

Physics motivations for sub-percent absolute cross sections

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** on leave from CERN and CNRS*



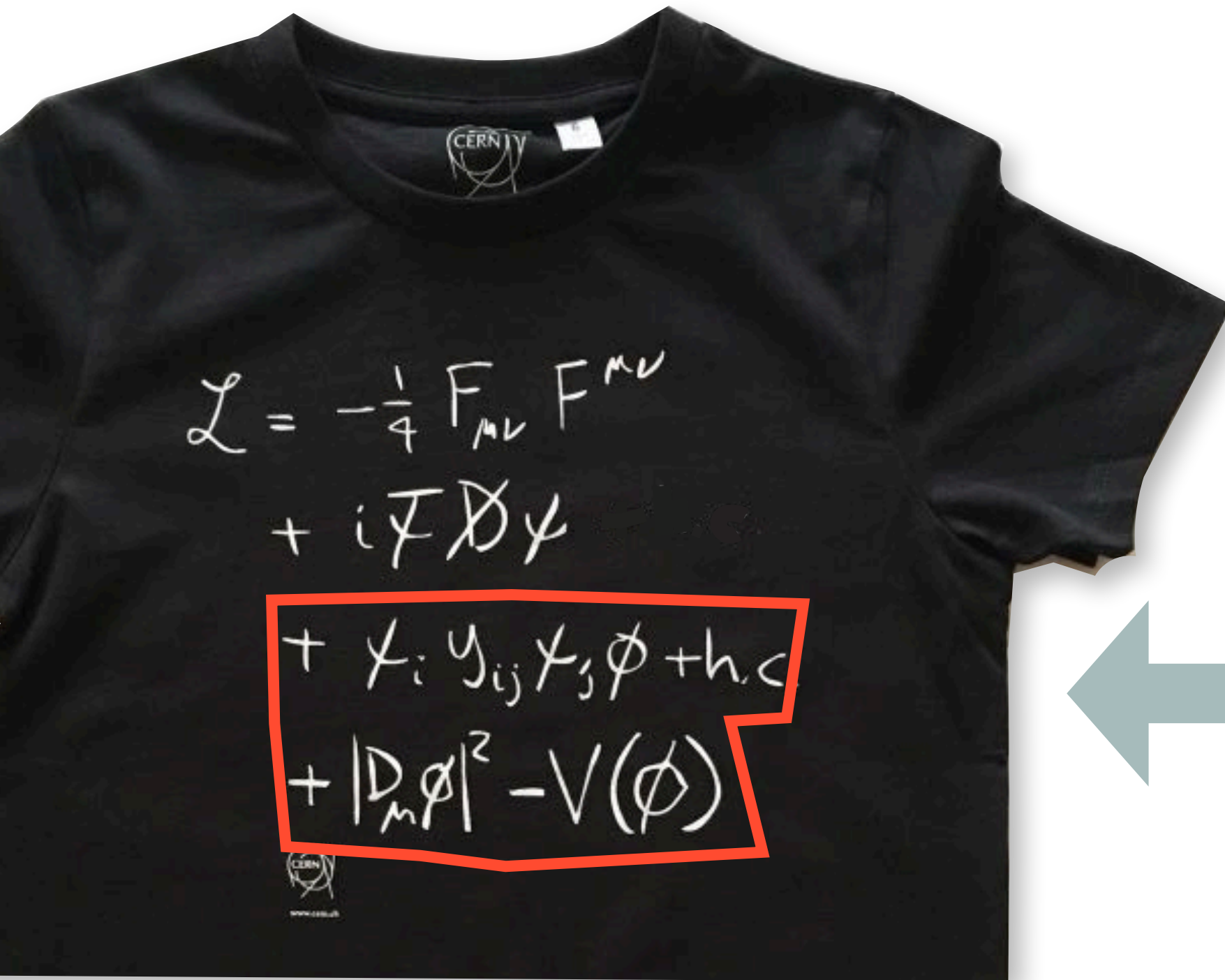
THE ROYAL SOCIETY



European Research Council
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**LHCb UK annual meeting,
University of Warwick, 4 January 2019**

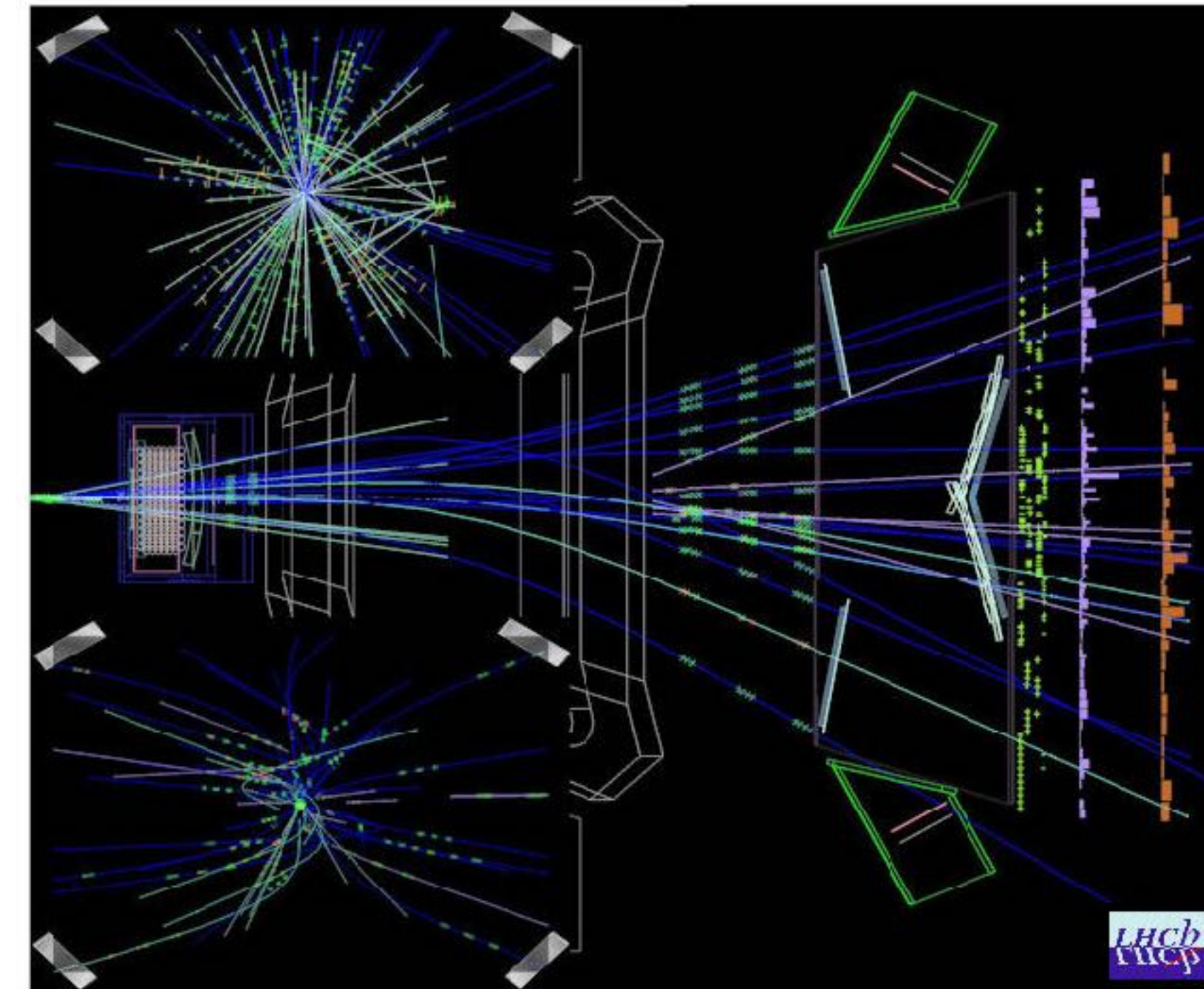
UNDERLYING THEORY



can we achieve sub-percent precision?



EXPERIMENTAL DATA

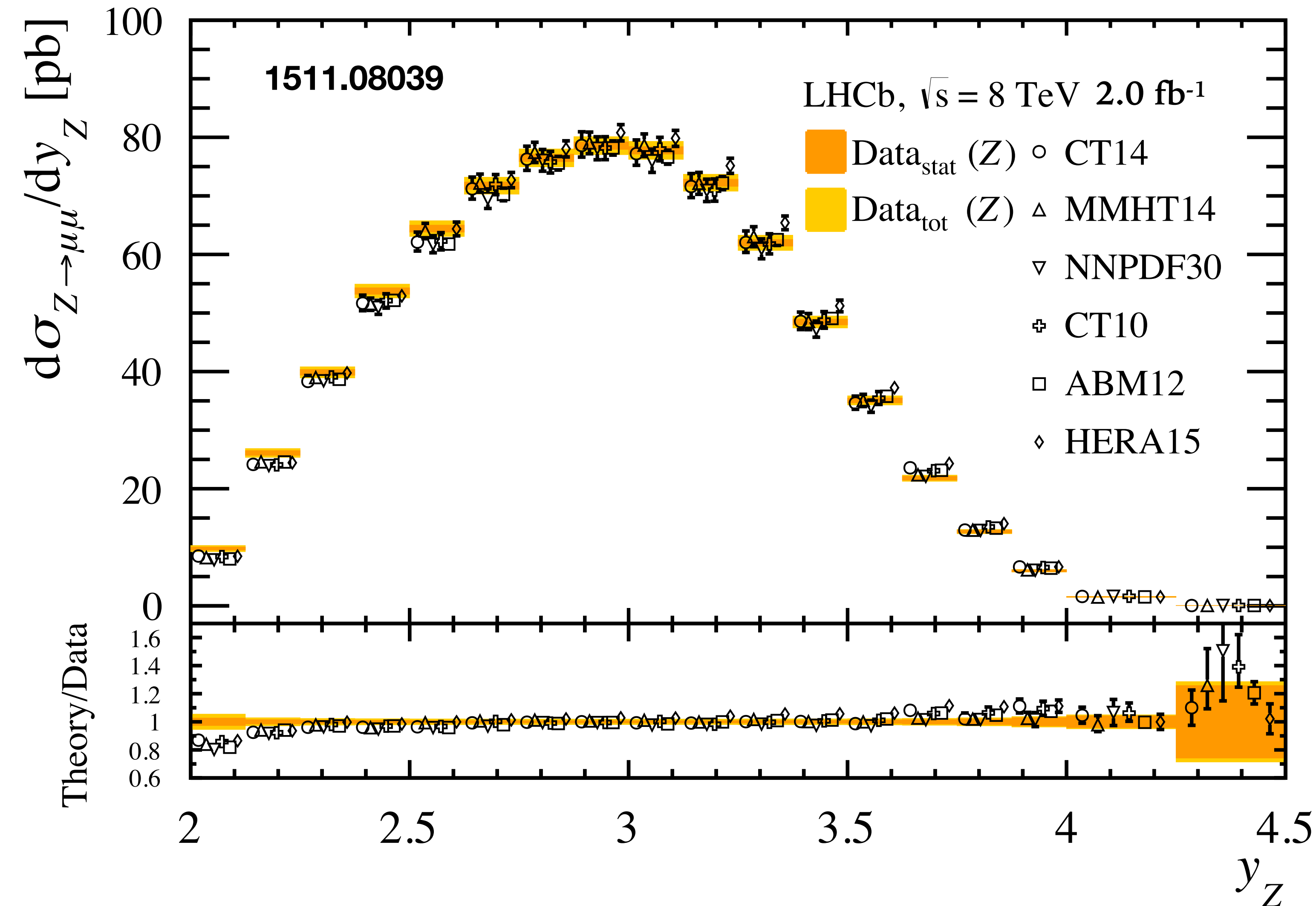


is it experimentally feasible?

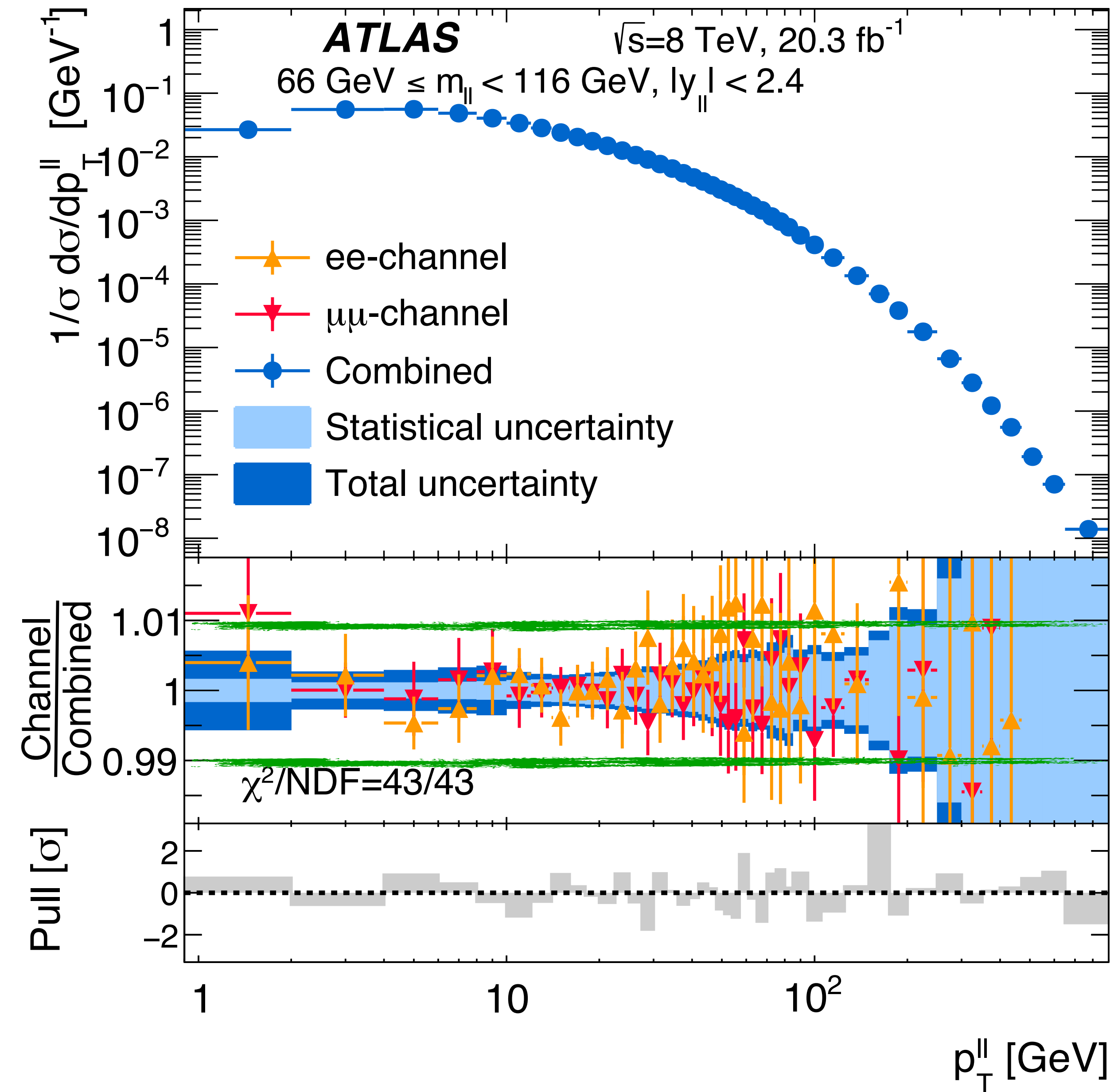
LHCb precision

$$\sigma_{Z \rightarrow \mu^+ \mu^-} = 95.0 \pm 0.3 \pm 0.7 \pm \cancel{1.1} \pm 1.1 \text{ pb,}$$

stat. syst. beam E lumi



LHCb achieves 0.8% uncertainty, aside from luminosity uncertainty (beam energy systematic greatly improved since this paper)



Other experiments?

One of the most precise results are perhaps for the Z transverse momentum (ATLAS)

- normalised to Z fiducal σ
- achieves $<1\%$, from $p_{\text{T}} = 1$ to 200 GeV , and $<0.5\%$ in some regions

Ratio to total cross section cancels lumi & some lepton-efficiency systematics.

One limiting factor: luminosity uncertainty

Experiment <i>pp</i> running period \sqrt{s} (TeV)	ALICE 2010 7.0	ATLAS 2012 8.0	CMS 2012 8.0	LHCb 2012 8.0		
Absolute-calibration method	<i>vdM</i>	<i>vdM</i>	<i>vdM</i>	<i>vdM</i>	Combined	BGI
Calibration uncertainty $\Delta \sigma_{vis} / \sigma_{vis}$ (%)	3.5	1.2	2.3	1.47	1.12	1.43
μ or total-rate dependence (%)	-	1.4	< 0.1		0.17	
Long-term stability (%)	1.5	0.6	1.0		0.22	
Subtraction of luminosity backgrounds (%)	3.0	0.2	0.5		0.13	
Other luminosity-dependent effects (%)	1.5		0.5		-	
Total luminosity uncertainty (%)	5.0	1.9	2.6	1.5	1.2	1.5

From LHCP 2016 talk by W. Kozanecki

LHCb can do $\pm 1.1\%$. Can that be improved upon?

