

# Colliders, Higgs and the strong interaction

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*\* on leave from CERN and CNRS*



THE ROYAL SOCIETY



UNIVERSITY OF  
OXFORD

# particle physics

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## “big unanswered questions”

about fundamental particles & their interactions  
(dark matter, matter-antimatter asymmetry,  
nature of dark energy, hierarchy of scales...)

v.

## “big answerable questions”

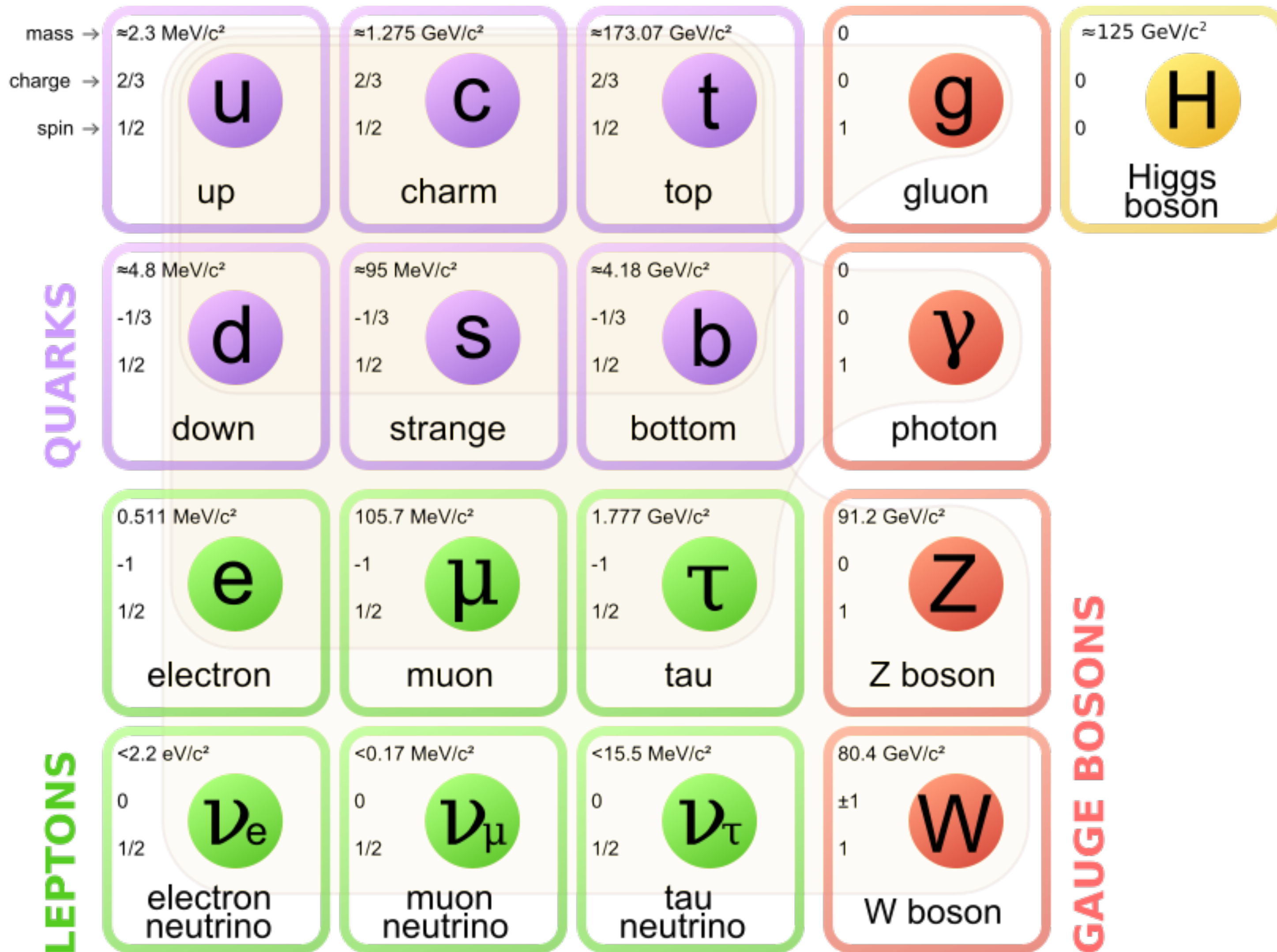
and how we go about answering them  
(nature of Higgs interactions, validity of SM up to high scales,  
lepton flavour universality, pattern of neutrino mixing, ...)

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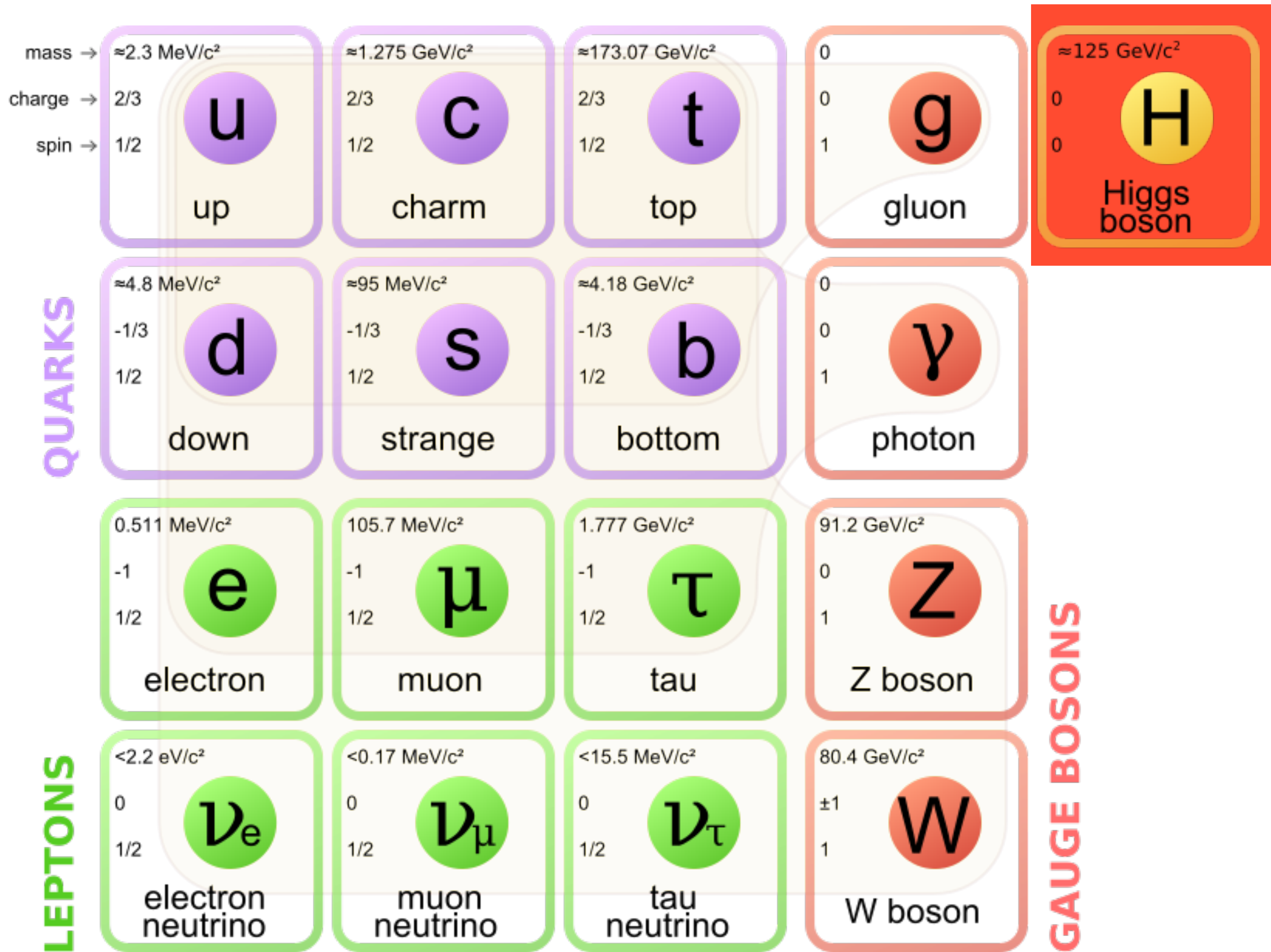
I personally expect supersymmetry to be discovered at the LHC

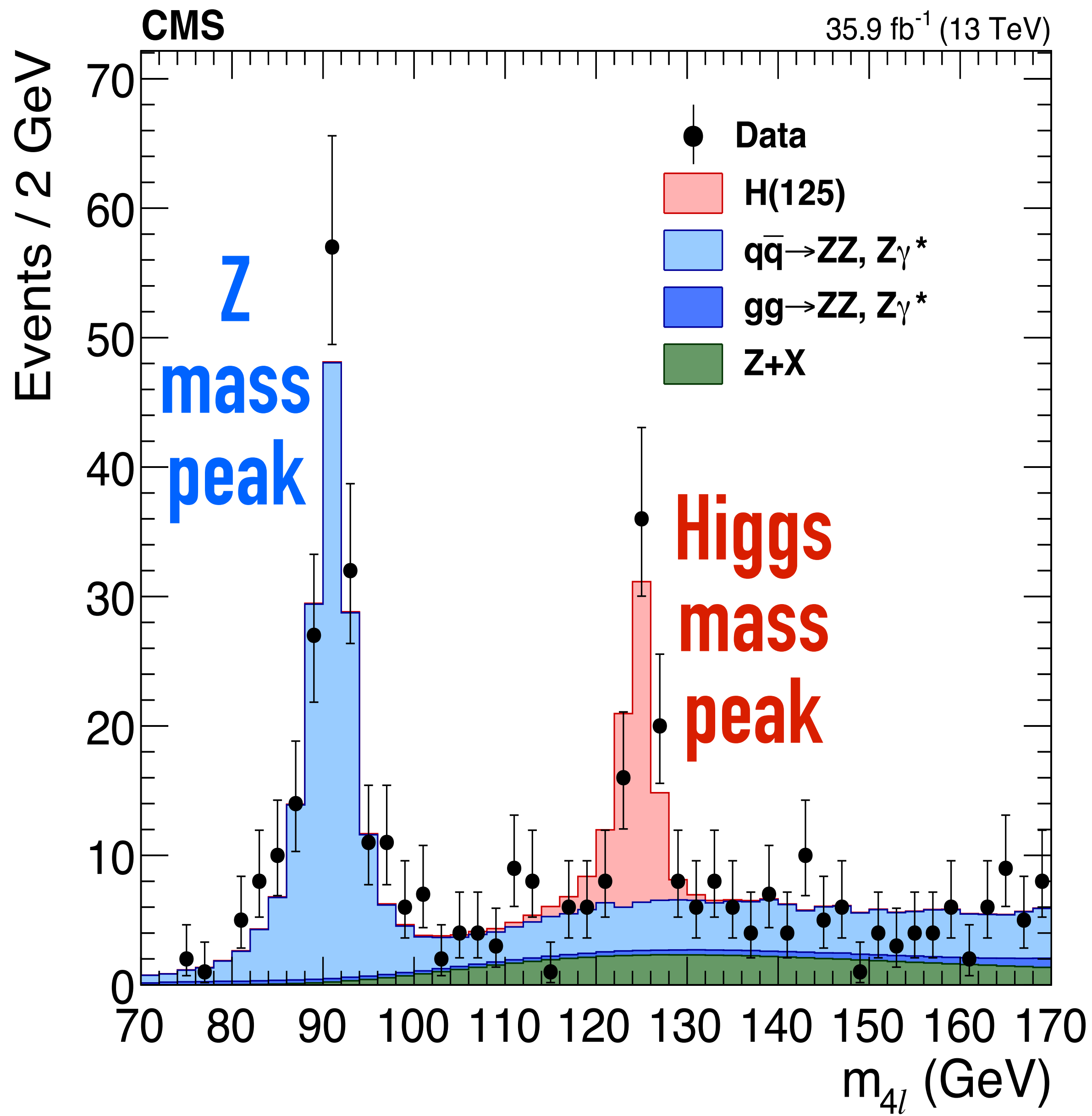
*-a Nobel prize-winning  
theorist [2008]*

# The Higgs boson



# The Higgs boson





ATLAS and CMS collaborations at  
 CERN's Large Hadron Collider  
 (LHC):

**2012 discovery of a  
 Higgs-like boson**

*plot shows more recent data*

# The Higgs boson (2012)

mass →	$\approx 2.3 \text{ MeV}/c^2$	$\approx 1.275 \text{ GeV}/c^2$	$\approx 173.07 \text{ GeV}/c^2$	0	$\approx 125 \text{ GeV}/c^2$
charge →	2/3	2/3	2/3	0	0
spin →	1/2	1/2	1/2	1	0
	<b>u</b> up	<b>c</b> charm	<b>t</b> top	<b>g</b> gluon	<b>H</b> Higgs boson
<b>QUARKS</b>	$\approx 4.8 \text{ MeV}/c^2$ -1/3 1/2 <b>d</b> down	$\approx 95 \text{ MeV}/c^2$ -1/3 1/2 <b>s</b> strange	$\approx 4.18 \text{ GeV}/c^2$ -1/3 1/2 <b>b</b> bottom	0 0 1 <b>γ</b> photon	
	0.511 $\text{MeV}/c^2$ -1 1/2 <b>e</b> electron	105.7 $\text{MeV}/c^2$ -1 1/2 <b>μ</b> muon	1.777 $\text{GeV}/c^2$ -1 1/2 <b>τ</b> tau	91.2 $\text{GeV}/c^2$ 0 1 <b>Z</b> Z boson	
<b>LEPTONS</b>	<2.2 $\text{eV}/c^2$ 0 1/2 <b>ν<sub>e</sub></b> electron neutrino	<0.17 $\text{MeV}/c^2$ 0 1/2 <b>ν<sub>μ</sub></b> muon neutrino	<15.5 $\text{MeV}/c^2$ 0 1/2 <b>ν<sub>τ</sub></b> tau neutrino	80.4 $\text{GeV}/c^2$ ±1 1 <b>W</b> W boson	<b>GAUGE BOSONS</b>

**Success!**  
**“The Standard Model is complete”**

# The Higgs boson (2012)

	mass →	charge →	spin →																									
QUARKS	$\approx 2.3 \text{ MeV}/c^2$	$2/3$	$1/2$	<b>u</b>	up	$\approx 1.275 \text{ GeV}/c^2$	$2/3$	$1/2$	<b>c</b>	charm	$\approx 173.07 \text{ GeV}/c^2$	$2/3$	$1/2$	<b>t</b>	top	0	0	1	<b>g</b>	gluon	$\approx 125 \text{ GeV}/c^2$	0	0	0	<b>H</b>	Higgs boson		
	$\approx 4.8 \text{ MeV}/c^2$	$-1/3$	$1/2$	<b>d</b>	down	$\approx 95 \text{ MeV}/c^2$	$-1/3$	$1/2$	<b>s</b>	strange	$\approx 4.18 \text{ GeV}/c^2$	$-1/3$	$1/2$	<b>b</b>	bottom	0	0	1	<b><math>\gamma</math></b>	photon								
	$0.511 \text{ MeV}/c^2$	-1	$1/2$	<b>e</b>	electron	$105.7 \text{ MeV}/c^2$	-1	$1/2$	<b><math>\mu</math></b>	muon	$1.777 \text{ GeV}/c^2$	-1	$1/2$	<b><math>\tau</math></b>	tau	0	0	1	<b>Z</b>	Z boson								
	$< 2.2 \text{ eV}/c^2$	0	$1/2$	<b><math>\nu_e</math></b>	electron neutrino	$< 0.17 \text{ MeV}/c^2$	0	$1/2$	<b><math>\nu_\mu</math></b>	muon neutrino	$< 15.5 \text{ MeV}/c^2$	0	$1/2$	<b><math>\nu_\tau</math></b>	tau neutrino	$\pm 1$	0	1	<b>W</b>	W boson								
LEPTONS																												

**Success!**  
 “The Standard Model is complete”

**Crisis!**  
 No supersymmetry, no extra dimensions, there's nothing left for us to do . . .



# The New York Times

By DENNIS OVERBYE    JUNE 19, 2017

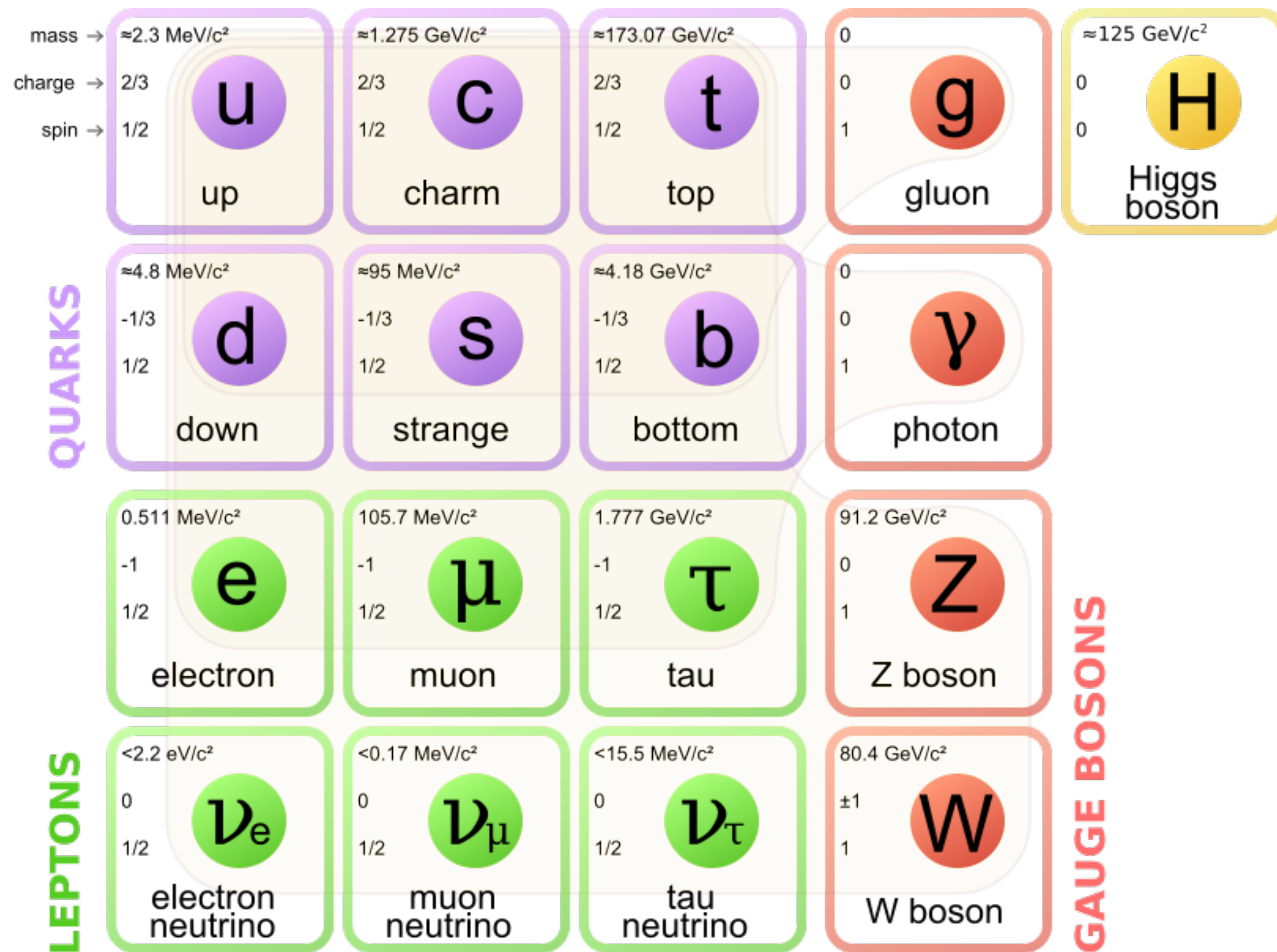
[...]

*What if there is nothing new to discover? That prospect is now a cloud hanging over the physics community.*

[...]

<https://www.nytimes.com/2017/06/19/science/cern-large-hadron-collider-higgs-physics.html>

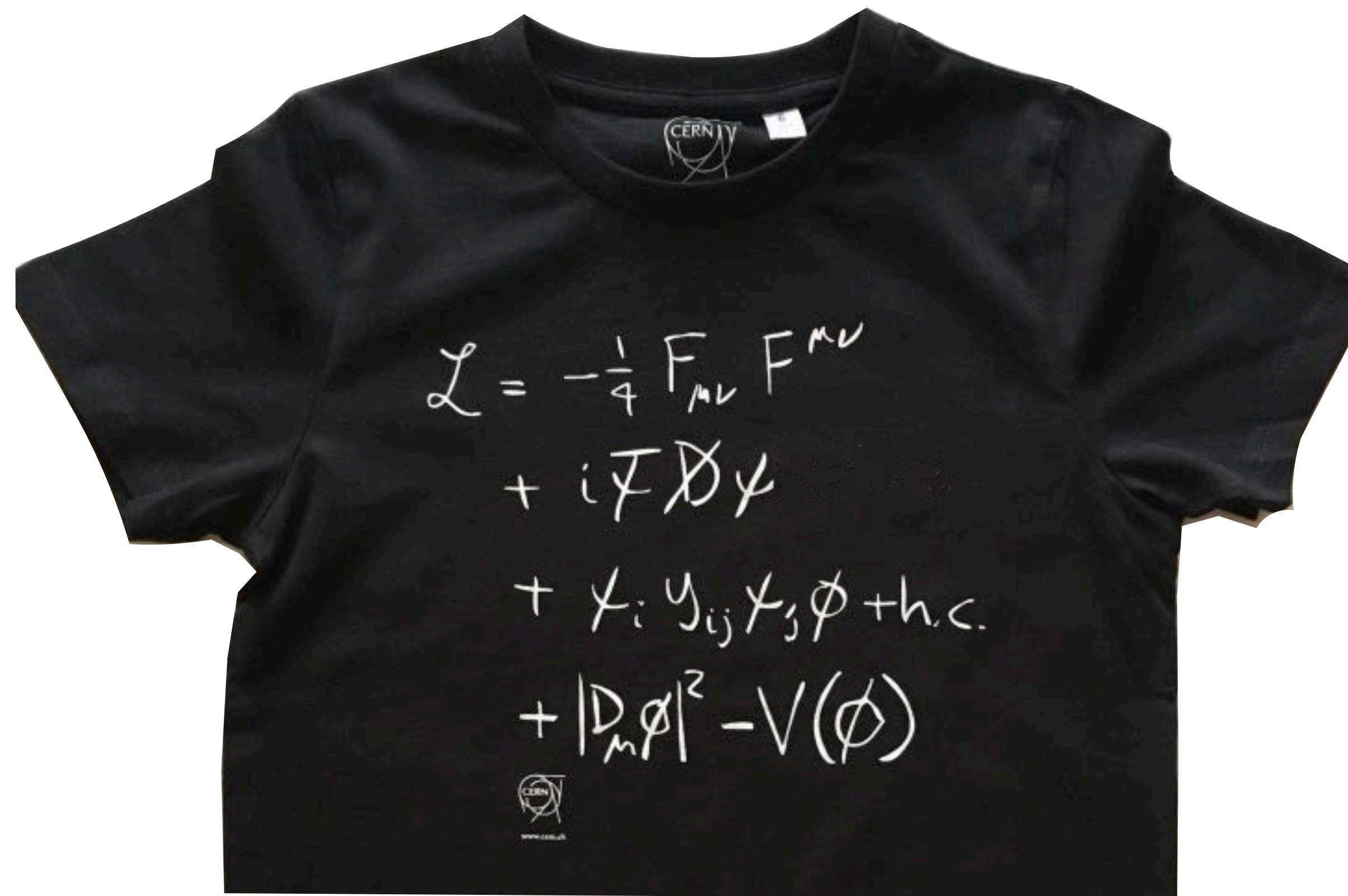
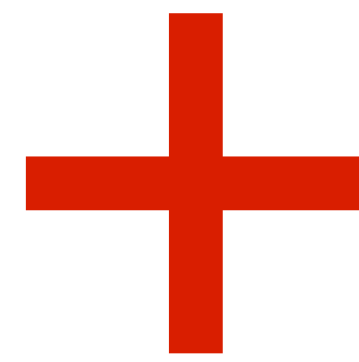
# what is the Standard Model?



*particles*

# what is the Standard Model?

mass →	≈2.3 MeV/c <sup>2</sup>	≈1.275 GeV/c <sup>2</sup>	≈173.07 GeV/c <sup>2</sup>	0	≈125 GeV/c <sup>2</sup>
charge →	2/3	2/3	2/3	0	0
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	<b>u</b> up	<b>c</b> charm	<b>t</b> top	<b>g</b> gluon	<b>H</b> Higgs boson
<b>QUARKS</b>					
	≈4.8 MeV/c <sup>2</sup>	≈95 MeV/c <sup>2</sup>	≈4.18 GeV/c <sup>2</sup>	0	
	-1/3	-1/3	-1/3	0	
	1/2	1/2	1/2	1	
	<b>d</b> down	<b>s</b> strange	<b>b</b> bottom	<b>γ</b> photon	
	0.511 MeV/c <sup>2</sup>	105.7 MeV/c <sup>2</sup>	1.777 GeV/c <sup>2</sup>	91.2 GeV/c <sup>2</sup>	
	-1	-1	-1	0	
	1/2	1/2	1/2	1	
	<b>e</b> electron	<b>μ</b> muon	<b>τ</b> tau	<b>Z</b> Z boson	
<b>LEPTONS</b>					
	<2.2 eV/c <sup>2</sup>	<0.17 MeV/c <sup>2</sup>	<15.5 MeV/c <sup>2</sup>	80.4 GeV/c <sup>2</sup>	
	0	0	0	±1	
	1/2	1/2	1/2	1	
	<b>ν<sub>e</sub></b> electron neutrino	<b>ν<sub>μ</sub></b> muon neutrino	<b>ν<sub>τ</sub></b> tau neutrino	<b>W</b> W boson	
					<b>GAUGE BOSONS</b>



*particles*

*interactions*

# STANDARD MODEL — KNOWABLE UNKNOWNNS

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$$\begin{aligned}\mathcal{L} = & -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} \\ & + i \bar{\psi} \not{D} \psi \\ & + \bar{\psi}_i Y_{ij} \psi_j \phi + \text{h.c.} \\ & + |D_\mu \phi|^2 - V(\phi)\end{aligned}$$

*These T-shirts come with  
a little explanation*

This equation neatly sums up our current understanding of fundamental particles and forces.

# STANDARD MODEL — KNOWABLE UNKNOWNNS

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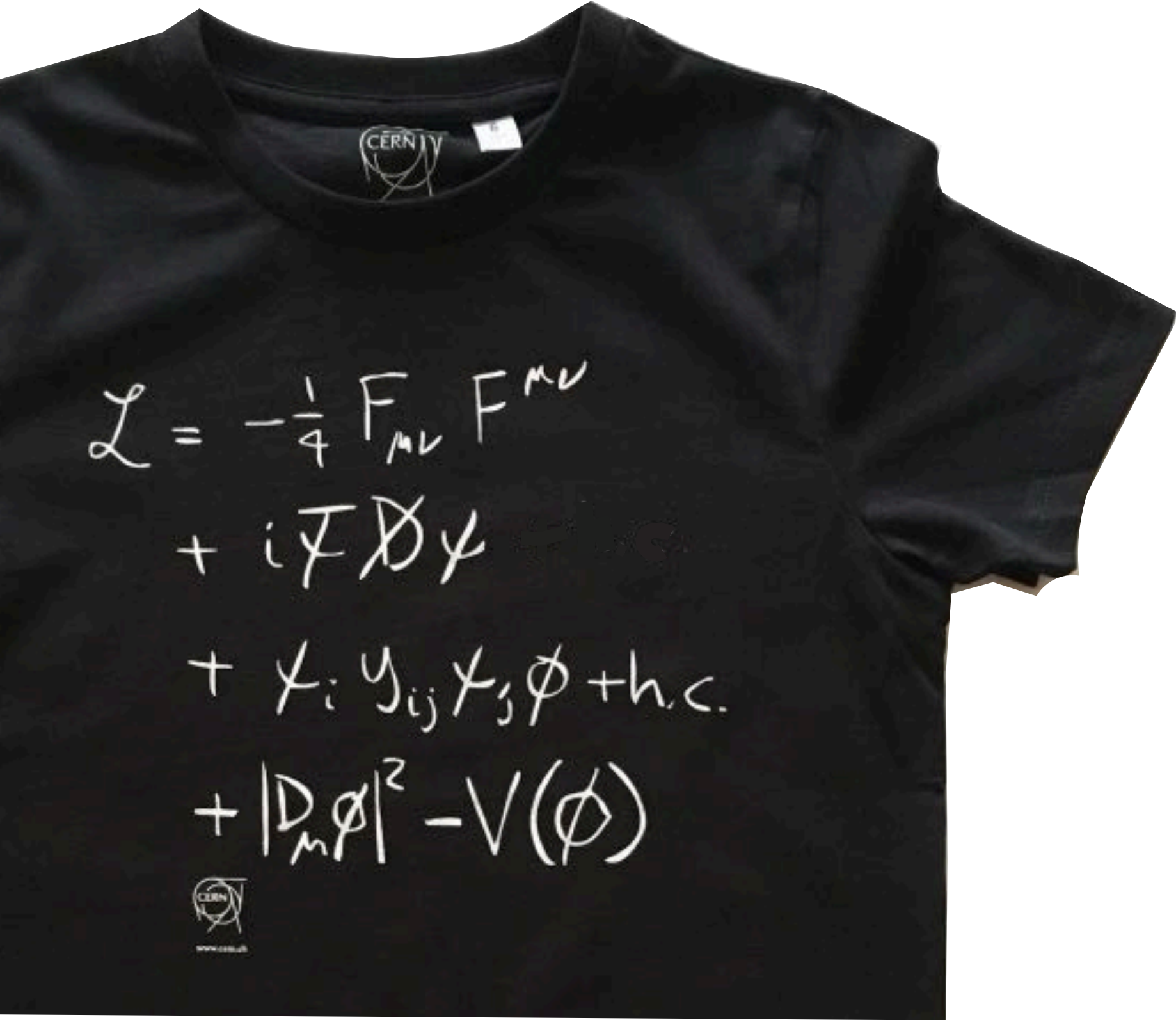
$$\begin{aligned} \mathcal{L} = & -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} \\ & + i \bar{\psi} \not{D} \psi \\ & + \bar{\psi}_i Y_{ij} \psi_j \phi + \text{h.c.} \\ & + |D_\mu \phi|^2 - V(\phi) \end{aligned}$$

*These T-shirts come with  
a little explanation*

*“understanding” = knowledge ?*

*“understanding” = assumption ?*

This equation neatly sums up our **current understanding** of fundamental particles and forces.



Standard Model Lagrangian (including neutrino mass terms)  
 From *An Introduction to the Standard Model of Particle Physics, 2nd Edition*,  
 W. N. Cottingham and D. A. Greenwood, Cambridge University Press, Cambridge, 2007,  
 Extracted by J.A. Shifflett, updated from Particle Data Group tables at pdg.lbl.gov, 2 Feb 2015.

$$\begin{aligned} \mathcal{L} = & -\frac{1}{4}B_{\mu\nu}B^{\mu\nu} - \frac{1}{8}\text{tr}(\mathbf{W}_{\mu\nu}\mathbf{W}^{\mu\nu}) - \frac{1}{2}\text{tr}(\mathbf{G}_{\mu\nu}\mathbf{G}^{\mu\nu}) & \text{(U(1), SU(2) and SU(3) gauge terms)} \\ & +(\bar{\nu}_L, \bar{e}_L)\bar{\sigma}^\mu iD_\mu \begin{pmatrix} \nu_L \\ e_L \end{pmatrix} + \bar{e}_R\sigma^\mu iD_\mu e_R + \bar{\nu}_R\sigma^\mu iD_\mu \nu_R + \text{(h.c.)} & \text{(lepton dynamical term)} \\ & -\frac{\sqrt{2}}{v}\left[(\bar{\nu}_L, \bar{e}_L)\phi M^e e_R + \bar{e}_R\bar{M}^e\bar{\phi} \begin{pmatrix} \nu_L \\ e_L \end{pmatrix}\right] & \text{(electron, muon, tauon mass term)} \\ & -\frac{\sqrt{2}}{v}\left[(\bar{e}_L, \bar{\nu}_L)\phi^* M^\nu \nu_R + \bar{\nu}_R\bar{M}^\nu\phi^T \begin{pmatrix} -\nu_L \\ \nu_L \end{pmatrix}\right] & \text{(neutrino mass term)} \\ & +(\bar{u}_L, \bar{d}_L)\bar{\sigma}^\mu iD_\mu \begin{pmatrix} u_L \\ d_L \end{pmatrix} + \bar{u}_R\sigma^\mu iD_\mu u_R + \bar{d}_R\sigma^\mu iD_\mu d_R + \text{(h.c.)} & \text{(quark dynamical term)} \\ & -\frac{\sqrt{2}}{v}\left[(\bar{u}_L, \bar{d}_L)\phi M^d d_R + \bar{d}_R\bar{M}^d\bar{\phi} \begin{pmatrix} u_L \\ d_L \end{pmatrix}\right] & \text{(down, strange, bottom mass term)} \\ & -\frac{\sqrt{2}}{v}\left[(\bar{d}_L, \bar{u}_L)\phi^* M^u u_R + \bar{u}_R\bar{M}^u\phi^T \begin{pmatrix} -d_L \\ u_L \end{pmatrix}\right] & \text{(up, charmed, top mass term)} \\ & +(\bar{D}_\mu\bar{\phi})D^\mu\phi - m_h^2[\bar{\phi}\phi - v^2/2]^2/2v^2. & \text{(Higgs dynamical and mass term)} \end{aligned} \quad (1)$$

where (h.c.) means Hermitian conjugate of preceding terms,  $\bar{\psi} = (\text{h.c.})\psi = \psi^\dagger = \psi^{*T}$ , and the derivative operators are

$$D_\mu \begin{pmatrix} \nu_L \\ e_L \end{pmatrix} = \left[ \partial_\mu - \frac{ig_1}{2}B_\mu + \frac{ig_2}{2}\mathbf{W}_\mu \right] \begin{pmatrix} \nu_L \\ e_L \end{pmatrix}, \quad D_\mu \begin{pmatrix} u_L \\ d_L \end{pmatrix} = \left[ \partial_\mu + \frac{ig_1}{6}B_\mu + \frac{ig_2}{2}\mathbf{W}_\mu + ig\mathbf{G}_\mu \right] \begin{pmatrix} u_L \\ d_L \end{pmatrix}, \quad (2)$$

$$D_\mu \nu_R = \partial_\mu \nu_R, \quad D_\mu e_R = [\partial_\mu - ig_1 B_\mu] e_R, \quad D_\mu u_R = \left[ \partial_\mu + \frac{i2g_1}{3}B_\mu + ig\mathbf{G}_\mu \right] u_R, \quad D_\mu d_R = \left[ \partial_\mu - \frac{ig_1}{3}B_\mu + ig\mathbf{G}_\mu \right] d_R, \quad (3)$$

$$D_\mu \phi = \left[ \partial_\mu + \frac{ig_1}{2}B_\mu + \frac{ig_2}{2}\mathbf{W}_\mu \right] \phi. \quad (4)$$

$\phi$  is a 2-component complex Higgs field. Since  $\mathcal{L}$  is  $SU(2)$  gauge invariant, a gauge can be chosen so  $\phi$  has the form

$$\phi^T = (0, v + h)/\sqrt{2}, \quad \langle \phi \rangle_0^T = (\text{expectation value of } \phi) = (0, v)/\sqrt{2}, \quad (5)$$

where  $v$  is a real constant such that  $\mathcal{L}_\phi = (\bar{\partial}_\mu\bar{\phi})\partial^\mu\phi - m_h^2[\bar{\phi}\phi - v^2/2]^2/2v^2$  is minimized, and  $h$  is a residual Higgs field.  $B_\mu$ ,  $\mathbf{W}_\mu$  and  $\mathbf{G}_\mu$  are the gauge boson vector potentials, and  $\mathbf{W}_\mu$  and  $\mathbf{G}_\mu$  are composed of  $2 \times 2$  and  $3 \times 3$  traceless Hermitian matrices. Their associated field tensors are

$$B_{\mu\nu} = \partial_\mu B_\nu - \partial_\nu B_\mu, \quad \mathbf{W}_{\mu\nu} = \partial_\mu \mathbf{W}_\nu - \partial_\nu \mathbf{W}_\mu + ig_2(\mathbf{W}_\mu \mathbf{W}_\nu - \mathbf{W}_\nu \mathbf{W}_\mu)/2, \quad \mathbf{G}_{\mu\nu} = \partial_\mu \mathbf{G}_\nu - \partial_\nu \mathbf{G}_\mu + ig(\mathbf{G}_\mu \mathbf{G}_\nu - \mathbf{G}_\nu \mathbf{G}_\mu). \quad (6)$$

The non-matrix  $A_\mu$ ,  $Z_\mu$ ,  $W_\mu^\pm$  bosons are mixtures of  $\mathbf{W}_\mu$  and  $B_\mu$  components, according to the weak mixing angle  $\theta_w$ ,

$$A_\mu = W_{11\mu}\sin\theta_w + B_\mu\cos\theta_w, \quad Z_\mu = W_{11\mu}\cos\theta_w - B_\mu\sin\theta_w, \quad W_\mu^\pm = W_{21\mu}^\pm/\sqrt{2}, \quad (7)$$

$$B_\mu = A_\mu\cos\theta_w - Z_\mu\sin\theta_w, \quad W_{11\mu} = -W_{22\mu} = A_\mu\sin\theta_w + Z_\mu\cos\theta_w, \quad W_{12\mu} = W_{21\mu}^* = \sqrt{2}W_\mu^\pm, \quad \sin^2\theta_w = .2315(4). \quad (8)$$

The fermions include the leptons  $e_R, e_L, \nu_R, \nu_L$  and quarks  $u_R, u_L, d_R, d_L$ . They all have implicit 3-component generation indices,  $e_i = (e, \mu, \tau)$ ,  $\nu_i = (\nu_e, \nu_\mu, \nu_\tau)$ ,  $u_i = (u, c, t)$ ,  $d_i = (d, s, b)$ , which contract into the fermion mass matrices  $M_{ij}^e, M_{ij}^\nu, M_{ij}^d, M_{ij}^u$ , and implicit 2-component indices which contract into the Pauli matrices,

$$\sigma^\mu = \left[ \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}, \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}, \begin{pmatrix} 0 & -i \\ i & 0 \end{pmatrix}, \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix} \right], \quad \bar{\sigma}^\mu = [\sigma^0, -\sigma^1, -\sigma^2, -\sigma^3], \quad \text{tr}(\sigma^i) = 0, \quad \sigma^{\mu\dagger} = \sigma^\mu, \quad \text{tr}(\sigma^\mu\sigma^\nu) = 2\delta^{\mu\nu}. \quad (9)$$

The quarks also have implicit 3-component color indices which contract into  $\mathbf{G}_\mu$ . So  $\mathcal{L}$  really has implicit sums over 3-component generation indices, 2-component Pauli indices, 3-component color indices in the quark terms, and 2-component  $SU(2)$  indices in  $(\nu_L, \bar{e}_L), (\bar{u}_L, \bar{d}_L), (-\bar{e}_L, \bar{\nu}_L), (-\bar{d}_L, \bar{u}_L), \phi, \mathbf{W}_\mu, (\nu_e, \nu_\mu, \nu_\tau), (u_e, u_c, u_t), (\bar{\nu}_e, \bar{\nu}_\mu, \bar{\nu}_\tau), (\bar{u}_e, \bar{u}_c, \bar{u}_t), (\bar{d}_e, \bar{d}_s, \bar{d}_b)$ .

The electroweak and strong coupling constants, Higgs vacuum expectation value (VEV), and Higgs mass are,

$$g_1 = e/\cos\theta_w, \quad g_2 = e/\sin\theta_w, \quad g > 6.5e = g(m_\tau^*), \quad v = 246\text{GeV} (PDG) \approx \sqrt{2} \cdot 180\text{GeV} (CG), \quad m_h = 125.02(30)\text{GeV} \quad (10)$$

where  $e = \sqrt{4\pi\alpha\hbar c} = \sqrt{4\pi/137}$  in natural units. Using (4,5) and rewriting some things gives the mass of  $A_\mu, Z_\mu, W_\mu^\pm$ ,

$$-\frac{1}{4}B_{\mu\nu}B^{\mu\nu} - \frac{1}{8}\text{tr}(\mathbf{W}_{\mu\nu}\mathbf{W}^{\mu\nu}) = -\frac{1}{4}A_{\mu\nu}A^{\mu\nu} - \frac{1}{4}Z_{\mu\nu}Z^{\mu\nu} - \frac{1}{2}W_{\mu\nu}^+W^{\mu\nu-} + \left( \begin{array}{l} \text{higher} \\ \text{order terms} \end{array} \right), \quad (11)$$

$$A_{\mu\nu} = \partial_\mu A_\nu - \partial_\nu A_\mu, \quad Z_{\mu\nu} = \partial_\mu Z_\nu - \partial_\nu Z_\mu, \quad W_{\mu\nu}^\pm = D_\mu W_\nu^\pm - D_\nu W_\mu^\pm, \quad D_\mu W_\nu^\pm = [\partial_\mu \pm ieA_\mu]W_\nu^\pm, \quad (12)$$

$$D_\mu \langle \phi \rangle_0 = \frac{iv}{\sqrt{2}} \begin{pmatrix} g_1 B_{12\mu}/2 \\ g_2 W_{12\mu}/2 + g_2 W_{22\mu}/2 \end{pmatrix} = \frac{ig_2 v}{2} \begin{pmatrix} W_{12\mu}/\sqrt{2} \\ (B_\mu \sin\theta_w / \cos\theta_w + W_{22\mu})/\sqrt{2} \end{pmatrix} = \frac{ig_2 v}{2} \begin{pmatrix} W_\mu^+ \\ -Z_\mu/\sqrt{2}\cos\theta_w \end{pmatrix}, \quad (13)$$

$$\Rightarrow m_A = 0, \quad m_{W^\pm} = g_2 v/2 = 80.425(38)\text{GeV}, \quad m_Z = g_2 v/2\cos\theta_w = 91.1876(21)\text{GeV}. \quad (14)$$

Ordinary 4-component Dirac fermions are composed of the left and right handed 2-component fields,

$$e = \begin{pmatrix} e_{L1} \\ e_{R1} \end{pmatrix}, \quad \nu_e = \begin{pmatrix} \nu_{L1} \\ \nu_{R1} \end{pmatrix}, \quad u = \begin{pmatrix} u_{L1} \\ u_{R1} \end{pmatrix}, \quad d = \begin{pmatrix} d_{L1} \\ d_{R1} \end{pmatrix}, \quad \text{(electron, electron neutrino, up and down quark)} \quad (15)$$

$$\mu = \begin{pmatrix} e_{L2} \\ e_{R2} \end{pmatrix}, \quad \nu_\mu = \begin{pmatrix} \nu_{L2} \\ \nu_{R2} \end{pmatrix}, \quad c = \begin{pmatrix} u_{L2} \\ u_{R2} \end{pmatrix}, \quad s = \begin{pmatrix} d_{L2} \\ d_{R2} \end{pmatrix}, \quad \text{(muon, muon neutrino, charmed and strange quark)} \quad (16)$$

$$\tau = \begin{pmatrix} e_{L3} \\ e_{R3} \end{pmatrix}, \quad \nu_\tau = \begin{pmatrix} \nu_{L3} \\ \nu_{R3} \end{pmatrix}, \quad t = \begin{pmatrix} u_{L3} \\ u_{R3} \end{pmatrix}, \quad b = \begin{pmatrix} d_{L3} \\ d_{R3} \end{pmatrix}, \quad \text{(tauon, tauon neutrino, top and bottom quark)} \quad (17)$$

$$\gamma^\mu = \begin{pmatrix} 0 & \sigma^\mu \\ \bar{\sigma}^\mu & 0 \end{pmatrix} \quad \text{where } \gamma^\mu\gamma^\nu + \gamma^\nu\gamma^\mu = 2I g^{\mu\nu}. \quad \text{(Dirac gamma matrices in chiral representation)} \quad (18)$$

The corresponding antiparticles are related to the particles according to  $\psi^c = -i\gamma^2\psi^*$  or  $\psi_L^c = -i\sigma^2\psi_R^*$ ,  $\psi_R^c = i\sigma^2\psi_L^*$ . The fermion charges are the coefficients of  $A_\mu$  when (8,10) are substituted into either the left or right handed derivative operators (2-4). The fermion masses are the singular values of the  $3 \times 3$  fermion mass matrices  $M^e, M^\nu, M^u, M^d$ ,

$$M^e = \mathbf{U}_L^{e\dagger} \begin{pmatrix} m_e & 0 & 0 \\ 0 & m_\mu & 0 \\ 0 & 0 & m_\tau \end{pmatrix} \mathbf{U}_R^e, \quad M^\nu = \mathbf{U}_L^{\nu\dagger} \begin{pmatrix} m_{\nu_e} & 0 & 0 \\ 0 & m_{\nu_\mu} & 0 \\ 0 & 0 & m_{\nu_\tau} \end{pmatrix} \mathbf{U}_R^\nu, \quad M^u = \mathbf{U}_L^{u\dagger} \begin{pmatrix} m_u & 0 & 0 \\ 0 & m_c & 0 \\ 0 & 0 & m_t \end{pmatrix} \mathbf{U}_R^u, \quad M^d = \mathbf{U}_L^{d\dagger} \begin{pmatrix} m_d & 0 & 0 \\ 0 & m_s & 0 \\ 0 & 0 & m_b \end{pmatrix} \mathbf{U}_R^d, \quad (19)$$

$$m_e = .510998910(13)\text{MeV}, \quad m_{\nu_e} \sim .001 - 2\text{eV}, \quad m_u = 1.7 - 3.1\text{MeV}, \quad m_d = 4.1 - 5.7\text{MeV}, \quad (20)$$

$$m_\mu = 105.658367(4)\text{MeV}, \quad m_{\nu_\mu} \sim .001 - 2\text{eV}, \quad m_c = 1.18 - 1.34\text{GeV}, \quad m_s = 80 - 130\text{MeV}, \quad (21)$$

$$m_\tau = 1776.84(17)\text{MeV}, \quad m_{\nu_\tau} \sim .001 - 2\text{eV}, \quad m_t = 171.4 - 174.4\text{GeV}, \quad m_b = 4.13 - 4.37\text{GeV}, \quad (22)$$

where the  $\mathbf{U}$ s are  $3 \times 3$  unitary matrices ( $\mathbf{U}^{-1} = \mathbf{U}^\dagger$ ). Consequently the "true fermions" with definite masses are actually linear combinations of those in  $\mathcal{L}$ , or conversely the fermions in  $\mathcal{L}$  are linear combinations of the true fermions,

$$e'_L = \mathbf{U}_L^e e_L, \quad e'_R = \mathbf{U}_R^e e_R, \quad \nu'_L = \mathbf{U}_L^\nu \nu_L, \quad \nu'_R = \mathbf{U}_R^\nu \nu_R, \quad u'_L = \mathbf{U}_L^u u_L, \quad u'_R = \mathbf{U}_R^u u_R, \quad d'_L = \mathbf{U}_L^d d_L, \quad d'_R = \mathbf{U}_R^d d_R, \quad (23)$$

$$e_L = \mathbf{U}_L^{e\dagger} e'_L, \quad e_R = \mathbf{U}_R^{e\dagger} e'_R, \quad \nu_L = \mathbf{U}_L^{\nu\dagger} \nu'_L, \quad \nu_R = \mathbf{U}_R^{\nu\dagger} \nu'_R, \quad u_L = \mathbf{U}_L^{u\dagger} u'_L, \quad u_R = \mathbf{U}_R^{u\dagger} u'_R, \quad d_L = \mathbf{U}_L^{d\dagger} d'_L, \quad d_R = \mathbf{U}_R^{d\dagger} d'_R. \quad (24)$$

When  $\mathcal{L}$  is written in terms of the true fermions, the  $\mathbf{U}$ s fall out except in  $\bar{u}'_L \mathbf{U}_L^u \bar{\sigma}^\mu W_\mu^\pm \mathbf{U}_L^d d'_L$  and  $\bar{d}'_L \mathbf{U}_L^d \bar{\sigma}^\mu W_\mu^\pm \mathbf{U}_L^u u'_L$ . Because of this, and some absorption of constants into the fermion fields, all the parameters in the  $\mathbf{U}$ s are contained in only four components of the Cabibbo-Kobayashi-Maskawa matrix  $\mathbf{V}^q = \mathbf{U}_L^q \mathbf{U}_L^{q\dagger}$  and four components of the Pontecorvo-Maki-Nakagawa-Sakata matrix  $\mathbf{V}^l = \mathbf{U}_L^l \mathbf{U}_L^{l\dagger}$ . The unitary matrices  $\mathbf{V}^q$  and  $\mathbf{V}^l$  are often parameterized as

$$\mathbf{V} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} e^{-i\delta/2} & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & e^{i\delta/2} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & s_{13} \\ 0 & 1 & 0 \\ -s_{13} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} e^{i\delta/2} & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & e^{-i\delta/2} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}, \quad c_j = \sqrt{1 - s_j^2}, \quad (25)$$

$$\delta^q = 69(4) \text{ deg}, \quad s_{12}^q = 0.2253(7), \quad s_{23}^q = 0.041(1), \quad s_{13}^q = 0.0035(2), \quad (26)$$

$$\delta^l = ?, \quad s_{12}^l = 0.560(16), \quad s_{23}^l = 0.7(1), \quad s_{13}^l = 0.153(28). \quad (27)$$

$\mathcal{L}$  is invariant under a  $U(1) \otimes SU(2)$  gauge transformation with  $U^{-1} = U^\dagger$ ,  $\det U = 1$ ,  $\theta$  real,

$$\mathbf{W}_\mu \rightarrow U \mathbf{W}_\mu U^\dagger - (2i/g_2)U \partial_\mu U^\dagger, \quad \mathbf{W}_{\mu\nu} \rightarrow U \mathbf{W}_{\mu\nu} U^\dagger, \quad B_\mu \rightarrow B_\mu + (2/g_1)\partial_\mu \theta, \quad B_{\mu\nu} \rightarrow B_{\mu\nu}, \quad \phi \rightarrow e^{-i\theta} U \phi, \quad (28)$$

$$\begin{pmatrix} \nu_L \\ e_L \end{pmatrix} \rightarrow e^{i\theta} U \begin{pmatrix} \nu_L \\ e_L \end{pmatrix}, \quad \begin{pmatrix} u_L \\ d_L \end{pmatrix} \rightarrow e^{-i\theta/3} U \begin{pmatrix} u_L \\ d_L \end{pmatrix}, \quad \nu_R \rightarrow \nu_R, \quad u_R \rightarrow e^{-4i\theta/3} u_R, \quad (29)$$

and under an  $SU(3)$  gauge transformation with  $V^{-1} = V^\dagger$ ,  $\det V = 1$ ,

$$\mathbf{G}_\mu \rightarrow V \mathbf{G}_\mu V^\dagger - (i/g)V \partial_\mu V^\dagger, \quad \mathbf{G}_{\mu\nu} \rightarrow V \mathbf{G}_{\mu\nu} V^\dagger, \quad u_L \rightarrow V u_L, \quad d_L \rightarrow V d_L, \quad u_R \rightarrow V u_R, \quad d_R \rightarrow V d_R. \quad (30)$$

## What does it mean?

---

$$\mathcal{L} = -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} + i\bar{\psi}\not{D}\psi + \bar{\psi}_i Y_{ij} \psi_j \phi + \text{h.c.} + |D_\mu \phi|^2 - V(\phi)$$

Quantum formulation of Maxwell's equations, (and their analogues for the weak and strong forces).



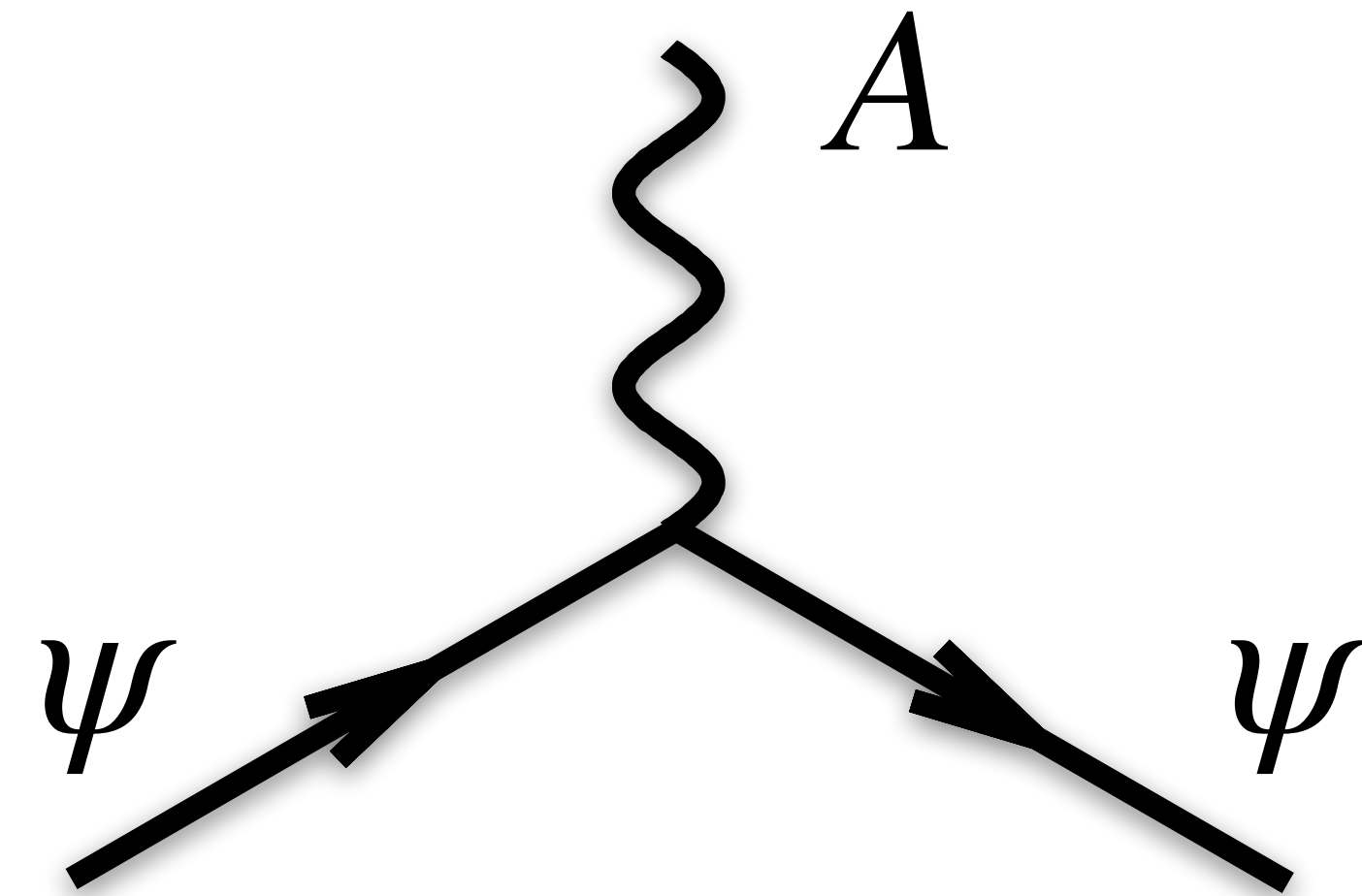
This equation neatly sums up our current understanding of fundamental particles and forces.

$$\mathcal{L} = -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} + i\bar{\psi}\not{D}\psi + \bar{\psi}_i Y_{ij} \psi_j \phi + \text{h.c.} + |D_\mu \phi|^2 - V(\phi)$$

## What does it mean?

$\psi = \text{fermion (e.g. electron) field}$

$D \sim eA (= \text{photon field}) + \dots$



*tells you there's an electron-photon interaction vertex*

This equation neatly sums up our current understanding of fundamental particles and forces.



$$\mathcal{L} = -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} + i\bar{\psi}\not{D}\psi + \bar{\psi}_i Y_{ij} \psi_j \phi + \text{h.c.} + |D_\mu \phi|^2 - V(\phi)$$

## What does it mean?

many experiments have probed these so-called “gauge” interactions (in classical form, they date back to 1860s)

Describe electromagnetism, full electroweak theory & the strong force.

**They work to high precision** (best tests go up to 1 part in  $10^8$ )

This equation neatly sums up our current understanding of fundamental particles and forces.

