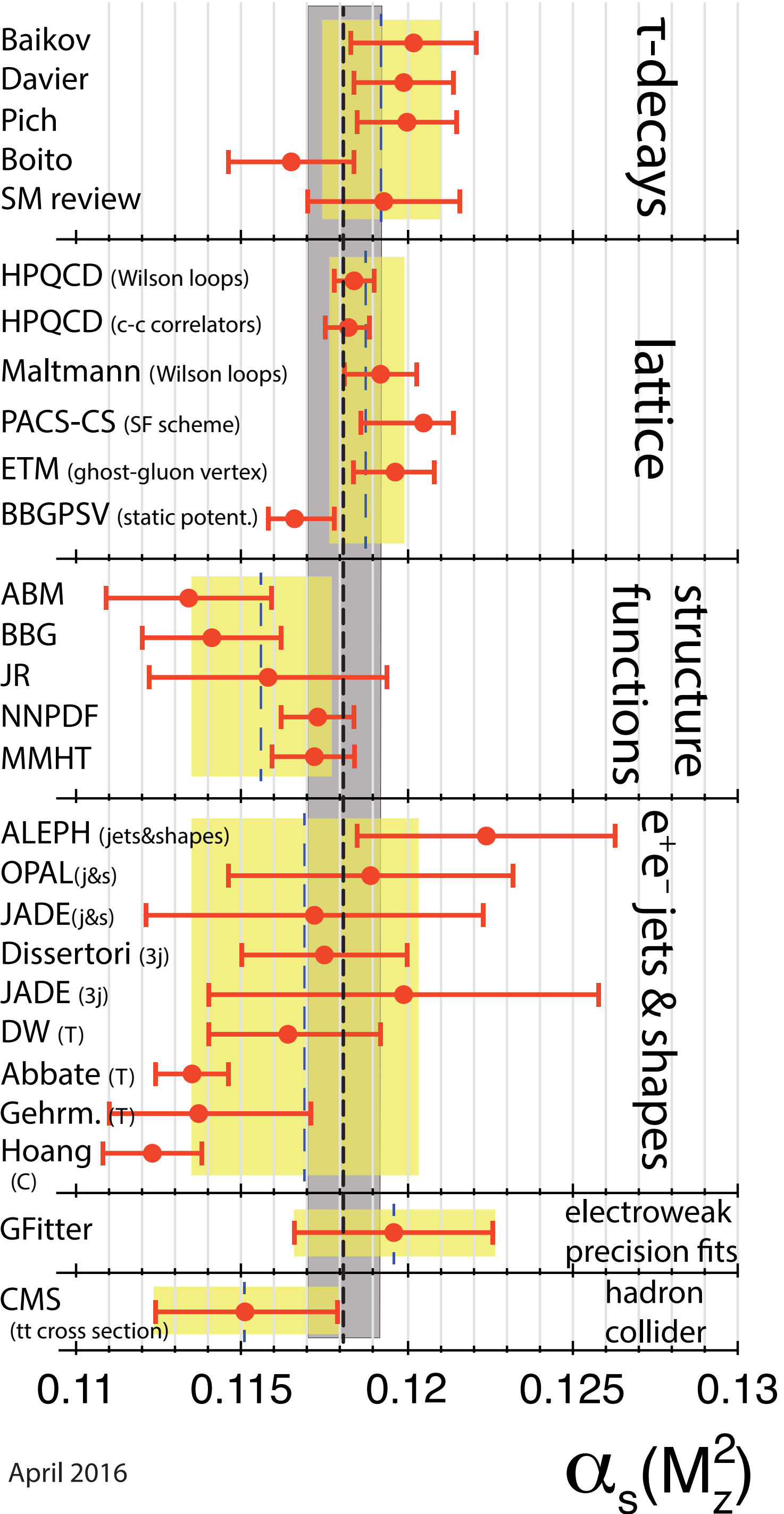


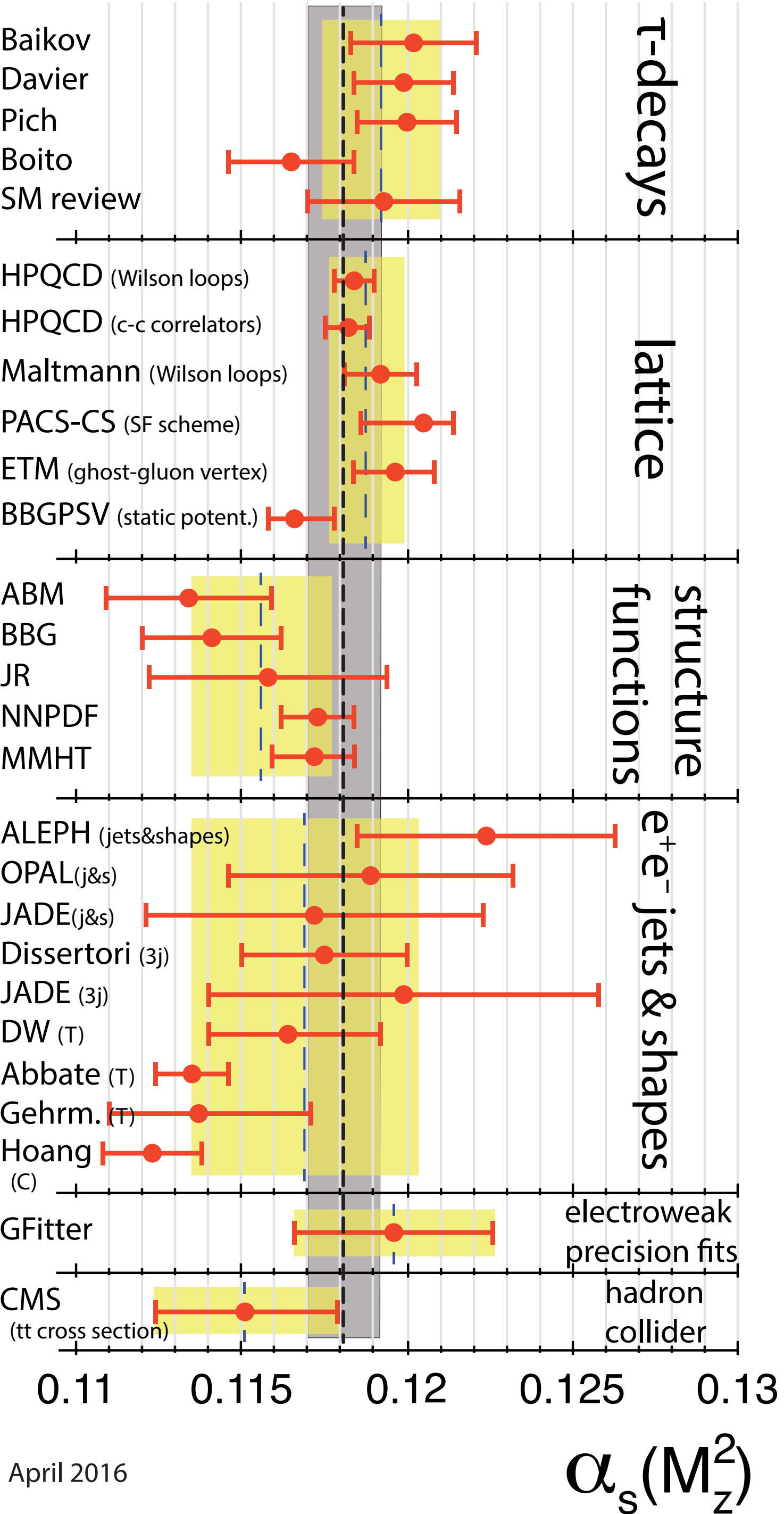
*(almost) all theory predictions for LHC are based on
perturbation theory, e.g.*

$$\sigma = a_s \sigma_1 + a_s^2 \sigma_2 + \dots$$

PDG World Average: $\alpha_s(M_Z) = 0.1181 \pm 0.0011$ (0.9%)

Bethke, Dissertori & GPS in PDG '16





PDG World Average: $\alpha_s(M_Z) = 0.1181 \pm 0.0011$ (0.9%)

- Most consistent set of independent determinations is from lattice
- Two best determinations are from same group (HPQCD, 1004.4285, 1408.4169)

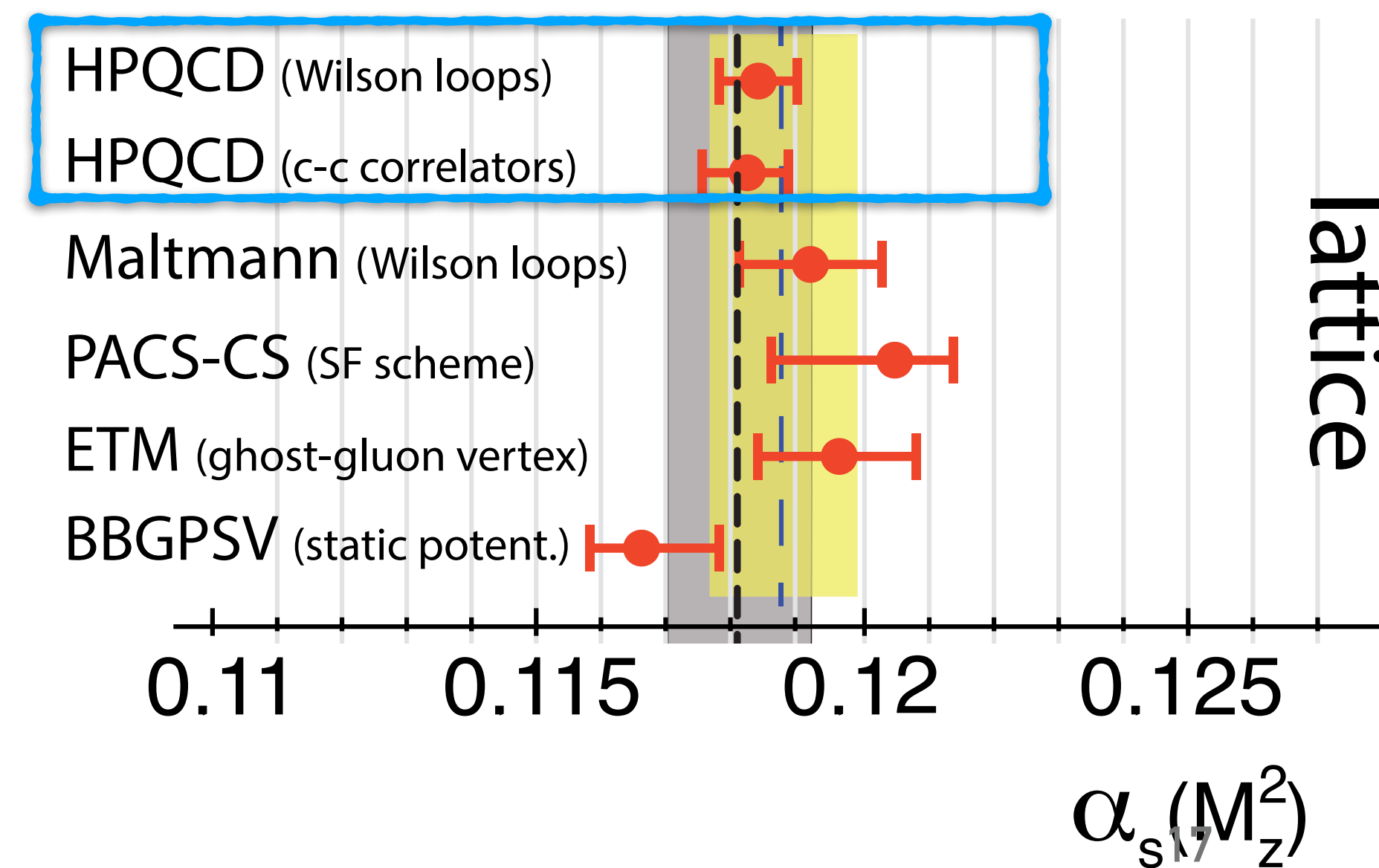
$\alpha_s(M_Z) = 0.1183 \pm 0.0007$ (0.6%) [heavy-quark correlators]

$\alpha_s(M_Z) = 0.1183 \pm 0.0007$ (0.6%) [Wilson loops]

- Error criticised by FLAG, who suggest

$\alpha_s(M_Z) = 0.1184 \pm 0.0012$ (1%)

- Worries include missing perturbative contributions, non-perturbative effects in 3–4 flavour transition at charm mass [addressed in some work], etc.



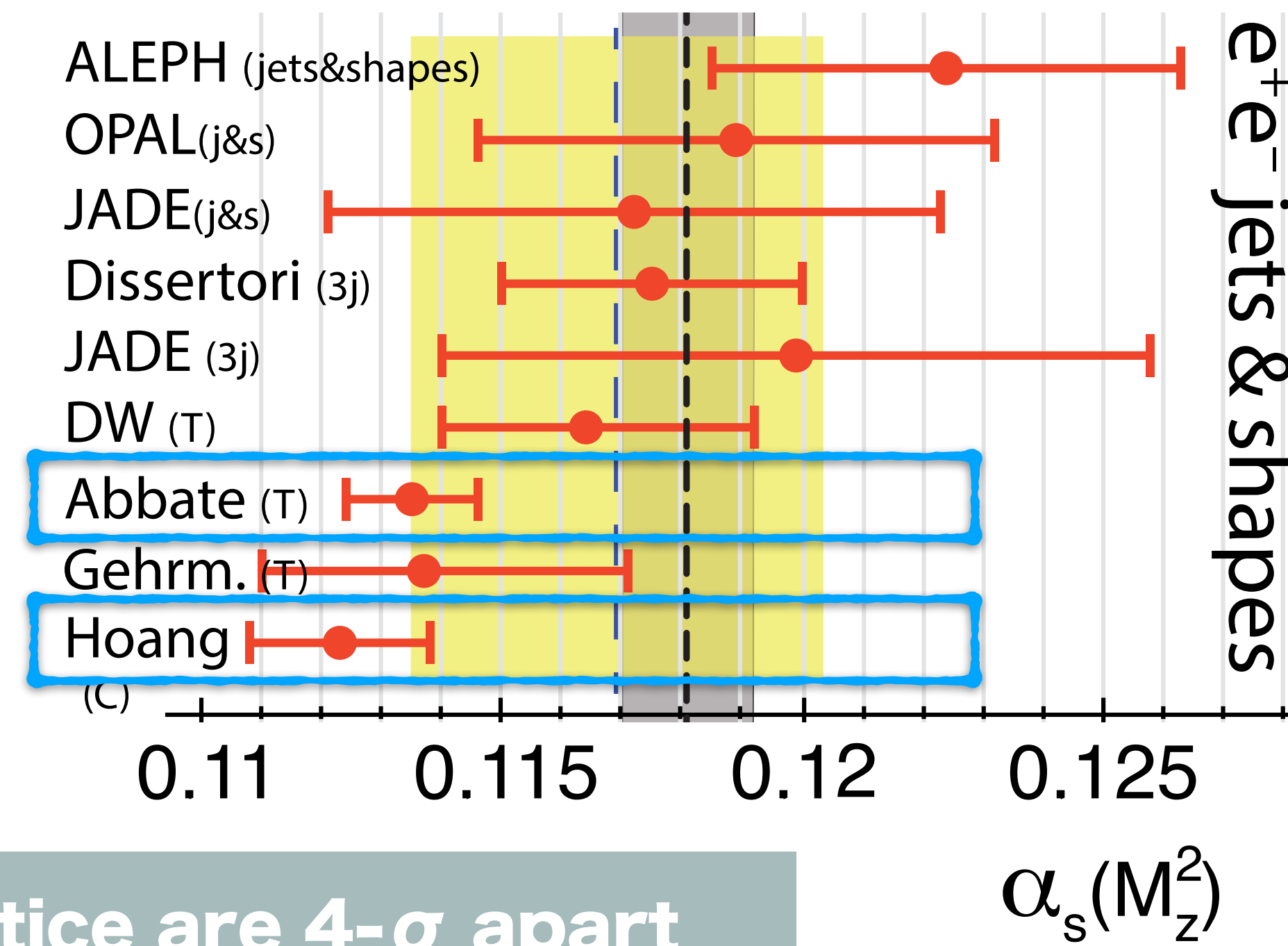
E+E- EVENT SHAPES AND JET RATES

- Two “best” determinations are from same group

(Hoang et al, 1006.3080, 1501.04111)

$$\alpha_s(M_Z) = 0.1135 \pm 0.0010 \text{ (0.9\%)} \text{ [thrust]}$$

$$\alpha_s(M_Z) = 0.1123 \pm 0.0015 \text{ (1.3\%)} \text{ [C-parameter]}$$



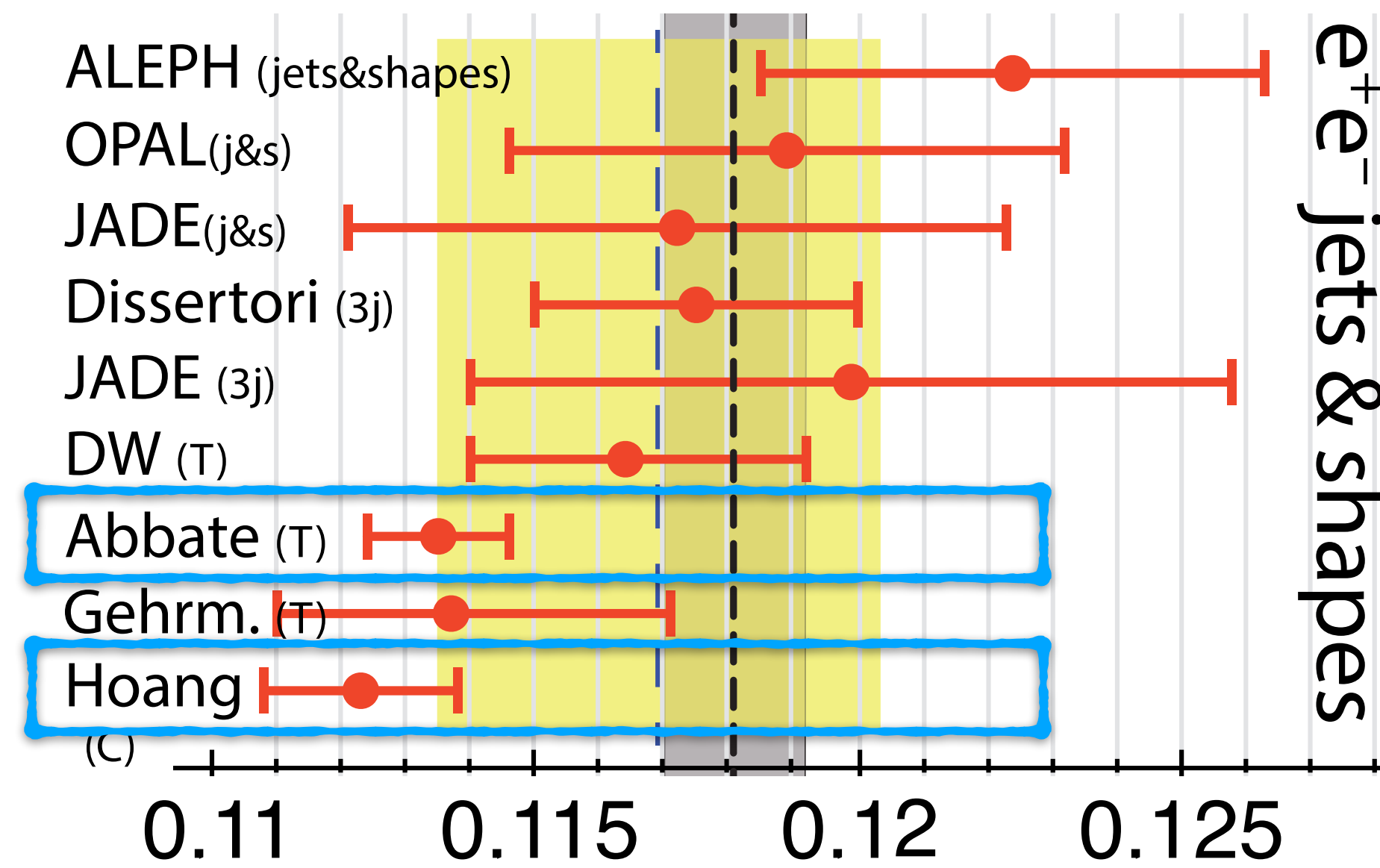
thrust & “best” lattice are 4- σ apart

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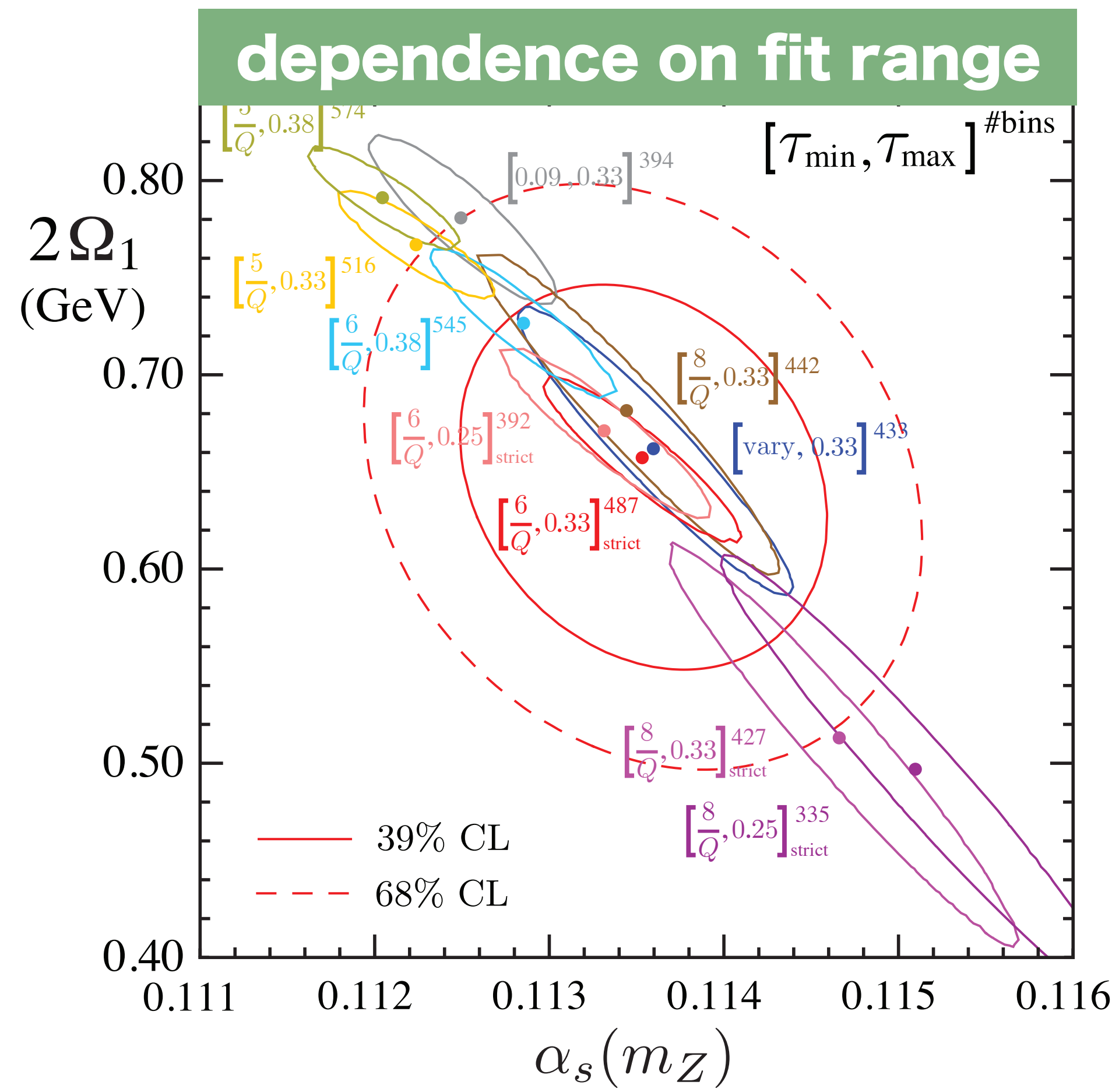
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thrust & “best” lattice are 4- σ apart

Comments:

- thrust & C-parameter are highly correlated observables
- Analysis valid far from 3-jet region, but not too deep into 2-jet region — at LEP, not clear how much of distribution satisfies this requirement
- thrust fit shows noticeable sensitivity to fit region (C-parameter doesn't)

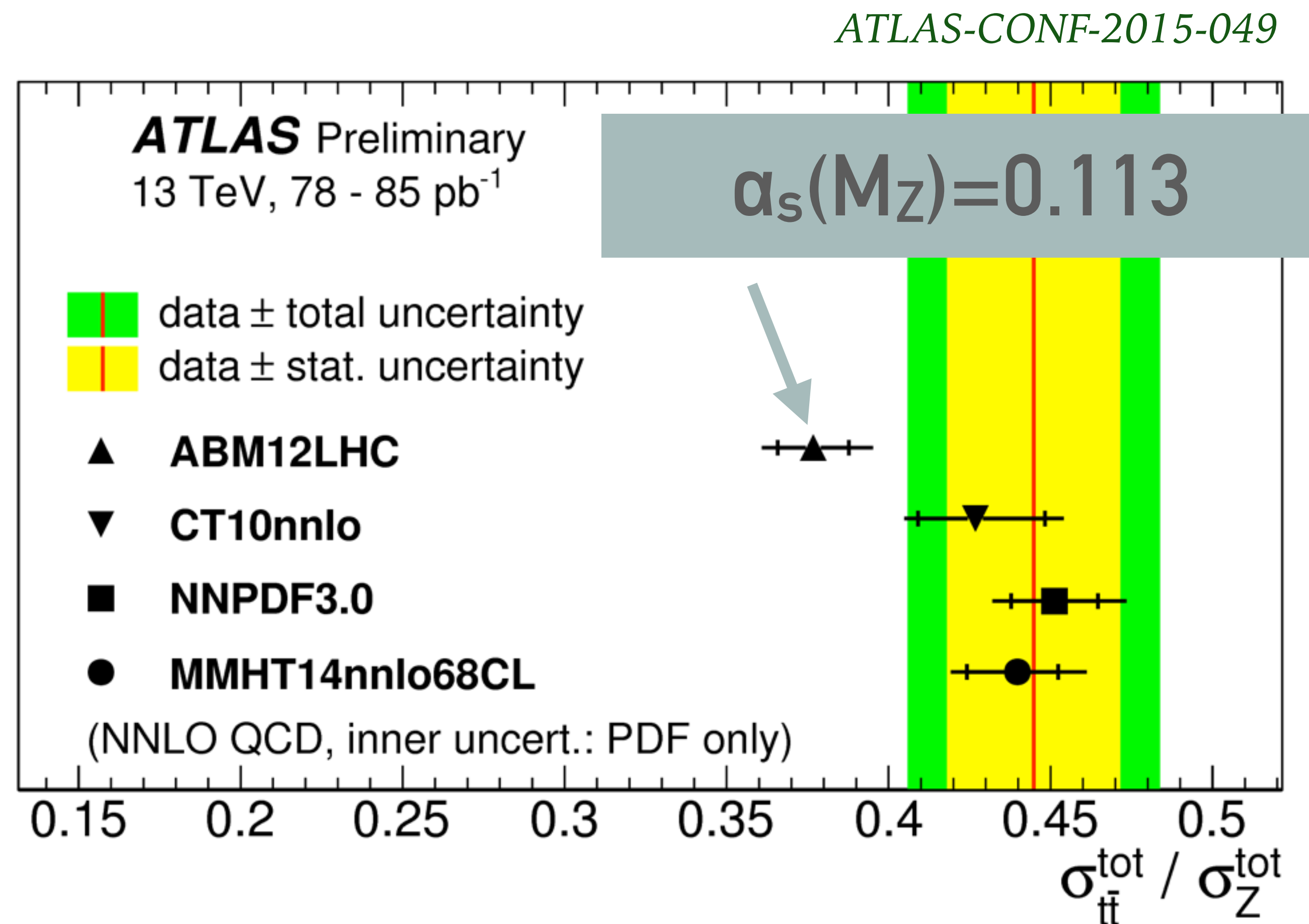


WHAT WAY FORWARD FOR α_s ?

- We need to settle question of whether “small” (0.113) α_s is possible.

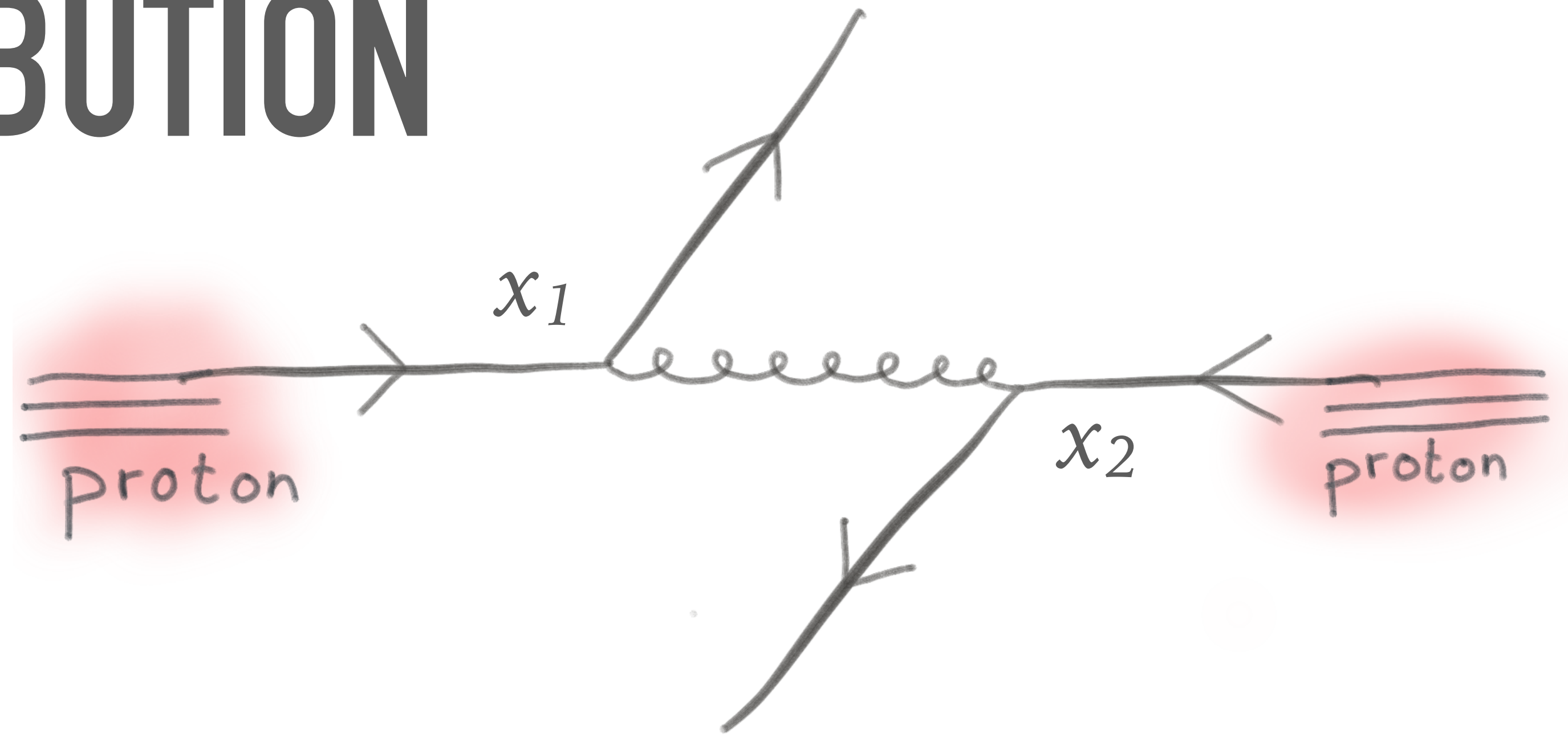
LHC data already weighing in on this (top data), further info in near future (Z p_T , cf. later slides)?

