

# PanScales parton showers

Rencontres de Moriond  
QCD & high-energy interactions  
March 2023

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Rudolf Peierls Centre for  
Theoretical Physics  
& All Souls College, Oxford



Science and  
Technology  
Facilities Council





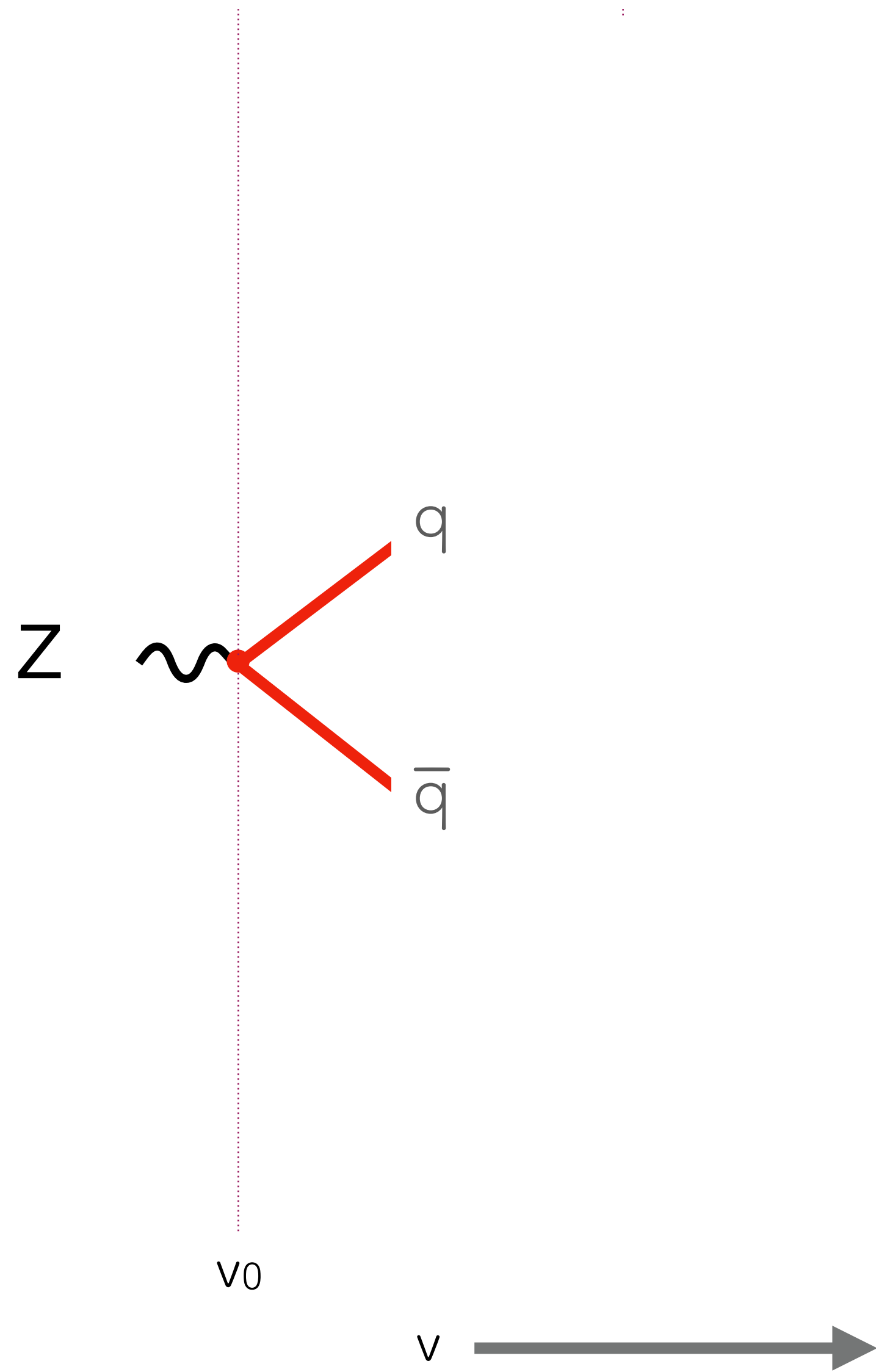
# QCD shower: an evolution equation (in **evolution scale $v$** , e.g. trans.mom.)