# Higgs sector

---

until 7 years ago none of these terms had ever been directly observed.

$$\mathcal{L} = -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} + i \bar{\psi} \not{D} \psi$$

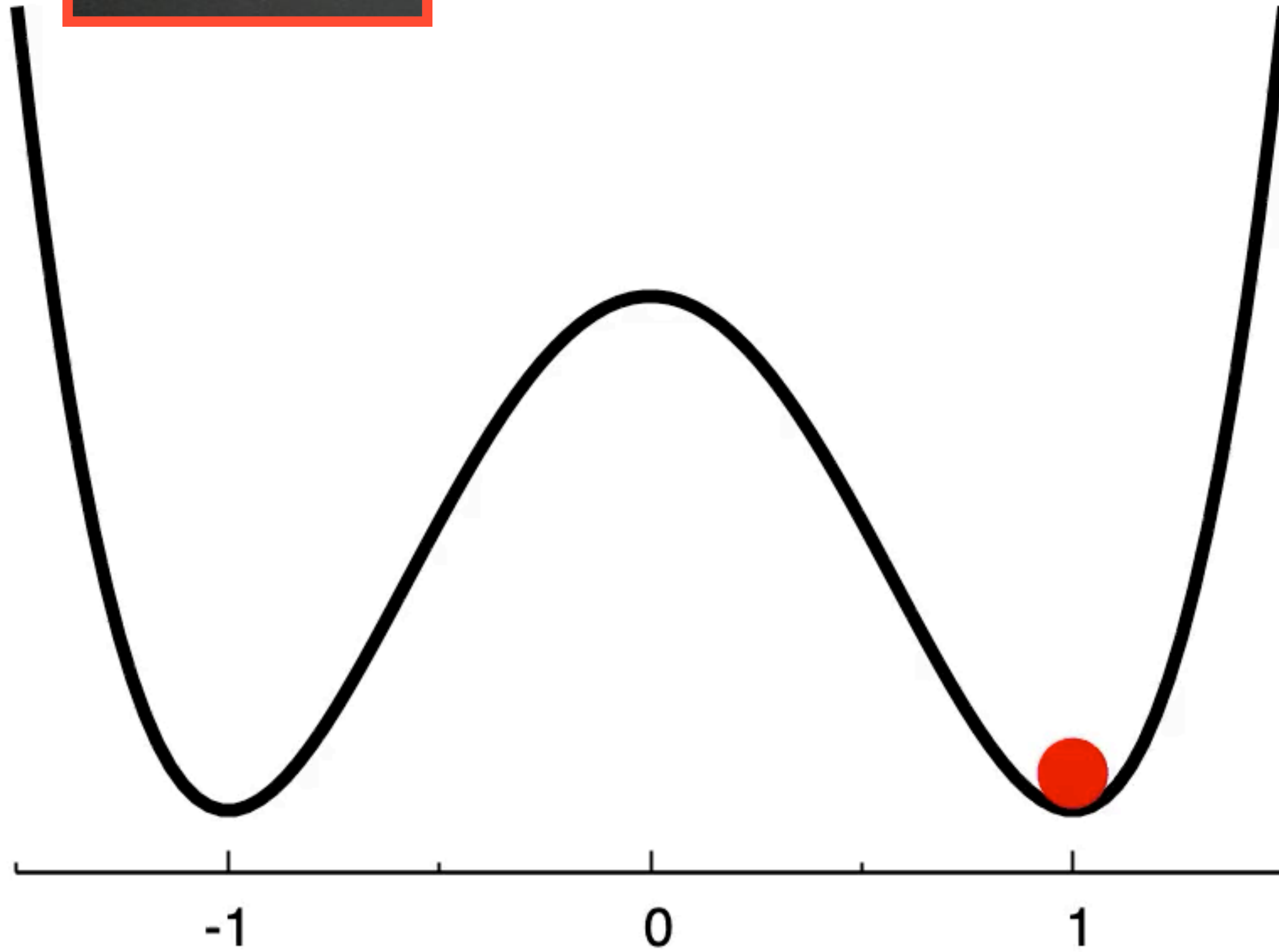
$$+ \sum_i Y_{ij} \bar{\psi}_i \psi_j \phi + \text{h.c.} + |D_\mu \phi|^2 - V(\phi)$$

This equation neatly sums up our current understanding of fundamental particles and forces.

$$V(\phi)$$

$$= -\mu^2\phi^2 + \lambda\phi^4$$

- $\phi$  is a field at every point in space (plot shows potential vs. 1 of 4 components, at 1 point in space)



Higgs field  $\phi$  [units of vacuum expectation value,  $\phi_0]$

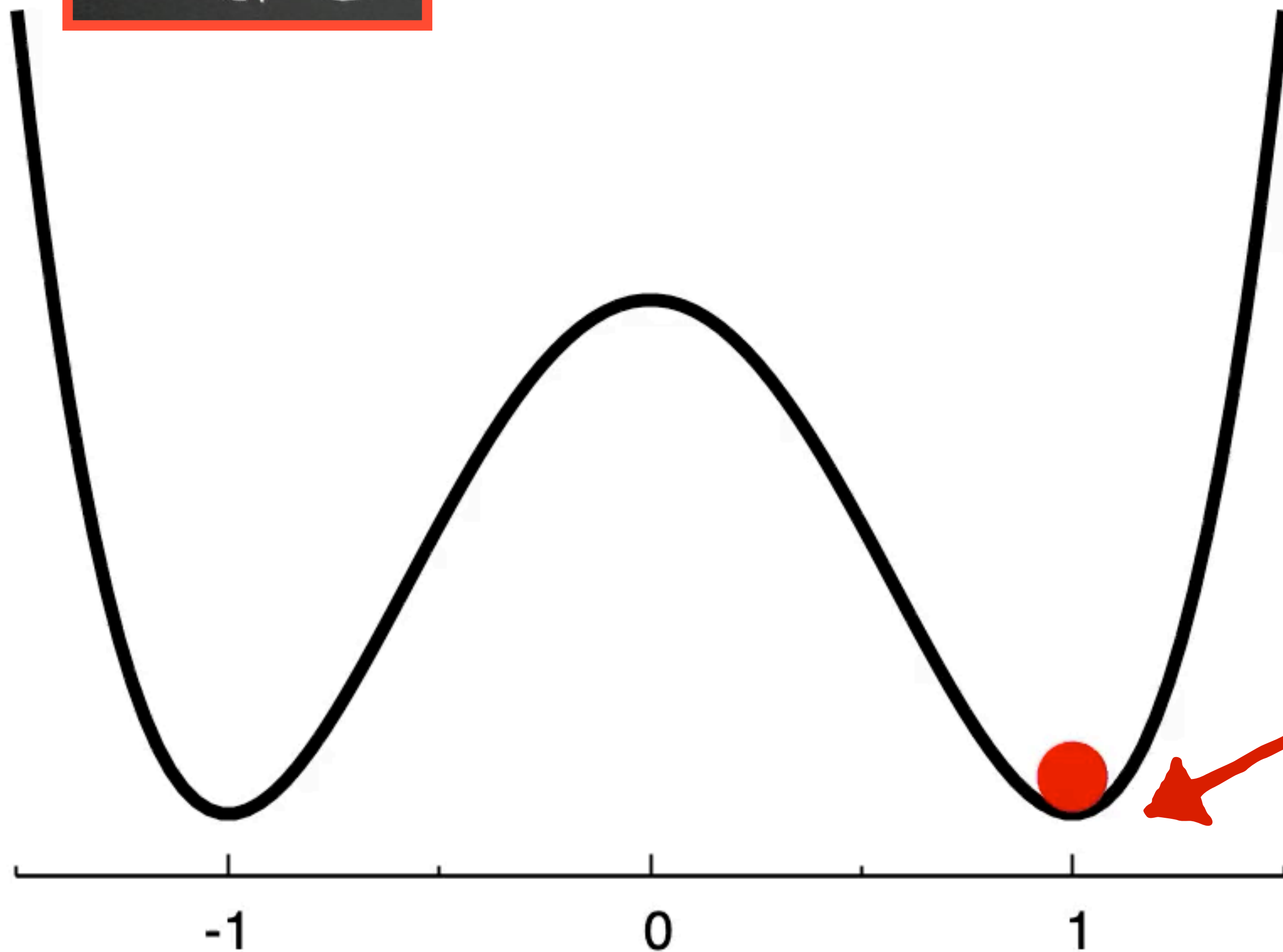
$$V(\phi)$$

$$= -\mu^2\phi^2 + \lambda\phi^4$$

- ▶  $\phi$  is a field at every point in space (plot shows potential vs. 1 of 4 components, at 1 point in space)

- ▶ Our universe sits at minimum of  $V(\phi)$ , at

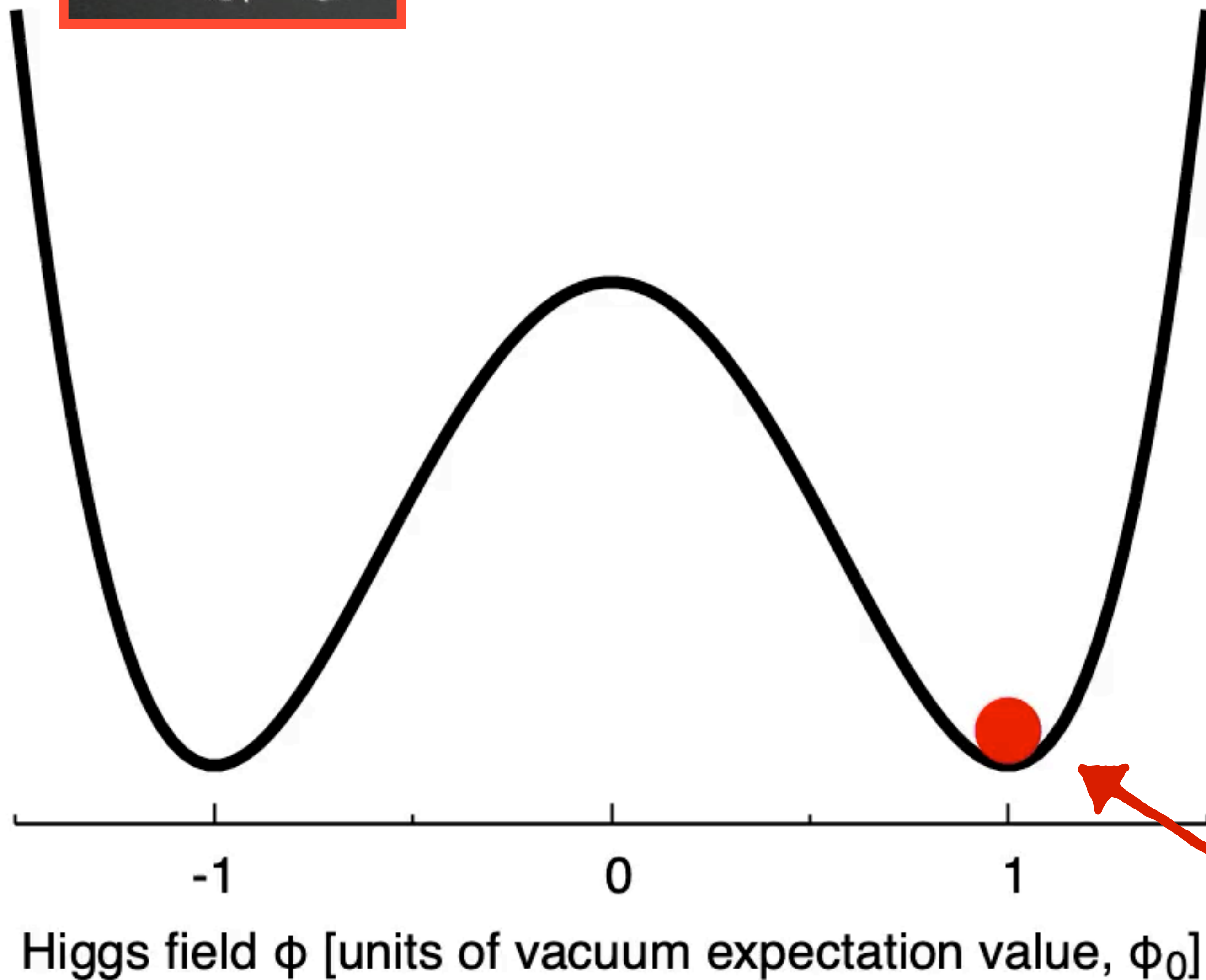
$$\phi = \phi_0 = \frac{\mu}{\sqrt{2\lambda}}$$



Higgs field  $\phi$  [units of vacuum expectation value,  $\phi_0$ ]

$$V(\phi)$$

$$= -\mu^2\phi^2 + \lambda\phi^4$$



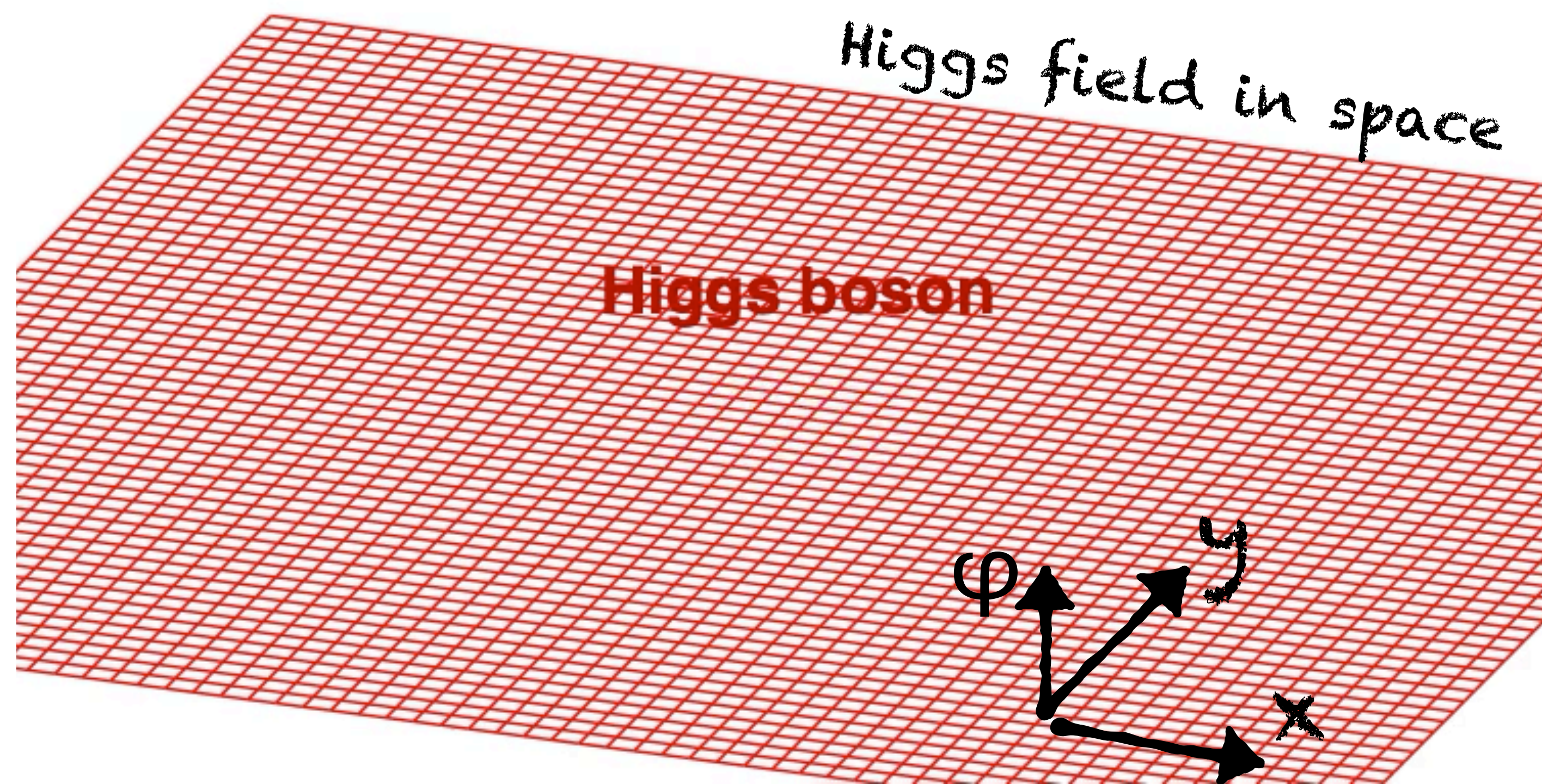
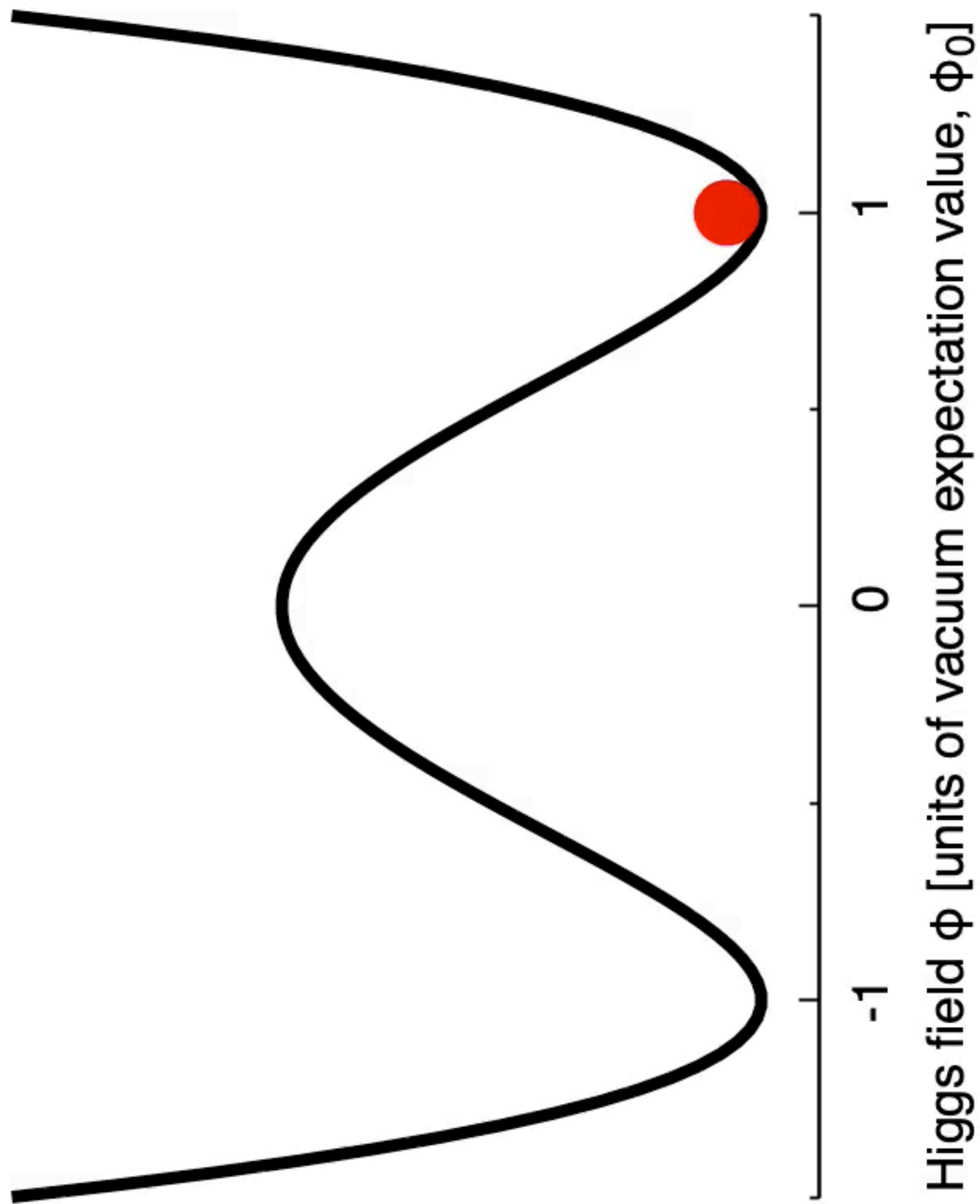
- ▶  $\phi$  is a field at every point in space (plot shows potential vs. 1 of 4 components, at 1 point in space)

- ▶ Our universe sits at minimum of  $V(\phi)$ , at

$$\phi = \phi_0 = \frac{\mu}{\sqrt{2\lambda}}$$

- ▶ Excitation of the  $\phi$  field around  $\phi_0$  is a Higgs boson ( $\phi = \phi_0 + H$ )

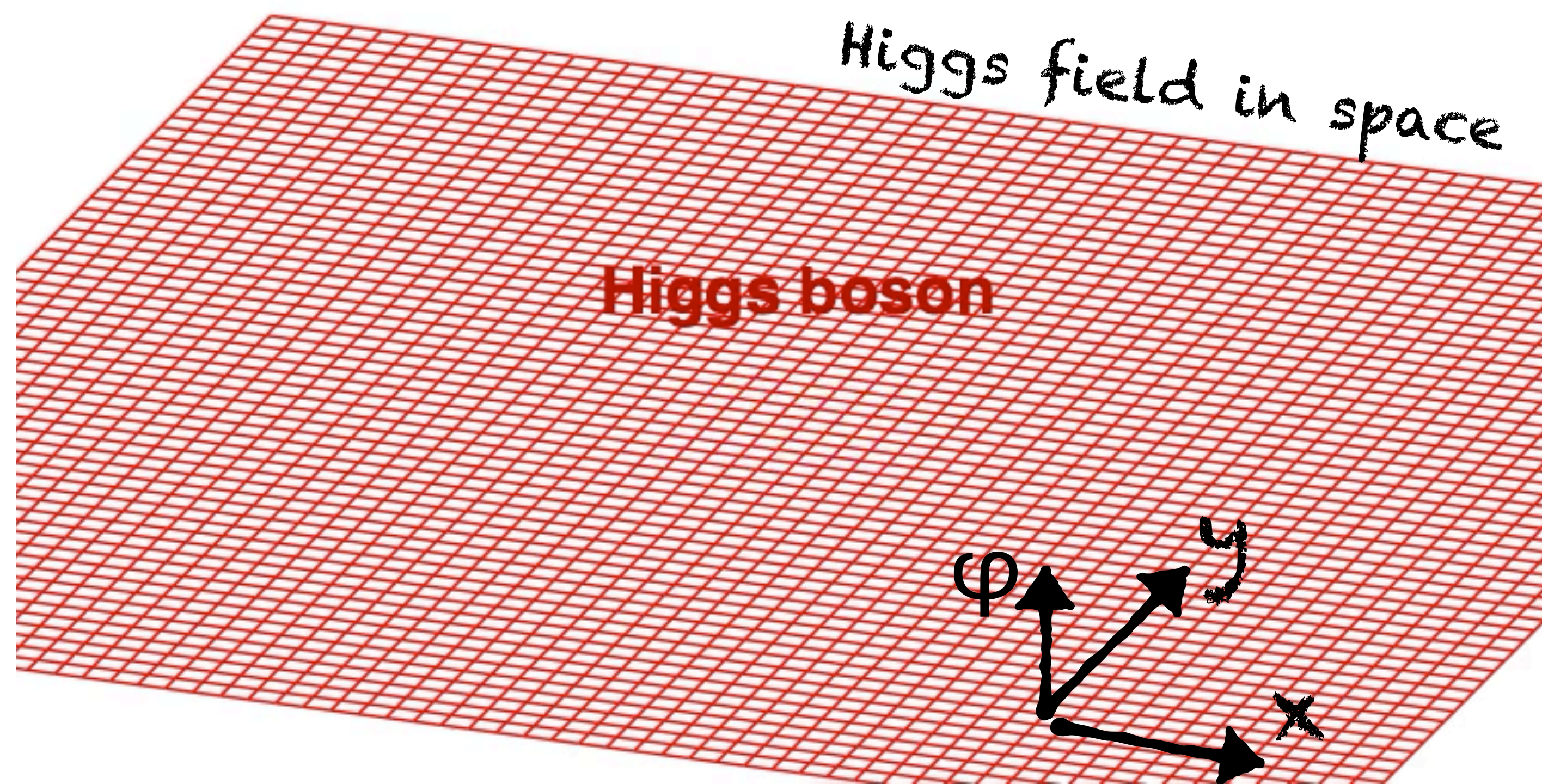
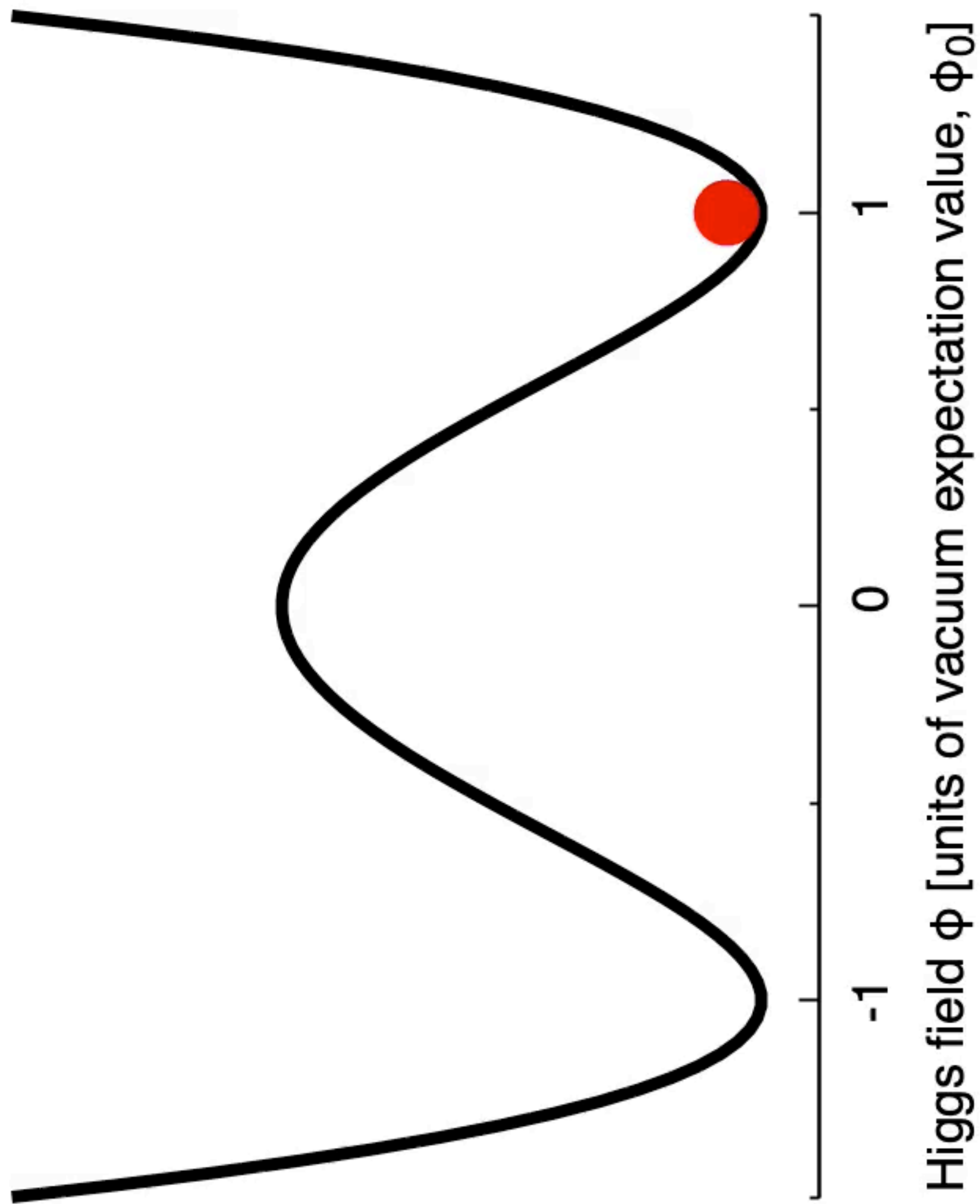
$$\varphi = \varphi_0 + H$$



Higgs field can be different at each point in space

A Higgs boson at a given point in space is a localised fluctuation of the field

$$\varphi = \varphi_0 + H$$



Higgs field can be different at each point in space

A Higgs boson at a given point in space is a localised fluctuation of the field


$$\varphi = \varphi_0 + H$$

**established**  
**(2012 Higgs boson discovery)**



$$\varphi = \varphi_0 + H$$

**established**  
**(2012 Higgs boson discovery)**


$$V(\phi) = -\mu^2\phi^2 + \lambda\phi^4$$

**hypothesis**

# what terms are there in the Higgs sector?

## 2. Gauge-Higgs term

$$\mathcal{L} = -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} + i\bar{\psi}\not{D}\psi + \chi_i y_{ij} \chi_j \phi + \text{h.c.} + |D_\mu \phi|^2 - V(\phi)$$

This equation neatly sums up our current understanding of fundamental particles and forces.


$$|D_\mu \phi|^2$$

$$\begin{array}{ccc} \begin{array}{c} \text{constants} \\ \underbrace{\hspace{2cm}} \end{array} & \begin{array}{c} \text{fields} \\ \underbrace{\hspace{2cm}} \end{array} & \\ \rightarrow & g^2 \phi_0^2 Z_\mu Z^\mu & + \\ & \text{Z-boson} & \\ & \text{mass term} & \\ & & + \\ & \begin{array}{c} \text{constants} \\ \underbrace{\hspace{2cm}} \end{array} & \begin{array}{c} \text{fields} \\ \underbrace{\hspace{2cm}} \end{array} & \\ & 2g^2 \phi_0 H Z_\mu Z^\mu & + \dots & \\ & \text{HZZ interaction} & \\ & \text{term} & \end{array}$$

$$[\phi^2 = (\phi_0 + H)^2 = \phi_0^2 + 2\phi_0 H + \dots]$$

# what terms are there in the Higgs sector?

## 2. Gauge-Higgs term

$$\mathcal{L} = -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} + i\bar{\psi}\not{D}\psi + \chi_i y_{ij} \chi_j \phi + h.c. + |D_\mu \phi|^2 - V(\phi)$$

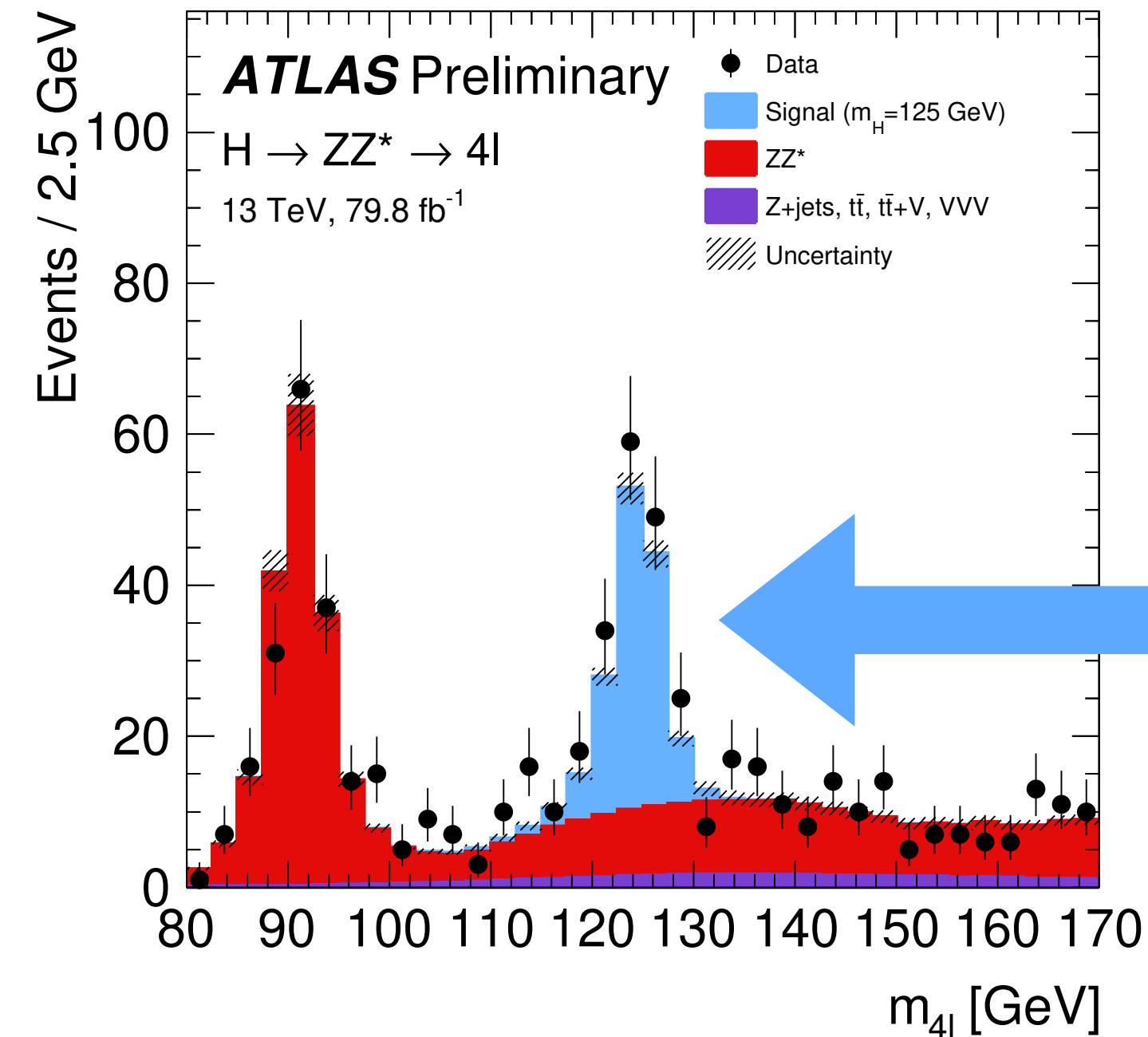
This equation neatly sums up our current understanding of fundamental particles and forces.

$$|D_\mu \phi|^2$$

$$\rightarrow g^2 \phi_0^2 Z_\mu Z^\mu + 2g^2 \phi_0 H Z_\mu Z^\mu + \dots$$

*Z-boson mass term*

*ZZH interaction term*



Higgs mechanism predicts specific relation between Z-boson mass and HZZ interaction

what terms are there in the Higgs sector?

## 2. Gauge-Higgs term

$$\mathcal{L} = -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} + i\bar{\psi}\not{D}\psi + \bar{\psi}_i y_{ij} \psi_j \phi + h.c. + |D_\mu \phi|^2 - V(\phi)$$

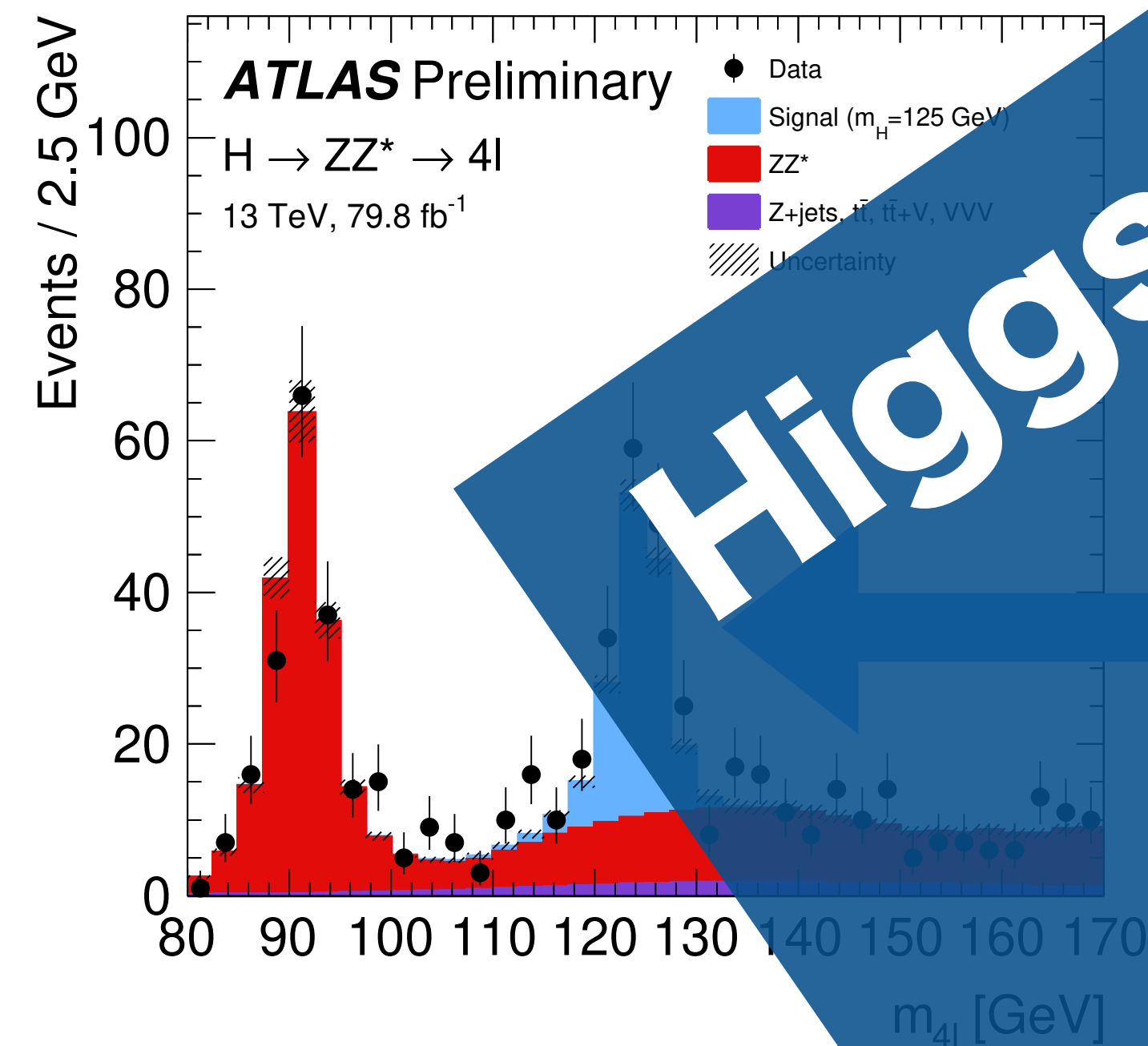
This equation neatly sums up our current understanding of fundamental particles and forces.

$$|D_\mu \phi|^2$$

$$\rightarrow g^2 \phi_0^2 Z_\mu Z^\mu + \dots$$

Higgs (BEH) mechanism for vector boson mass = 2013 Nobel prize

Higgs mechanism predicts specific relation between Z-boson mass and HZZ interaction



# what terms are there in the Higgs sector?

## 3. Fermion-Higgs (Yukawa) term

$$\mathcal{L} = -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} + i\bar{\psi}\not{D}\psi + \bar{\psi}_i y_{ij} \psi_j \phi + \text{h.c.} + |D_\mu \phi|^2 - V(\phi)$$

This equation neatly sums up our current understanding of fundamental particles and forces.

$$\bar{\psi}_i y_{ij} \psi_j \phi$$

$$\rightarrow y_{ij} \phi_0 \psi_i \psi_j + y_{ij} H \psi_i \psi_j$$

*fermion mass term*  
 $m_i = y_{ii} \phi_0$

*Higgs-fermion-fermion interaction term;*  
*coupling  $\sim y_{ii}$*

$i$	$y_i$	$i$	$y_i$
u	$2 \cdot 10^{-5}$	d	$3 \cdot 10^{-5}$
c	$8 \cdot 10^{-3}$	s	$6 \cdot 10^{-4}$
b	$3 \cdot 10^{-2}$	t	1
$\nu_e$	$\sim 10^{-13}$ ?	e	$3 \cdot 10^{-6}$
$\nu_\mu$		$\mu$	$6 \cdot 10^{-4}$
$\nu_\tau$		$\tau$	$1 \cdot 10^{-4}$

$$\phi = \phi_0 + H$$

what terms are there in the Higgs sector?

### 3. Fermion-Higgs (Yukawa) term

$$\mathcal{L} = -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} + i\bar{\psi}\not{D}\psi + \bar{\psi}_i y_{ij} \psi_j \phi + h.c. + |D_\mu \phi|^2 - V(\phi)$$

This equation neatly sums up our current understanding of fundamental particles and forces.

$$\bar{\psi}_i y_{ij} \psi_j \phi$$

→

$$y_{ij} H \psi_i \psi_j$$

Higgs-fermion-fermion interaction term; coupling  $\sim y_{ii}$

$i$	$y_i$	$i$	$y_i$
u	$2 \cdot 10^{-5}$	d	$3 \cdot 10^{-5}$
c	$8 \cdot 10^{-3}$	s	$6 \cdot 10^{-4}$
b	$3 \cdot 10^{-2}$	t	1
$\nu_e$	$\sim 10^{-13}$ ?	e	$3 \cdot 10^{-6}$
$\nu_\mu$		$\mu$	$6 \cdot 10^{-4}$
$\nu_\tau$		$\tau$	$1 \cdot 10^{-4}$

$$m_i = y_{ii} \phi_0$$

the subject of the next few slides

$$\phi = \phi_0 + H$$

# Yukawa interaction hypothesis

---

*Yukawa couplings  $\sim$  fermion mass*

**first fundamental interaction that we probe at the quantum level where interaction strength ( $y_{ij}$ ) not quantised**  
*(i.e. no underlying unit of conserved charge across particles)*

# Why do Yukawa couplings matter?

(1) Because, within SM **conjecture**, they're what give masses to all **quarks**

$$\mathcal{L} = -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} + i\bar{\psi}\not{D}\psi + \bar{\psi}_i y_{ij} \psi_j \phi + h.c. + |D_\mu\phi|^2 - V(\phi)$$

This equation neatly sums up our current understanding of fundamental particles and forces.

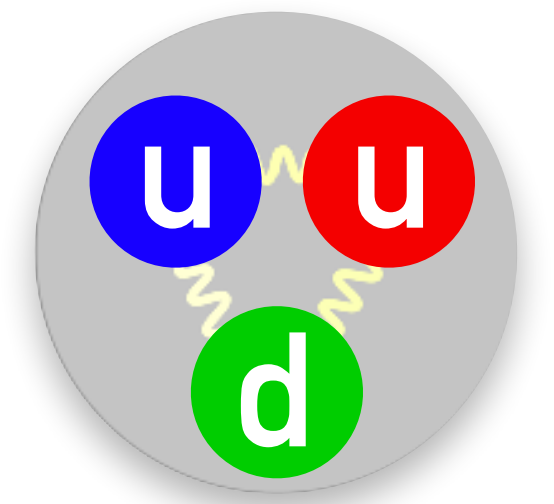
Up quarks (mass  $\sim 2.2$  MeV) are lighter than down quarks (mass  $\sim 4.7$  MeV)

**proton** (up+up+down):  $2.2 + 2.2 + 4.7 + \dots = 938.3$  MeV  
**neutron** (up+down+down):  $2.2 + 4.7 + 4.7 + \dots = 939.6$  MeV

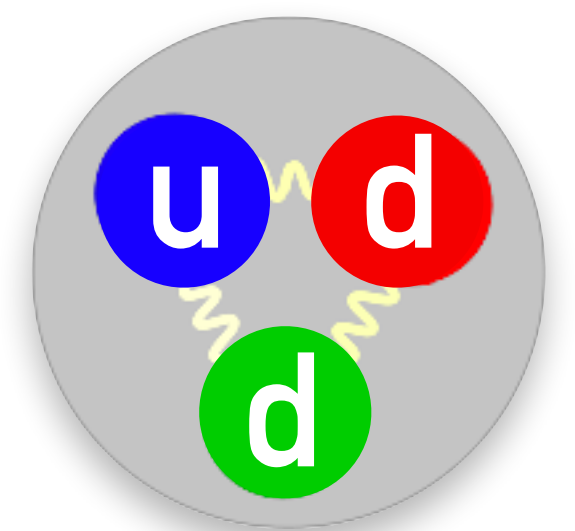
So protons are **lighter** than neutrons,  
 $\rightarrow$  protons are stable.

Which gives us the hydrogen atom,  
& chemistry and biology as we know it

*proton*  
mass = 938.3 MeV



*neutron*  
mass = 939.6 MeV





# Why do Yukawa couplings matter?

(2) Because, within SM **conjecture**, they're what give masses to all **leptons**

$$\begin{aligned} \mathcal{L} = & -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} \\ & + i\bar{\psi}\not{D}\psi \\ & + \bar{\psi}_i y_{ij} \psi_j \phi + h.c. \\ & + |D_\mu\phi|^2 - V(\phi) \end{aligned}$$

This equation neatly sums up our current understanding of fundamental particles and forces.

**Bohr radius**

$$a_0 = \frac{4\pi\epsilon_0\hbar^2}{m_e e^2} = \frac{\hbar}{m_e c \alpha} \propto \frac{1}{y_e}$$

electron mass determines size of all atoms

it sets energy levels of all chemical reactions

mass →

charge →

spin →

**QUARKS**

$\approx 2.3 \text{ MeV}/c^2$	$\approx 1.275 \text{ GeV}/c^2$	$\approx 173.07 \text{ GeV}/c^2$
$2/3$	$2/3$	$2/3$
$1/2$	$1/2$	$1/2$
<b>u</b> up	<b>c</b> charm	<b>t</b> top
$\approx 4.8 \text{ MeV}/c^2$	$\approx 95 \text{ MeV}/c^2$	$\approx 4.18 \text{ GeV}/c^2$
$-1/3$	$-1/3$	$-1/3$
$1/2$	$1/2$	$1/2$
<b>d</b> down	<b>s</b> strange	<b>b</b> bottom
$0.511 \text{ MeV}/c^2$	$105.7 \text{ MeV}/c^2$	$1.777 \text{ GeV}/c^2$
$-1$	$-1$	$-1$
$1/2$	$1/2$	$1/2$
<b>e</b> electron	<b><math>\mu</math></b> muon	<b><math>\tau</math></b> tau

	mass	$\approx 2.3 \text{ MeV}/c^2$	$\approx 1.275 \text{ GeV}/c^2$	$\approx 173.07 \text{ GeV}/c^2$
charge	$2/3$	$2/3$	$2/3$	$2/3$
spin	$1/2$	$1/2$	$1/2$	$1/2$
		<b>u</b> up	<b>c</b> charm	<b>t</b> top
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		<b>d</b> down	<b>s</b> strange	<b>b</b> bottom
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	$-1$	$-1$	$-1$	$-1$
	$1/2$	$1/2$	$1/2$	$1/2$
		<b>e</b> electron	<b><math>\mu</math></b> muon	<b><math>\tau</math></b> tau

**QUARKS**

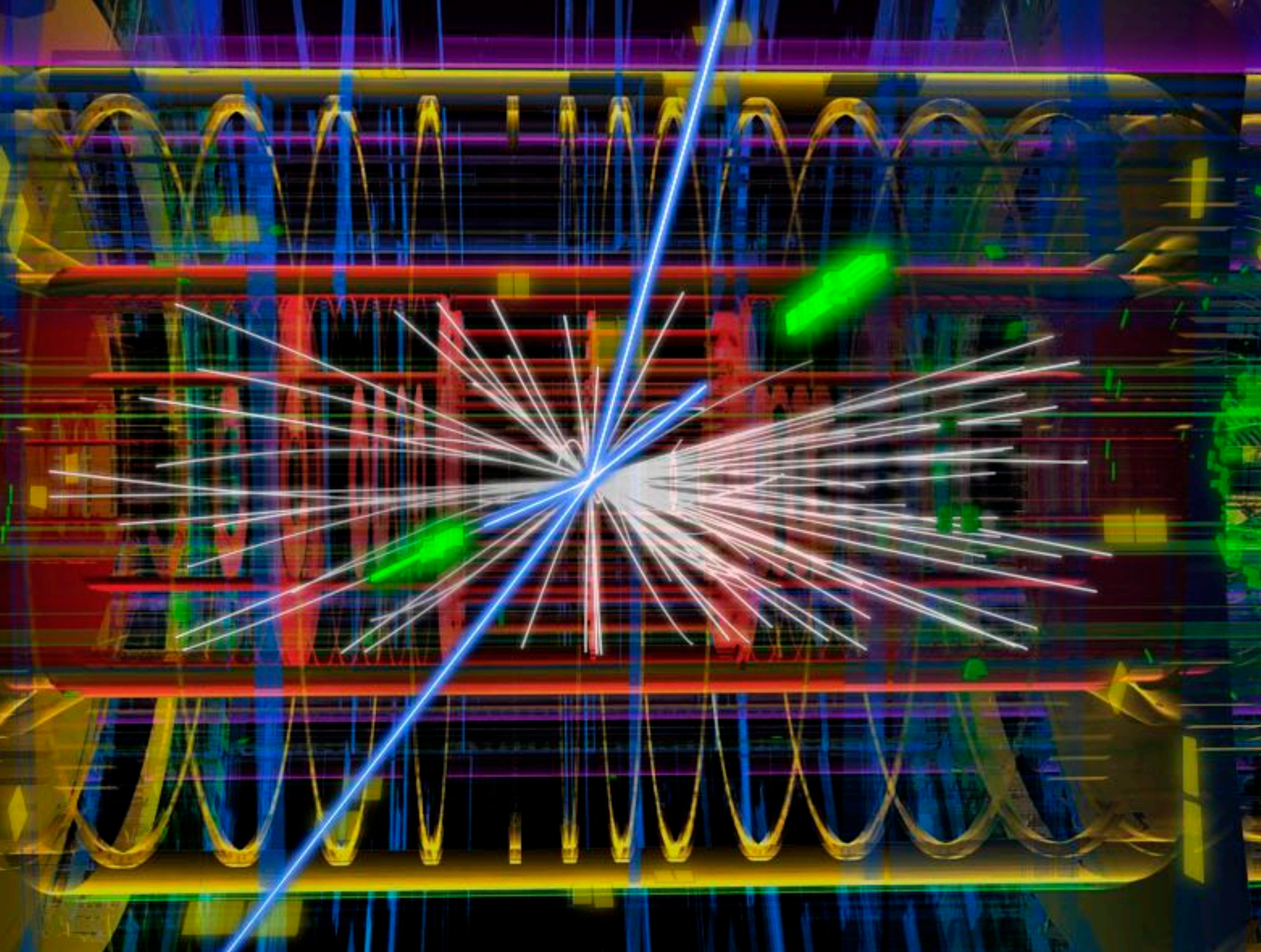
1st generation (us) has low mass because of weak interactions with Higgs field (and so with Higgs bosons):  
**too weak to test today**

	1st generation	2nd generation	3rd generation
mass	$\approx 2.3 \text{ MeV}/c^2$	$\approx 1.275 \text{ GeV}/c^2$	$\approx 173.07 \text{ GeV}/c^2$
charge	$2/3$	$2/3$	$2/3$
spin	$1/2$	$1/2$	$1/2$
	<b>u</b> up	<b>c</b> charm	<b>t</b> top
	$\approx 4.8 \text{ MeV}/c^2$	$\approx 95 \text{ MeV}/c^2$	$\approx 4.18 \text{ GeV}/c^2$
	$-1/3$	$-1/3$	$-1/3$
	$1/2$	$1/2$	$1/2$
	<b>d</b> down	<b>s</b> strange	<b>b</b> bottom
	$0.511 \text{ MeV}/c^2$	$105.7 \text{ MeV}/c^2$	$1.777 \text{ GeV}/c^2$
	$-1$	$-1$	$-1$
	$1/2$	$1/2$	$1/2$
	<b>e</b> electron	<b><math>\mu</math></b> muon	<b><math>\tau</math></b> tau

**QUARKS**

1st generation (us) has low mass because of weak interactions with Higgs field (and so with Higgs bosons):  
**too weak to test today**

3rd generation (us) has high mass because of strong interactions with Higgs field (and so with Higgs bosons):  
**can potentially be tested**



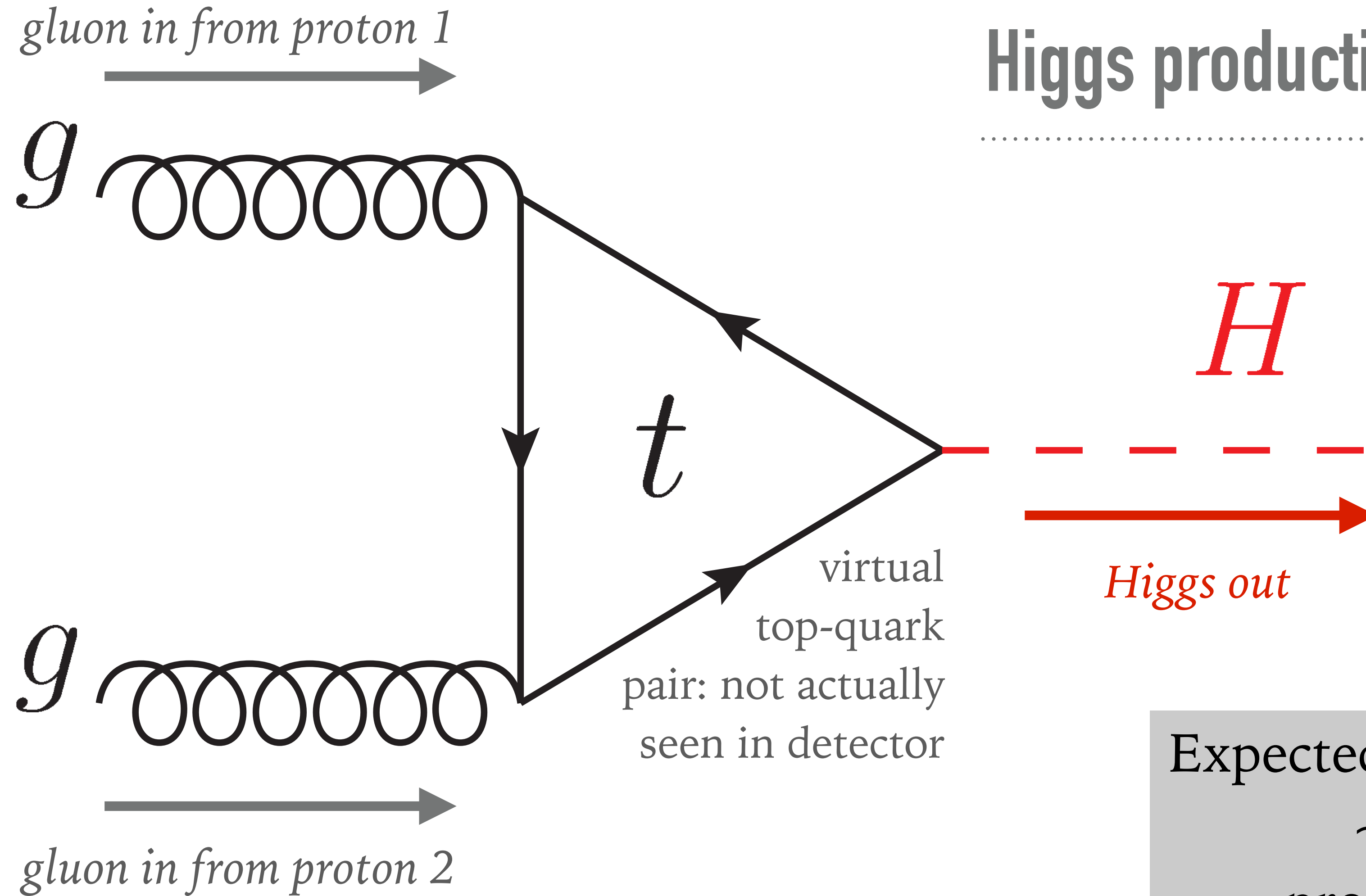
# ATLAS & CMS @LHC

**~ up to 2 billion  
collisions/second**

**(+ lower rates at  
LHCb and ALICE)**

**what underlying processes tell  
us about Yukawa interactions?**

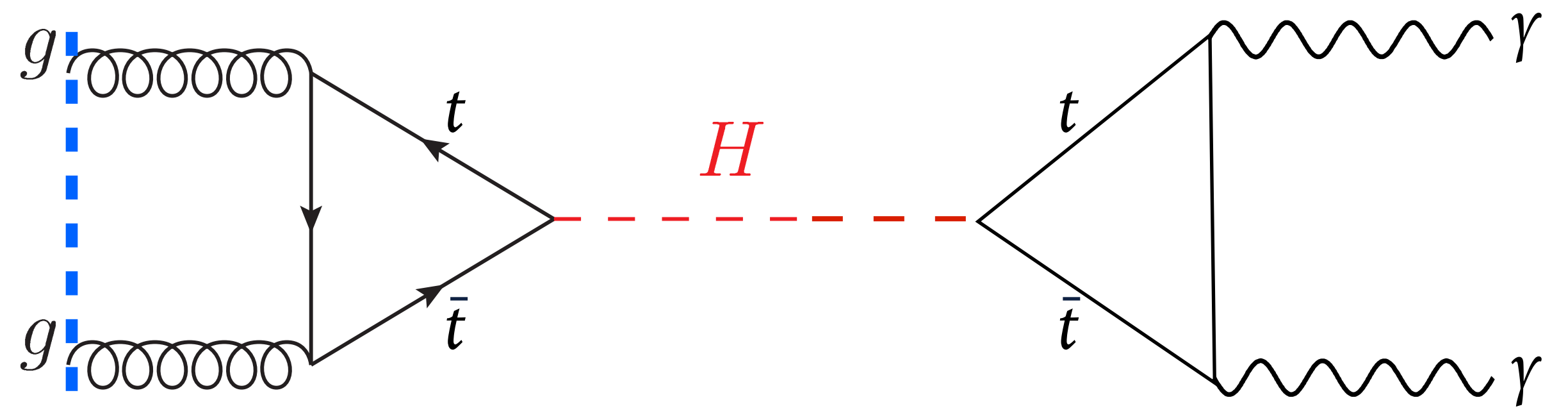
# Higgs production: the dominant channel



Expected to happen once for every  
~2 billion inelastic  
proton-proton collisions