- To go beyond 1%, best hope is probably lattice QCD — on a 10-year timescale, there will likely be enough progress that multiple groups will have high-precision determinations



NB: top-quark mass choice affects this plot

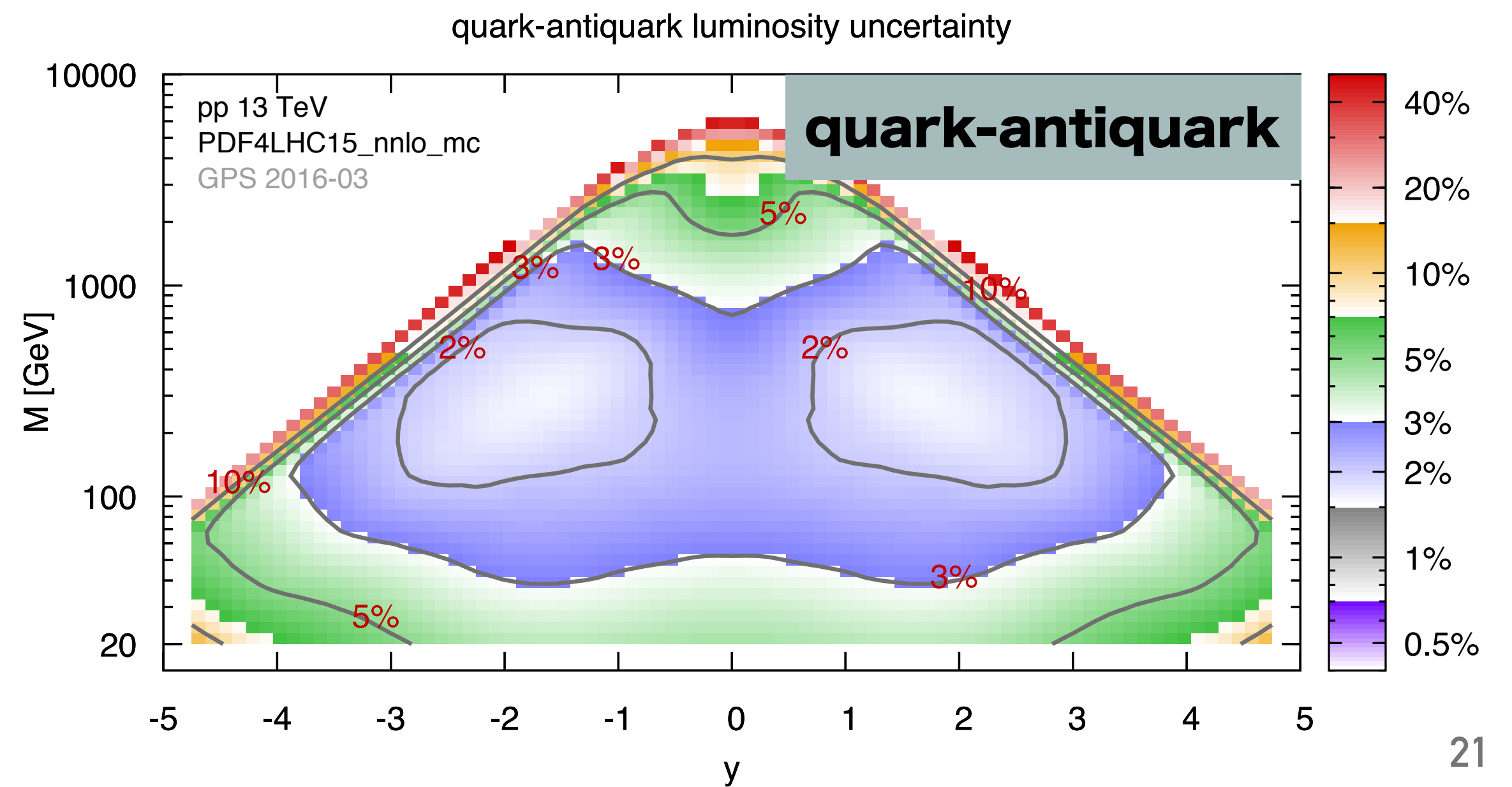
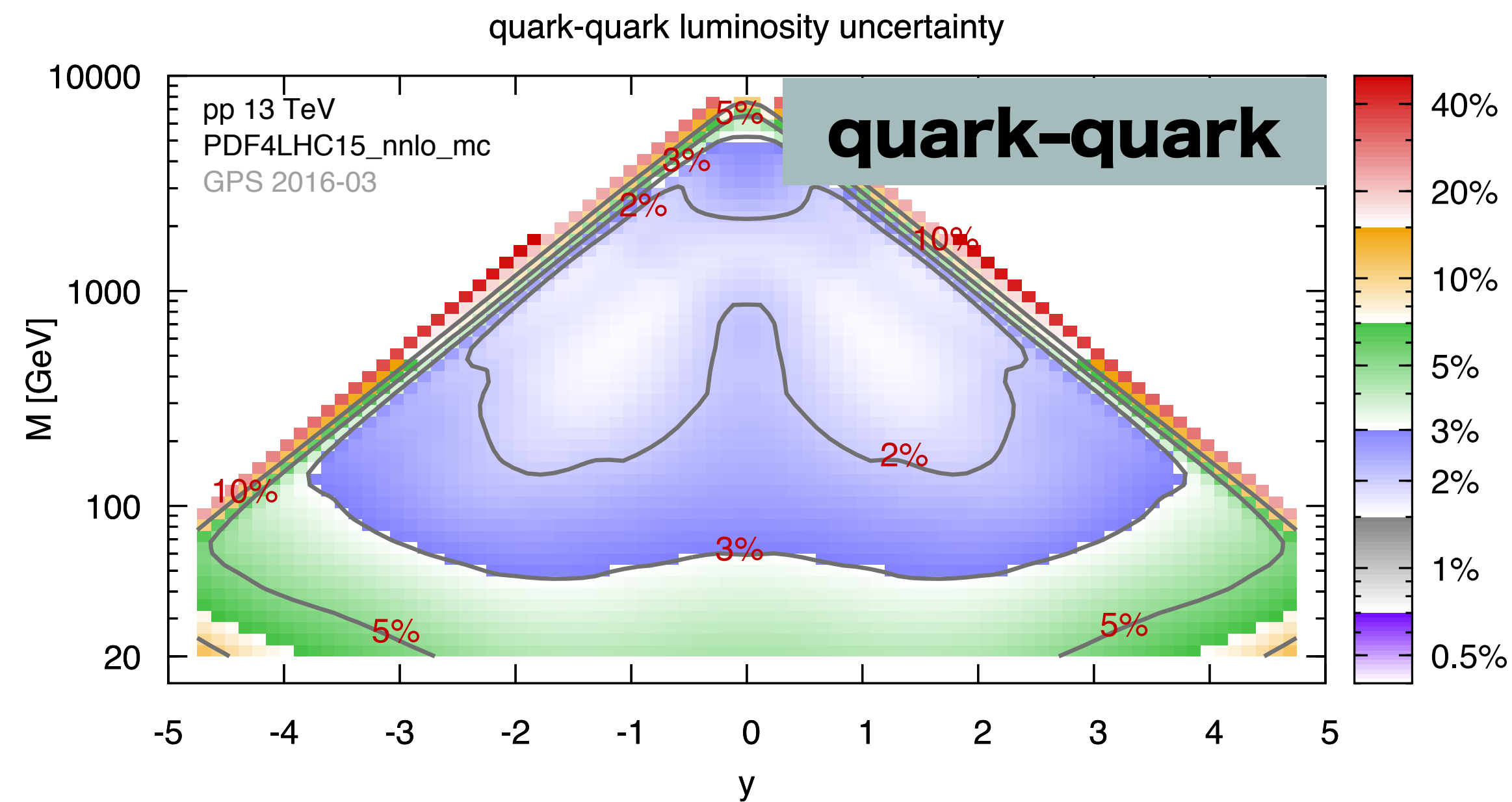
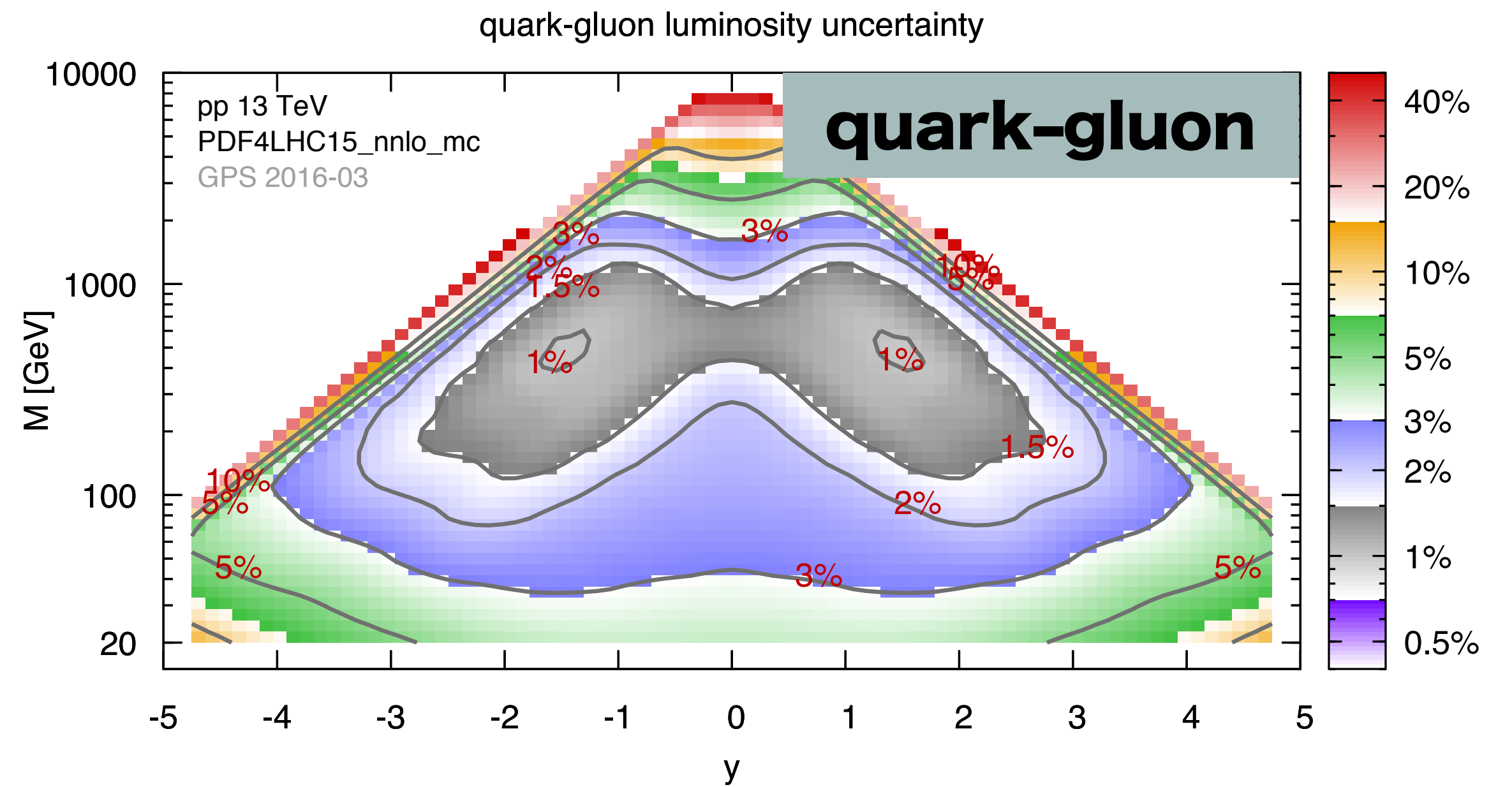
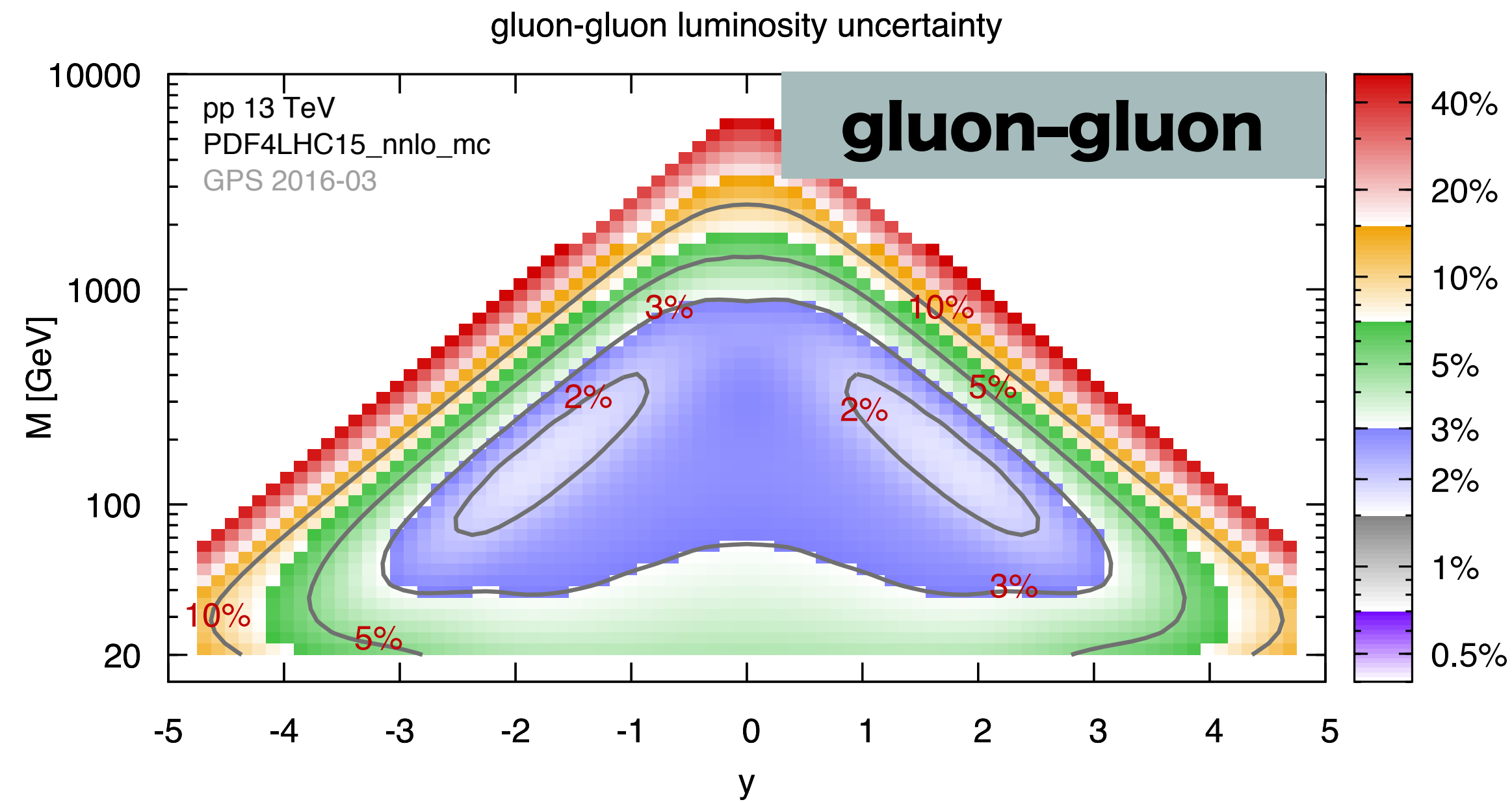
PARTON DISTRIBUTION FUNCTIONS (PDFs)



*how many quarks and gluons are there
carrying a fraction x of the proton's momentum?*

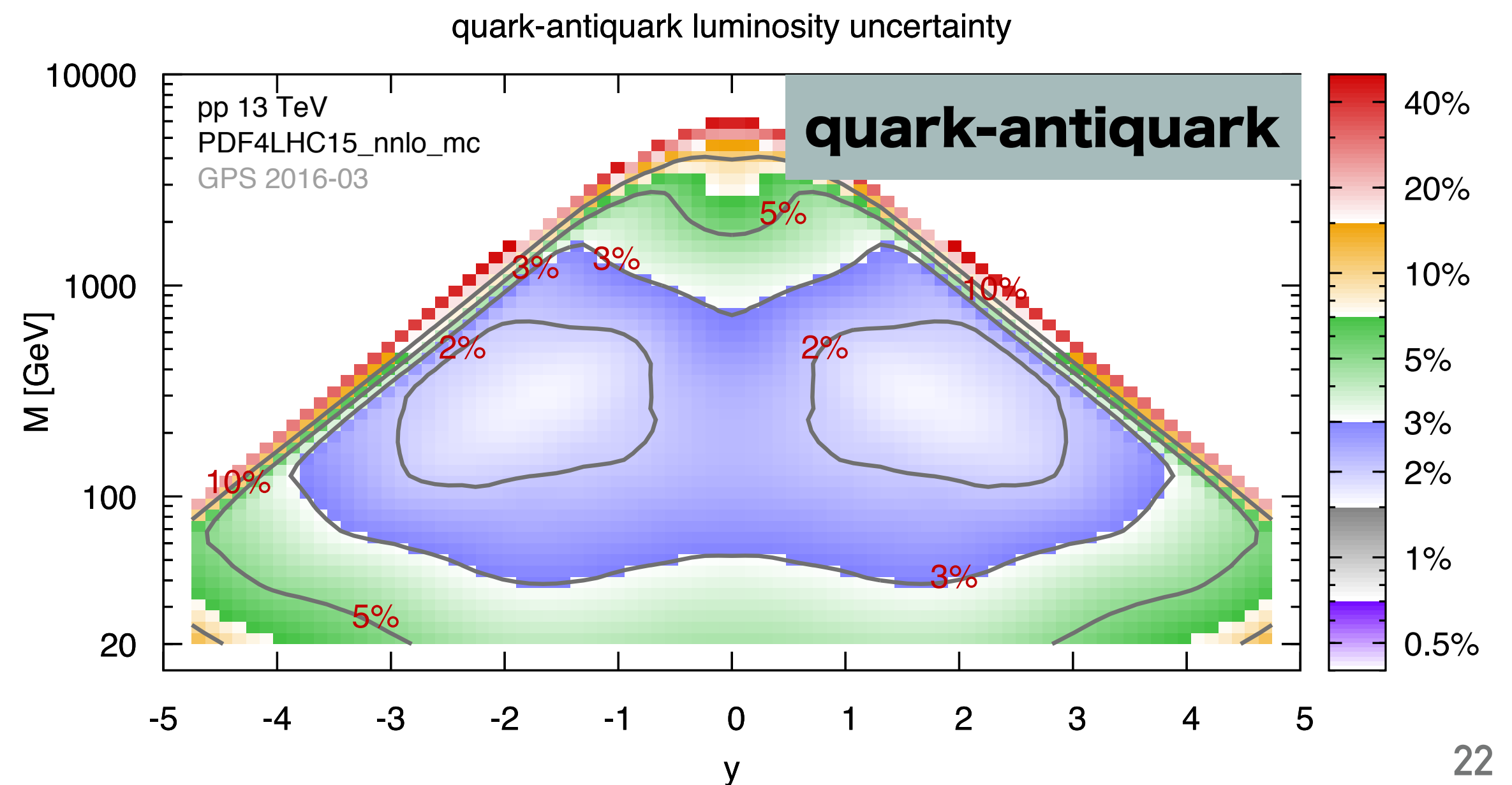
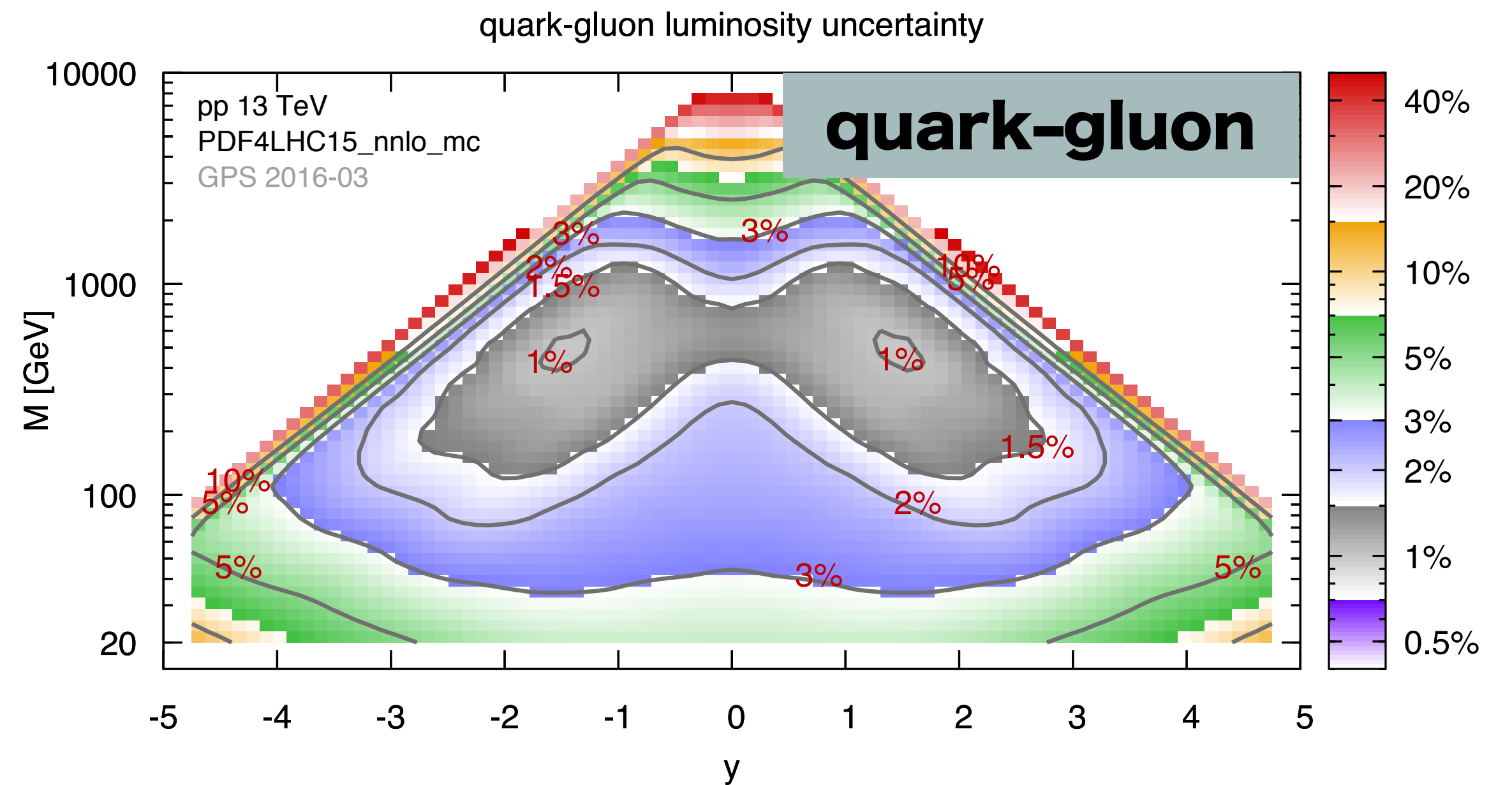
$$\sigma \propto f_{q/p}(x_1, \mu^2) f_{q/p}(x_2, \mu^2)$$

UNCERTAINTIES ON PARTONIC LUMINOSITIES — V. RAPIDITY(Y) AND MASS

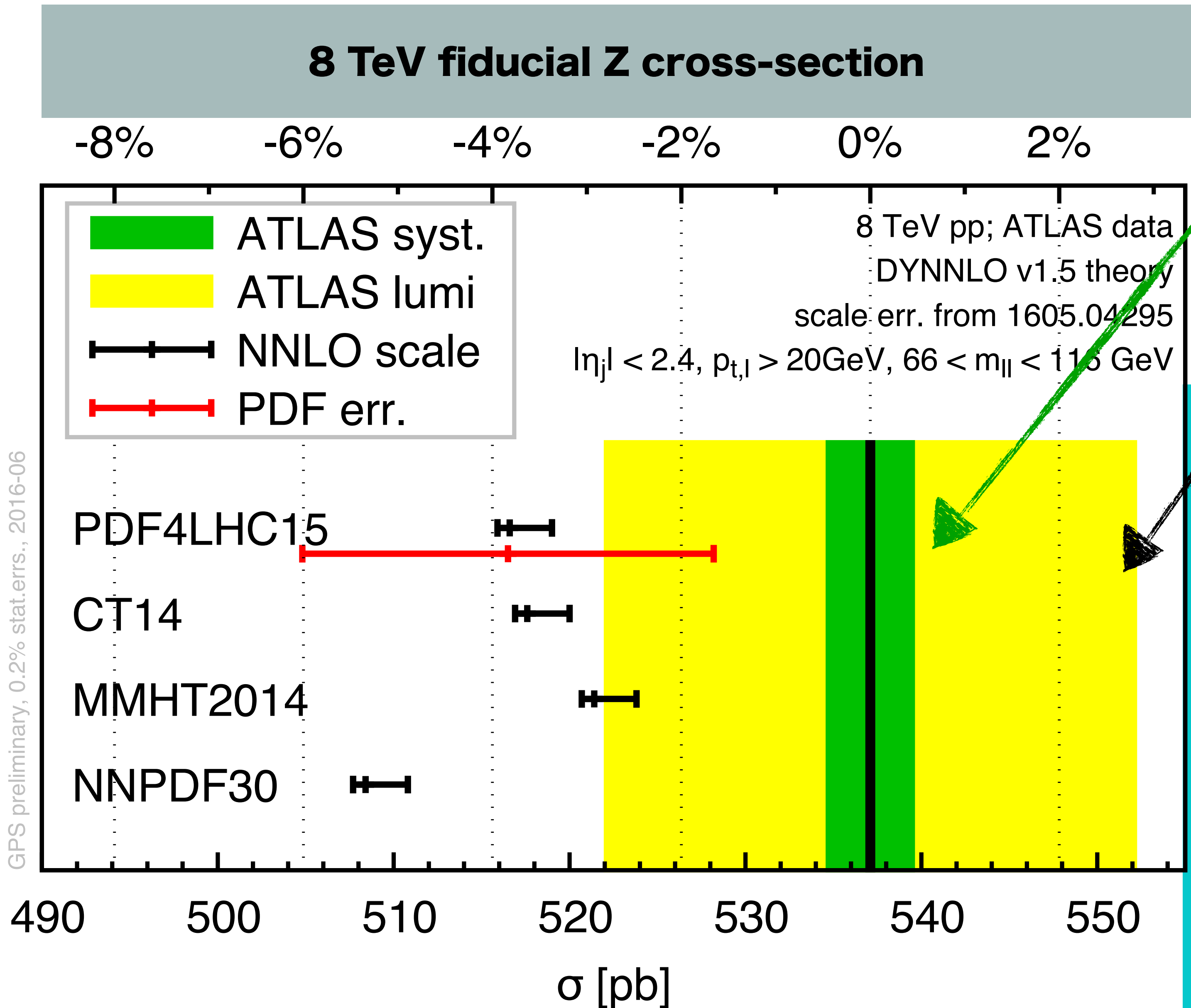


WHAT ROUTE FOR PROGRESS?

- Current status is 2–3% for core “precision” region
- Path to 1% is not clear — e.g. $Z p_T$'s strongest constraint is on qg lumi, which is already best known (why?)
- It'll be interesting to revisit the question once $t\bar{t}$, incl. jets, $Z p_T$, etc. have all been incorporated at NNLO
- Can expts. get **better lumi determination?**
- [is it time for PDFs to include theory uncertainties?]



There are, however, issues. Notably in Z production



$\pm 0.45\%$ syst. **$\times 6$**

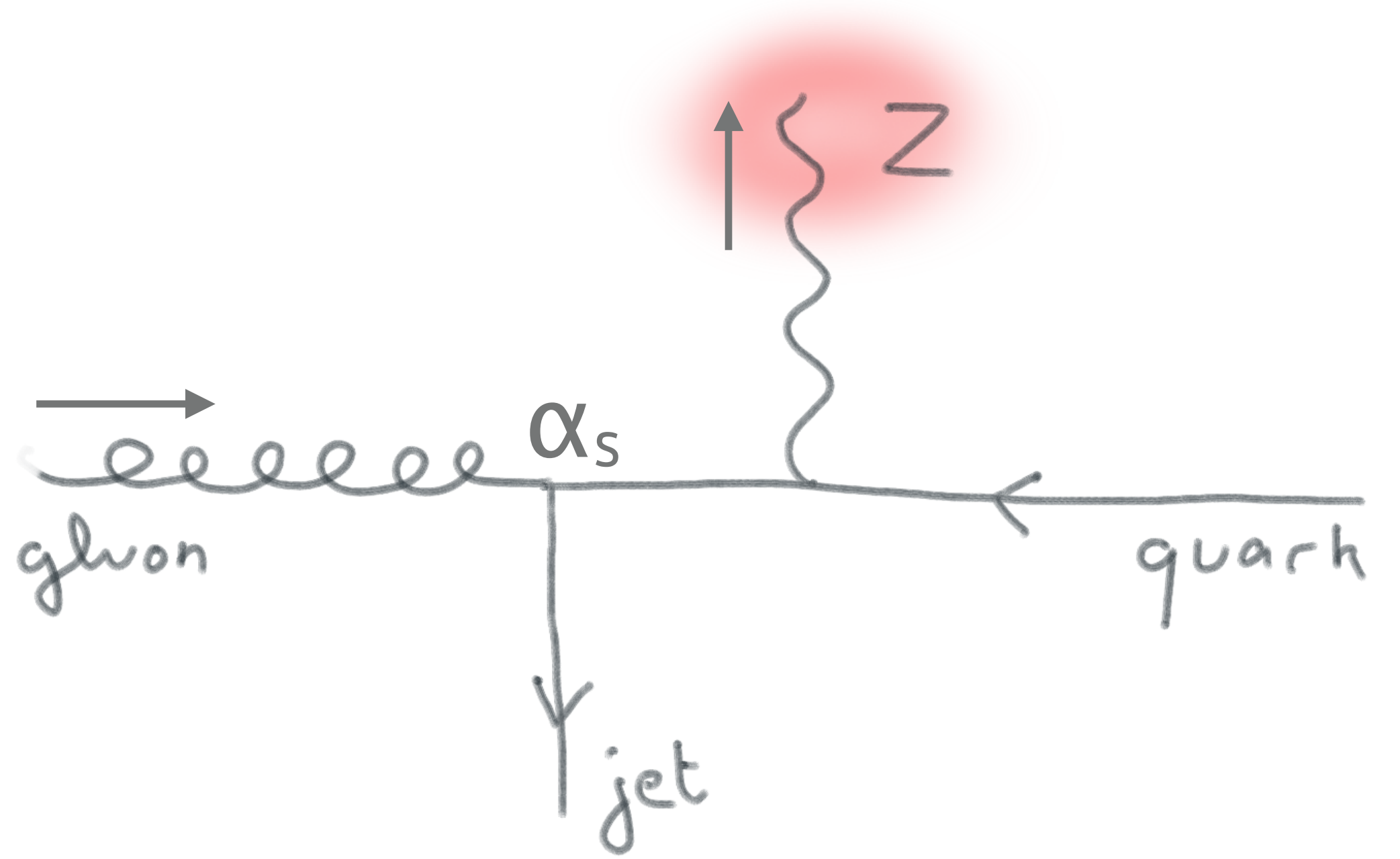
$\pm 2.8\%$ lumi

Up to 5% discrepancy with data

Experimental progress on luminosity determination may be the **keystone** for precision physics at LHC.

Are there hardware changes to HL-LHC that could help with lumi determination?