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Start with  $q\bar{q}$  state.

Throw a random number to determine down to what scale state persists unchanged

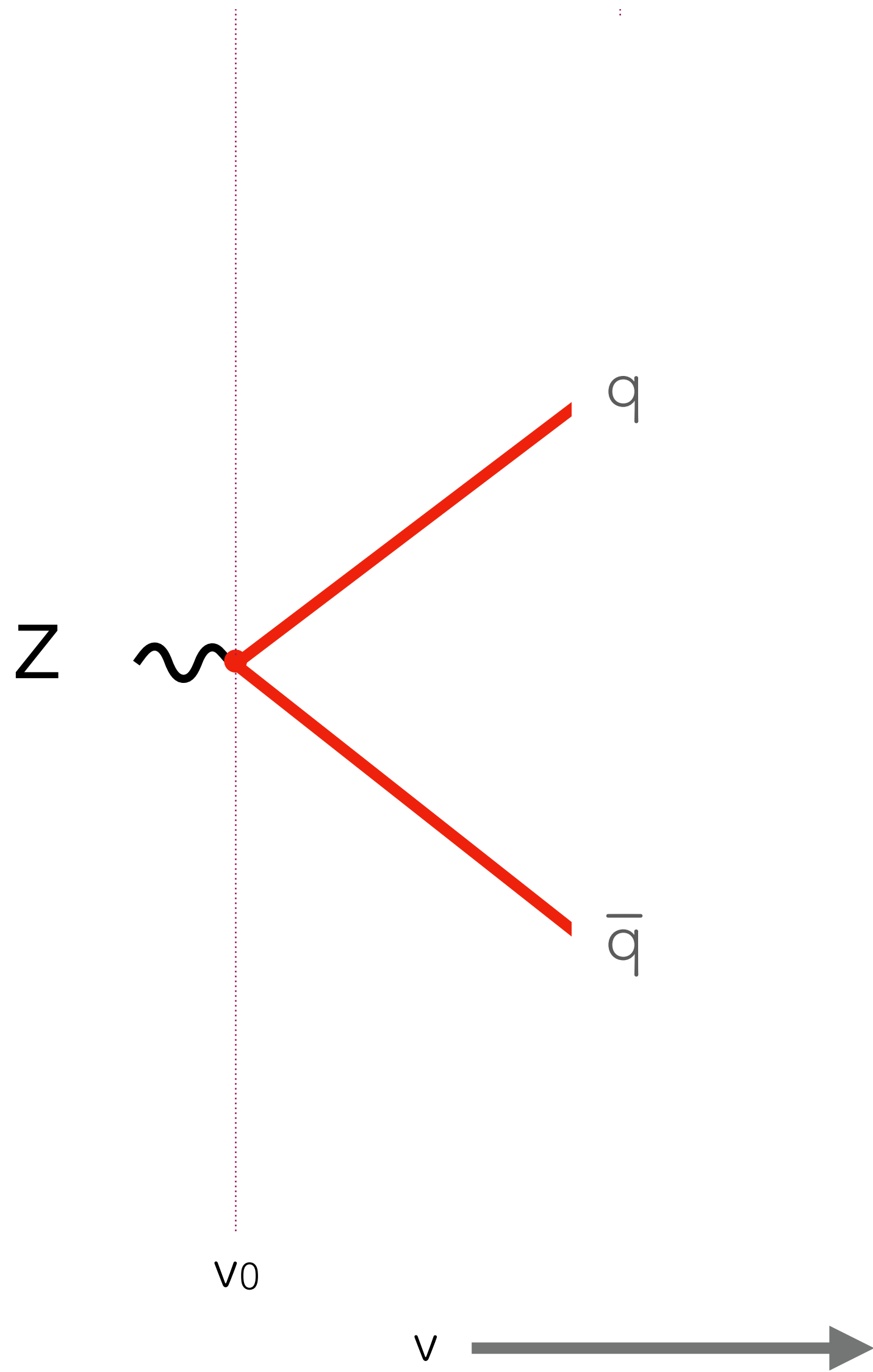
$$\frac{dP_2(v)}{dv} = -f_{2 \rightarrow 3}^{q\bar{q}}(v) P_2(v)$$



# QCD shower: an evolution equation (in **evolution scale $v$** , e.g. trans.mom.)

Start with  $q$ - $q$ bar state.