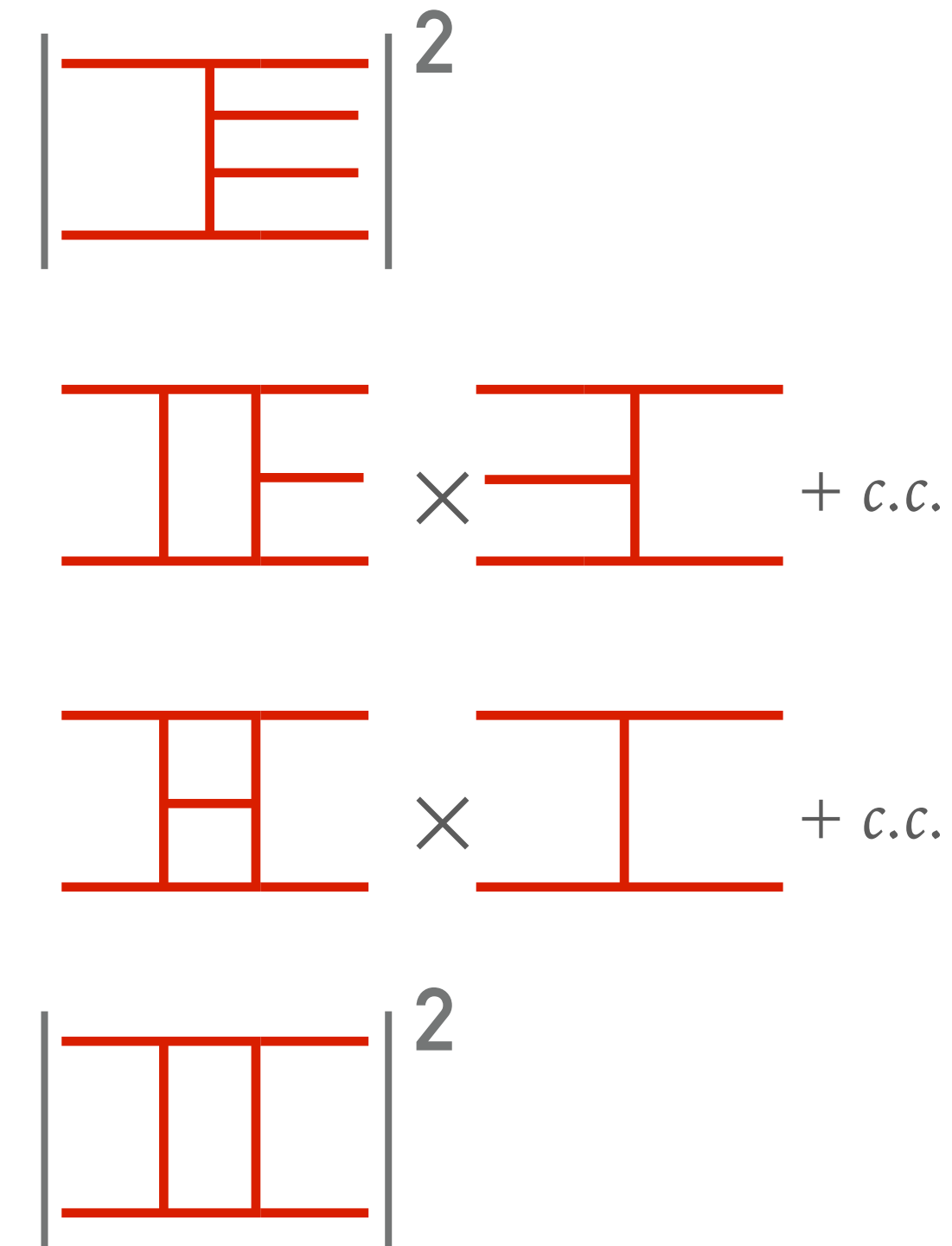
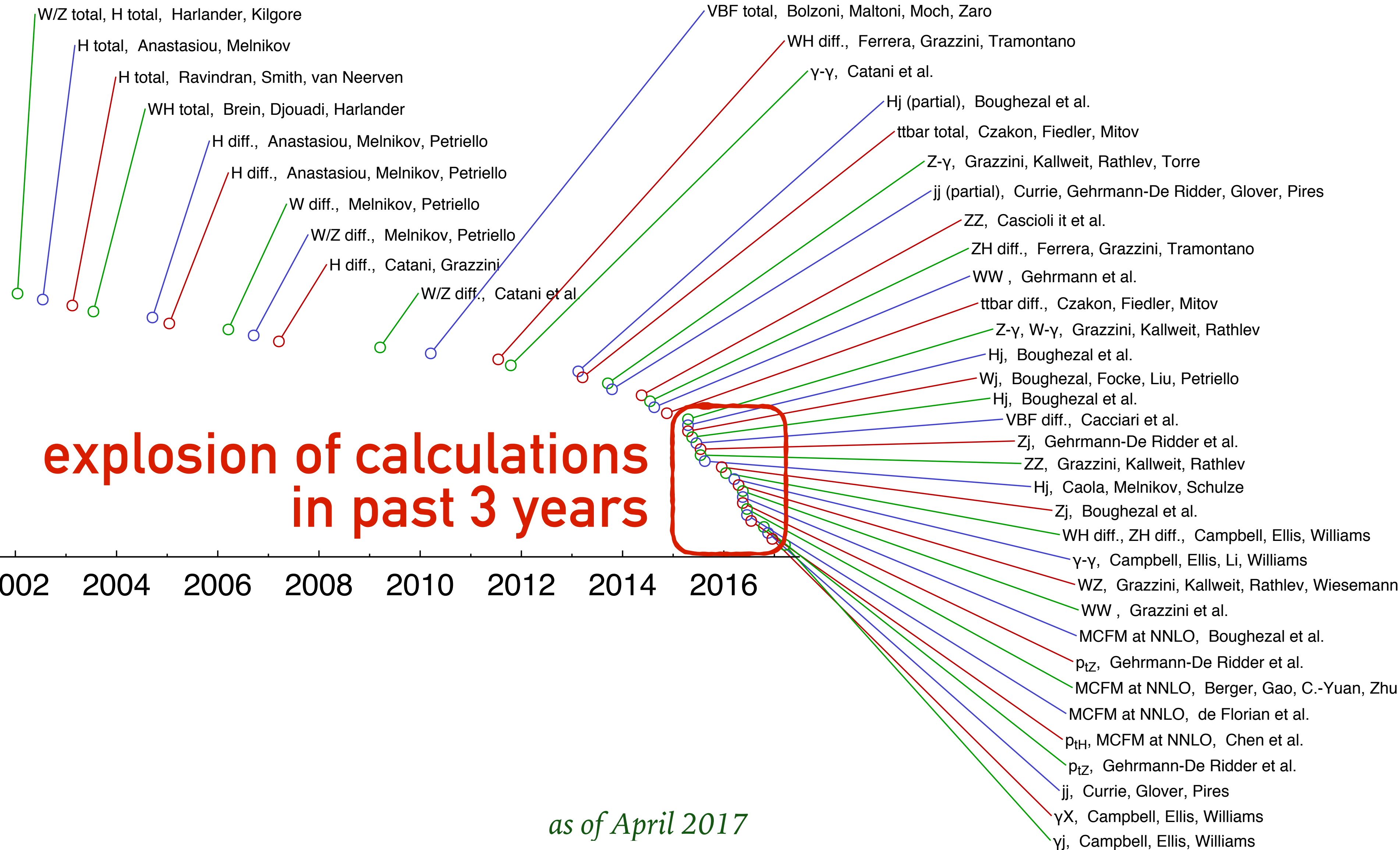
Other experiments have $\sim 2\%$ lumi uncertainty. Can new hardware help them match LHCb?

If LHCb remains the best, can its lumi uncertainty be transferred to other experiments (e.g. J/ψ & $Z \rightarrow \mu\mu$ measurements)

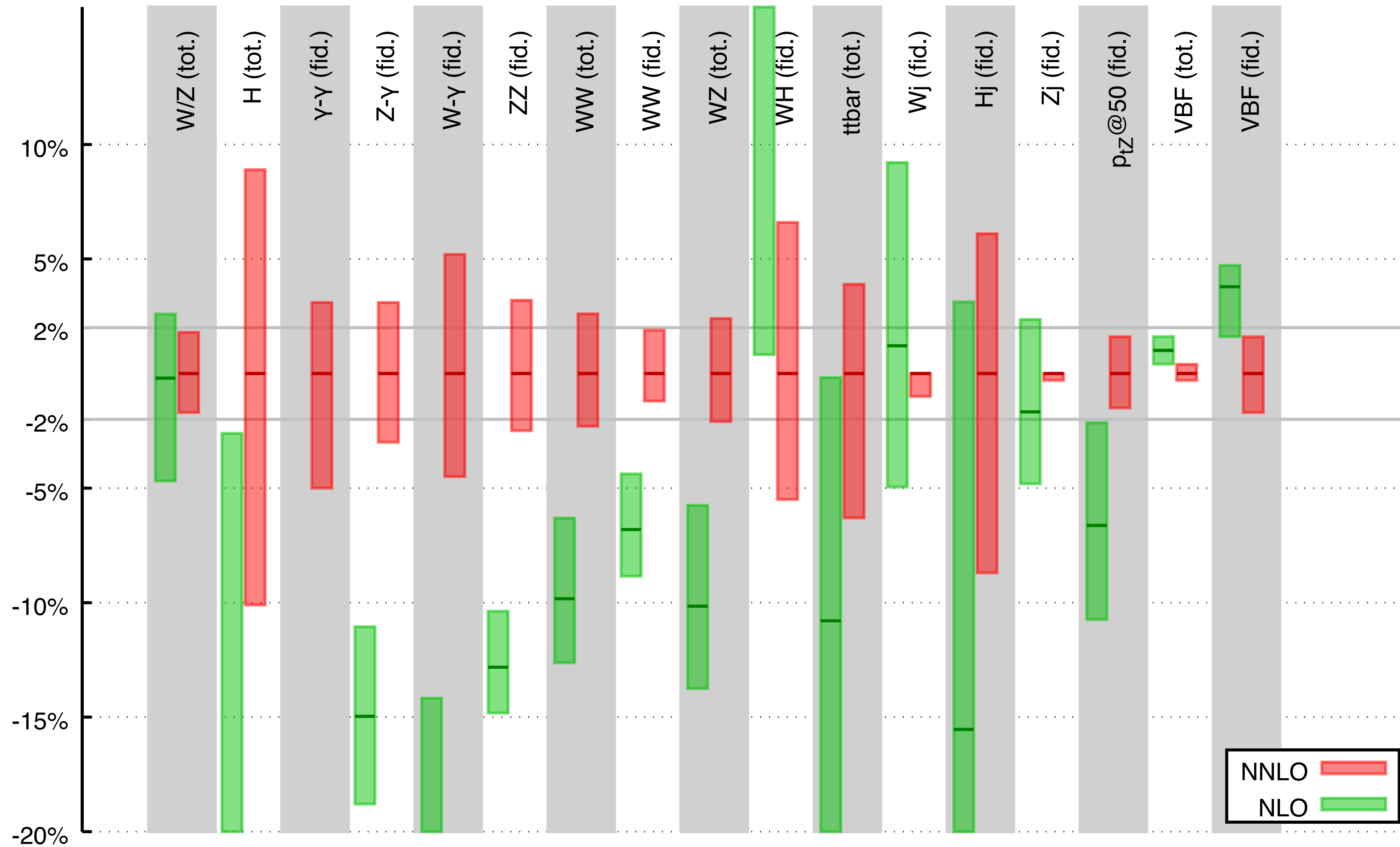
luminosity is potential keystone measurement for LHC precision programme

is QCD theory up to it?

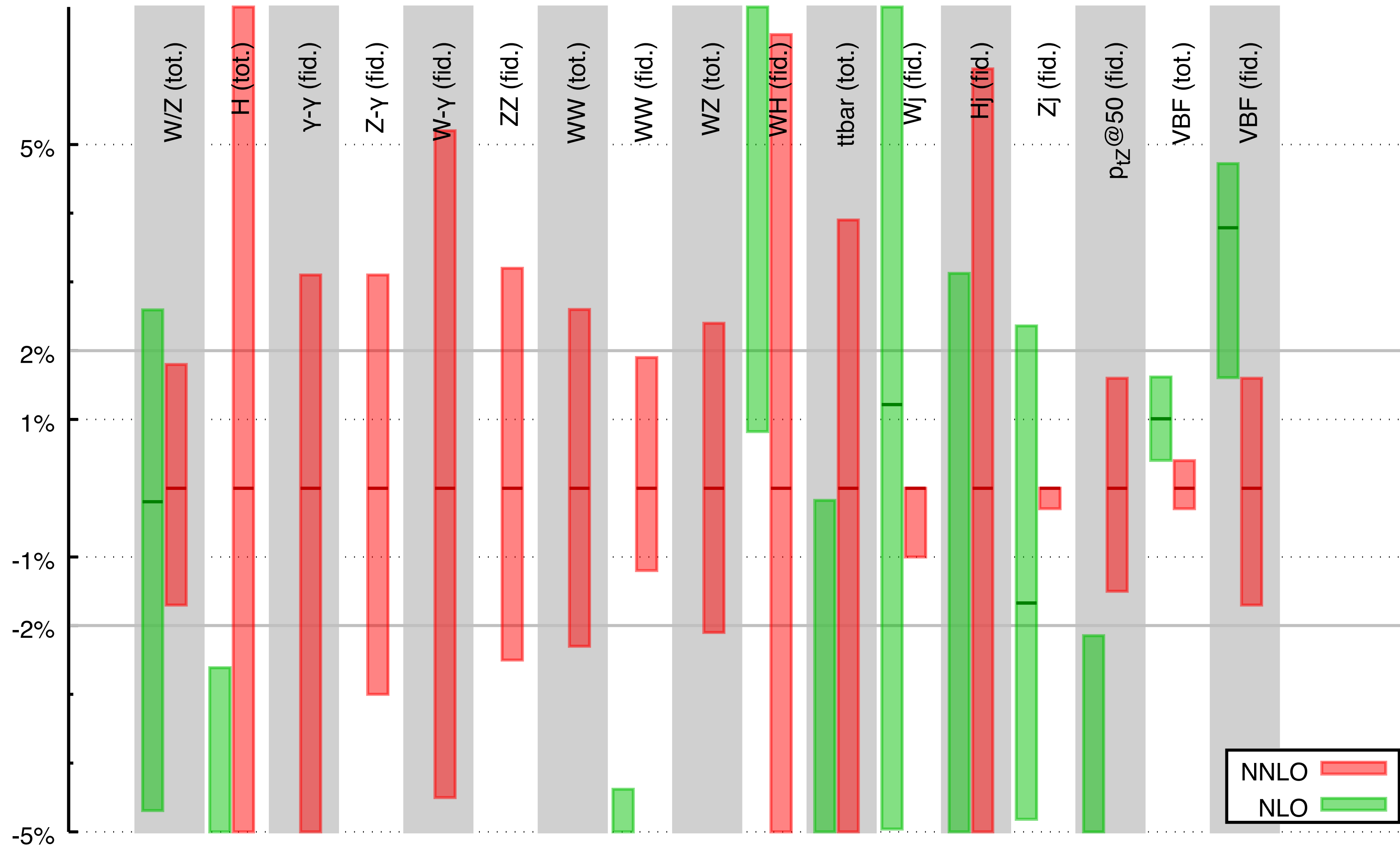
Hard processes: to 3rd order (NNLO) in perturbation theory strong coupling constant (α_s)



NNLO precision



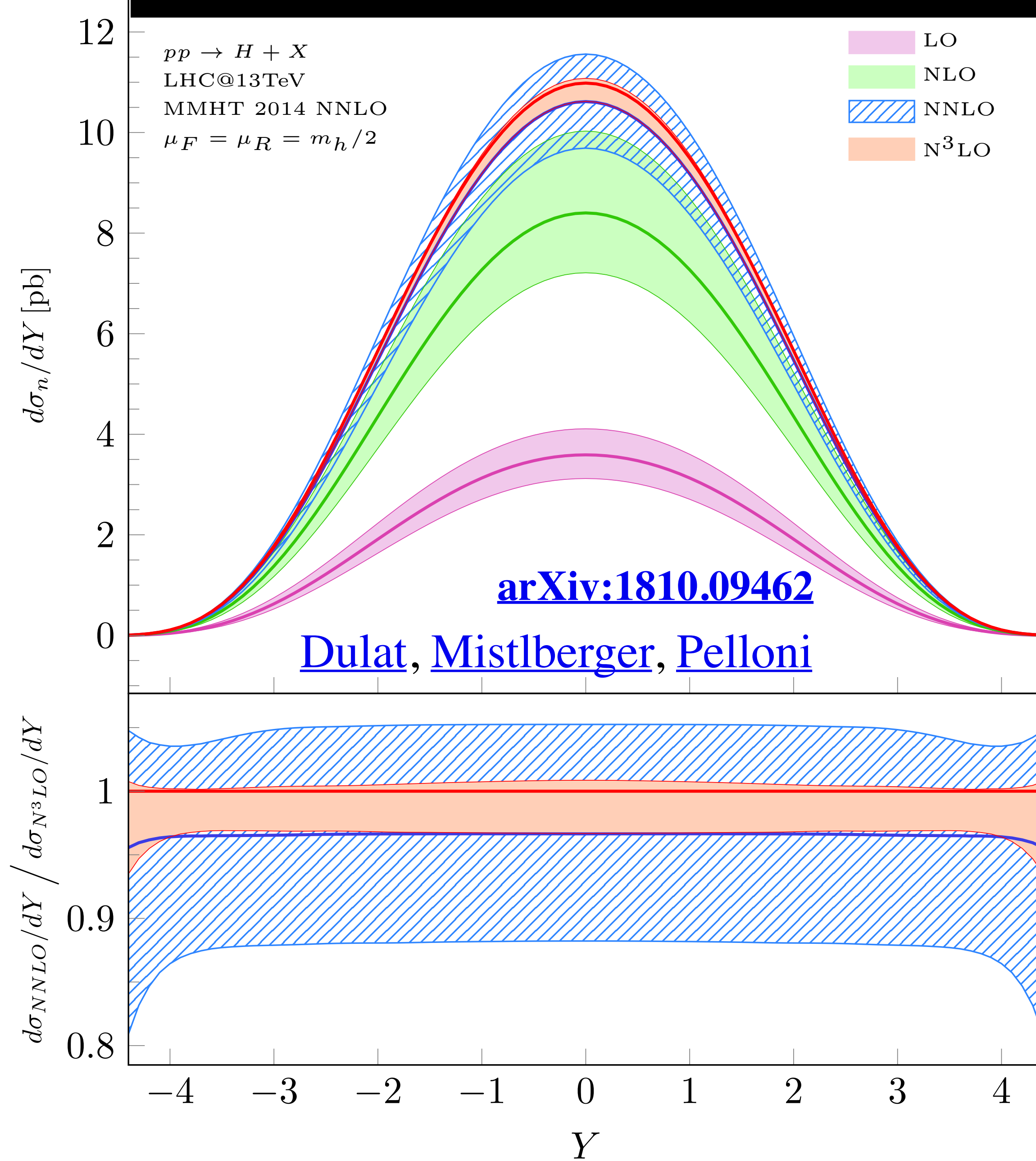
NNLO precision (magnified)



NNLO just barely gets us to 1% accuracy in some cases

(insofar as you believe in uncertainties from scale variation)

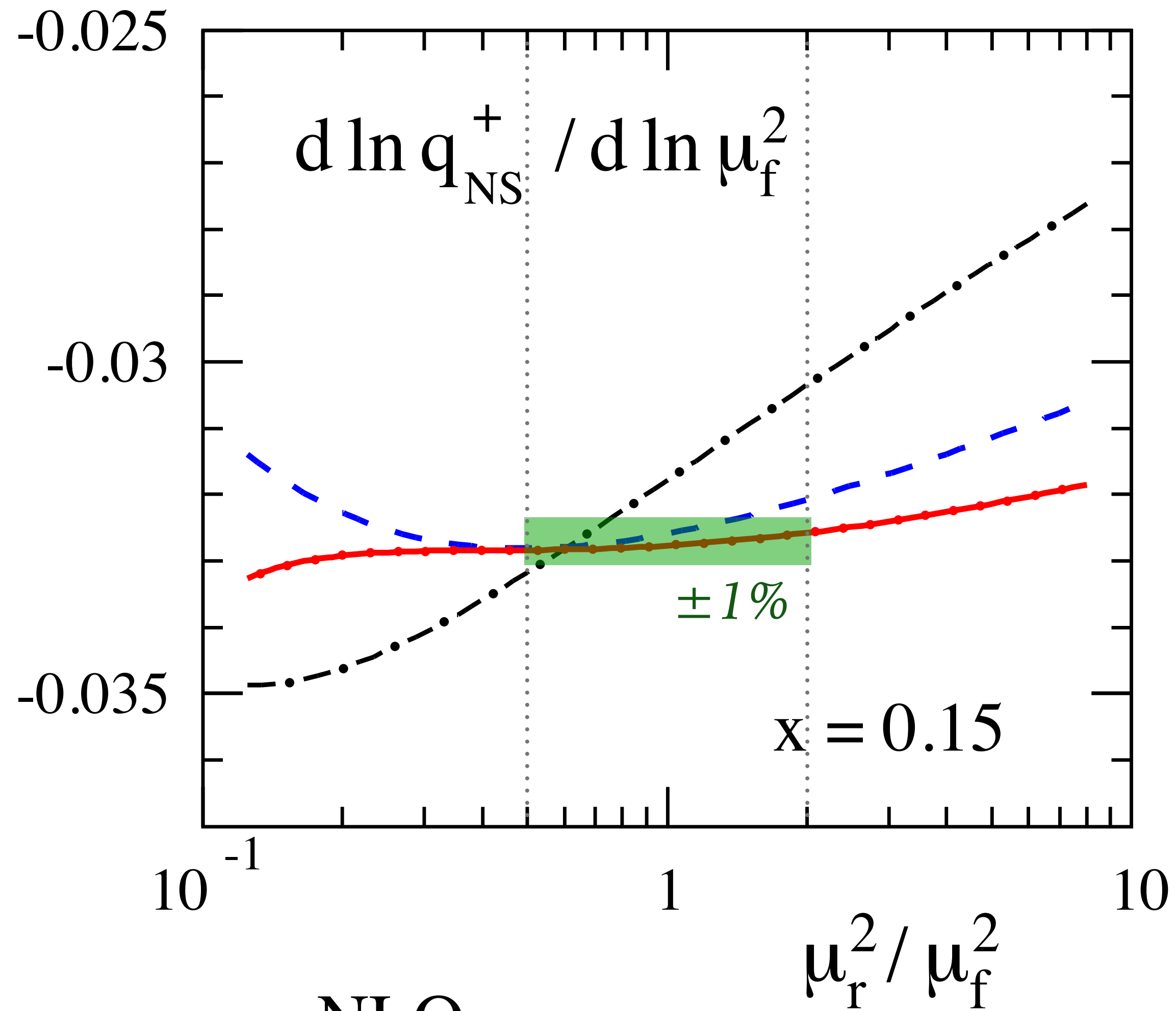
N3LO Higgs rap. dist.