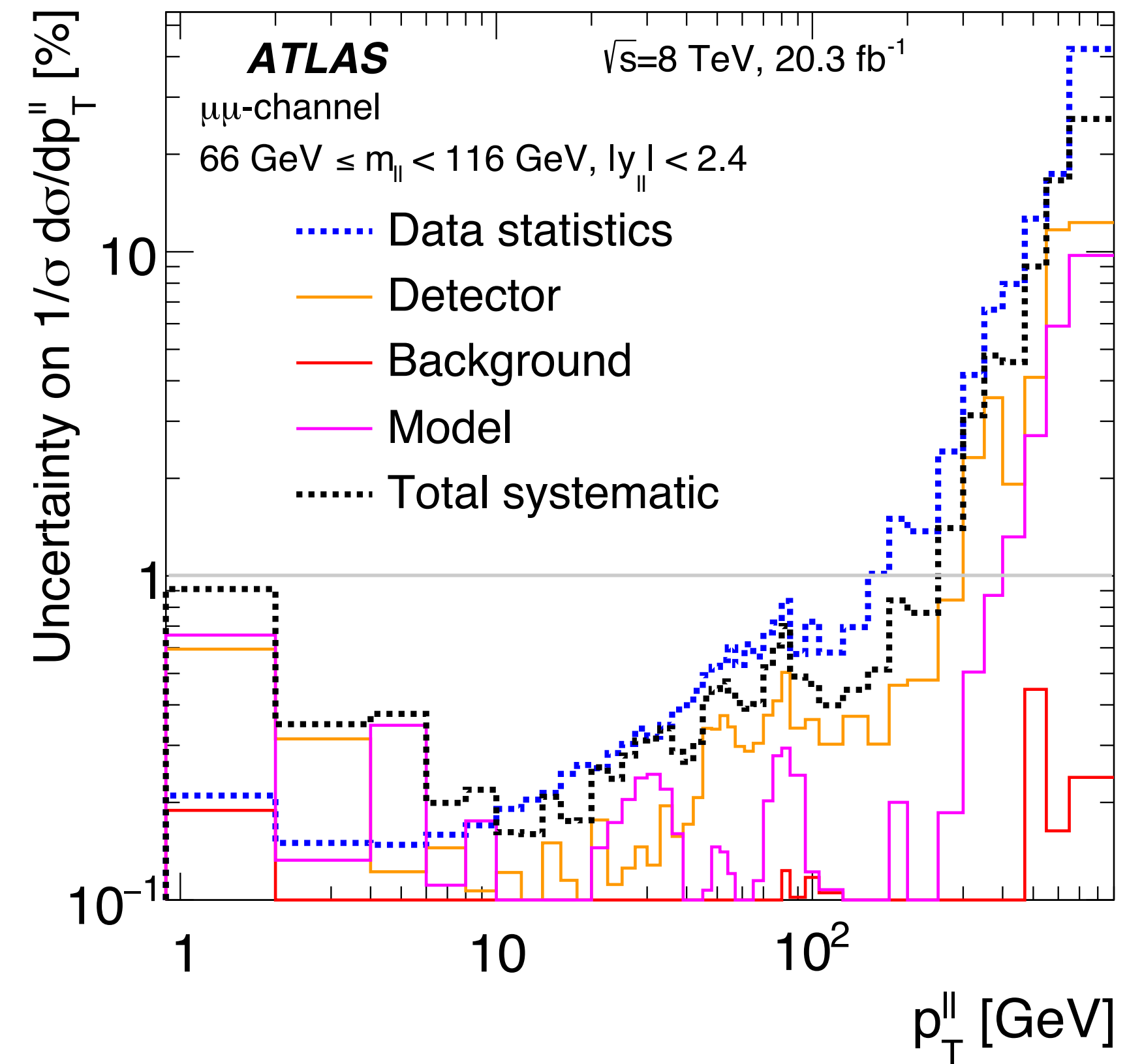
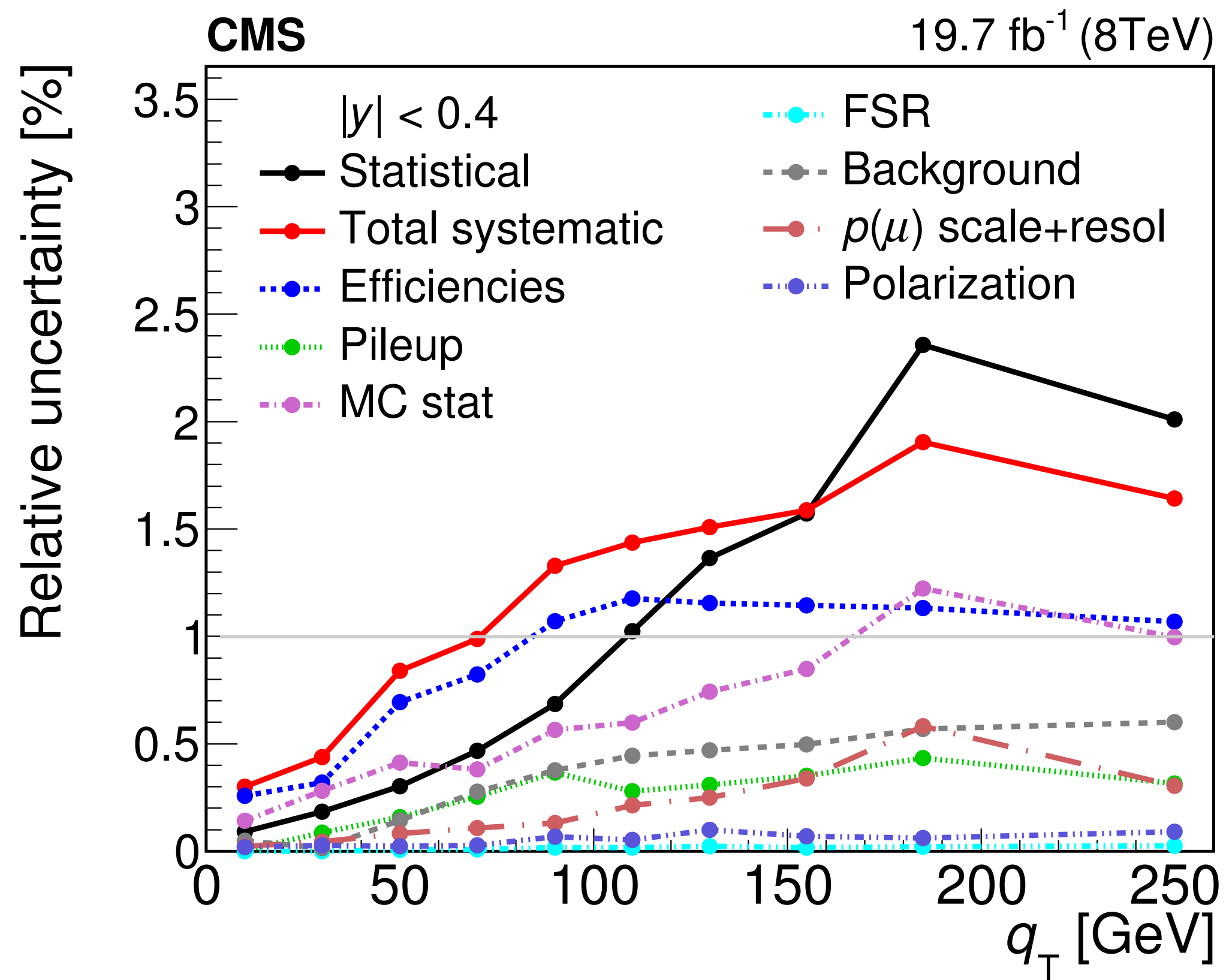
Z P_T : the “ideal” hard process?



*For both data and theory, Z p_T is
an immediate testing ground for 1% effects.*

(& unlike Z & W prodⁿ it's sensitive to α_s)

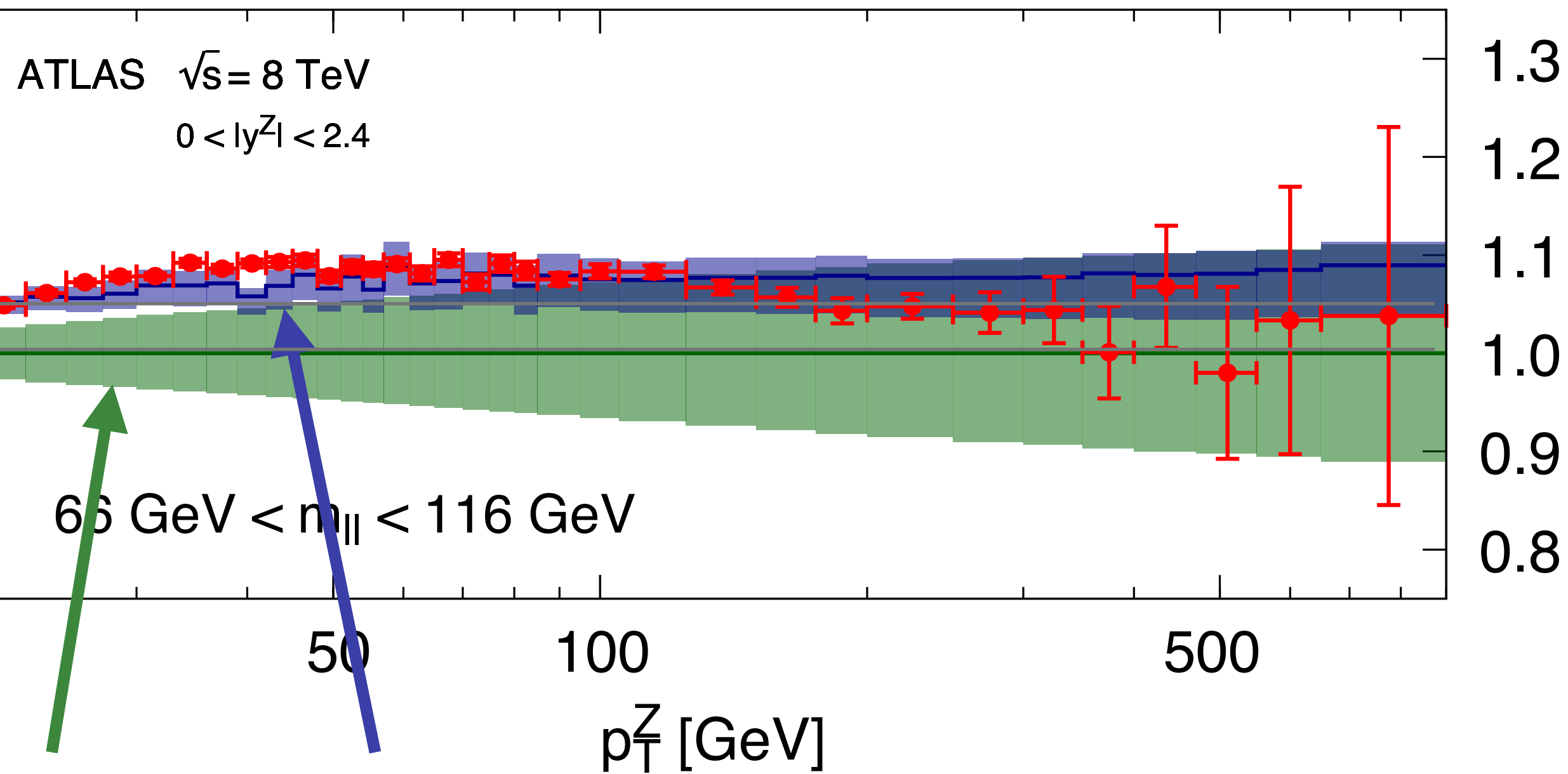
Z p_T : uncertainties somewhat smaller for ATLAS than CMS



Z p_T : Data v. two theory calculations

$p p \rightarrow Z + \geq 0 \text{ jet} \quad (p_T^Z > 20 \text{ GeV})$

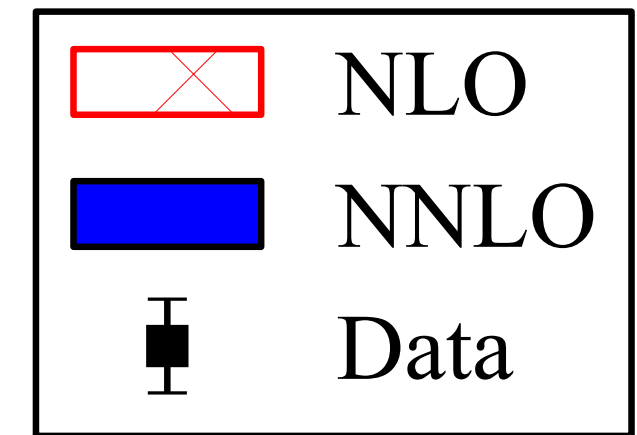
NLO — NNLO — Data —●—



NLO **NNLO**

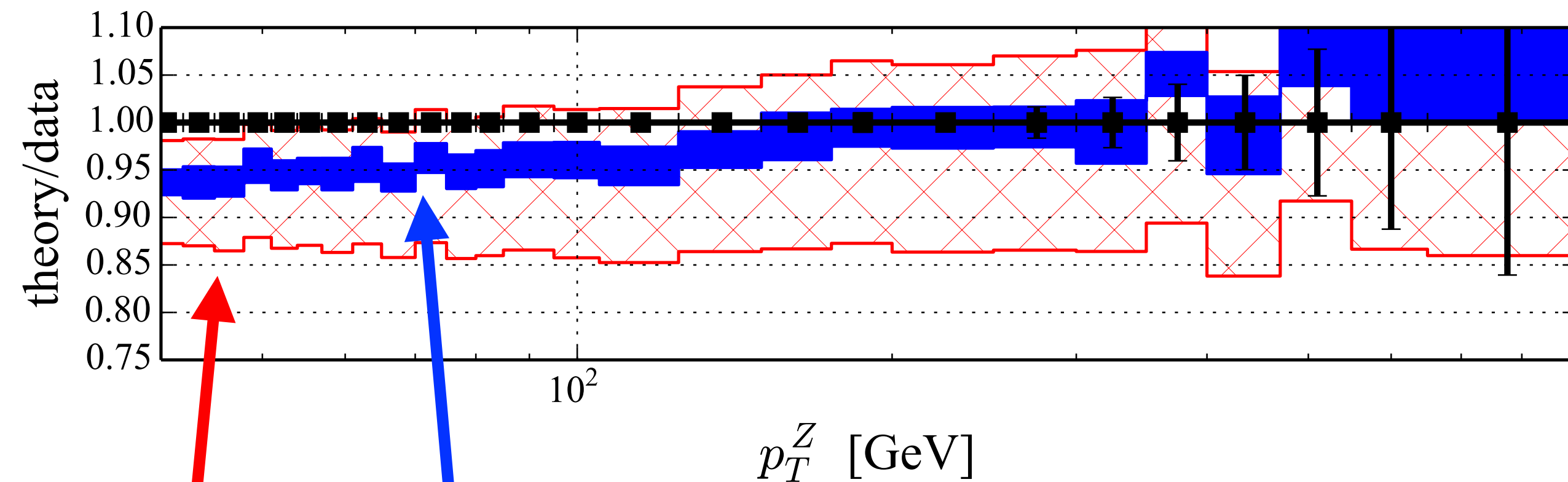
*Gehrmann-de Ridder, Gehrmann
Glover, Huss & Morgan*

arXiv:1605.04295



8 TeV ATLAS Z

(CT14)



NLO **NNLO**

*Boughezal, Liu & Petriello
'16 preliminary*

NNLO ~ ±1.5 %

REMARKS

- Looks like scale uncertainties are $\pm 1\text{--}2\%$ (but how well does series converge?)
- In key 50–100 GeV region, data seem $\sim 4\%$ higher than NNLO theory
- This could have important implications for α_s and PDFs (smaller α_s will not help!)
- **What about non-perturbative effects?**

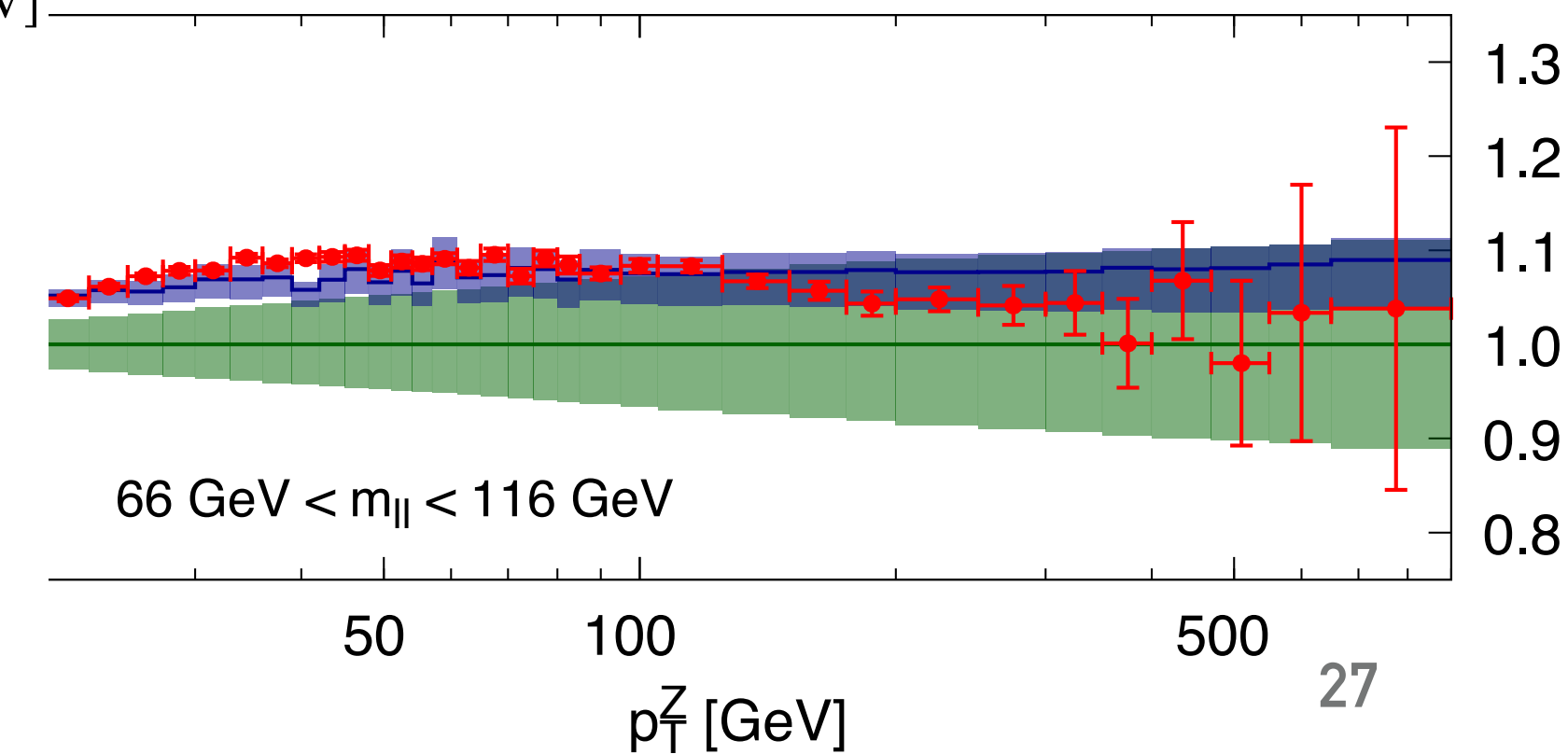
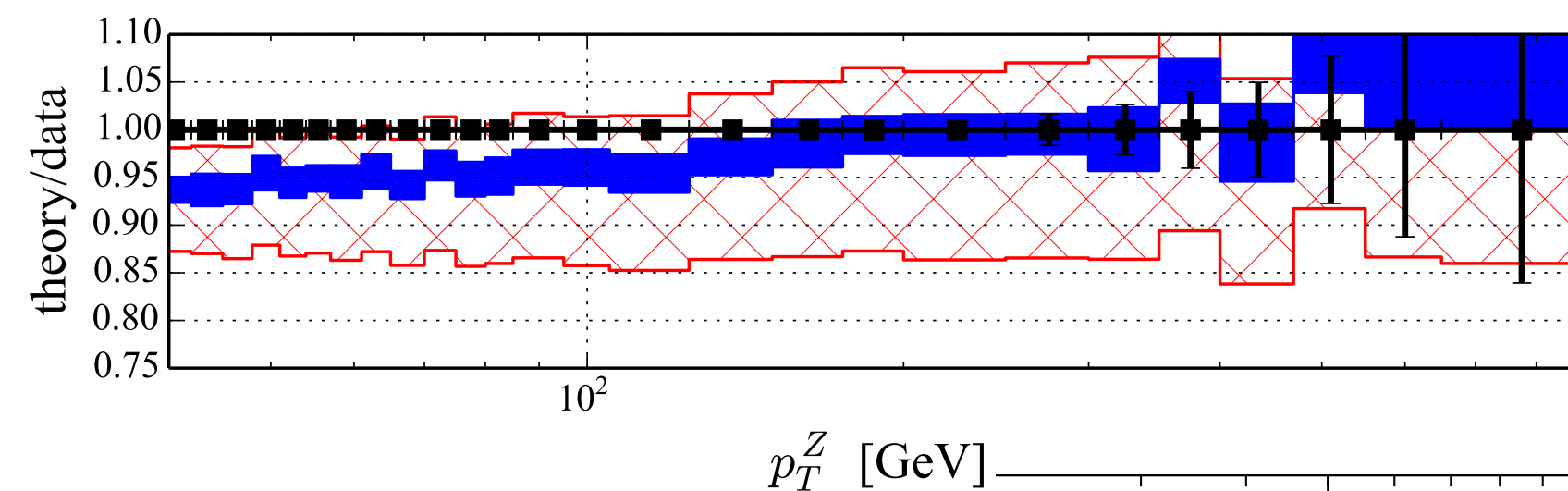
NB: both calcⁿ use a central scale

$$\mu = \sqrt{m_Z^2 + p_{T,Z}^2}$$

An alternative

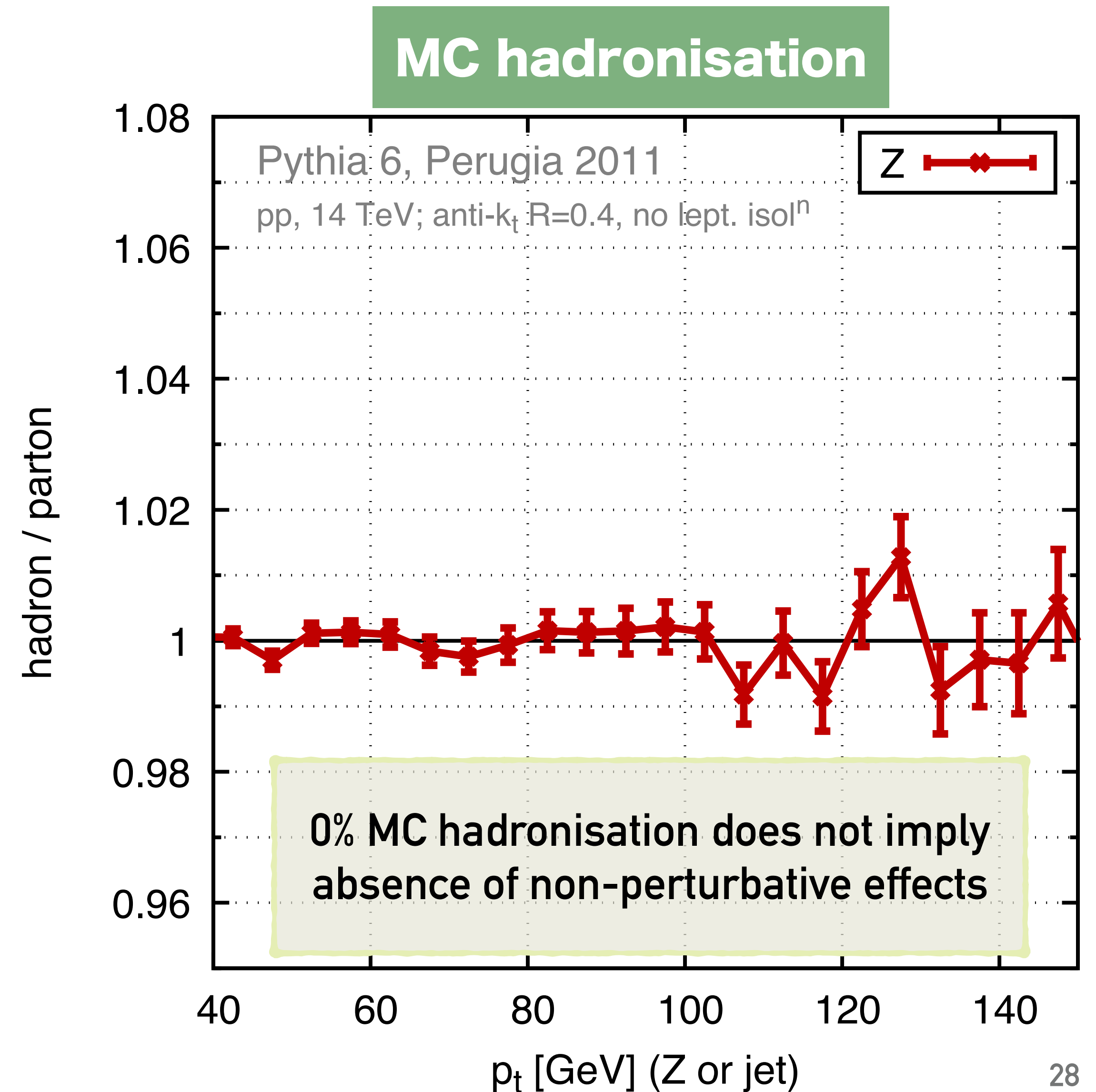
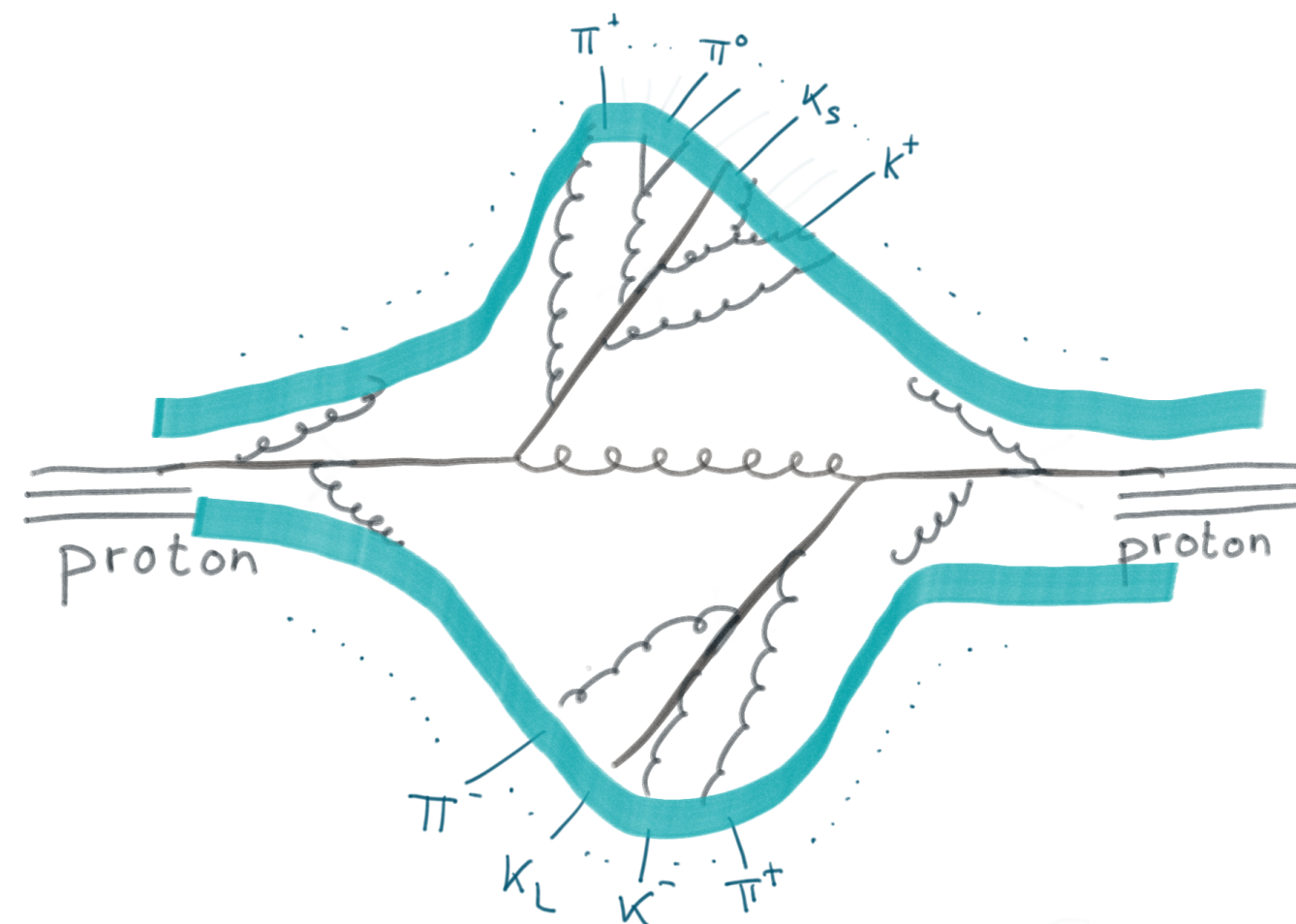
$$\mu = \frac{1}{2} \left(p_{T,Z} + \sqrt{m_Z^2 + p_{T,Z}^2} \right)$$

would seem more consistent with choices being made elsewhere (and might show better convergence?)