Throw a random number to determine down to what scale state persists unchanged



$$\frac{dP_2(v)}{dv} = -f_{2 \rightarrow 3}^{q\bar{q}}(v) P_2(v)$$

# QCD shower: an evolution equation (in **evolution scale $v$** , e.g. trans.mom.)

Start with q-qbar state.

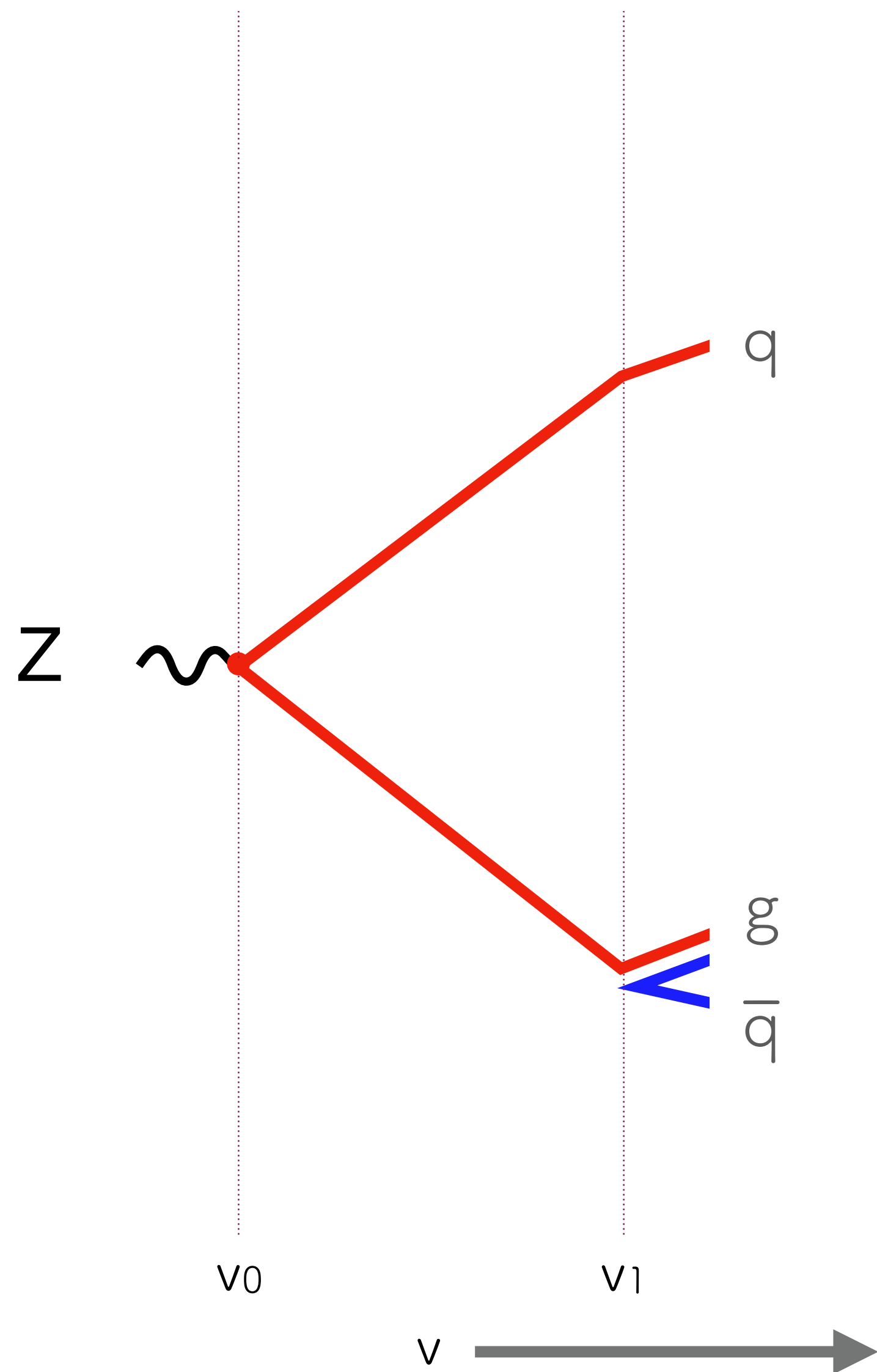
Throw a random number to determine down to what scale state persists unchanged