LHC data consistent with that  
already at discovery in 2012

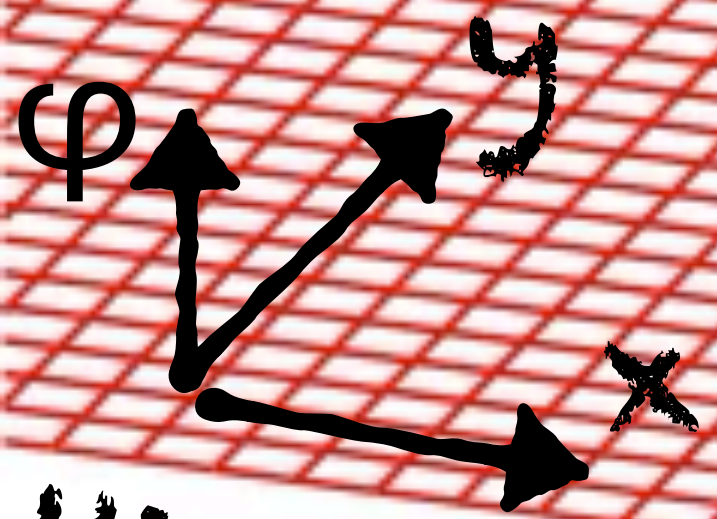
QUARKS	up	charm	top
mass	$\approx 2.3 \text{ MeV}/c^2$	$\approx 1.275 \text{ GeV}/c^2$	$\approx 173.07 \text{ GeV}/c^2$
charge	$2/3$	$2/3$	$2/3$
spin	$1/2$	$1/2$	$1/2$
down	strange	bottom	
mass	$\approx 4.8 \text{ MeV}/c^2$	$\approx 95 \text{ MeV}/c^2$	$\approx 4.18 \text{ GeV}/c^2$
charge	$-1/3$	$-1/3$	$-1/3$
spin	$1/2$	$1/2$	$1/2$
leptons	electron	muon	tau
mass	$0.511 \text{ MeV}/c^2$	$105.7 \text{ MeV}/c^2$	$1.777 \text{ GeV}/c^2$
charge	$-1$	$-1$	$-1$
spin	$1/2$	$1/2$	$1/2$



quon

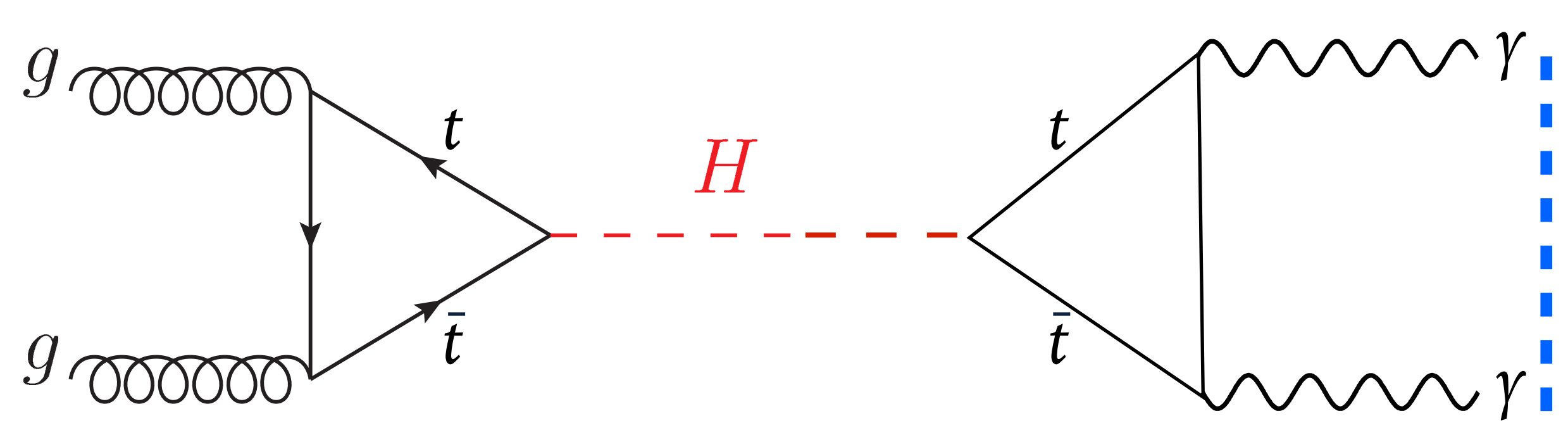


gluon



Higgs field in space

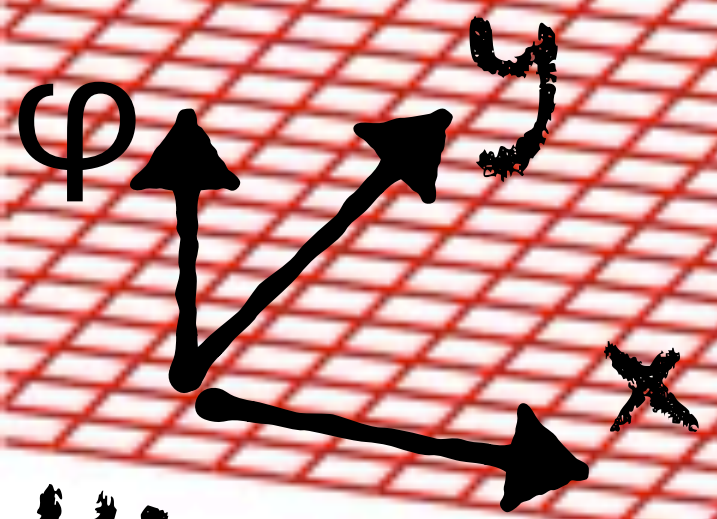




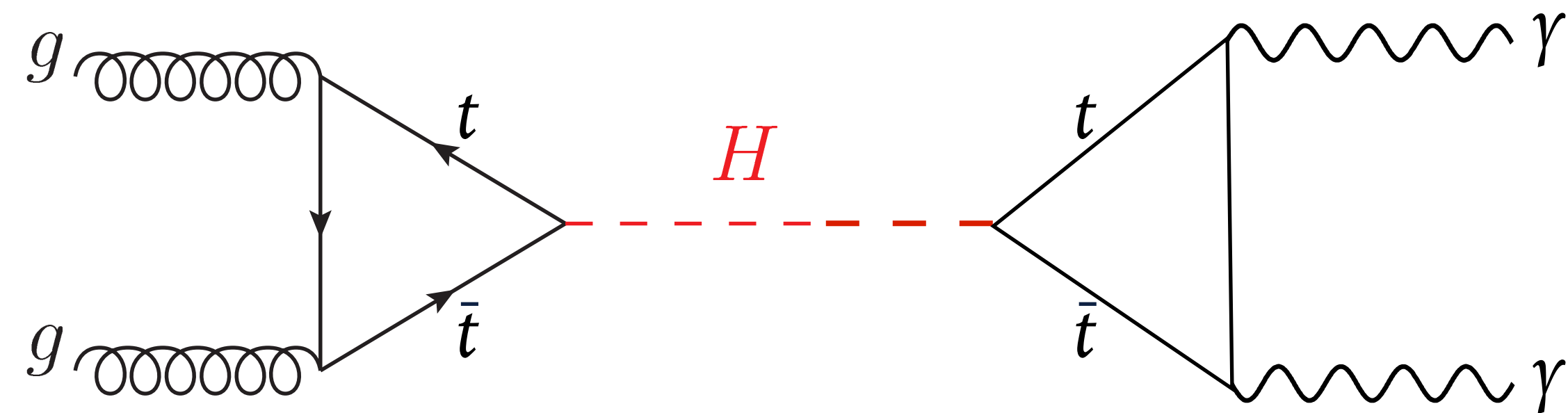
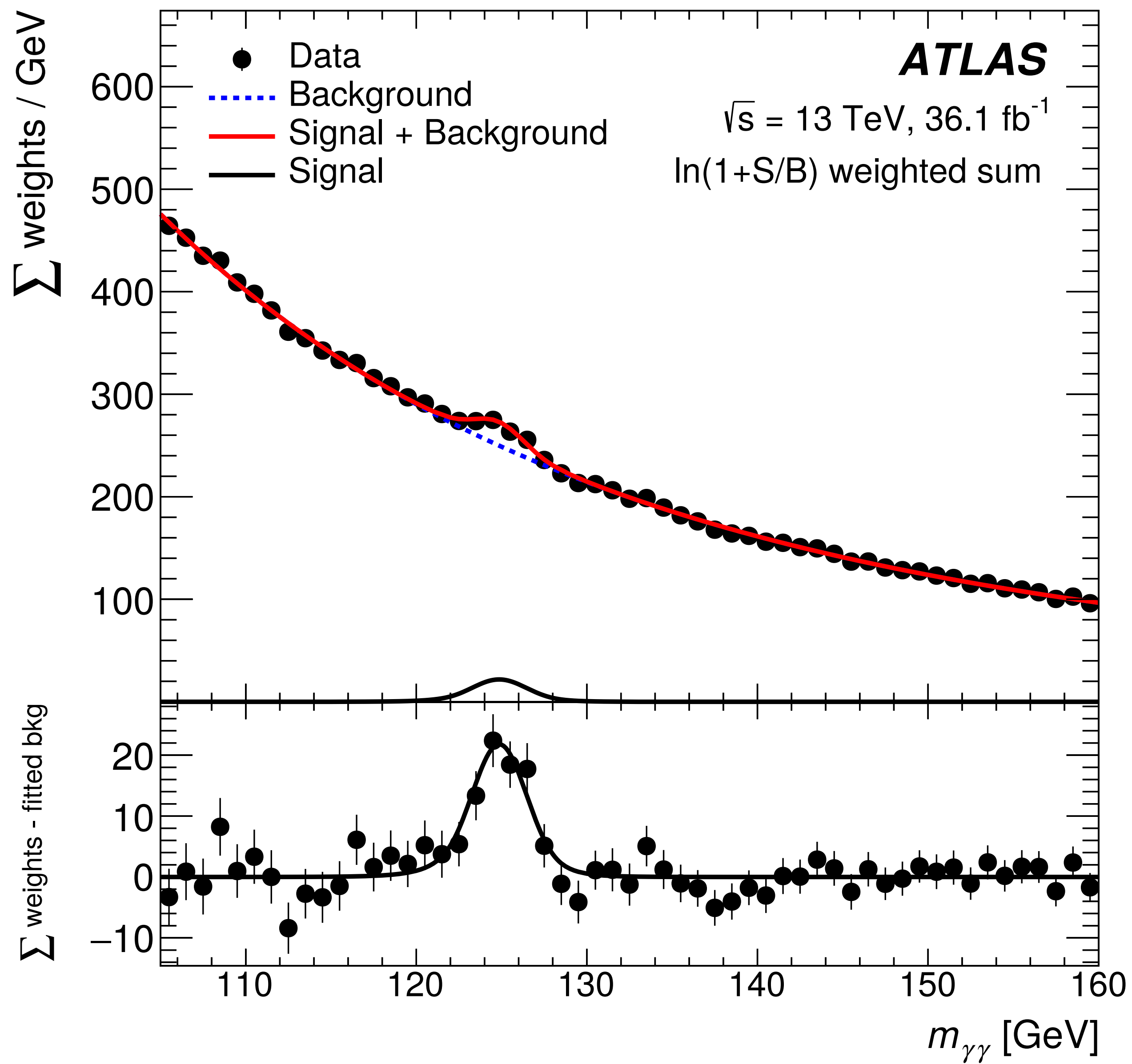
quon

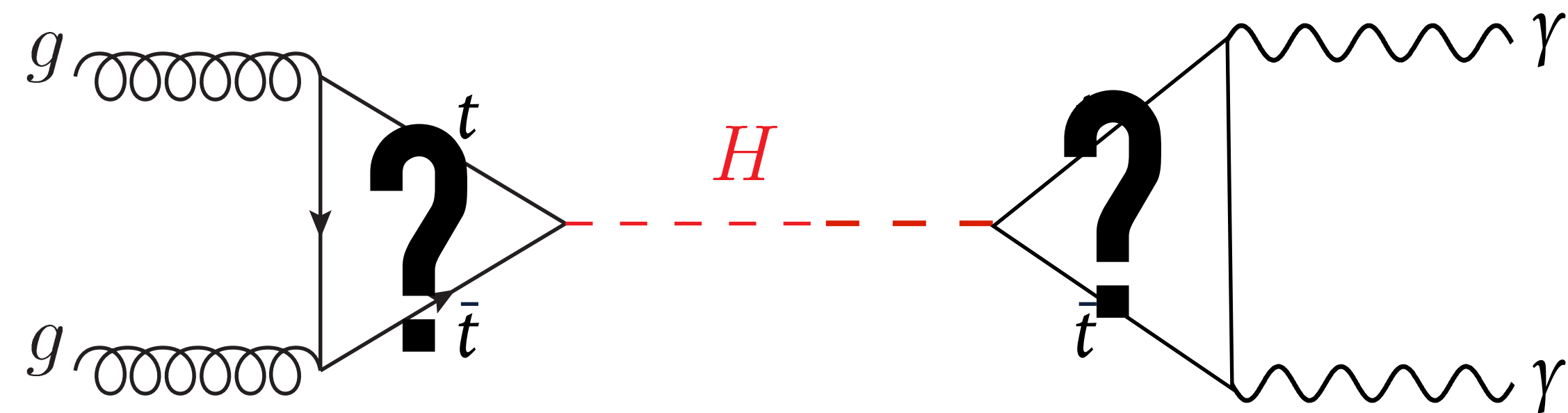
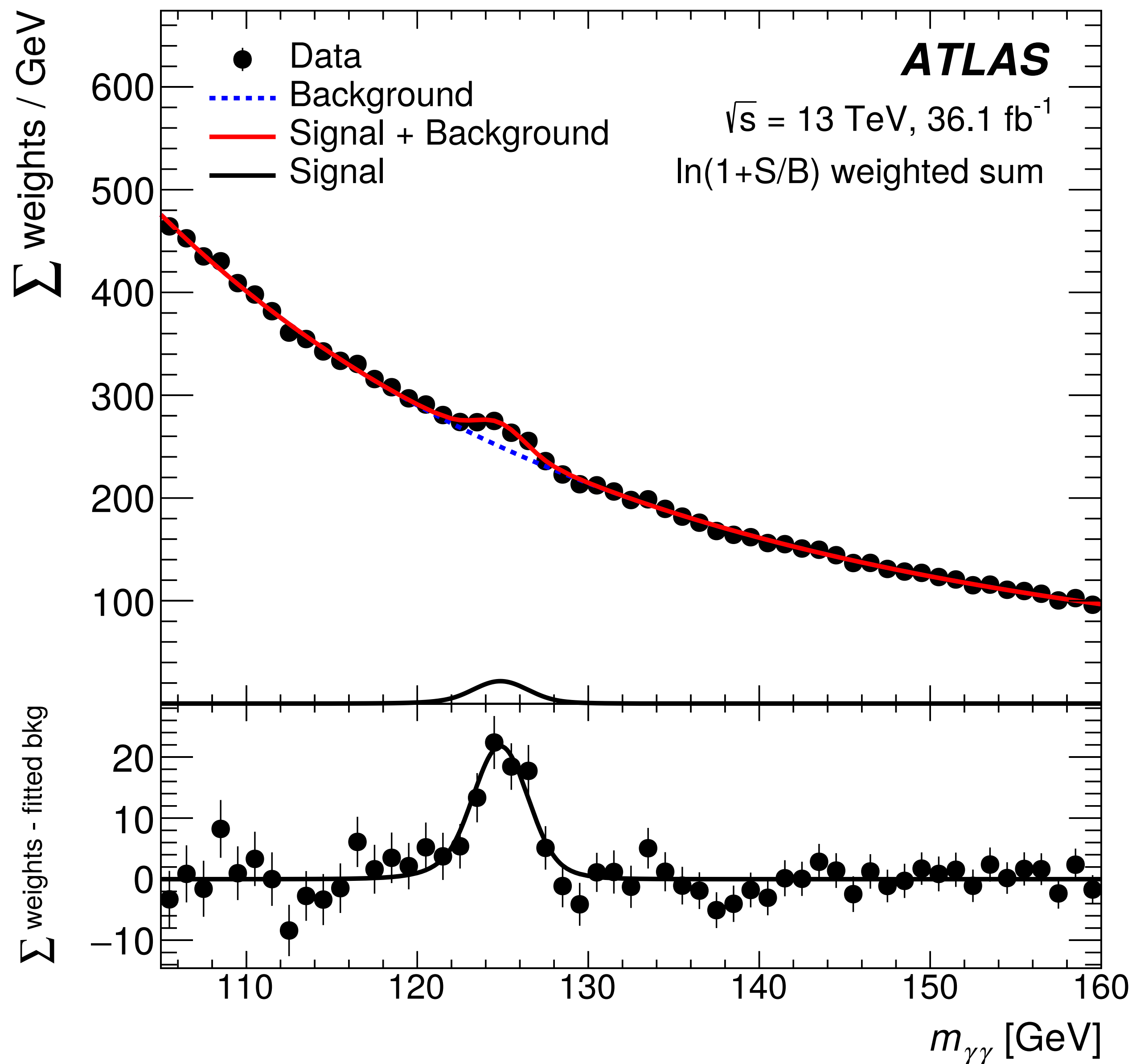


gluon



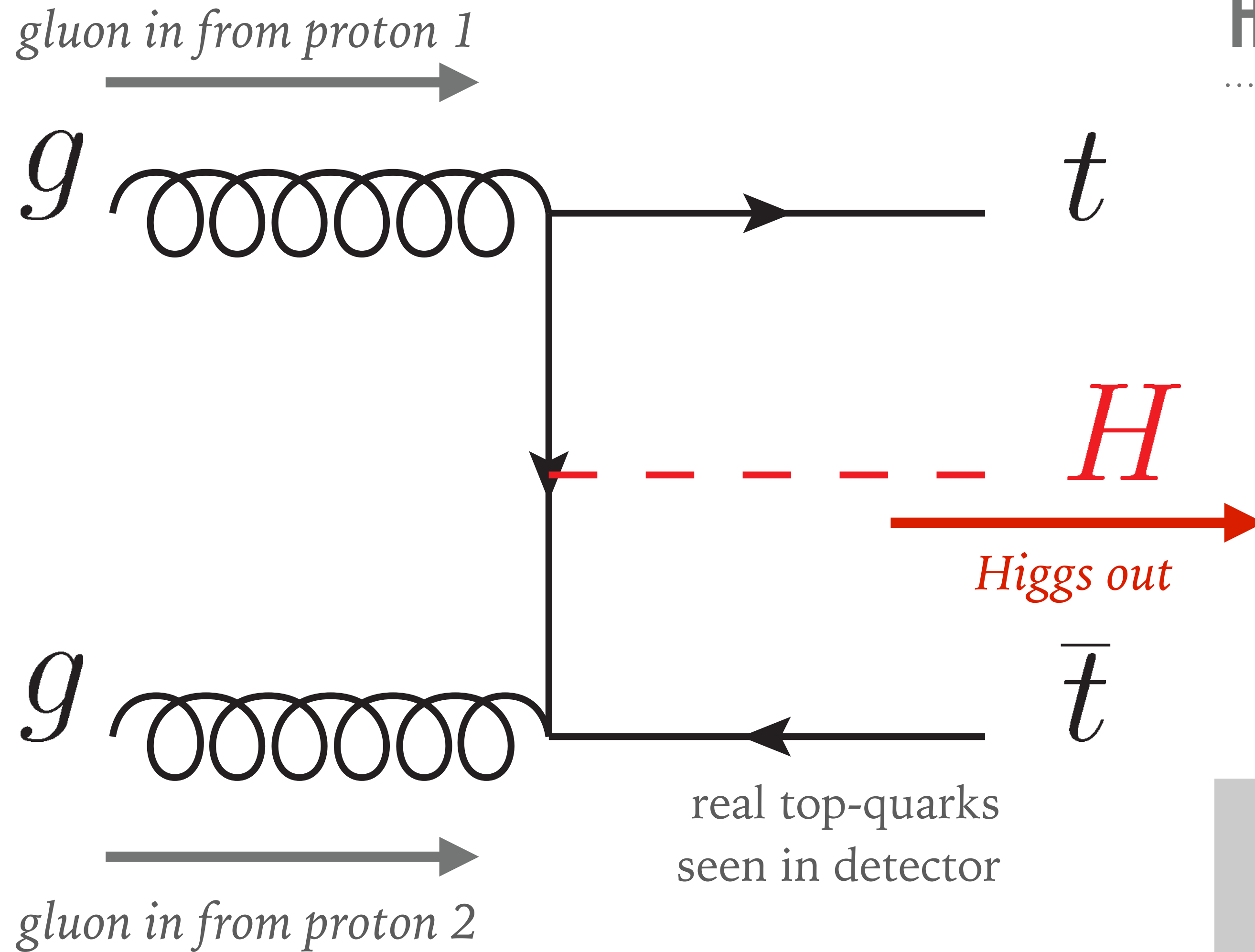
Higgs field in space





**but how can you be sure the Higgs boson is really being radiated off a top-quark, i.e. that you're actually seeing a Yukawa coupling?**

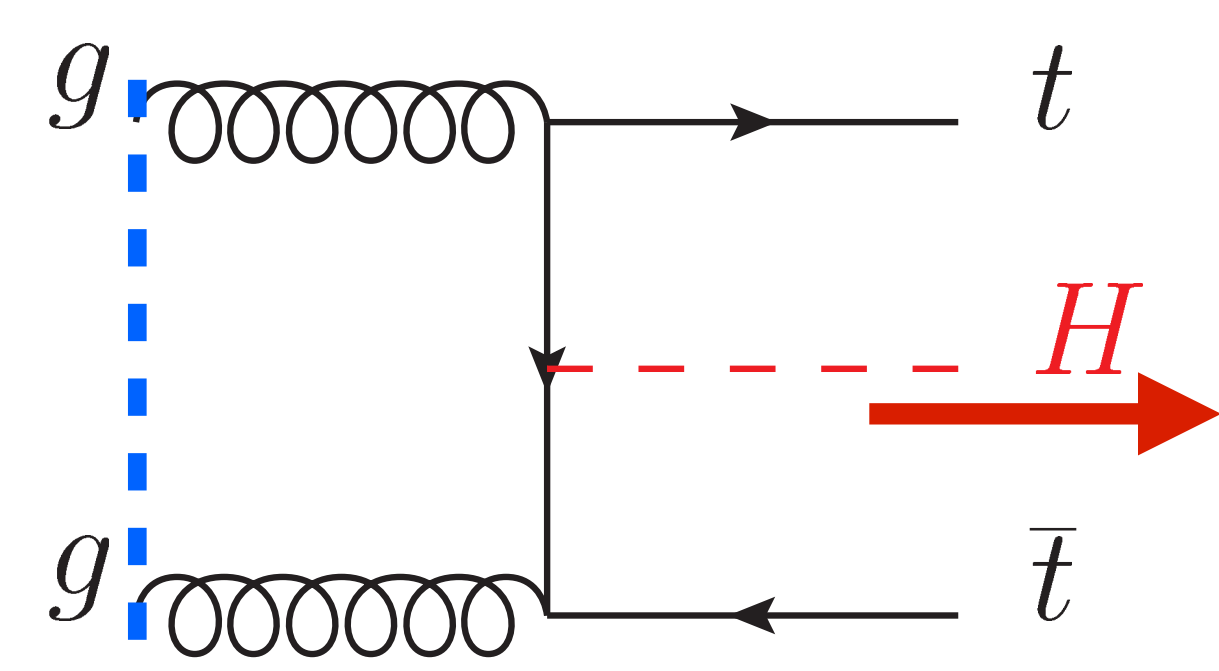
# Higgs production: the ttH channel



If SM top-Yukawa hypothesis is correct, expect 1 Higgs for every 1600 top-quark pairs.

(rather than 1 Higgs for every 2 billion pp collisions)

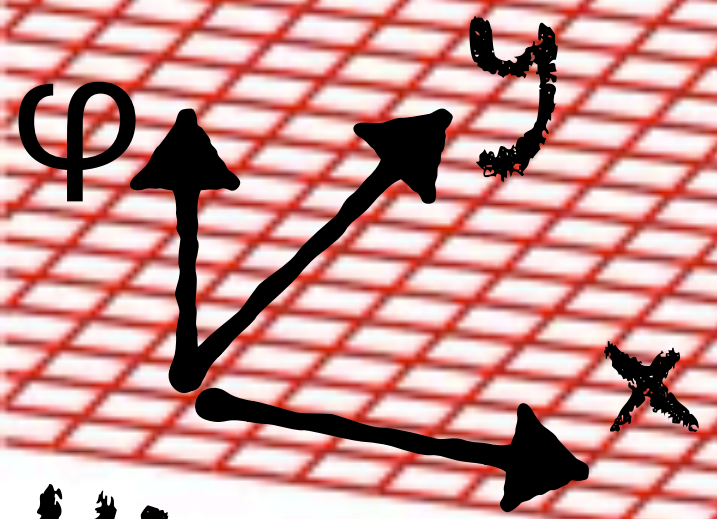
QUARKS		
mass → ≈2.3 MeV/c <sup>2</sup>	≈1.275 GeV/c <sup>2</sup>	≈173.07 GeV/c <sup>2</sup>
charge → 2/3	2/3	2/3
spin → 1/2	1/2	1/2
<b>u</b> up	<b>c</b> charm	<b>t</b> top
4.8 MeV/c <sup>2</sup>	≈95 MeV/c <sup>2</sup>	
-1/3	-1/3	-1/3
1/2	1/2	1/2
<b>d</b> down	<b>s</b> strange	<b>b</b> bottom
0.511 MeV/c <sup>2</sup>	105.7 MeV/c <sup>2</sup>	1.777 GeV/c <sup>2</sup>
-1	-1	-1
1/2	1/2	1/2
<b>e</b> electron	<b>μ</b> muon	<b>τ</b> tau



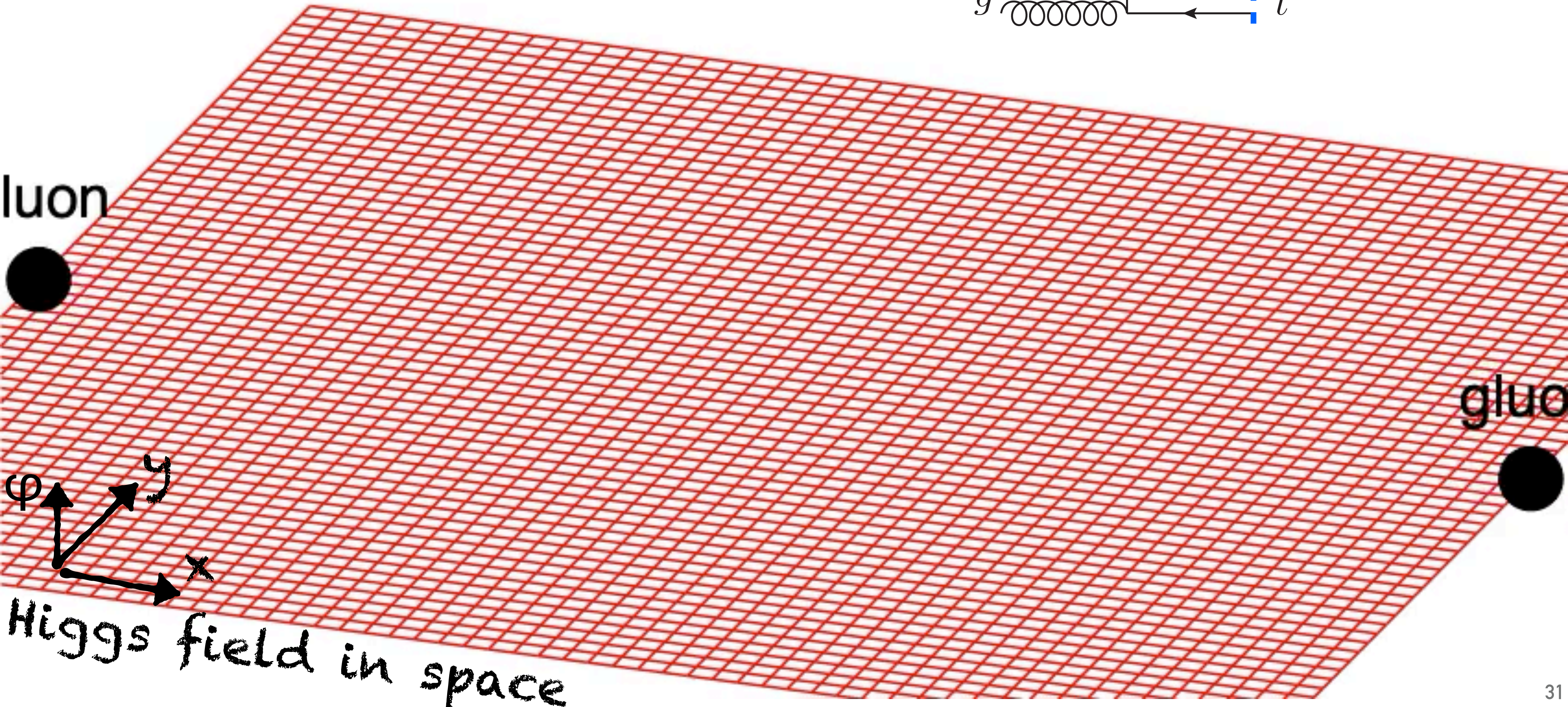
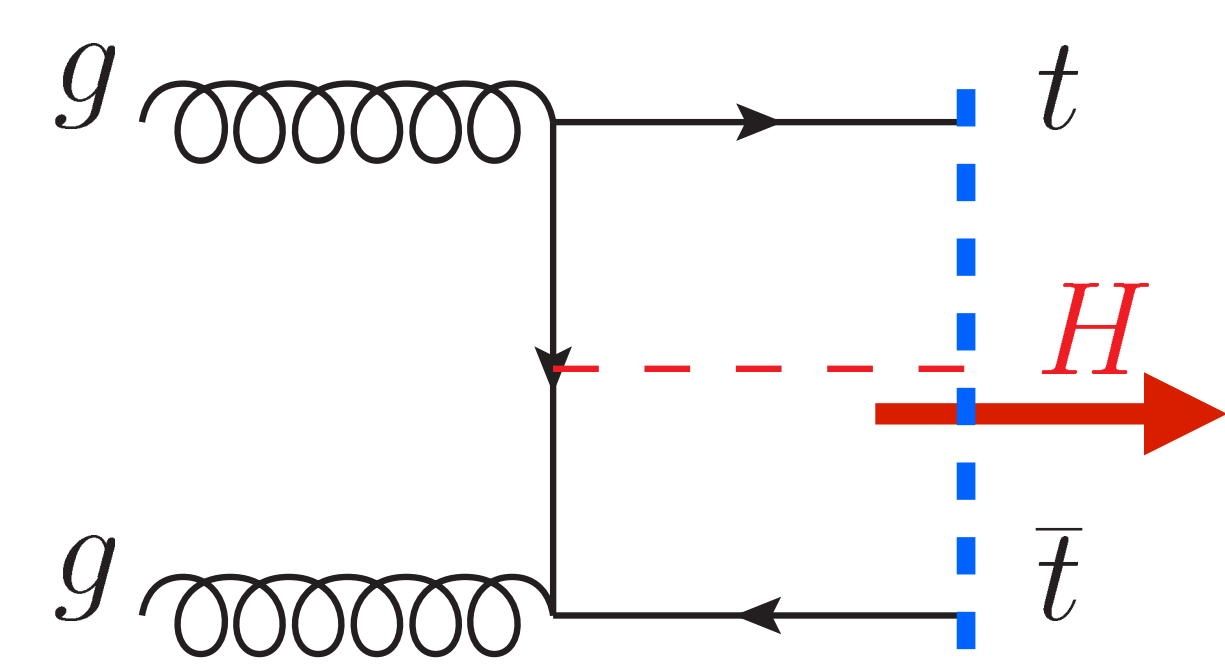
quon

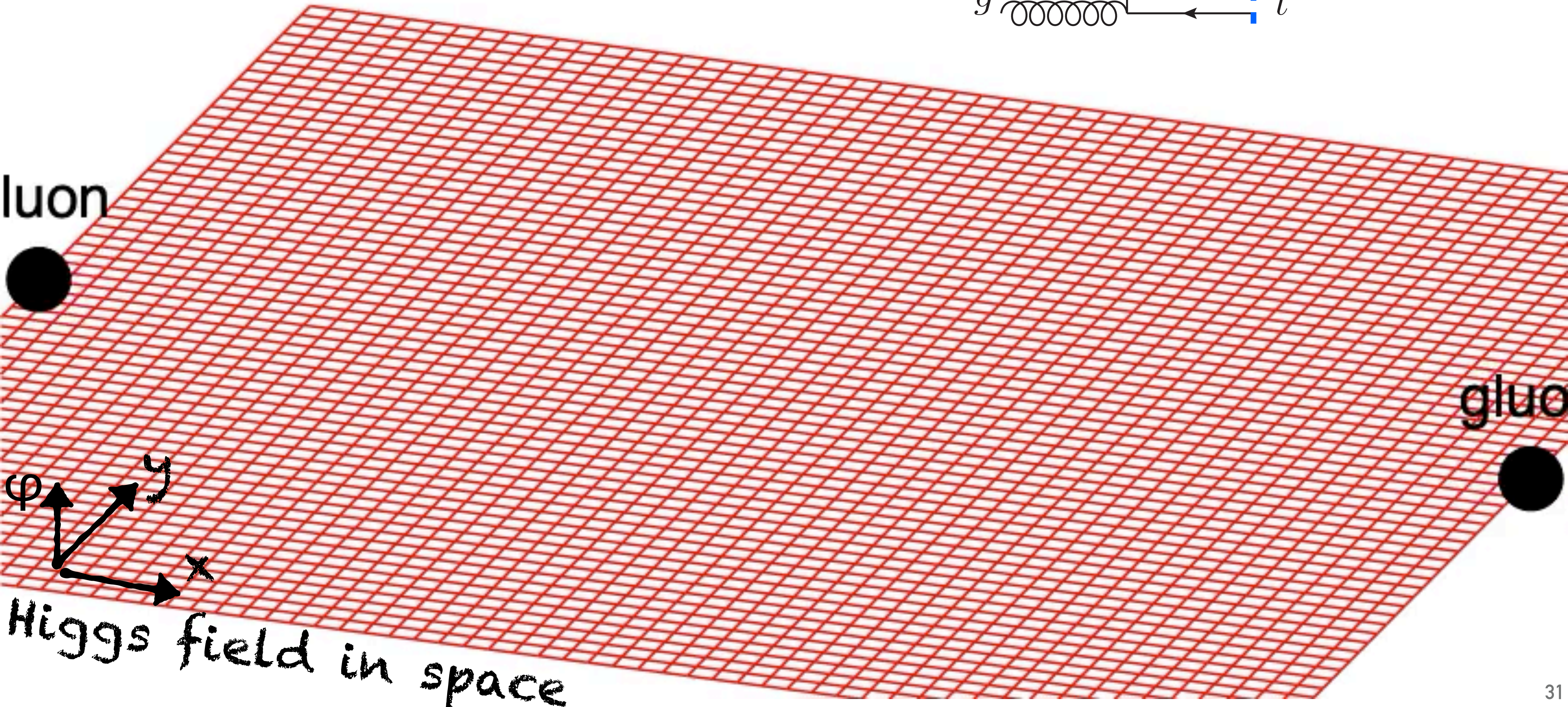
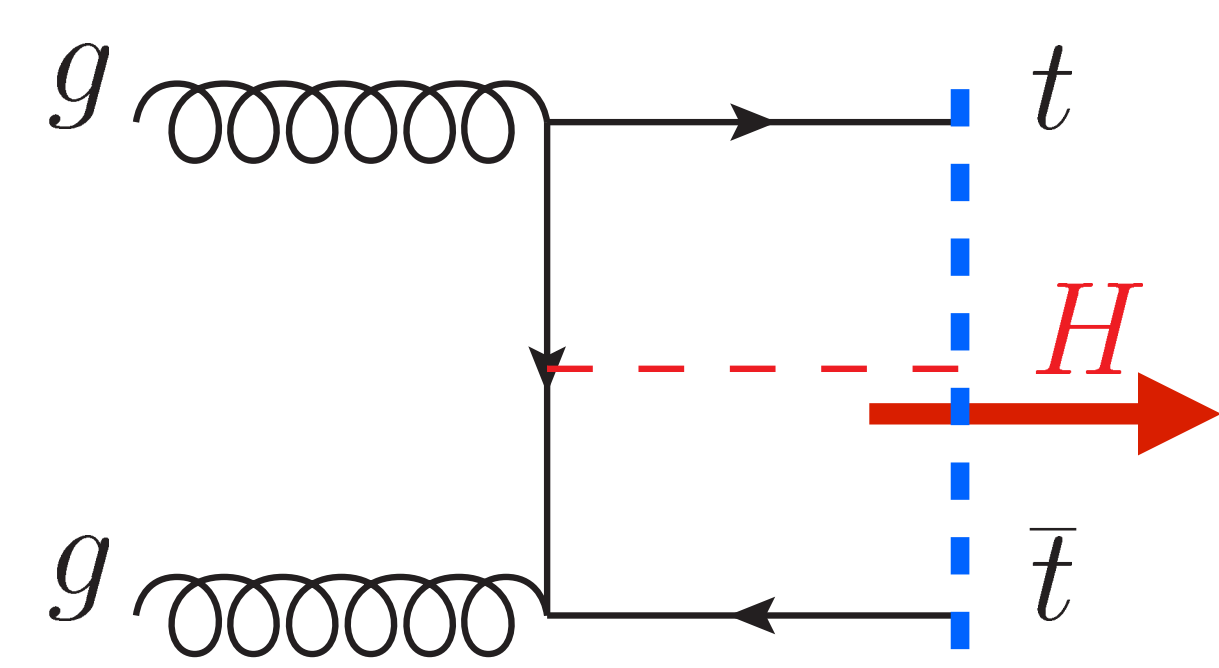


gluon



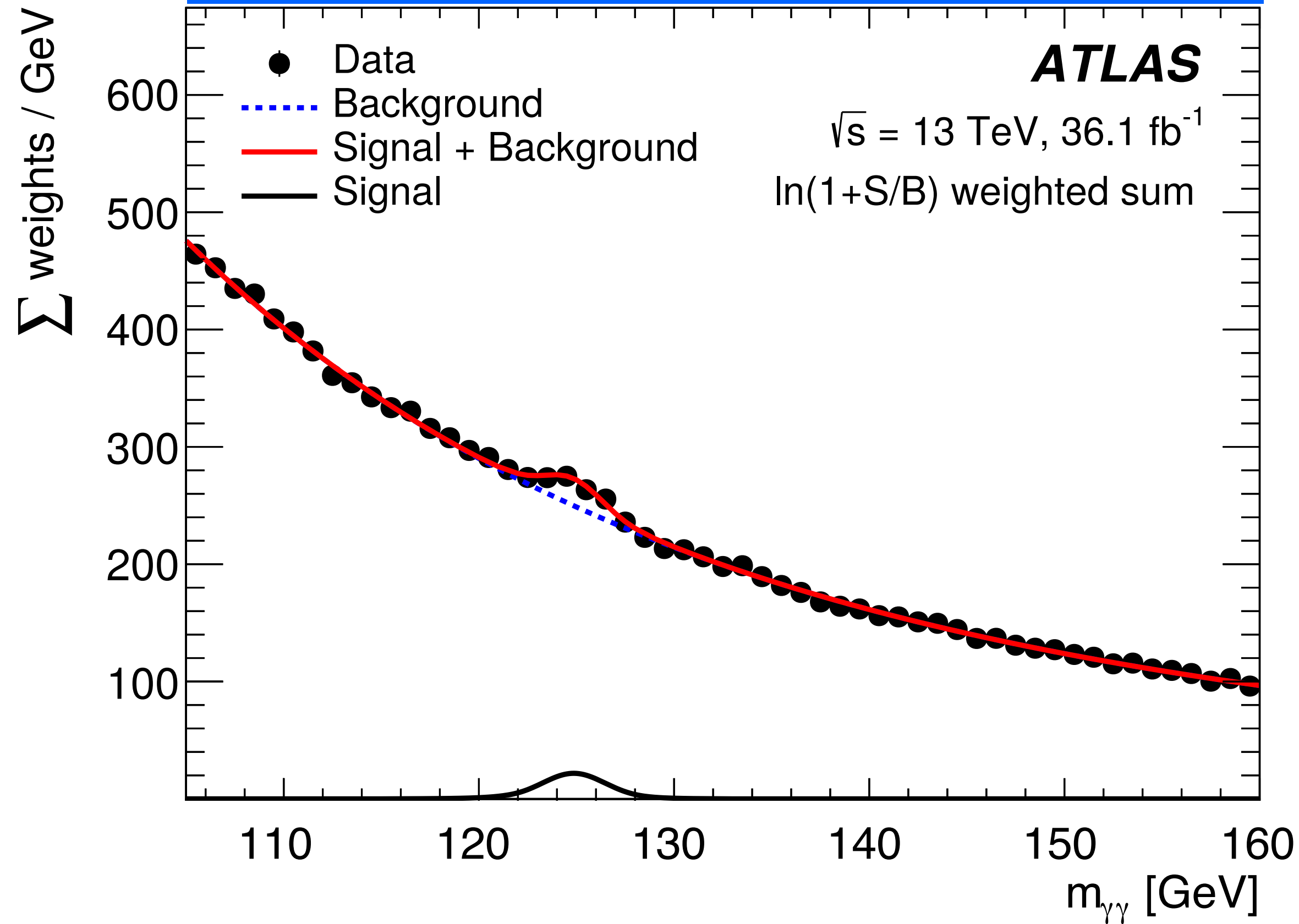
Higgs field in space



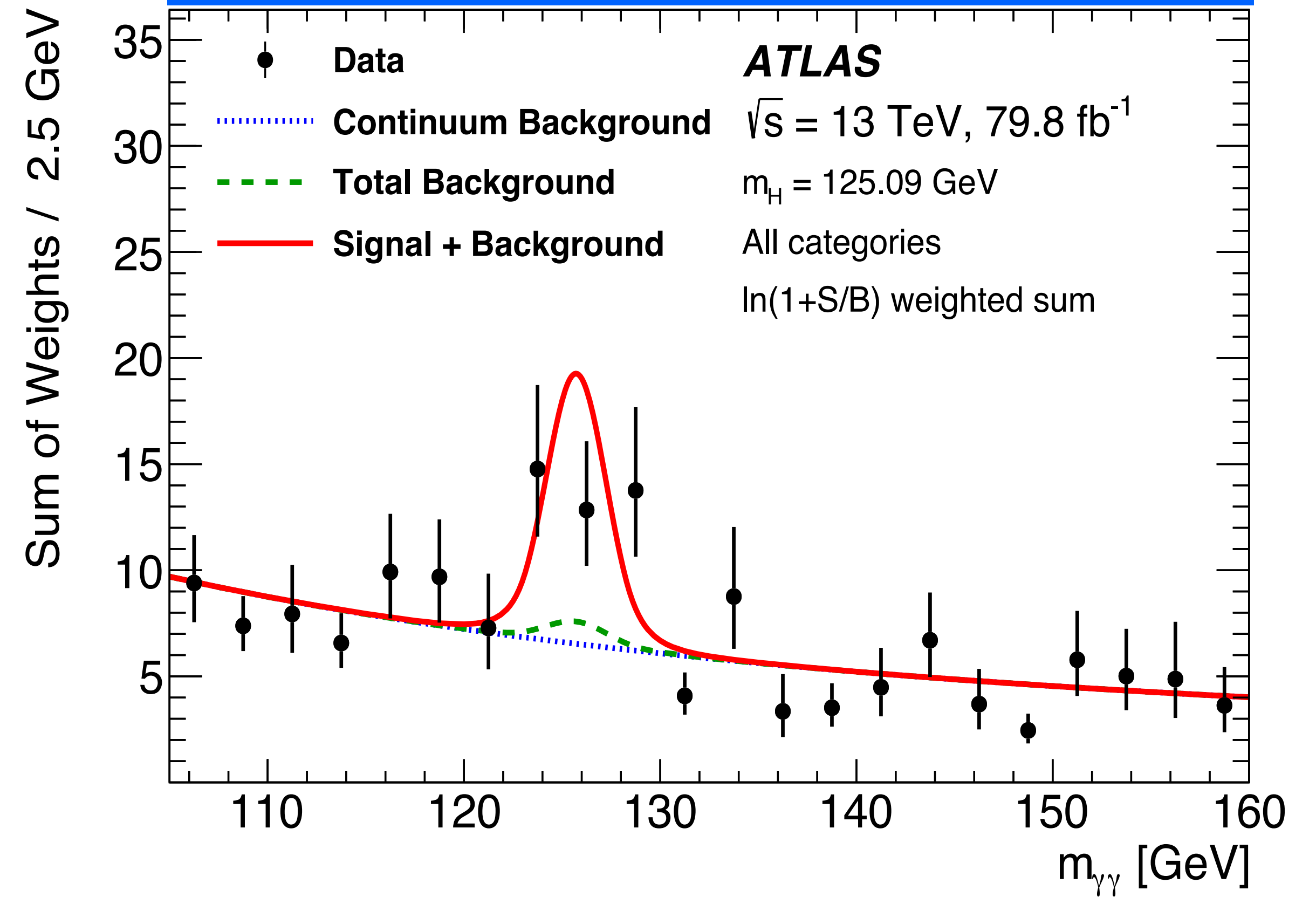


# the news of the past 18 months: ATLAS & CMS see events with top-quarks & Higgs simultaneously

across all events



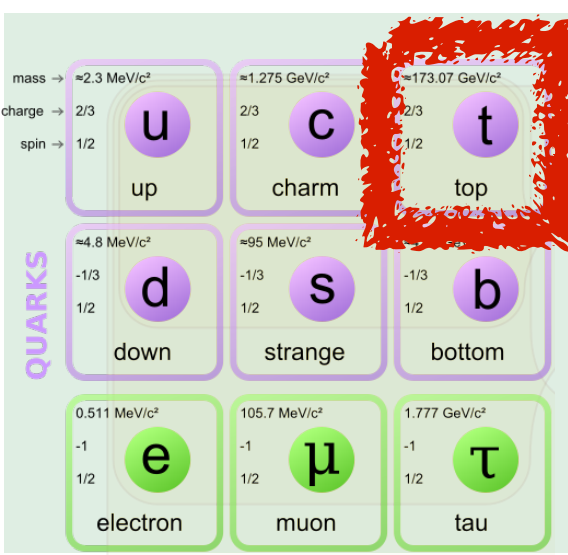
in events with top quarks



enhanced fraction of Higgs bosons in events with top quarks

→ direct observation of Higgs interaction with tops

(consistent with SM to c. ±20%)





# 2017/18 discovery of 3rd generation Yukawa interactions by ATLAS & CMS

mass →  
charge →  
spin →

**QUARKS**

$\approx 2.3 \text{ MeV}/c^2$ $2/3$ $1/2$ <b>u</b> up	$\approx 1.275 \text{ GeV}/c^2$ $2/3$ $1/2$ <b>c</b> charm	$\approx 173.07 \text{ GeV}/c^2$ $2/3$ $1/2$ <b>t</b> top
$\approx 4.8 \text{ MeV}/c^2$ $-1/3$ $1/2$ <b>d</b> down	$\approx 95 \text{ MeV}/c^2$ $-1/3$ $1/2$ <b>s</b> strange	$\approx 4.18 \text{ GeV}/c^2$ $-1/3$ $1/2$ <b>b</b> bottom
$0.511 \text{ MeV}/c^2$ $-1$ $1/2$ <b>e</b> electron	$105.7 \text{ MeV}/c^2$ $-1$ $1/2$ <b><math>\mu</math></b> muon	$1.777 \text{ GeV}/c^2$ $-1$ $1/2$ <b><math>\tau</math></b> tau

Discovery  $\equiv 5\sigma \simeq \pm 20\%$

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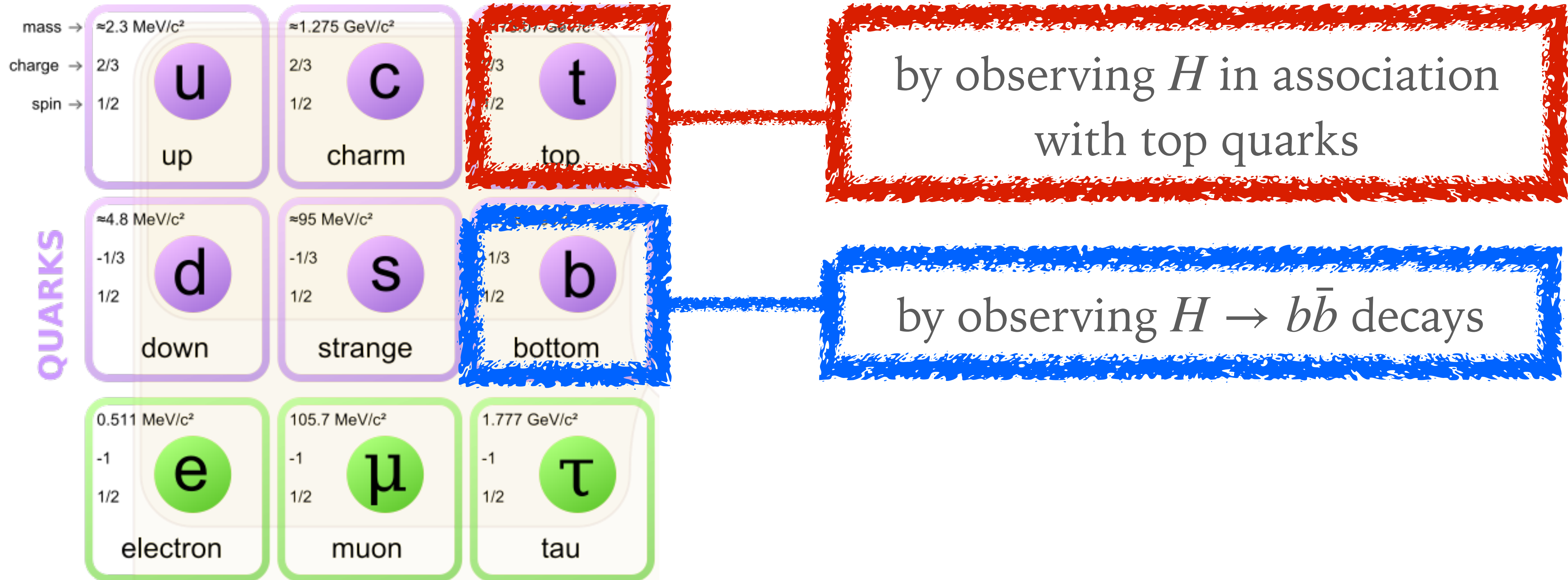
**QUARKS**

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by observing  $H$  in association with top quarks

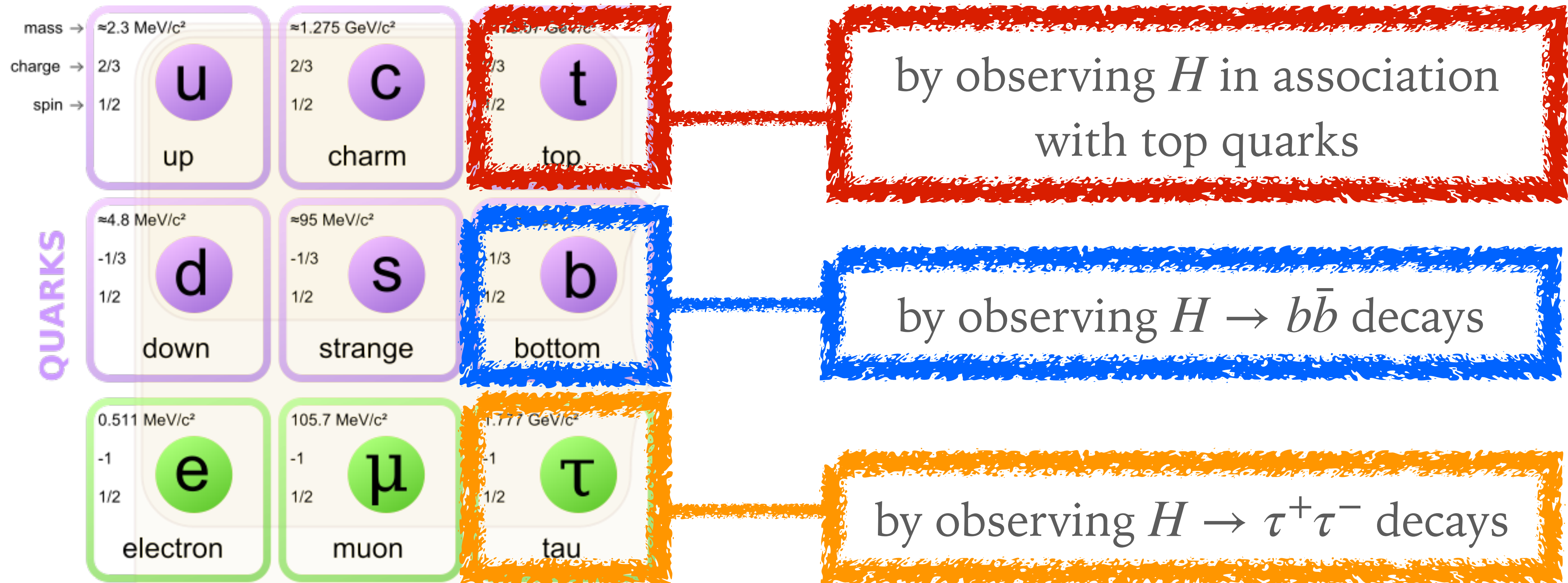
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Discovery  $\equiv 5\sigma \simeq \pm 20\%$

# 2017/18 discovery of 3rd generation Yukawa interactions by ATLAS & CMS



Discovery  $\equiv 5\sigma \simeq \pm 20\%$

# what's the message?

---

The  $>5\sigma$  observations of the  $t\bar{t}H$  process and of  $H \rightarrow \tau\tau$  and  $H \rightarrow b\bar{b}$  decays, independently by ATLAS and CMS, **firmly establish the existence of a new kind of fundamental interaction, Yukawa interactions.**

Yukawa interactions are important because they are:

- (1) **qualitatively unlike any quantum interaction probed before** (effective charge not quantised),
- (2) **hypothesized to be responsible for the stability of hydrogen**, and for determining the size of atoms and the energy scales of chemical reactions.

Establishing the pattern of Yukawa couplings across the full remaining set of quarks and charged leptons is one of the major challenges for particle physics today.

# what's the message?

---

The  $>5\sigma$  observations of the  $t\bar{t}H$  process and of  $H \rightarrow \tau\tau$  and  $H \rightarrow b\bar{b}$  decays, independently by ATLAS and CMS, **firmly establish the existence of a new kind of fundamental interaction, Yukawa interactions.**

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Establishing the pattern of Yukawa couplings across the full remaining set of quarks and charged leptons is one of the major challenges for particle physics today.