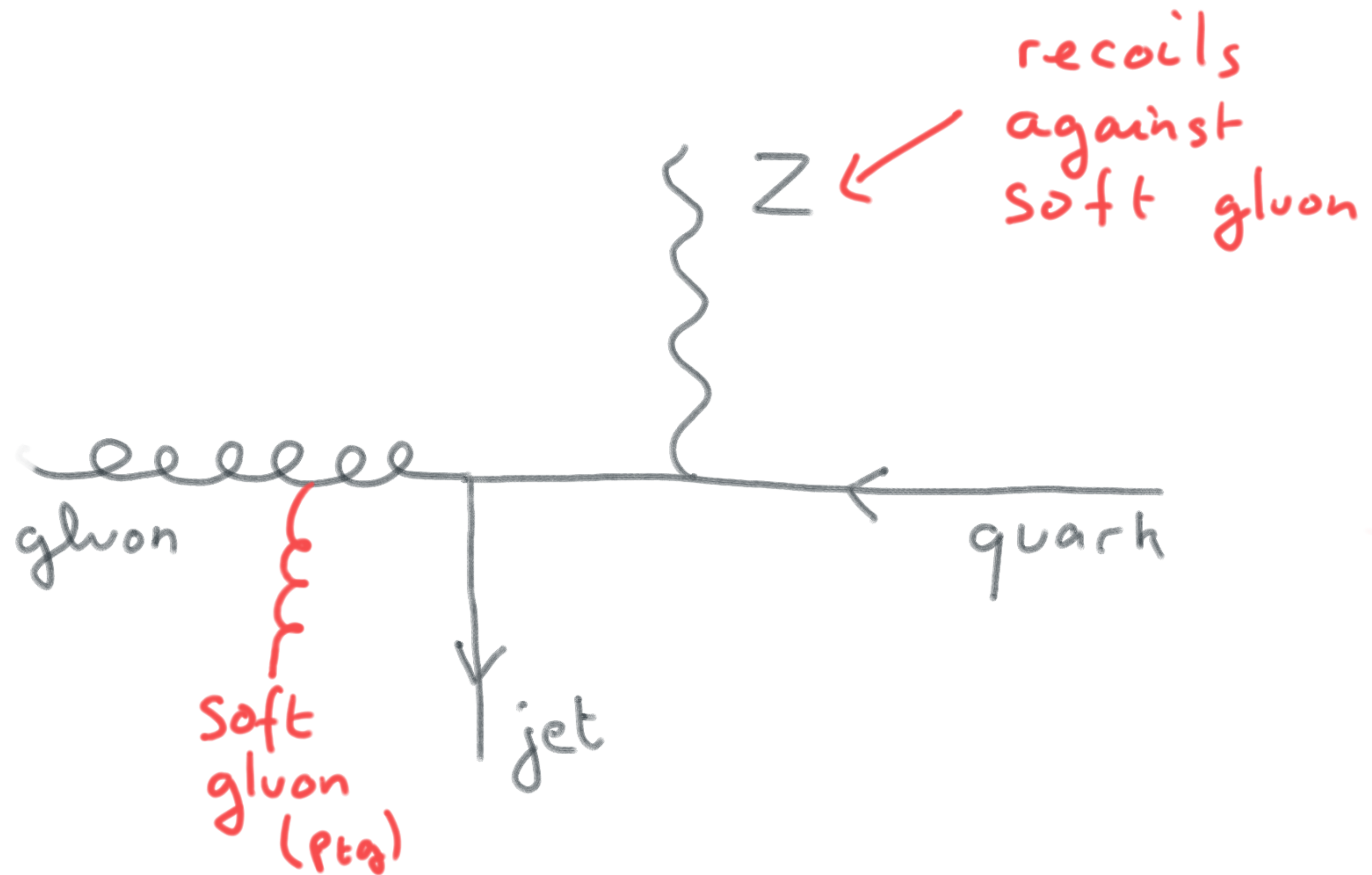


Non-perturbative effects in $Z p_T$

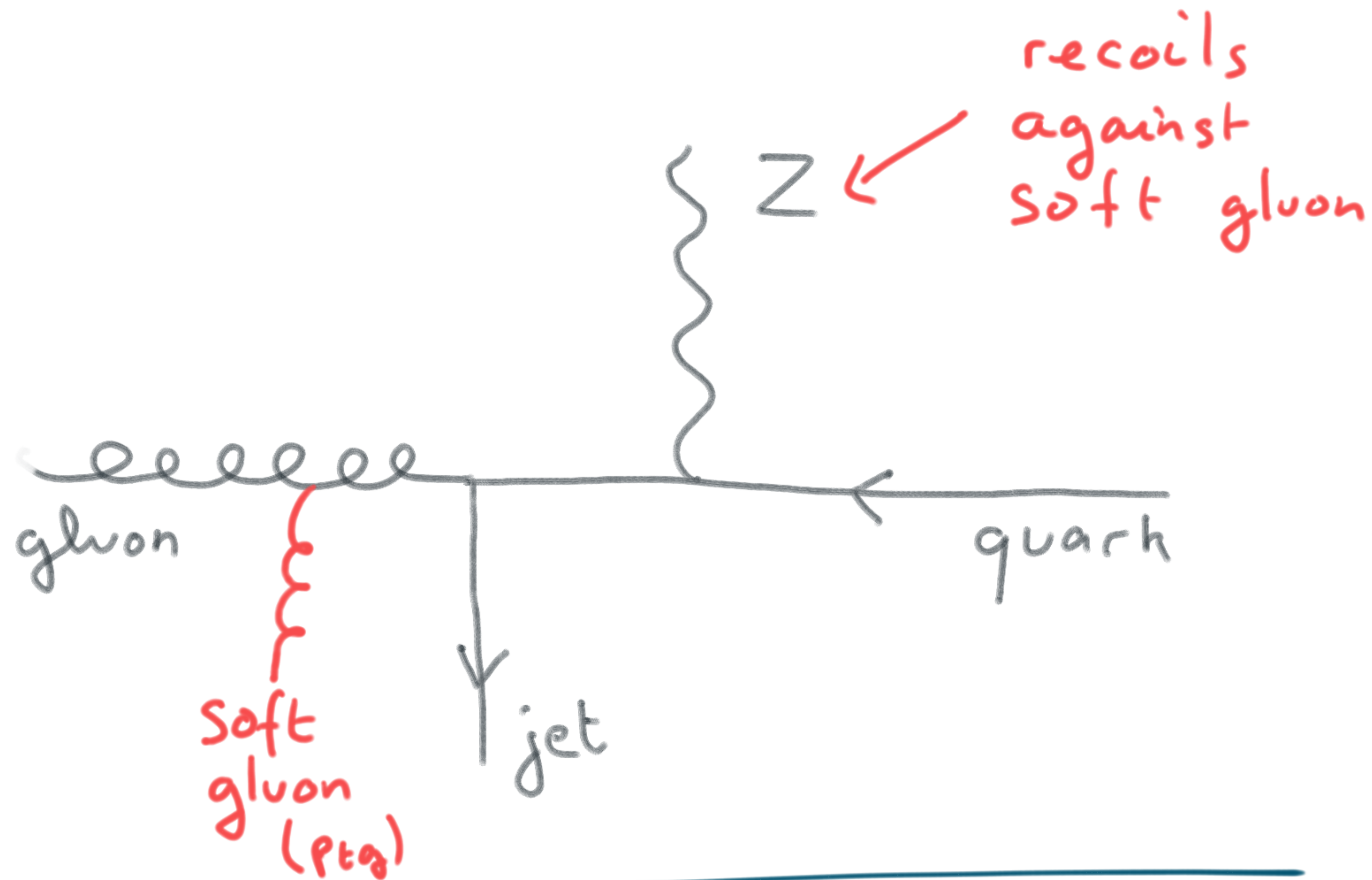
- Inclusive Z cross section should have $\sim \Lambda^2/M^2$ corrections ($\sim 10^{-4}$?)
- $Z p_T$ is **not inclusive** so corrections can be $\sim \Lambda/M$.
- It seems size of effect can't be probed by turning MC hadronisation on/off [maybe by modifying underlying MC parameters?]



Non-perturbative effects in $Z p_T$



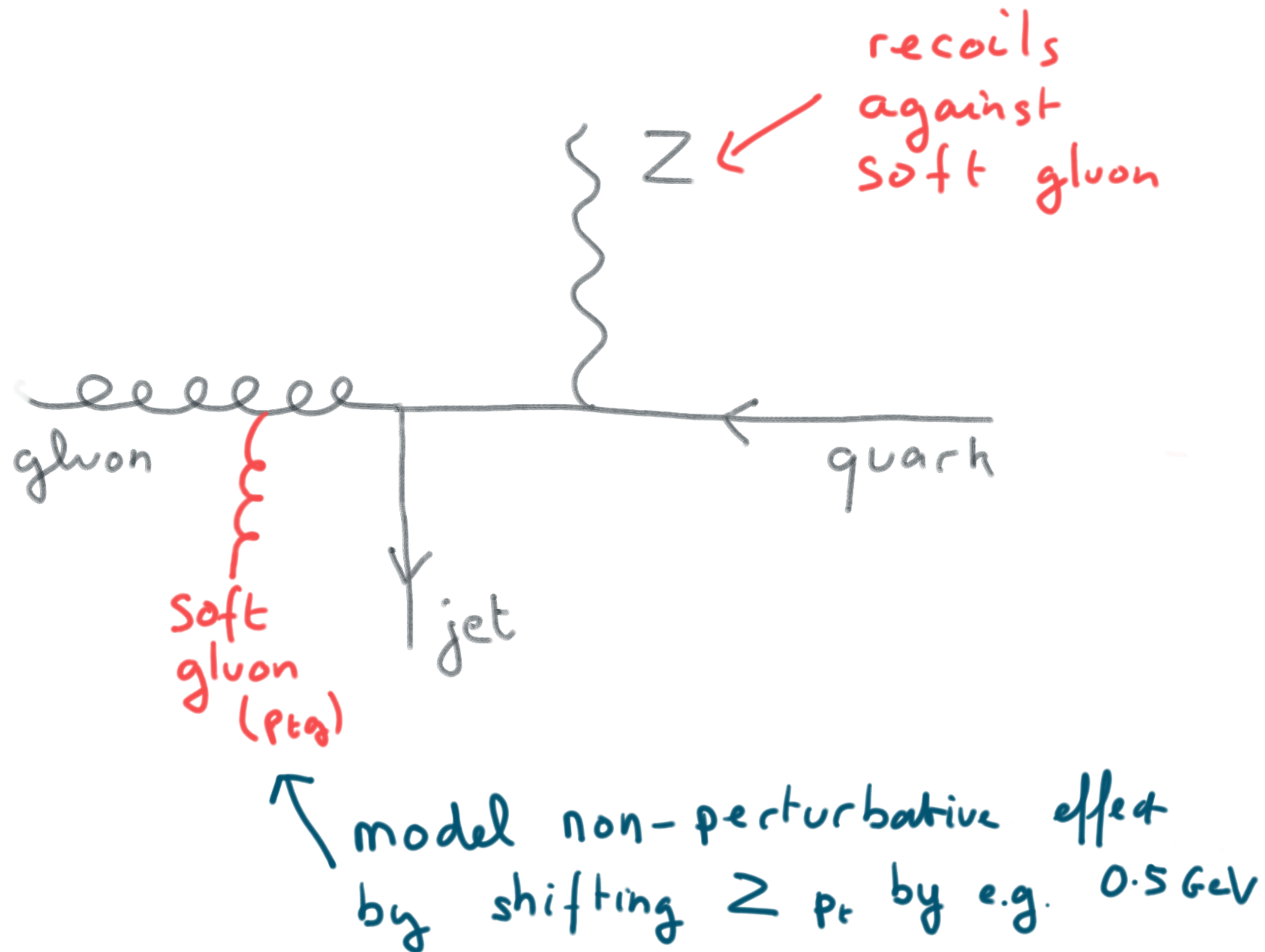
Non-perturbative effects in $Z p_T$



$$\text{recoil} \sim \int_0 \frac{dP_{Tg}}{P_{Tg}} \alpha_s(P_{Tg})$$

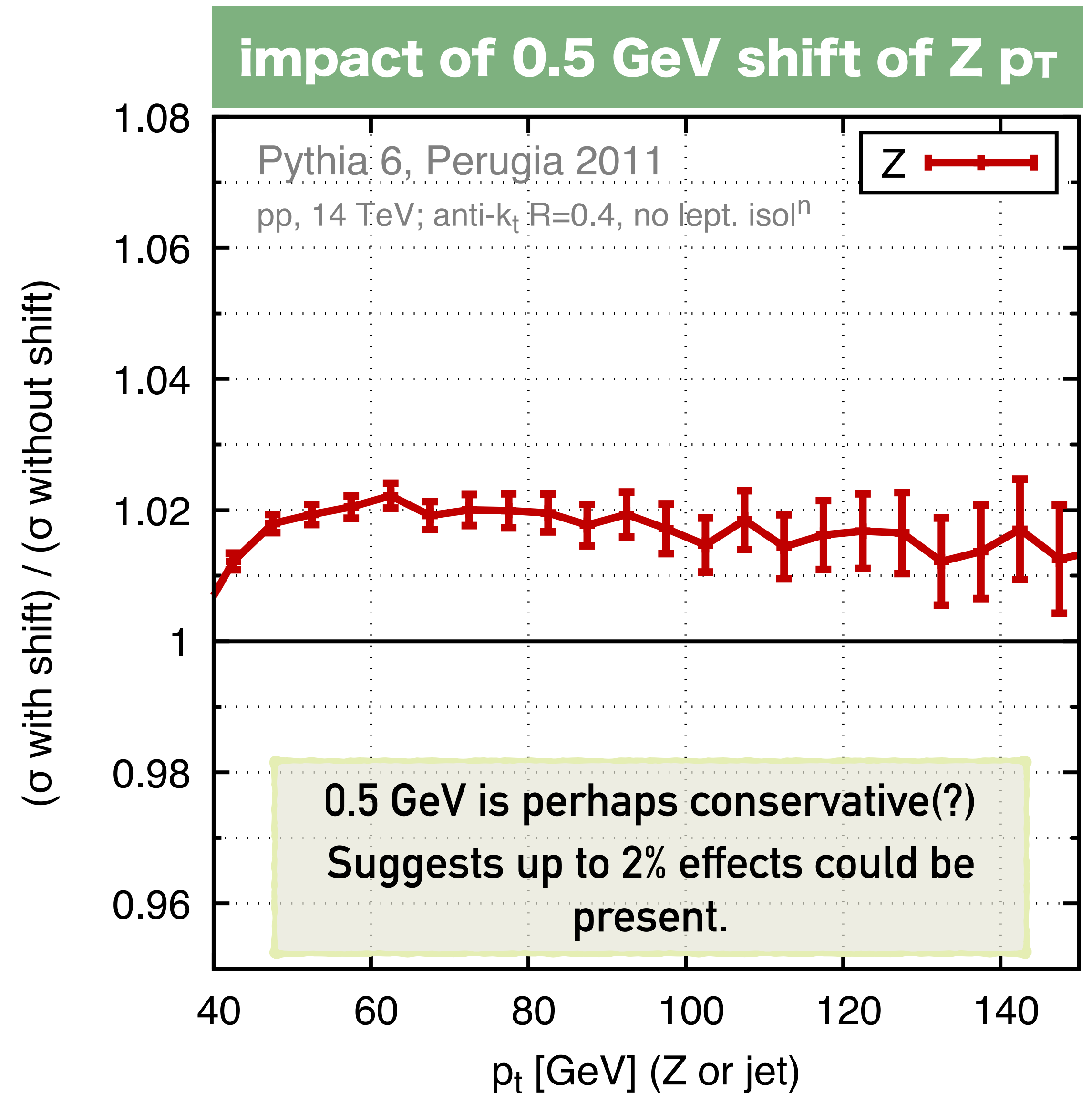
integral over low P_T emissions is non-perturbative

Non-perturbative effects in $Z p_T$



Non-perturbative effects in $Z p_T$

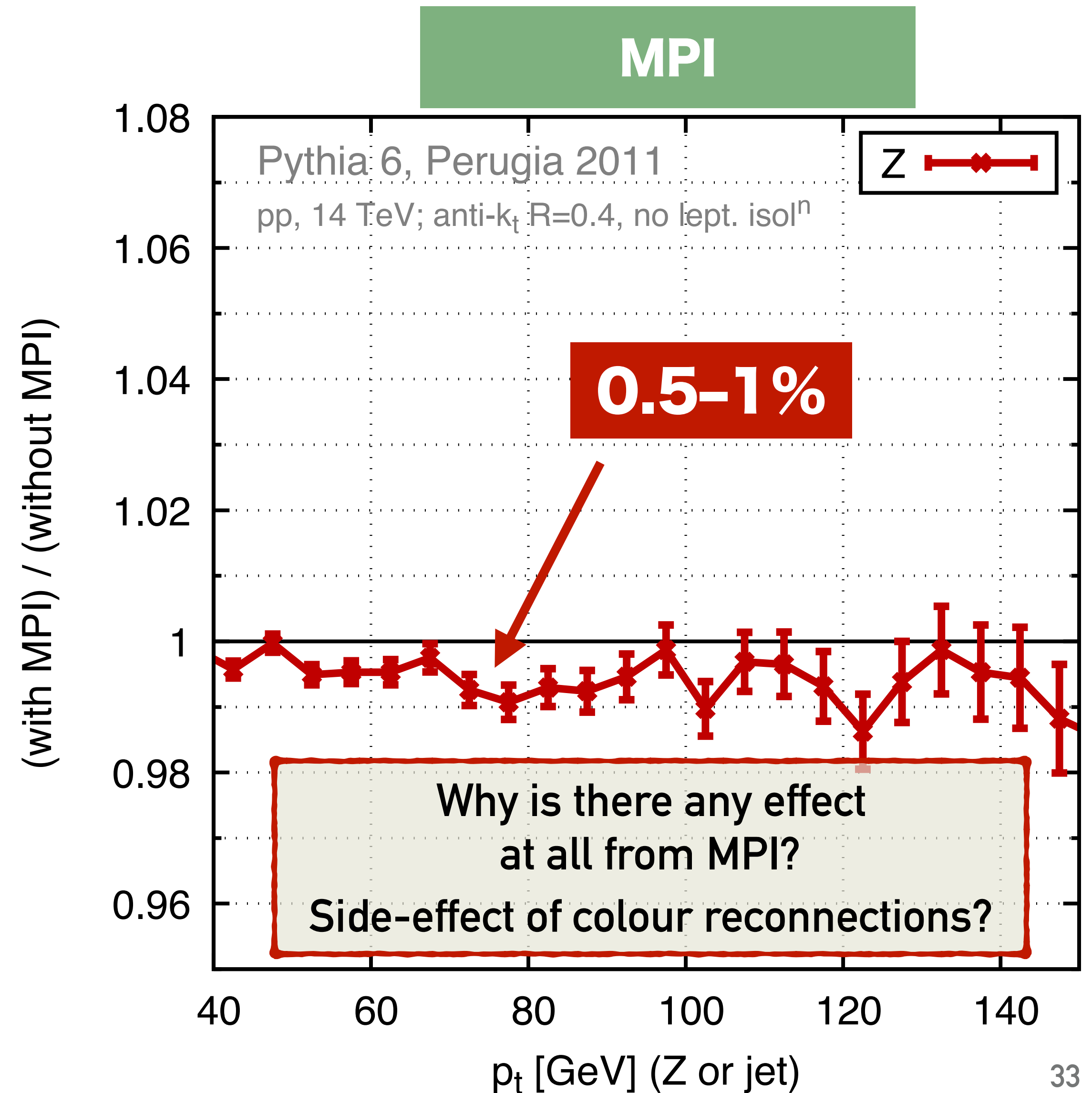
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- Size of effect can't be probed by turning MC hadronisation on/off
[maybe by modifying underlying MC parameters?]
- Shifting $Z p_T$ by a finite amount illustrates what could happen



A conceptually similar problem is present for the W momentum in top decays

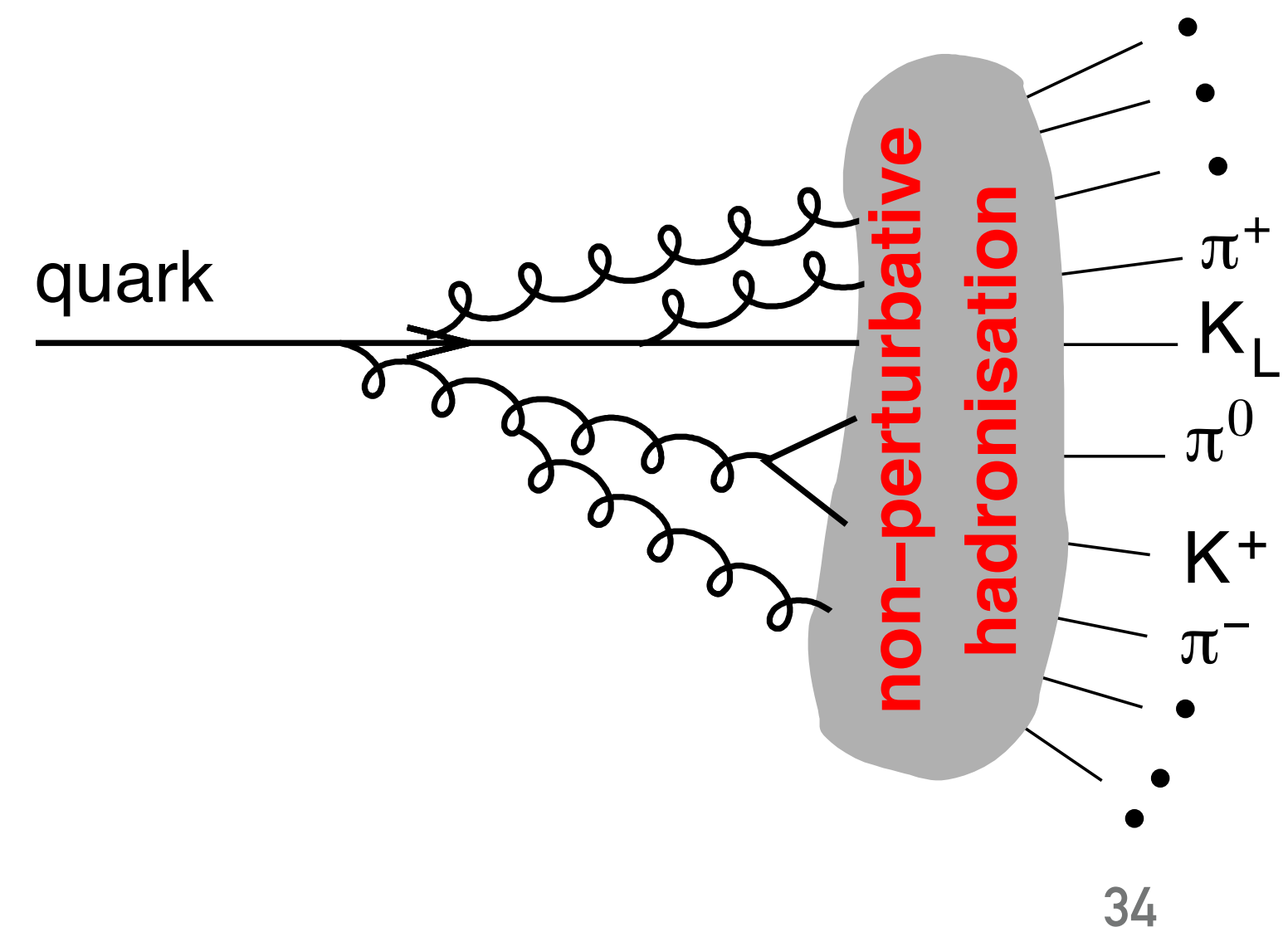
Multi-Parton Interactions?

- Naively, you'd expect these are not correlated with $Z p_T$ — but in at least one MC (Pythia 6) switching them on/off changes distribution by $O(1\%)$



PROCESSES WITH (MEASURED) JETS

*much less inclusive wrt QCD radiation
subject to larger hadronisation effects*



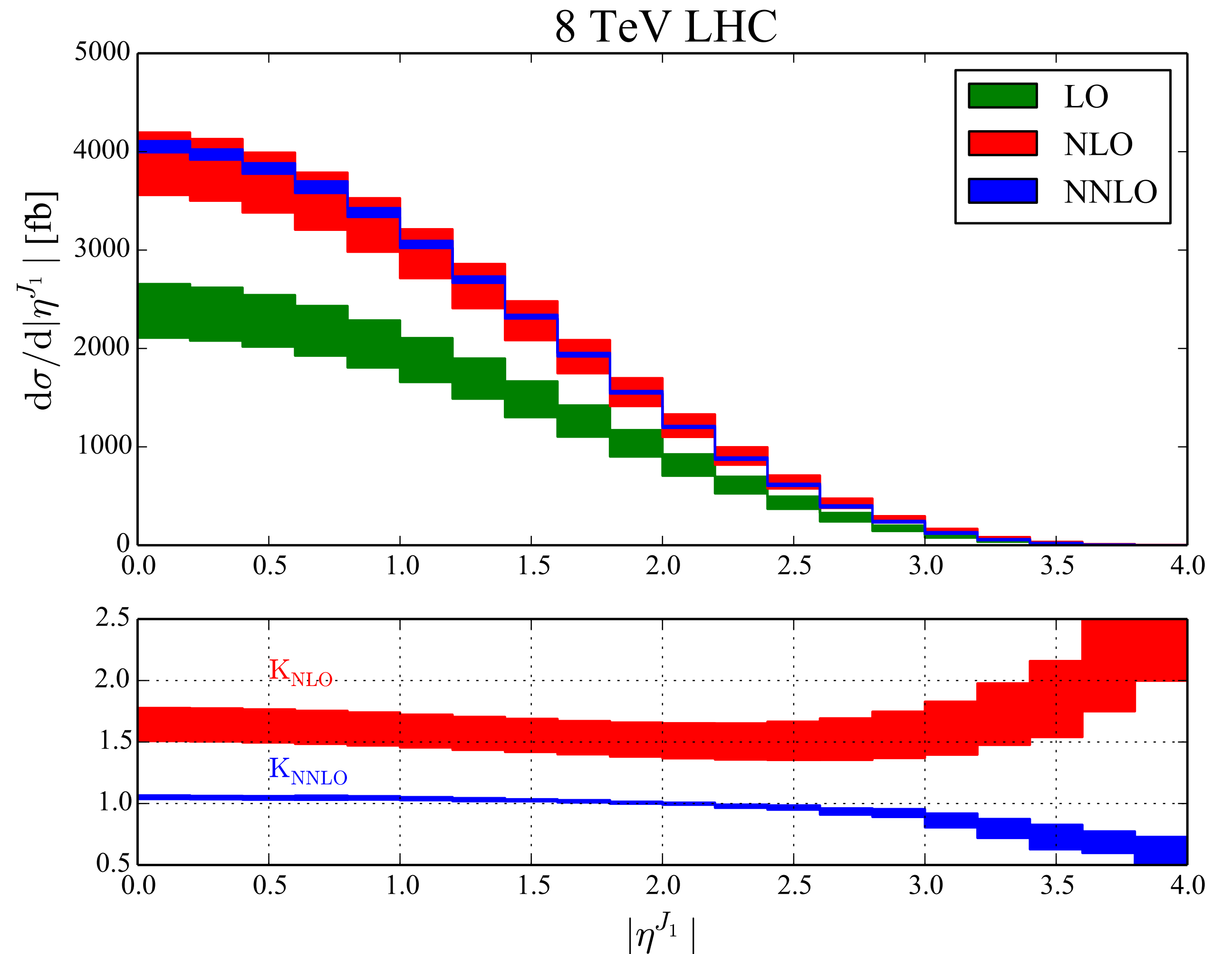
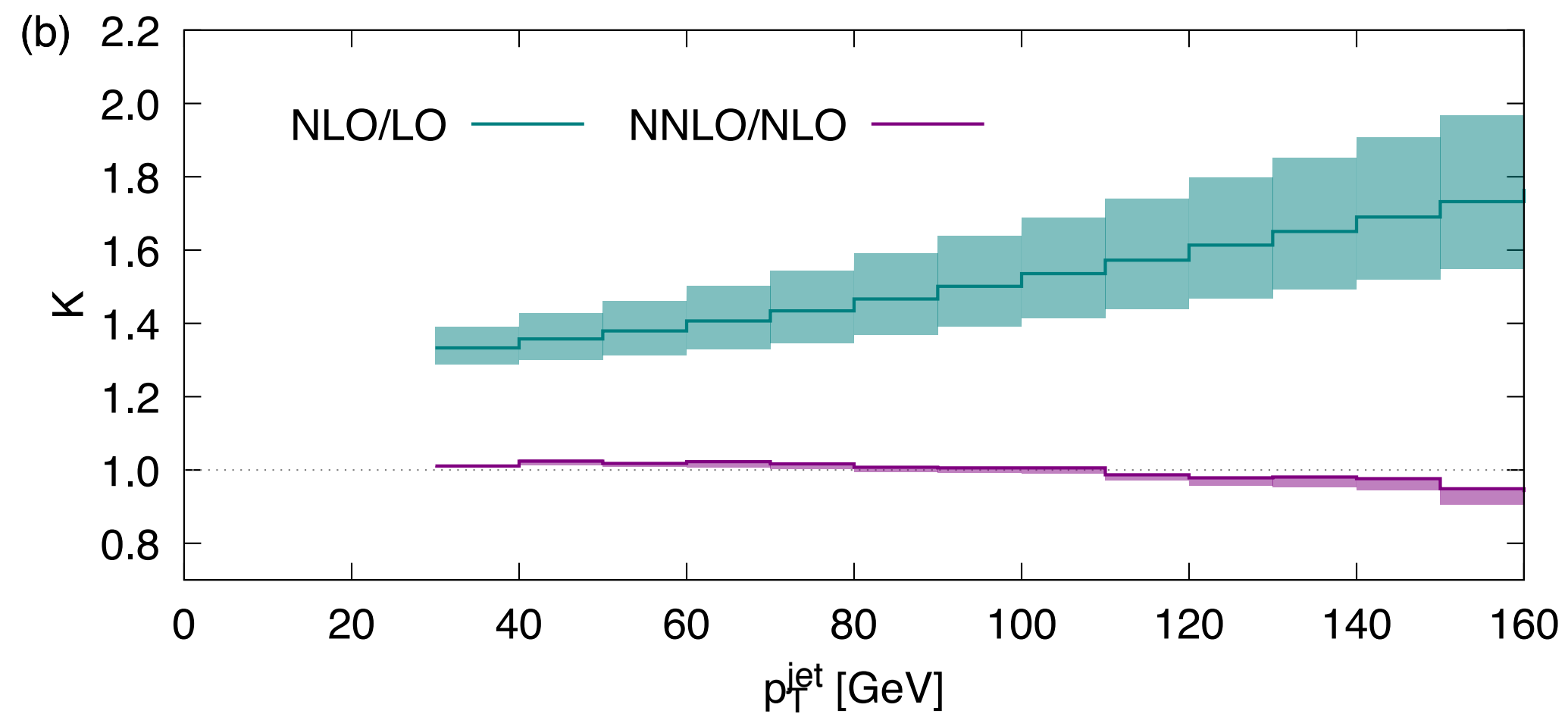
THE JET IN Z+JET @ NNLO

Boughezal, Liu & Petriello, 1602.08140

1-jet cross sections					
	σ_{LO} (pb)	σ_{NLO} (pb)	σ_{NNLO} (pb)	K_{NLO}	K_{NNLO}
8 TeV	$4.17^{+0.55}_{-0.47}$	$6.59^{+0.62}_{-0.53}$	$6.86^{+0.01}_{-0.13}$	1.58	1.04
13 TeV	$9.12^{+0.88}_{-0.79}$	$14.90^{+1.29}_{-1.06}$	$15.54^{+0.01}_{-0.24}$	1.63	1.04