At some point, **state splits** (2→3, i.e. emits gluon). Evolution equation changes

$$\frac{dP_3(v)}{dv} = - \left[ f_{2 \rightarrow 3}^{qg}(v) + f_{2 \rightarrow 3}^{g\bar{q}}(v) \right] P_3(v)$$

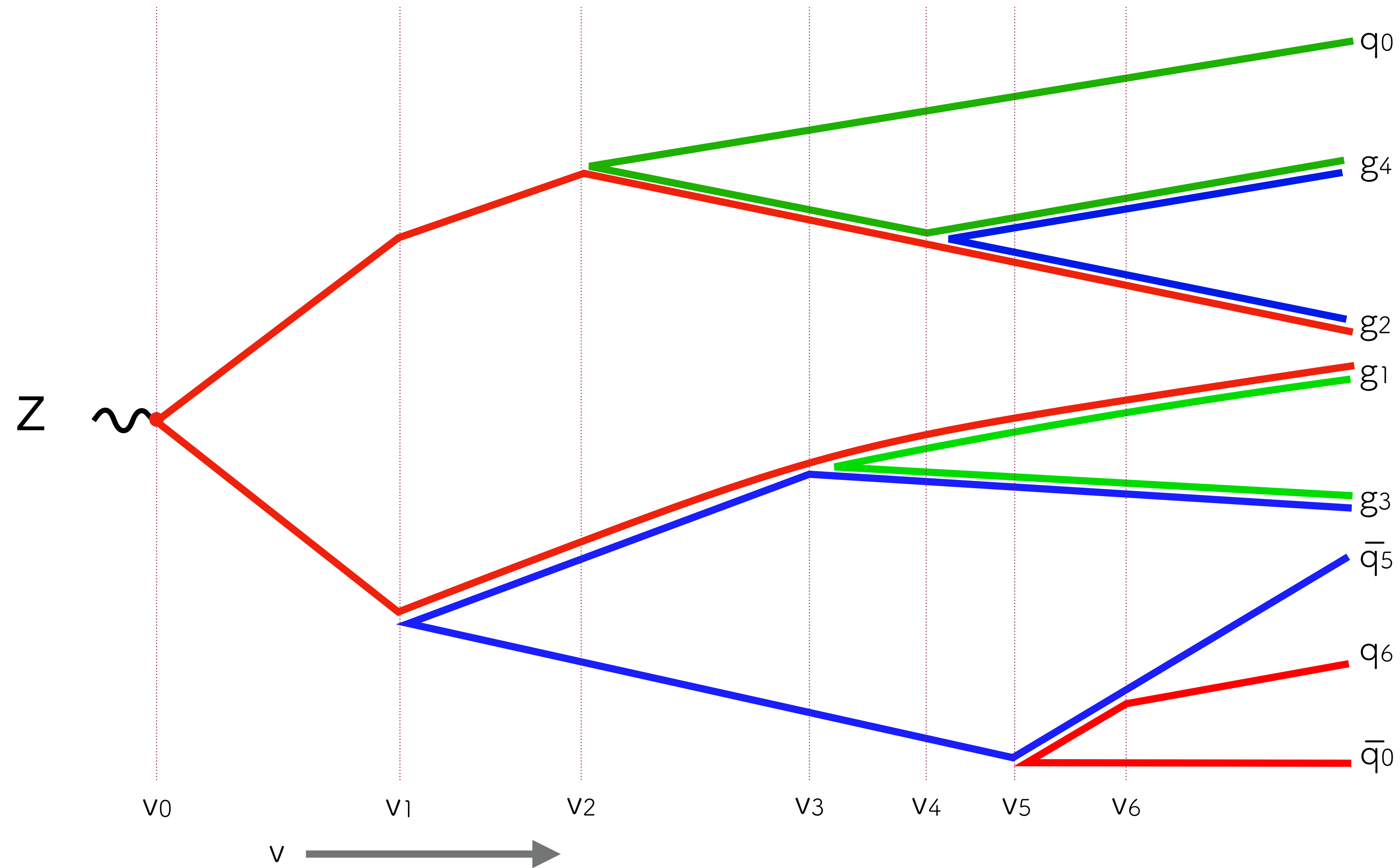
gluon is part of two dipoles  $(qg)$ ,  $(g\bar{q})$ , each treated as independent