NNLO → N3LO

- ▶ Technology is there for simple processes
- ▶ Demonstrated in Higgs case (poorly convergent perturbative expansion → +0.9% -3.4% uncertainty).
- ▶ Expect DY/Z production @N3LO soonish, with hope of genuine sub-percent uncertainties.

see also Cieri, Chen, Gehrmann, Glover, Huss
[arXiv:1807.11501](https://arxiv.org/abs/1807.11501)



- · - · - NLO
 - - - N²LO
 - · - · - N³LO_{A,B}

N3LO splitting functions

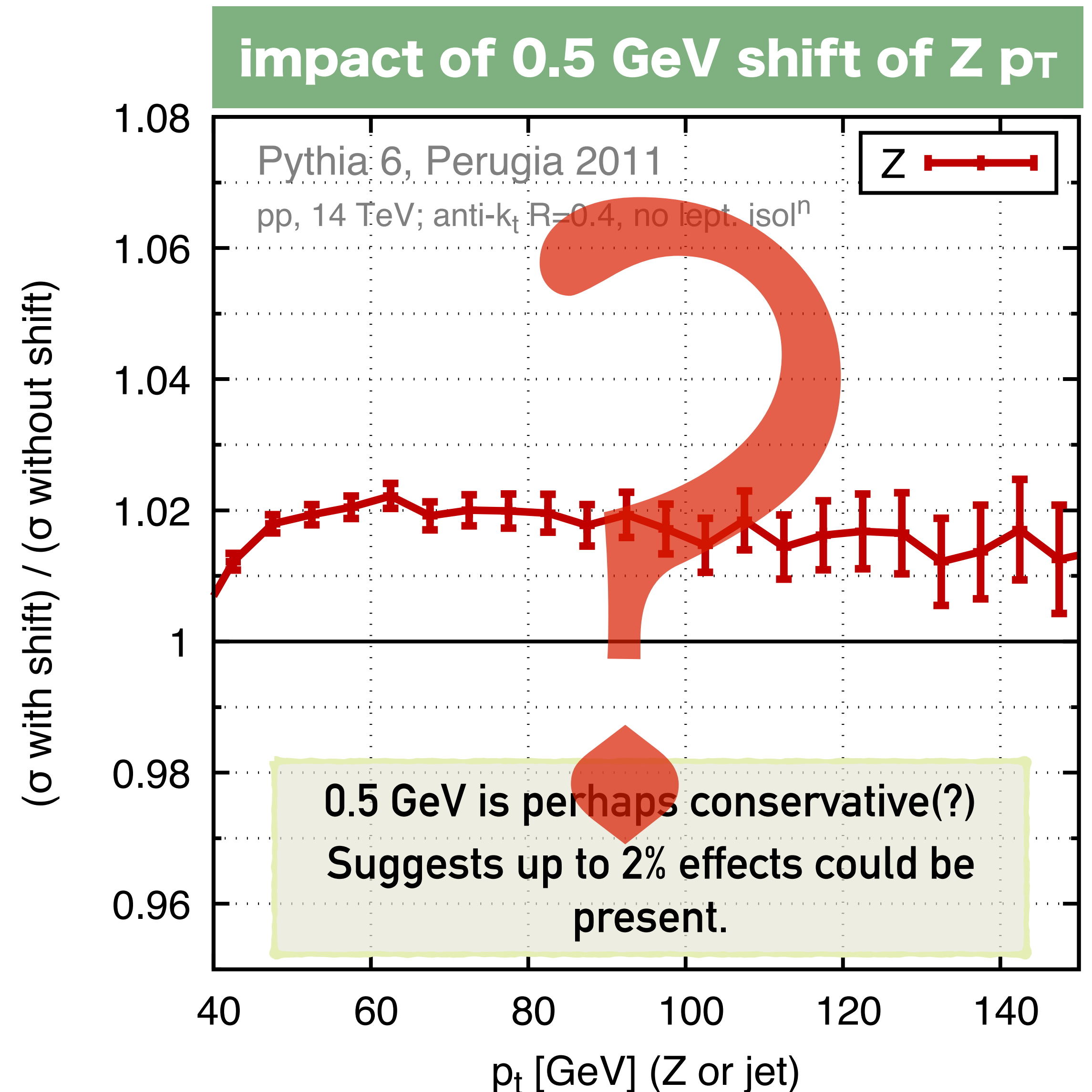
- ▶ non-singlet splitting functions (e.g. for DGLAP evolution of u-ubar) are now essentially known
- ▶ uncertainties on evolution are $\sim \pm 0.5\%$ in the figure (\sim half those at NNLO)
- ▶ singlet (e.g. P_{gg}) still in progress

[1707.08315](#) Moch, Ruijl, Ueda, Vermaseren, Vogt

N4LO progress: 1812.11818

Non-perturbative effects in Z (& H?) p_T

- **Inclusive** Z/W, H, VV cross sections should have $\sim \Lambda_{\text{QCD}}^2/M^2$ **corrections** ($\sim 10^{-4}$?)
- Z (&H) p_T **not inclusive** so corrections can be $\sim \Lambda/M$.
- Size of effect can't be probed by turning MC hadronisation on/off [maybe by modifying underlying MC parameters?]
- Shifting Z p_T by a finite amount illustrates what could happen



what might we do with it?

0. many processes, much phase space within 1% statistical reach

A huge range of phasespace will reach $< 1\%$ statistical precision @ HL-LHC

For example, processes with two or more leptons

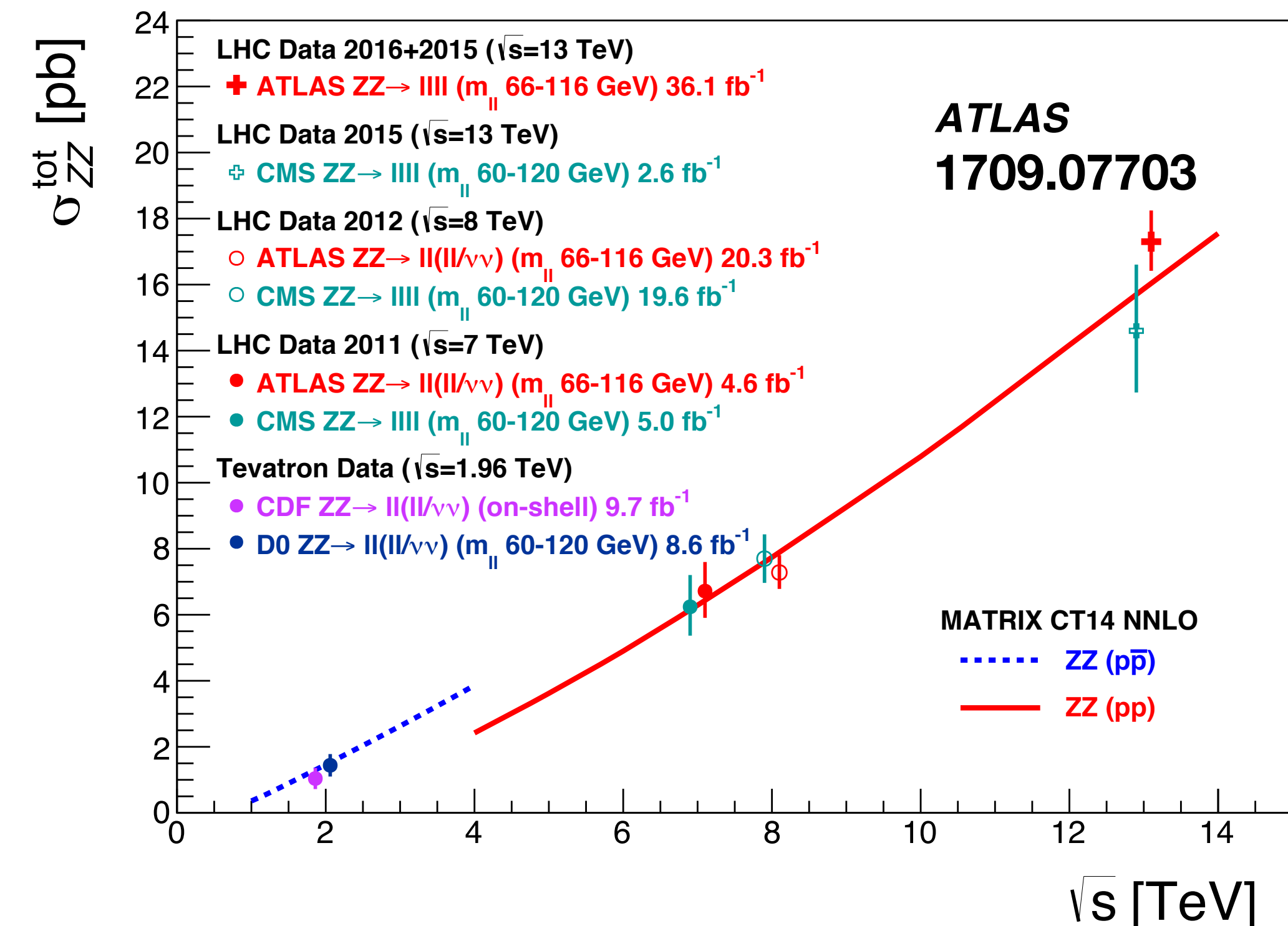
- Drell-Yan: $m_{\mu\mu}$ up to 1 TeV
- high p_T Z, up to 1 TeV
- top-antitop (di-lepton channels)
 - M_{tt} up to 2 TeV,
 - $p_{T,top}$ up to 1 TeV
- VV production

ZZ

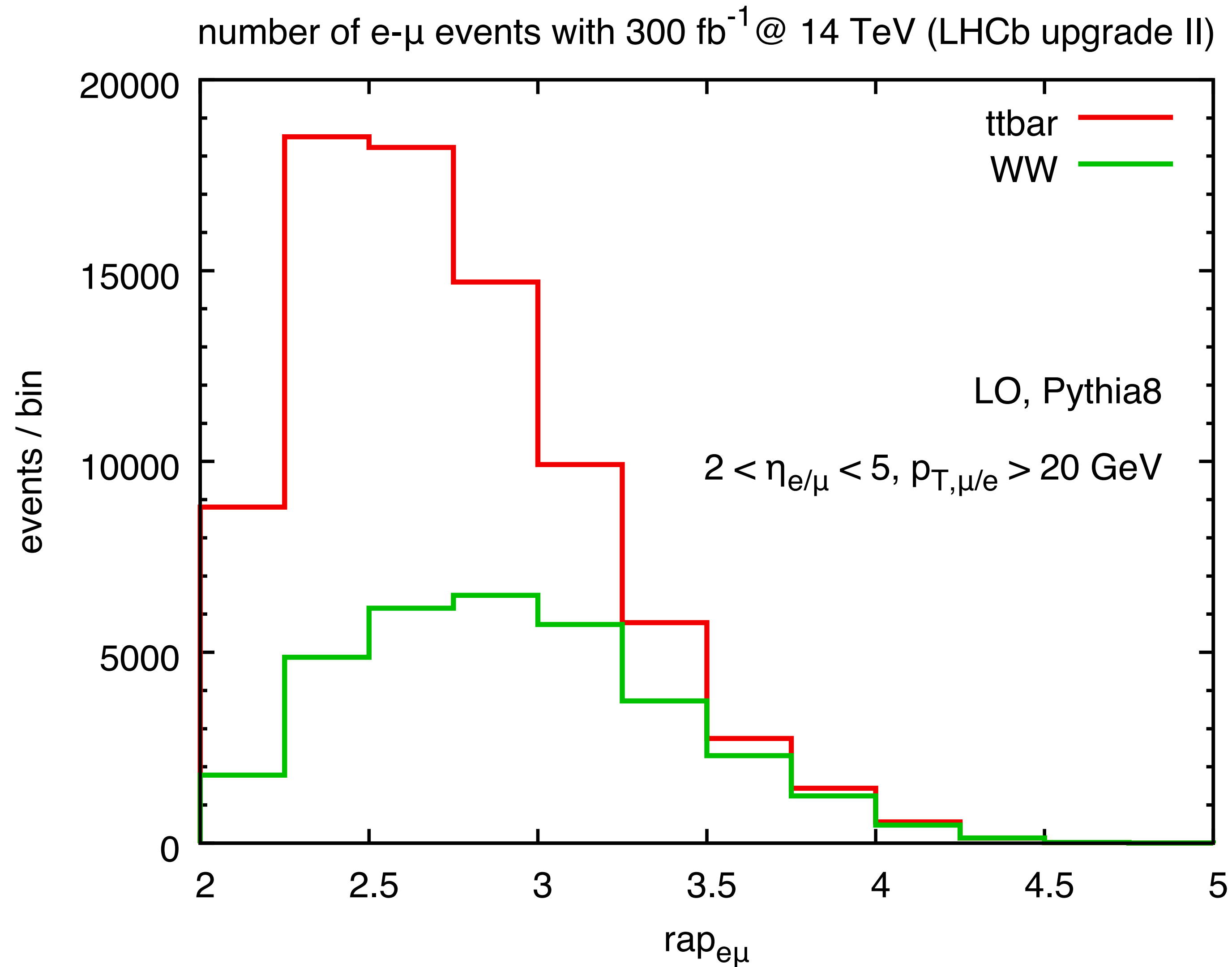
36.1 fb⁻¹ @ 13 TeV:

17.3 ± 0.9 [± 0.6 (stat.) ± 0.5 (syst.) ± 0.6 (lumi.)] pb.

→ expect stat errs of 0.3% for 3000 fb⁻¹



e- μ events (a mix of $t\bar{t}$ and VV) at LHCb



*this is a quick study to gauge orders
of magnitude*

(Pythia8, LO, no showering)

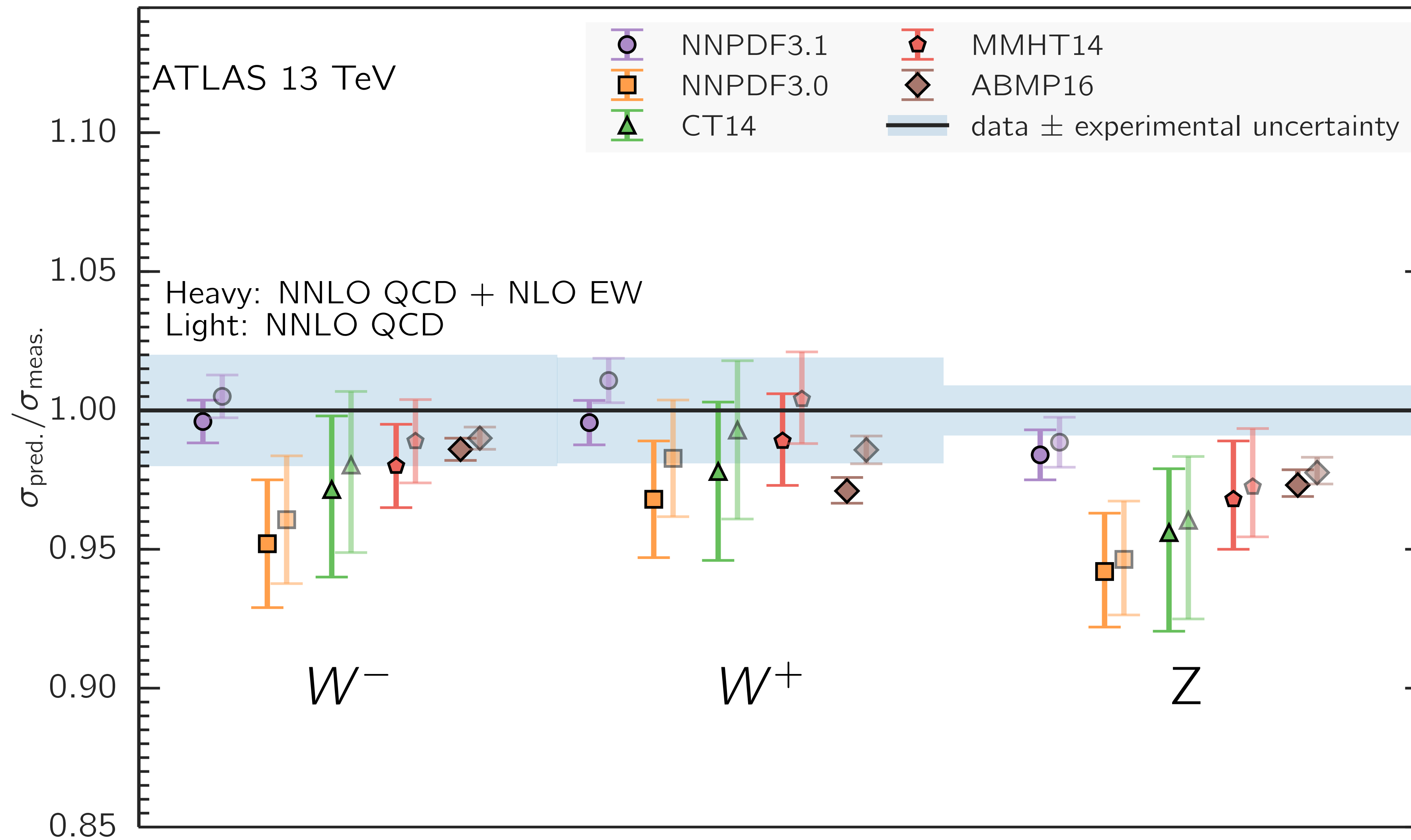
*N(N)LO K-factors will increase
rates significantly*

*there will also be other VV channels
(probably smaller)*

what might we do with it?