➤ NNLO K-factor is a few%

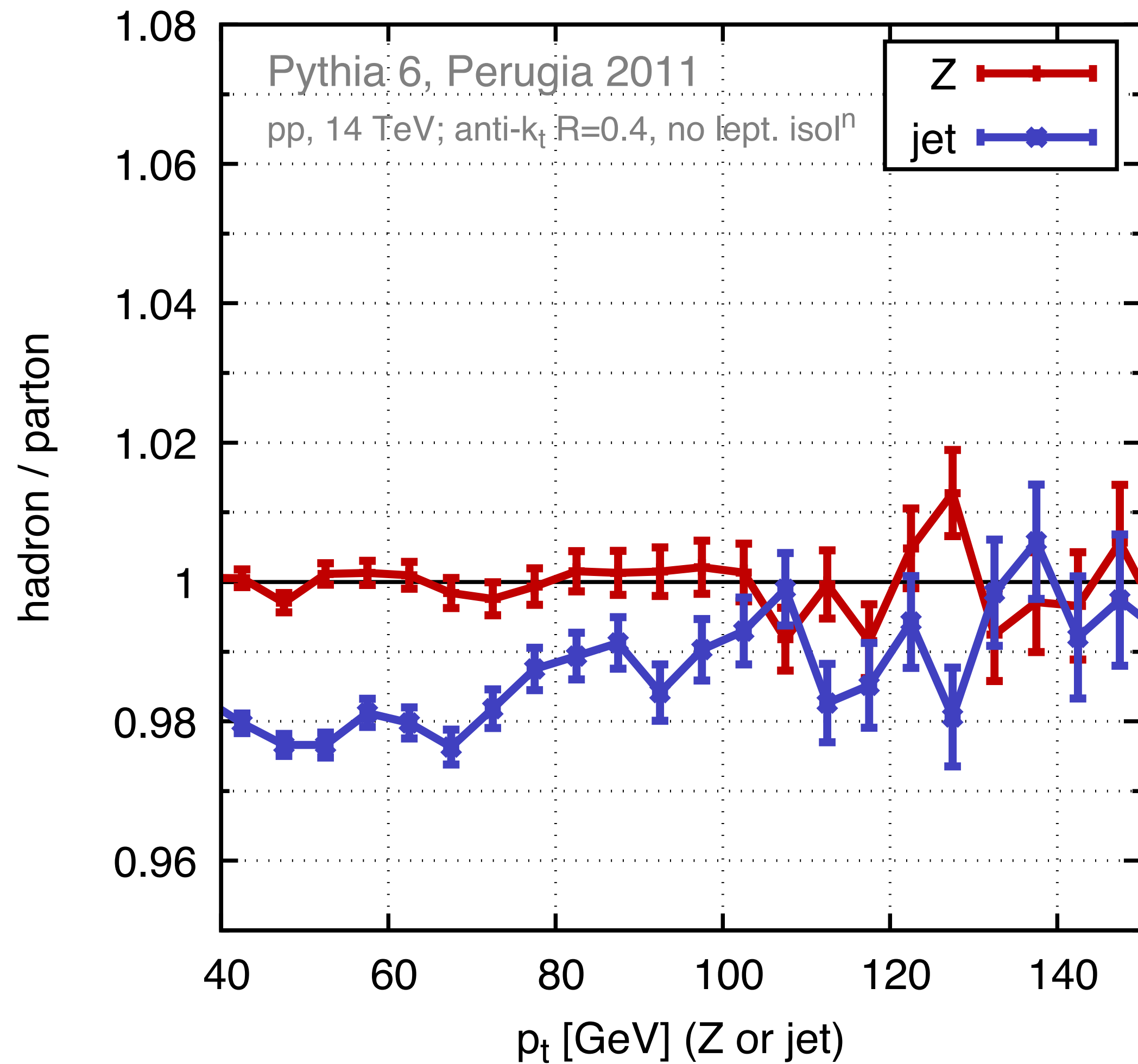
➤ Residual scale uncertainty < 2%



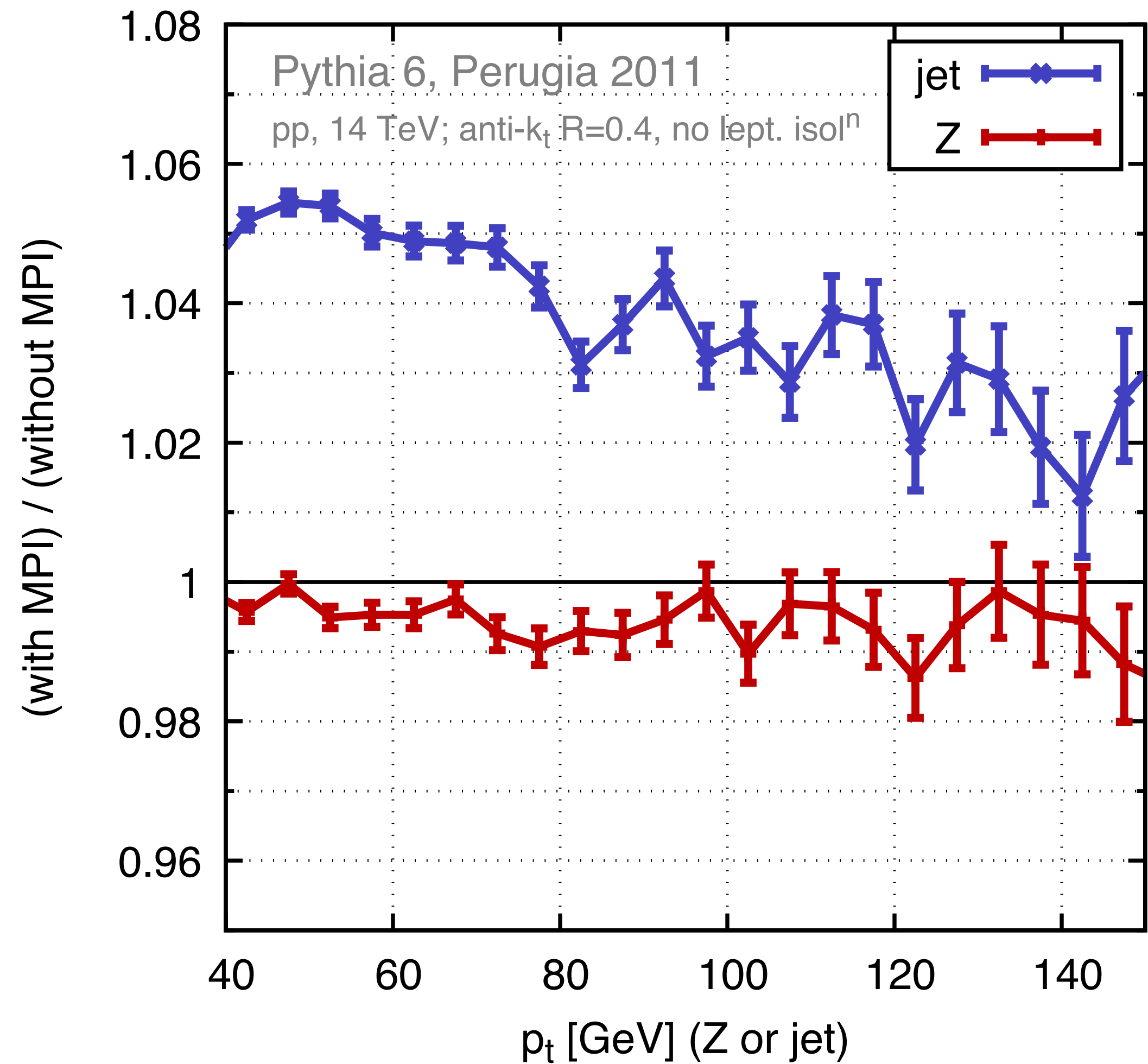
Gehrmann-De Ridder et al, 1607.01749

Hadronisation: Jet v. Z in Z+jet process

impact of hadronisation



impact of MPI (UE)



2 - 5% effects for jets

POWERFUL HANDLE: EXPLORE A RANGE OF JET RADII

Dasgupta, Dreyer, GPS
& Soyez, 1602.01110

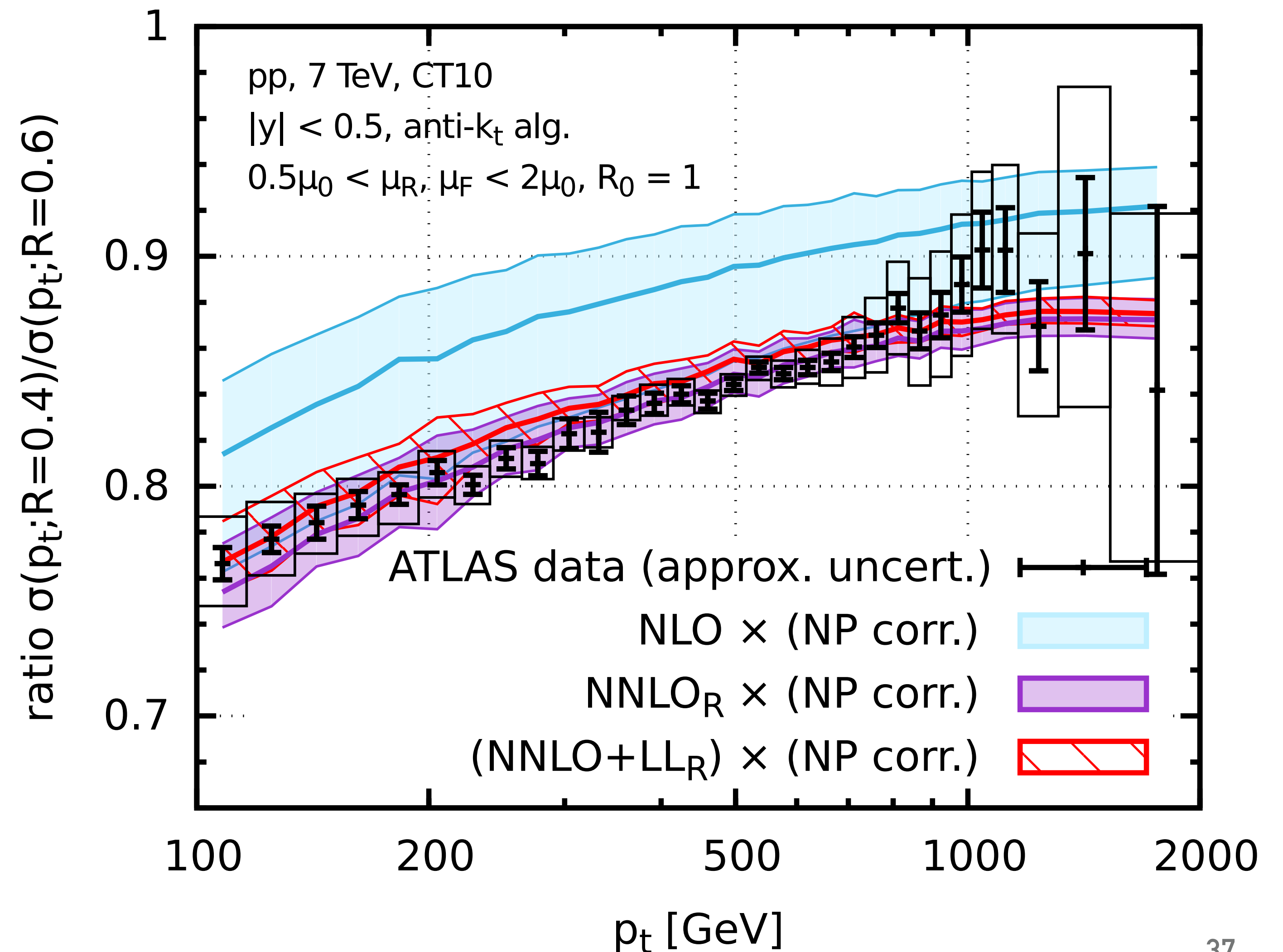
3 effects:

- perturbative ($\sim \ln R$)
- hadronisation ($\sim 1/R$)
- MPI/UE ($\sim R^2$)

To disentangle them, need ≥ 3 R values:

- 0.6–0.7: large MPI/UE
- 0.4: non-pert. effects cancel?
- **0.2–0.3: large hadronisation**

ratio of inclusive jet spectra at $R=0.4$ and 0.6



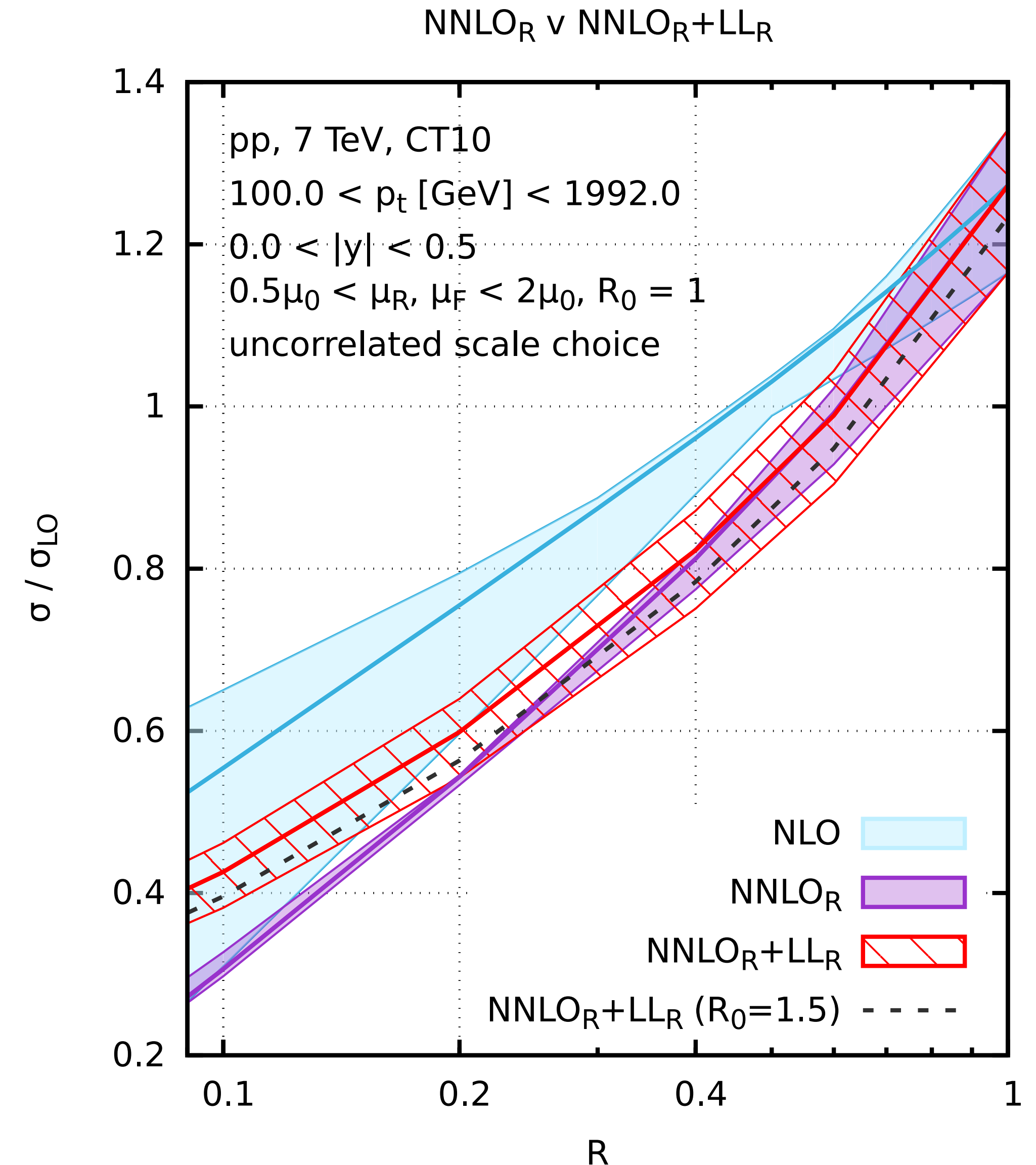
NNLO_R & small-R resummation

- to explore full R-range, need resummation as well

$$\sigma(R) = \sigma(R_0 = 1) \times \text{ratio}(R, R_0)_{\text{fixed-order}} + \text{LL}_R$$

At R=0.4, NNLO corrections are 15%
(up to 30% for R=0.2, where resummation also needed)

If we're to reach 1% accuracy for jet processes, NNLO may not be enough

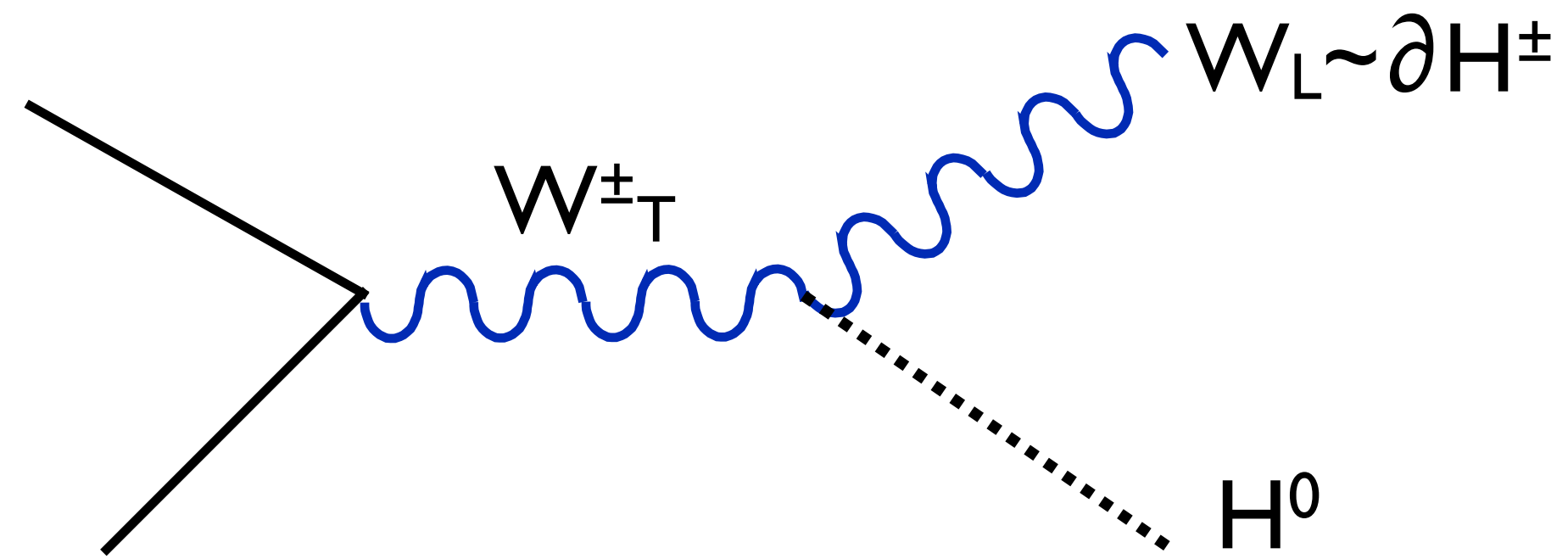


precision physics & discoveries

how do we make convince ourselves it's new physics if we see a discrepancy in new precision studies?

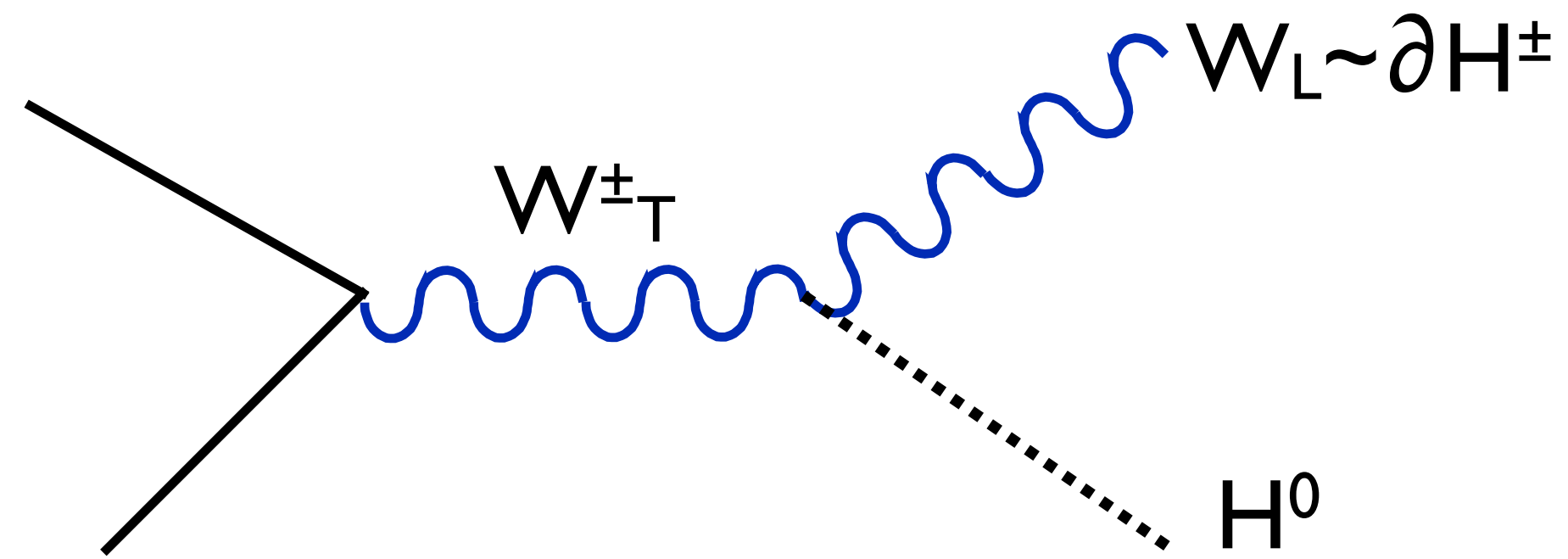
VH production at large $m(\text{VH})$

See e.g.
Biekötter, Knochel, Krämer, Liu, Riva,
arXiv:1406.7320



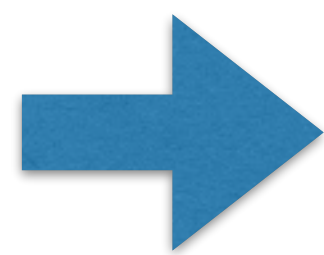
VH production at large $m(\text{VH})$

See e.g.
Biekötter, Knochel, Krämer, Liu, Riva,
arXiv:1406.7320



In presence of a higher-dim op such as:

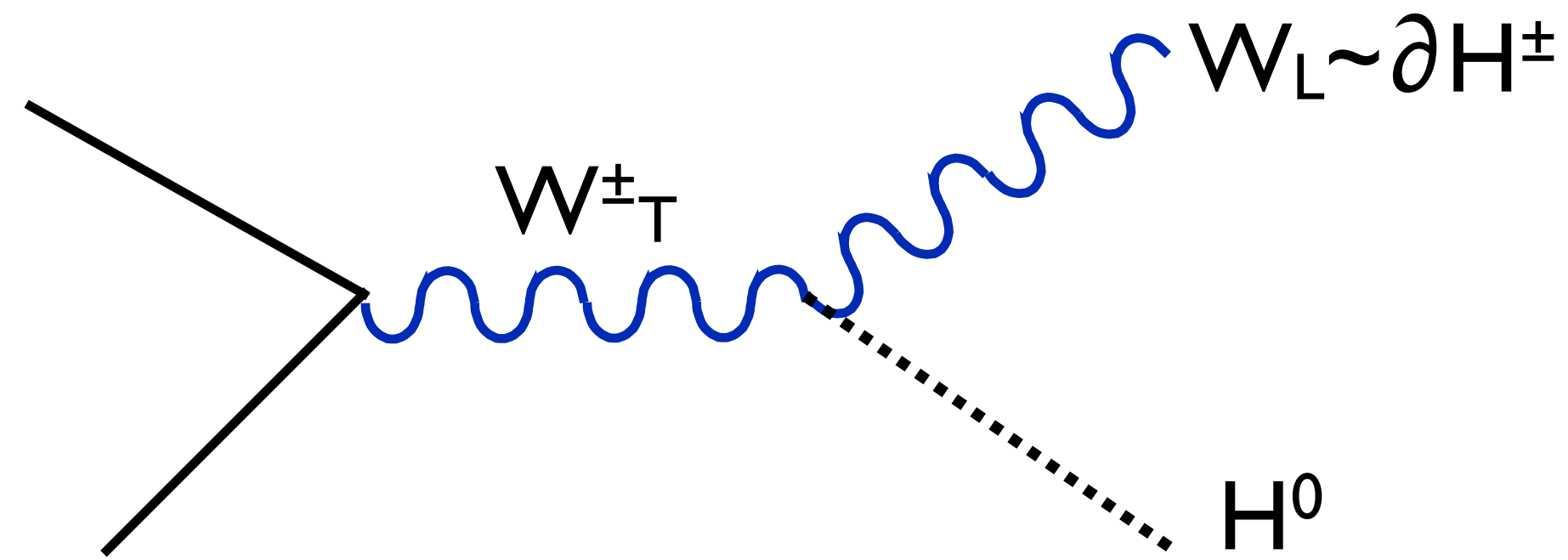
$$L_{D=6} = \frac{ig}{2} \frac{c_W}{\Lambda^2} (H^\dagger \sigma^a D^\mu H) D^\nu V_{\mu\nu}^a$$



$$\frac{\sigma}{\sigma_{SM}} \sim \left(1 + c_W \frac{\hat{s}}{\Lambda^2} \right)^2$$

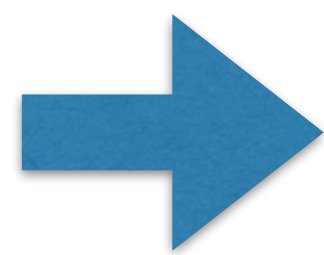
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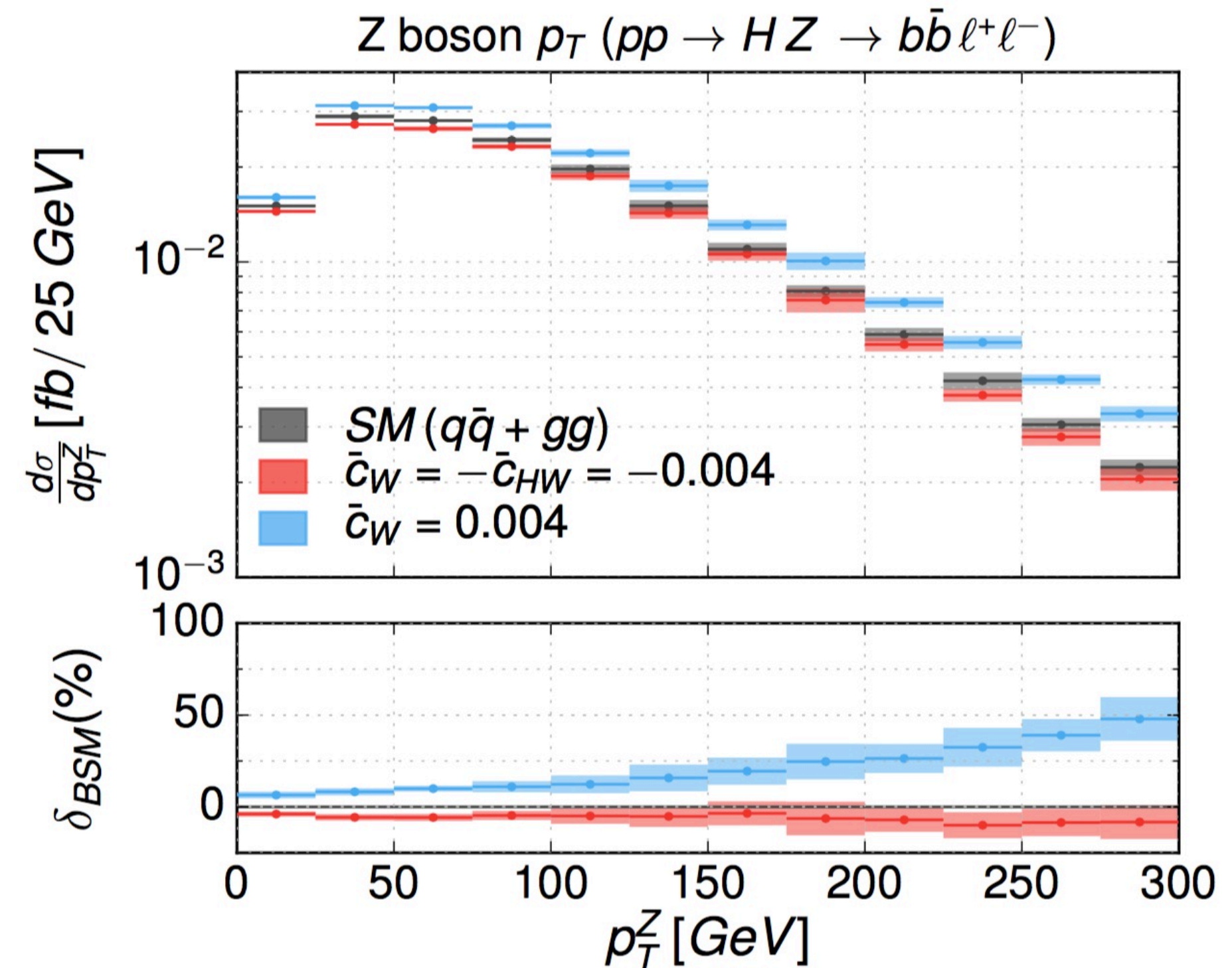


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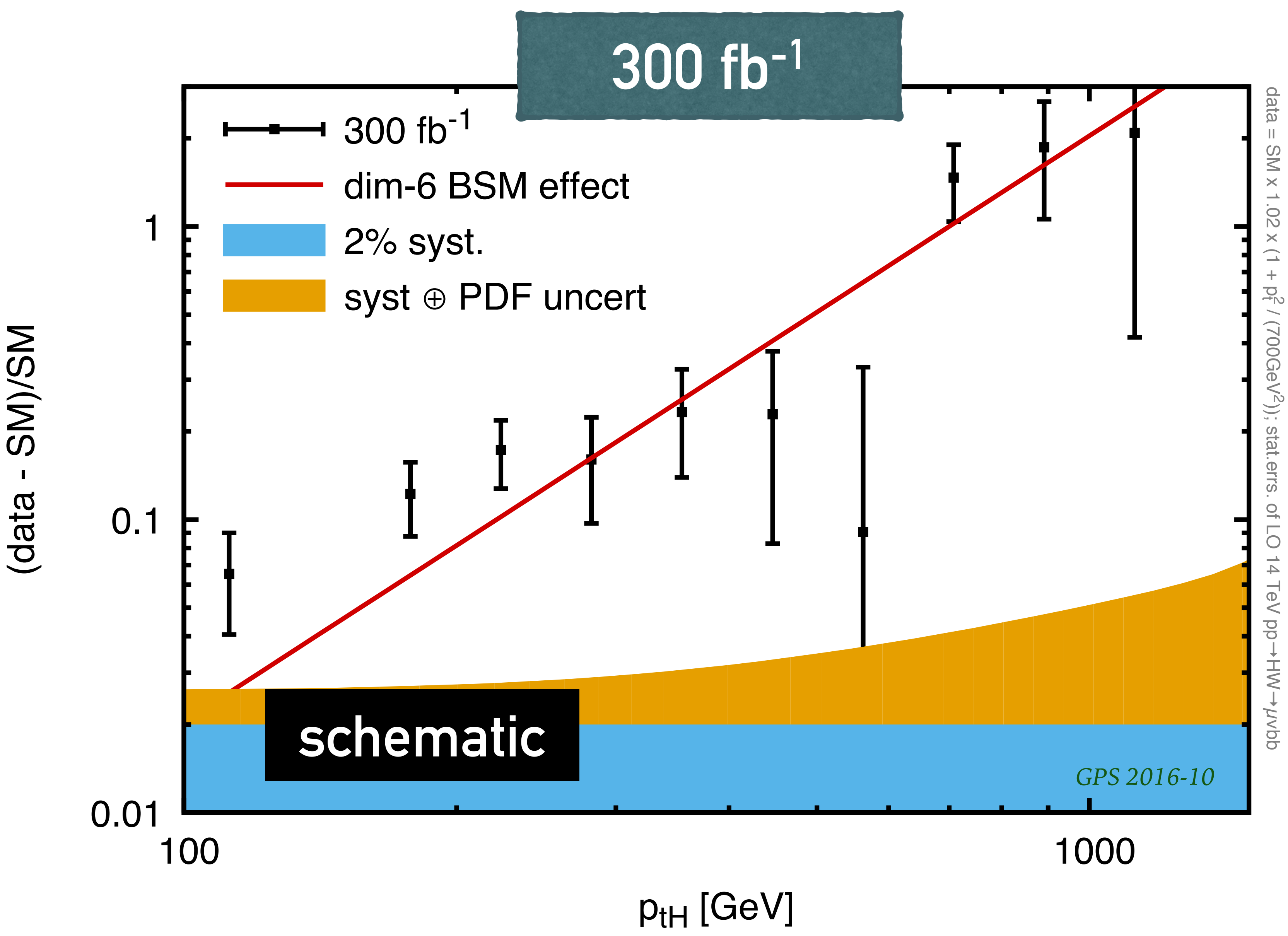