**(many showers use a large  $N_C$  limit)**





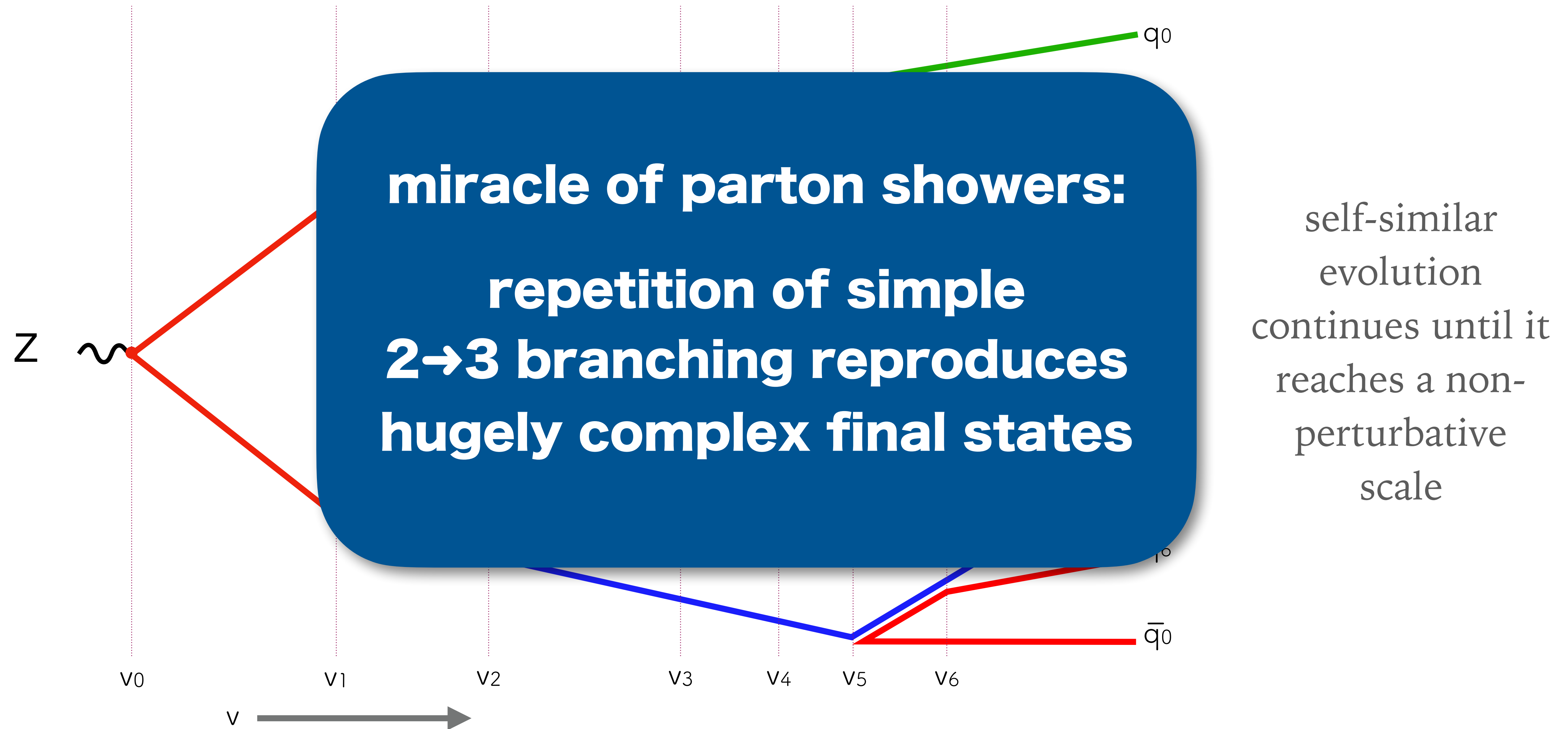
# QCD shower: an evolution equation (in **evolution scale $v$** , e.g. trans.mom.)



self-similar  
evolution  
continues until it  
reaches a non-  
perturbative  
scale



# QCD shower: an evolution equation (in **evolution scale $v$** , e.g. trans.mom.)





# selected collider-QCD accuracy milestones

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## Drell-Yan ( $\gamma/Z$ ) & Higgs production at hadron colliders

LO

NLO

NNLO[.....]