**Is this any less important than the discovery of the Higgs boson itself?**

**My opinion: no, because fundamental interactions are as important as fundamental particles**

# what could one be saying about it?

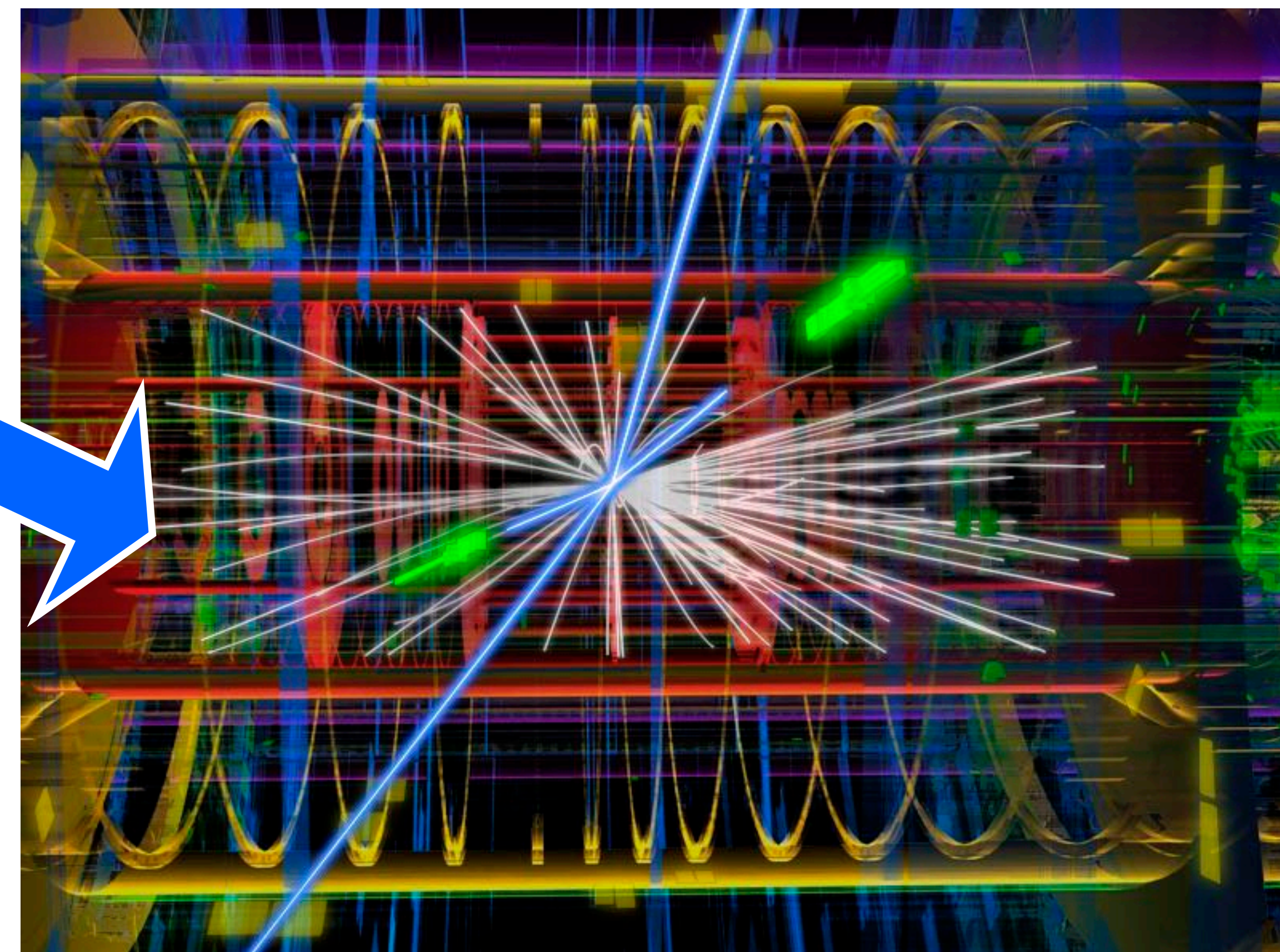
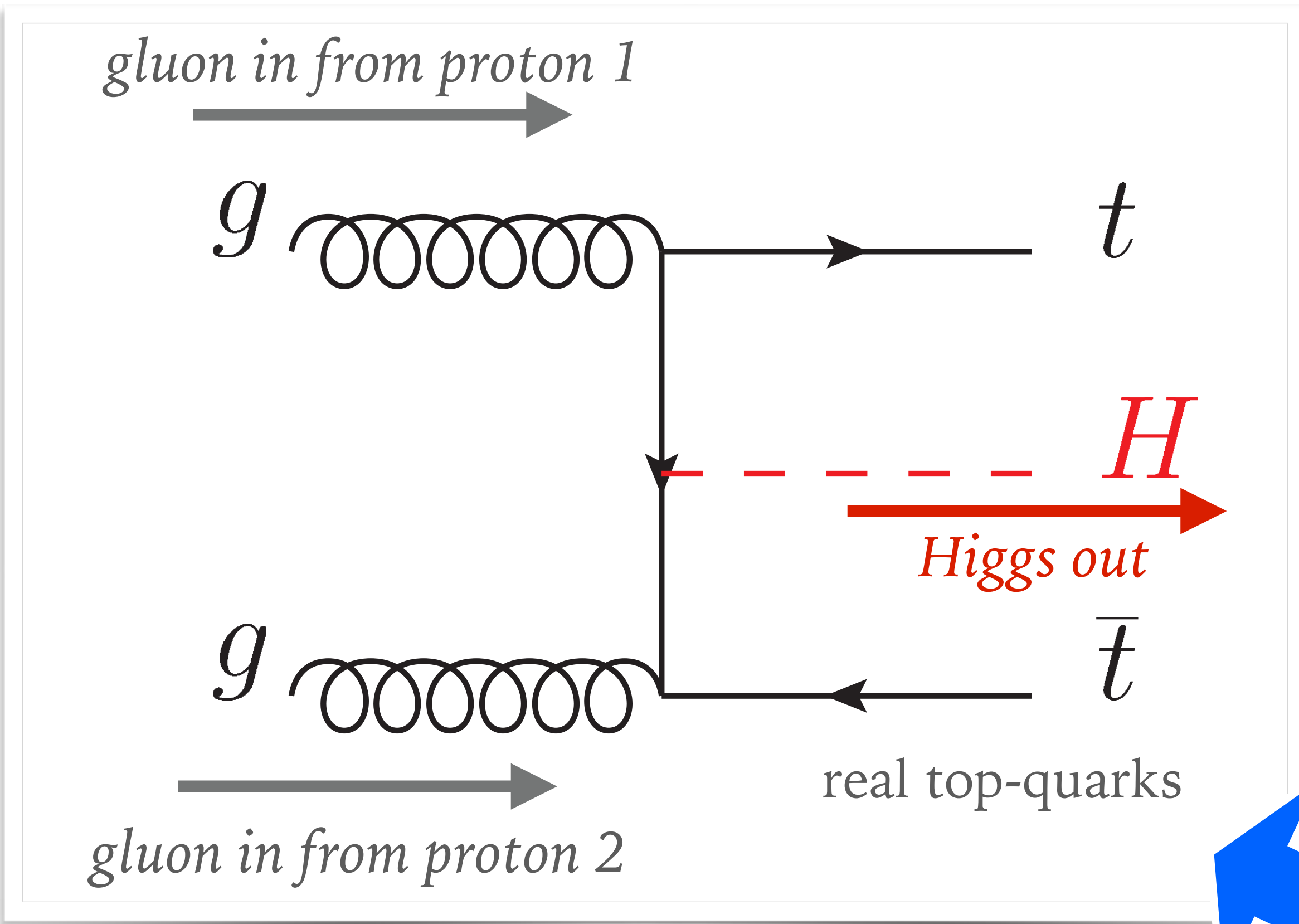
---

This is a fifth force, the “Higgs force”

(up to you to decide whether you prefer to talk about new interactions or new force)

**Is this any less important than the discovery of the Higgs boson itself?**

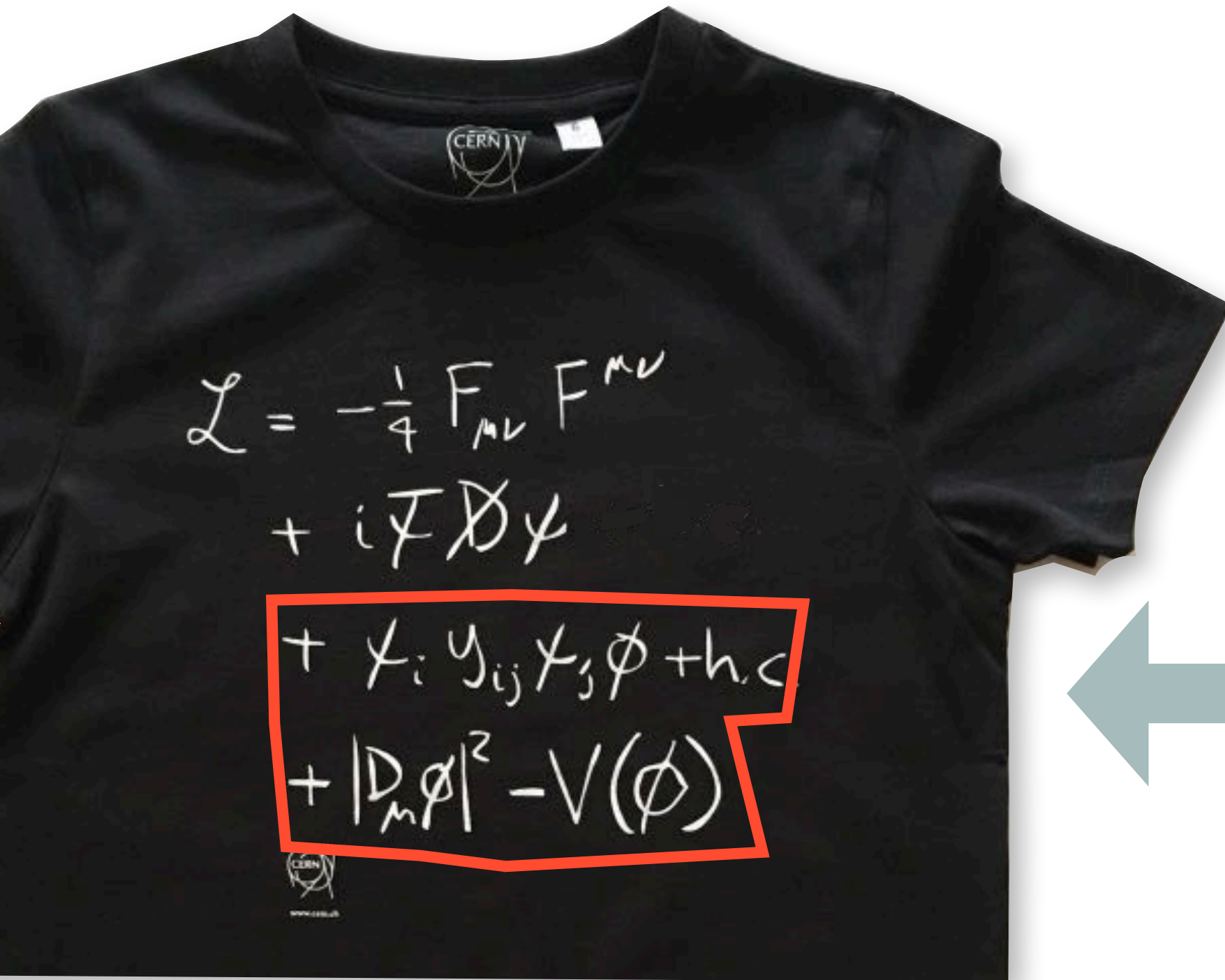
**My opinion: no, because fundamental interactions are as important as fundamental particles**



how can one claim a connection,  
let alone a quantitative one?



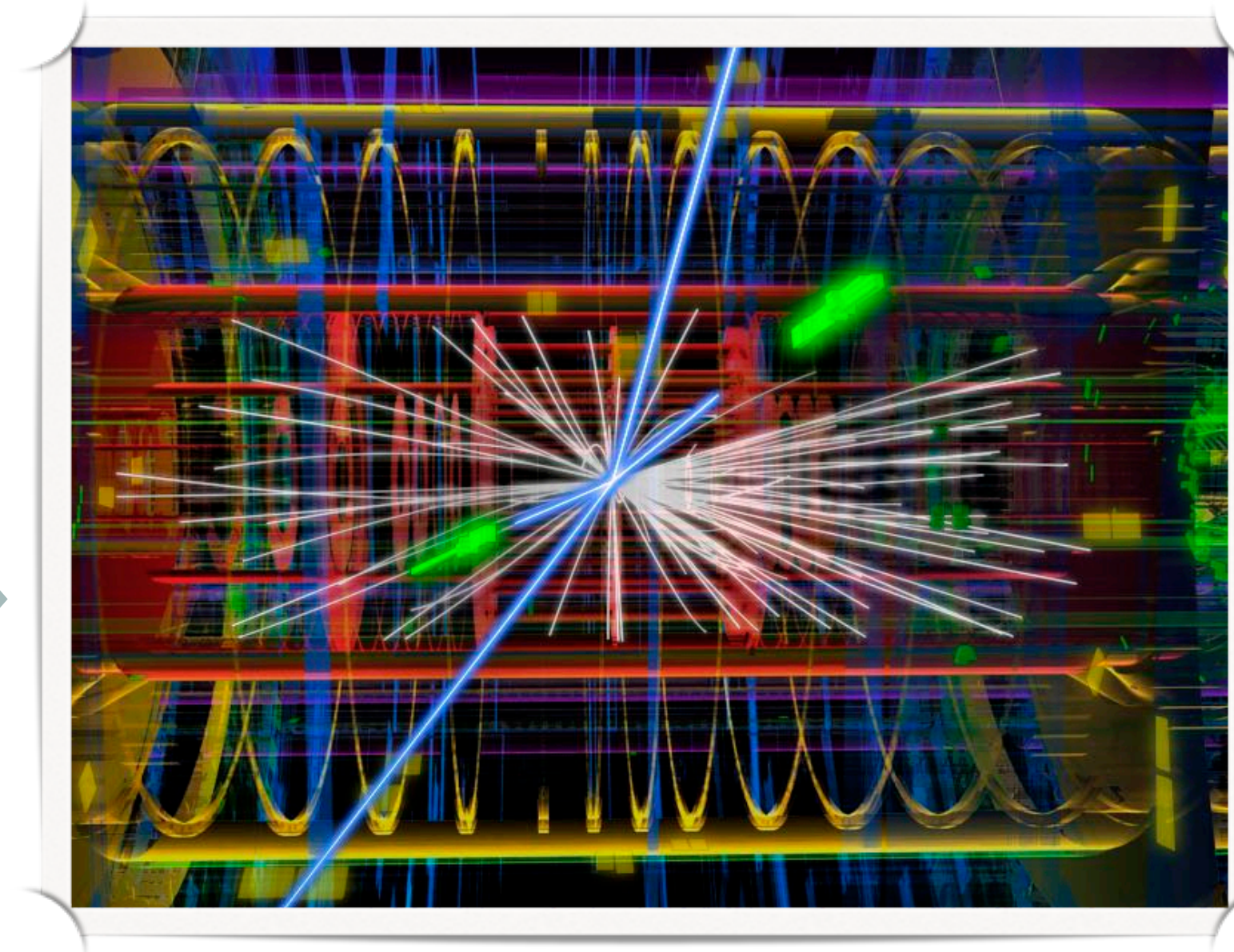
# UNDERLYING THEORY



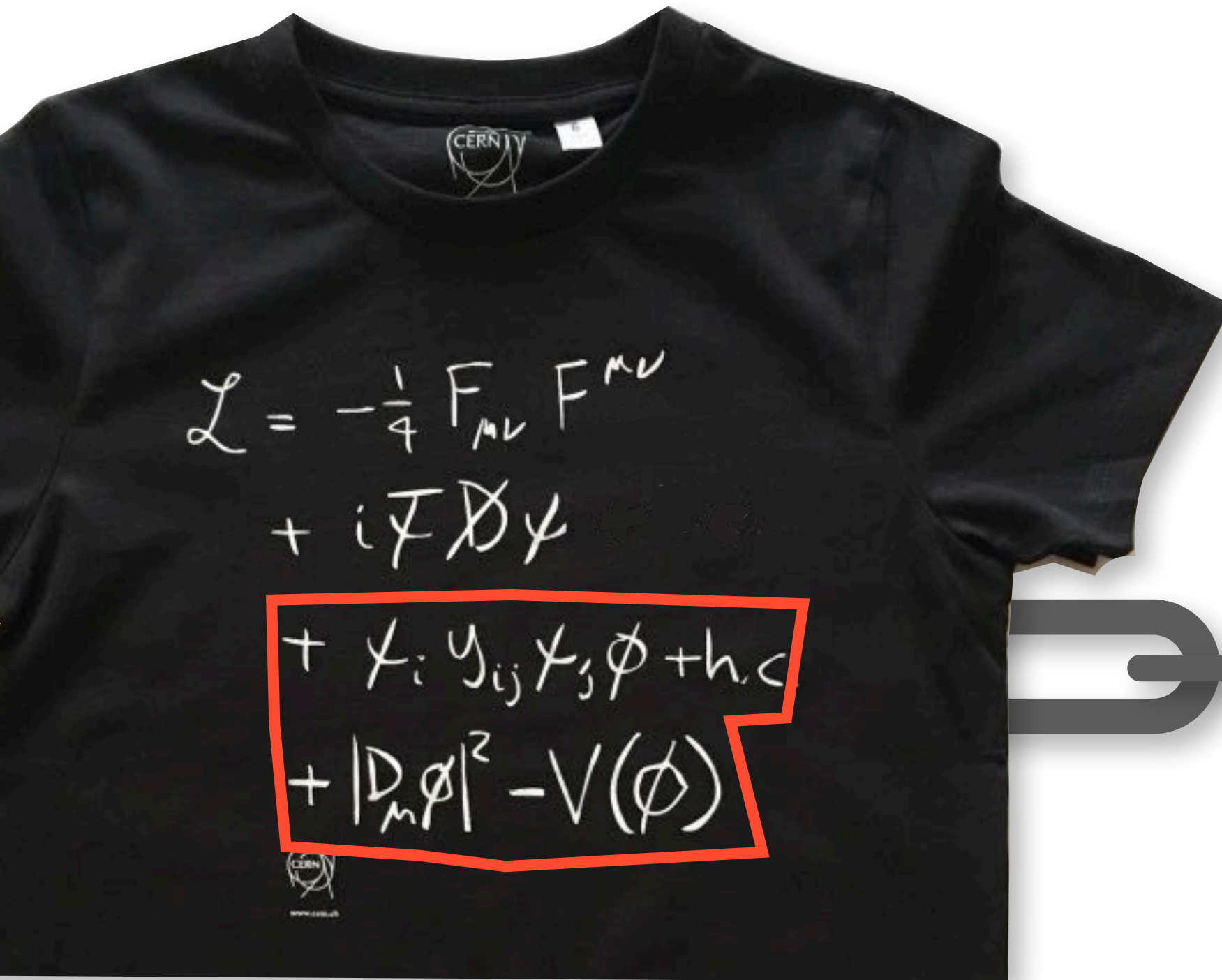
*how do you make  
quantitative  
connection?*



# EXPERIMENTAL DATA



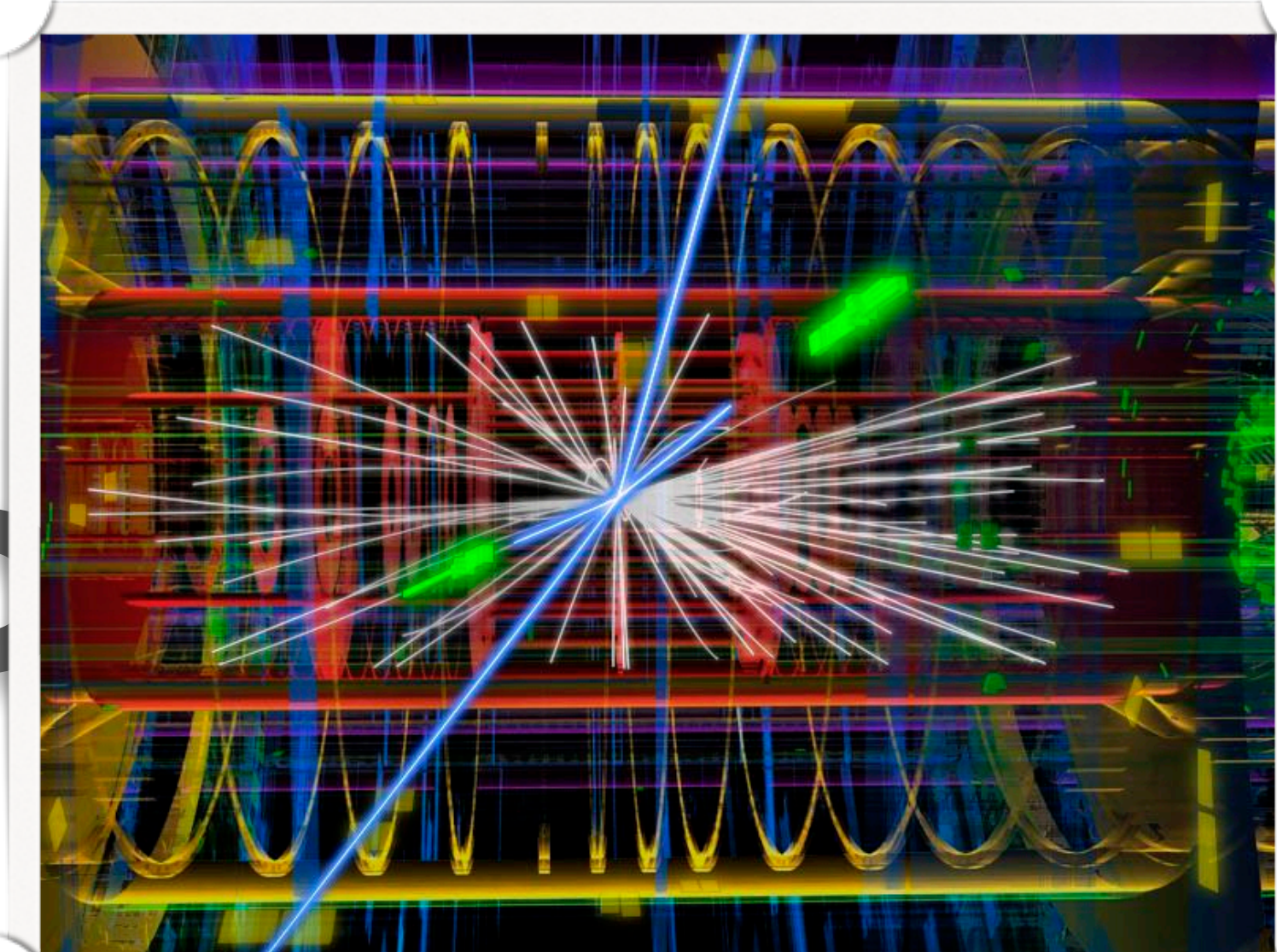
# UNDERLYING THEORY



*how do you make  
quantitative  
connection?*

*through a chain  
of experimental  
and theoretical links*

# EXPERIMENTAL DATA



# QCD

---

*quantum chromodynamics*

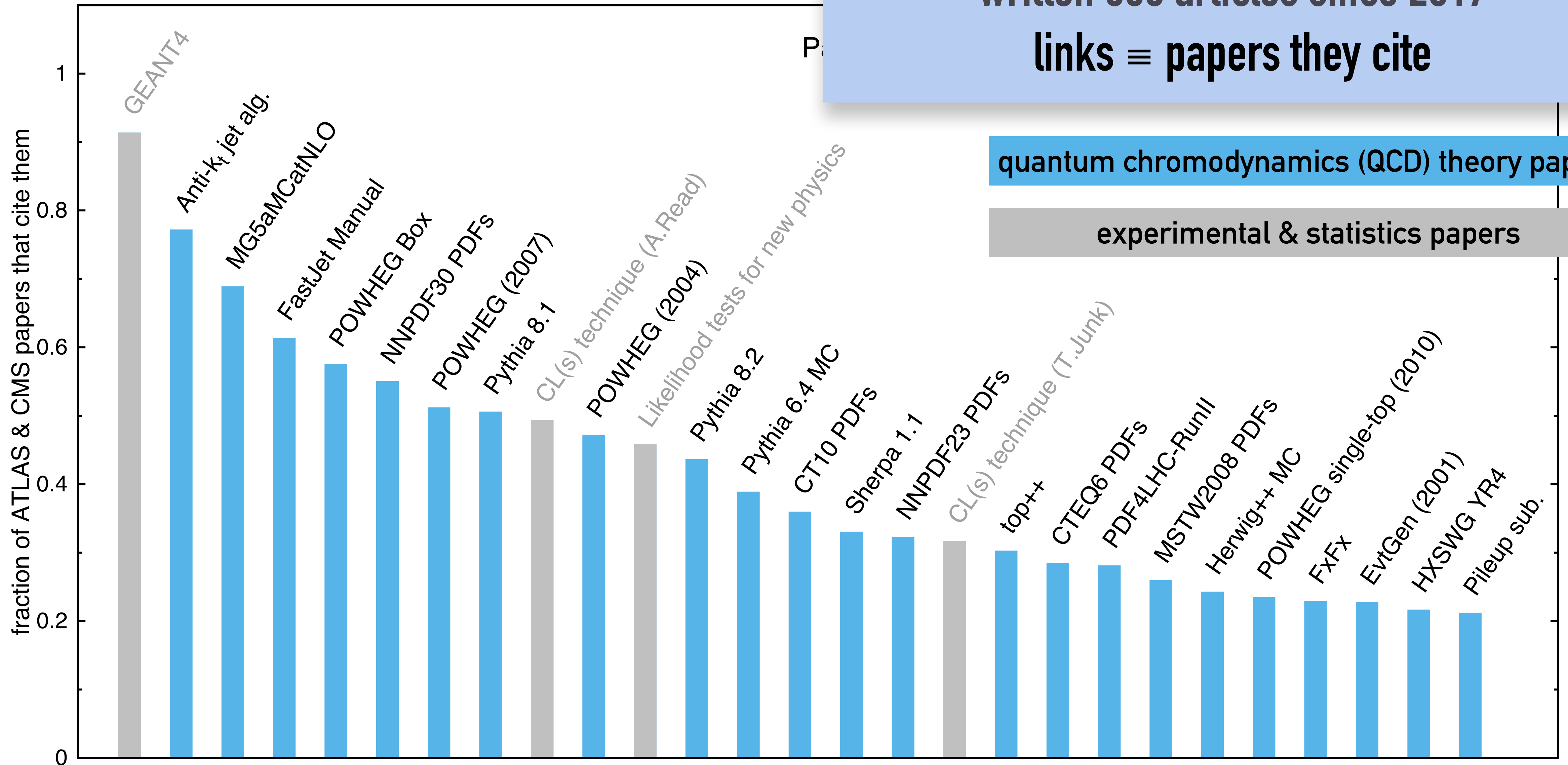
*the theory of the strong interaction*

# What are the links?

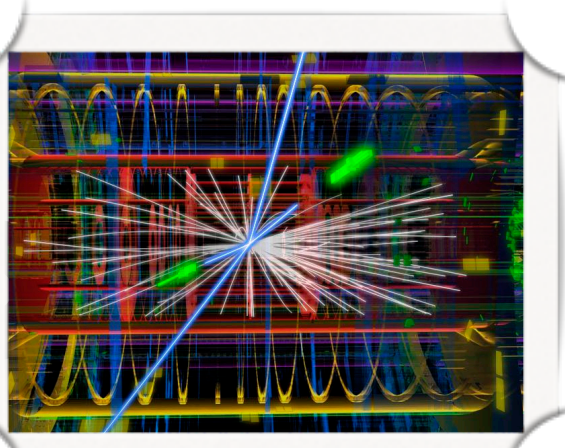
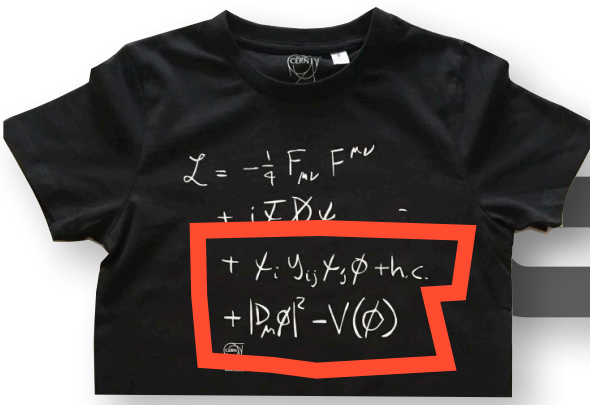
ATLAS and CMS (big LHC expts.) have written 650 articles since 2017  
links  $\equiv$  papers they cite

quantum chromodynamics (QCD) theory papers

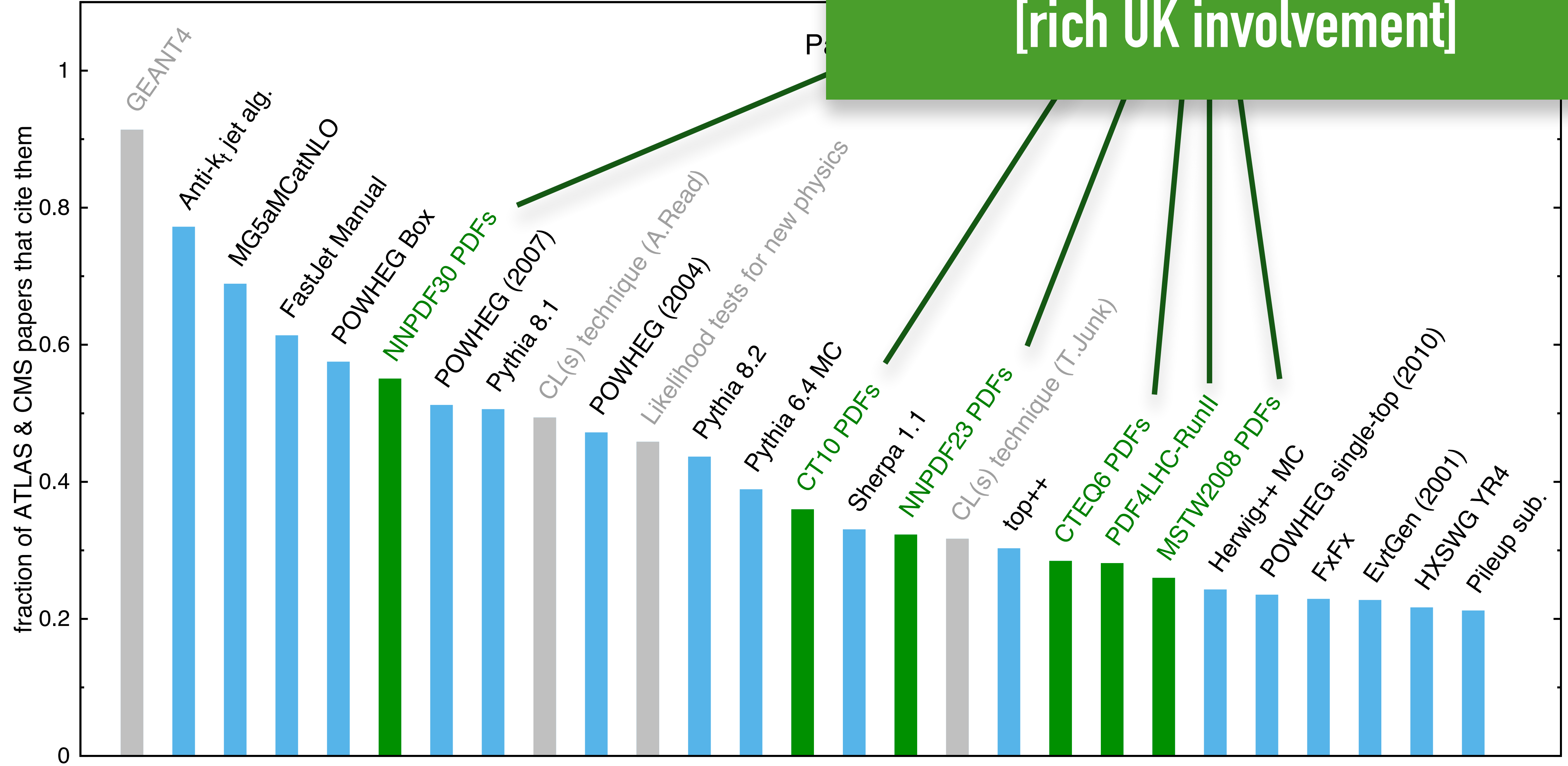
experimental & statistics papers



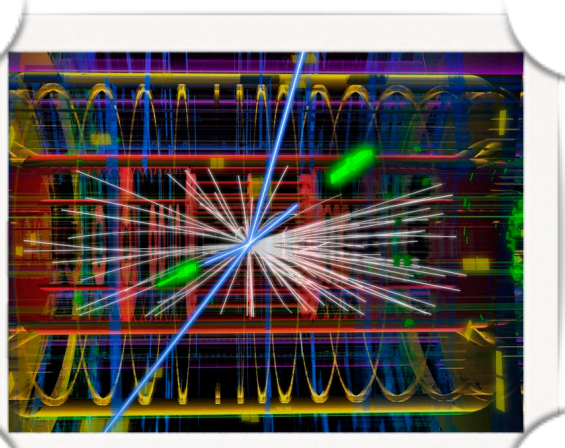
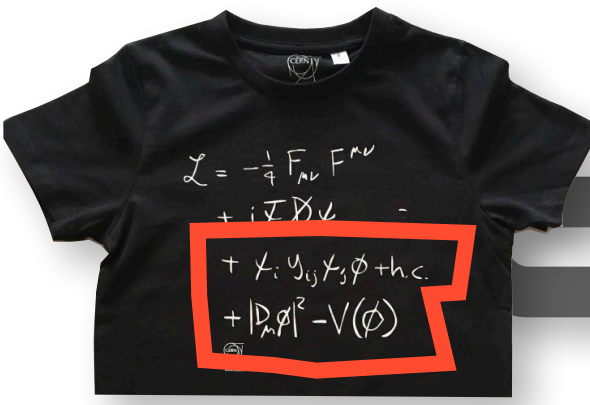
Plot by GP Salam based on data from InspireHEP



knowing what goes into a collision  
i.e. proton structure  
[rich UK involvement]

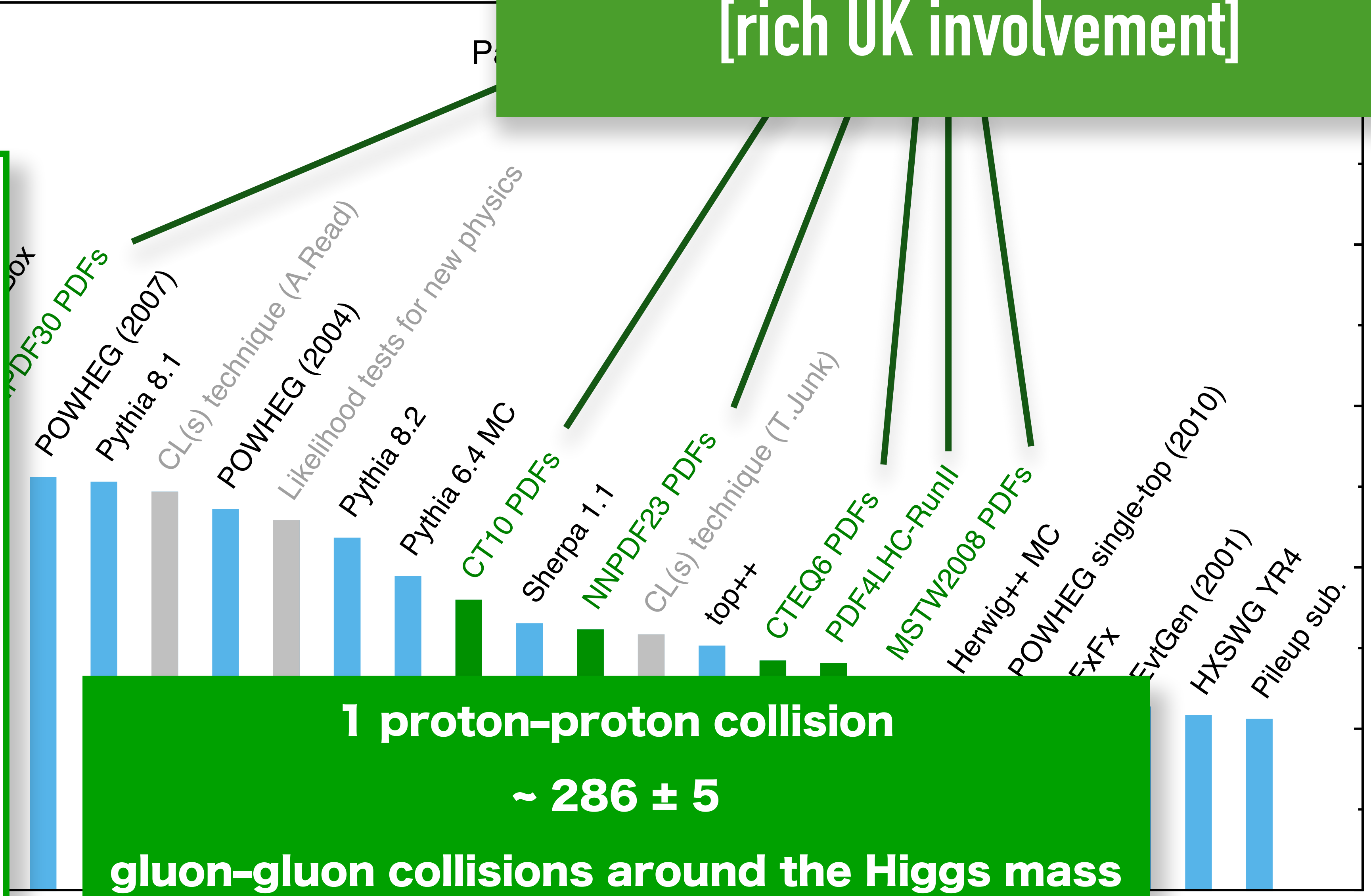
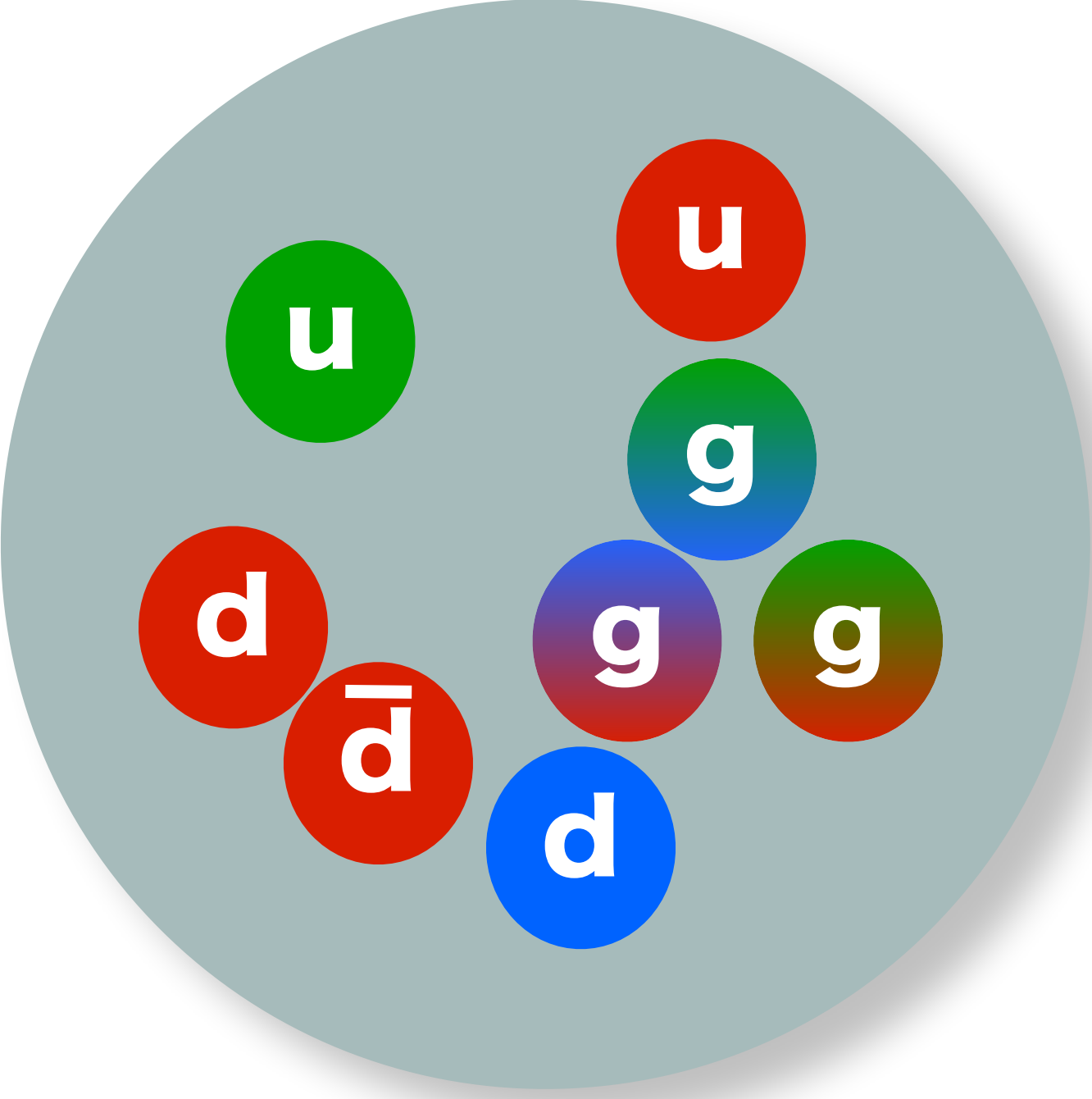


Plot by GP Salam based on data from InspireHEP

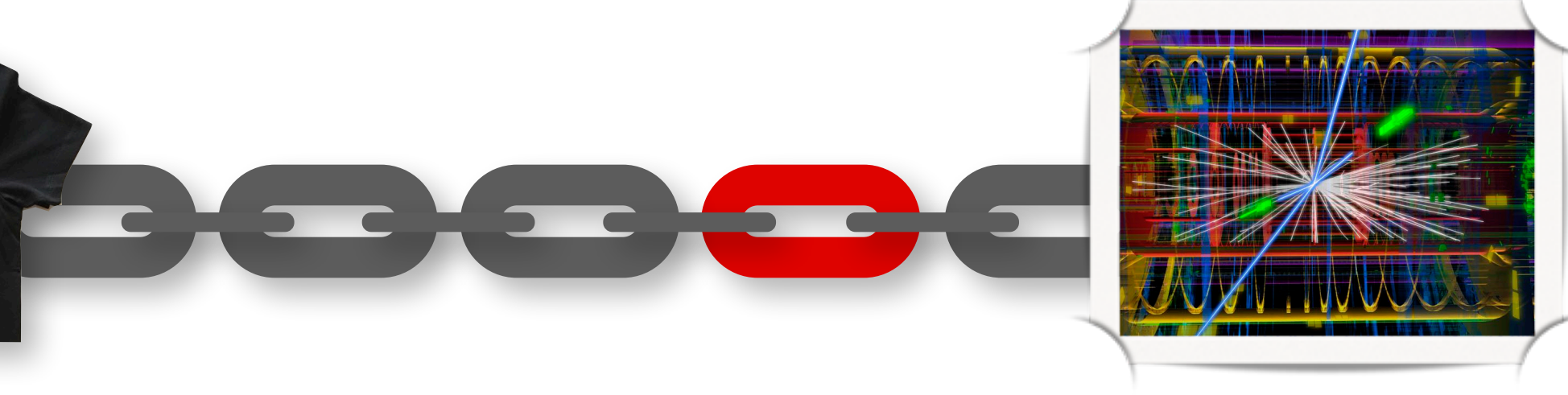
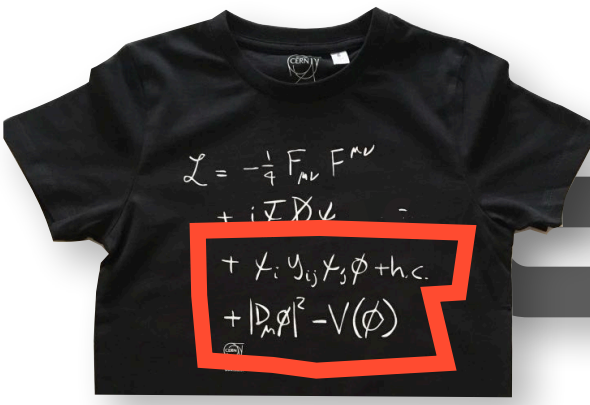


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# PROTON

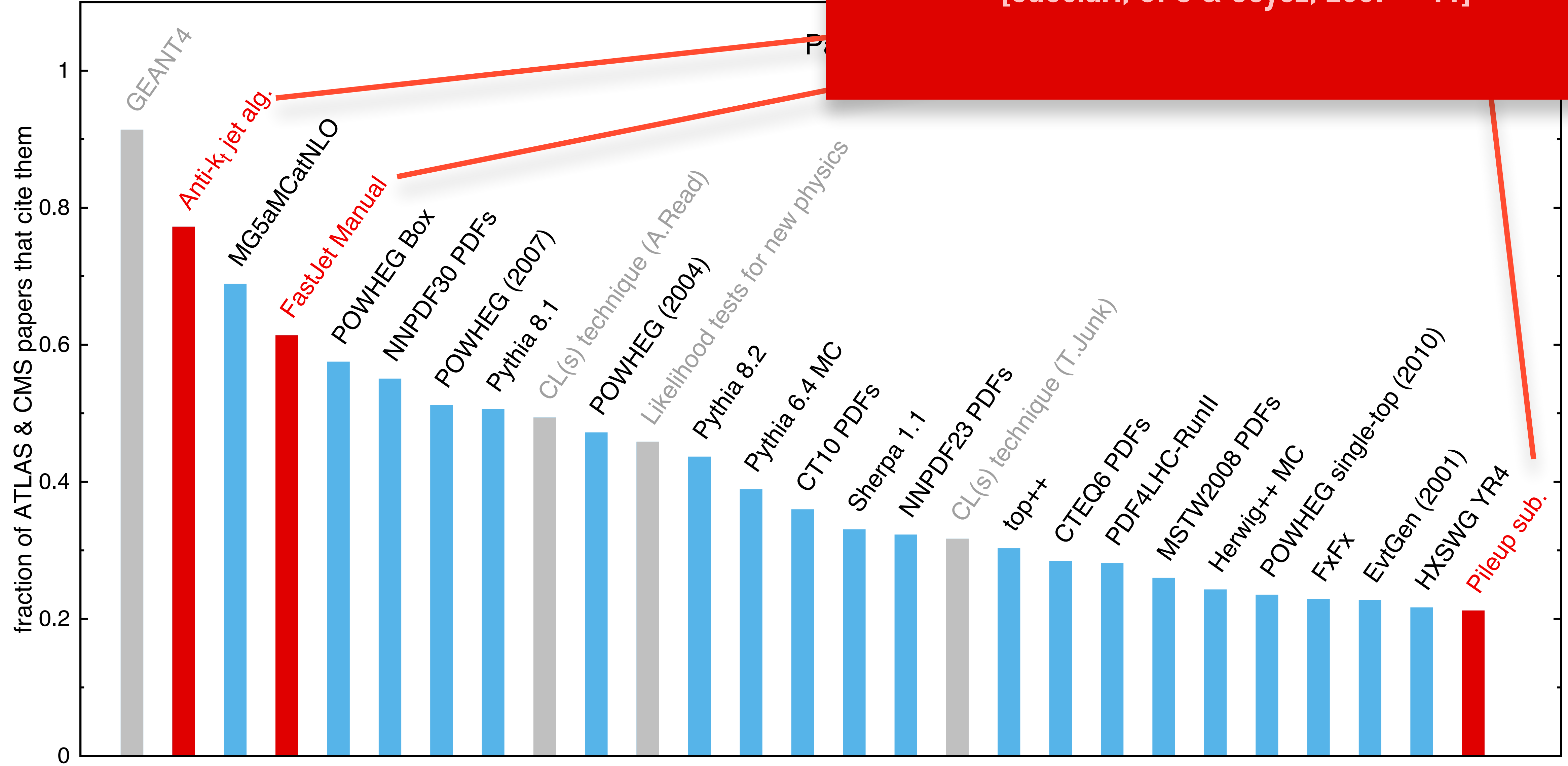


Plot by GP Salam based on data from InspireHEP

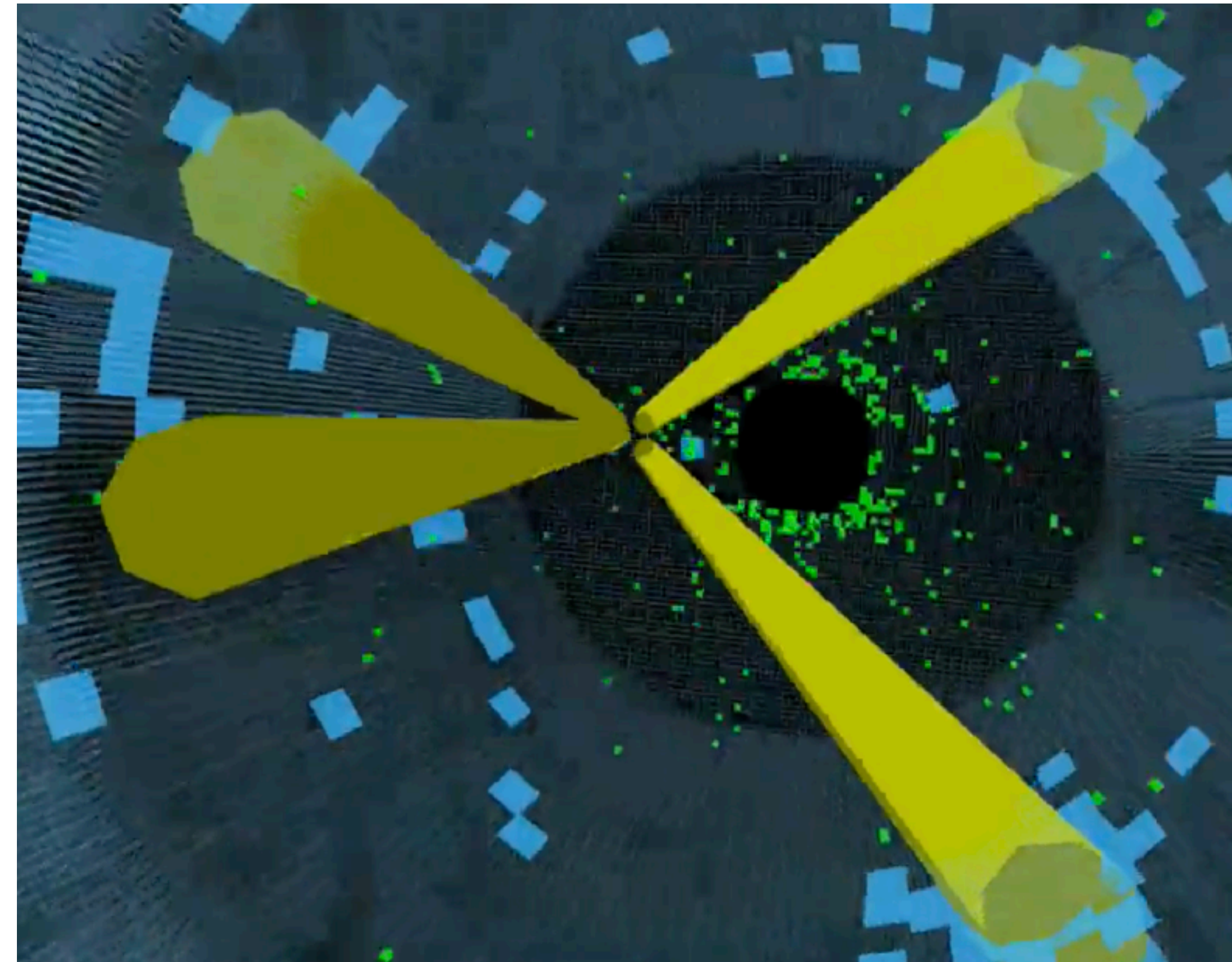
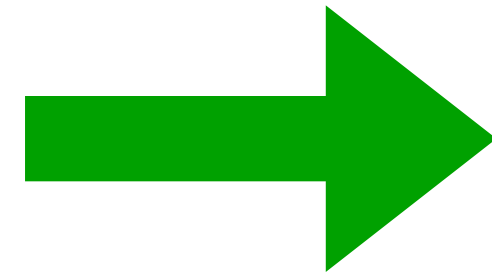
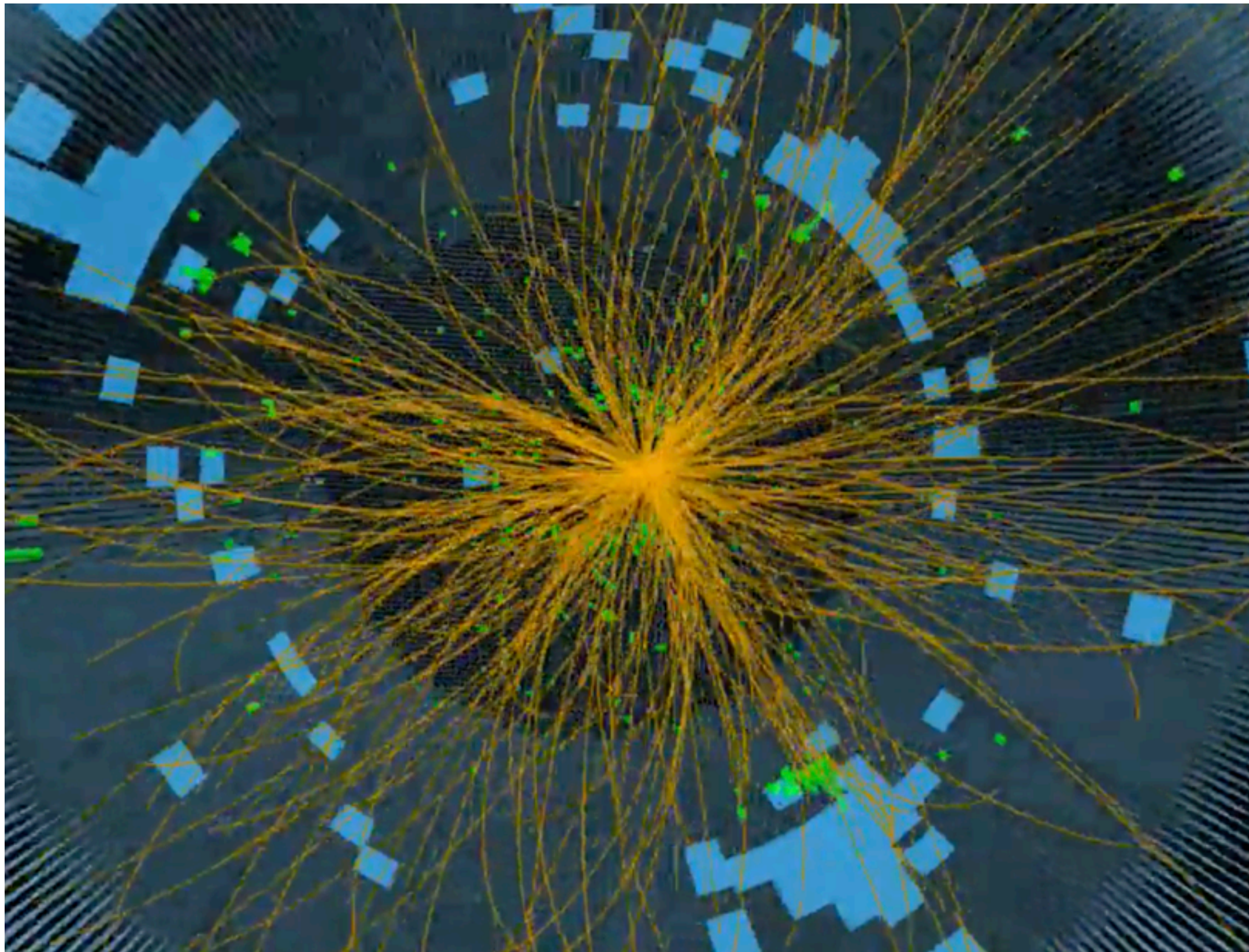


# organising event information ("jets")

[Cacciari, GPS & Soyez, 2007 – 11]

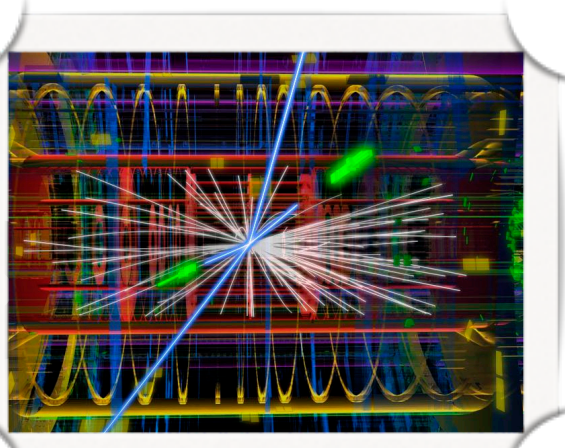
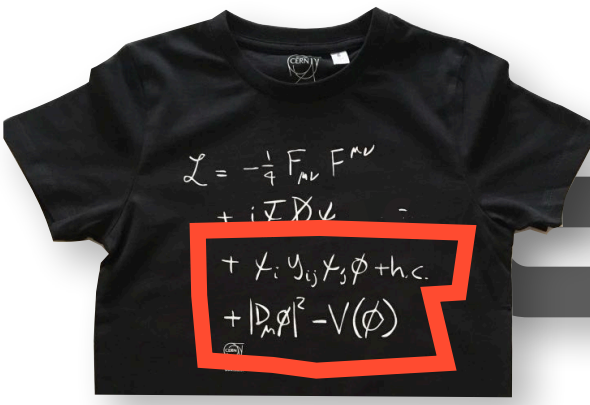


Plot by GP Salam based on data from InspireHEP

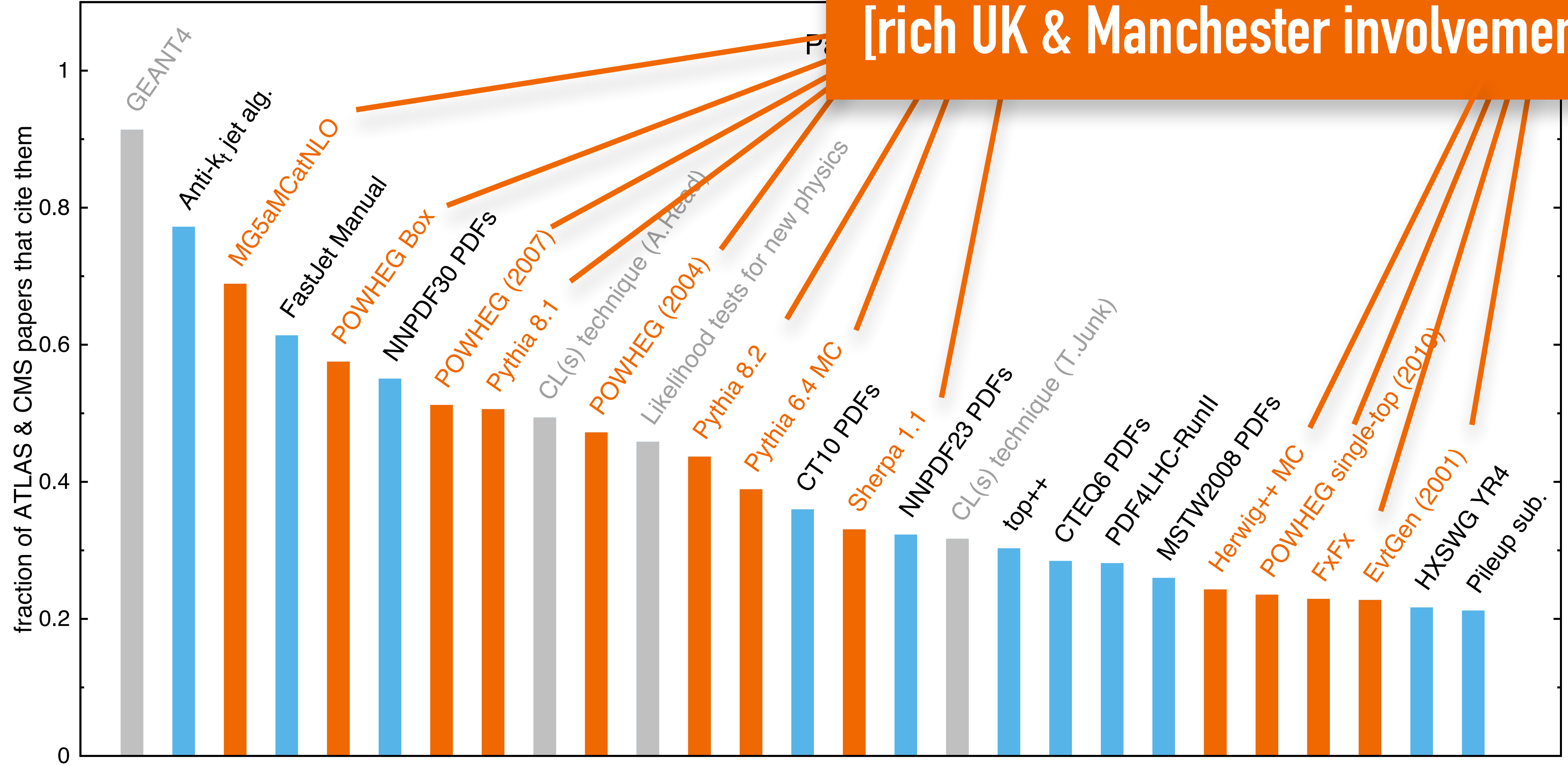


*the question of organising information from hundreds of particles will come back later*