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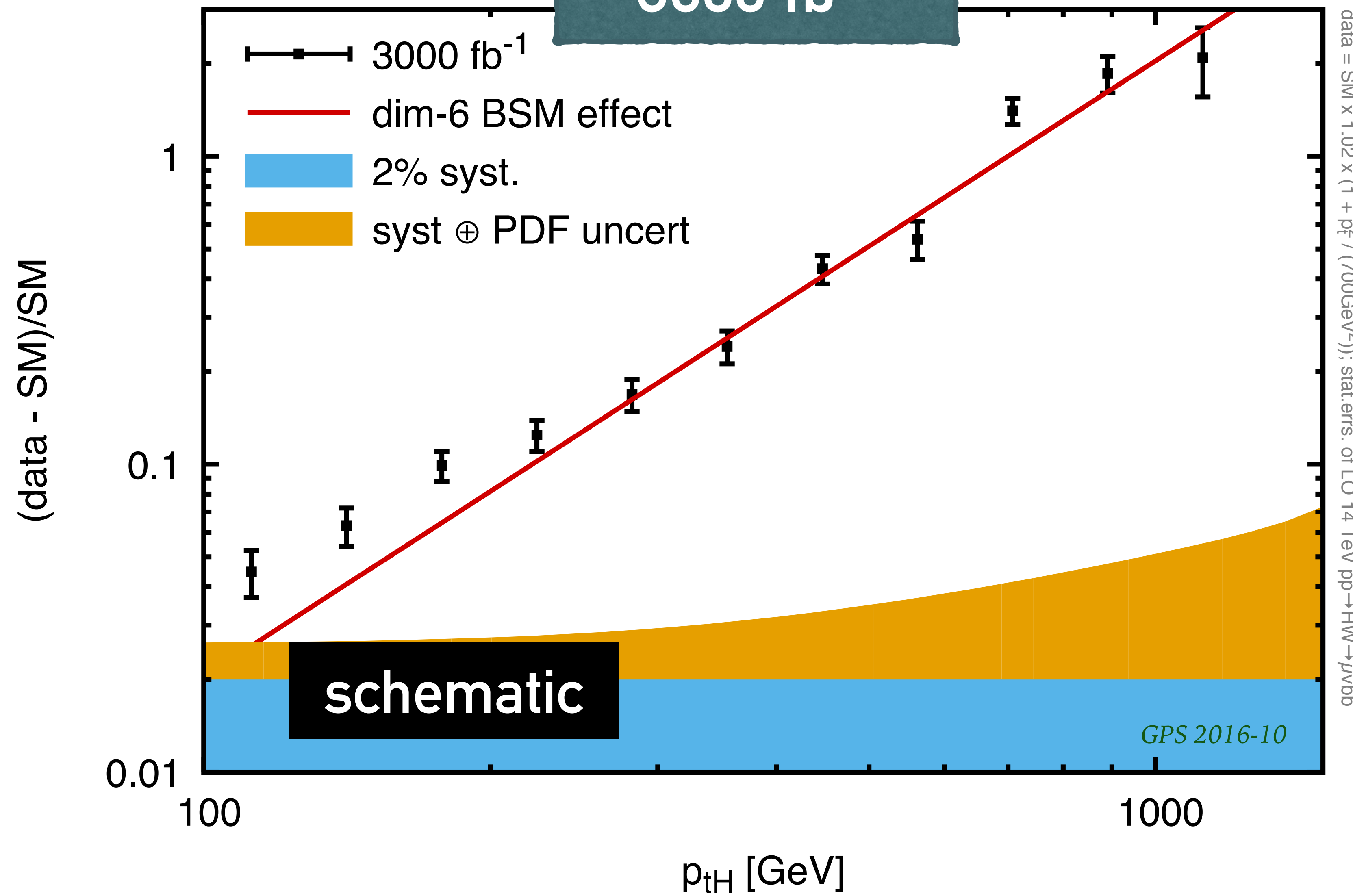
Mimasu, Sanz, Williams, arXiv:1512.02572v

WH at large Q^2 with dim-6 BSM effect



WH at large Q^2 with dim-6 BSM effect

3000 fb⁻¹



new physics isn't just a single number that's wrong (think g-2)

but rather a **distinct scaling pattern of deviation** ($\sim p_T^2$)

moderate and high p_T's have similar statistical significance — so it's useful to understand whole p_T range

Precision buys us kinematic reach to establish scaling pattern of any deviation

cf also Wulzer et al, arXiv:1609.08157

COMMENTS / CONCLUSIONS

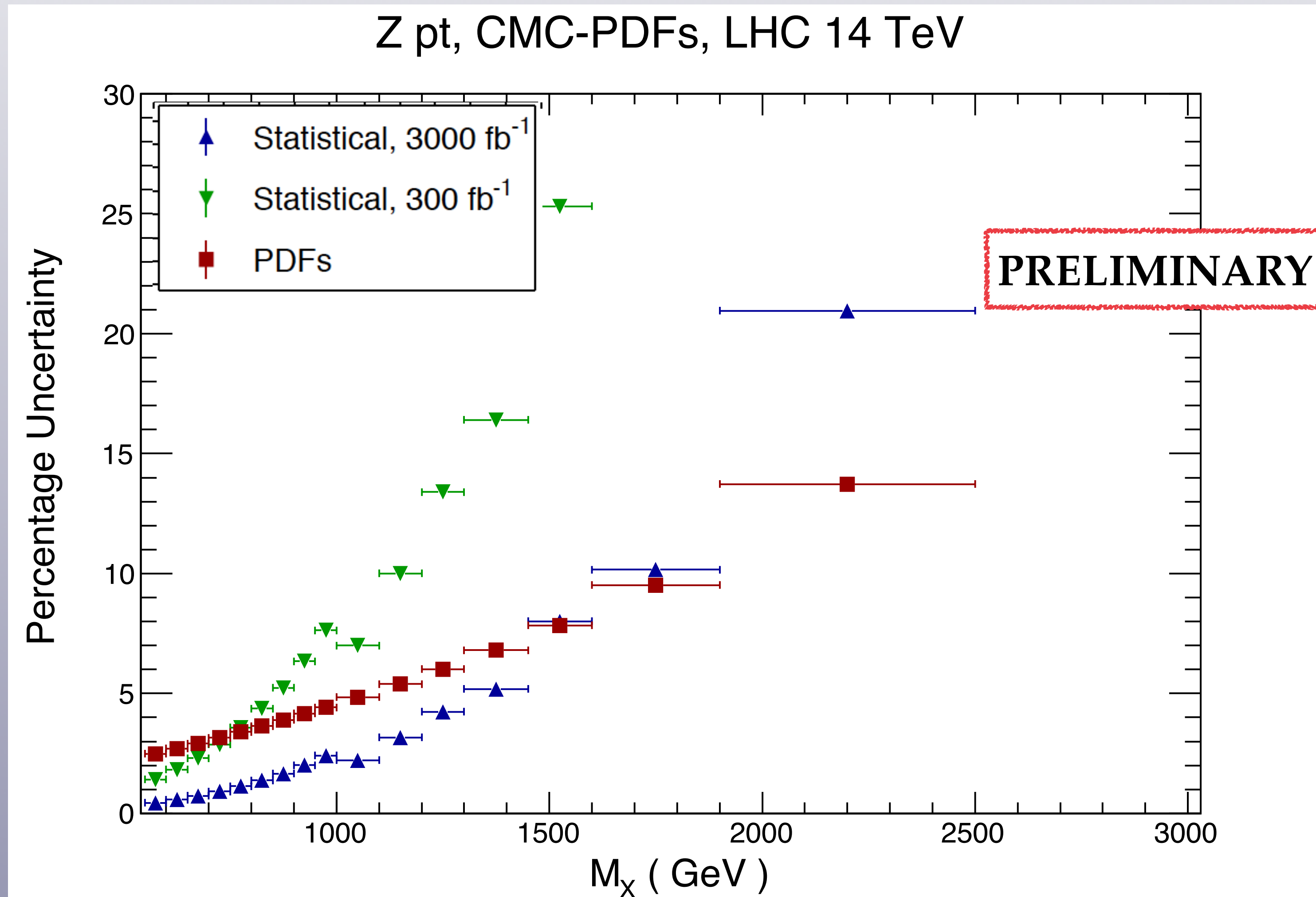
- 1% precision is something that we will want to reach for a range of processes to get full value out of the “precision” part of LHC’s programme (Higgs, top, dilepton, ...)
- We’re entering the precision era today, notably with 1% Z p_T distribution (first hadron-collider process $\propto \alpha_s$ known with this precision)
- Some problems remain to be solved:
 - consensus on PDFs (& path to 1%), strong coupling
 - non-perturbative effects (e.g. study multiple R values for jets?)
- Keep in mind that new physics effects in “precision physics” may show up with distinct scaling (almost as good as a bump or shoulder?)

BACKUP

EXPERIMENTAL PERSPECTIVES

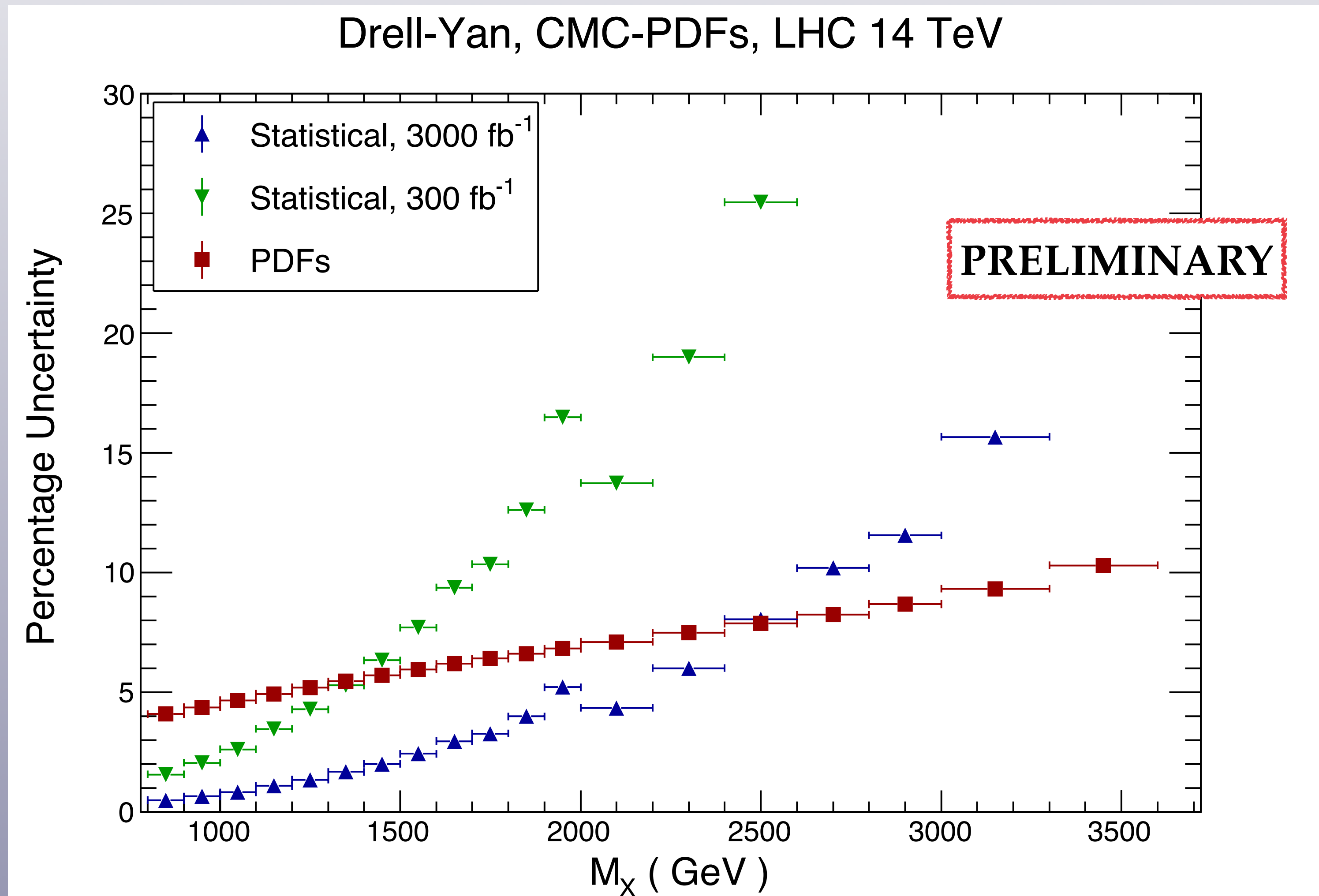
Generation of pseudo-data: the Z pt

- Generate pseudo-data for the **transverse momentum distribution of Z bosons decaying into leptons**
- Statistical uncertainties determined from **number of events per bin**, after a binning optimisation
- Added a **2% systematic uncertainty** to the statistical uncertainty



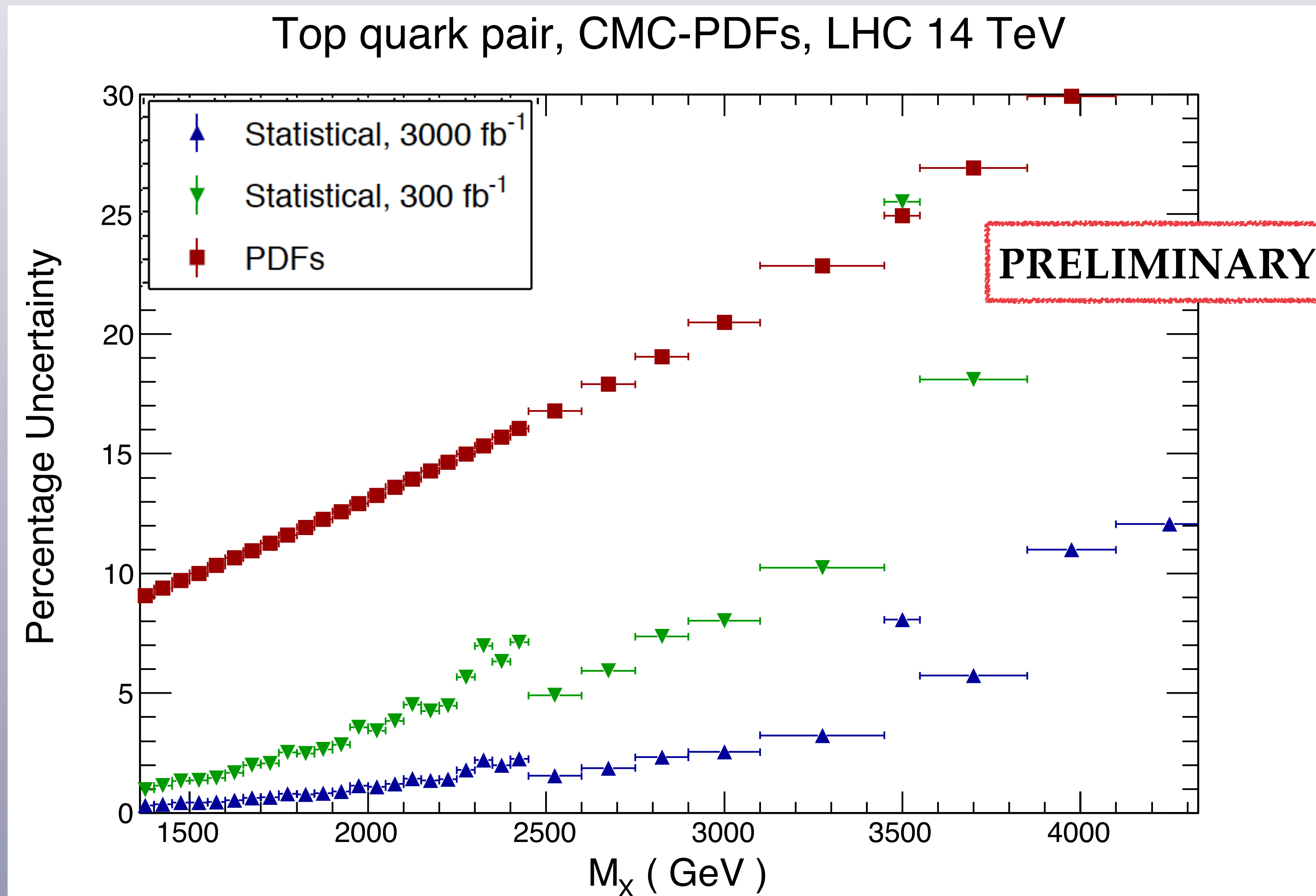
Generation of pseudo-data: high-mass Drell-Yan

- Generate pseudo-data for the **invariant mass distribution** of **di-electrons** and **di-muons**
- Statistical uncertainties determined from **number of events per bin**, after a binning optimisation
- Added a **2% systematic uncertainty** to the statistical uncertainty



Generation of pseudo-data: top quark pair

- Generate pseudo-data for the **invariant mass distribution** in the **leptonic final state**
- Statistical uncertainties determined from **number of events per bin**, after a binning optimisation
- Added a **3% systematic uncertainty** to the statistical uncertainty



ABSOLUTE CROSS-SECTIONS MEASURED TO $\sim 1\%$?

Beam Imaging and Luminosity Calibration

arXiv:1603.03566v1 [hep-ex]

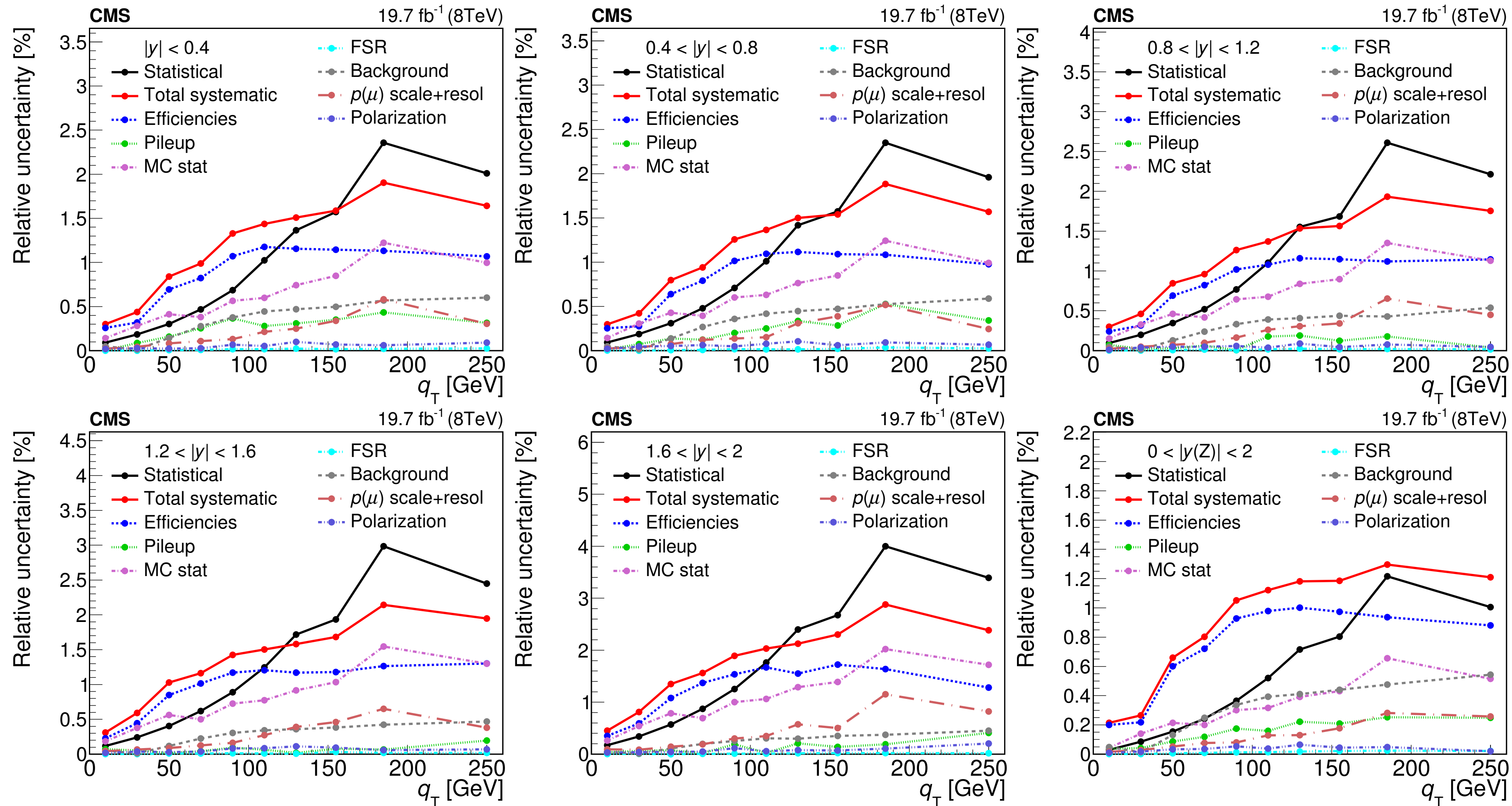
March 14, 2016

Markus Klute, Catherine Medlock, Jakob Salfeld-Nebgen
Massachusetts Institute of Technology

We discuss a method to reconstruct two-dimensional proton bunch densities using vertex distributions accumulated during LHC beam-beam scans. The x - y correlations in the beam shapes are studied and an alternative luminosity calibration technique is introduced. We demonstrate the method on simulated beam-beam scans and estimate the uncertainty on the luminosity calibration associated to the beam-shape reconstruction to be below 1%.

Z P_T

CMS Z p_T uncertainties (normalised to total fiducial)



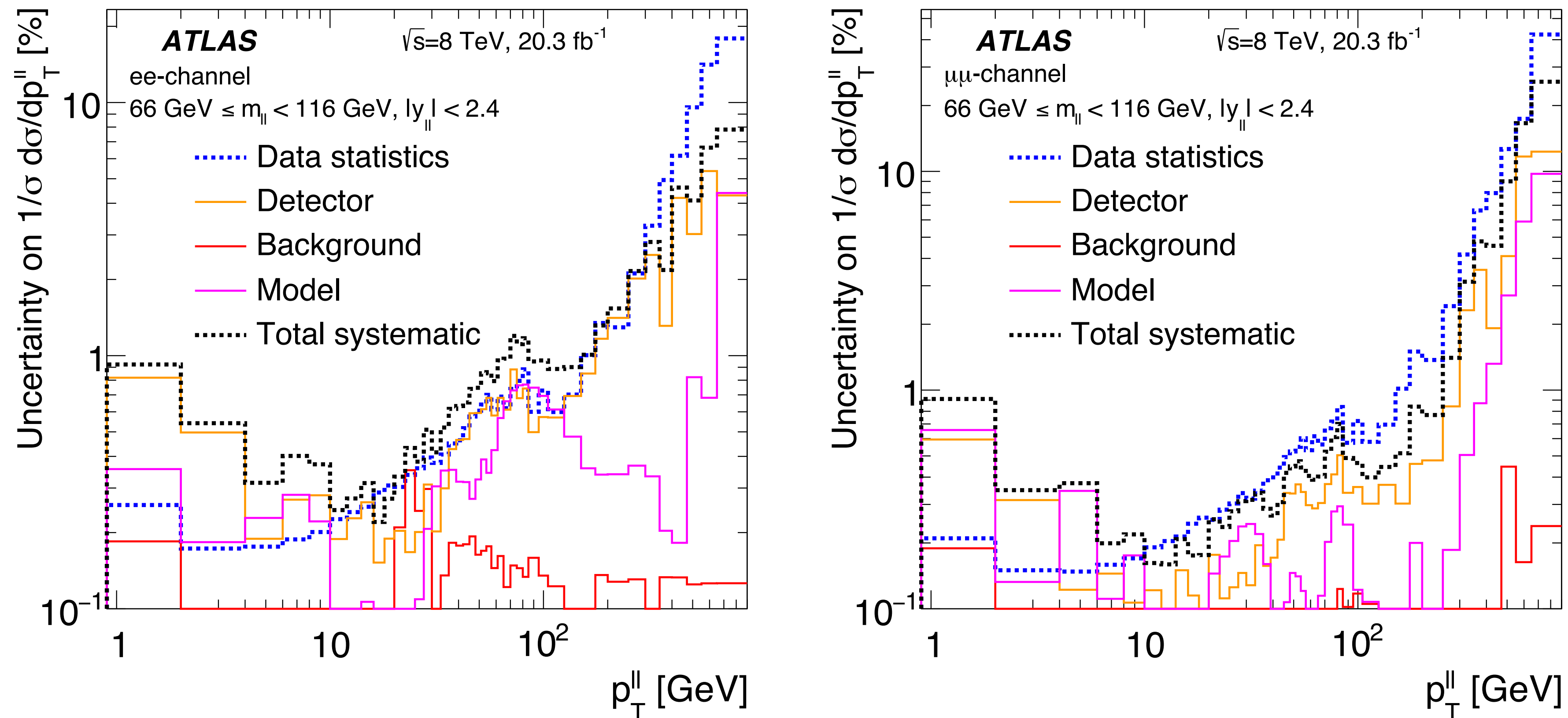
Uncertainties seem significantly larger for CMS.

Where are the differences wrt ATLAS?

1504.03511

Figure 1: Relative uncertainties in percent of the normalised fiducial cross section measurement. Each plot shows the q_T dependence in the indicated ranges of $|y|$.

ATLAS Z p_T uncertainties (normalised to total fiducial)



Uncertainties seem significantly larger for CMS.

Where are the differences wrt ATLAS?

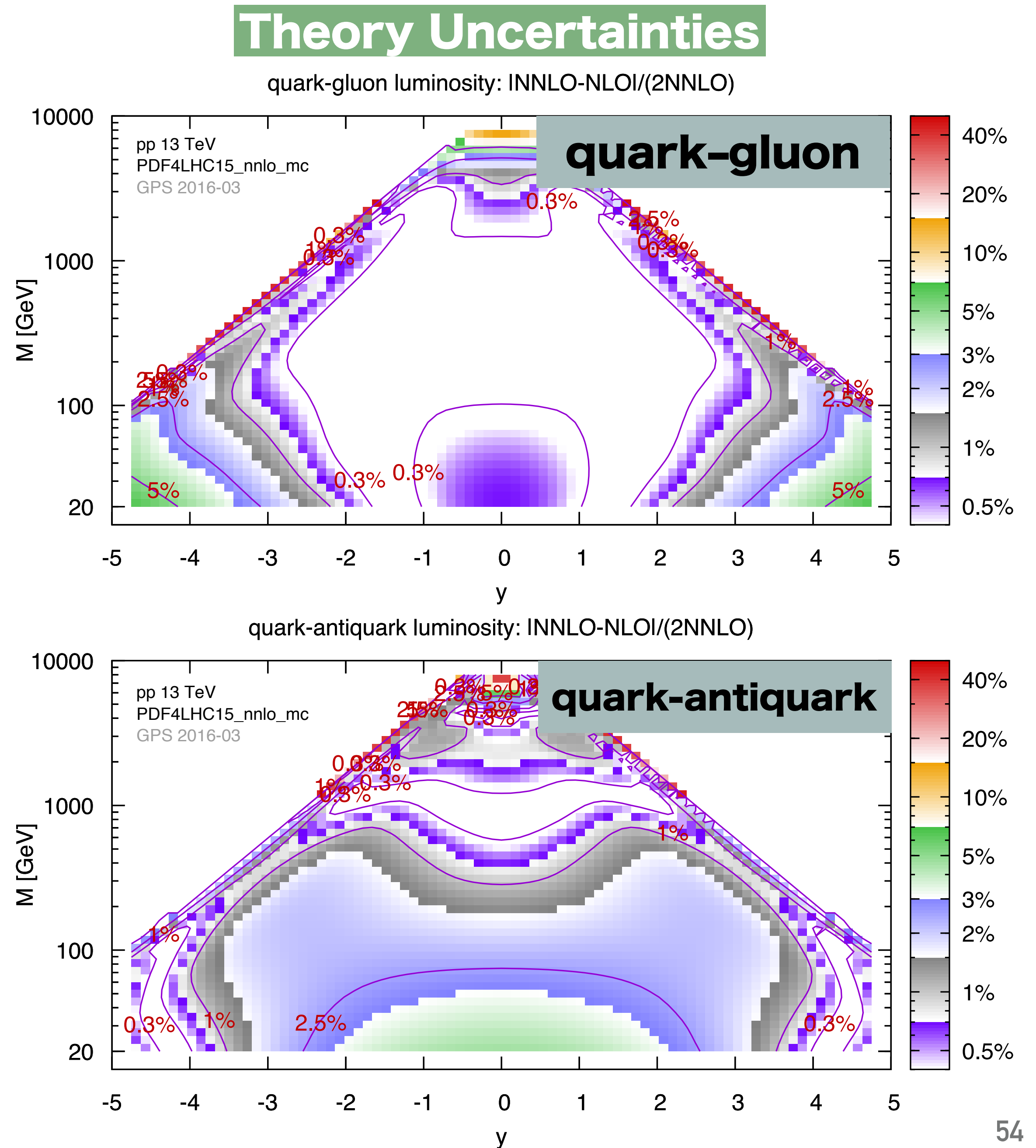
1512.02912

Figure 4: Uncertainty from various sources on $(1/\sigma) d\sigma/d\phi_{\eta}^*$ (top) and $(1/\sigma) d\sigma/dp_T^{\ell\ell}$ (bottom) for events with $66 \text{ GeV} < m_{\ell\ell} < 116 \text{ GeV}$ and $|y_{\ell\ell}| < 2.4$. Left: electron-pair channel at dressed level. Right: muon-pair channel at bare level.

PDFS

WHAT ROUTE FOR PROGRESS?

- Current status is 2–3% for core “precision” region
- Path to 1% is not clear — e.g. $Z p_T$'s strongest constraint is on qg lumi, which is already best known (why?)
- It'll be interesting to revisit the question once $t\bar{t}$, incl. jets, $Z p_T$, etc. have all been incorporated at NNLO
- Can expts. get **better lumi determination?**
- [is it time for PDFs to include theory uncertainties?]