1. As an input to everything else: PDFs

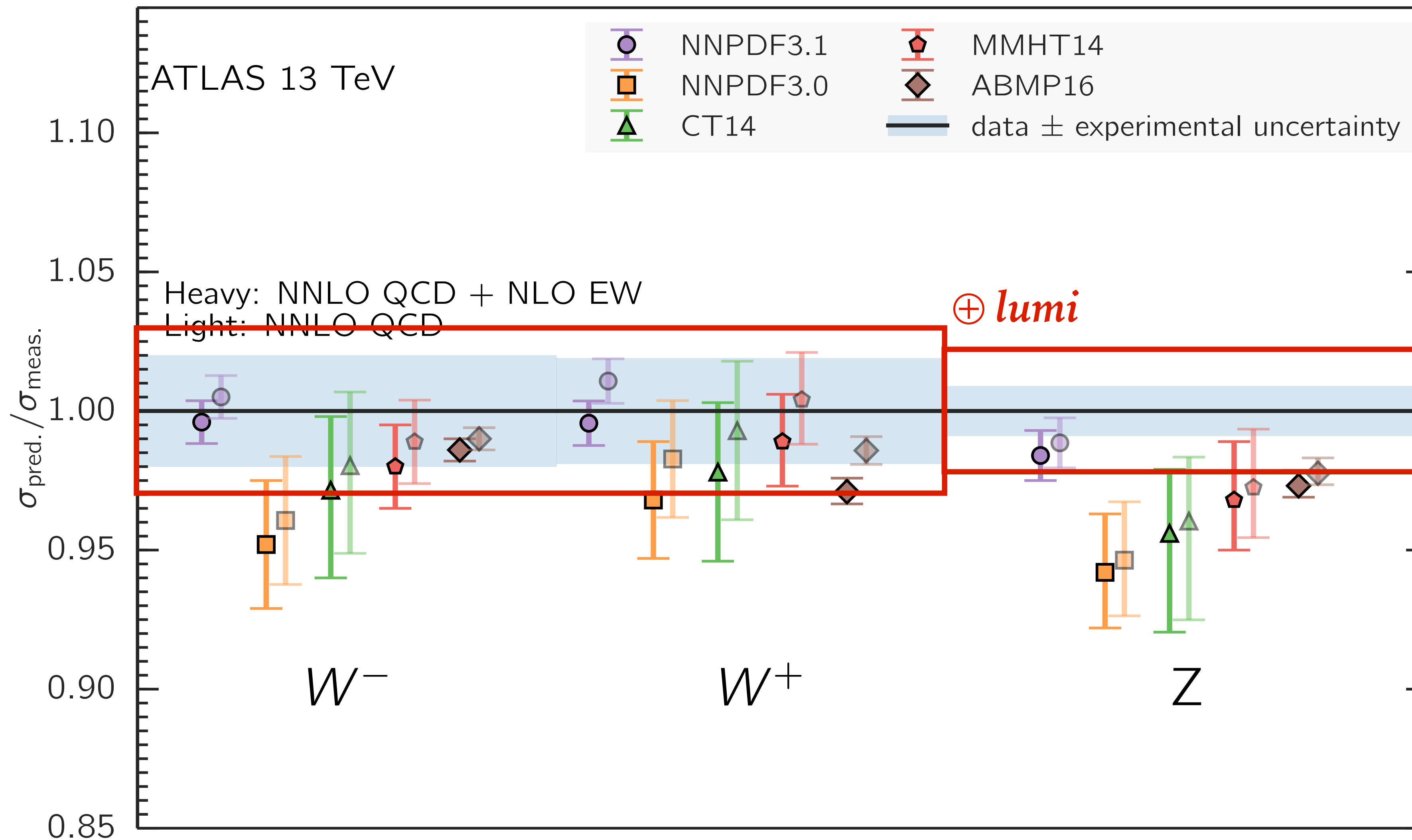
Drell-Yan as input to PDF fits



PDFs in the most basic process, Drell-Yan/Z, would be tightly constrained ($\sim 0.9\%$) were it not for the luminosity uncertainty ($\sim 2\%$)

NNPDF3.1, 1706.00428 (data from 1603.09222)

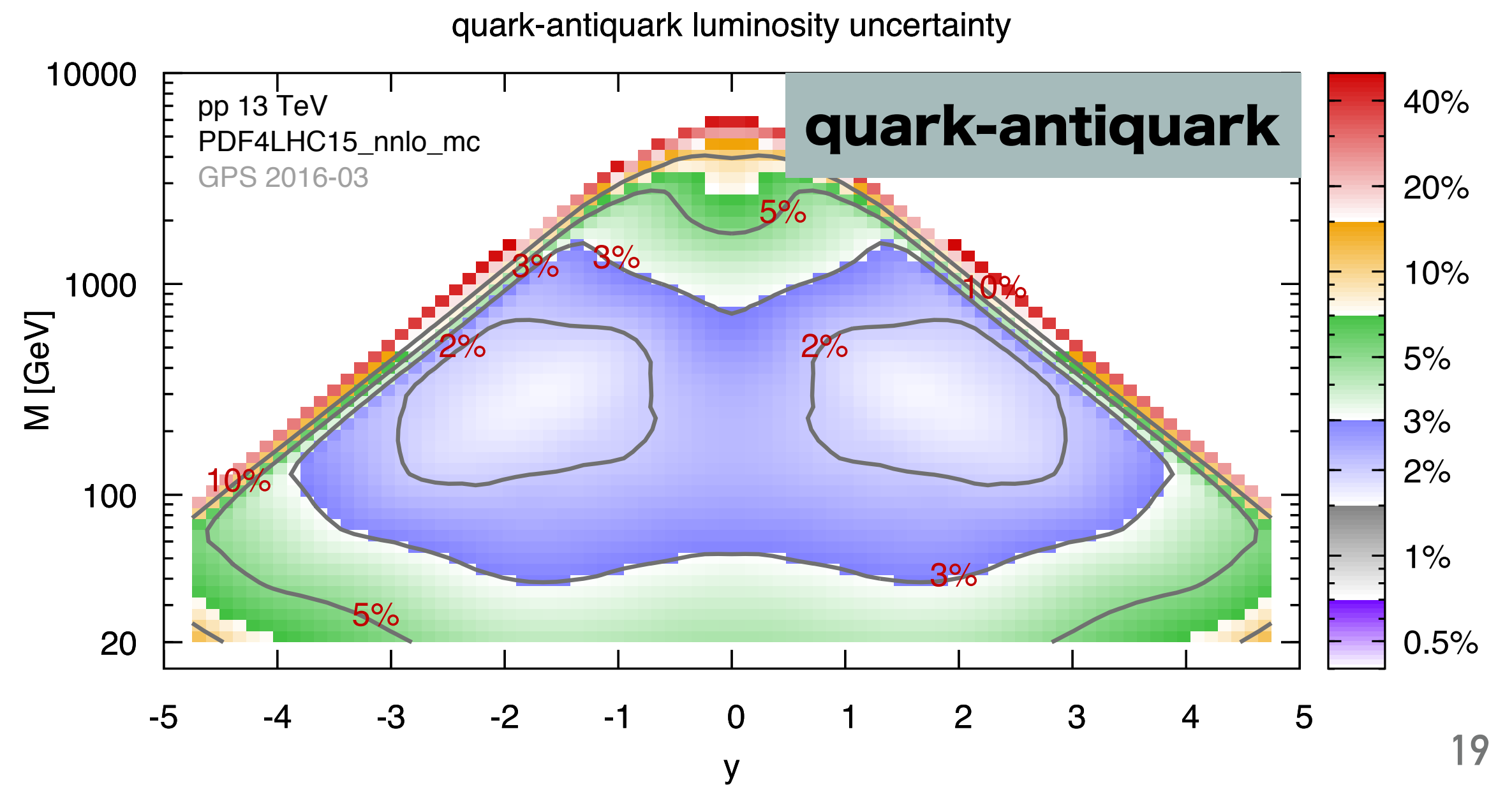
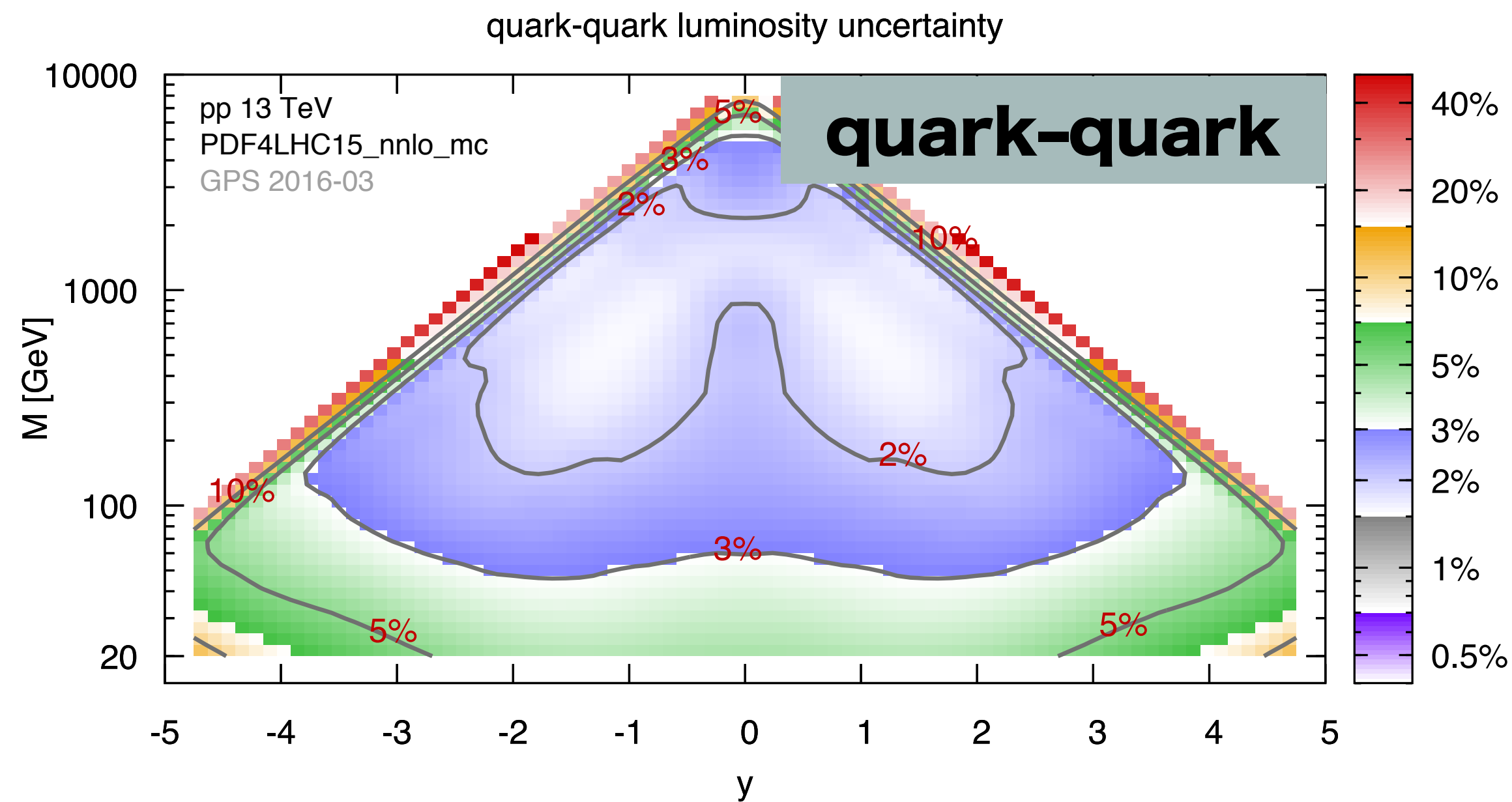
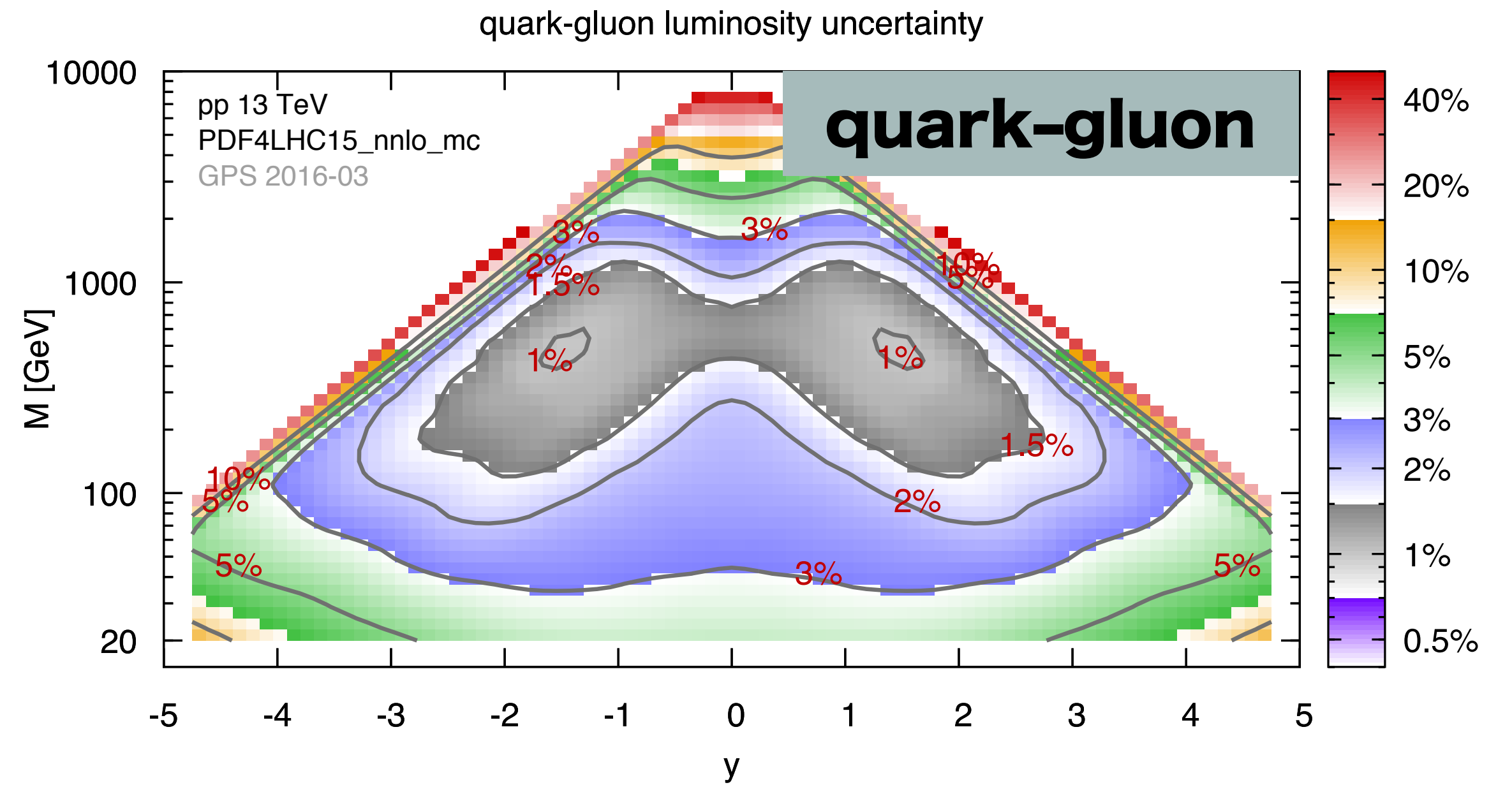
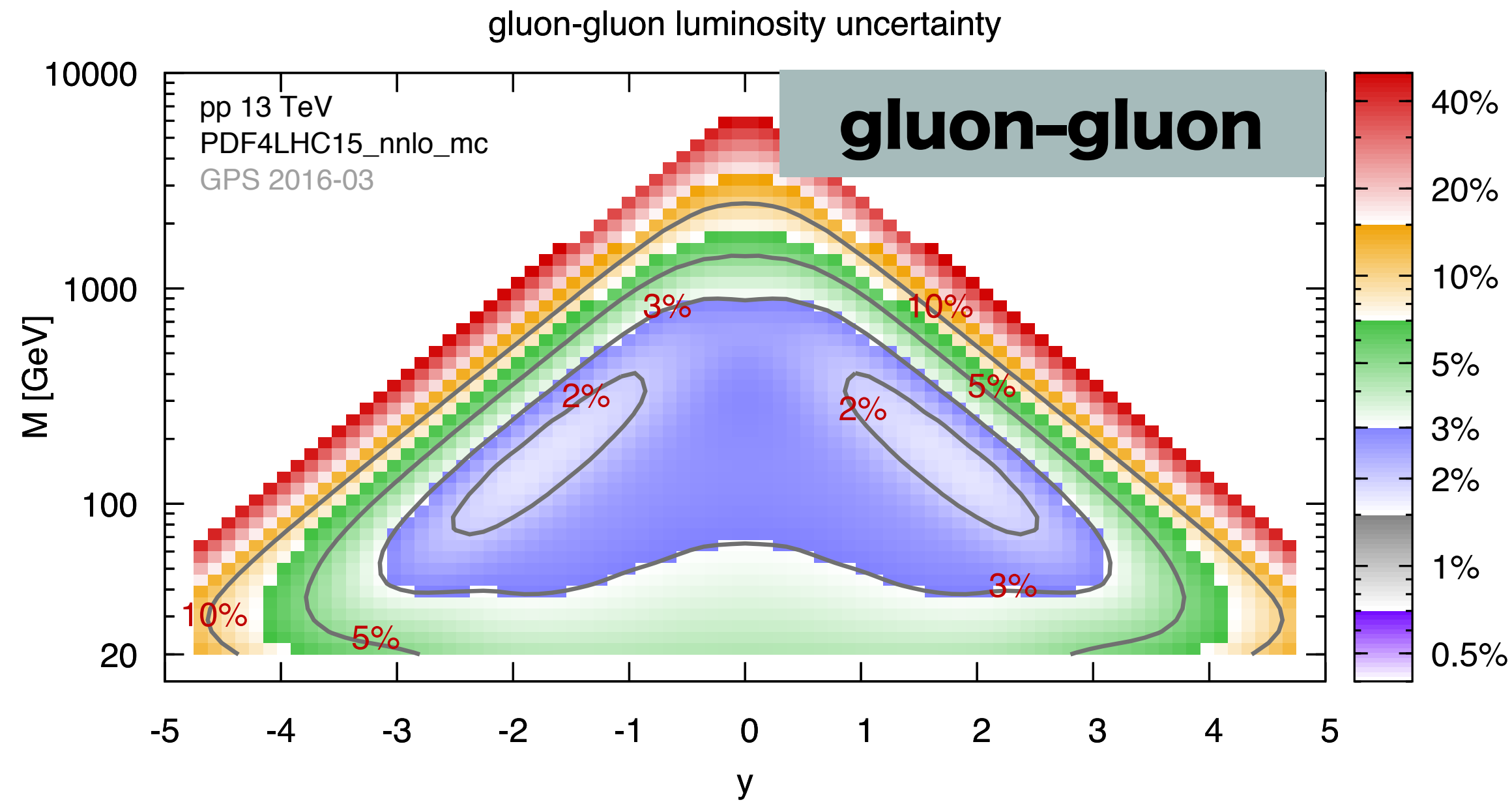
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UNCERTAINTIES ON PARTONIC LUMINOSITIES — V. RAPIDITY(y) AND MASS

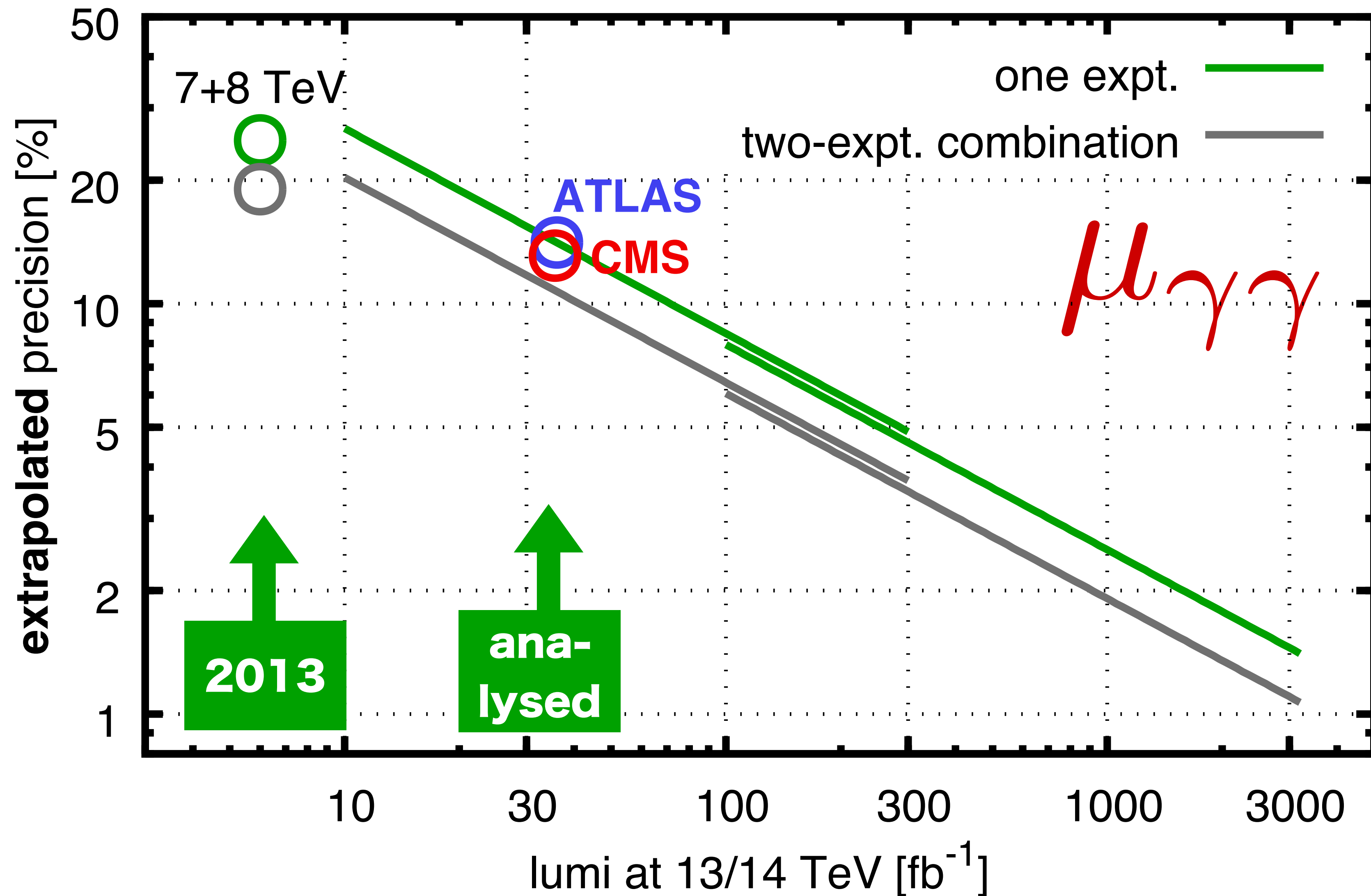


what might we do with it?