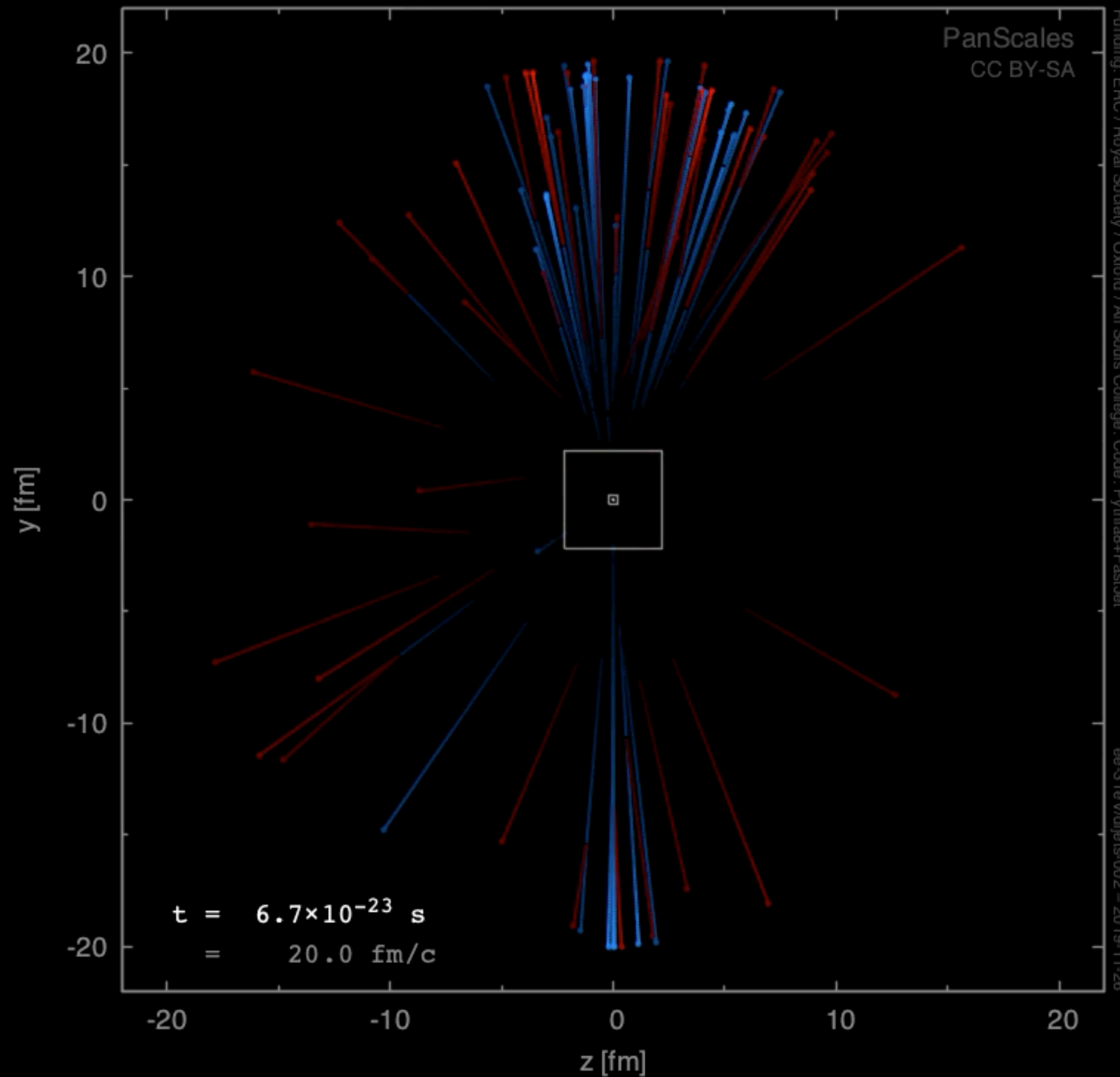




predicting full particle structure  
that comes out of a collision  
[rich UK & Manchester involvement]

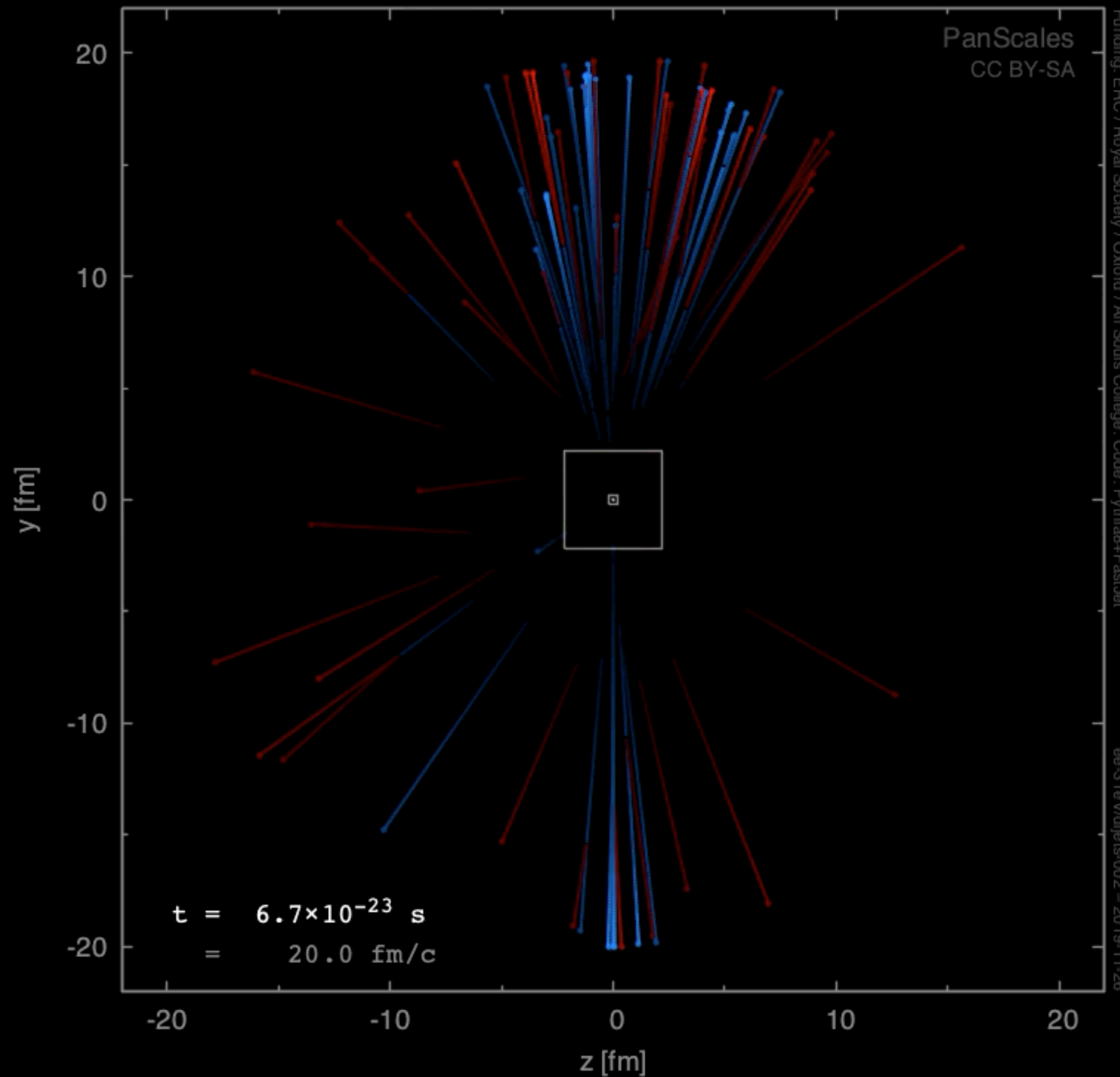


Plot by GP Salam based on data from InspireHEP



- incoming beam particle
- intermediate particle
- final particle

Event evolution spans 7 orders of magnitude in space-time

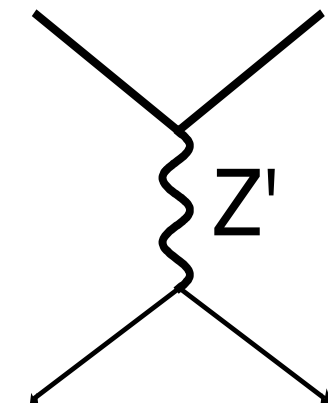


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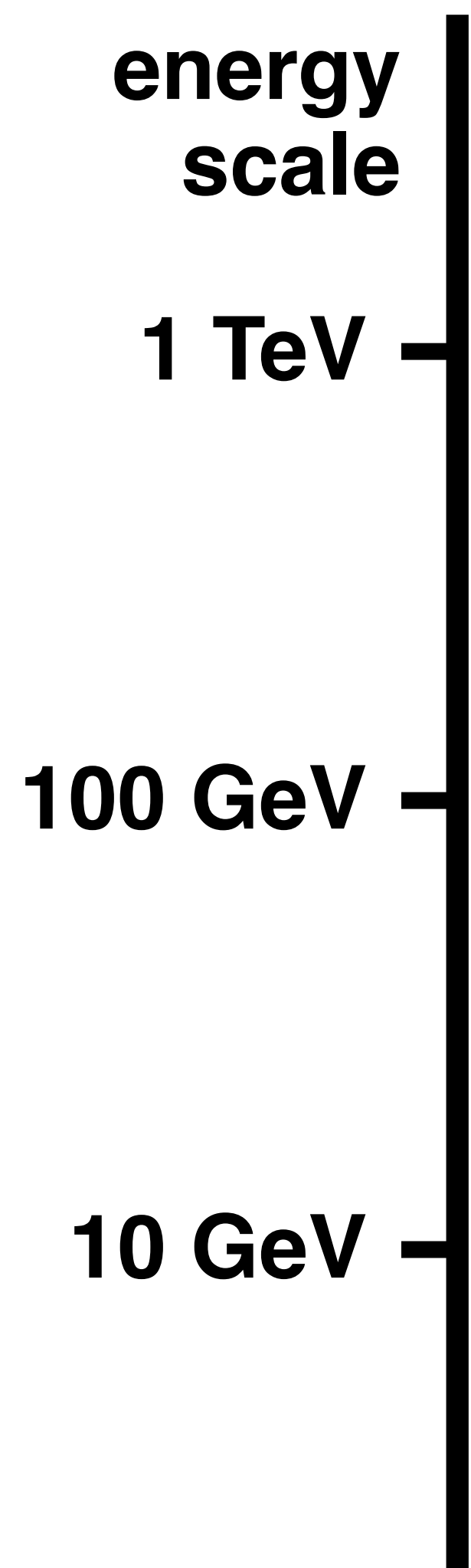
energy  
scale  
1 TeV

hard process



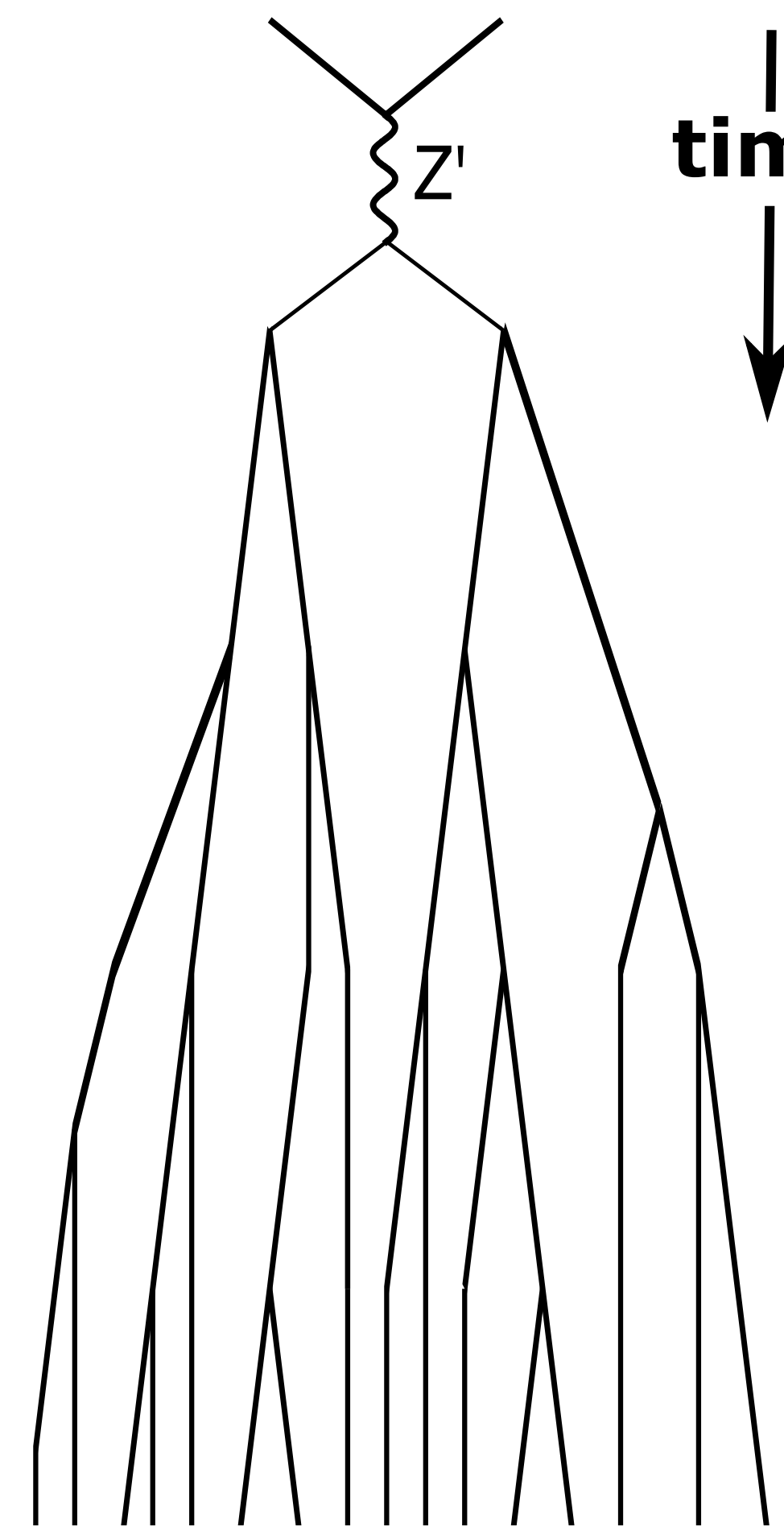
time

schematic view of key  
components of QCD  
predictions and Monte  
Carlo event simulation

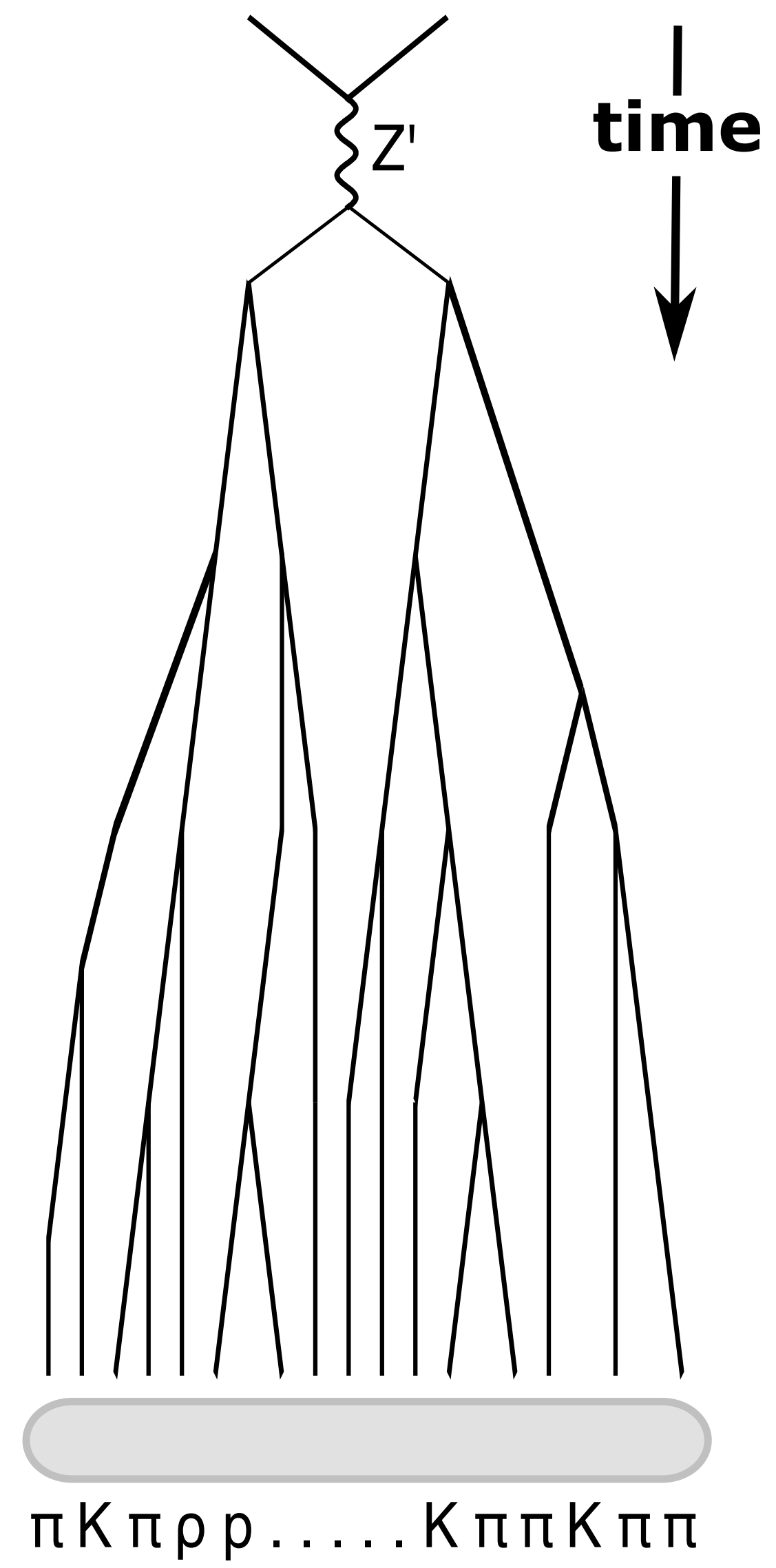
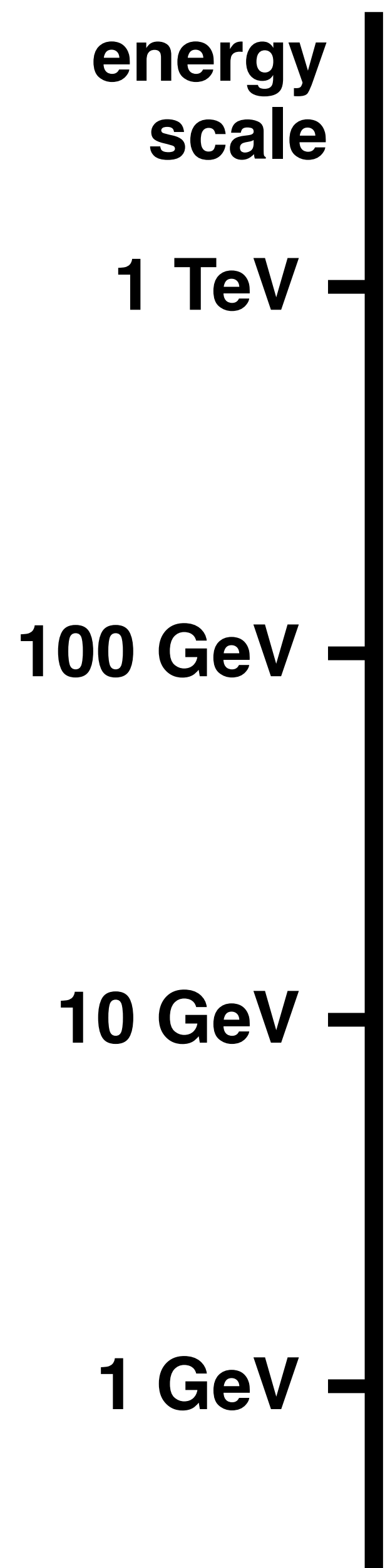


hard process

parton shower



schematic view of key components of QCD predictions and Monte Carlo event simulation



schematic view of key components of QCD predictions and Monte Carlo event simulation

pattern of particles in MC can be directly compared to pattern in experiment

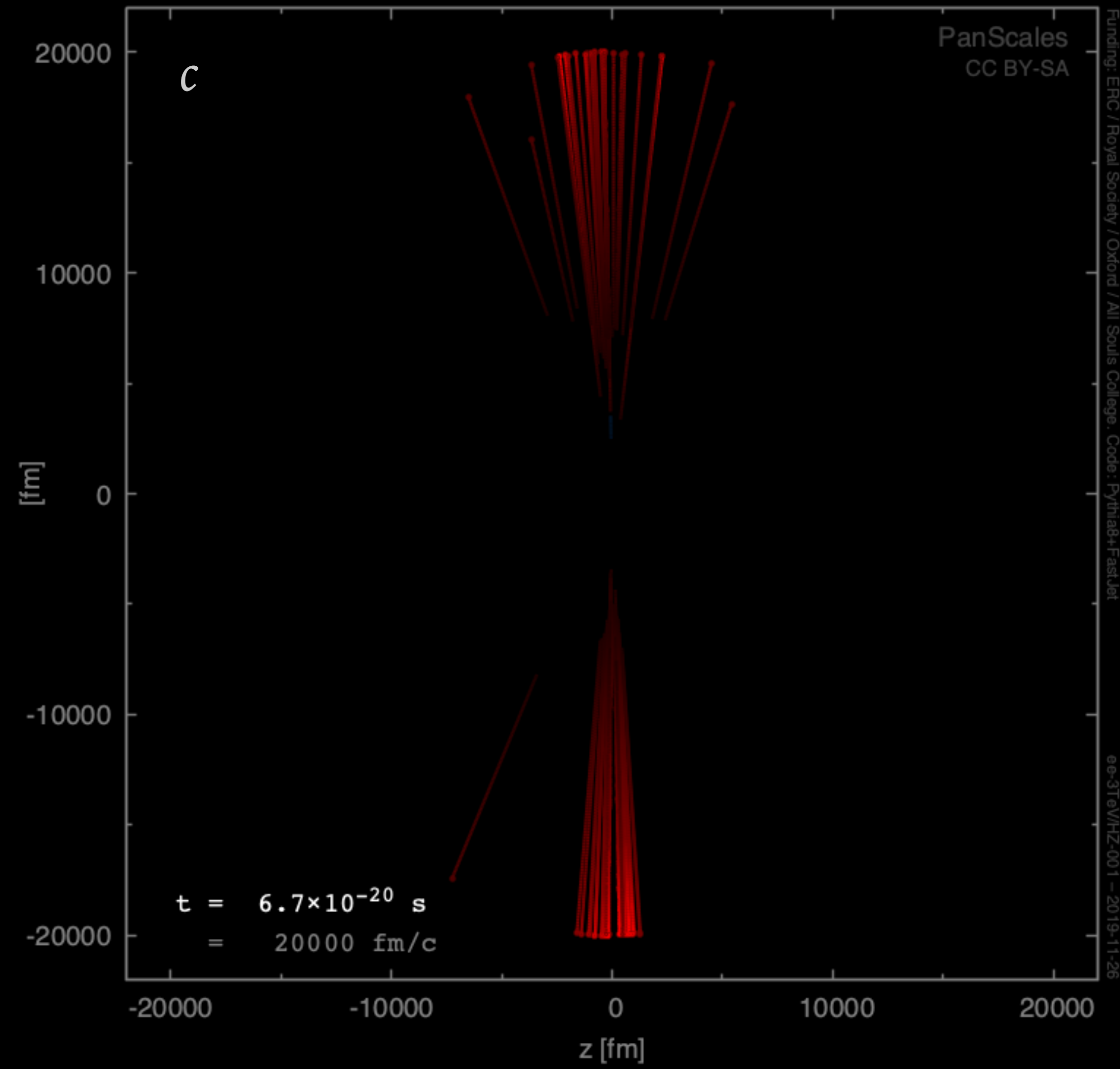
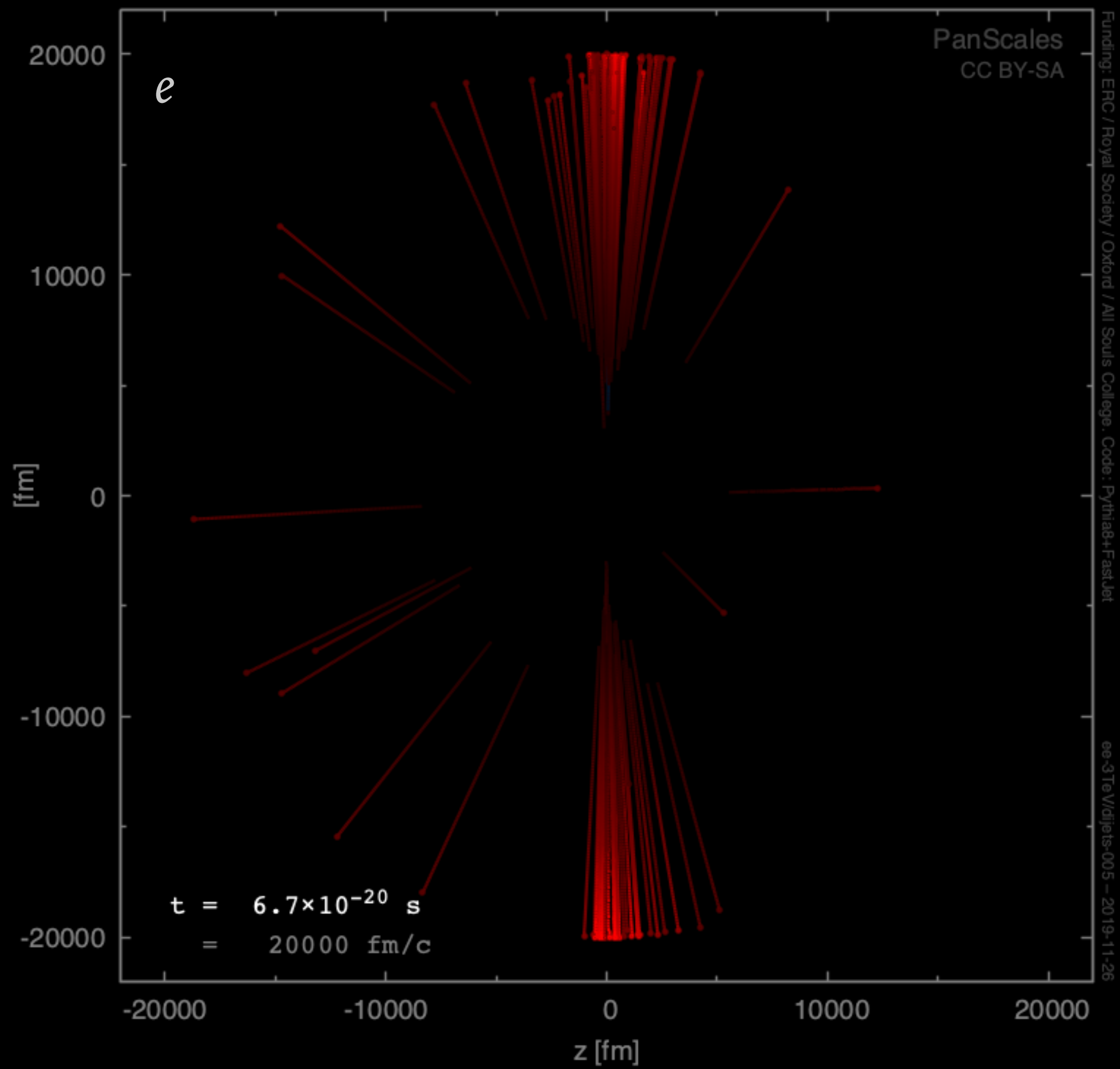
# (jet) substructure

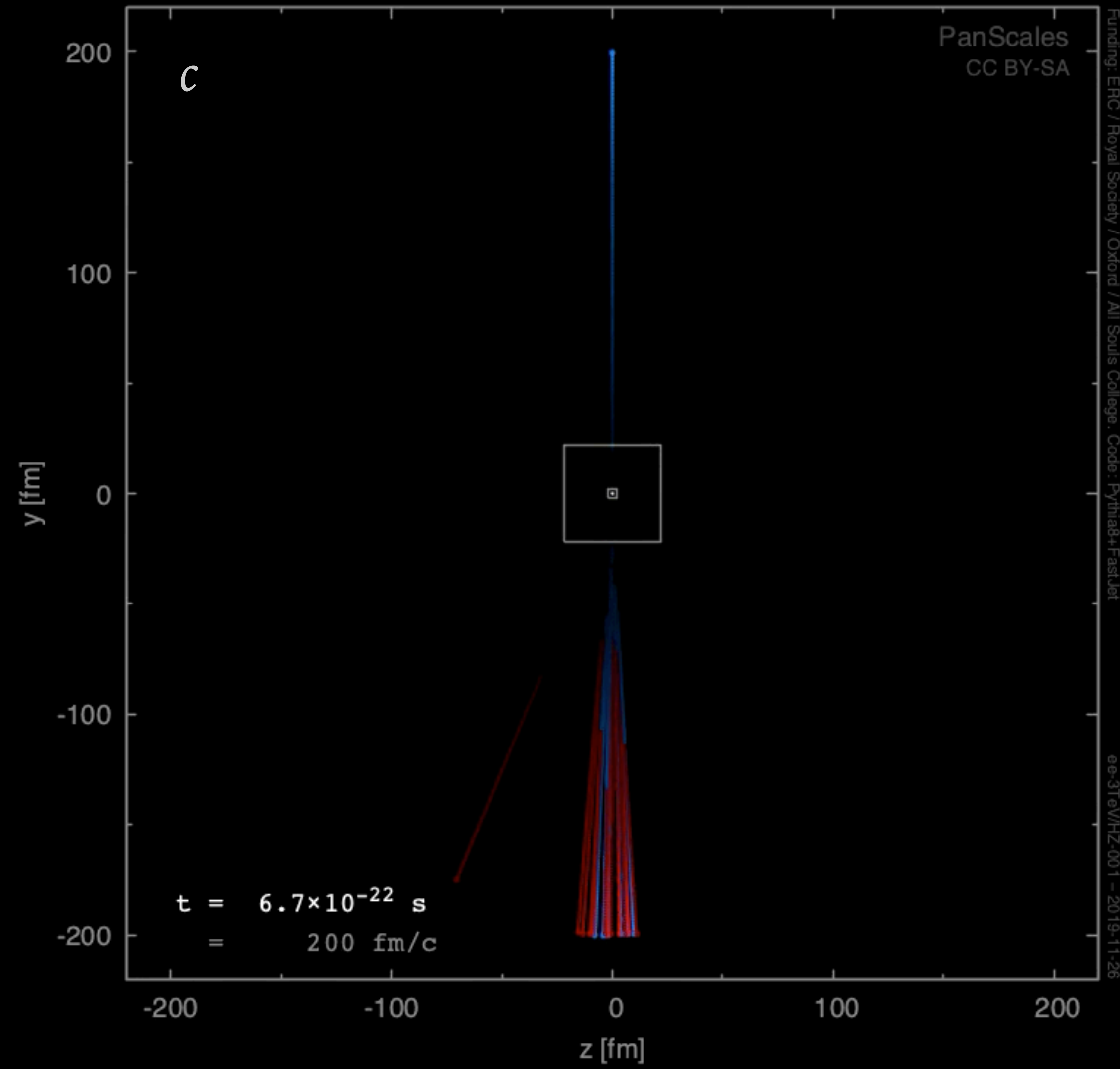
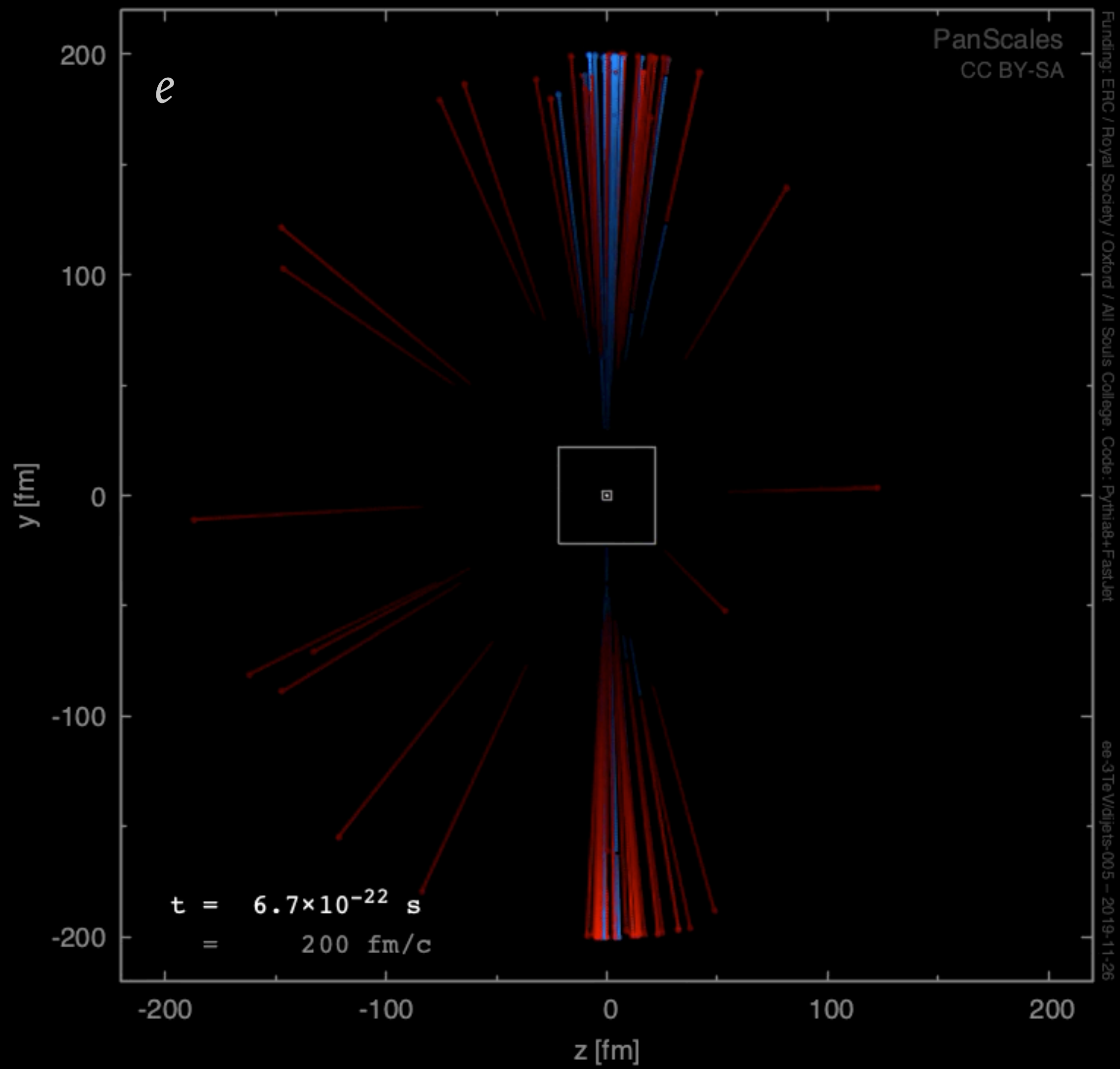
---

*how much information is hidden among  
the hundreds of particles produced in a collisions?*

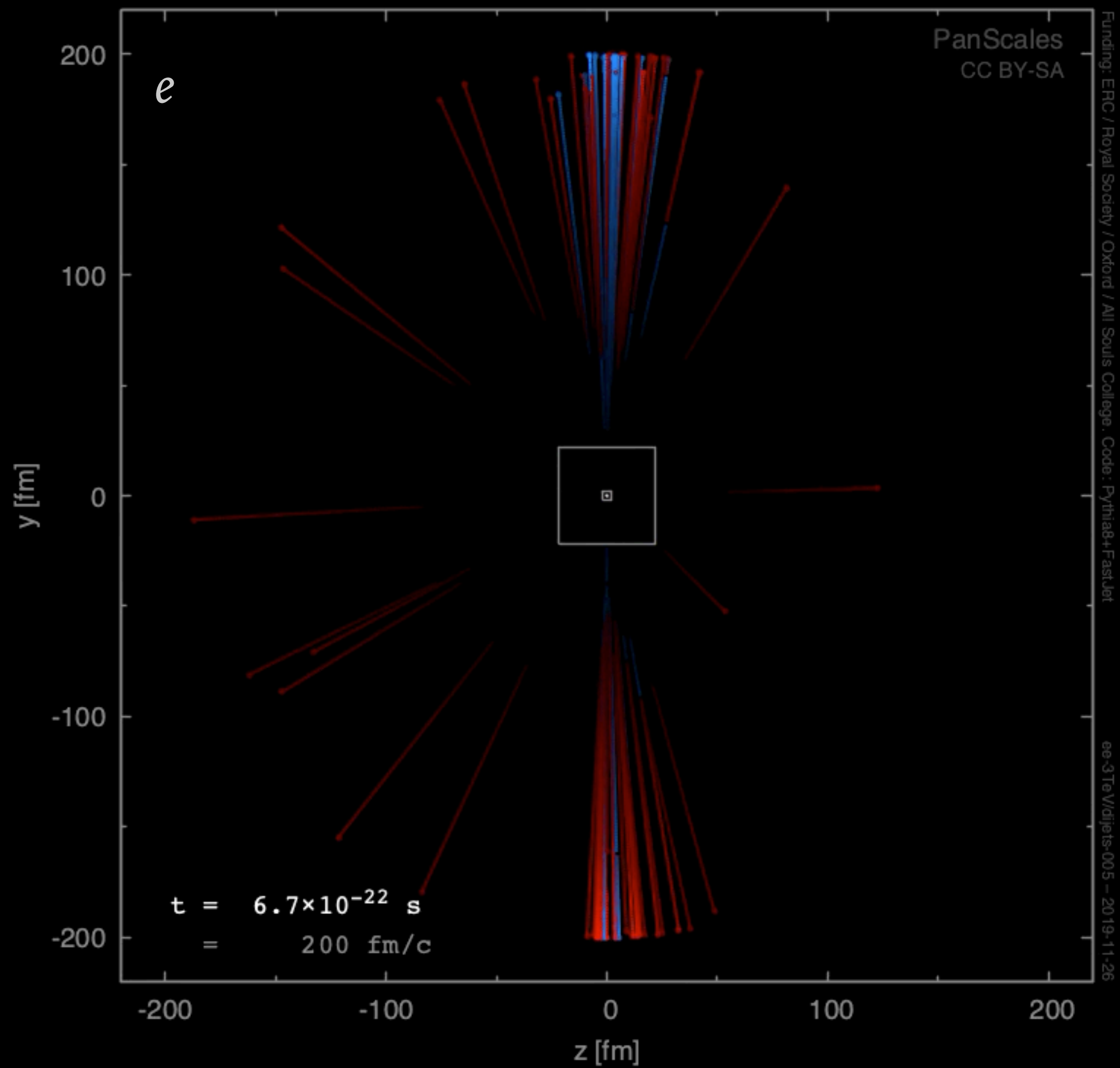




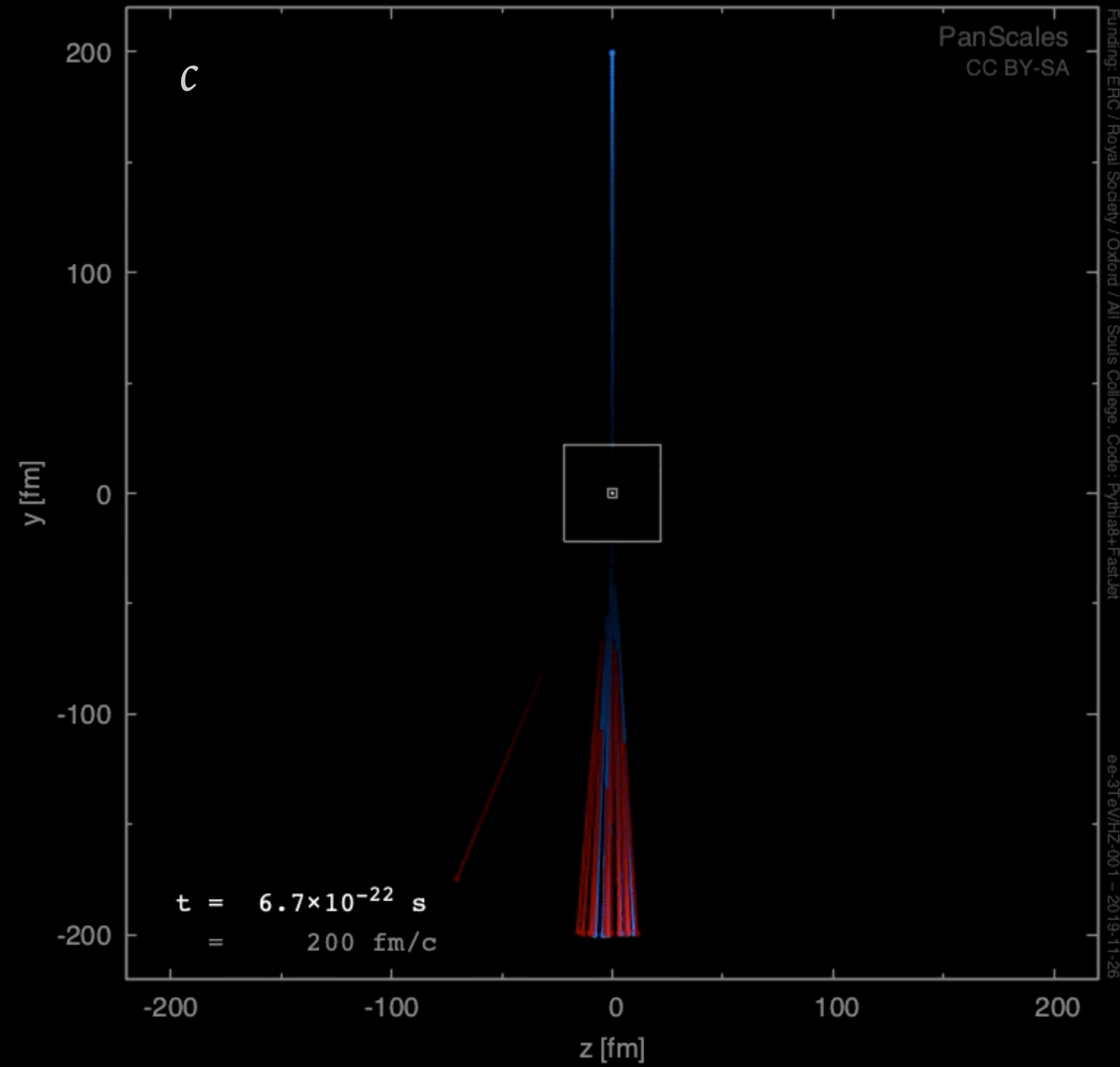




# pure QCD event



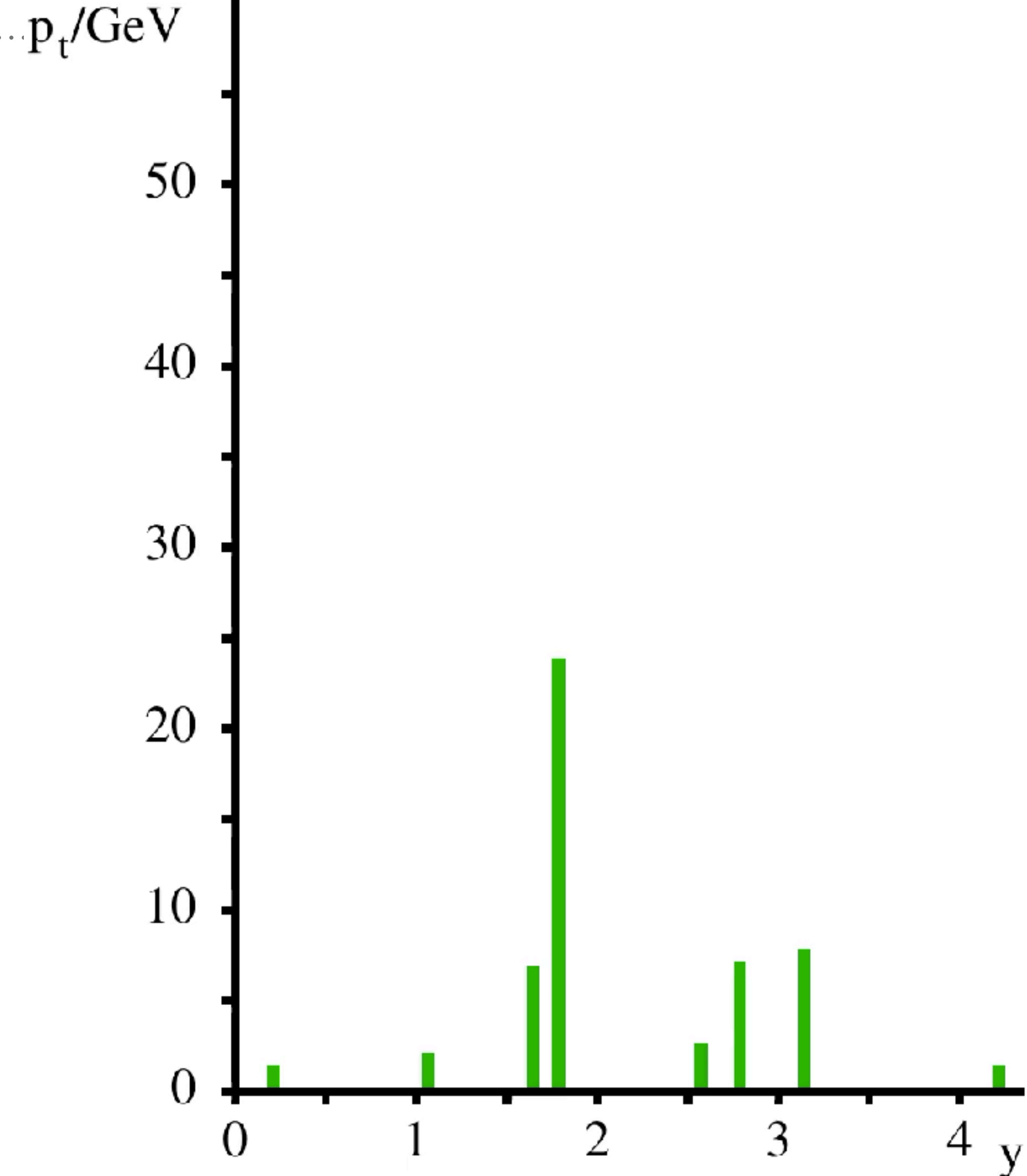
# event with Higgs & Z boson decays



# the Cambridge / Aachen (C/A) jet algorithm

1. Identify pair of particles,  $i$  &  $j$ , with smallest  $\Delta R_{ij}$
2. If  $\Delta R_{ij} < R$  (jet radius parameter)
  - A. recombine  $i$  &  $j$  into a single particle
  - B. loop back to step 1
3. Otherwise, stop the clustering

*Dokshitzer, Leder, Moretti & Webber '97*  
*Wobisch & Wengler '98*

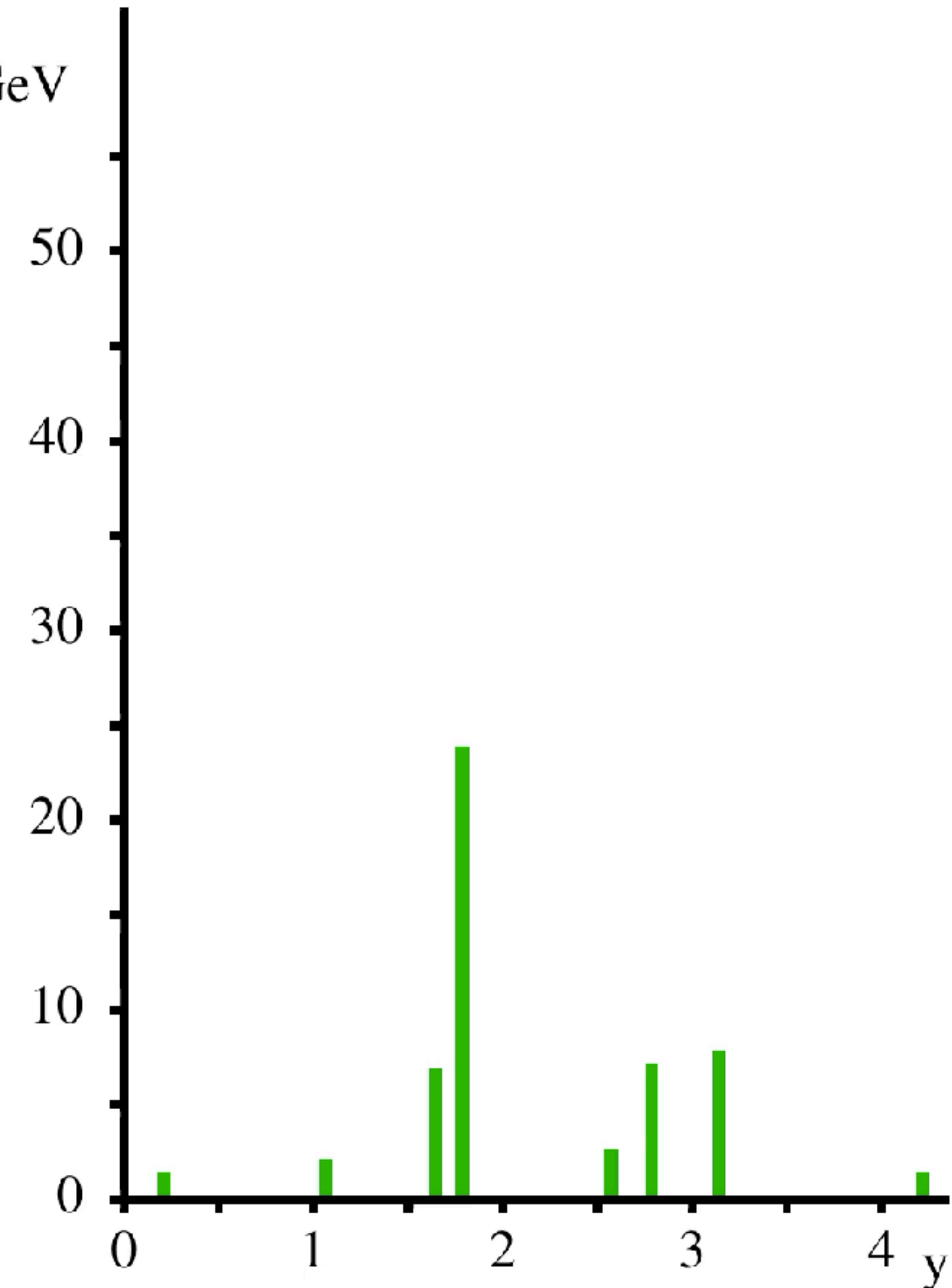


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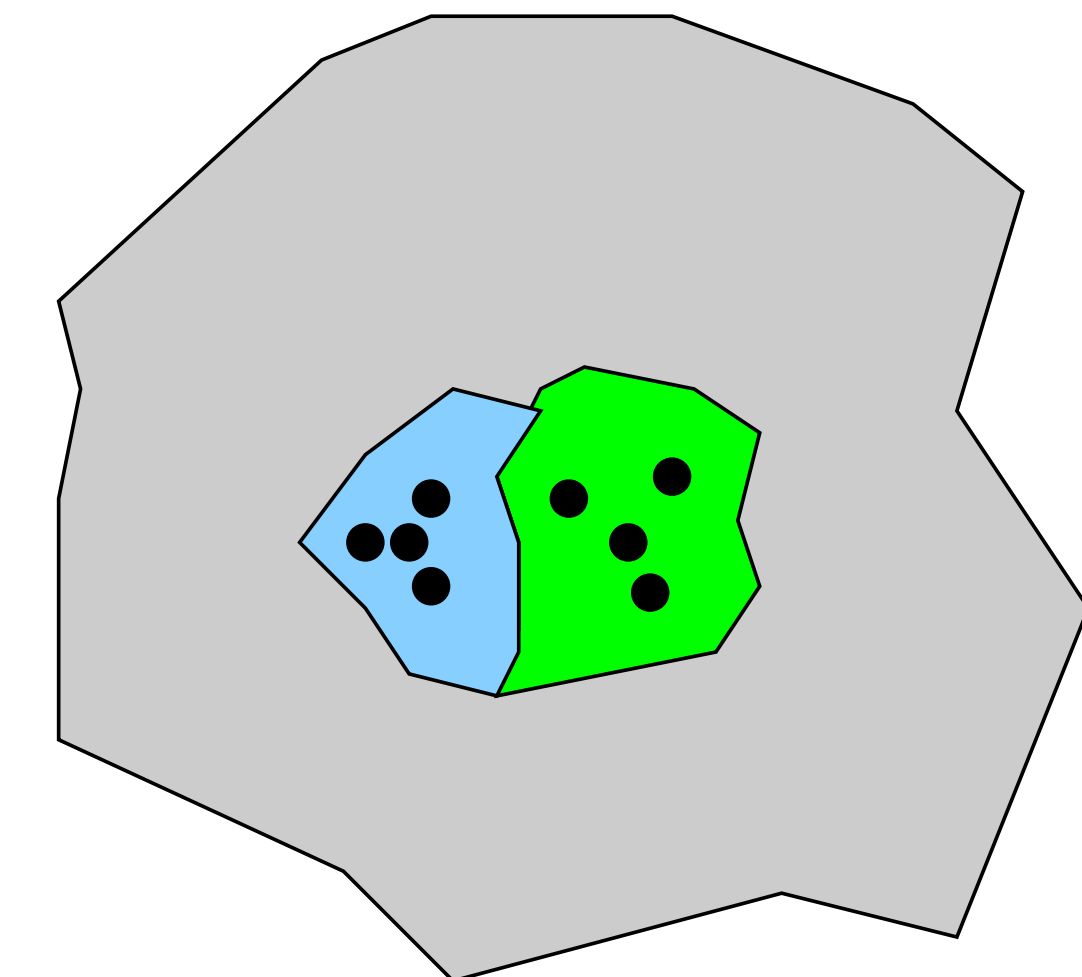
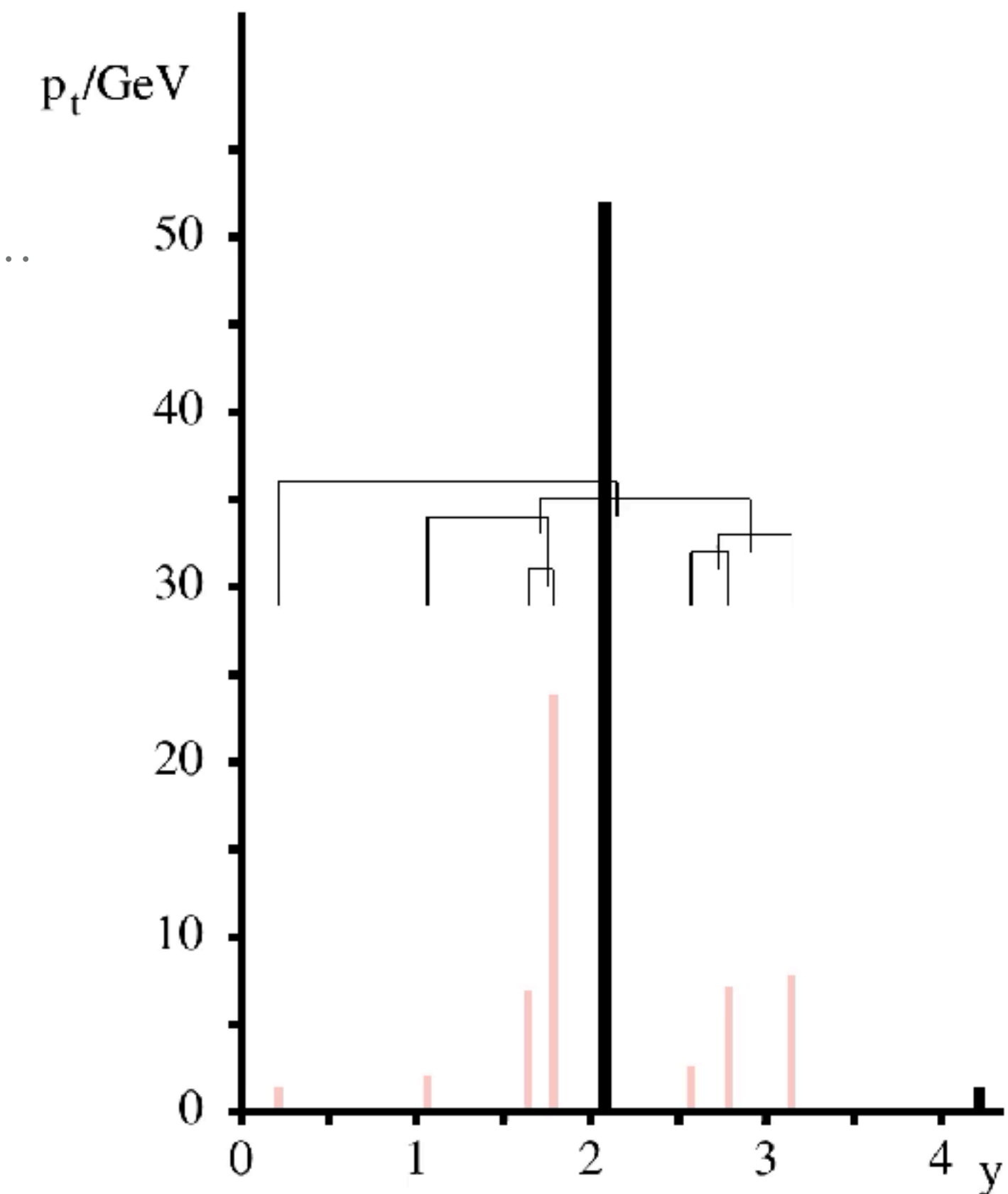
$p_t/\text{GeV}$



# A sequence of jet substructure tools taggers

- 1993:  $k_t$  declustering for boosted W's: [Seymour]
- 2002: Y-Splitter ( $k_t$  declustering with a cut) [Butterworth, Cox, Forshaw]
- 2008: Mass-Drop Tagger (C/A declustering with a  $k_t/m$  cut) [Butterworth, Davison, Rubin, GPS]
- 2013: Soft Drop,  $\beta=0$  [Dasgupta, Fregoso, Marzani, GPS]
- 2014: Soft Drop,  $\beta \neq 0$  [Larkoski, Marzani, Soyez, Thaler]