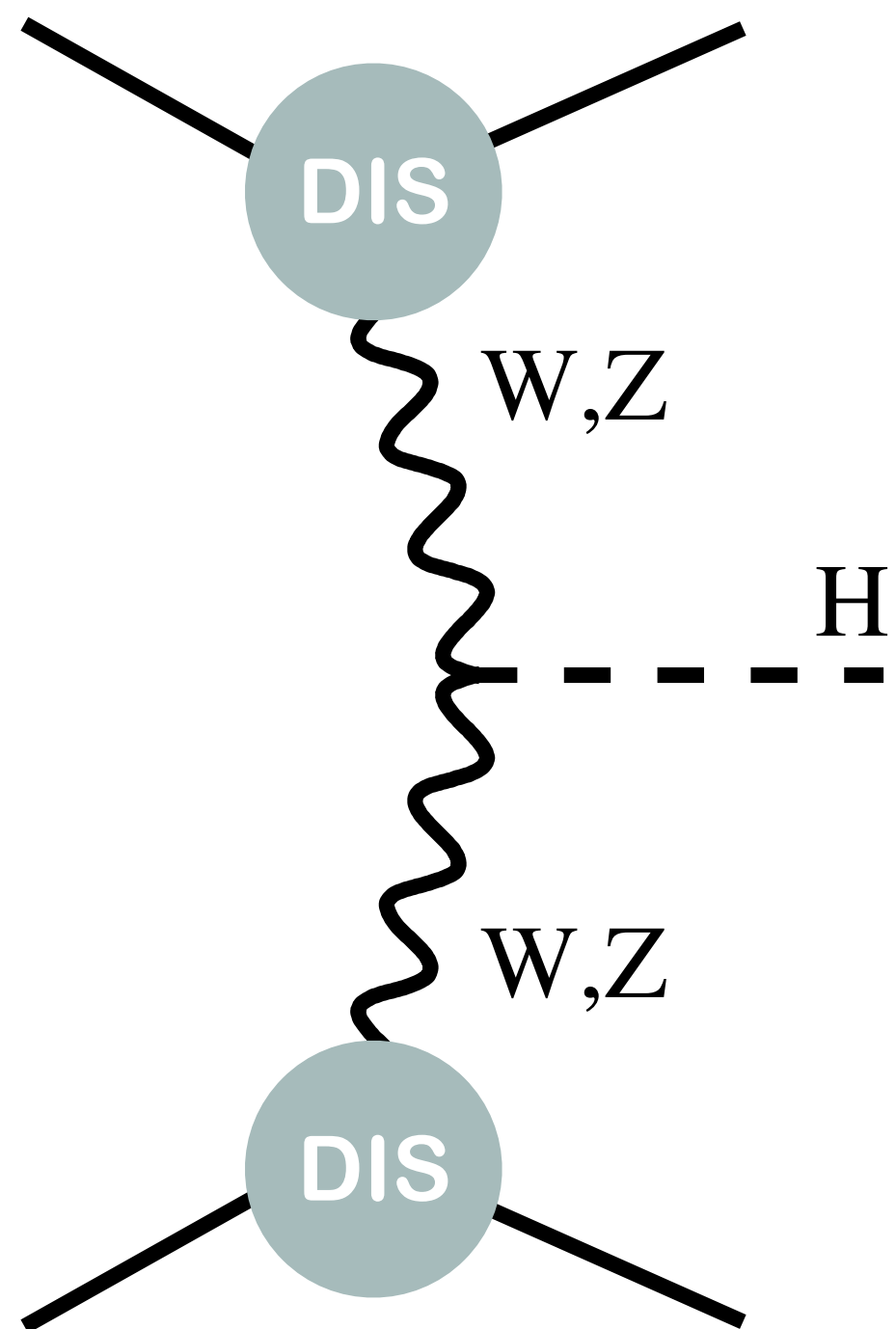


VBF HIGGS PRODUCTION

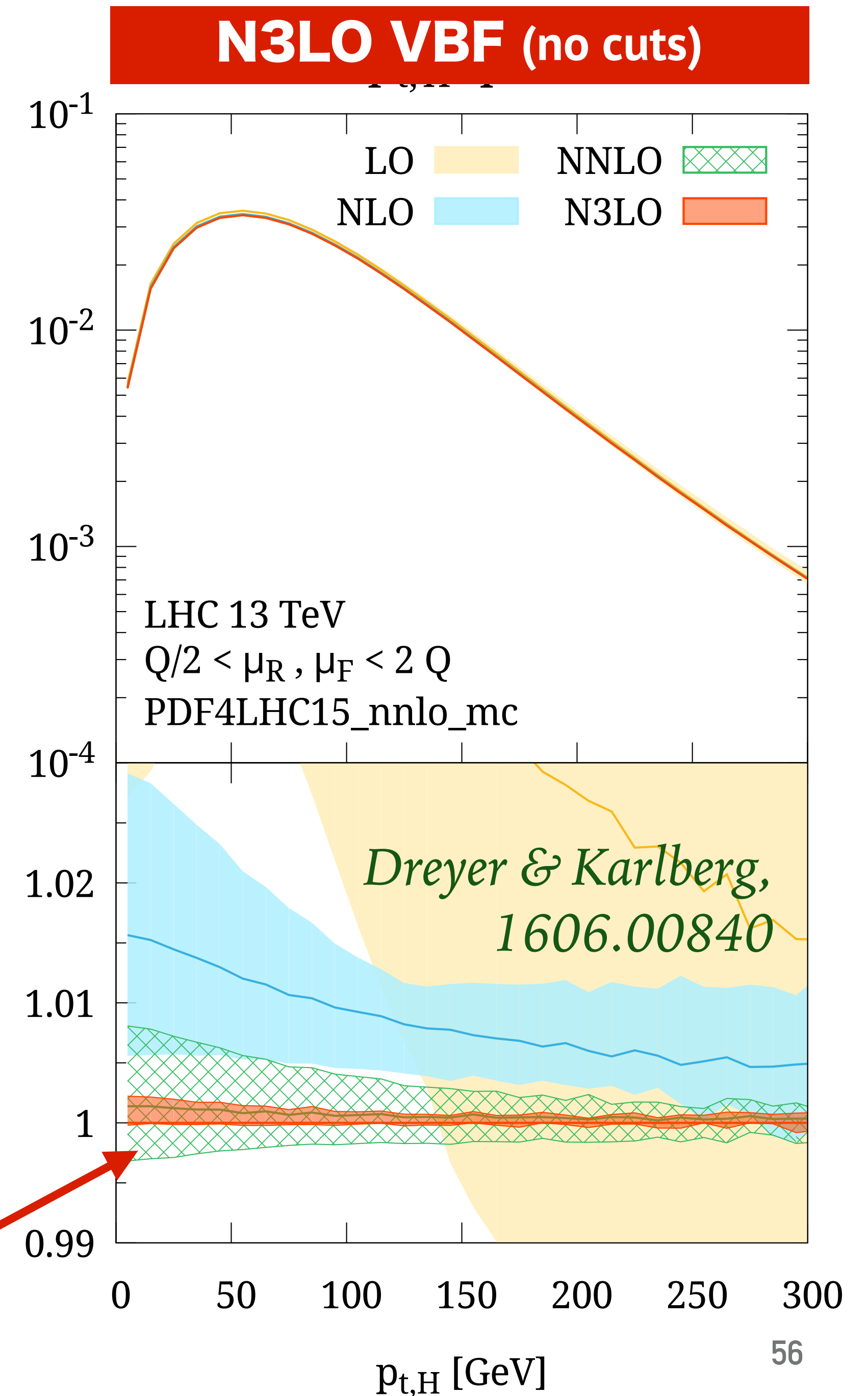
VECTOR-BOSON FUSION → HIGGS

- ▶ double DIS approximation is powerful tool for VBF, using structure functions for the W/Z production (Han, Valencia & Willenbrock 1992, NNLO by Bolzoni et al 1003.4451)

- ▶ Now extended to N3LO, shows scale uncertainties $\ll 1\%$ for observables inclusive wrt the jets
- ▶ good stability from NNLO to N3LO



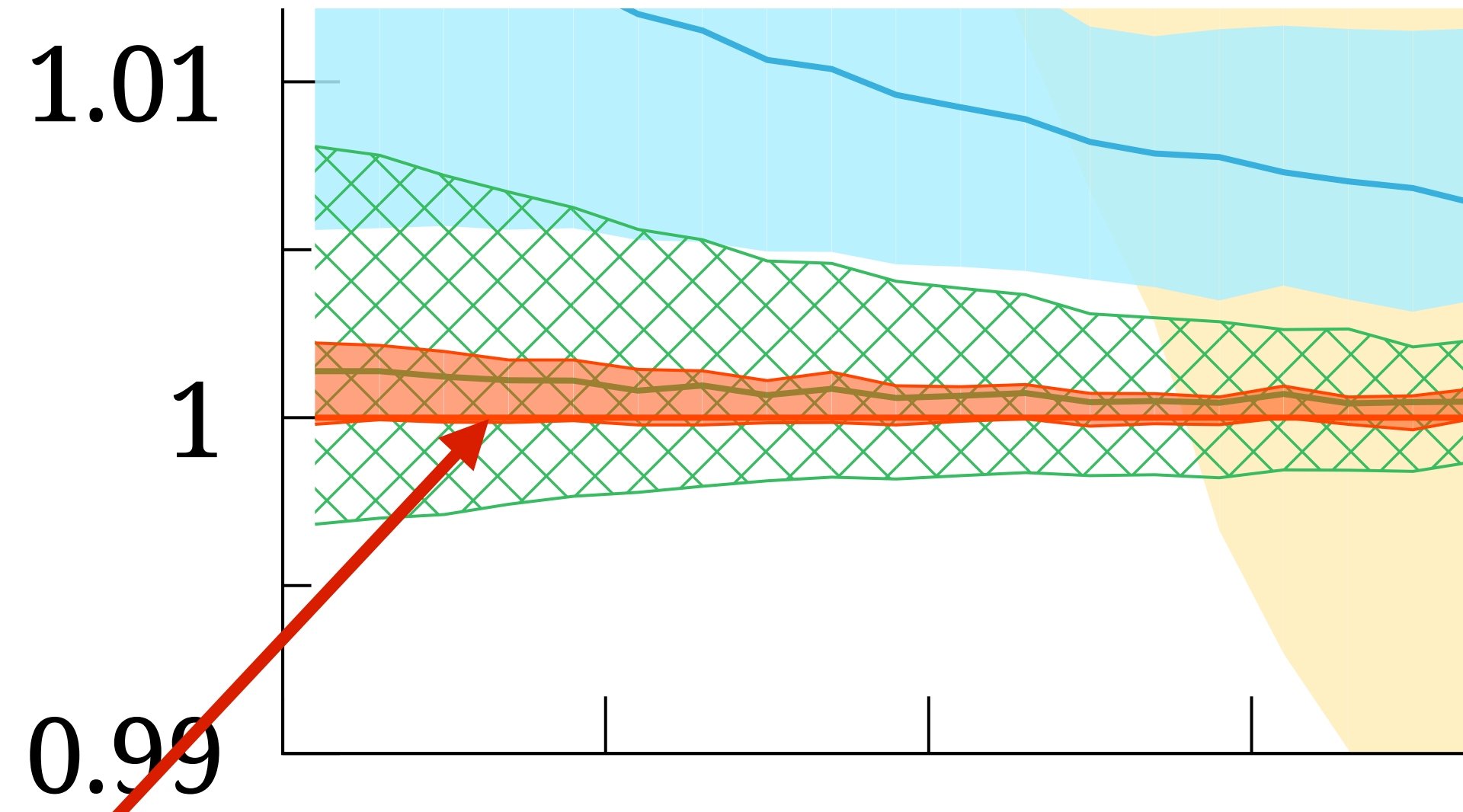
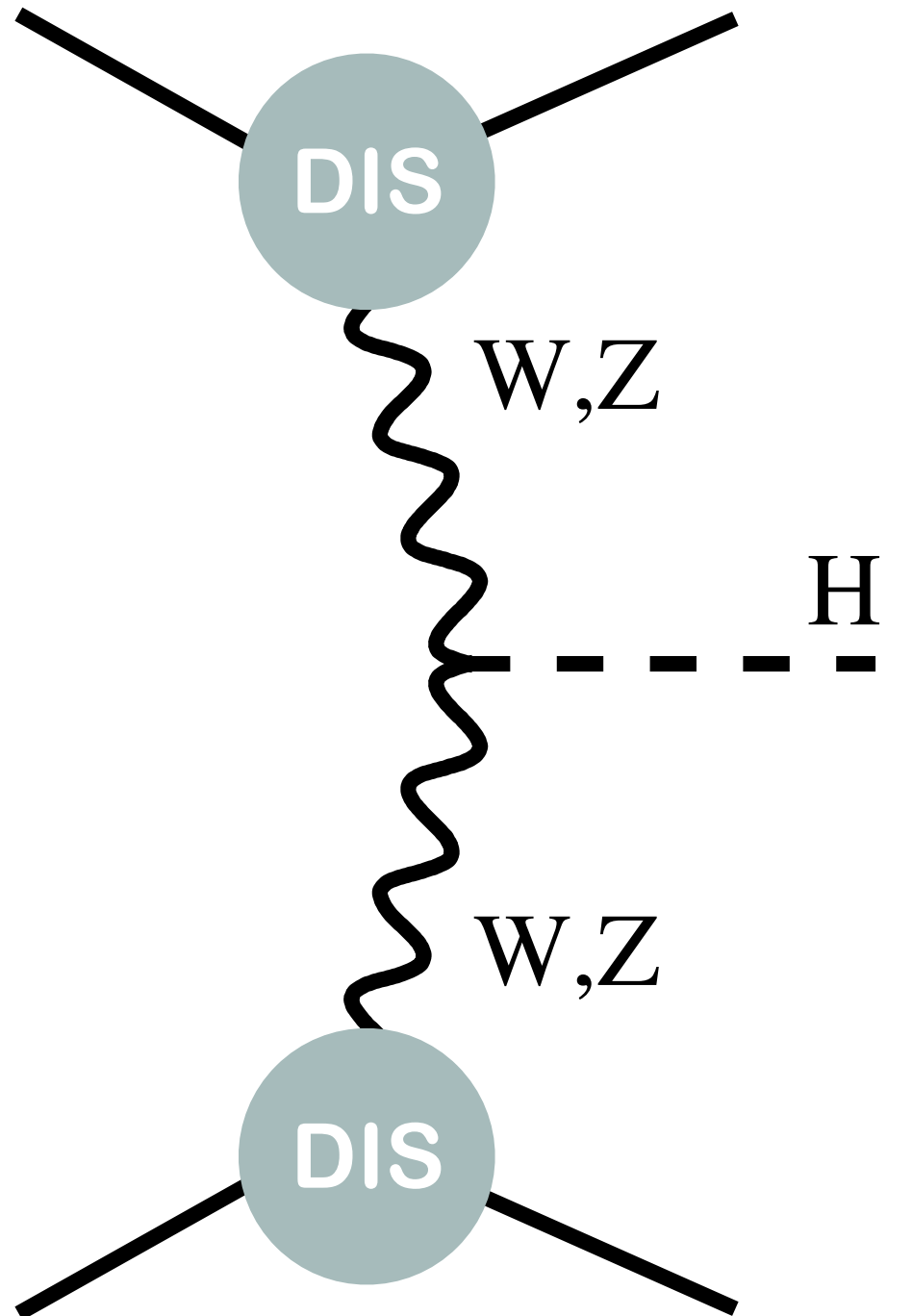
N3LO



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Dreyer & Karlberg, 1606.00840

N3LO

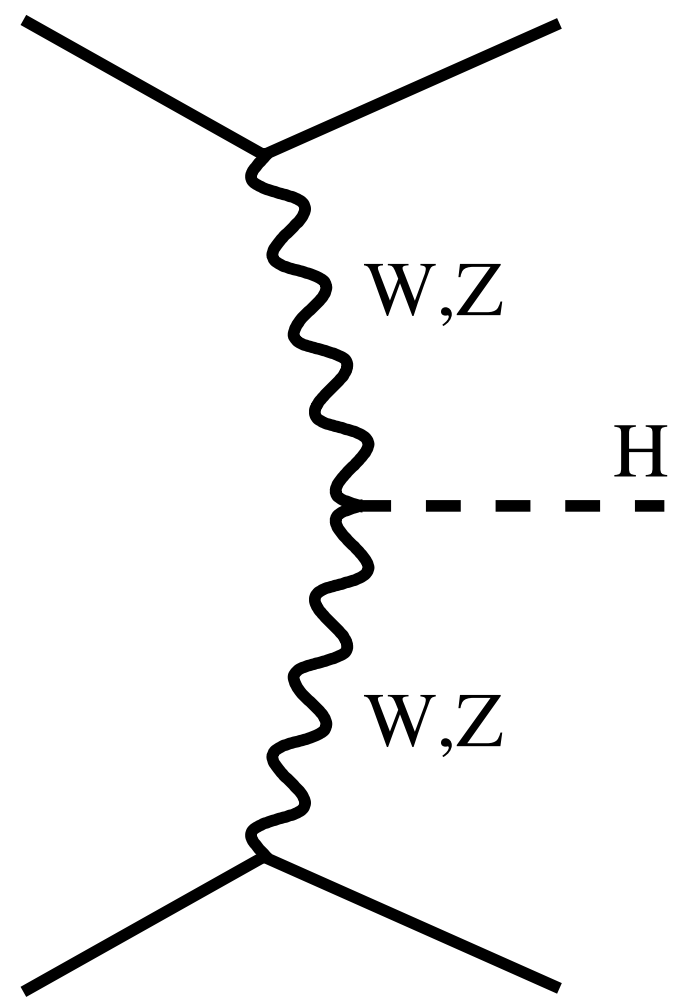
*Exact in “ $QCD_1 \otimes QCD_2$ ”
Non-trivial real-world corrections believed $< 1\%$*

VBF with cuts on jets: Projection to Born method

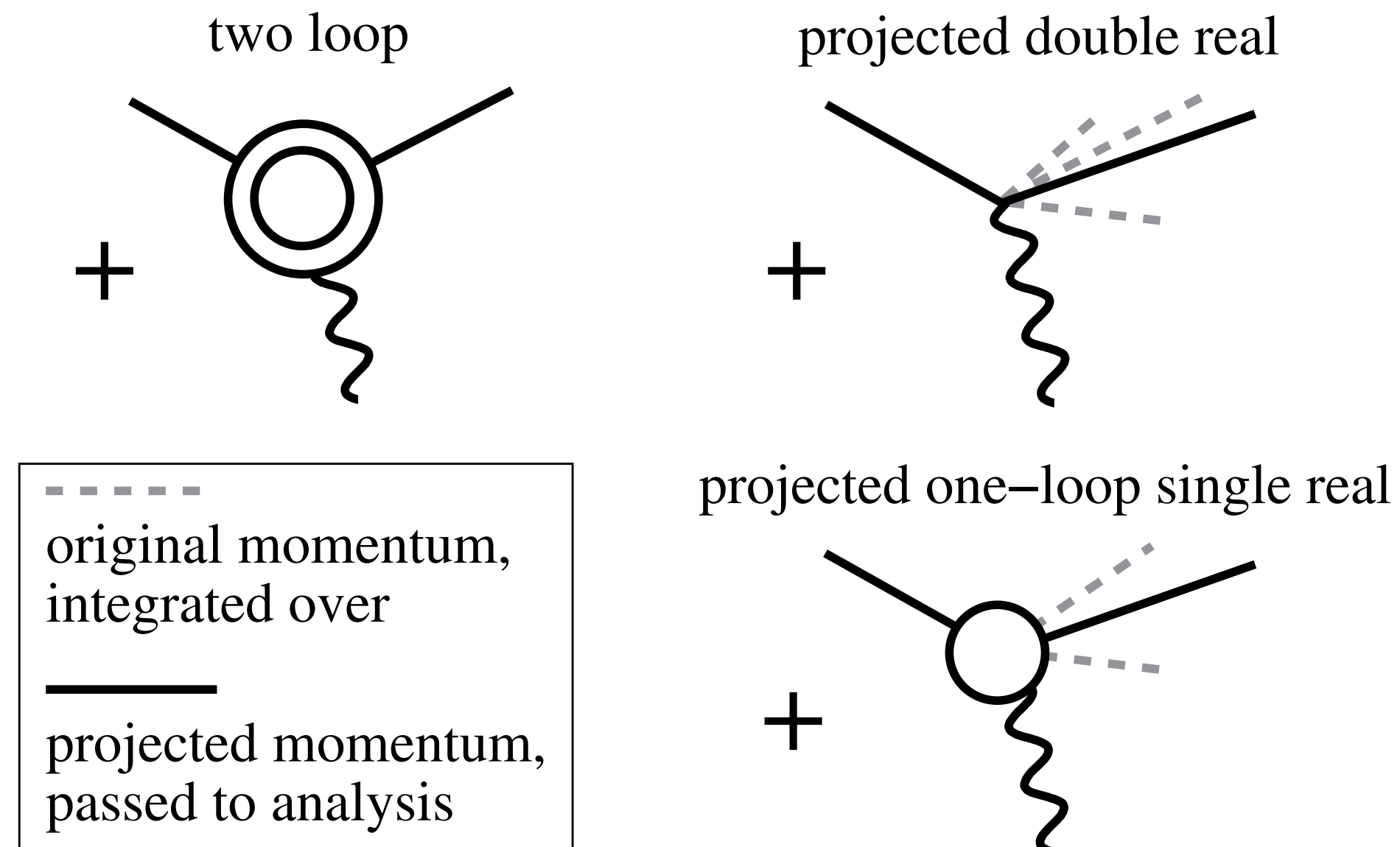
Cacciari, Dreyer, Karlberg, GPS & Zanderighi, 1506.02660

Exact in "QCD₁ ⊗ QCD₂"

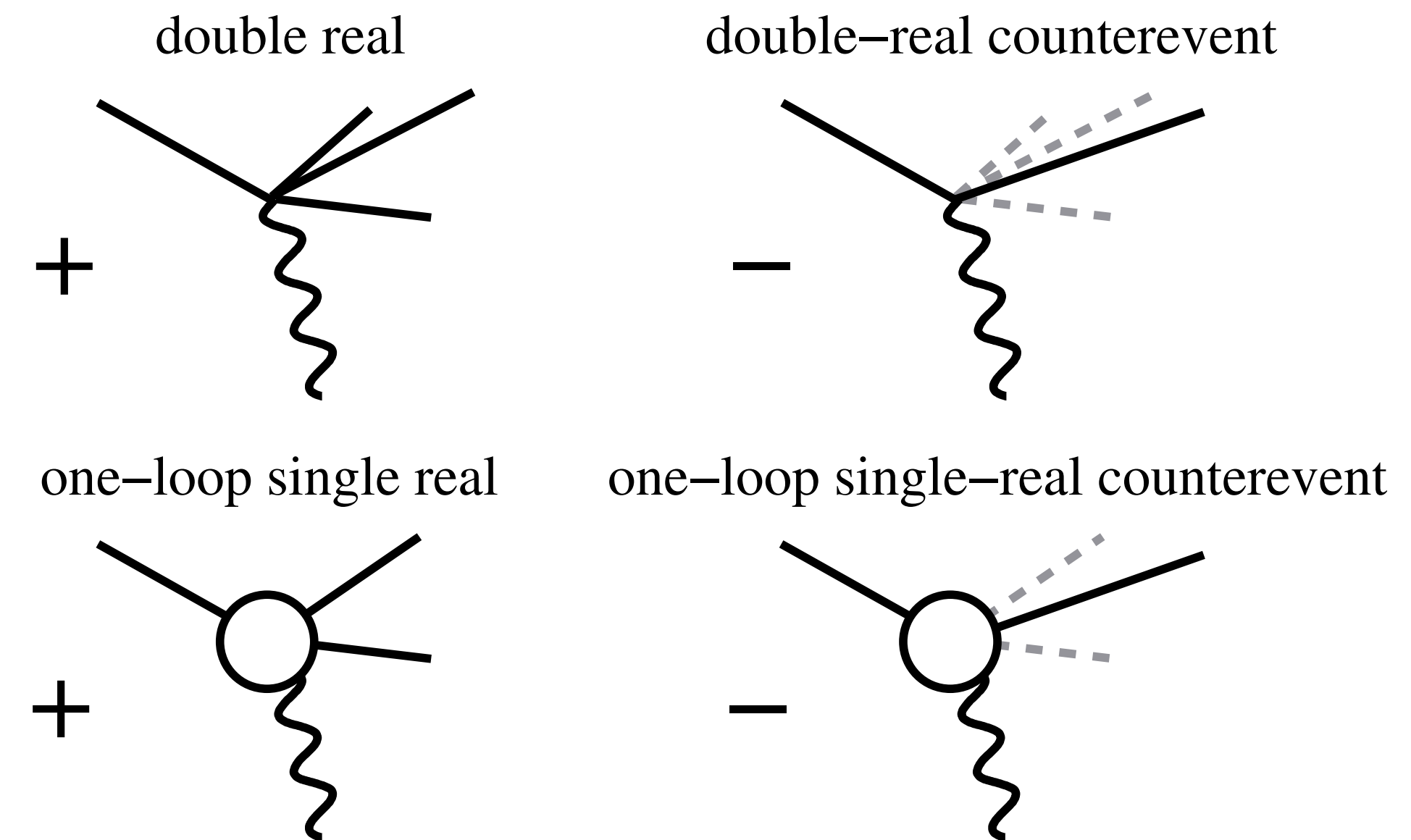
(a) Born VBF process



(b) NNLO "inclusive" part (from structure function method)



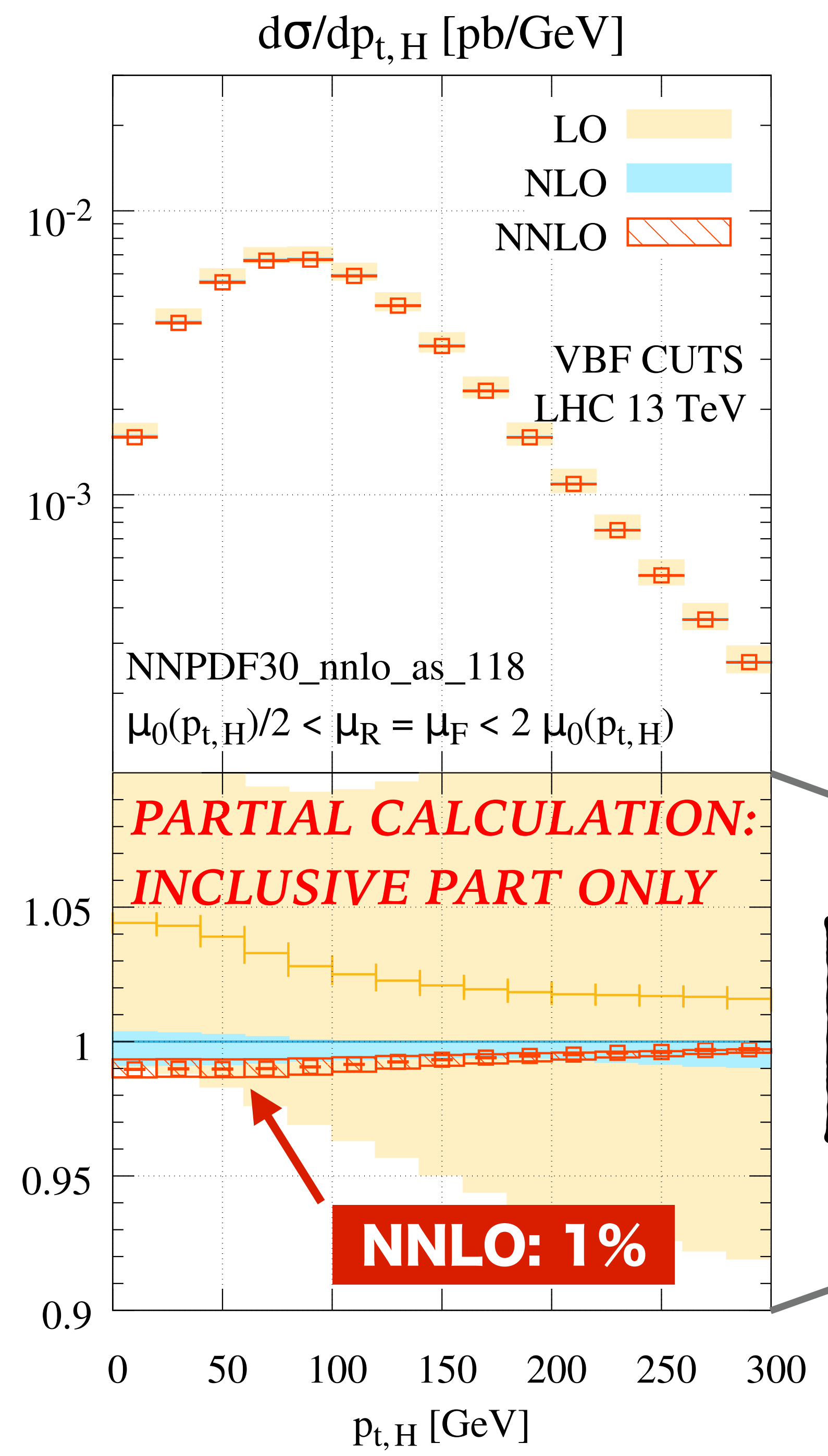
(c) NNLO "exclusive" part (from VBF H+3j@NLO)



using VBF 3-jet @ NLO from Jäger, Schissler & Zeppenfeld, 1405.6950

Inclusive part only (with VBF cuts)

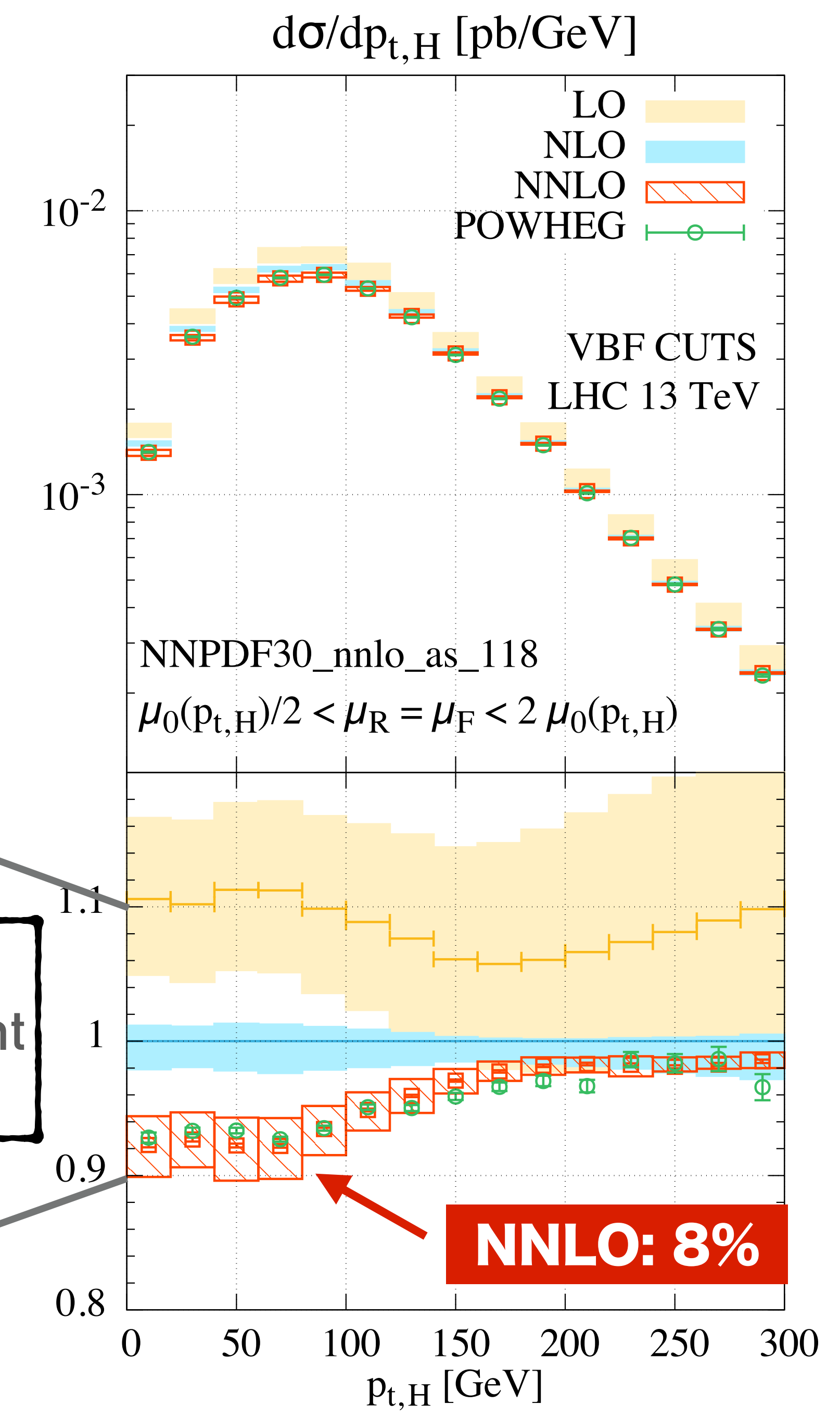
NNLO is 1% effect



Full calculation (with VBF cuts)

NNLO is up to 8% effect

Almost all of which comes from jet fragmentation



2 KINDS OF EFFECT IN SUCH PROCESSES ?

- “Inclusive” correction to process as a whole (insofar as this is meaningful)
- corrections related to jet fragmentation

Can we make such a distinction meaningful?