N3LO

1970

1980

1990

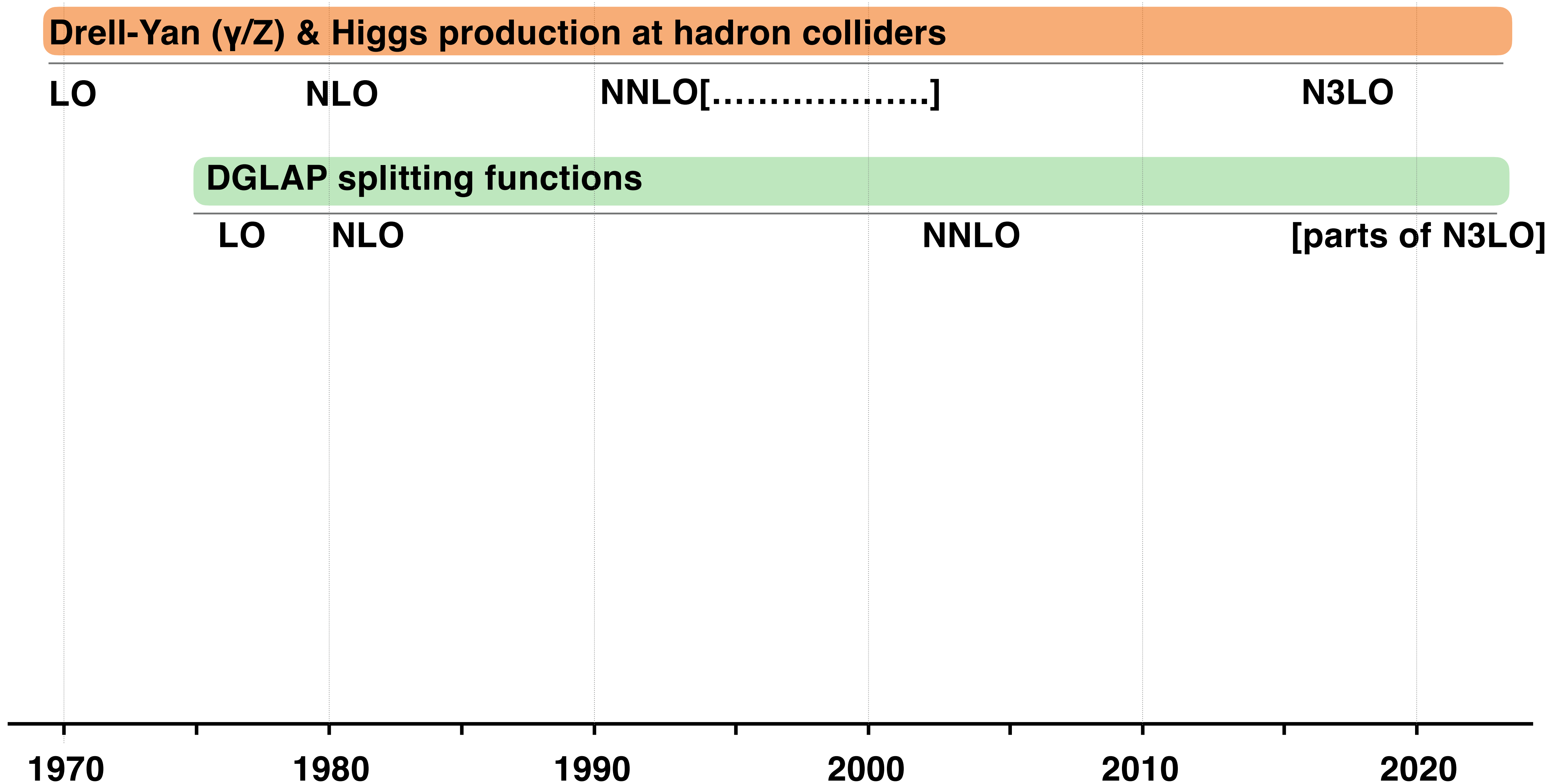
2000

2010