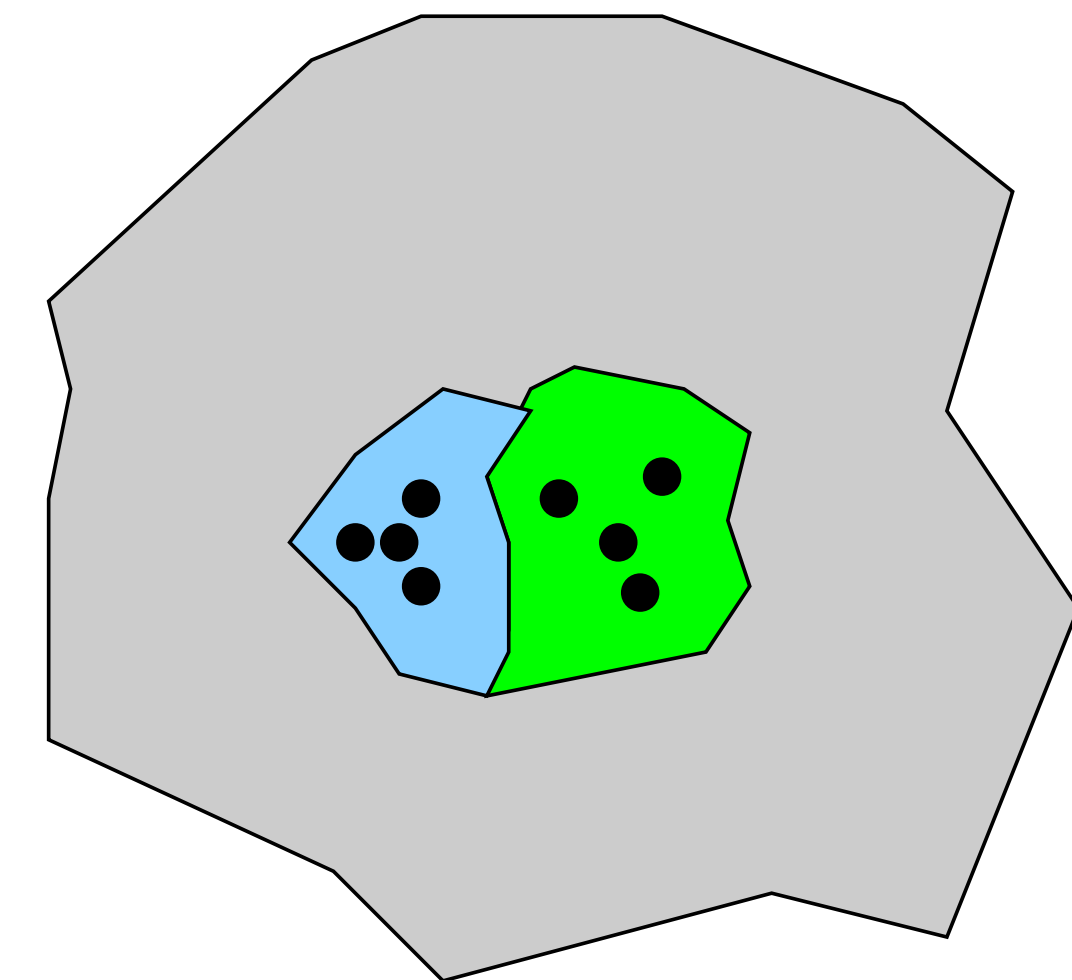
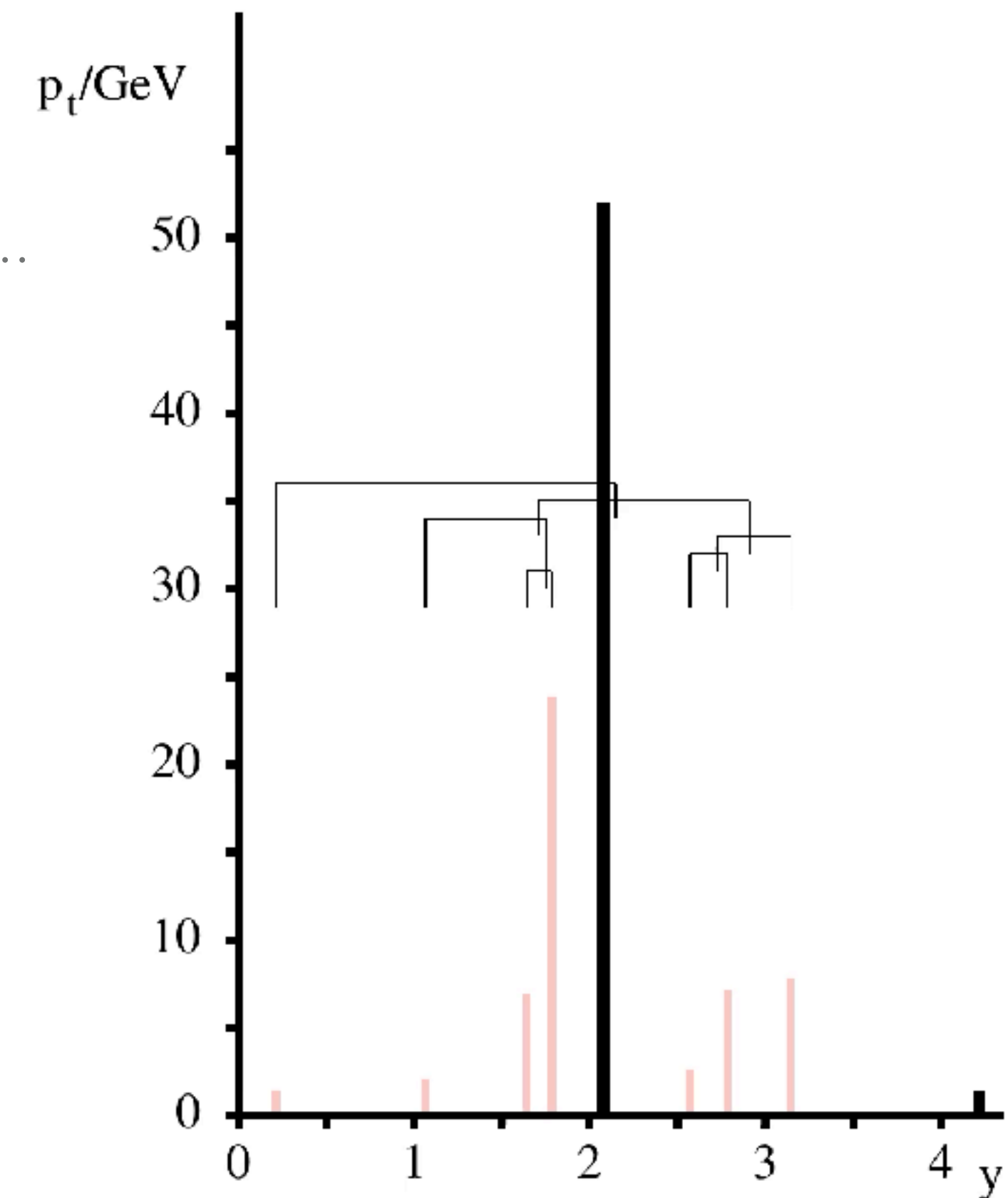
1. Undo last clustering of C/A jet into subjects 1, 2
2. Stop if  $z = \frac{\min(p_{t1}, p_{t2})}{p_{t1} + p_{t2}} \left( \frac{\Delta R_{12}}{R} \right)^\beta > z_{\text{cut}}$
3. Else discard softer branch, repeat step 1 with harder branch



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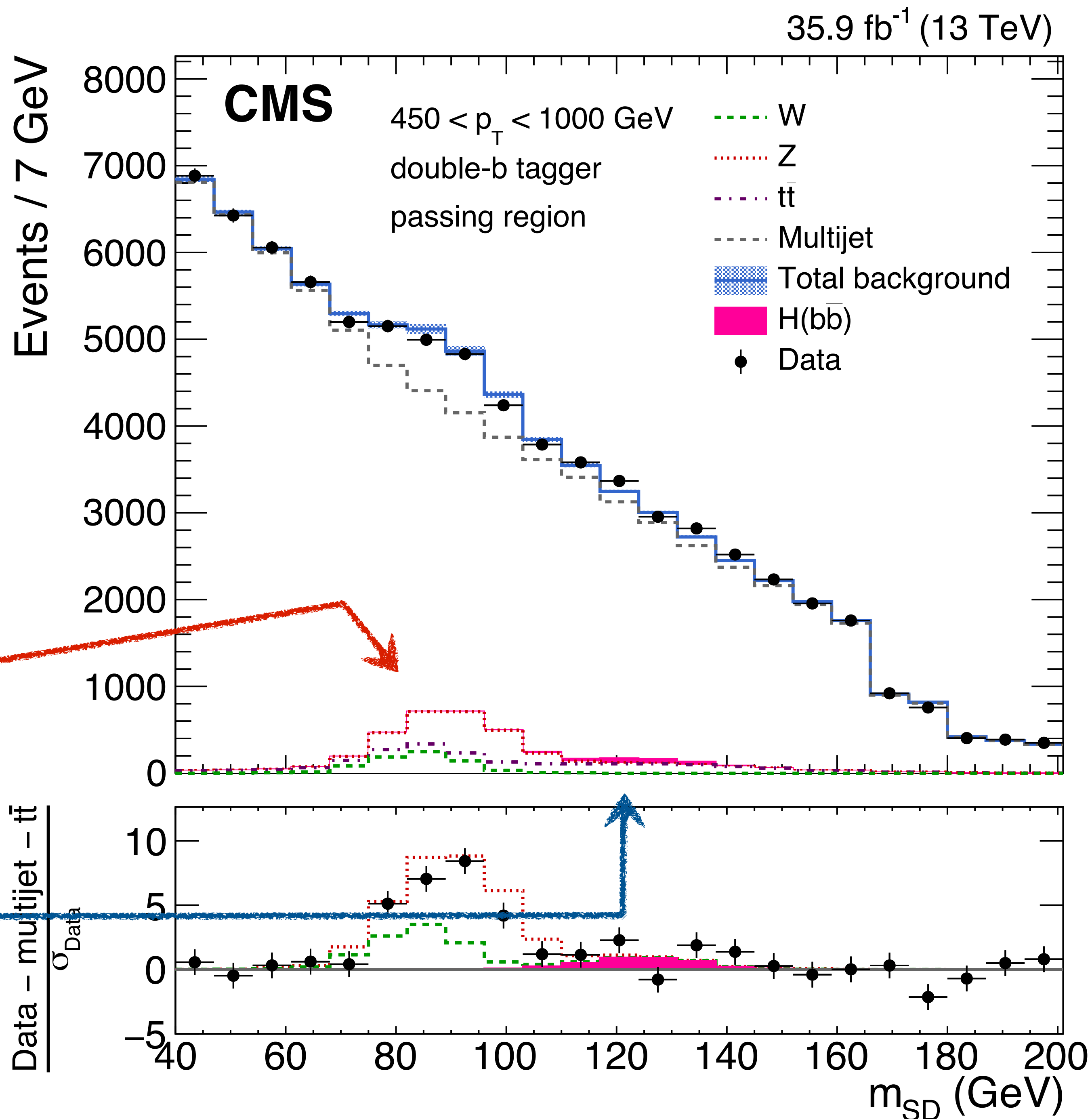
# Soft Drop & high $p_T$ Higgs

We wouldn't trust electromagnetism if we'd only tested at one length/momentum scale.

New Higgs interactions need testing at both low and (here) high momenta.

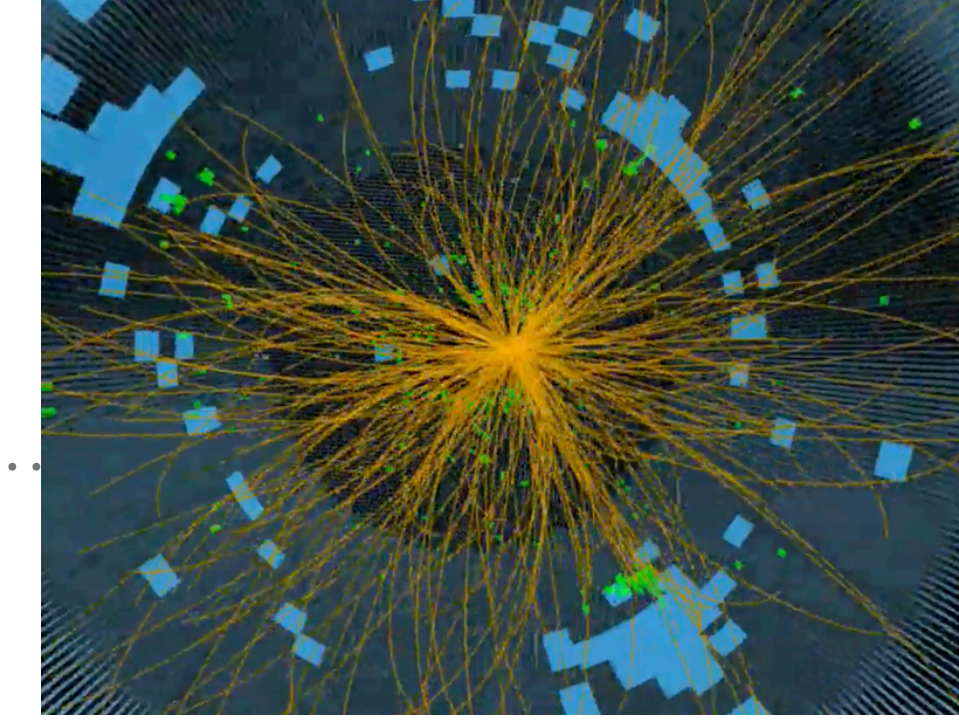
**high- $p_T$   $Z \rightarrow bb$  ( $5\sigma$ )**

**high- $p_T$   $H \rightarrow bb$  ( $\sim 1\sigma$ )**

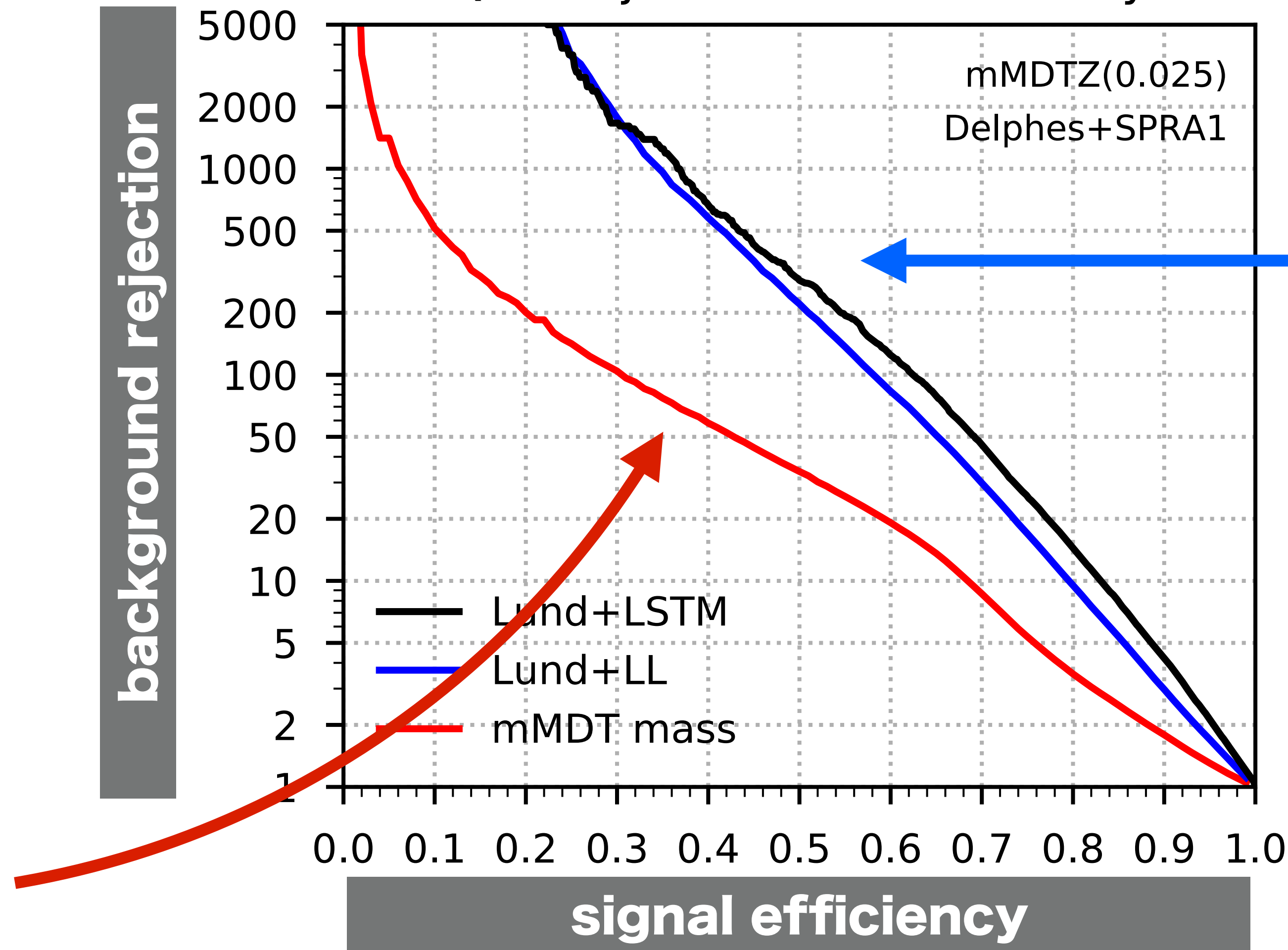




# using full event information for H/etc. boson tagging



QCD rejection v. W efficiency



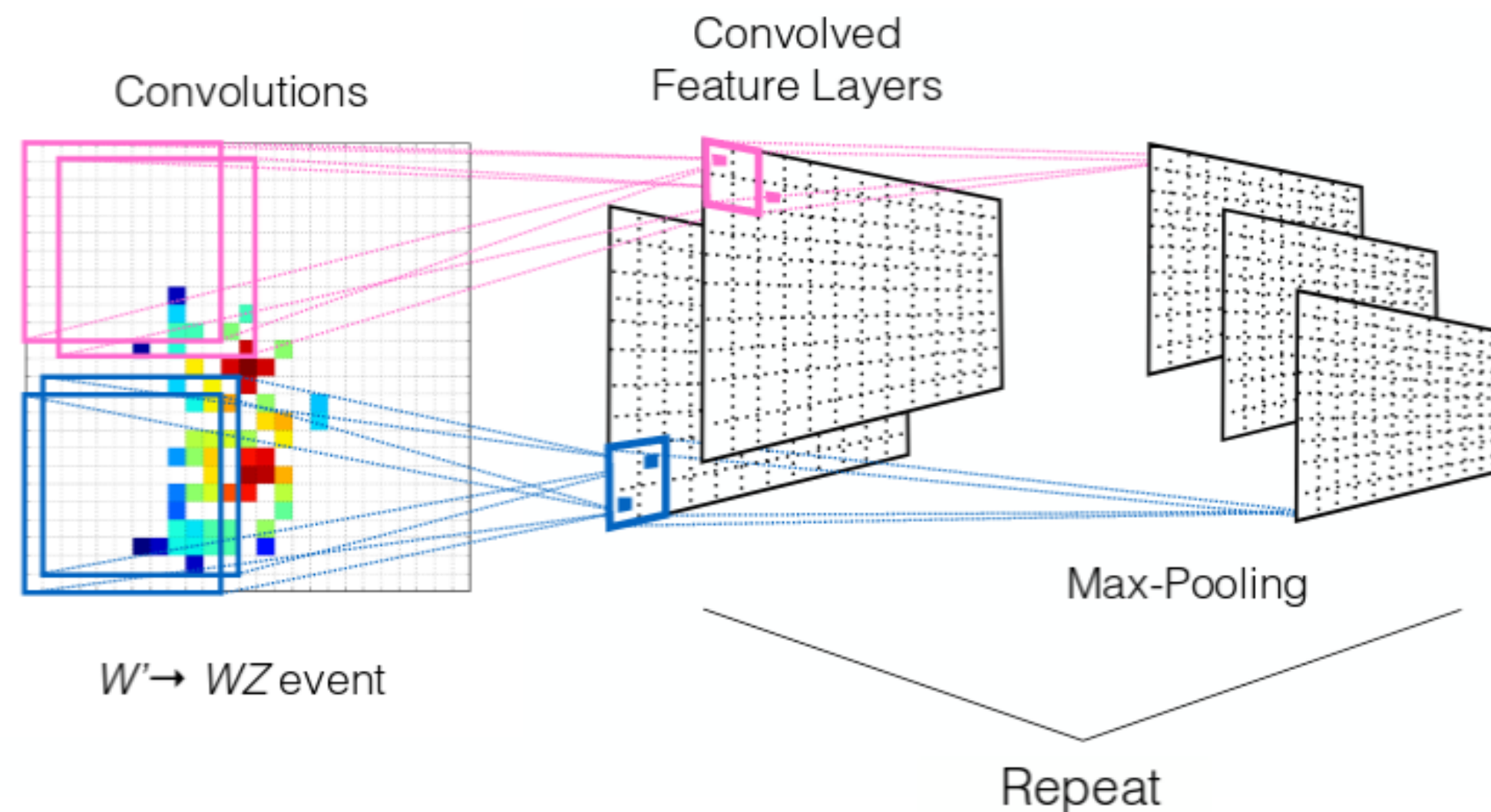
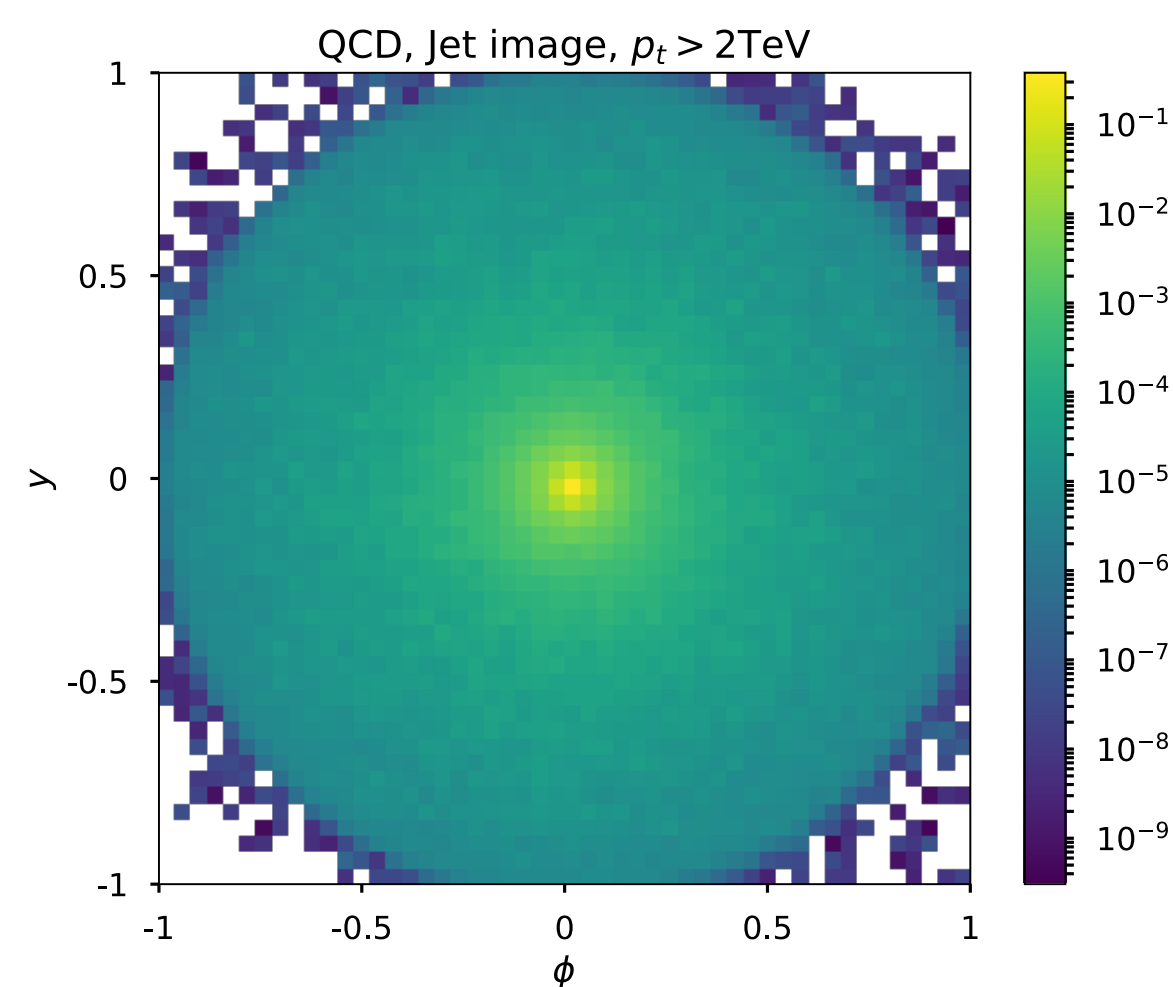
*QCD rejection with just jet mass (SD/mMDT) i.e. 2008 tools & their descendants*

*QCD rejection with use of full jet substructure (2018 tools) 5-10x better*

*First started to be exploited by Thaler & Van Tilburg with "N-subjettiness" (2010/11)*

# Convolutional neural networks and jet images

- ▶ Project a jet onto a fixed  $n \times n$  pixel image in rapidity-azimuth, where each pixel intensity corresponds to the momentum of particles in that cell.
- ▶ Can be used as input for classification methods used in computer vision, such as deep convolutional neural networks.



[Cogan, Kagan, Strauss, Schwartzman [JHEP 1502 \(2015\) 118](#)]

[de Oliveira, Kagan, Mackey, Nachman, Schwartzman [JHEP 1607 \(2016\) 069](#)]

**powerful**  
**but black box**

# the “Lund plane”

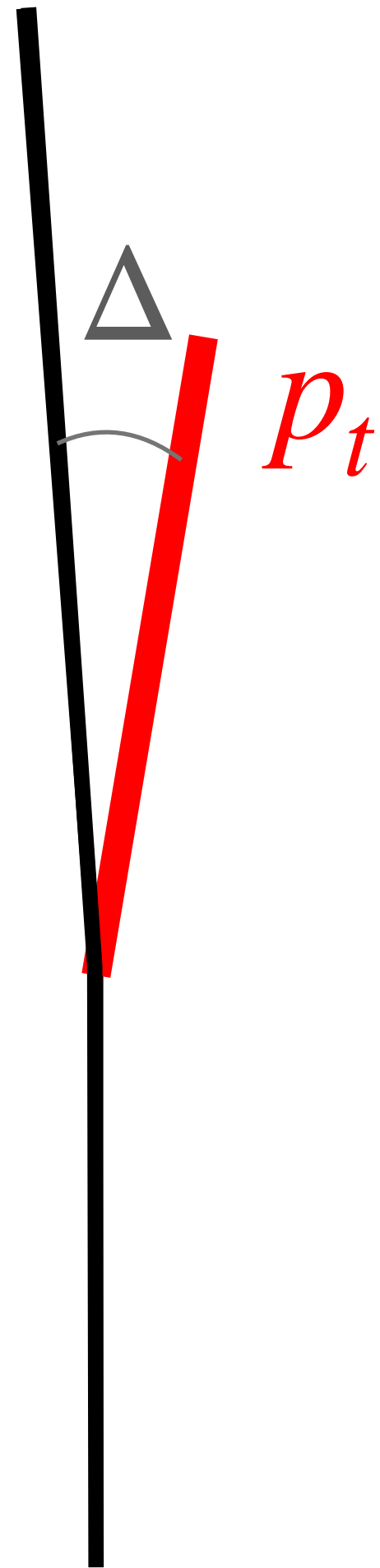
---

*can we construct observables that are*

- (a) **transparent** in terms of the physical info they extract?*
- (b) close to **optimal** for multivariate techniques & machine-learning?*

# Phase space: two key variables (+ azimuth)

---



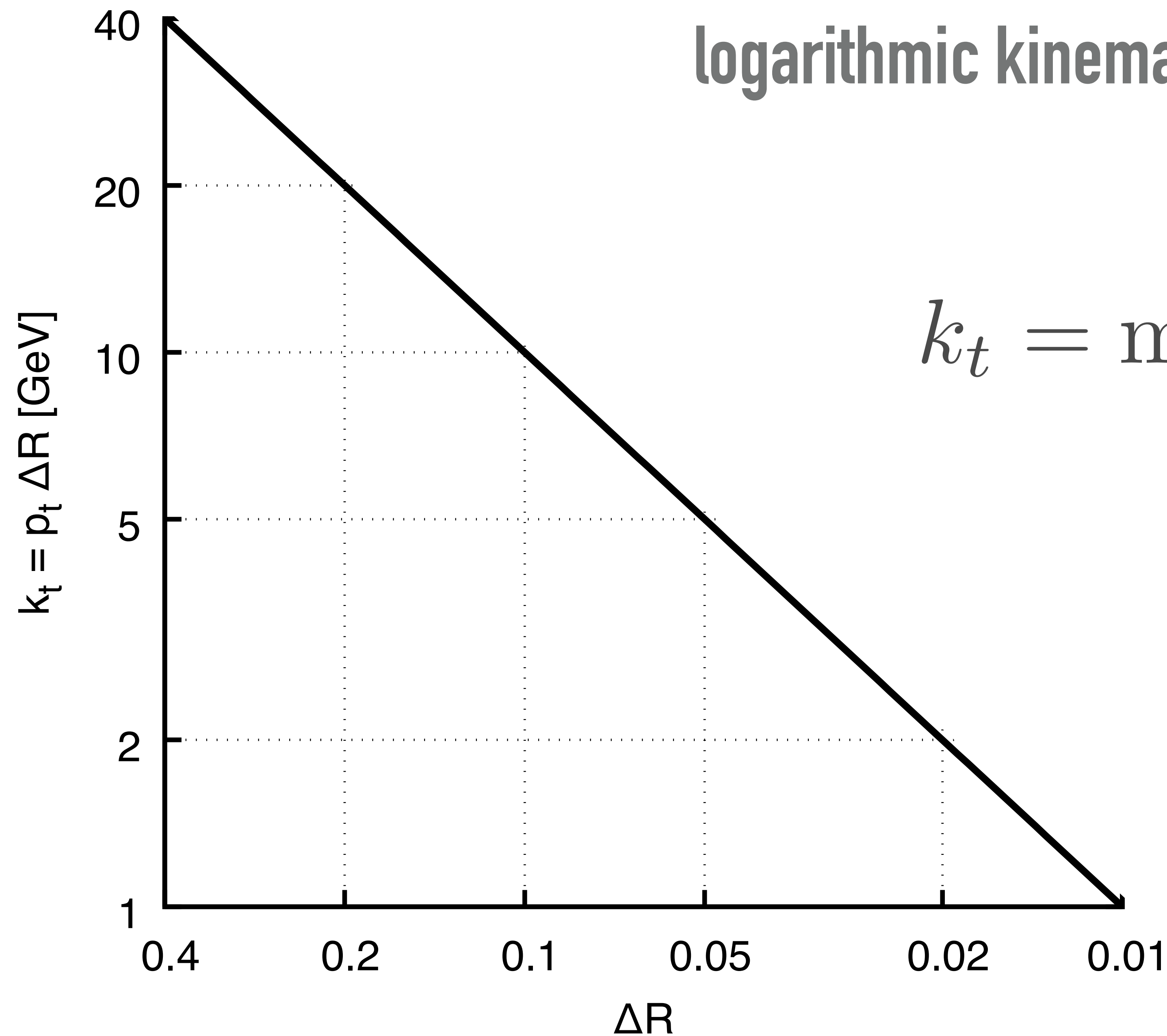
$\Delta R$  (or just  $\Delta$ )

*opening angle of a splitting*

$$k_t = p_t \Delta$$

*$p_t$  (or  $p_\perp$ ) is transverse momentum wrt beam*

*$k_t$  is  $\sim$  transverse momentum wrt jet axis*



logarithmic kinematic plane whose two variables are

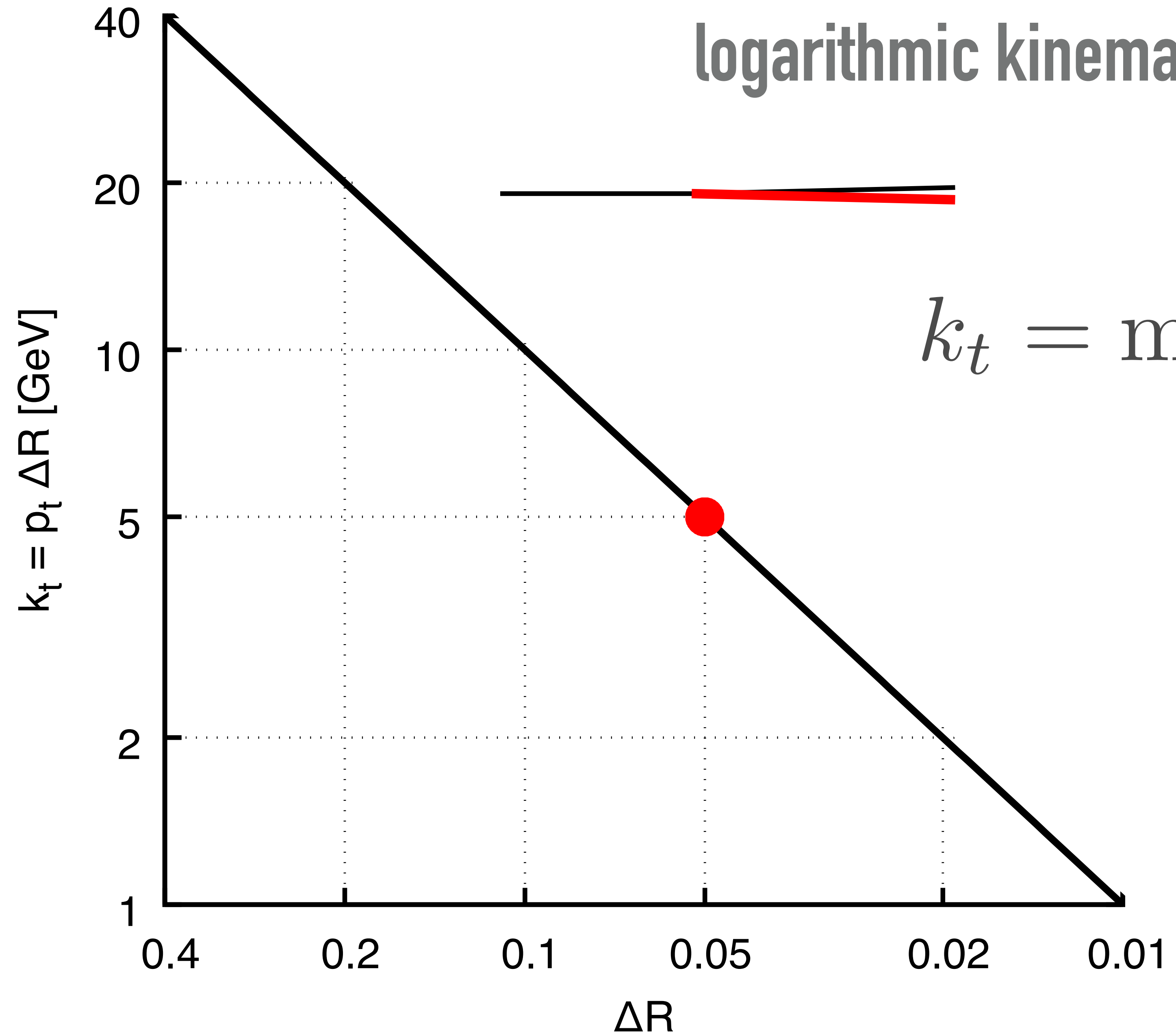
$$\Delta R_{ij}$$

$$k_t = \min(p_{ti}, p_{tj}) \Delta R_{ij}$$

Introduced for understanding  
Parton Shower Monte Carlos by  
B. Andersson, G. Gustafson L.  
Lonnblad and Pettersson, 1989

**The Lund Plane**

jet with  $R = 0.4$ ,  $p_t = 200$  GeV



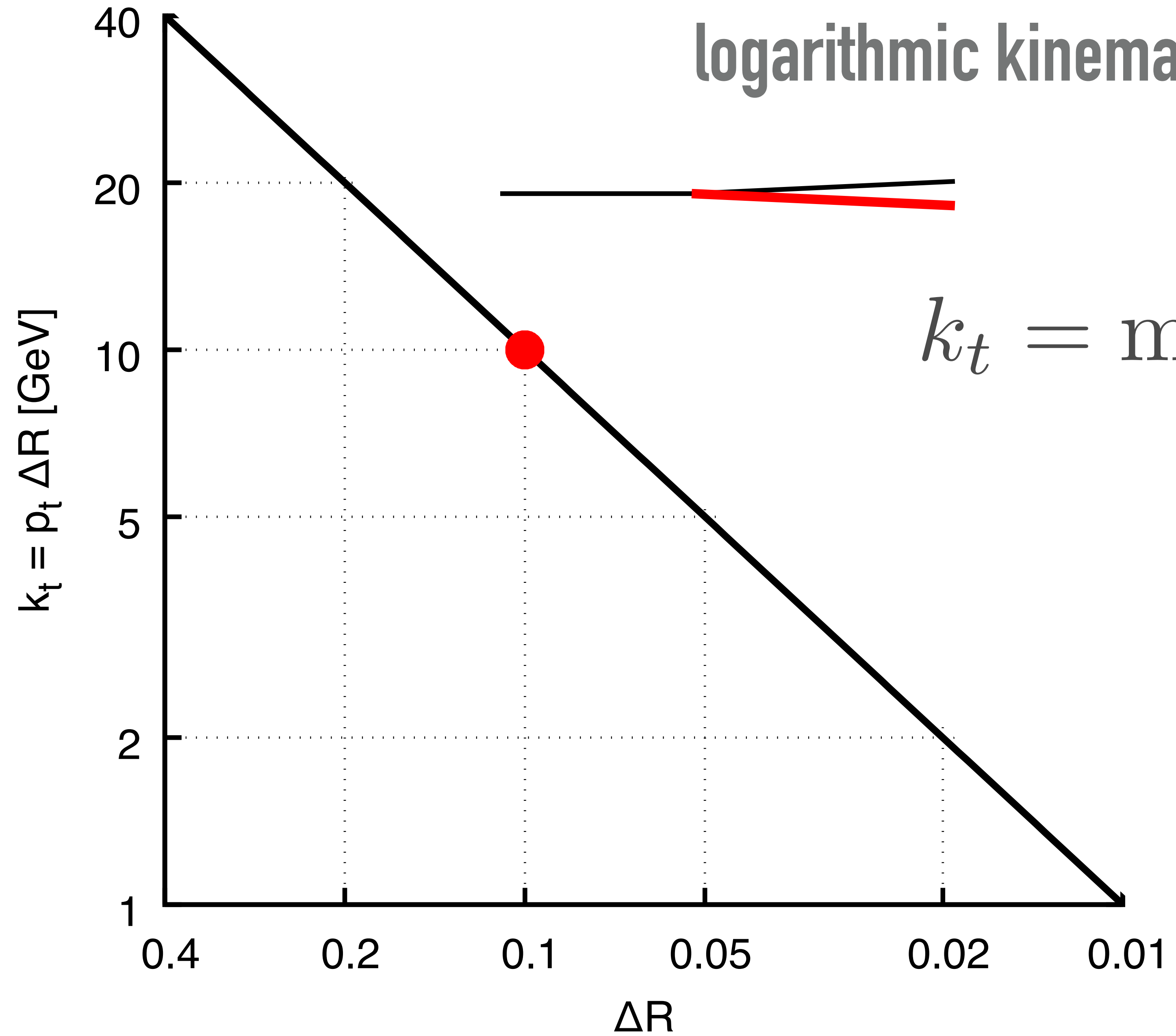
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# The Lund Plane



logarithmic kinematic plane whose two variables are

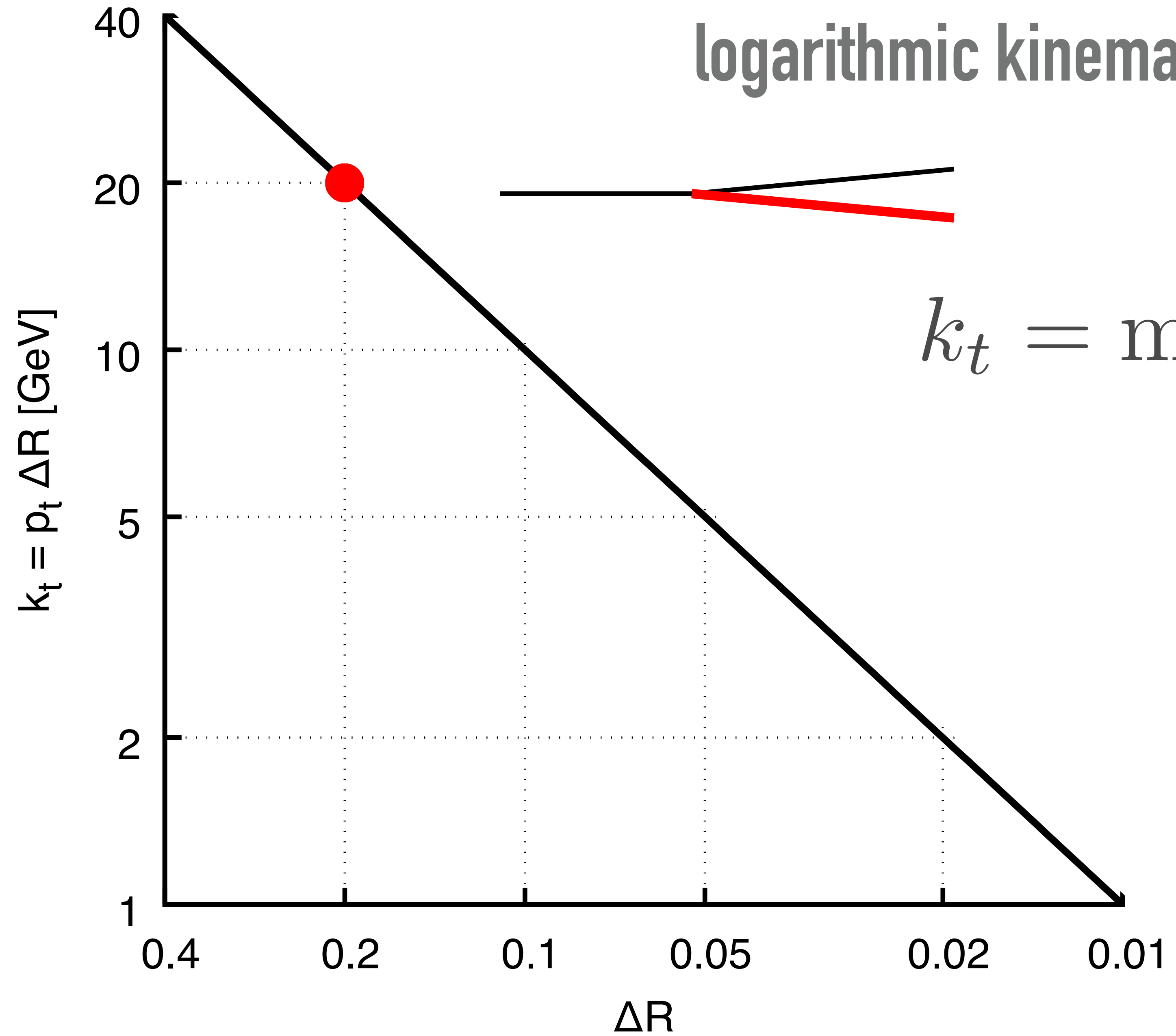
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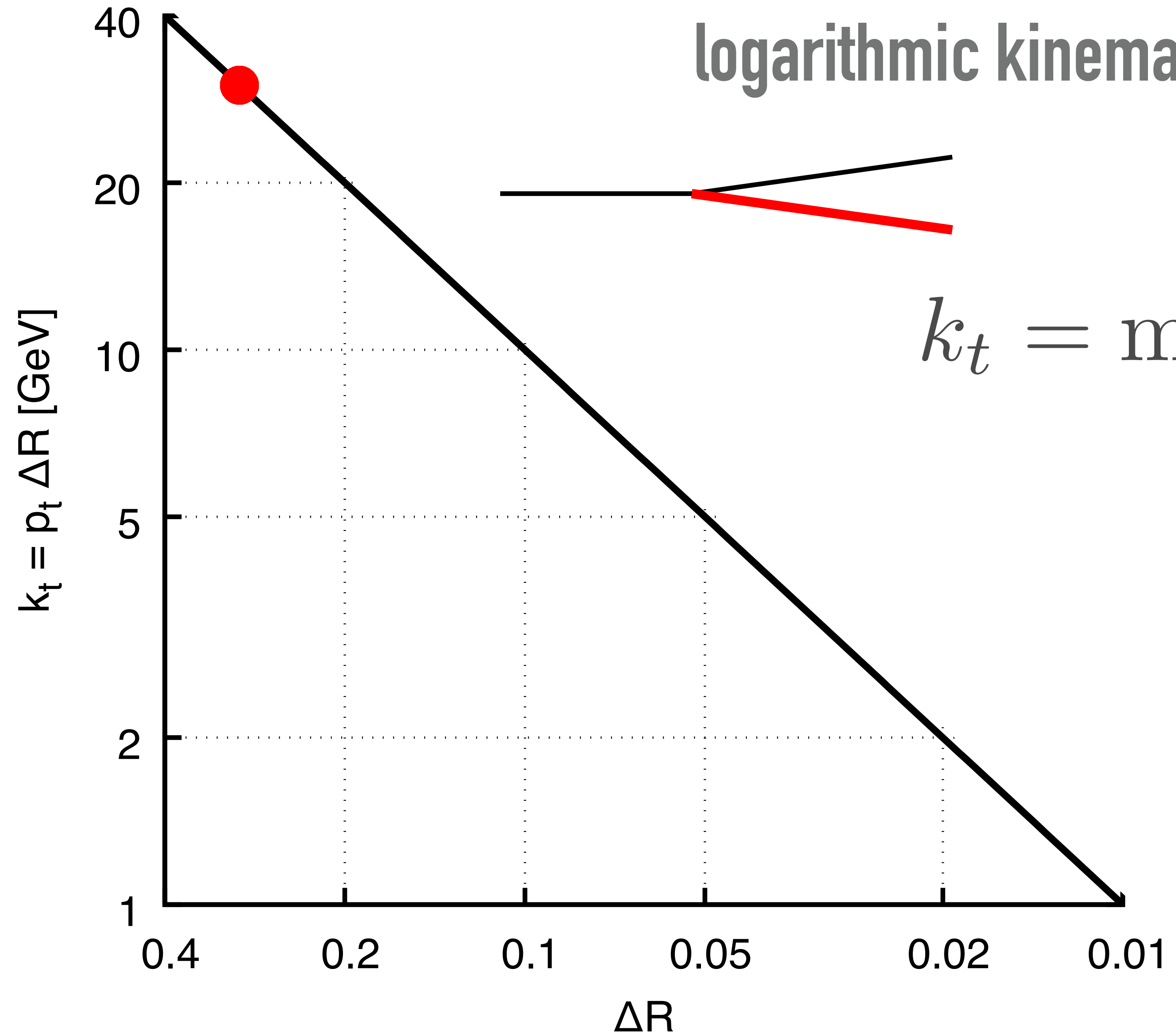
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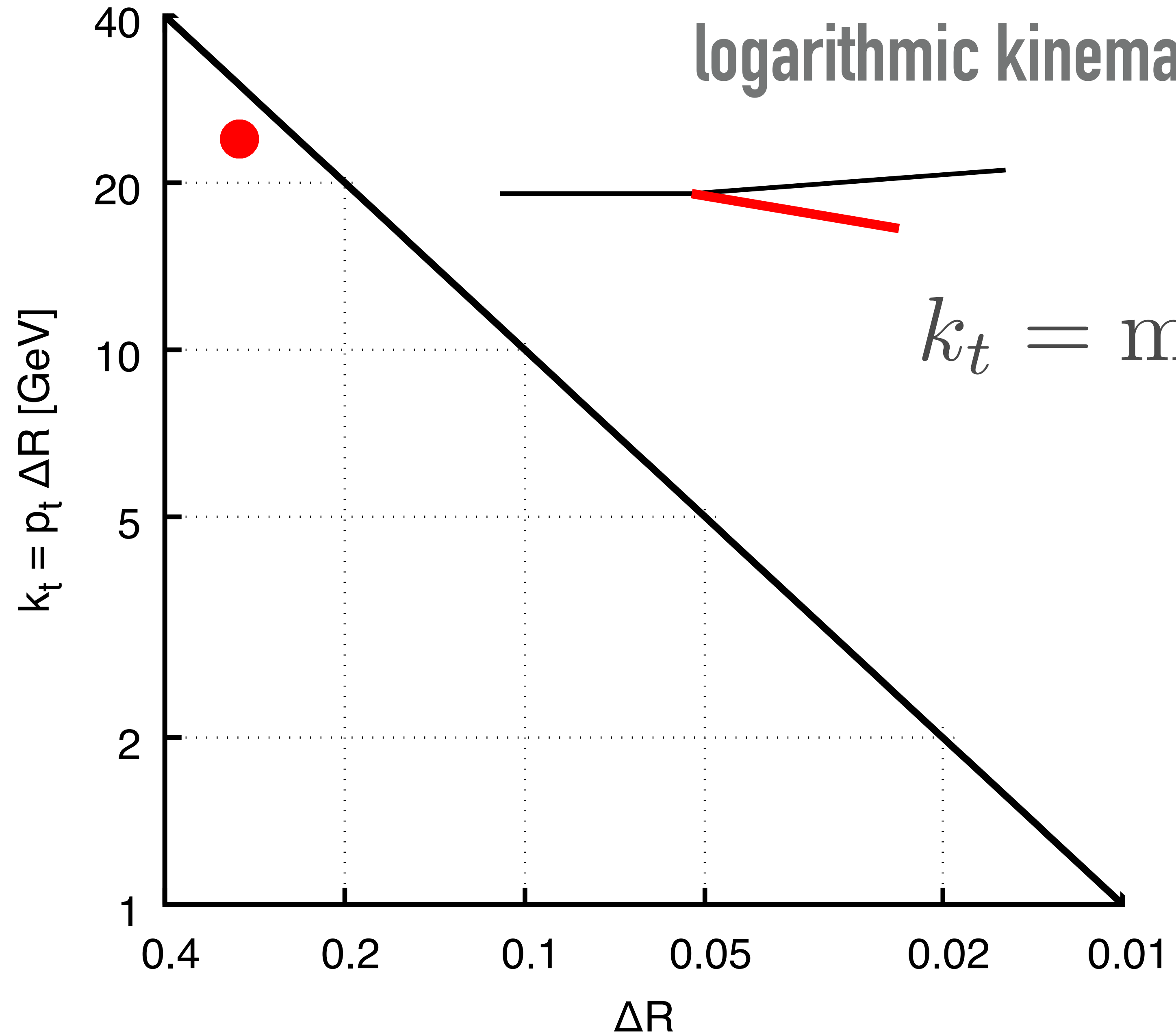
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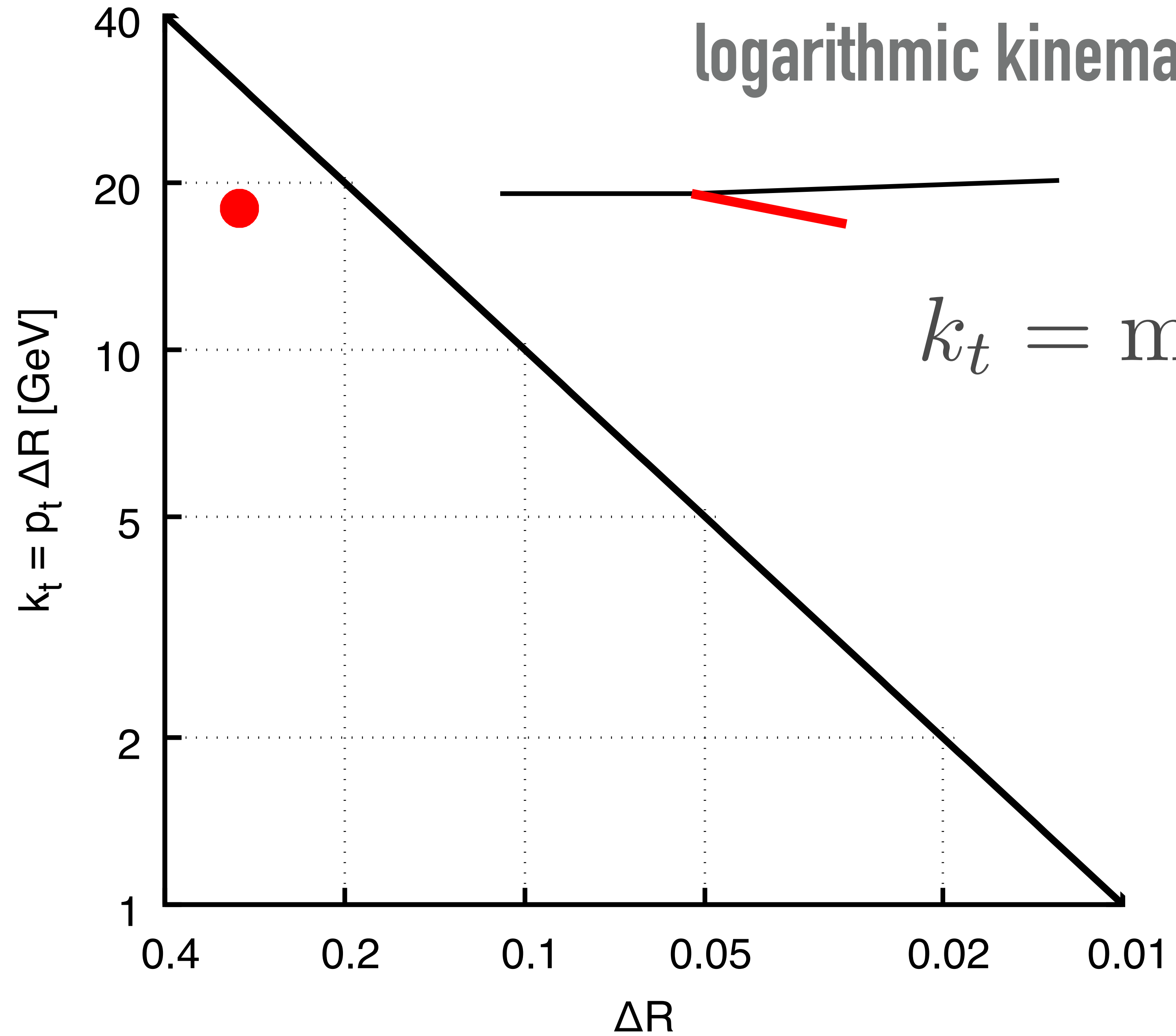
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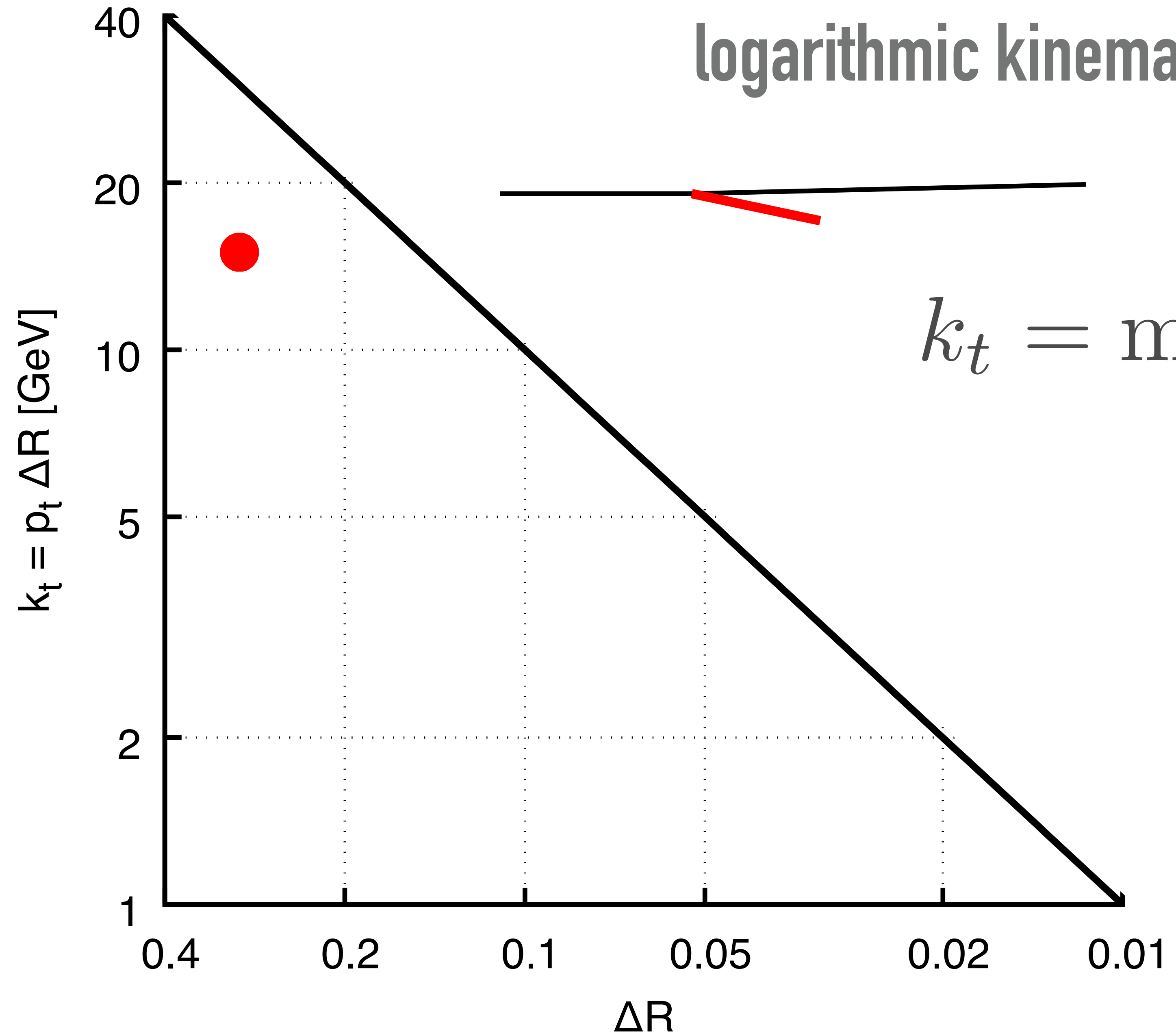
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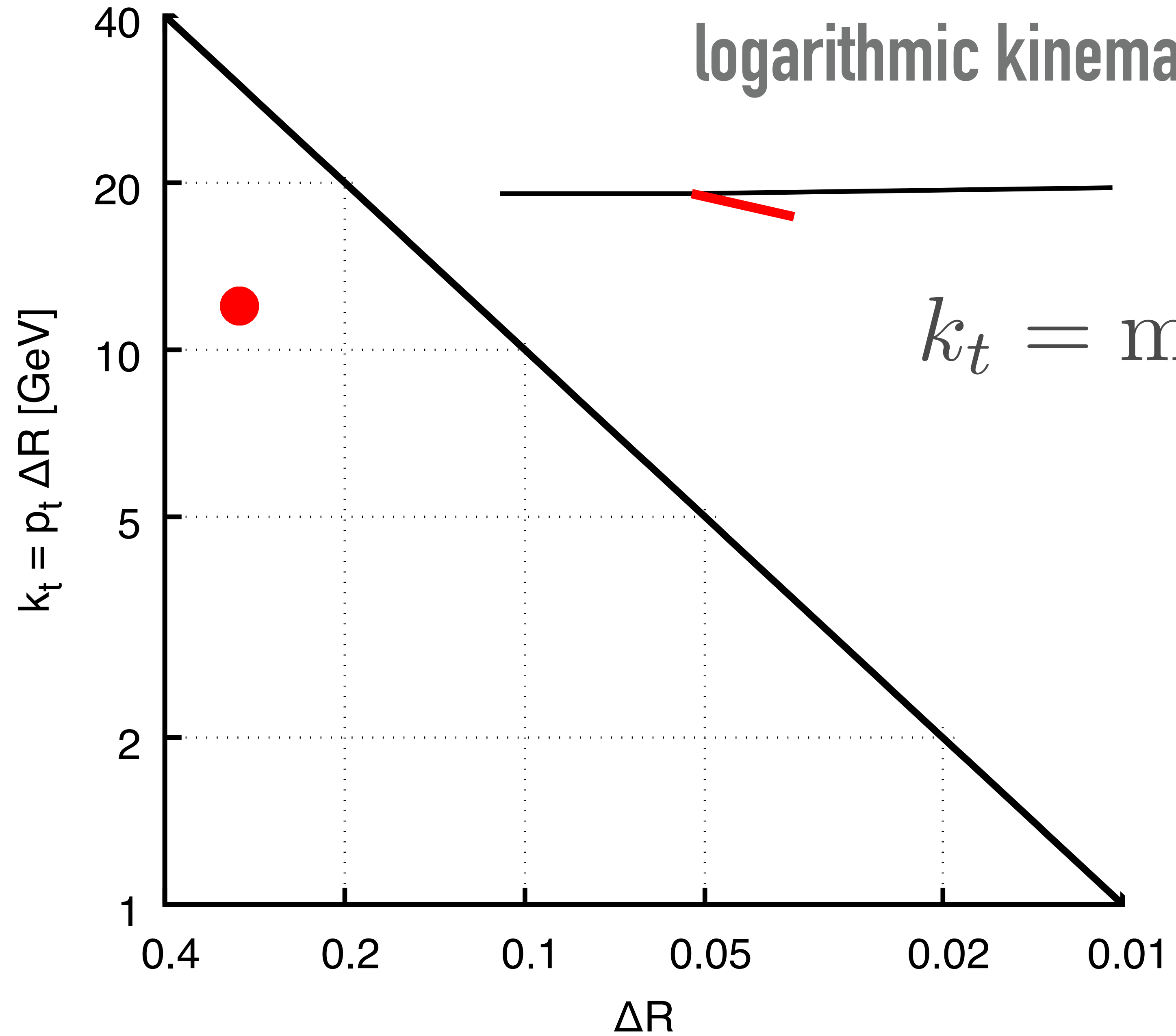
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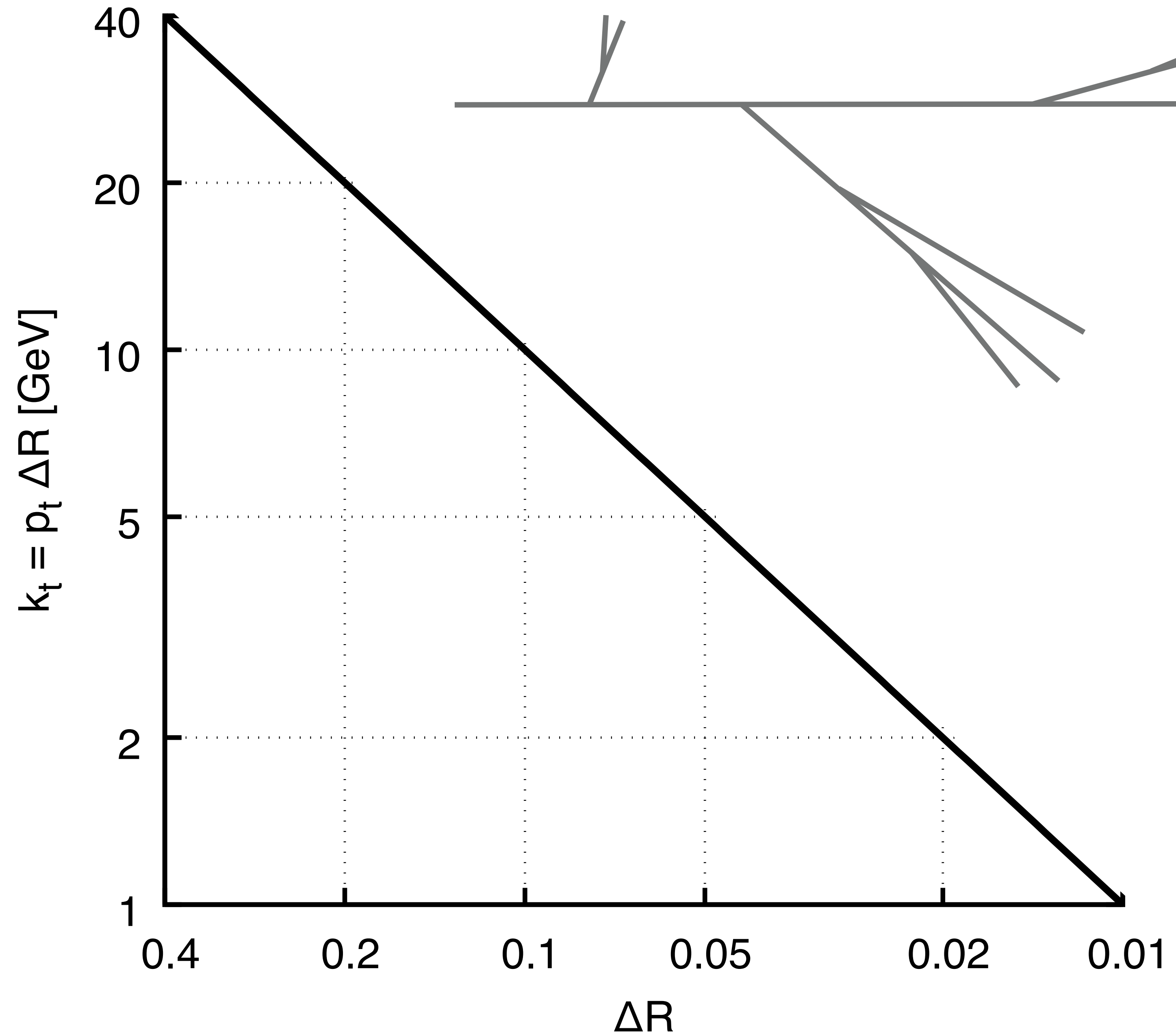
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# The Lund Plane