2. Higgs

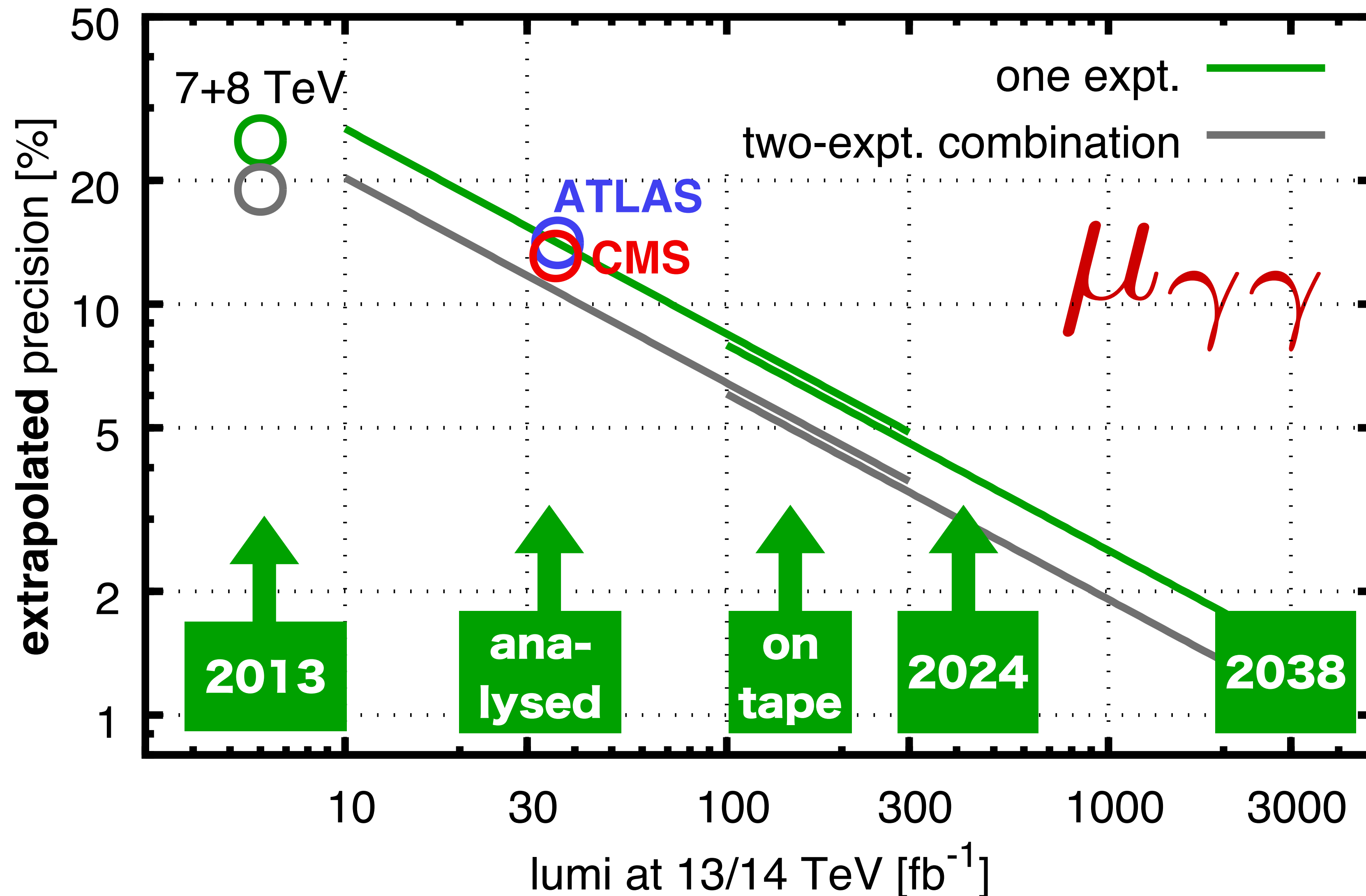
Higgs precision ($H \rightarrow \gamma\gamma$) : semi-optimistic estimate v. luminosity & time

extrapolation of $\mu_{\gamma\gamma}$ precision from 7+8 TeV results



Higgs precision ($H \rightarrow \gamma\gamma$) : semi-optimistic estimate v. luminosity & time

extrapolation of $\mu_{\gamma\gamma}$ precision from 7+8 TeV results



The LHC has the statistical potential to take Higgs physics from “observation” to 1–2% precision

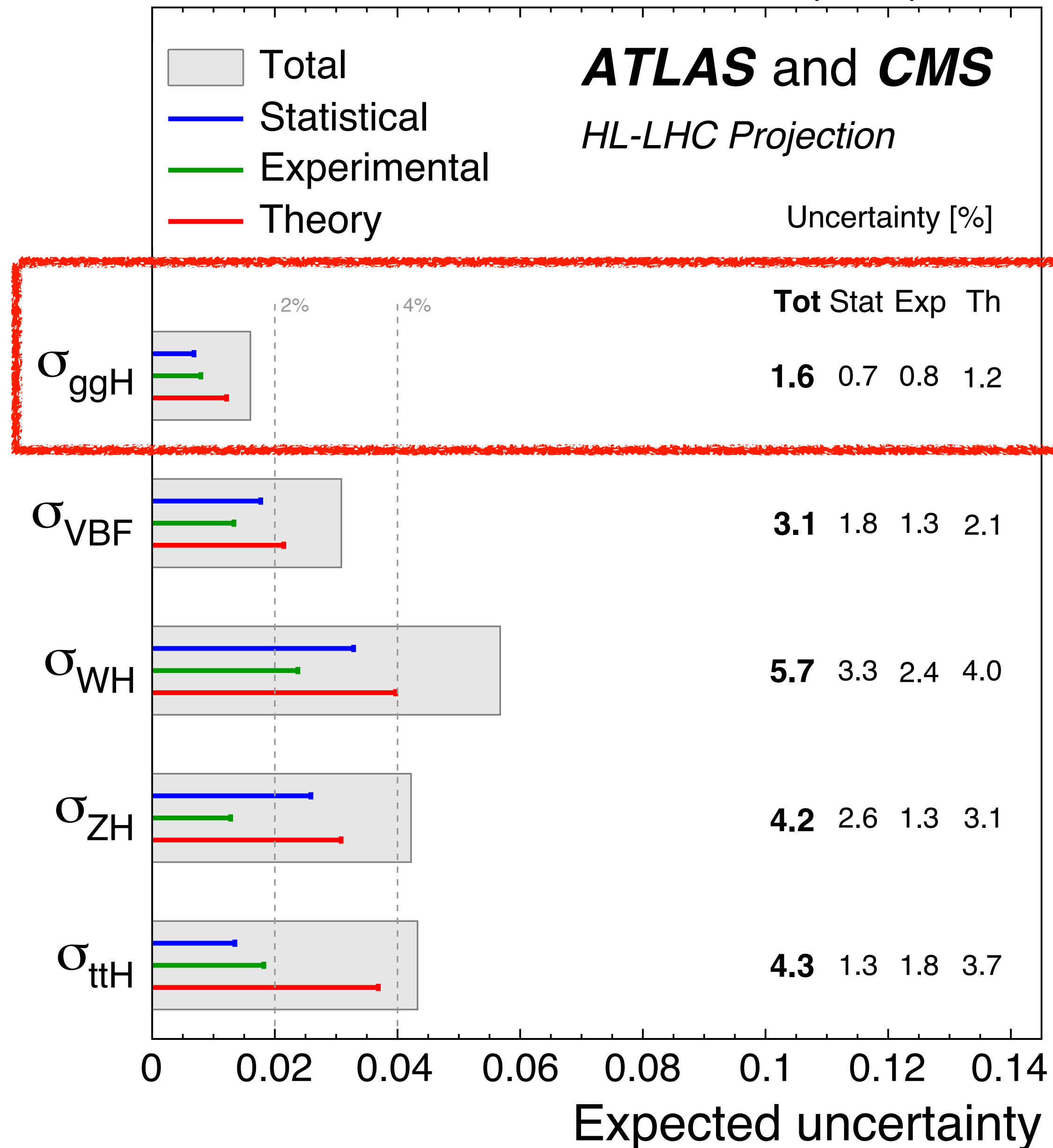
But only if we learn how to connect experimental observations with theory at that precision

1 fb^{-1} = 10^{14} collisions

Higgs Physics at the HL-LHC and HE-LHC

Official Higgs projections for HL-LHC indicate 1% experimental uncertainties from ATLAS/CMS combination for main production cross section, σ_{ggH}

Credibility will be greatly enhanced if we can demonstrate <1% control across a range of processes



DI-HIGGS PRODUCTION AT HL-LHC ($HH \rightarrow 4b, 3ab^{-1}$)

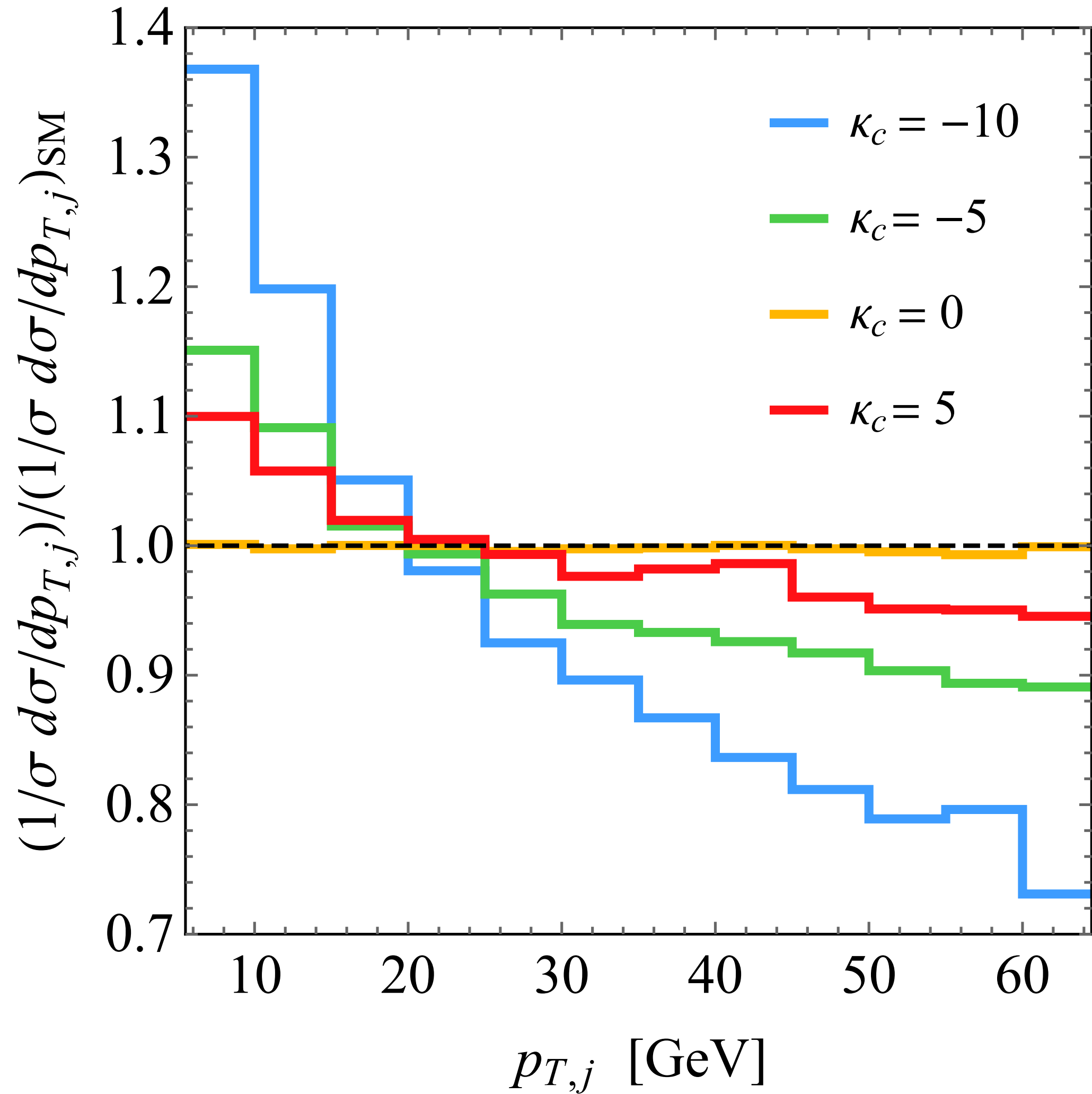
Behr, Bortoletto, Frost, Hartland, Issever & Rojo, 1512.08928

Category		signal	background		$S/\sqrt{B_{\text{tot}}}$	$S/\sqrt{B_{4b}}$	S/B_{tot}	S/B_{4b}
		N_{ev}	$N_{\text{ev}}^{\text{tot}}$	N_{ev}^{4b}				
Boosted	no PU	290	$1.2 \cdot 10^4$	$8.0 \cdot 10^3$	2.7	3.2	0.03	0.04
	PU80+SK+Trim	290	$3.7 \cdot 10^4$	$1.2 \cdot 10^4$	1.5	2.7	0.01	0.02
Intermediate	no PU	130	$3.1 \cdot 10^3$	$1.5 \cdot 10^3$	2.3	3.3	0.04	0.08
	PU80+SK+Trim	140	$5.6 \cdot 10^3$	$2.4 \cdot 10^3$	1.9	2.9	0.03	0.06
Resolved	no PU	630	$1.1 \cdot 10^5$	$5.8 \cdot 10^4$	1.9	2.7	0.01	0.01
	PU80+SK	640	$1.0 \cdot 10^5$	$7.0 \cdot 10^4$	2.0	2.6	0.01	0.01
Combined	no PU				4.0	5.3		
	PU80+SK+Trim				3.1	4.7		

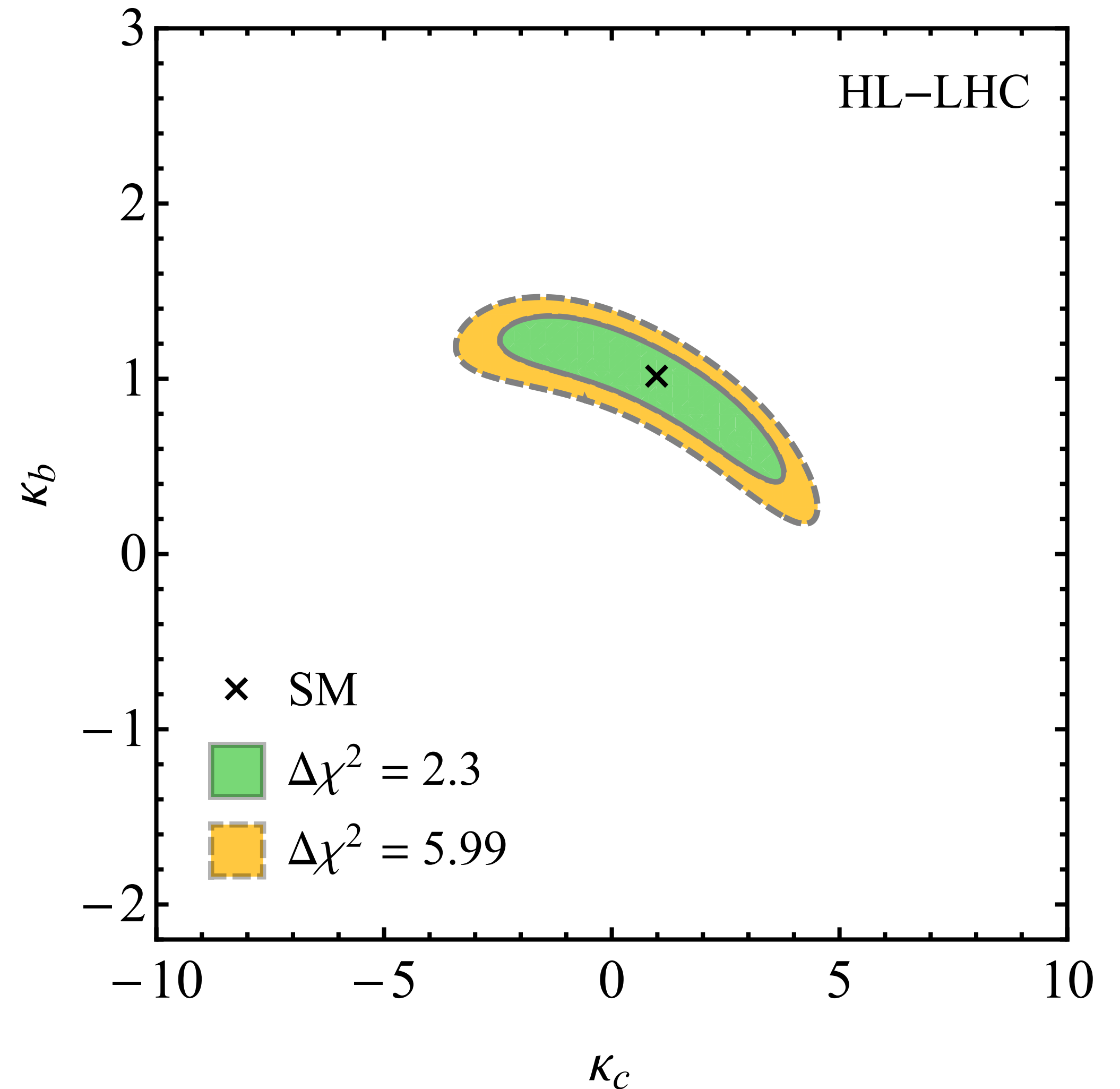
Key signal channels will need ~1% control of complex bkgds

indirect constraints on Hcc

impact of modified Hcc coupling on Higgs+jet p_T dist



joint limits on κ_c & κ_b @ HL-LHC



what might we do with it?