Can we examine same idea in other contexts? **E.g. inclusive jet spectrum**

- There is no way of defining the “inclusive” part in most cases
- But there are arguments that for a jet radius $R_m \approx 1$, ISR and FSR effects mostly cancel each other [*Soyez, 1006.3634*]
- So try looking at effect of NNLO corrections relative to $R_m = 1$ [*can be done with NLO 3-jet calcⁿ from NLOJET++*]

*Dasgupta, Dreyer, GPS
& Soyez, 1602.01110*

$$\sigma^{\text{NNLO}}_R(R, R_m) \equiv \underbrace{\sigma_0 + \sigma_1(R)}_{\text{NLO}} + \underbrace{[\sigma_2(R) - \sigma_2(R_m)]}_{\substack{\text{R-dependent piece of} \\ \text{NNLO, relative to } R_m}}$$

- Full NNLO will have an additional NNLO term associated with the effective K-factor for the “inclusive” piece — we miss that part (and unlike VBF, it may not be small)

JETS

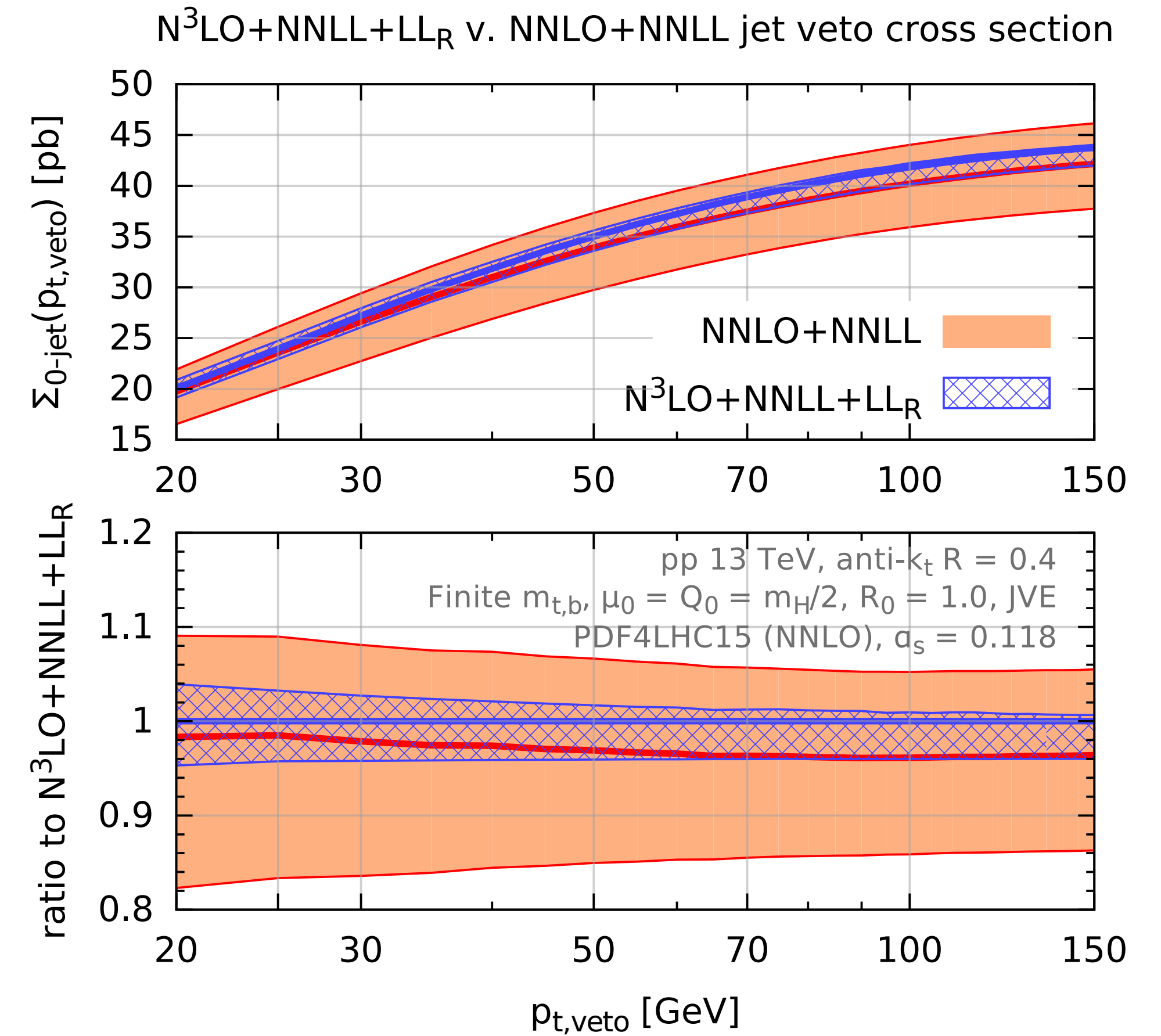
HIGGS JET VETO @ N3LO + NNLL

Anastasiou, Duhr, Dulat, Herzog & Mistlberger 1503.06056

Boughezal, Caola, Melnikov, Petriello & Schulze 1504.07922

*Banfi, Caola, Dreyer, Monni, GPS, Zanderighi & Dulat
1511.02886*

- N3LO effects at 2–4%
- **Residual uncertainty up to 4%** (fairly conservative estimate)



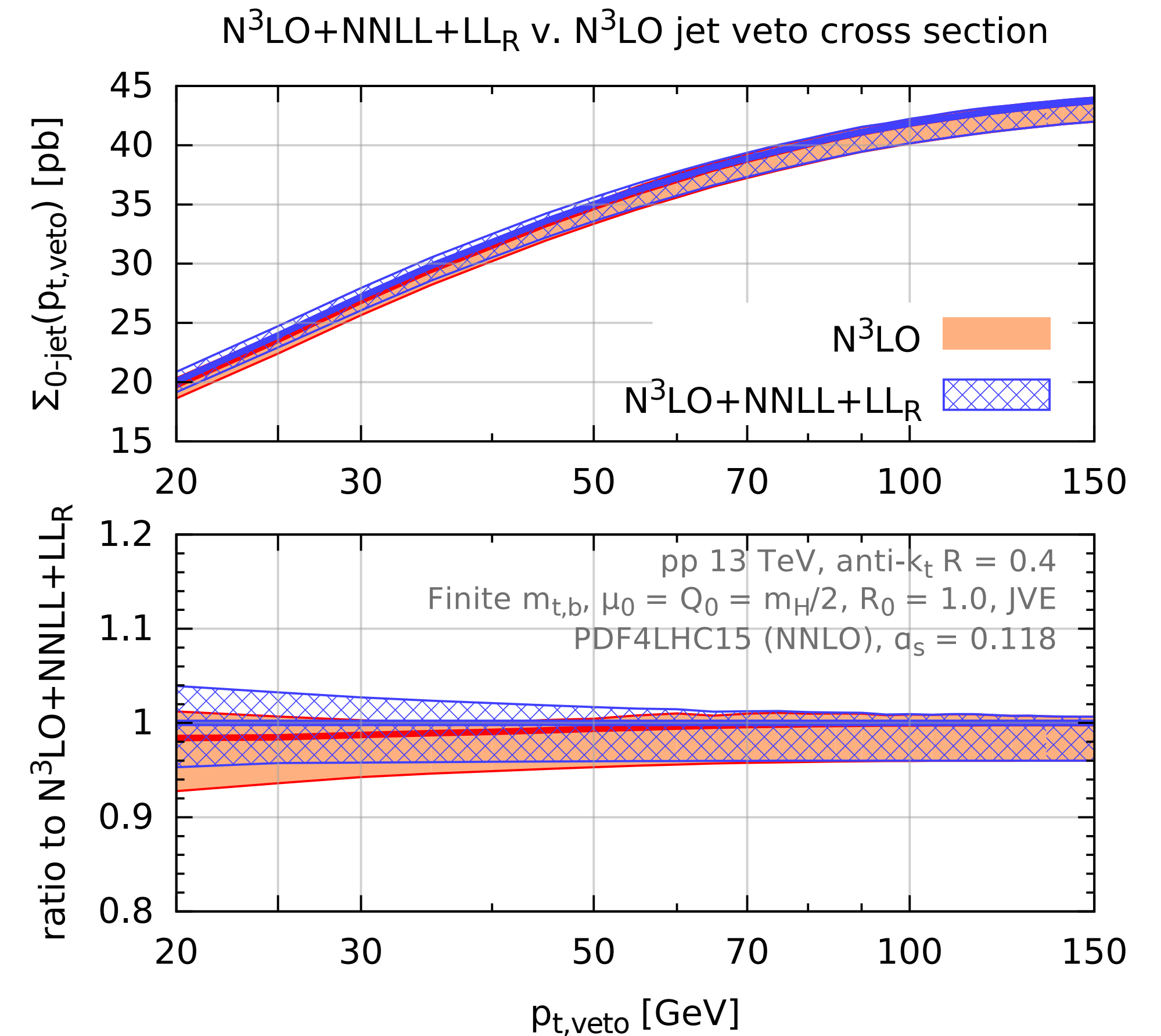
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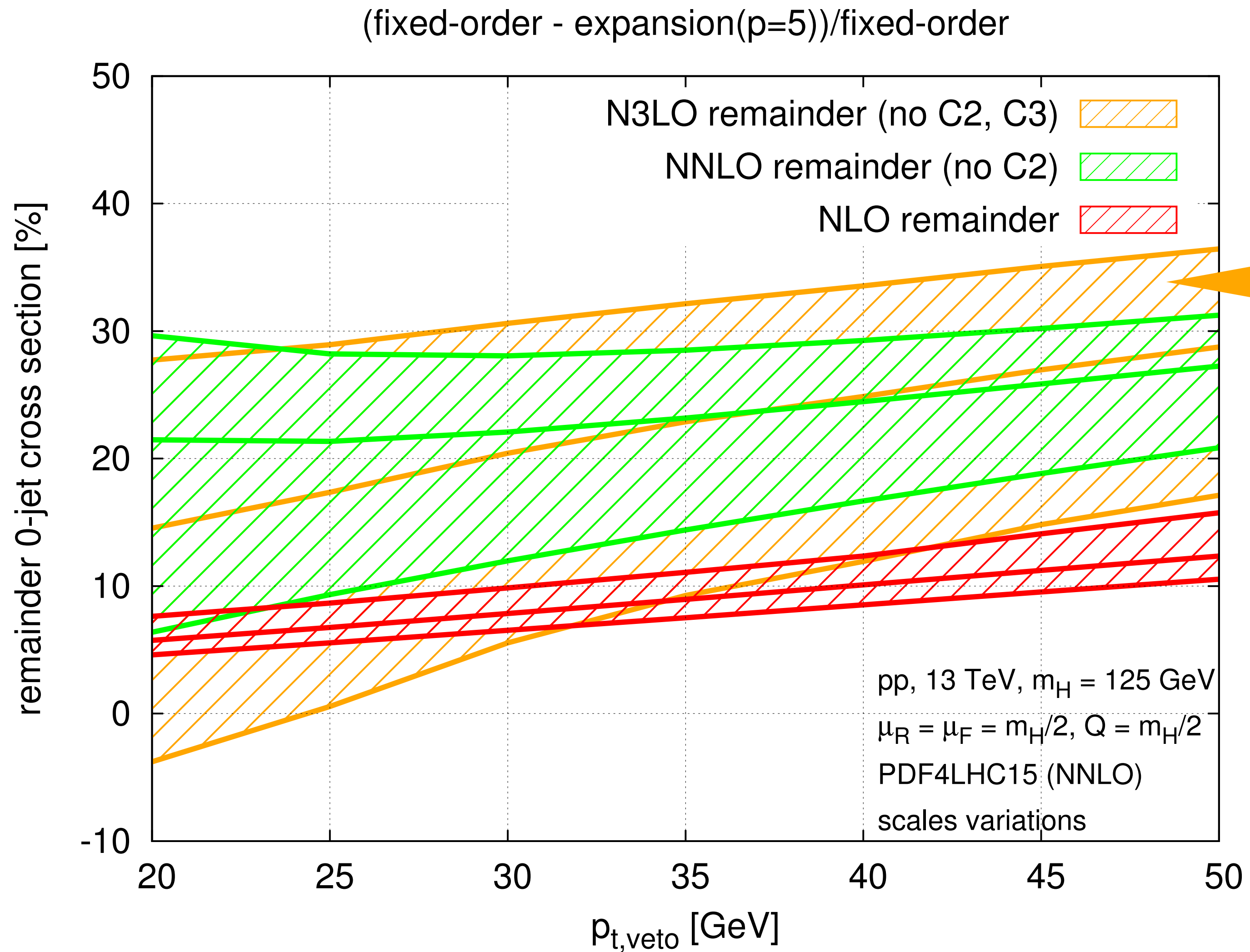
Boughezal, Caola, Melnikov, Petriello & Schulze 1504.07922

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- N3LO effects at 2–4%
- Residual uncertainty up to 4% (fairly conservative)
- rather stable ($\sim 2\%$) wrt jet- p_T resummation effects



how good is resummation at finite p_t ?



$$\frac{\text{N3LO-NNLL@N3LO}}{\text{N3LO}}$$

- Resummation is designed for $p_t \ll m_H$,
- At what point does it actually become relevant?
- From figure, for $p_t/m_H \sim 0.4$ it already captures 70% of fixed order

thanks to P. Monni for producing this plot

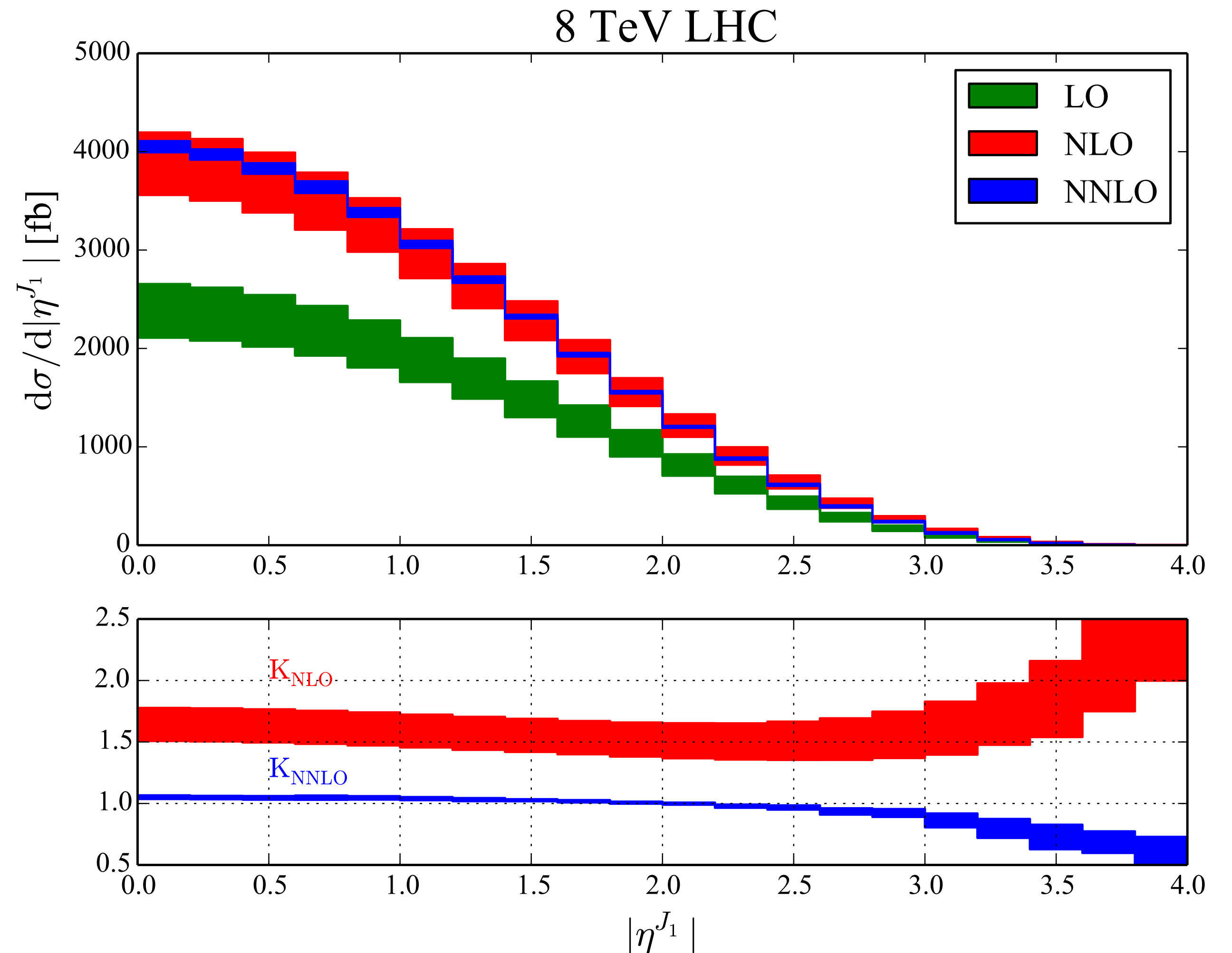
THE JET IN Z+JET @ NNLO

Boughezal, Liu & Petriello, 1602.08140

1-jet cross sections

	σ_{LO} (pb)	σ_{NLO} (pb)	σ_{NNLO} (pb)	K_{NLO}	K_{NNLO}
8 TeV	$4.17^{+0.55}_{-0.47}$	$6.59^{+0.62}_{-0.53}$	$6.86^{+0.01}_{-0.13}$	1.58	1.04
13 TeV	$9.12^{+0.88}_{-0.79}$	$14.90^{+1.29}_{-1.06}$	$15.54^{+0.01}_{-0.24}$	1.63	1.04

- NNLO K-factor is 4%
- Residual scale uncertainty < 2%



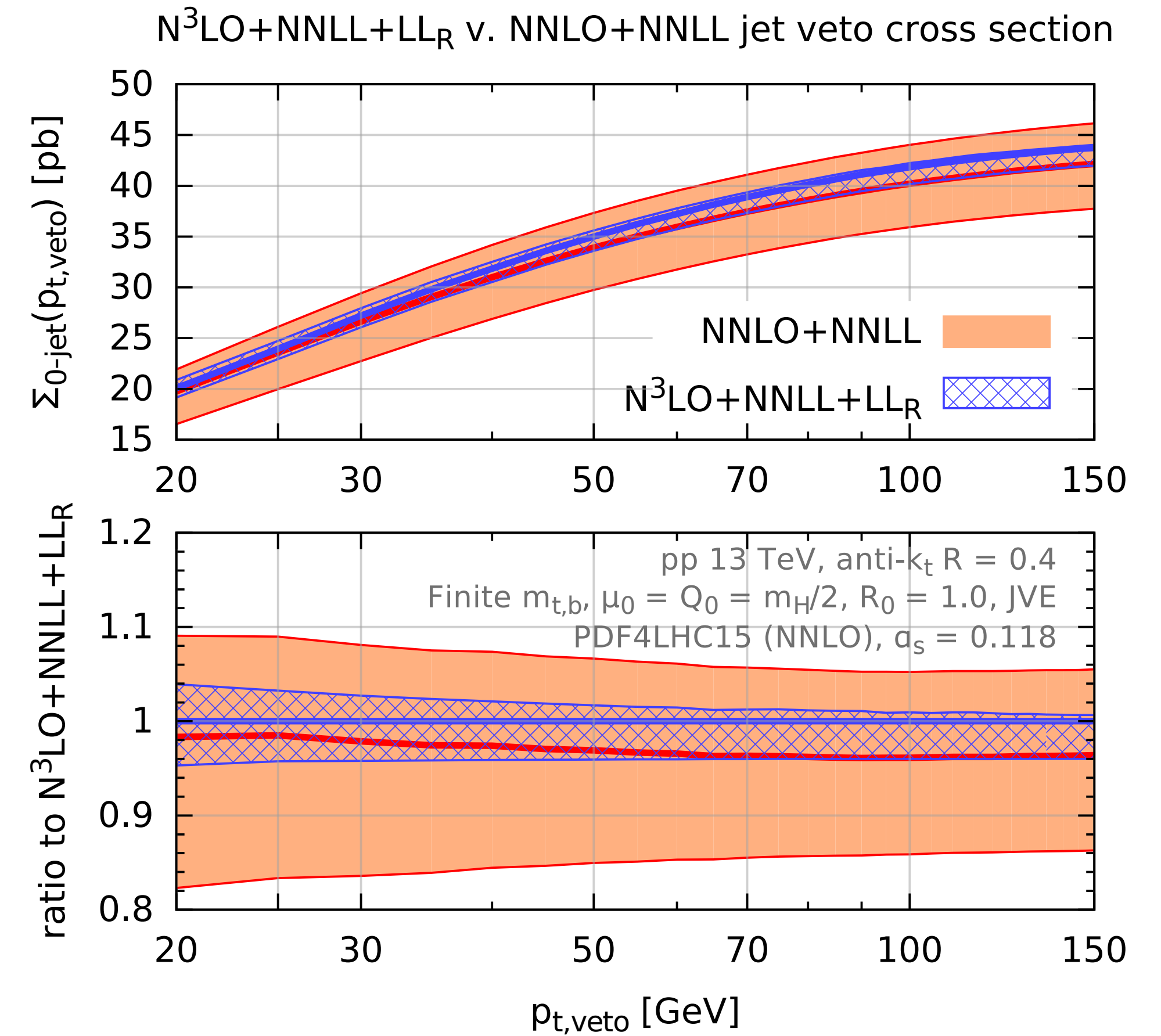
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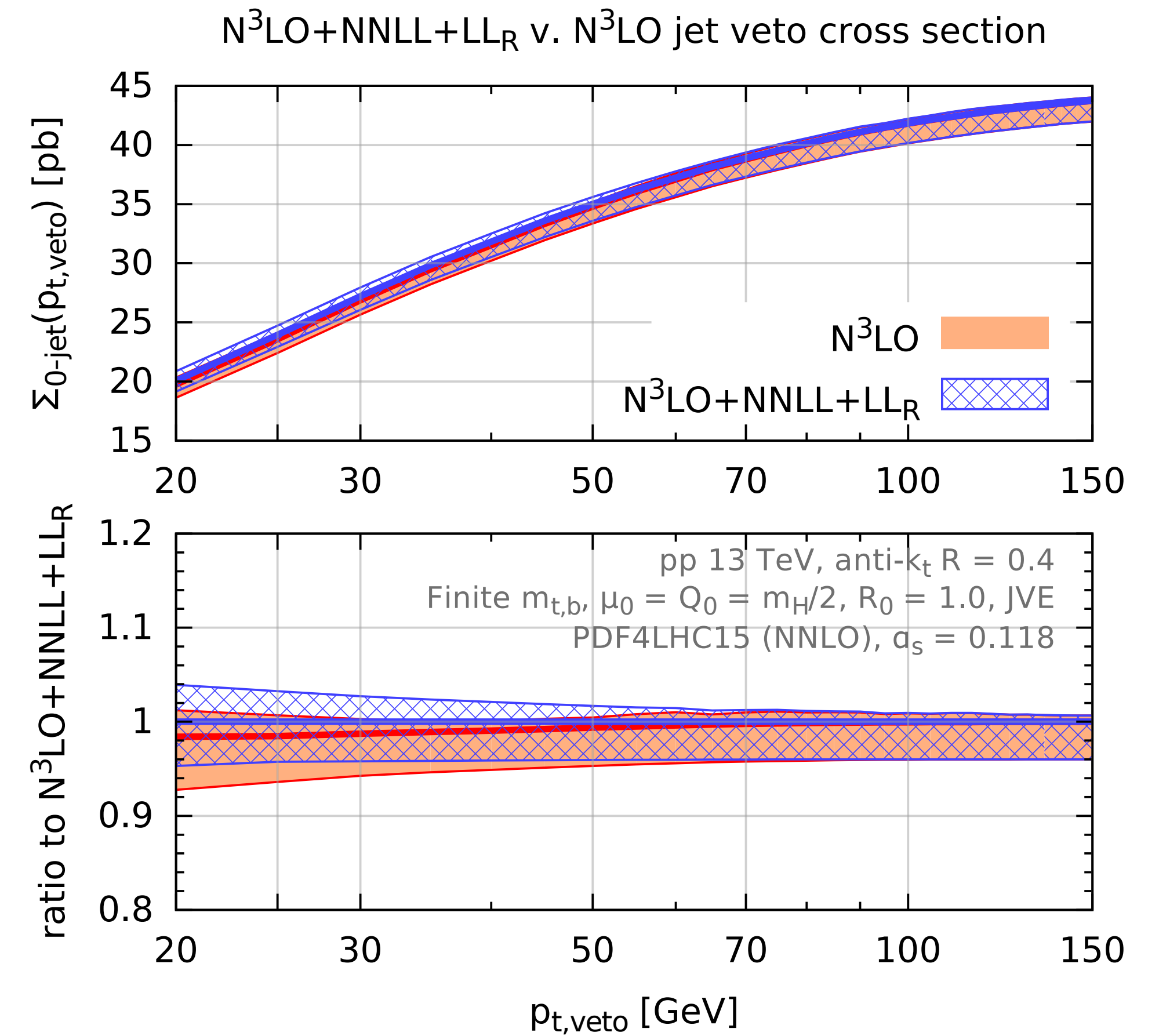
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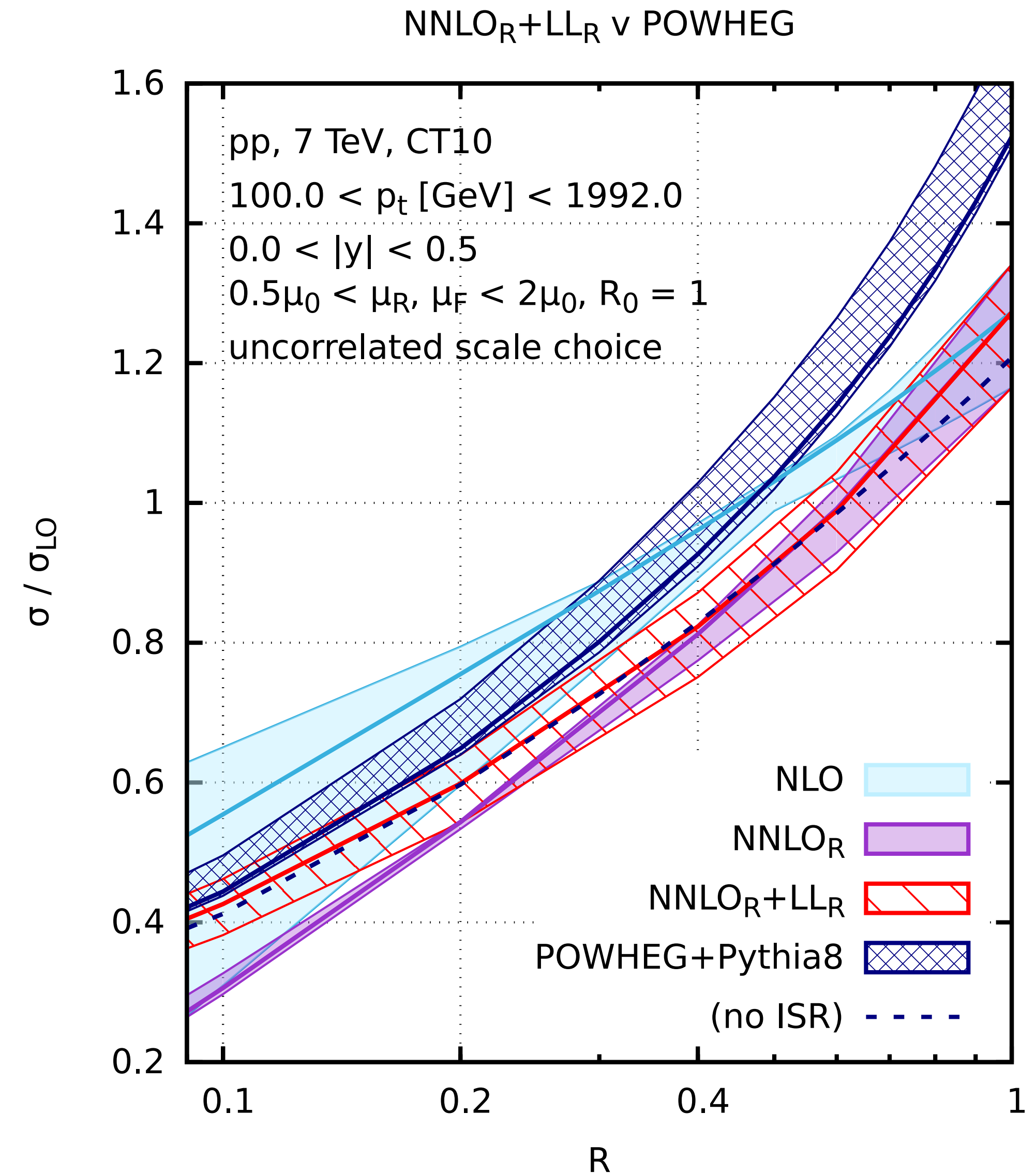
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NNLO_R & small-R resummation

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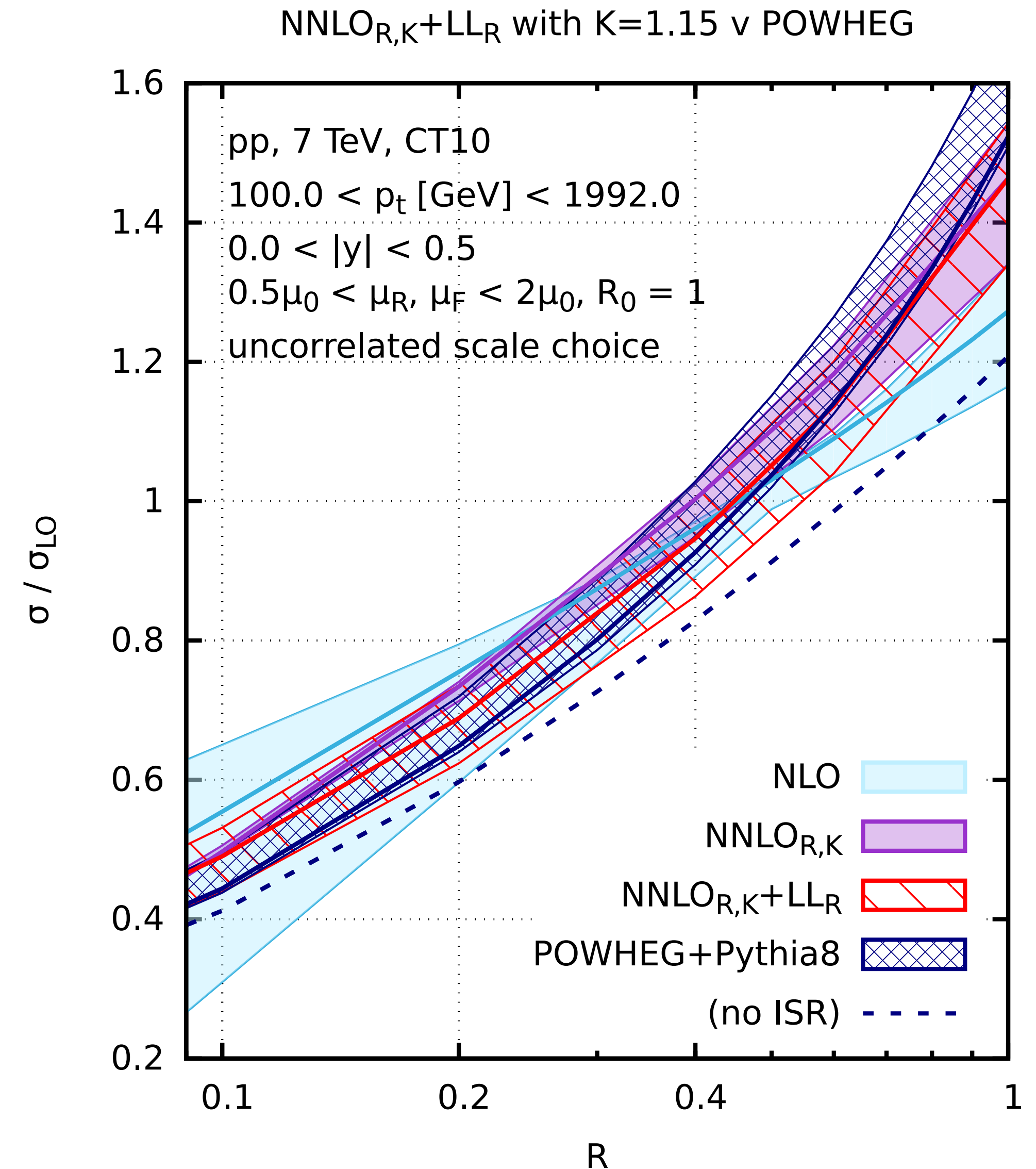
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NNLO_R & small-R resummation

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SMALL-R APPROX.

NLL SMALL-R TERMS