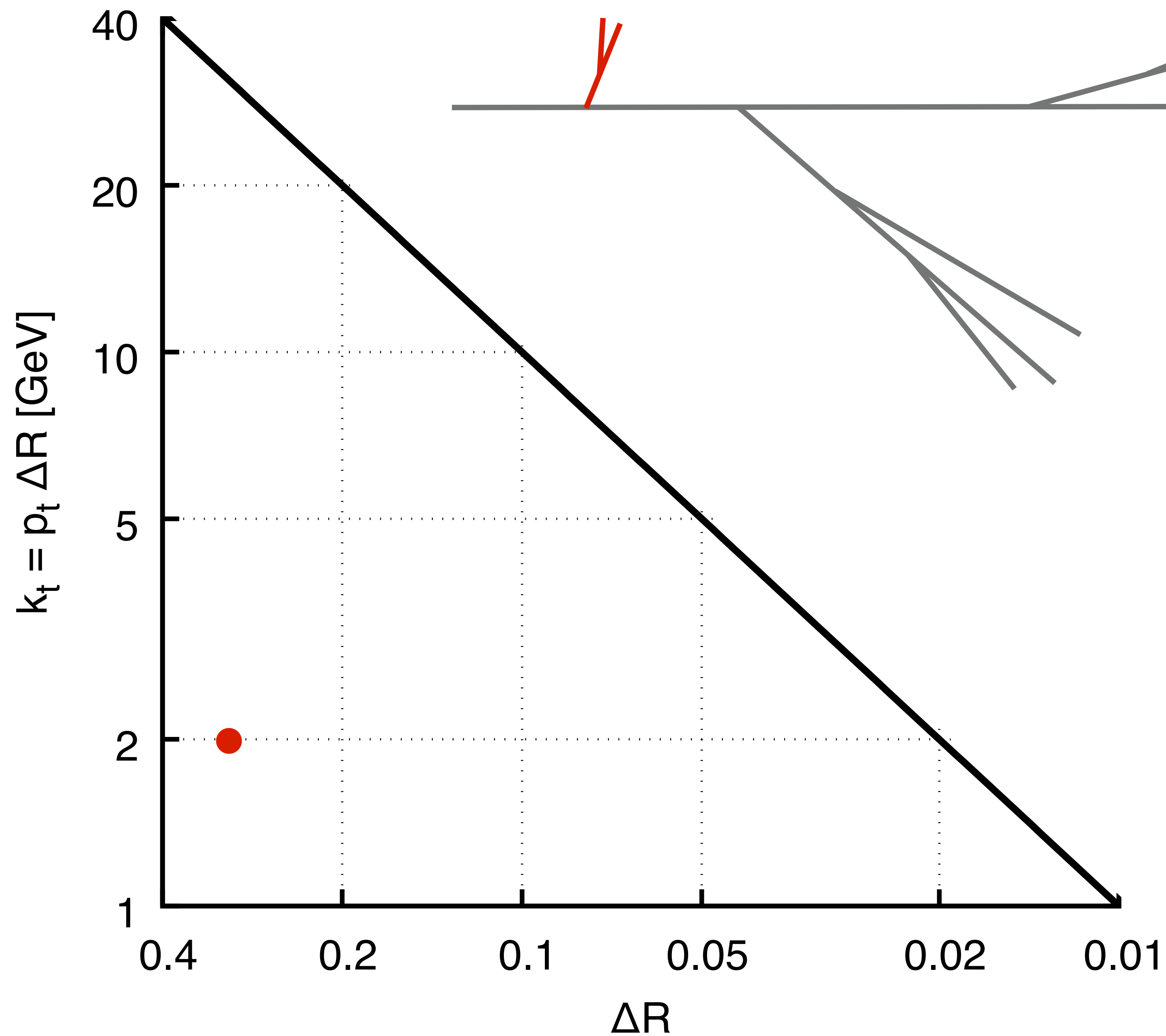
jet with  $R = 0.4$ ,  $p_t = 200$  GeV



**decluster a C/A jet:  
at each step record  $\Delta R, k_t$   
as a point in the Lund plane  
repeatedly follow harder branch**

5th heavy-ion workshop @ CERN, [1808.03689](#)  
Dreyer, Soyez & GPS, [1807.04758](#) (for pp applications)

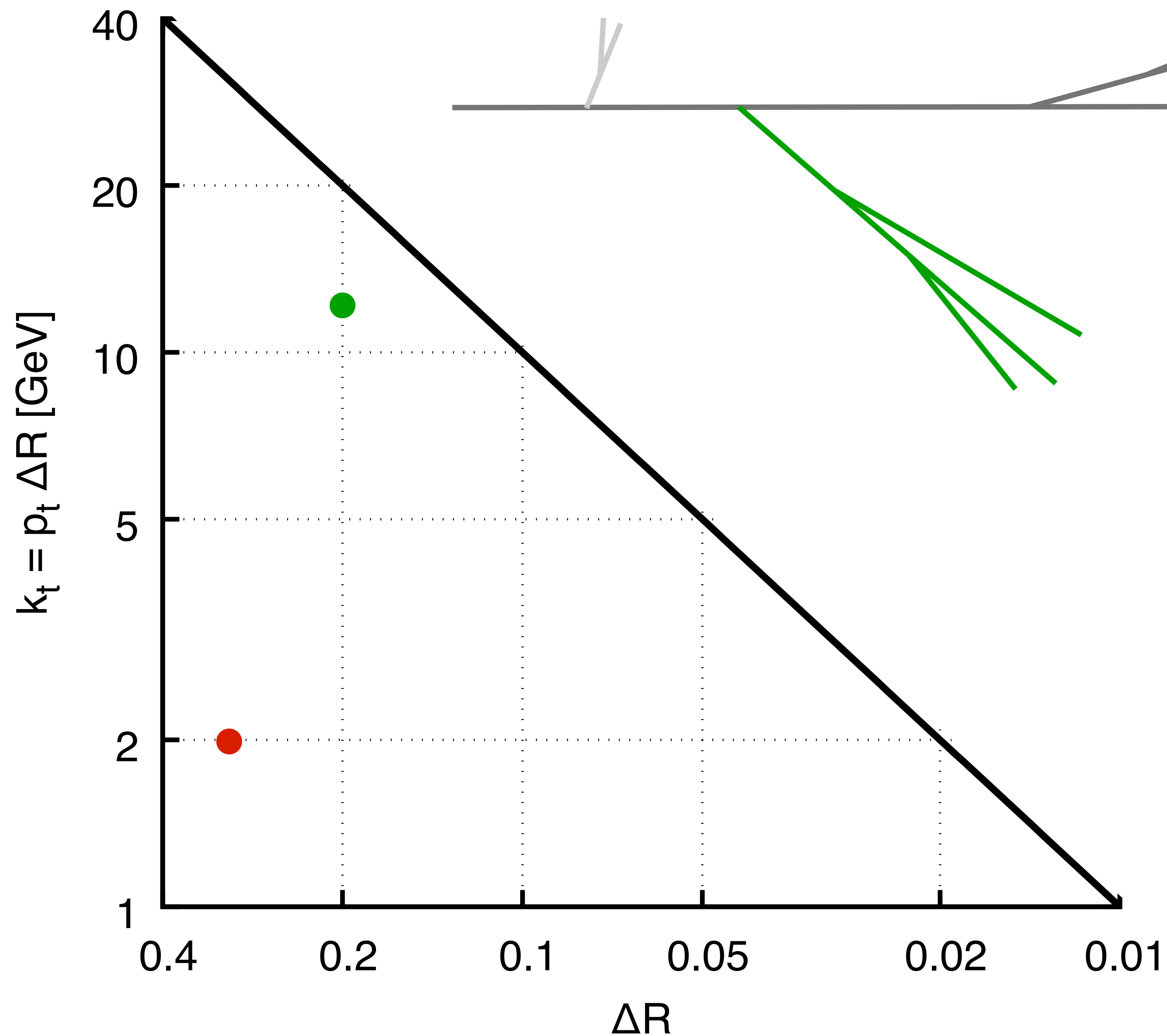
**constructing the Lund plane**



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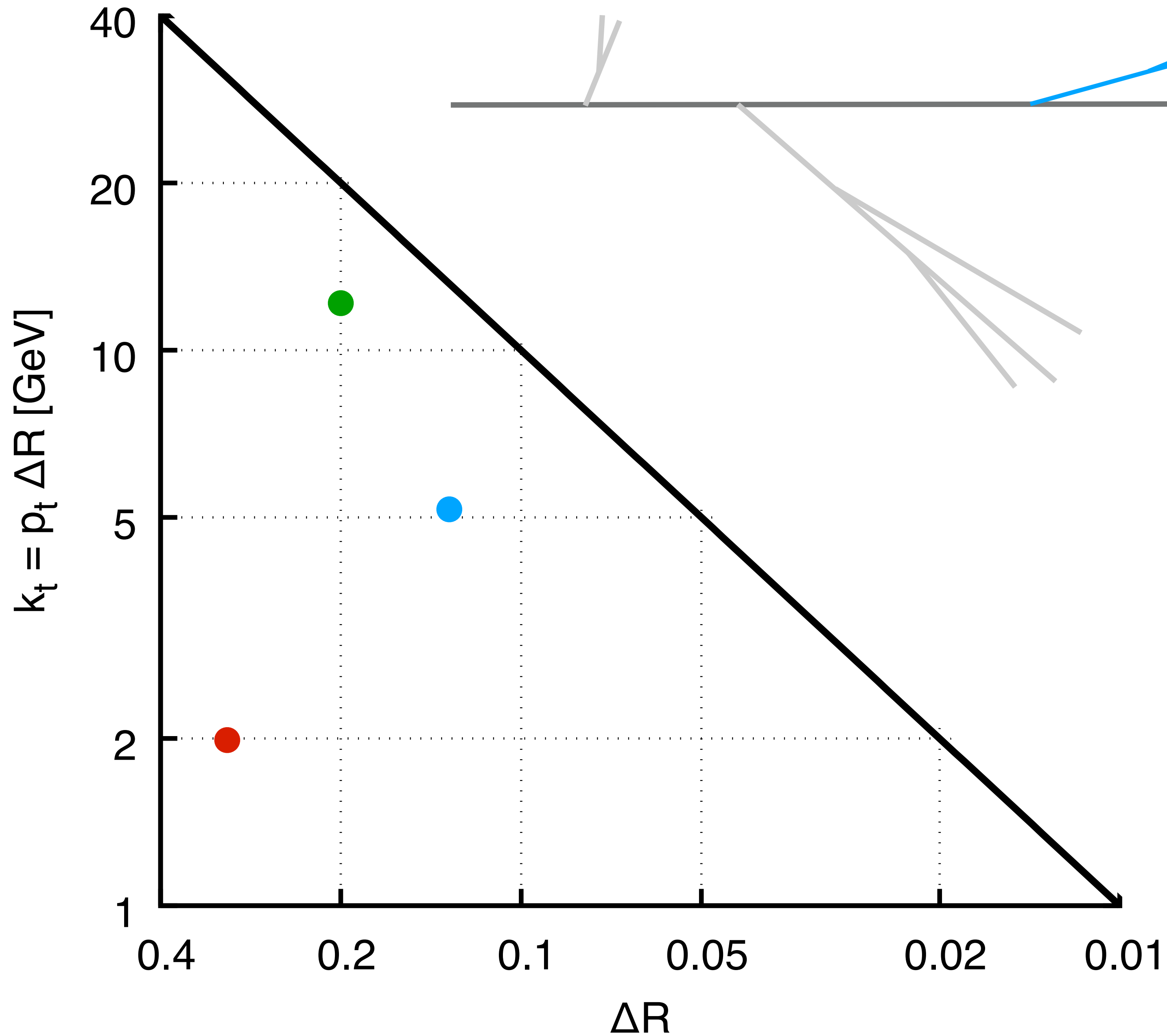


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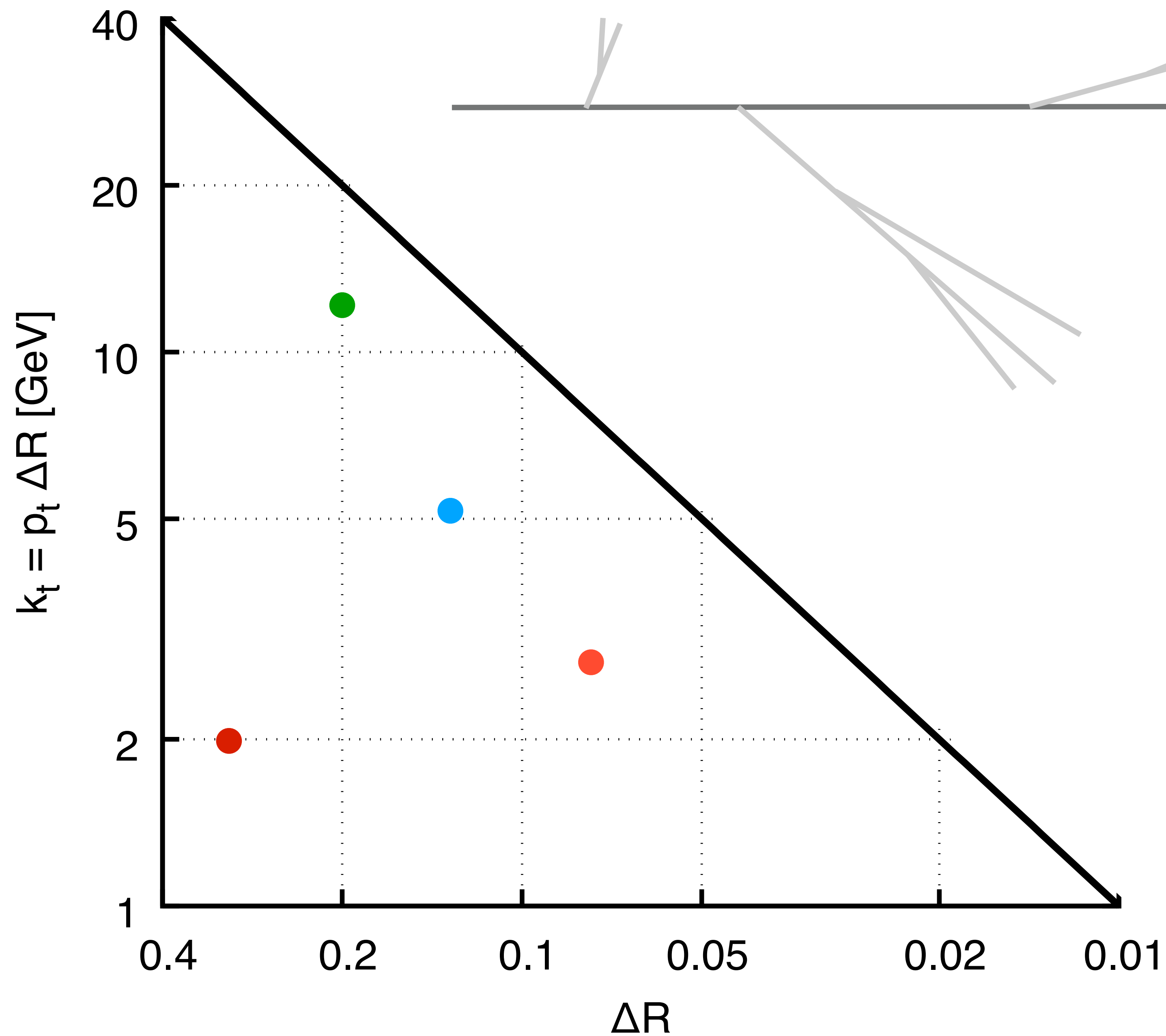




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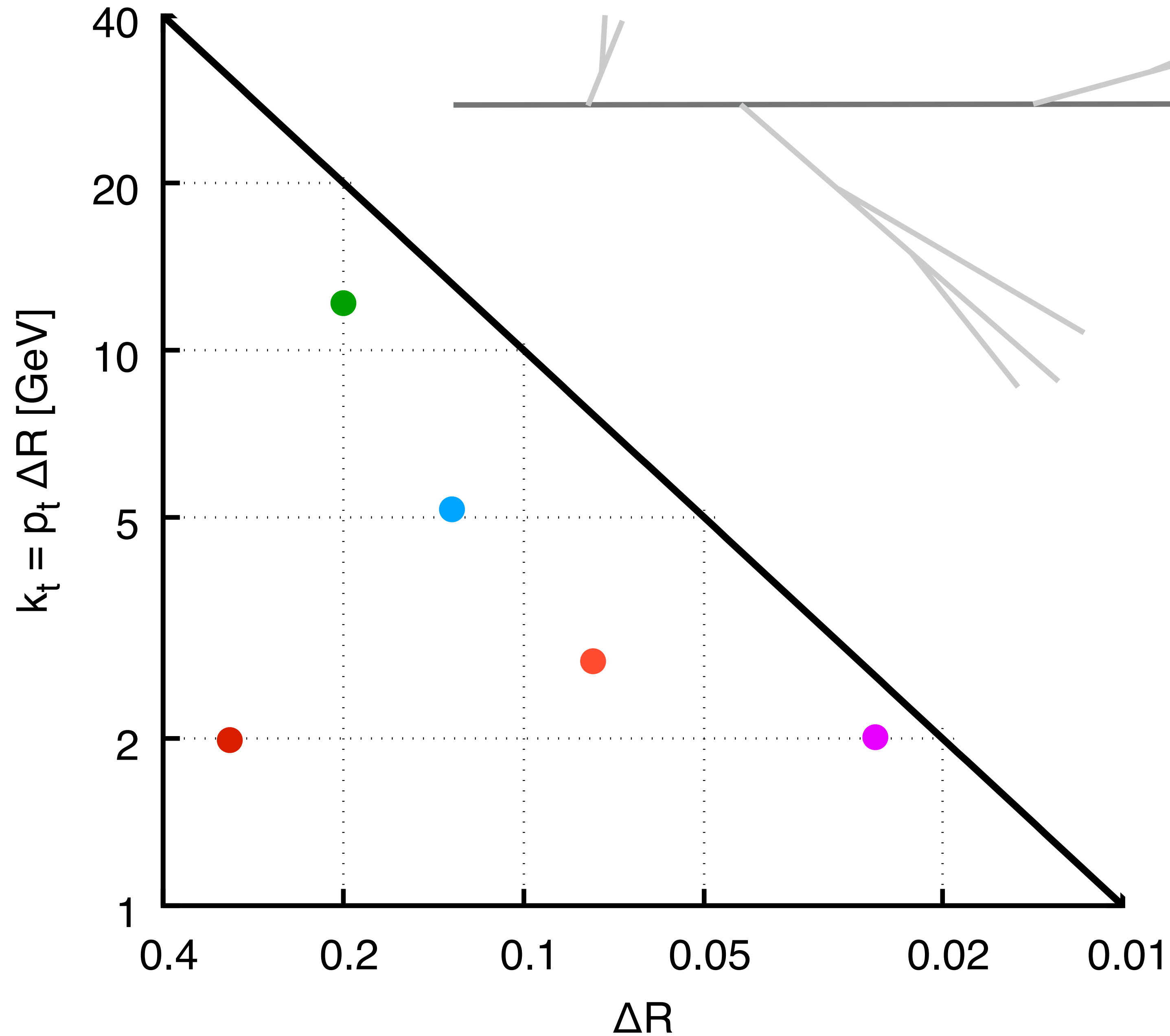
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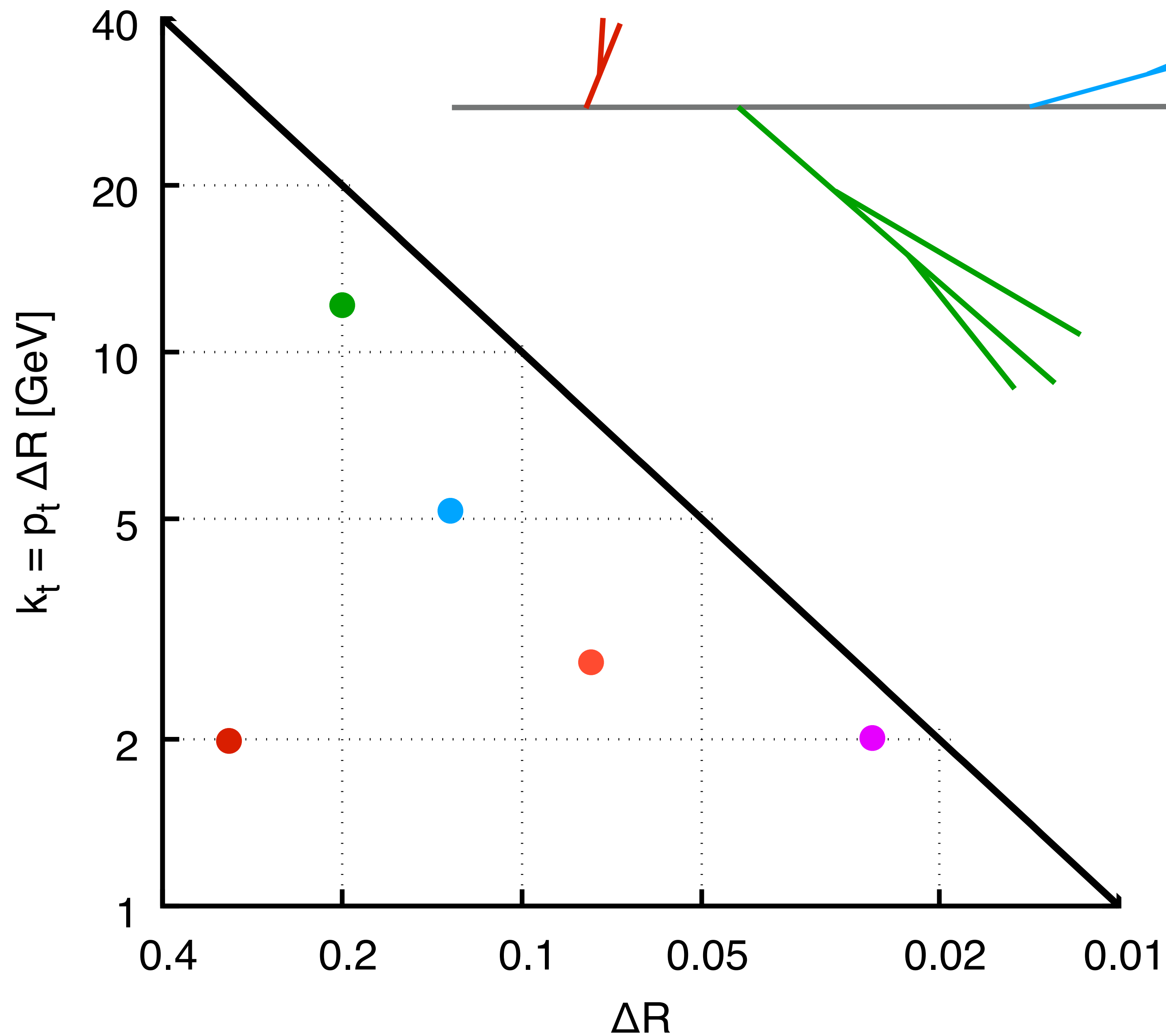
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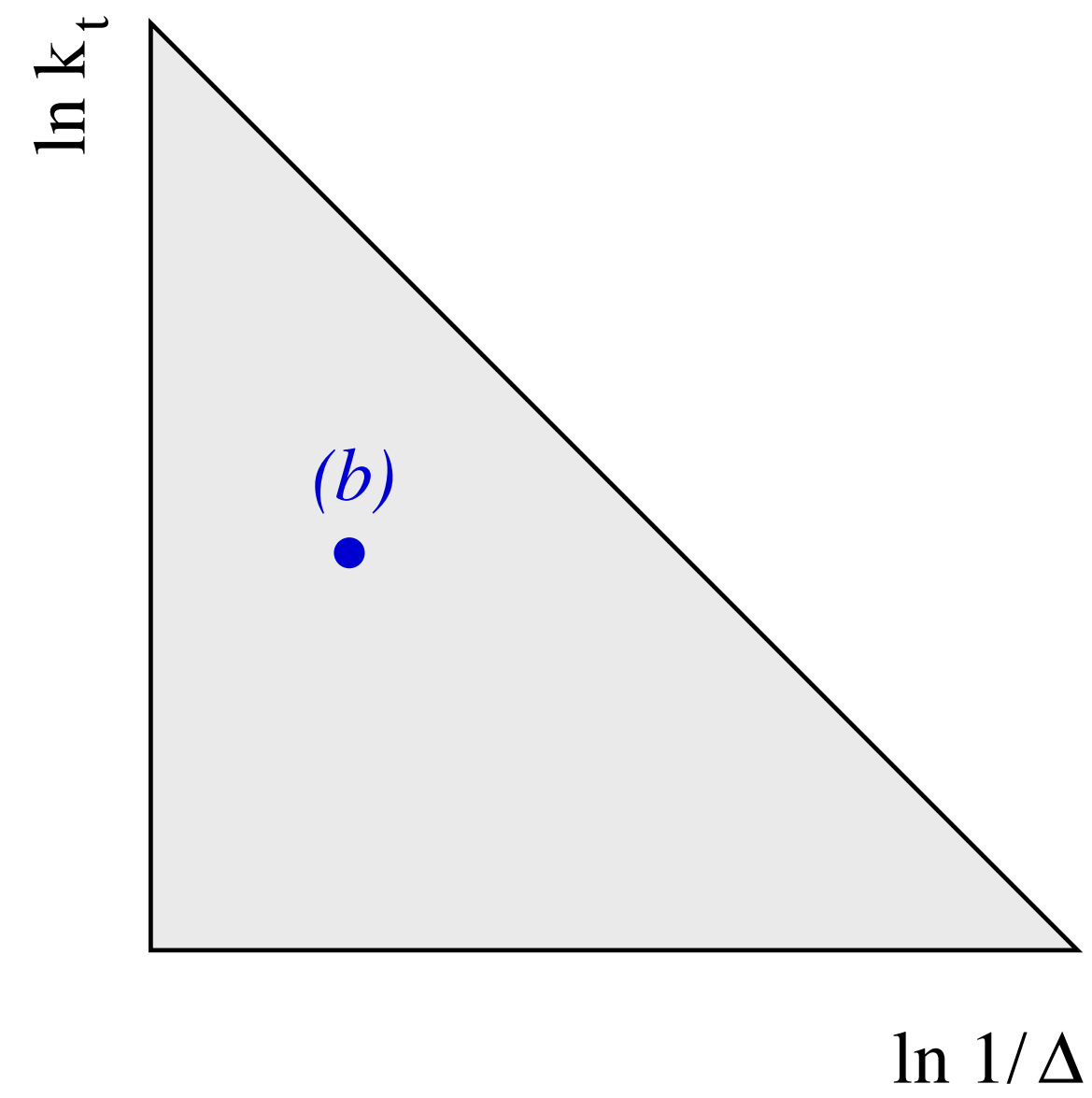
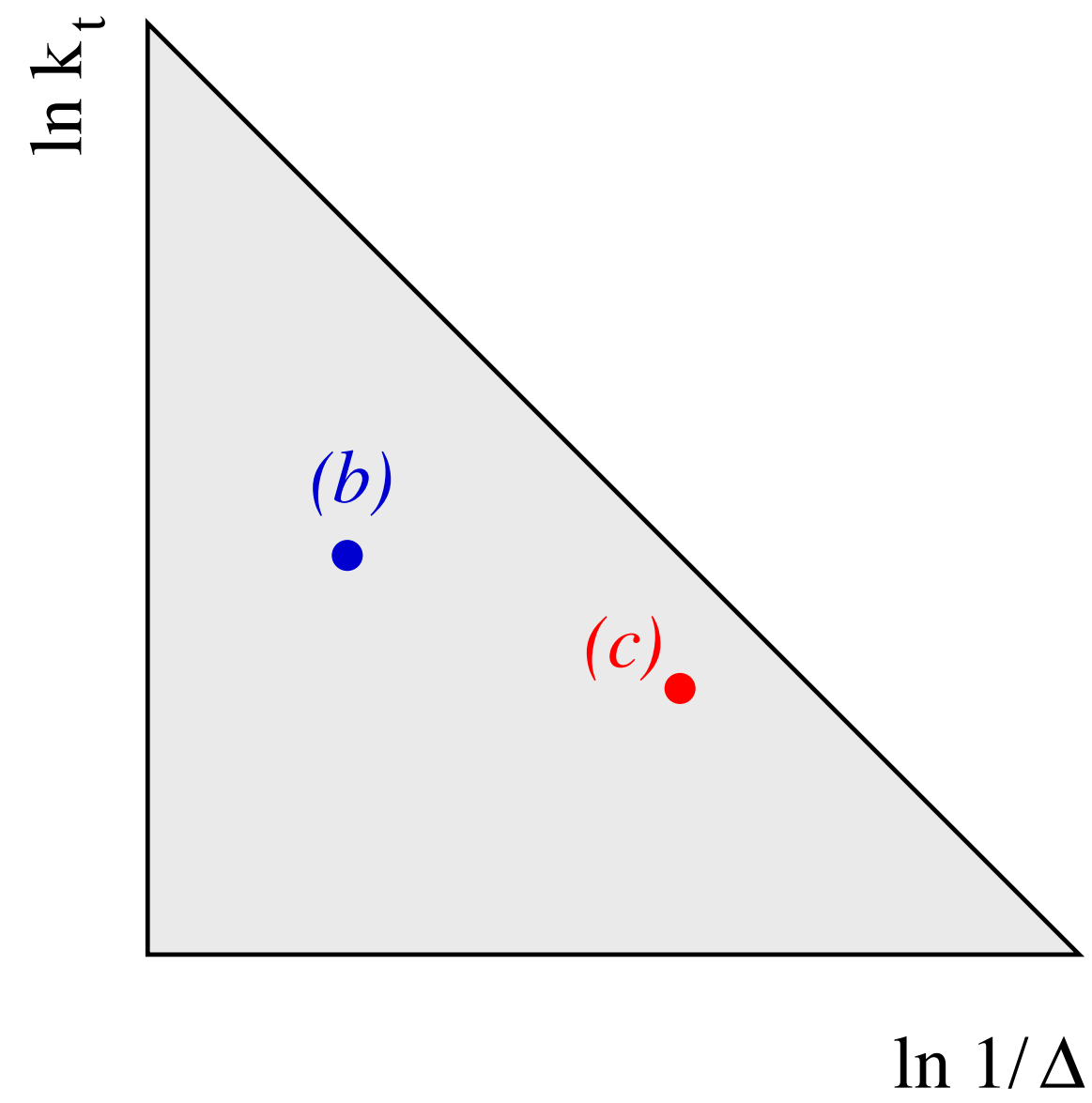
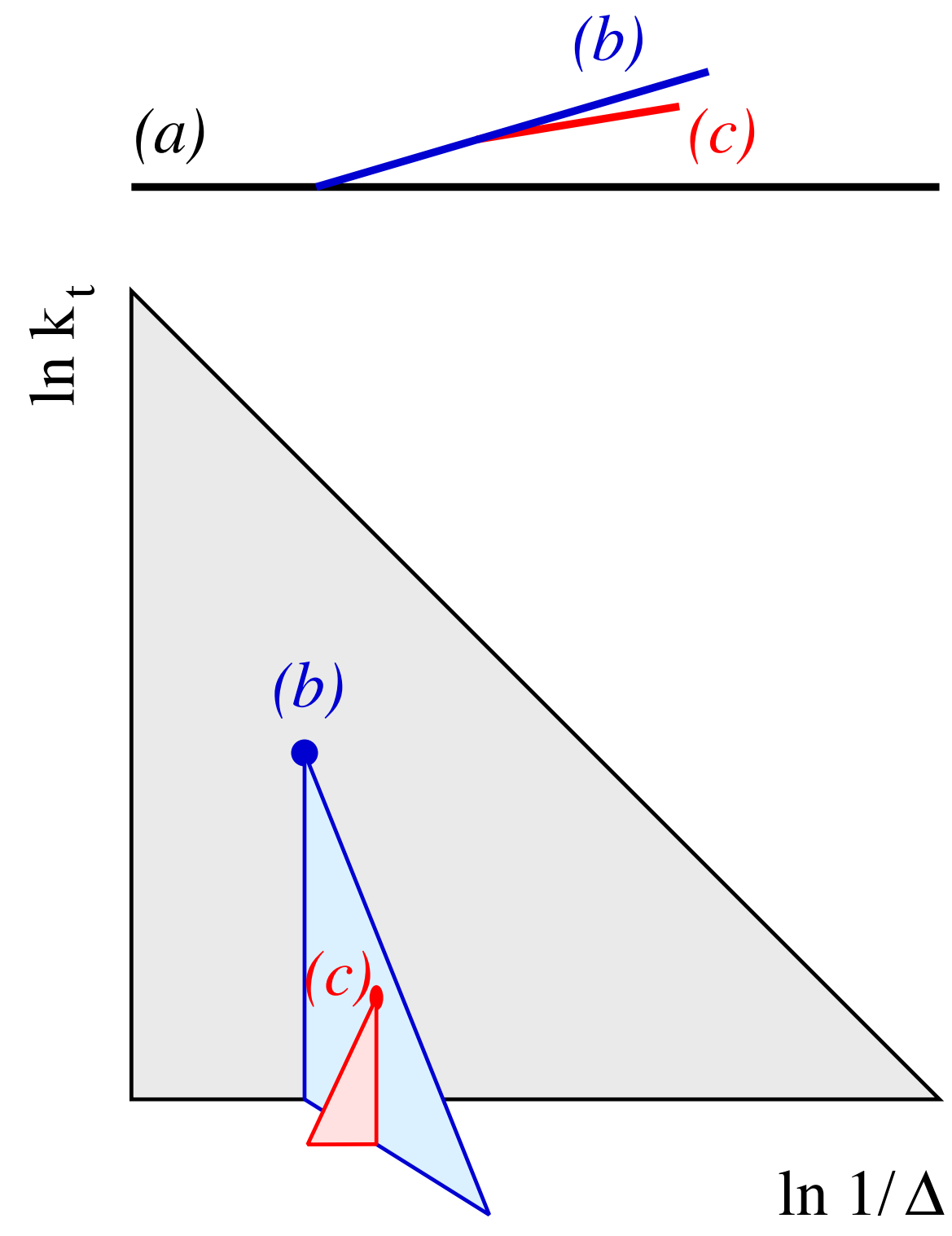
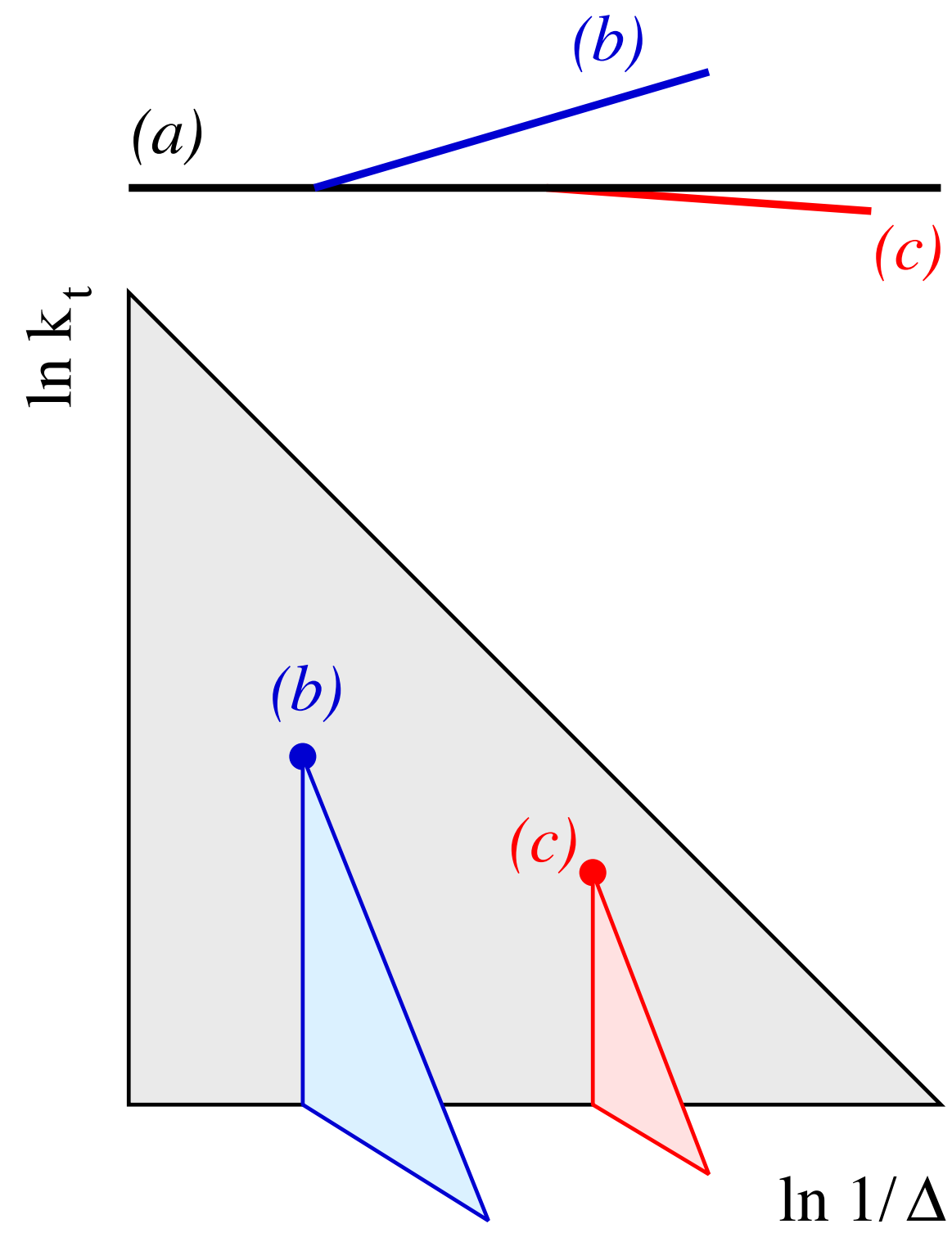
5th heavy-ion workshop @ CERN, [1808.03689](#)  
Dreyer, Soyez & GPS, [1807.04758](#) (for pp applications)

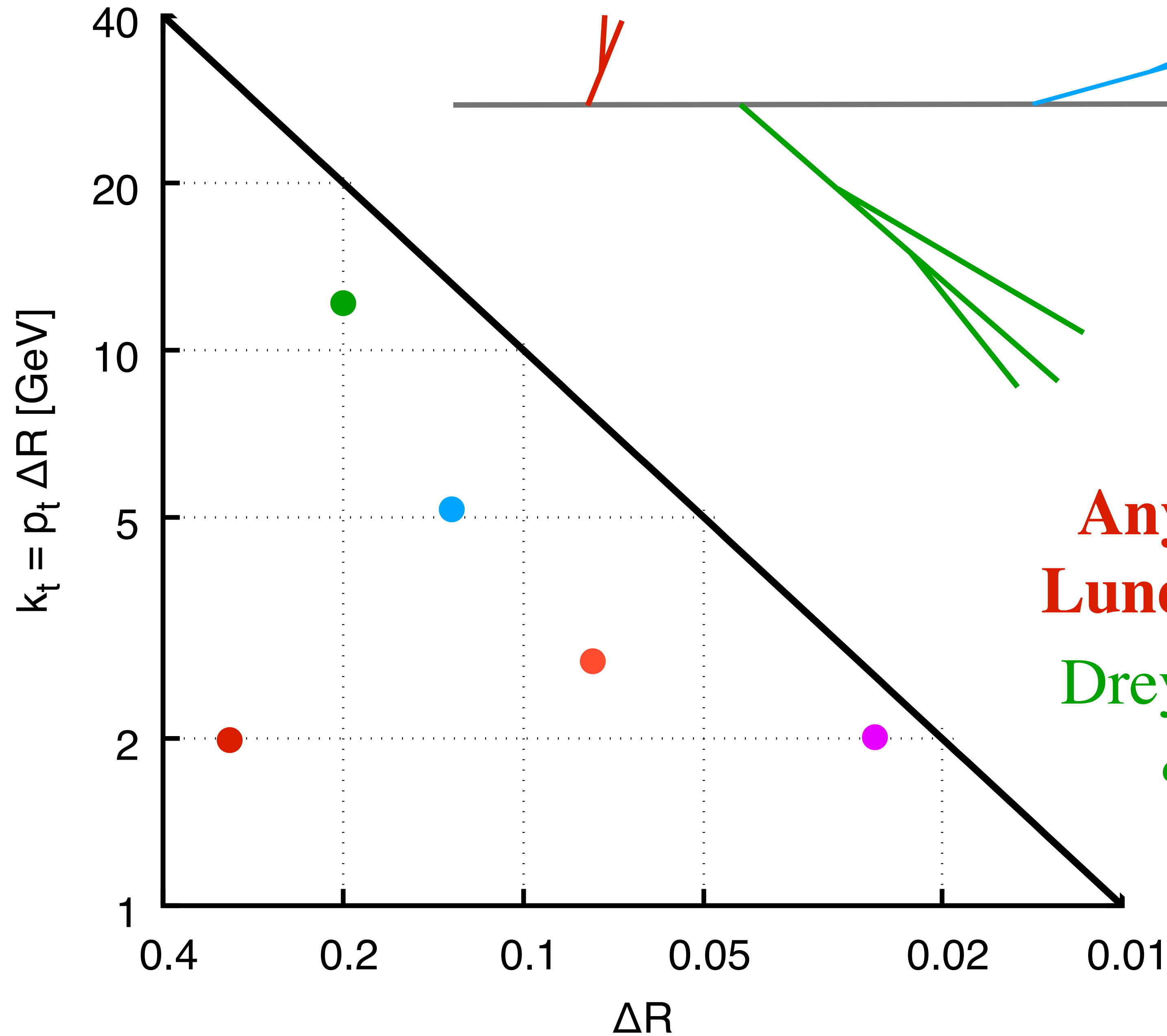
**constructing the Lund plane**

**JET**

**LUND DIAGRAM**

**PRIMARY LUND PLANE**

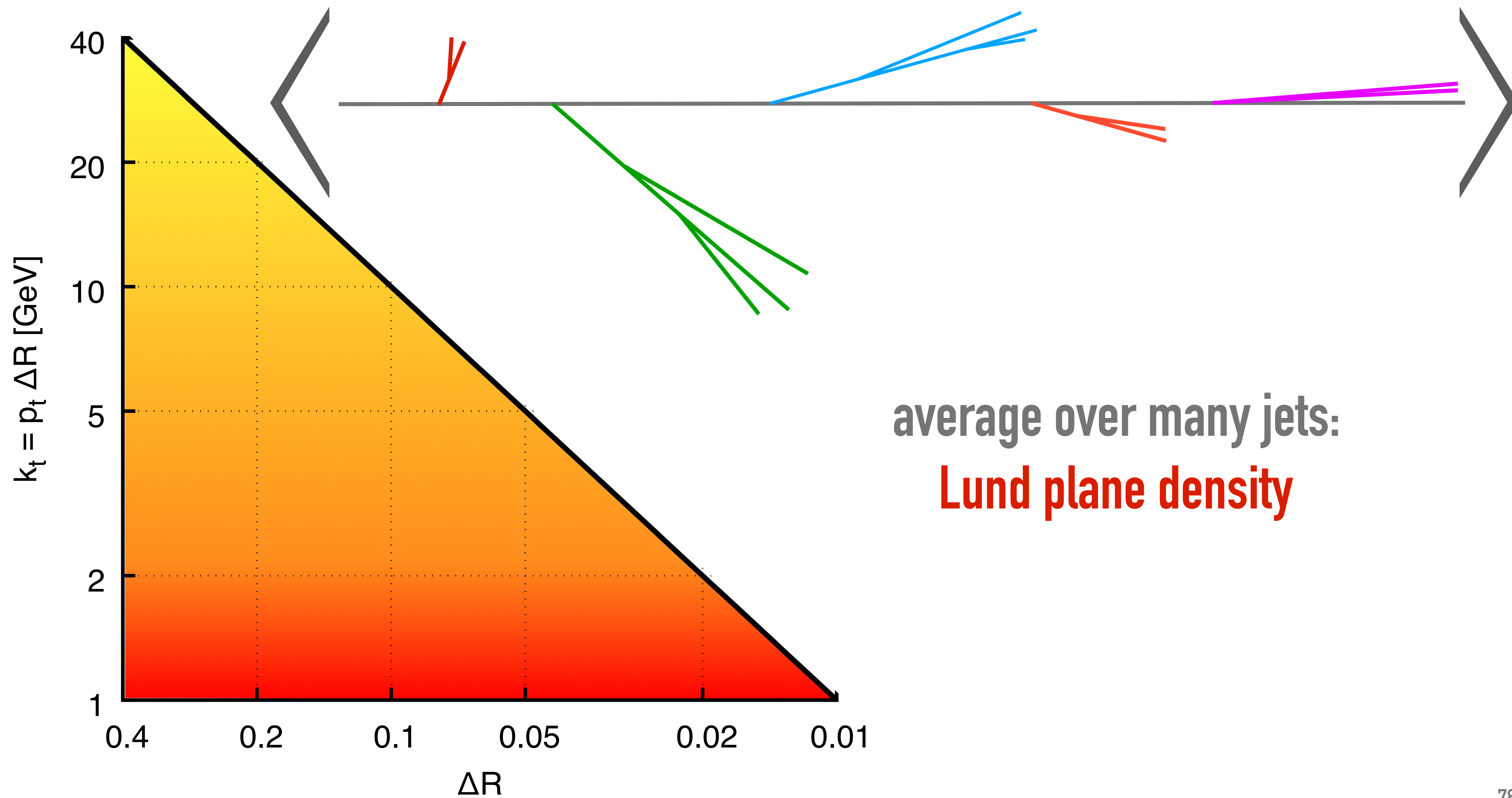




**Any jet can be mapped onto the  
Lund Plan with the C/A algorithm**

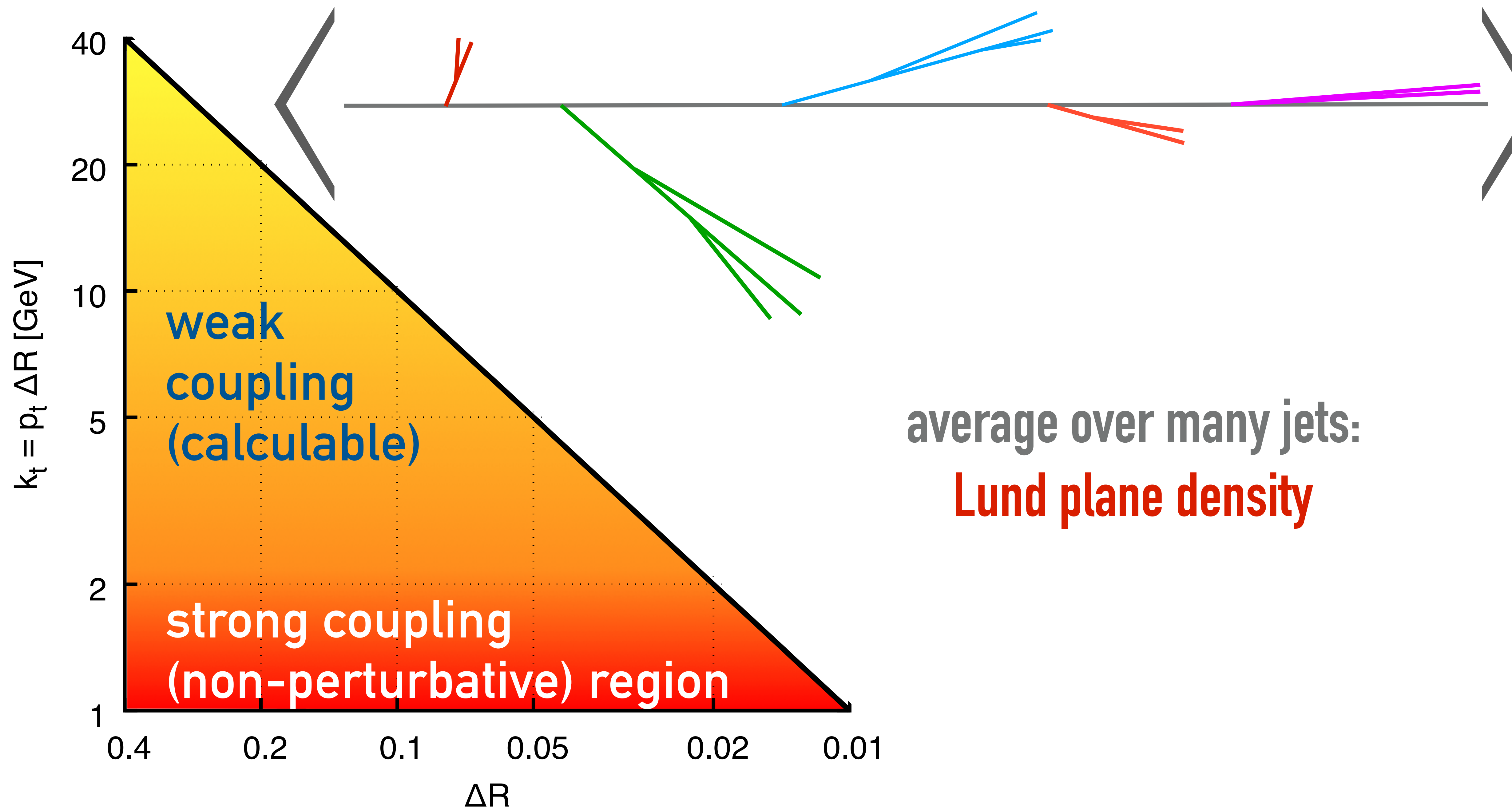
Dreyer, Soyez & GPS, [1807.04758](#)  
& 5th heavy-ion workshop,  
[1808.03689](#)

jet with  $R = 0.4$ ,  $p_t = 200 \text{ GeV}$



average over many jets:  
**Lund plane density**

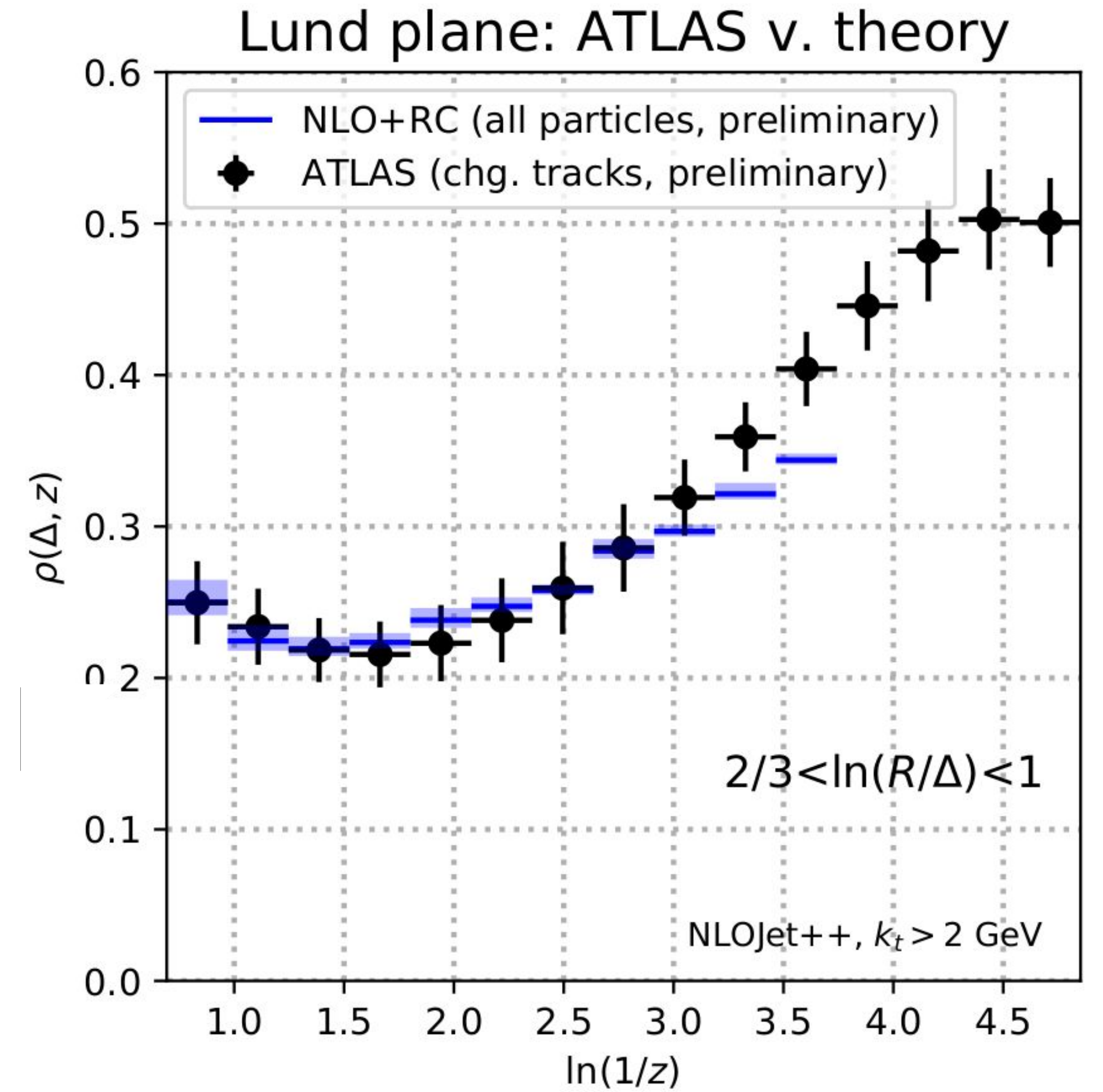
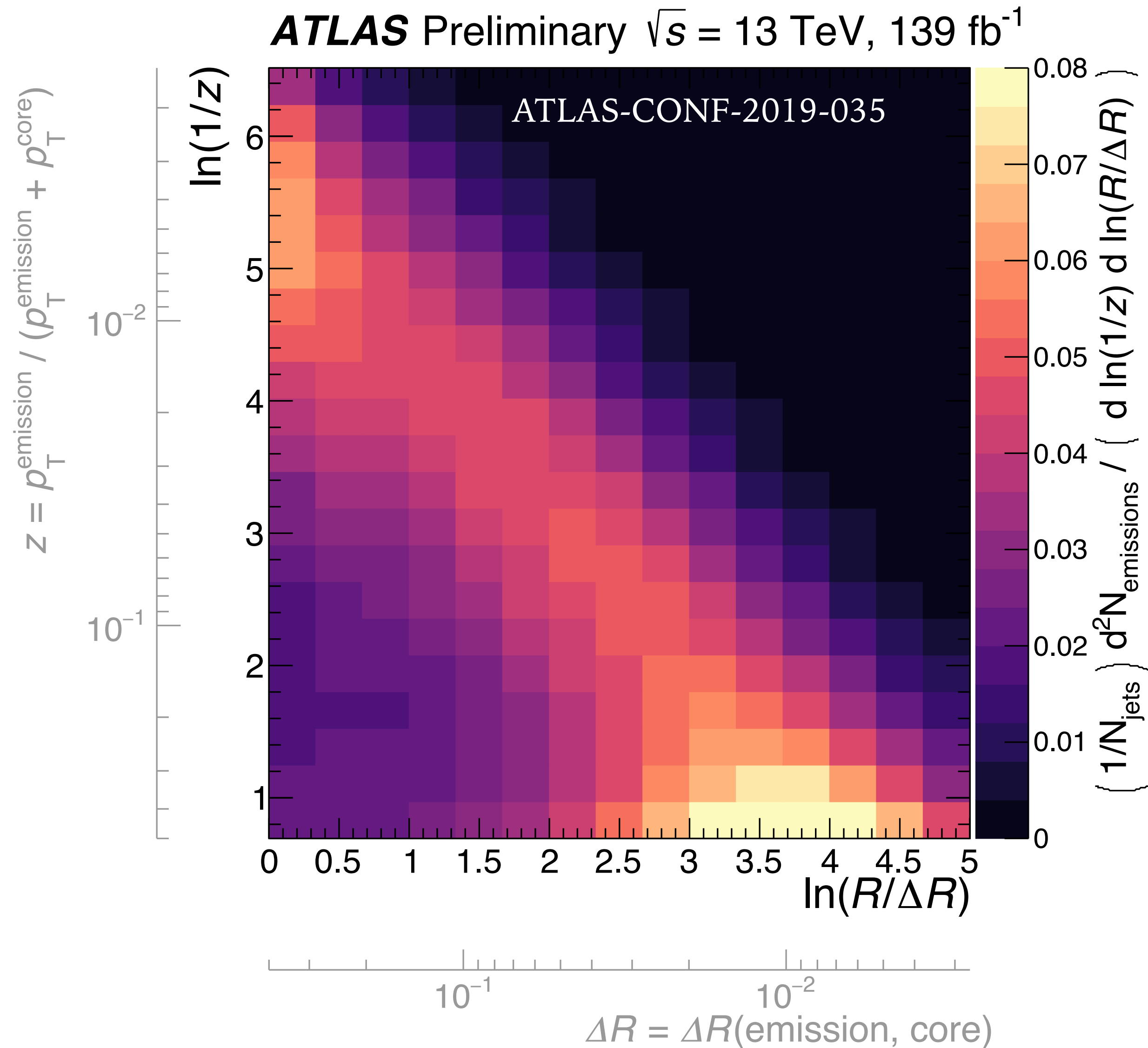
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average over many jets:  
**Lund plane density**