3. New physics searches

VH production at large $m(\text{VH})$ [specific illustration of a generic point]

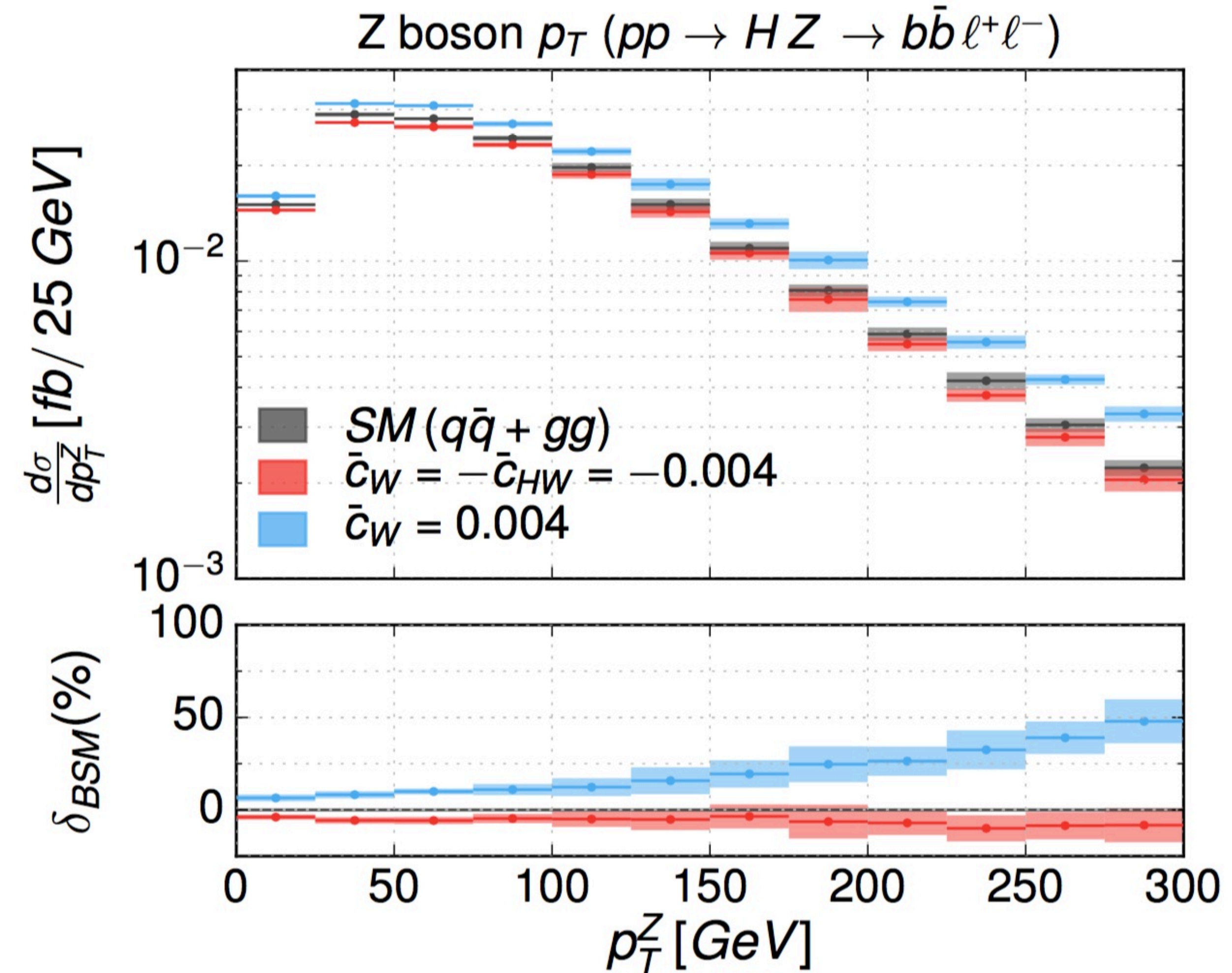
- Higher-dimension operators cause deviations that grow as, e.g.

$$\frac{\delta\sigma_{\text{dim-6}}}{\sigma} \sim \frac{p_T^2}{\Lambda^2}$$

- In some relevant range of p_T , Λ value to which you're sensitive grows as

$$\Lambda \sim (\text{Lumi})^{1/4}$$

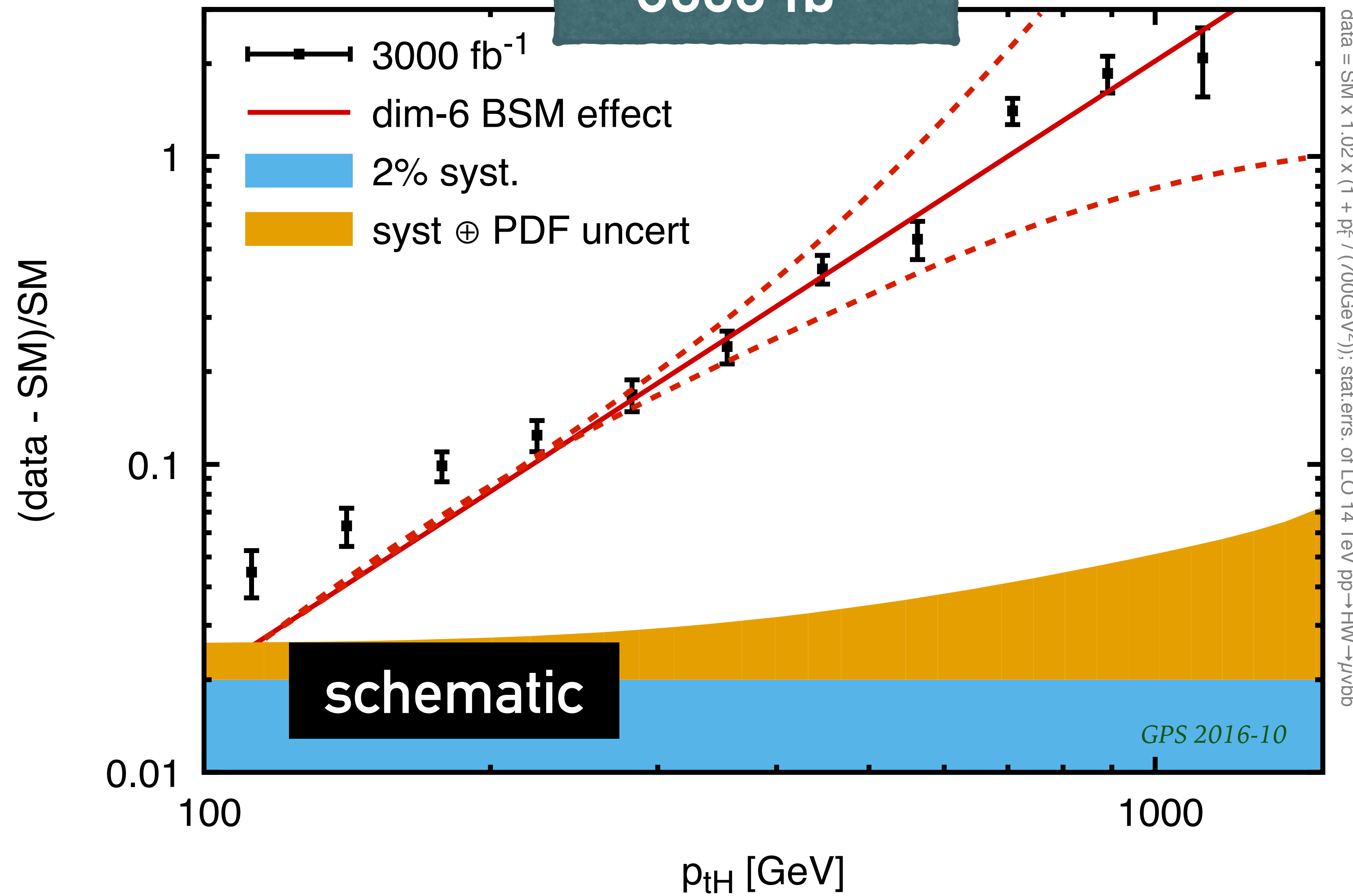
- that's faster than most direct searches (x100 in lumi \rightarrow x1.5 in reach for Z')



Mimasu, Sanz, Williams, arXiv:1512.02572v

WH at large Q^2 with dim-6 BSM effect

3000 fb⁻¹



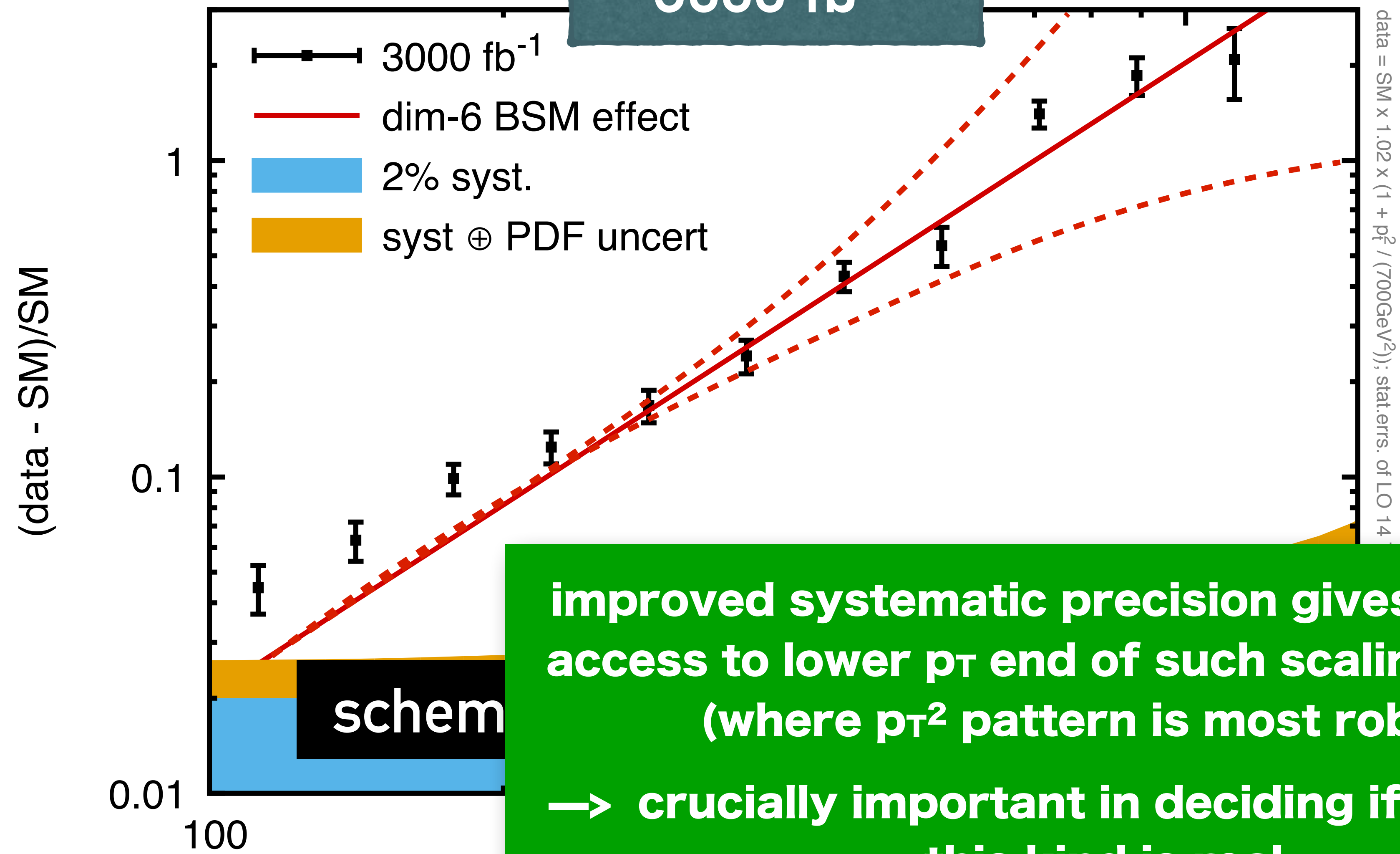
data = SM x 1.02 x (1 + p_T² / (700GeV²)); stat. errs. of LO 14 TeV pp → HW → $\mu\nu b\bar{b}$

new physics isn't just a single number that's wrong (think $g-2$) but rather a **distinct scaling pattern of deviation** ($\sim p_T^2$)

moderate and high p_T 's have similar statistical significance — so it's useful to understand whole p_T range

WH at large Q^2 with dim-6 BSM effect

3000 fb⁻¹



improved systematic precision gives enhanced access to lower p_T end of such scaling patterns (where p_T^2 pattern is most robust)
 → crucially important in deciding if a signal of this kind is real

new physics isn't just a single number that's wrong (think $g-2$) but rather a **distinct scaling pattern of deviation** ($\sim p_T^2$)

moderate and high p_T 's similar statistical precision — so it's to understand the p_T range

conclusions

Conclusions

- **Experimentally:** relative sub-percent precision looks feasible for many leptonic processes. Open question is absolute precision, especially luminosity.
- **Theoretically:** expect substantial further progress on higher-order perturbative calculations. For a subset of processes (non-inclusive), open questions about non-perturbative effects. *[Technology probably exists to answer this questions]*
- **Varied applications:**
 - many processes, over wide phase space, will have statistical precision $< 1\%$
 - could bring PDFs into new era of precision (& complementary to low- Q^2 DIS?)
 - will build confidence in precision needed for precision Higgs physics
 - can provide crucial low- p_T end of lever-arm in searches for higher-dim. BSM operators

backup

Input parameters? Especially, a_s

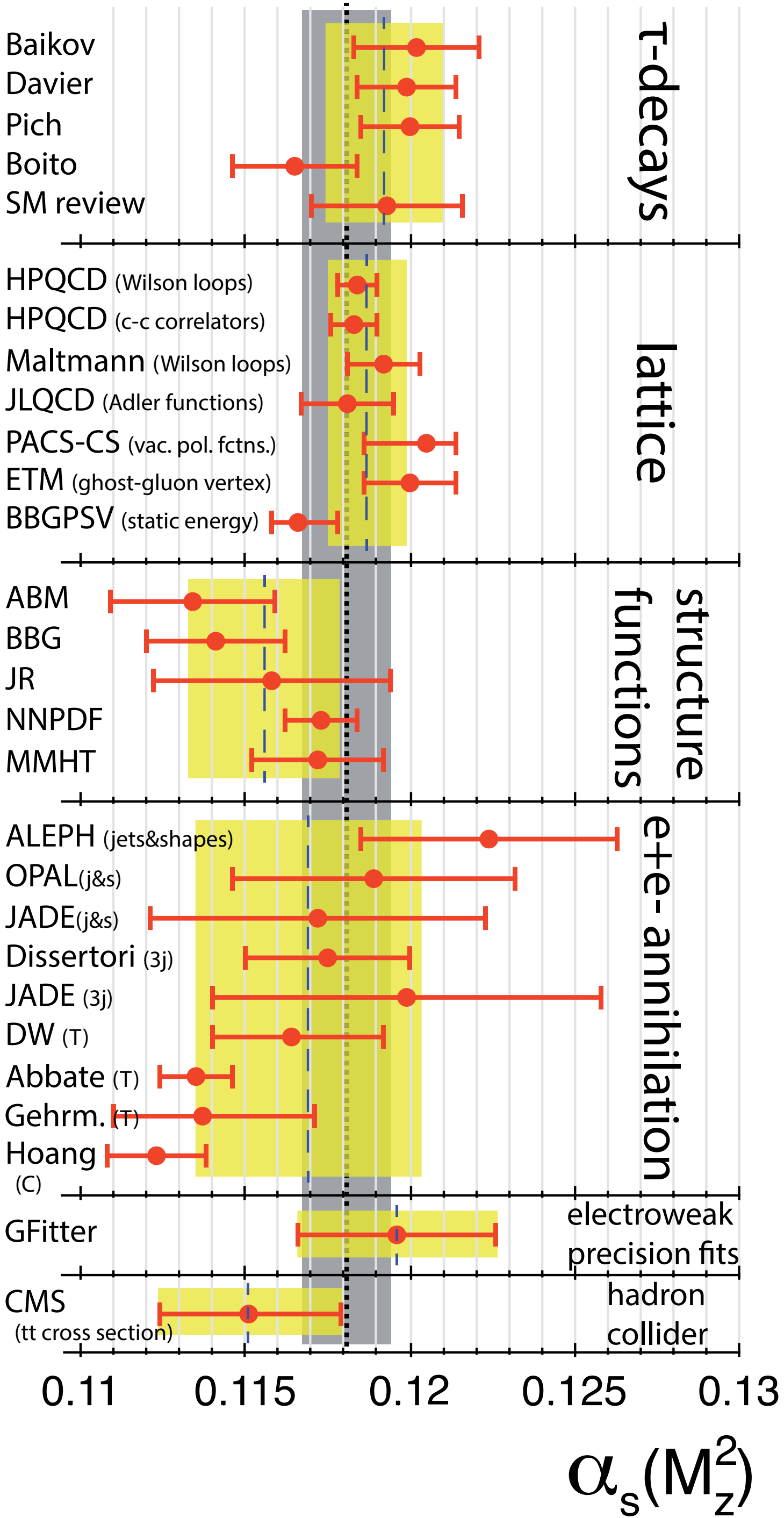
(almost) all theory predictions for LHC are based on perturbation theory, e.g.

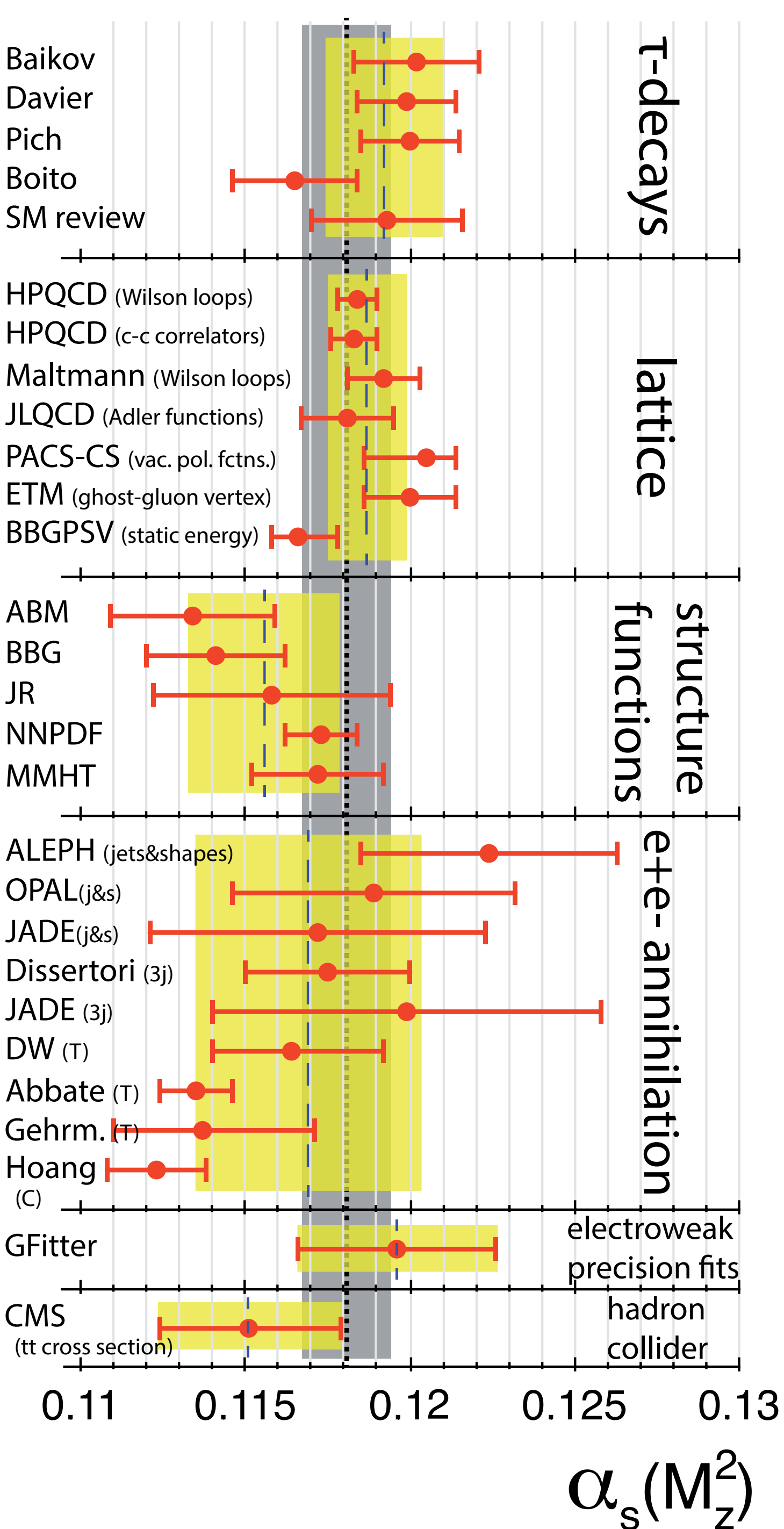
$$\sigma = a_s \sigma_1 + a_s^2 \sigma_2 + \dots$$

*not so critical for DY, VV (LO doesn't depend on a_s),
but is crucial for $t\bar{t}$ and other processes that start at $O(a_s^2)$*

PDG World Average: $\alpha_s(M_Z) = 0.1181 \pm 0.0013$ (1.1%)

Bethke, Dissertori & GPS in PDG '16





PDG World Average: $\alpha_s(M_Z) = 0.1181 \pm 0.0013$ (1.1%)

➤ Most consistent set of independent determinations is from lattice

➤ Two best determinations are from same group (HPQCD, 1004.4285, 1408.4169)

$\alpha_s(M_Z) = 0.1183 \pm 0.0007$ (0.6%) [heavy-quark correlators]

$\alpha_s(M_Z) = 0.1183 \pm 0.0007$ (0.6%) [Wilson loops]

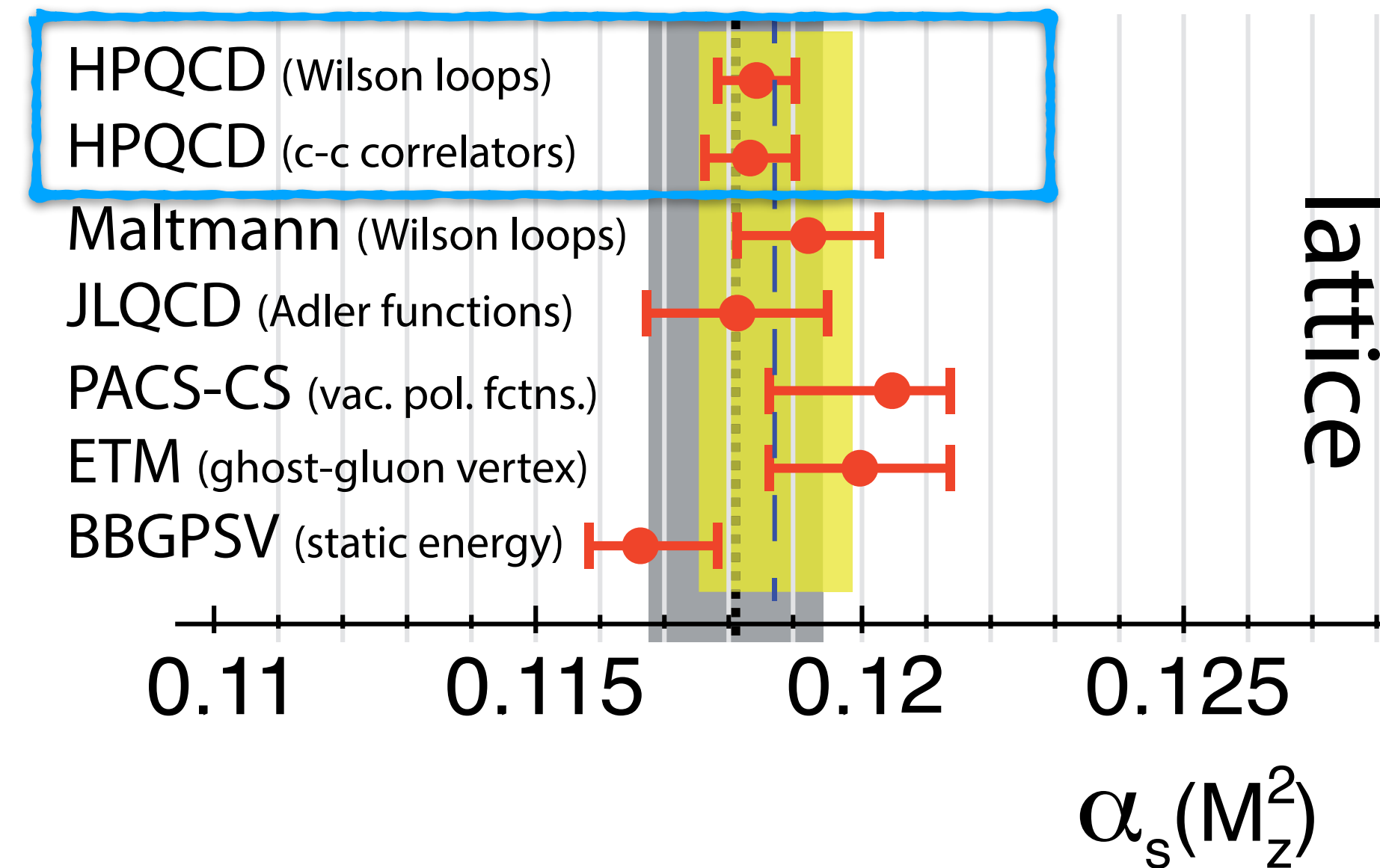
➤ Error criticised by FLAG, who suggest

$\alpha_s(M_Z) = 0.1184 \pm 0.0012$ (1%)

➤ Worries include missing perturbative contributions, non-perturbative effects in 3–4 flavour transition at charm mass [addressed in some work], etc.

➤ New ALPHA extraction (1706.03821) is cleaner in many respects

$\alpha_s(M_Z) = 0.1185 \pm 0.00084$ (0.7%)

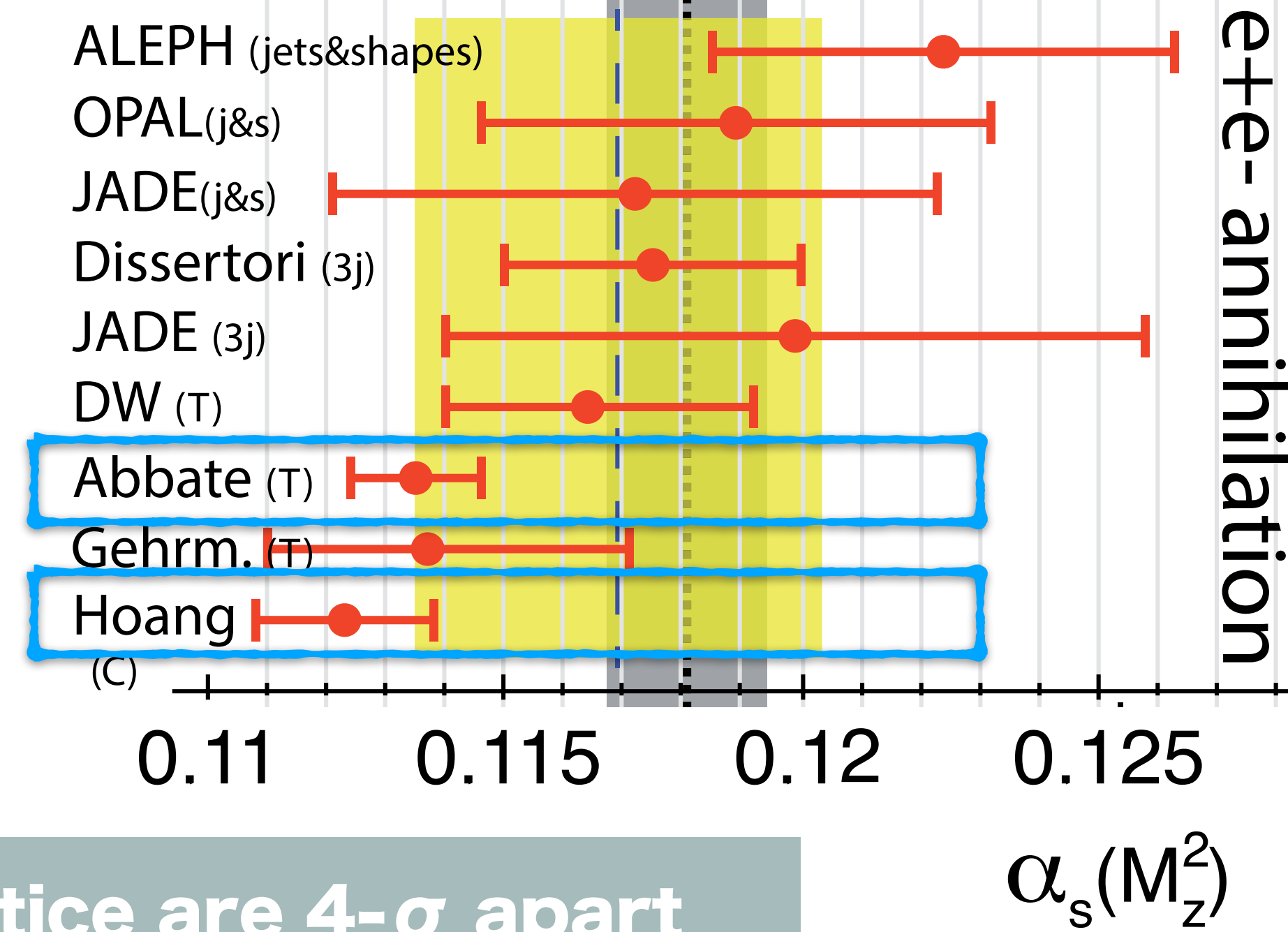


E+E- EVENT SHAPES AND JET RATES

- Two “best” determinations are from same group (Hoang et al, 1006.3080, 1501.04111)

$$\alpha_s(M_Z) = 0.1135 \pm 0.0010 \text{ (0.9\%)} \text{ [thrust]}$$

$$\alpha_s(M_Z) = 0.1123 \pm 0.0015 \text{ (1.3\%)} \text{ [C-parameter]}$$



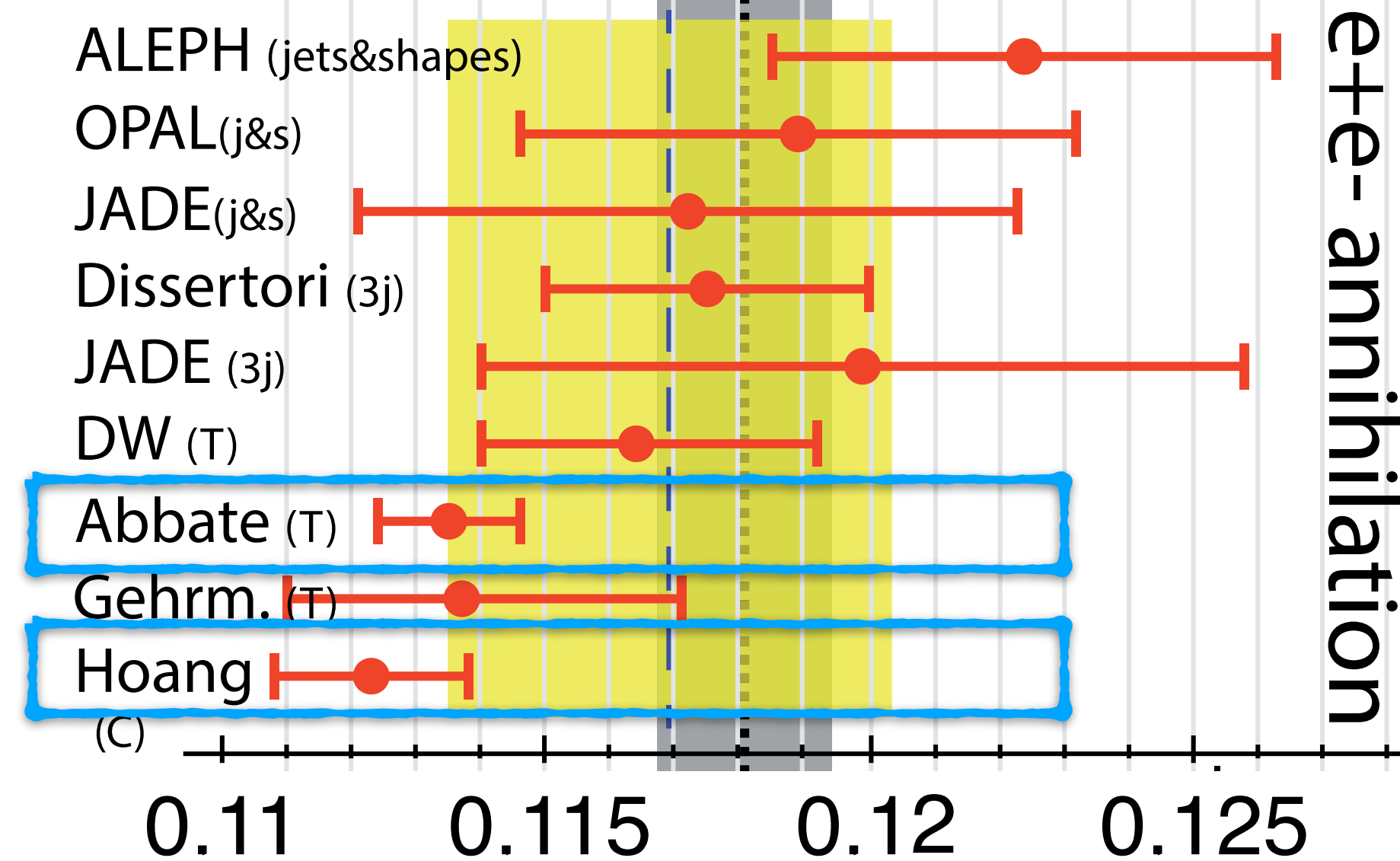
thrust & “best” lattice are 4- σ apart

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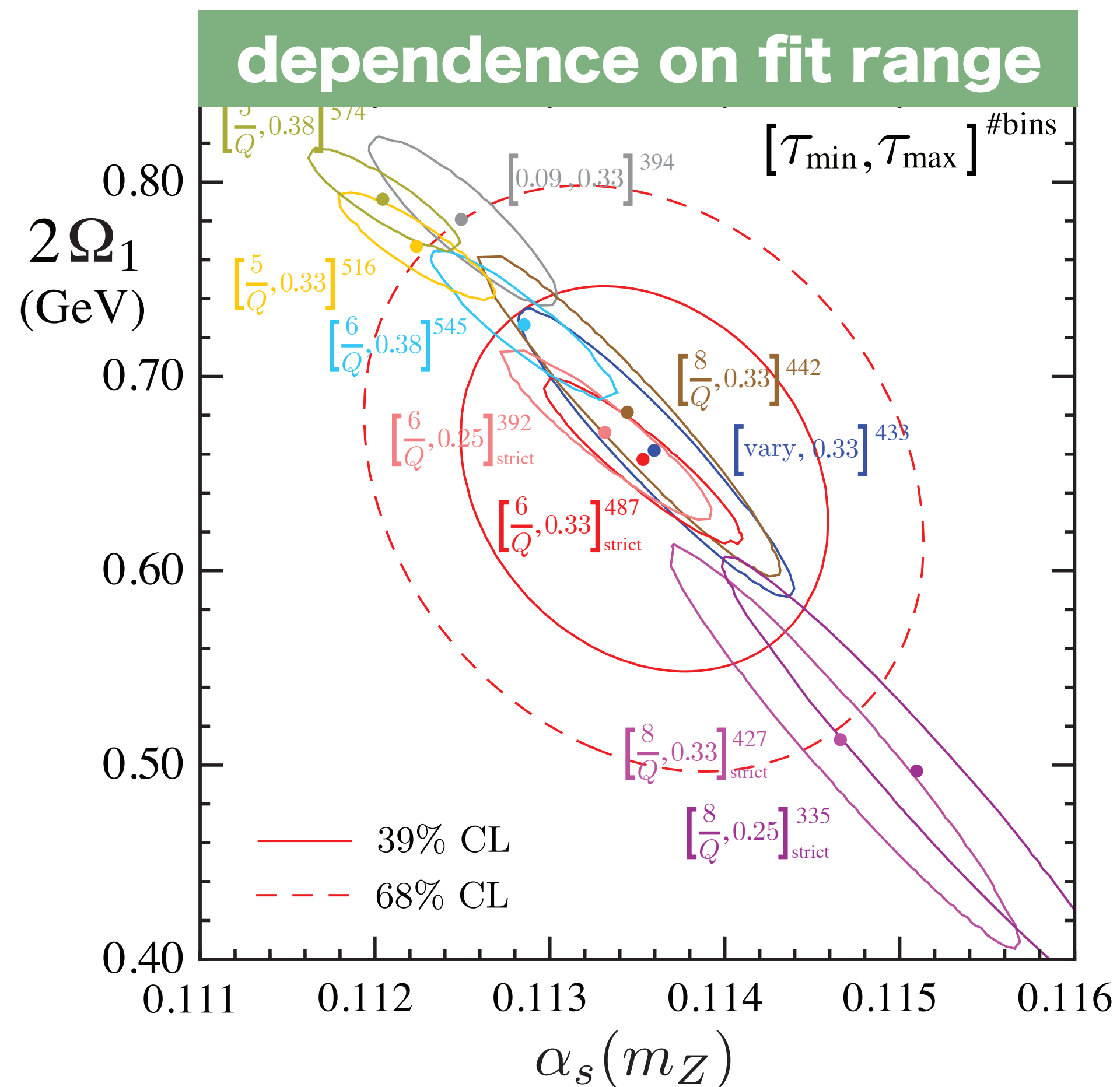
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thrust & “best” lattice are 4- σ apart

Comments:

- thrust & C-parameter are highly correlated observables
- Analysis valid far from 3-jet region, but not too deep into 2-jet region — at LEP, not clear how much of distribution satisfies this requirement
- thrust fit shows noticeable sensitivity to fit region (C-parameter doesn't)