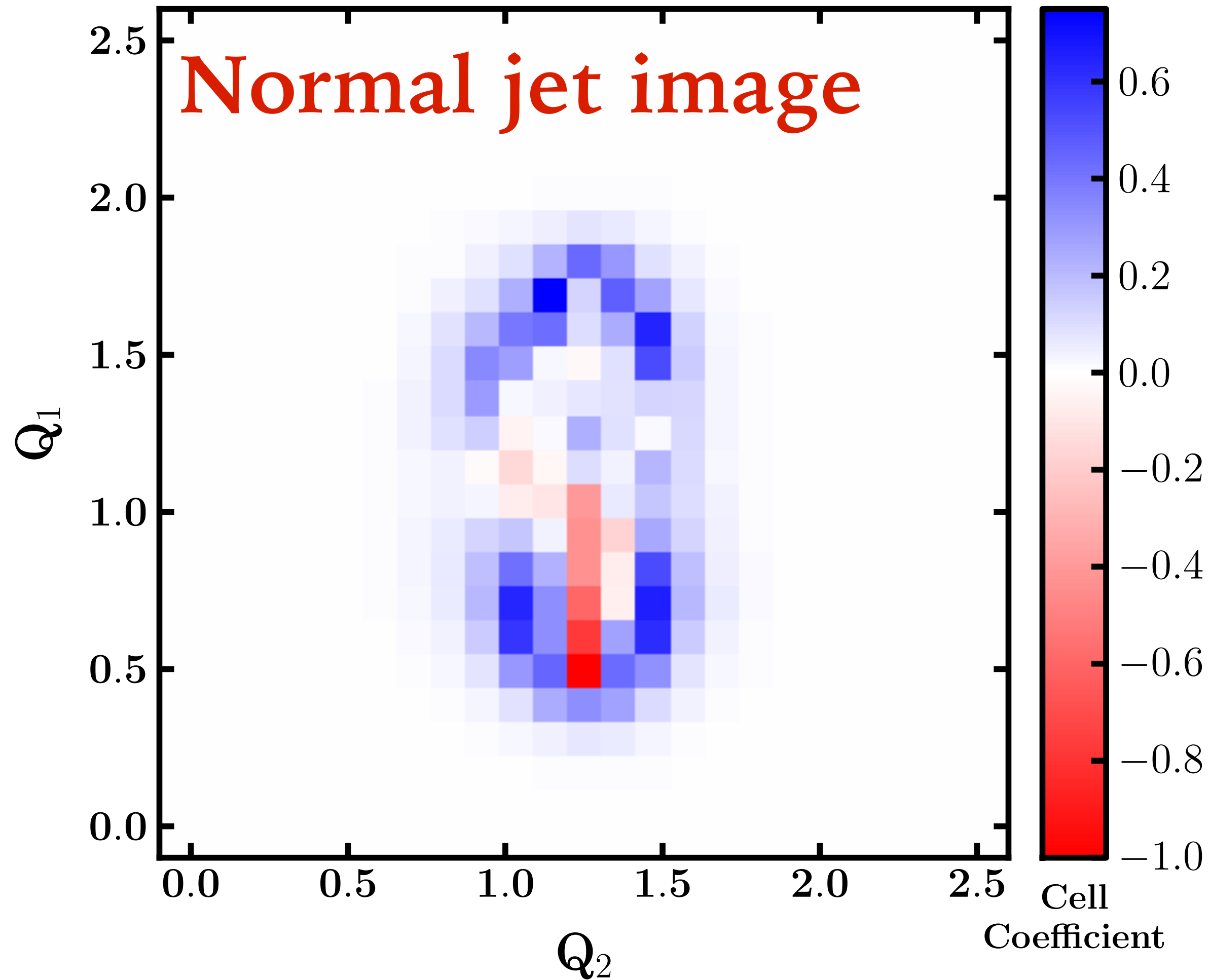


# Lund plane measurement

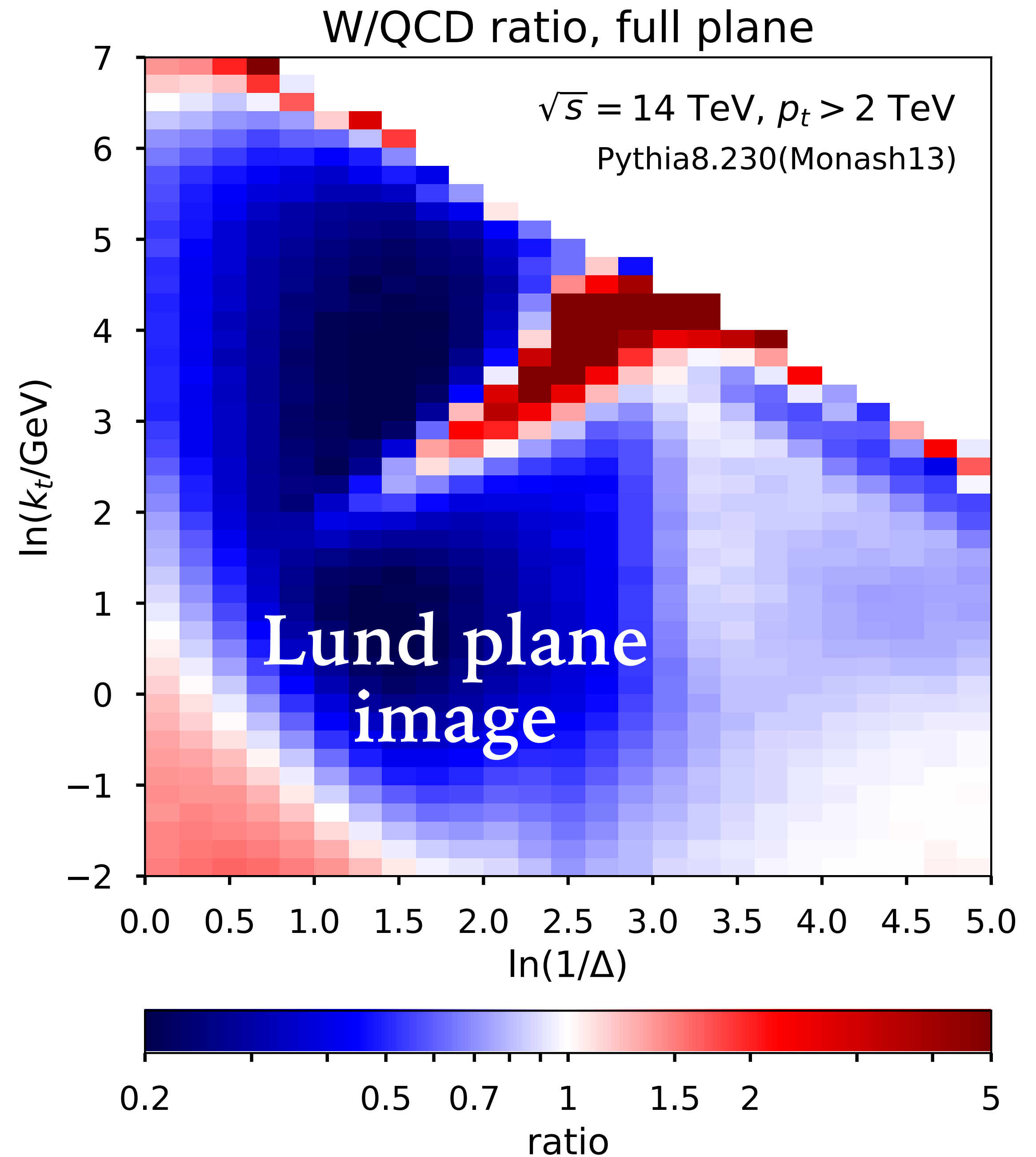


*Dreyer & Soyez prelim @Boost 2019*

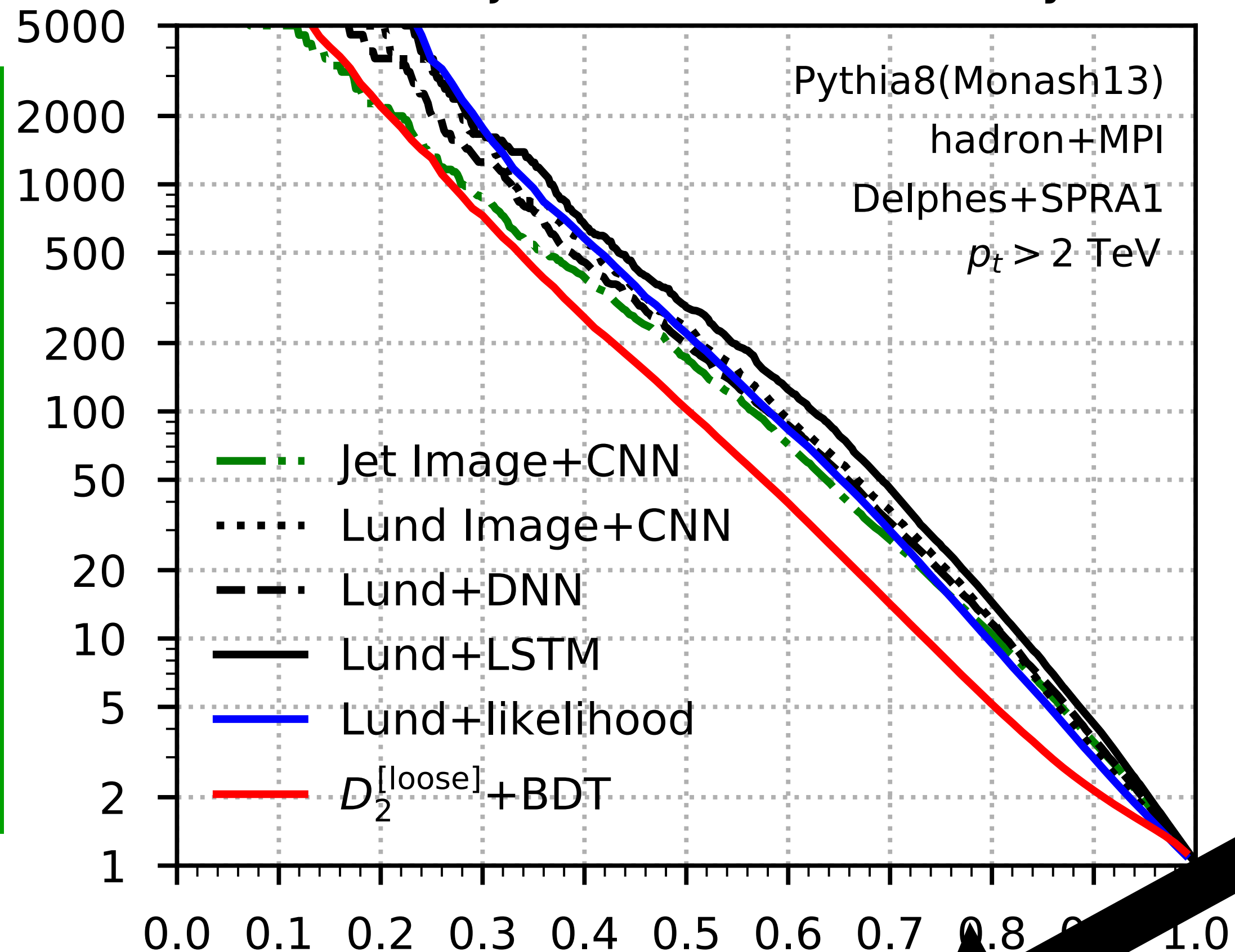
# W-boson ( $\sim$ H-boson) v. normal jets



*Cogan, Kagan, Strauss, Schwartzman, 1407.5674*



# QCD rejection v. W efficiency



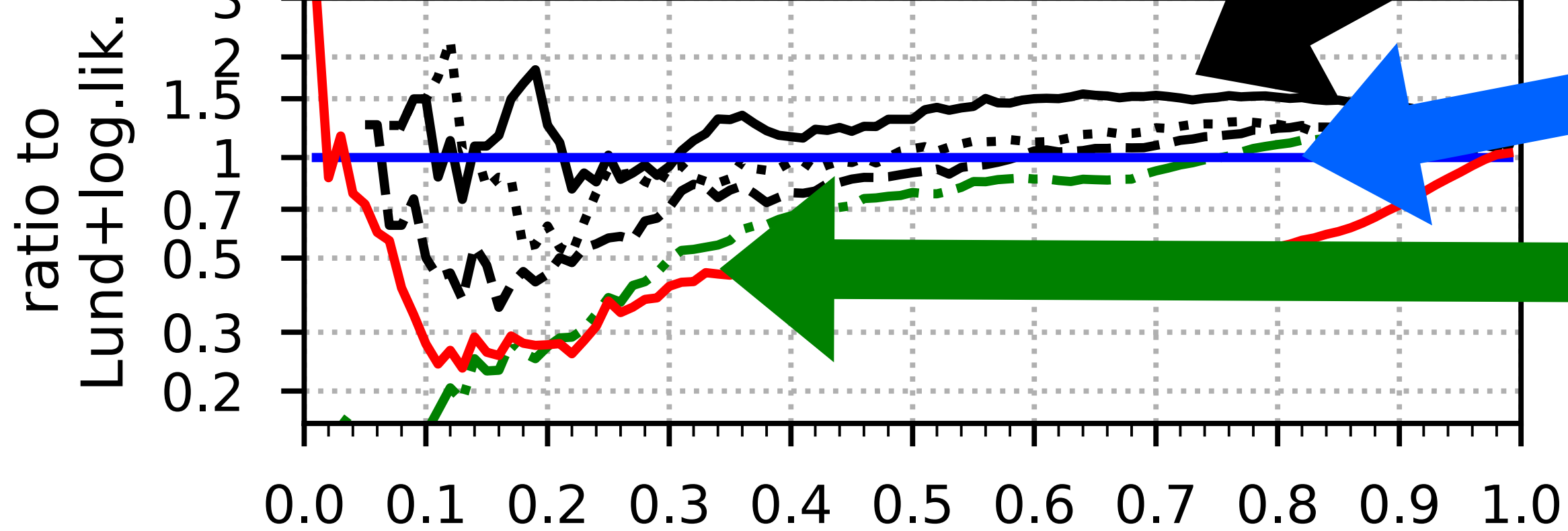
background rejection

Performance:  
background rejection v. signal efficiency

Lund + machine-learning (LSTM)  
up to twice the bkgd rejection  
compared to non-Lund methods

Lund info without machine learning

Jet image + CNN



signal efficiency

**can we trust machine learning?** A question of confidence in the training...

“

Unless you are highly confident in the information you have about the markets, you may be better off ignoring it altogether

*- Harry Markowitz (1990 Nobel Prize in Economics)  
[via S Gukov]*

# understanding parton showers, the core simulation tool (& machine-learning training tool)

---

*illustrate with dipole / antenna showers*

*Gustafson & Pettersson 1988, Ariadne 1992, main Sherpa & Pythia8 showers, option in Herwig7,  
Vincia shower & (partially) Deductor shower*

*results from Dasgupta, Dreyer, Hamilton, Monni & GPS, 1805.09327*

*[using an approach pioneered by Banfi, Corcella, Dasgupta, hep-ph/0612282 for angular-ordered showers; see also Bewick, Ravasio-Ferrario, Richardson & Seymour 1904.11866]*

# A parton shower, at its simplest

---

$$\sum_{n=0}^{\infty} \prod_{i=1}^n \left( \begin{array}{c} \diagup \\ \rightarrow \\ \diagdown \end{array} \right) = \dots \begin{array}{c} \diagup \\ \rightarrow \\ \diagdown \end{array}$$

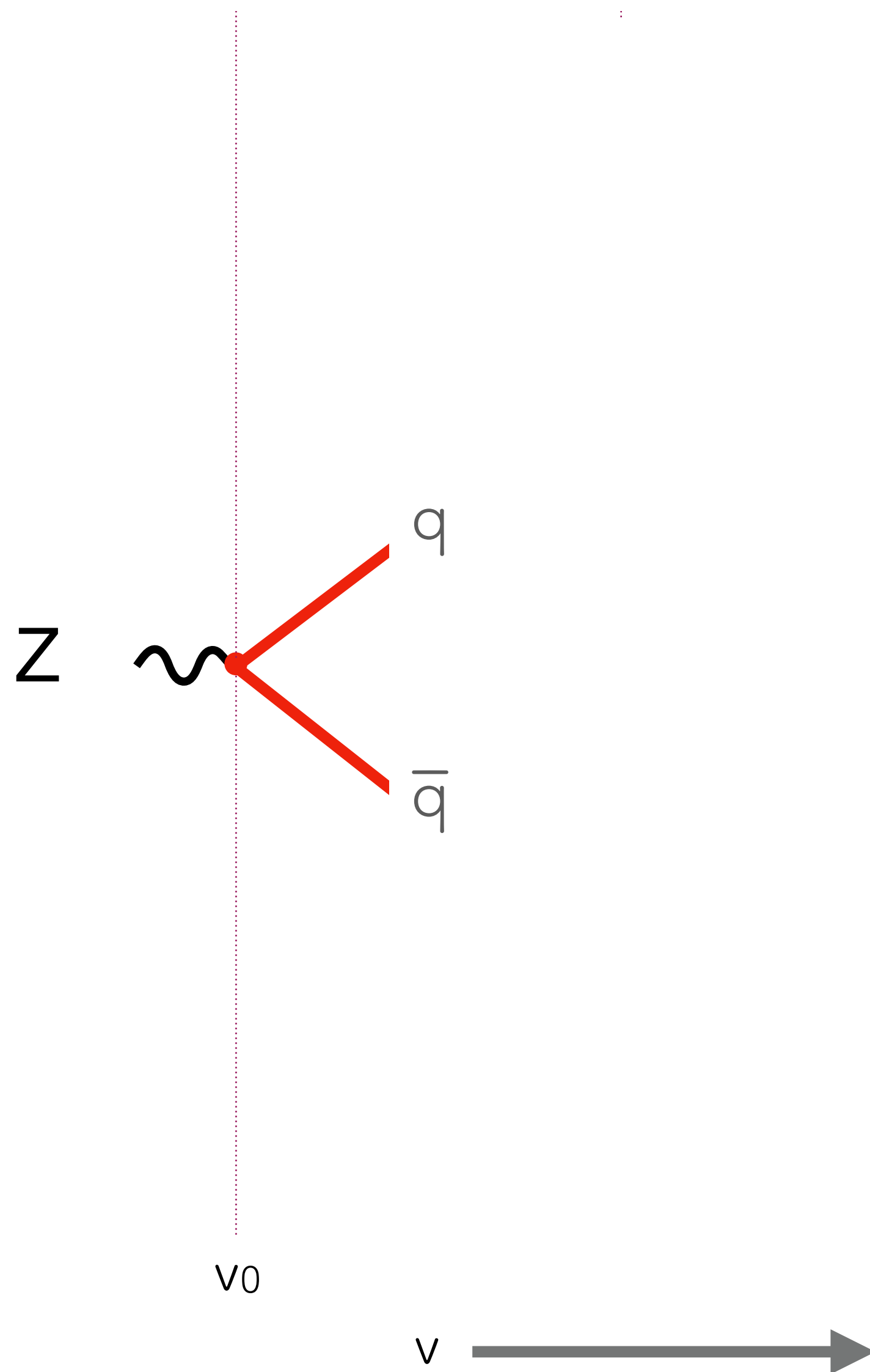
iteration of  $2 \rightarrow 3$  (or  $1 \rightarrow 2$ ) splitting kernel

# in practice: an evolution equation (in **evolution scale $v$** , e.g. $1/\text{trans.mom.}$ )

---

Start with  $q$ - $q$ bar state.

Evolve a step in  $v$  and throw a random number to decide if state remains unchanged

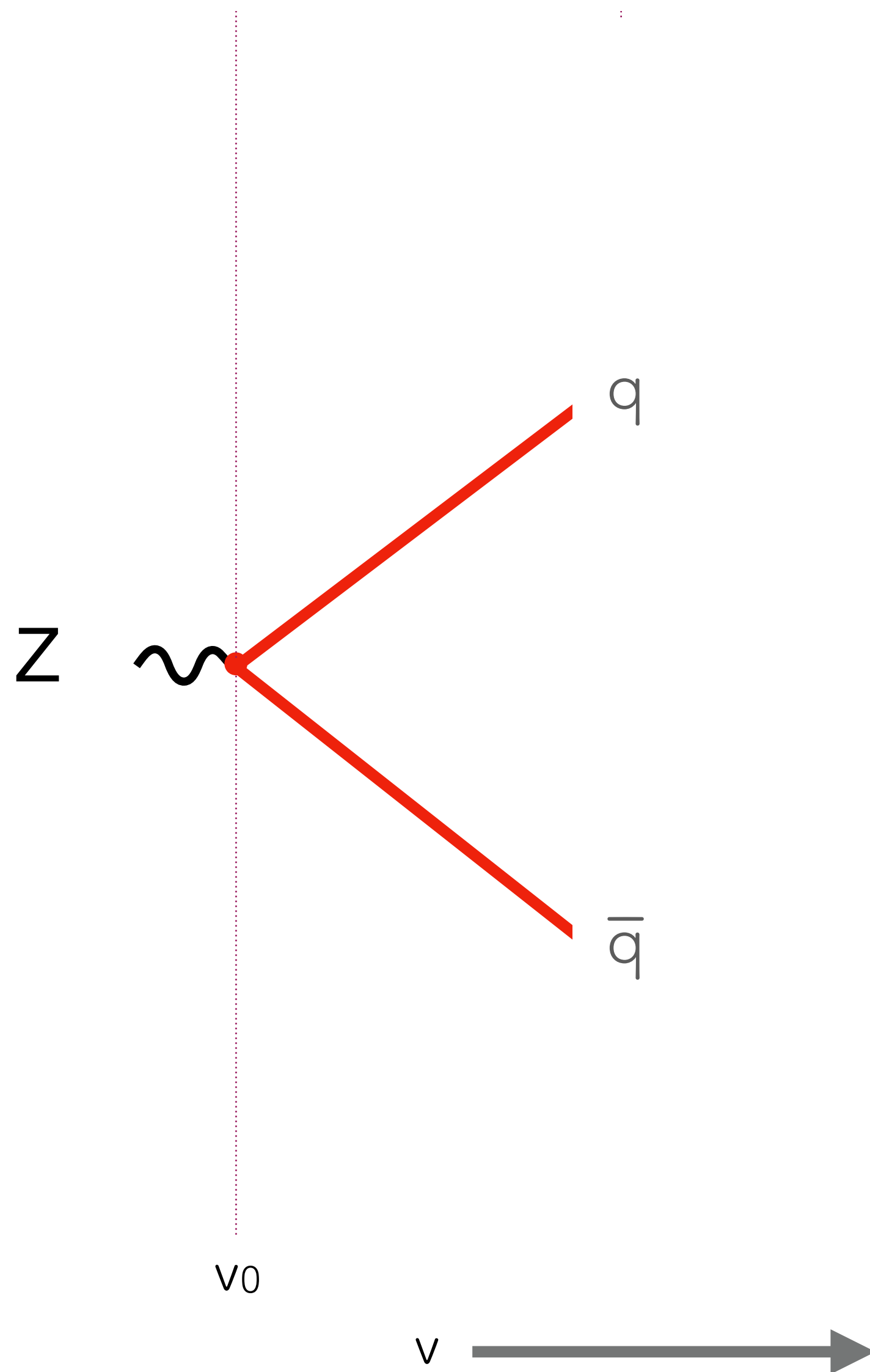


$$\frac{dP_2(v)}{dv} = -f_{2 \rightarrow 3}^{q\bar{q}}(v) P_2(v)$$

# in practice: an evolution equation (in **evolution scale $v$** , e.g. $1/\text{trans.mom.}$ )

Start with  $q$ - $q$ bar state.

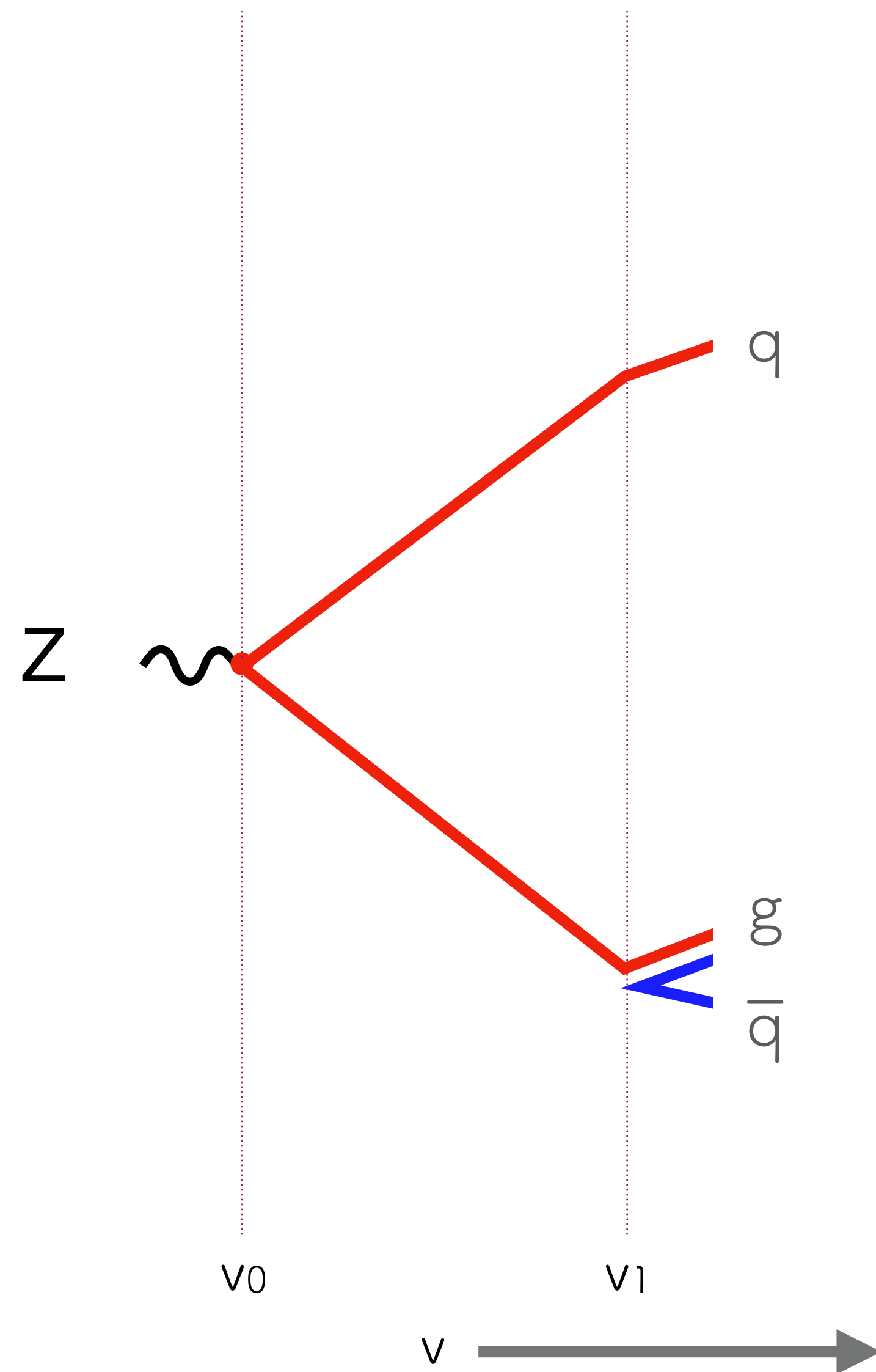
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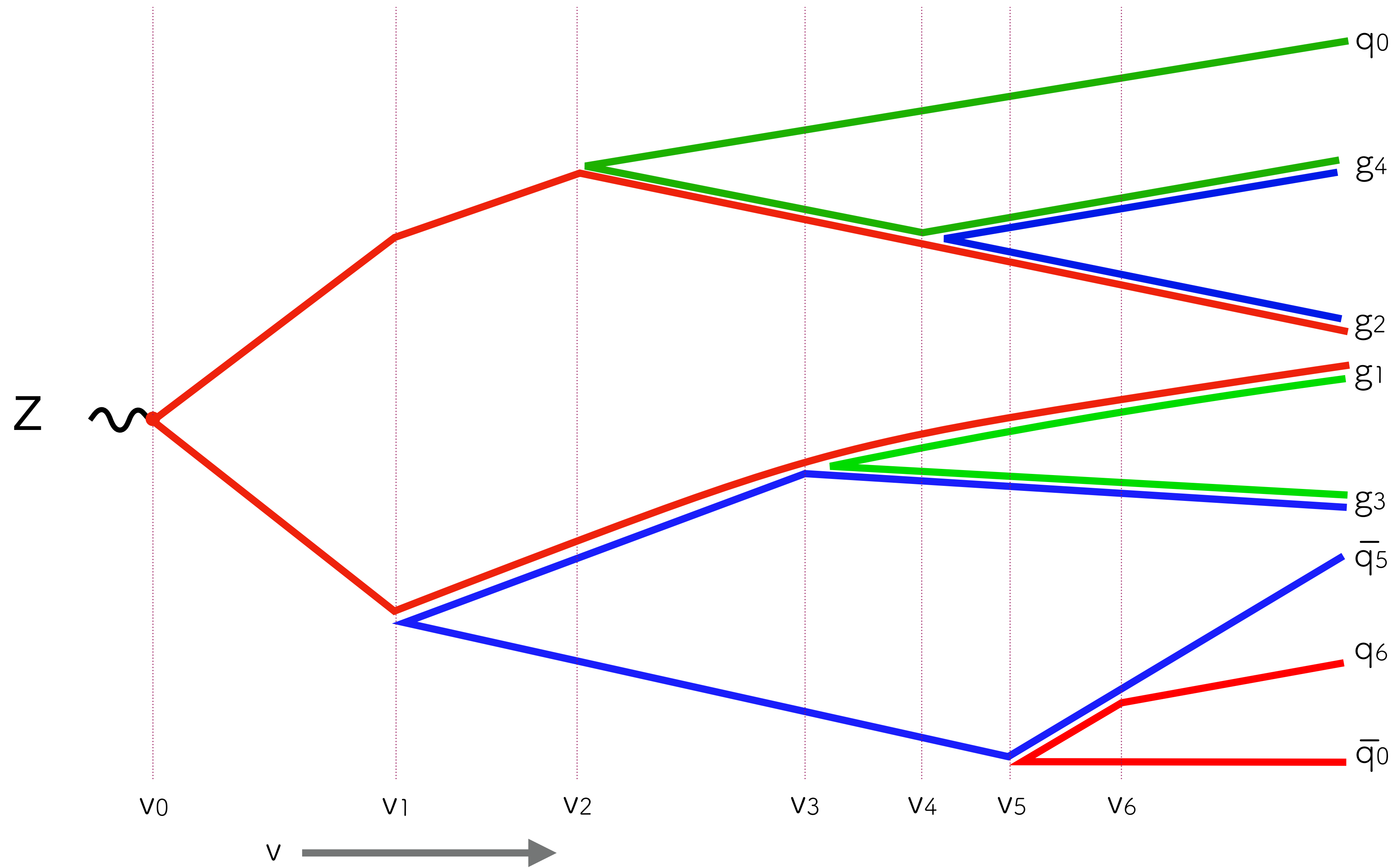
Evolve a step in  $v$  and throw a random number to decide if state remains unchanged

At some point, rand.numb. is such that **state splits** ( $2 \rightarrow 3$ , i.e. emits gluon). Evolution equation changes

$$\frac{dP_3(v)}{dv} = - \left[ f_{2 \rightarrow 3}^{qg}(v) + f_{2 \rightarrow 3}^{g\bar{q}}(v) \right] P_3(v)$$

gluon is part of two dipoles ( $qg, \bar{q}g$ )

in practice: an evolution equation (in **evolution scale  $v$** , e.g.  $1/\text{trans.mom.}$ )

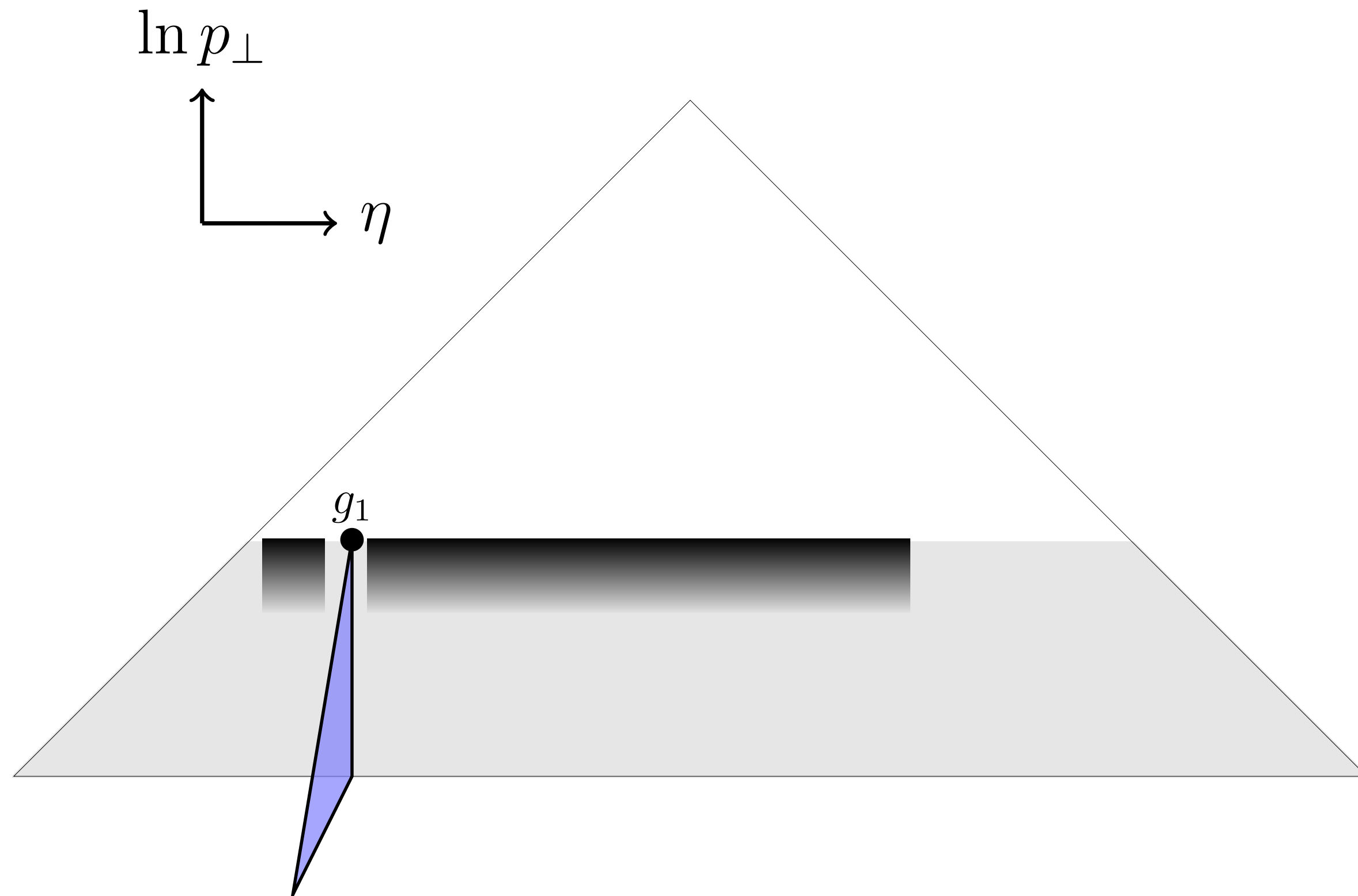


self-similar  
evolution  
continues until it  
reaches a non-  
perturbative  
scale

# Does such a procedure produce the right pattern for two emissions?

---

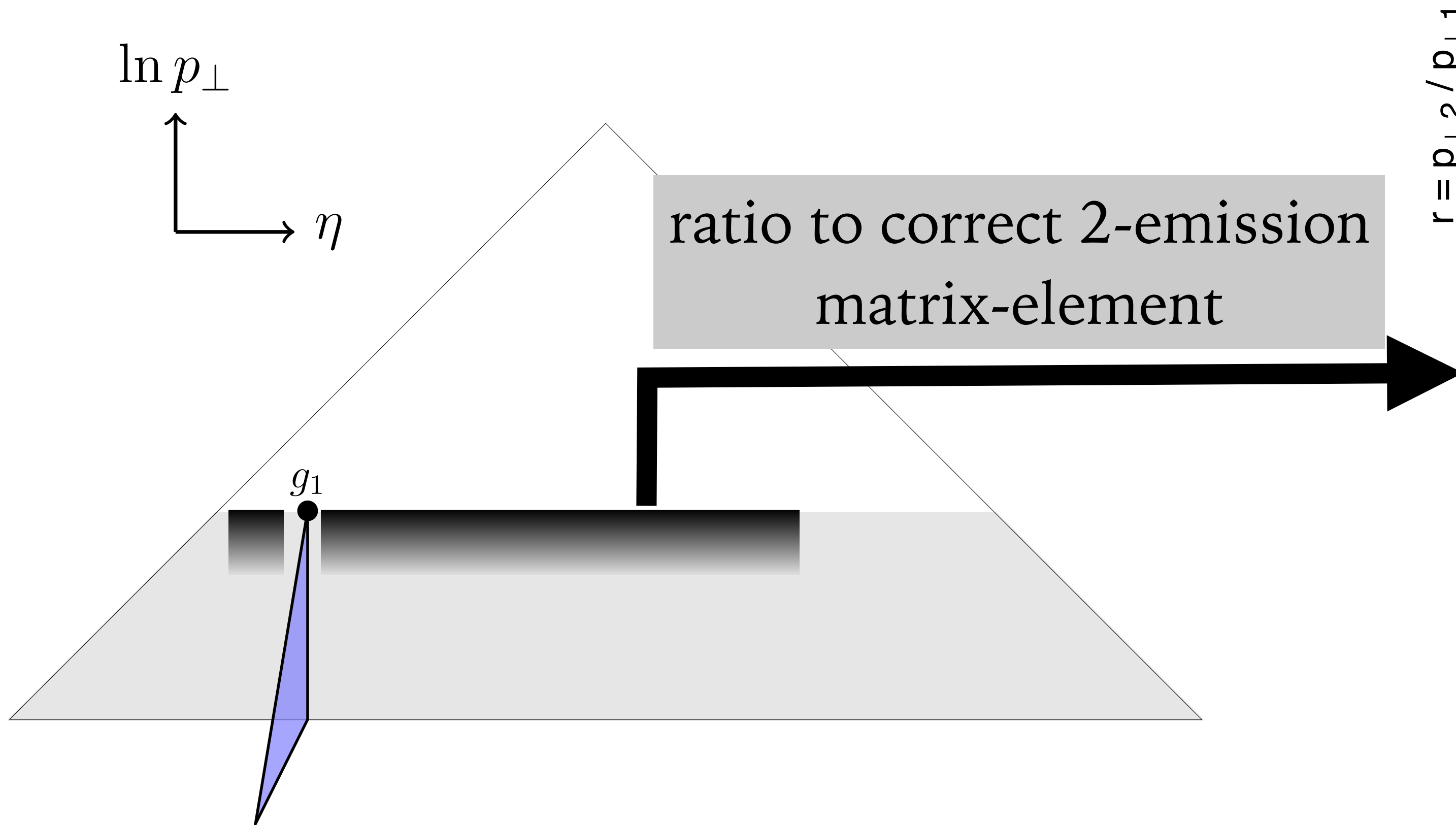
## Lund phasespace map



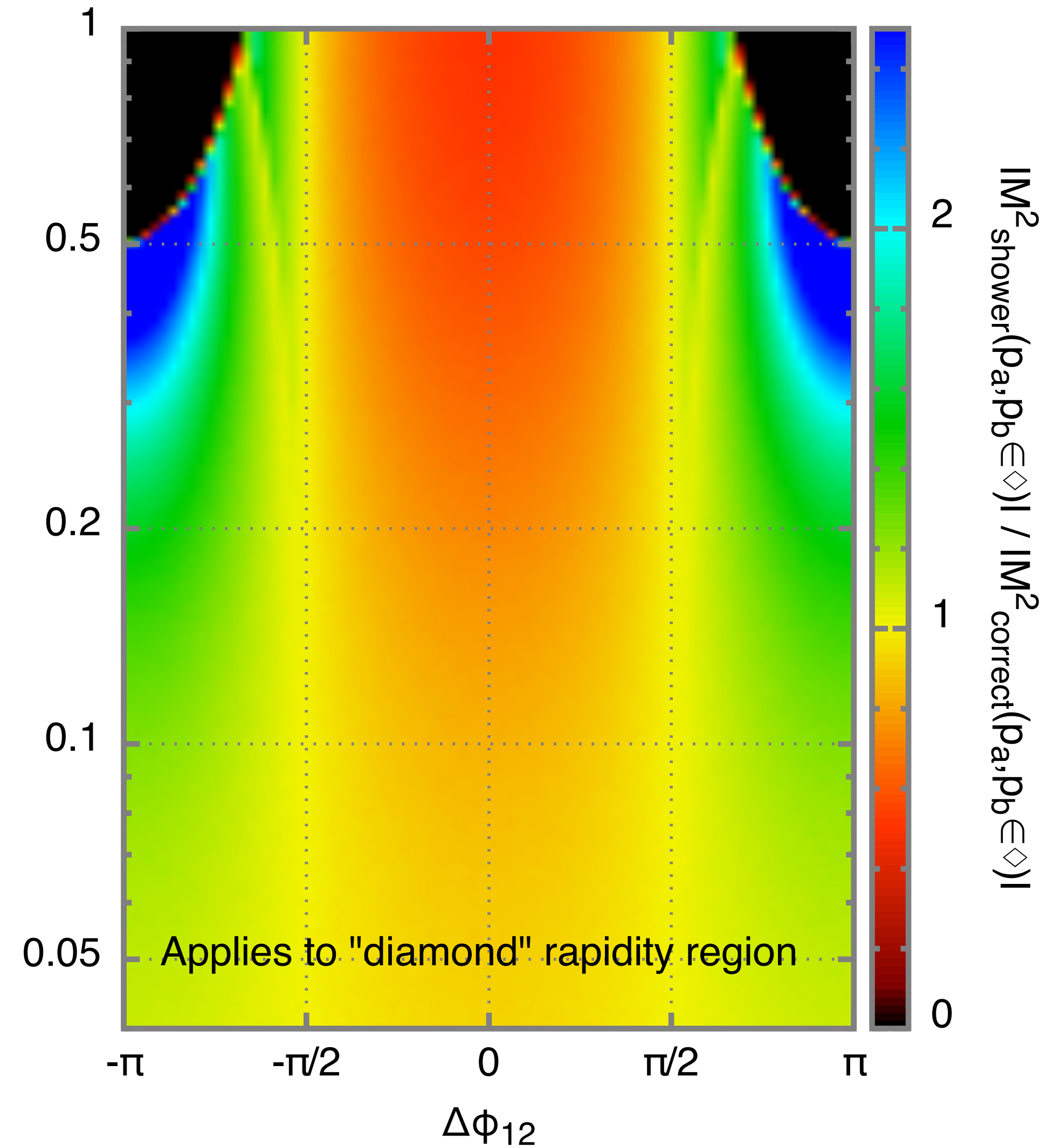
*analogous effect commented on by Nagy & Soper for Drell-Yan recoil, but wider relevance not appreciated?*

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## Lund phasespace map



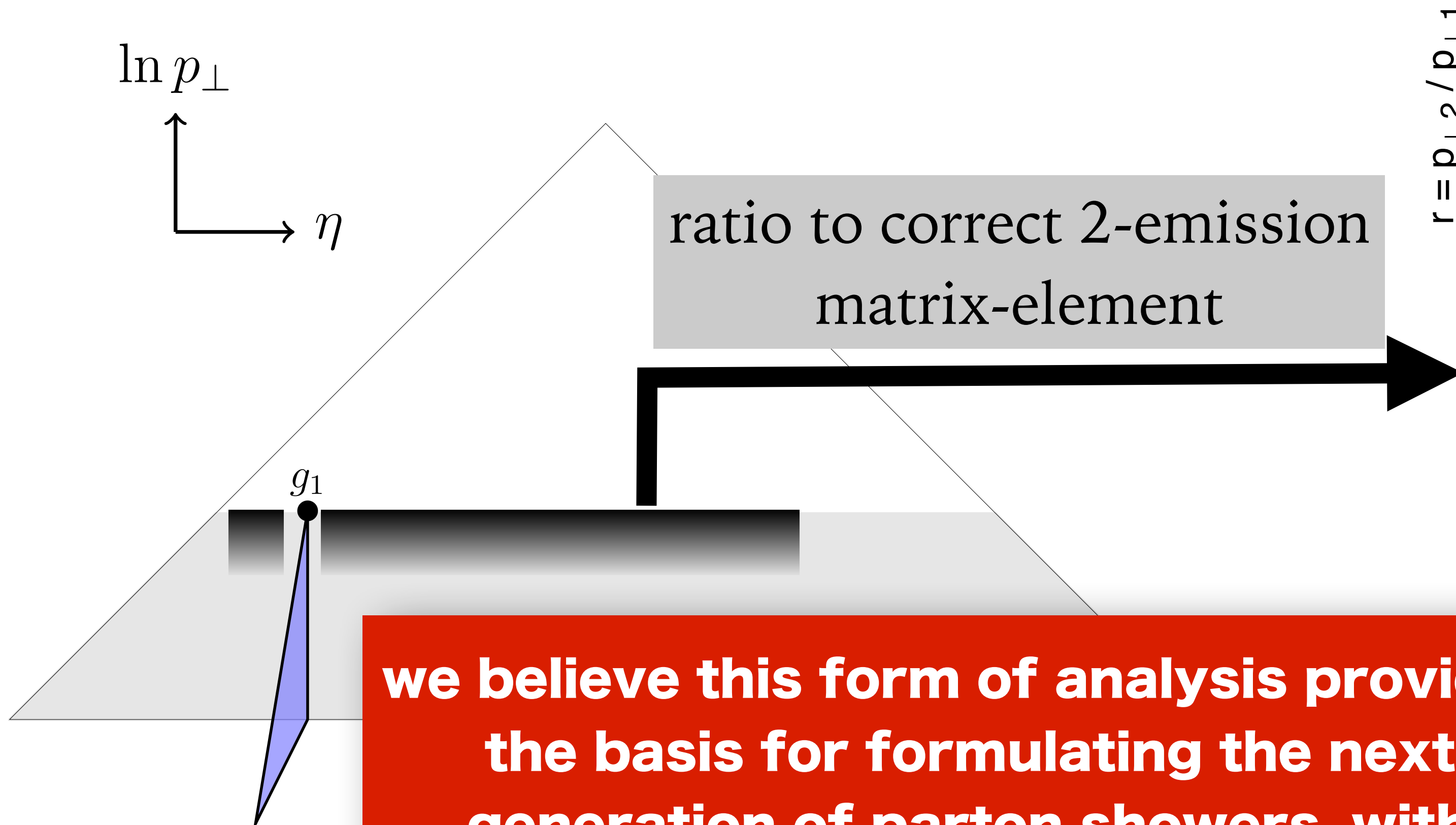
ratio of dipole-shower double-soft ME to correct result



*analogous effect commented on by Nagy & Soper for Drell-Yan recoil, but wider relevance not appreciated?*

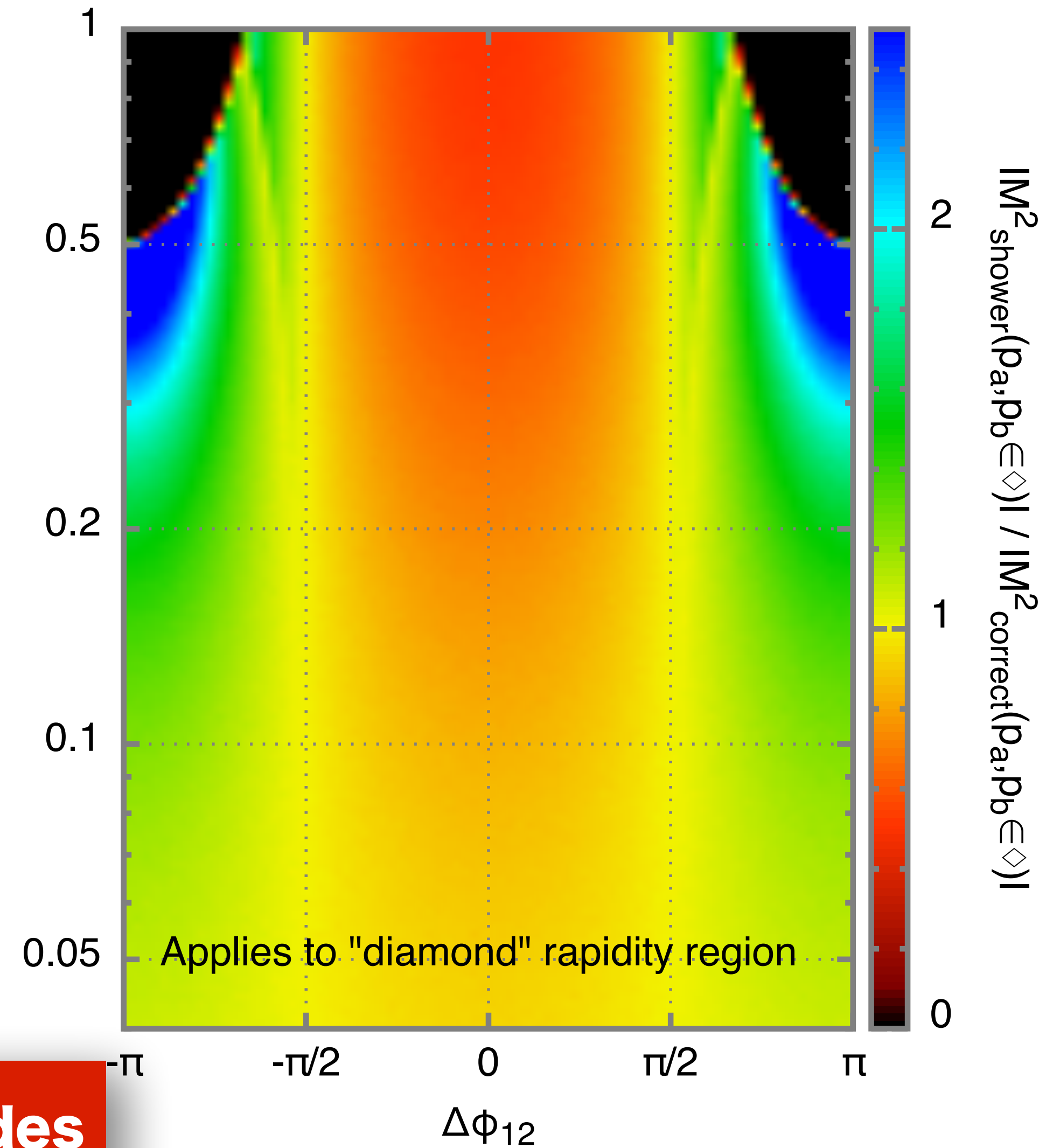
# Does such a procedure produce the right pattern for two emissions?

## Lund phasespace map



**we believe this form of analysis provides the basis for formulating the next generation of parton showers, with quantifiable accuracy**

ratio of dipole-shower double-soft ME to correct result



*analogous effect commented on by Nagy & Soper for Drell-Yan recoil, but wider relevance not appreciated?*

**outlook**

# Where is collider particle physics going?

---

- Higgs discovery opened a new chapter in particle physics
- **Qualitatively new kind of interaction — Yukawa interactions (“fifth force”)**
  - critical to the world as we know it
  - so far probed only to 20%
  - and in only a corner of phase space
- **The biggest [accessible] challenge for the future is to see what we can learn, experimentally, about the Higgs potential,  $V(\varphi)$  (one of strongest drivers for a new collider)**
- Many other challenges remain (e.g. dark matter), but much as we should search for them, we should be wary of promising breakthroughs

“

I think Nature is smarter than physicists. We should have the courage to say: "Let Nature tell us what is going on."

*-Carlo Rubbia [2008]*



# How can we get there?

---

- Collider physics relies crucially on understanding QCD
- **Two big frontiers**
  - learning to use all the information contained in events, each with 100s of particles
  - accurate quantitative connection between events and fundamental Lagrangian
- Even with machine-learning, we seem to **benefit from physics-driven understanding of how to structure event information**
- Structuring event information likely **crucial also in understanding what to ask of a key QCD tool, the parton shower**