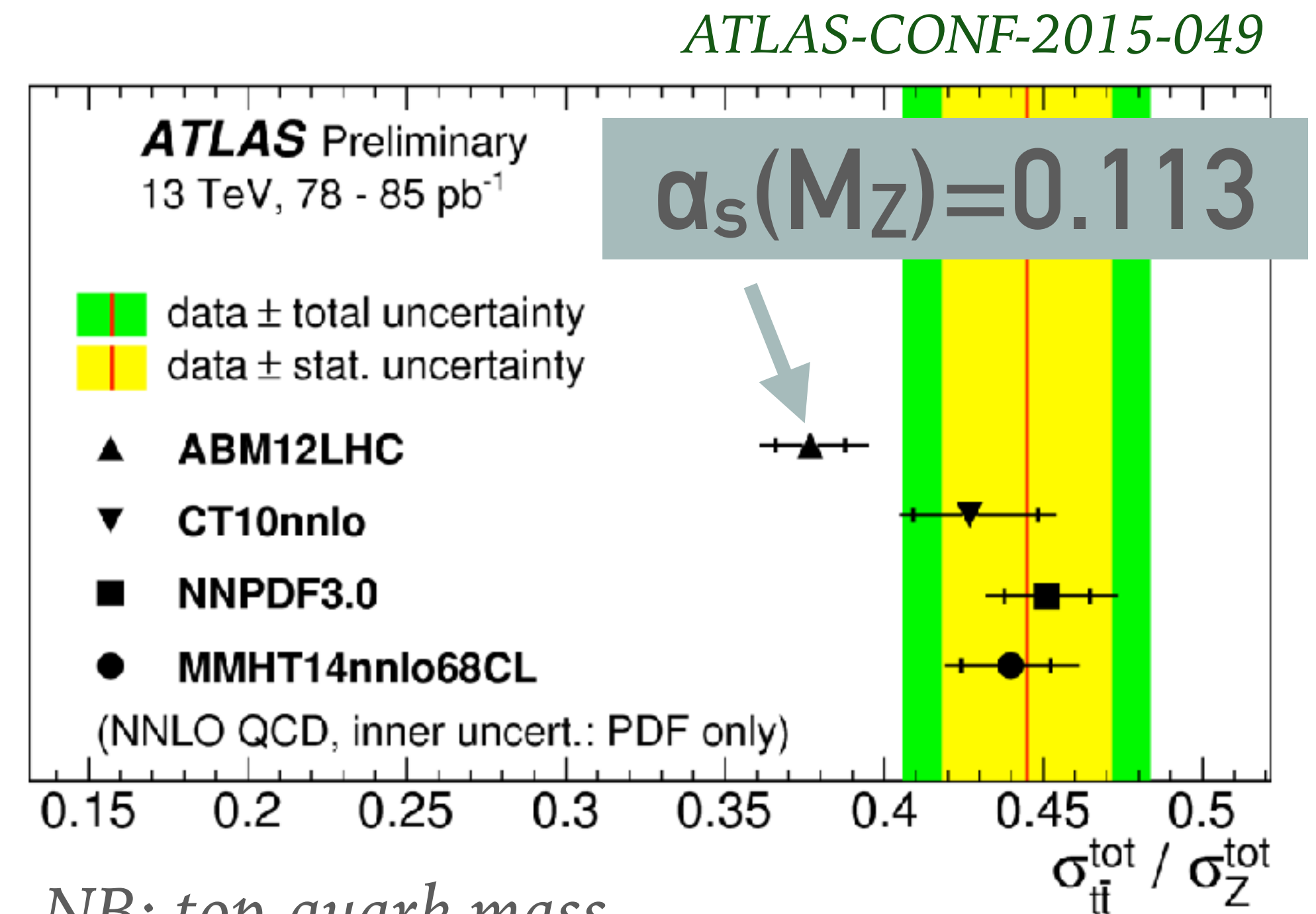


WHAT WAY FORWARDS FOR α_s ?

- ▶ We need to settle question of whether “small” (0.113) α_s is possible.

LHC data already weighing in on this (top data),
further info in near future ($Z p_T$, cf. later slides)

- ▶ To go beyond 1%, best hope is probably lattice QCD — on a 10-year timescale, there will likely be enough progress that multiple groups will have high-precision determinations



*NB: top-quark mass
choice affects this plot*

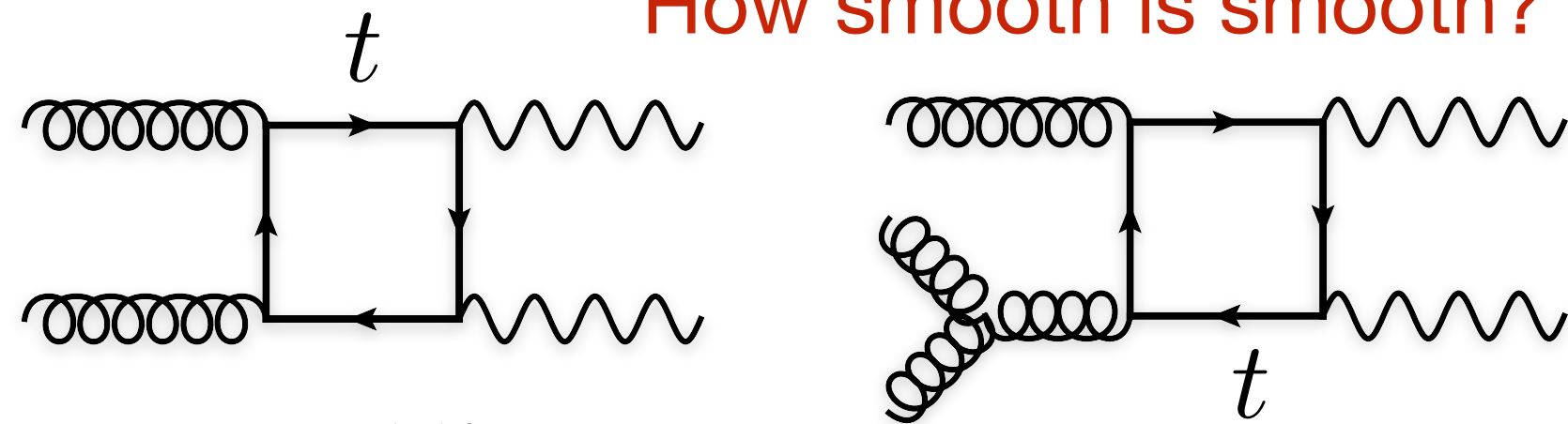
DATA-DRIVEN BKGD ESTIMATES: NON-SMOOTHNESS AT 1% LEVEL



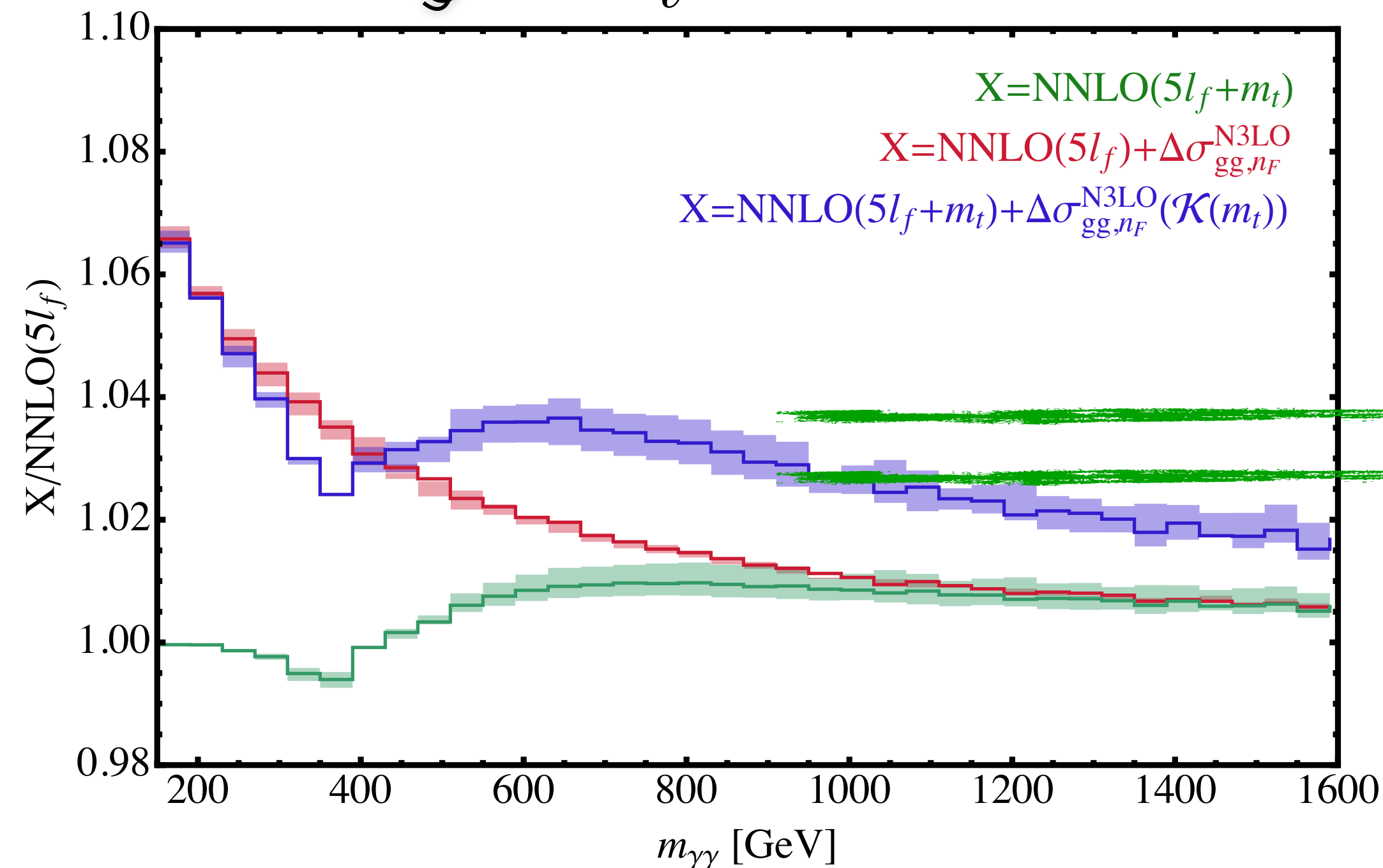
Predictions at high invariant masses.

As we all know, bump hunts in the diphoton system assume a smooth function which can be fitted to the data. Begging the question,

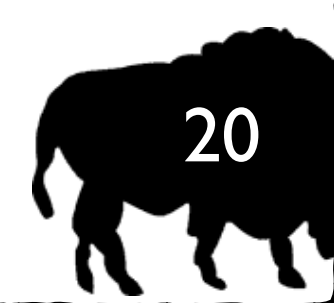
How smooth is smooth? :-)



*C. Williams
Moriond QCD '16*

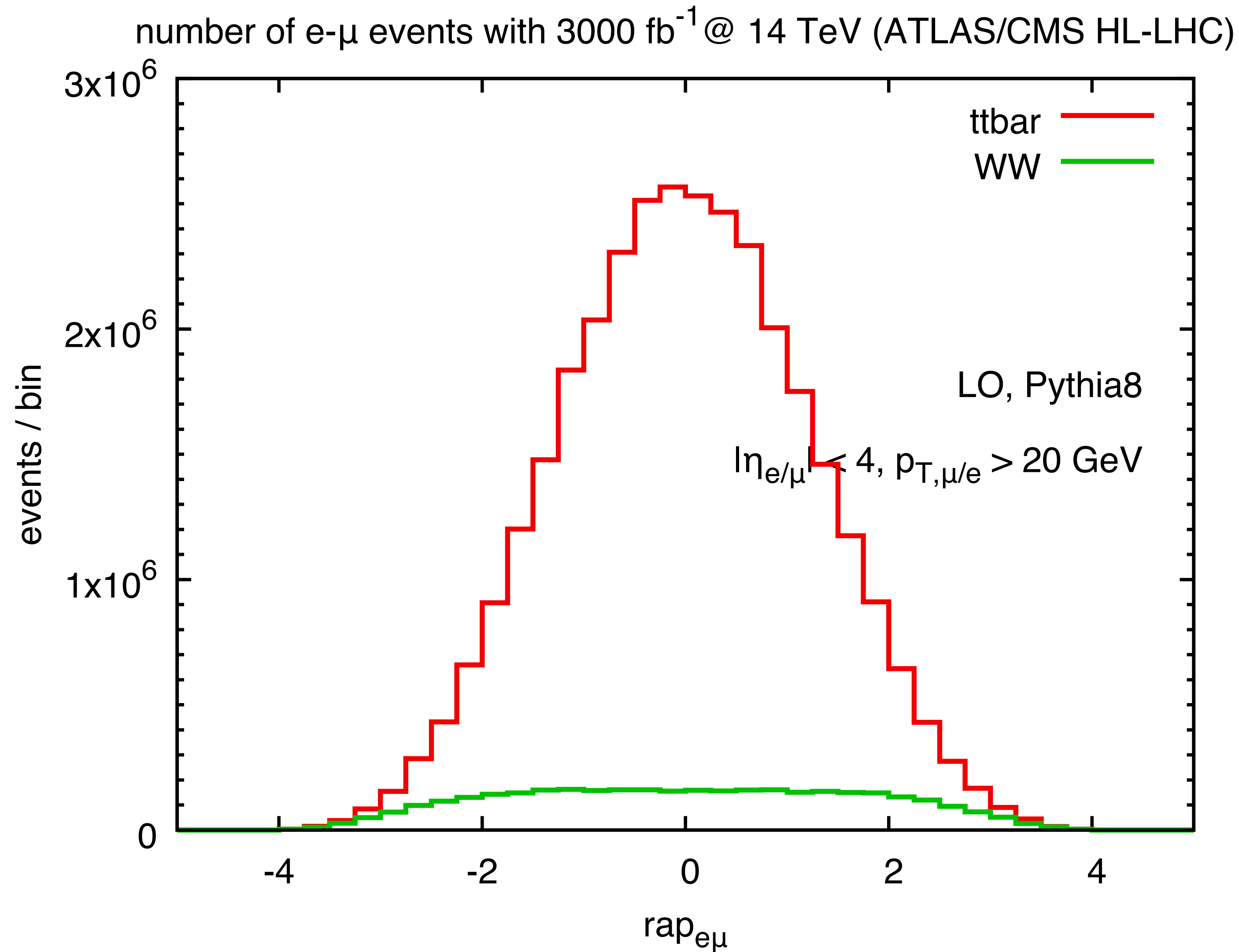


1%



Standard experimental techniques, like data-driven bkgd estimates, can be skewed by 0(1%) theoretical subtleties.

e- μ events (a mix of $t\bar{t}$ and VV) at HL-LHC ATLAS/CMS



this is a quick study to gauge orders of magnitude

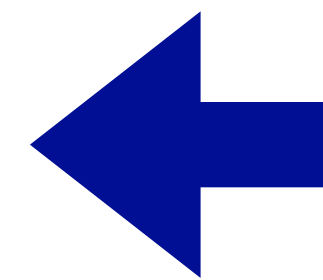
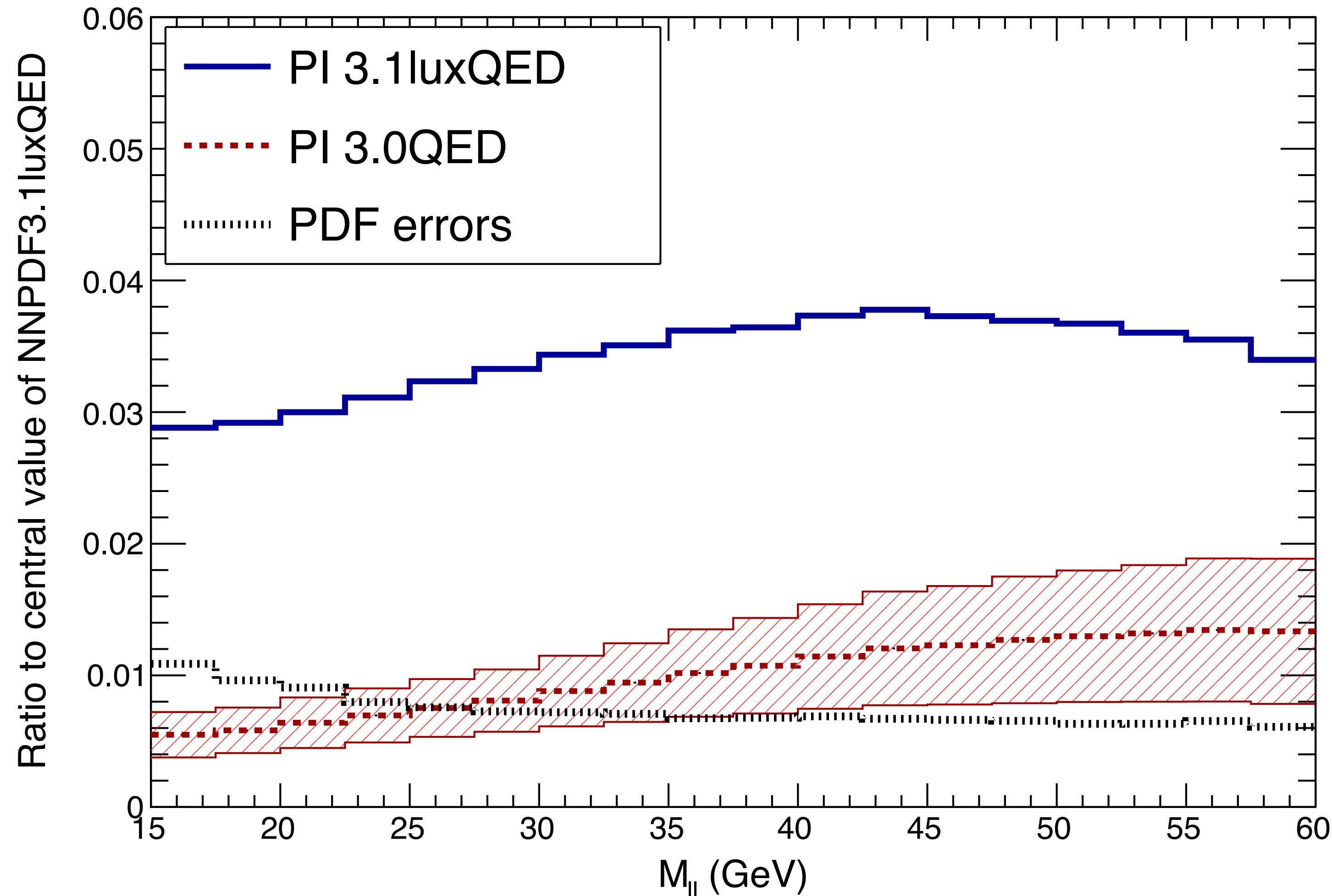
(Pythia8, LO, no showering)

N(N)LO K-factors will increase rates significantly

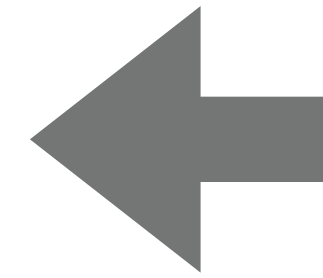
there will also be other VV channels (probably smaller)

Photon PDF (NNPDF3.1luxQED, using Manohar, Nason, GPS & Zanderighi, [1607.04266](#))

$$p p \rightarrow l^+ l^- @ \sqrt{s} = 13 \text{ TeV}, 0 < |y_{||}| < 2.5$$



barely any uncertainty on $\gamma\gamma$ -induced contribution



DY measurements can genuinely constraint other PDF contributions