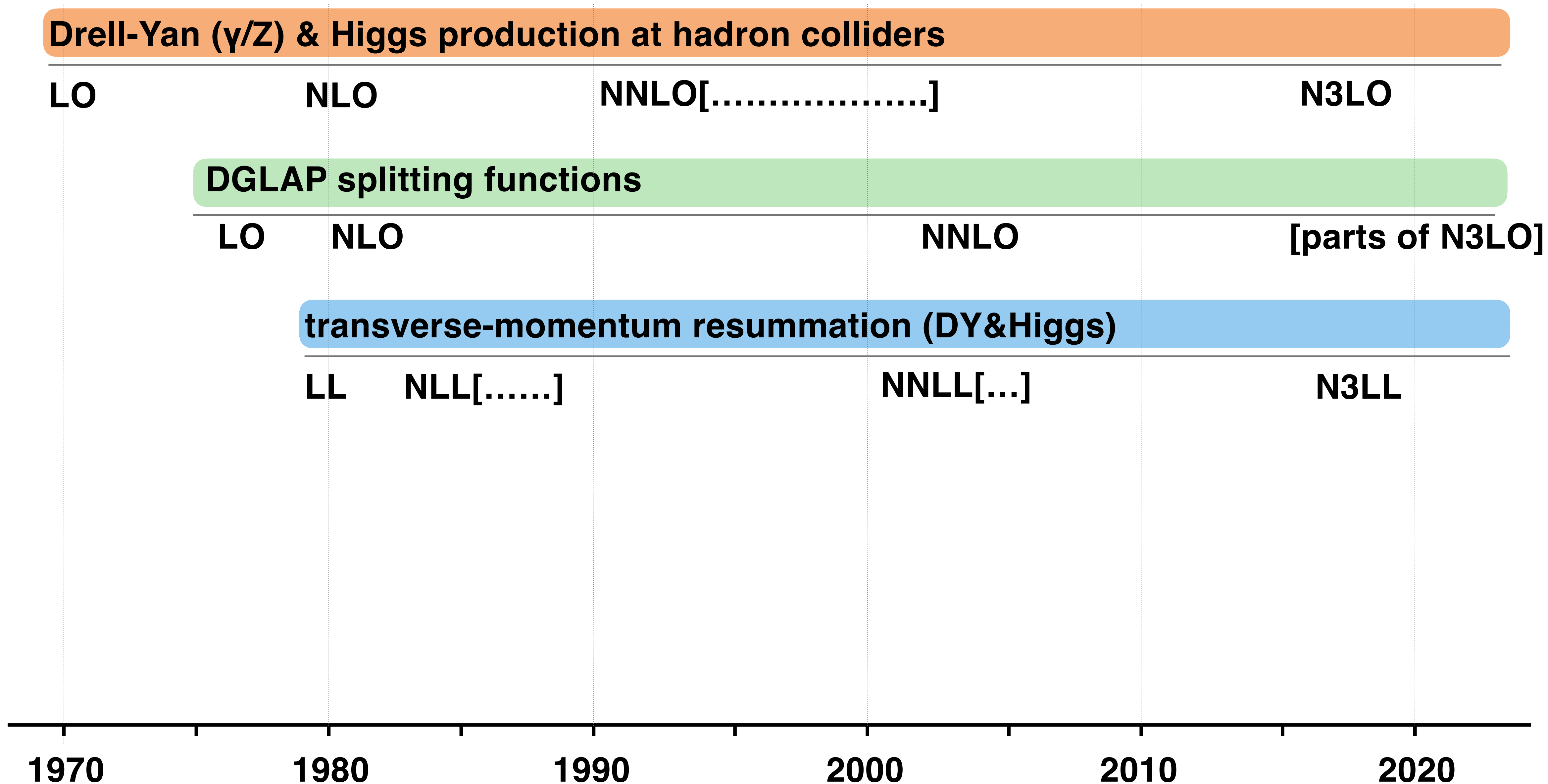
2020



# selected collider-QCD accuracy milestones

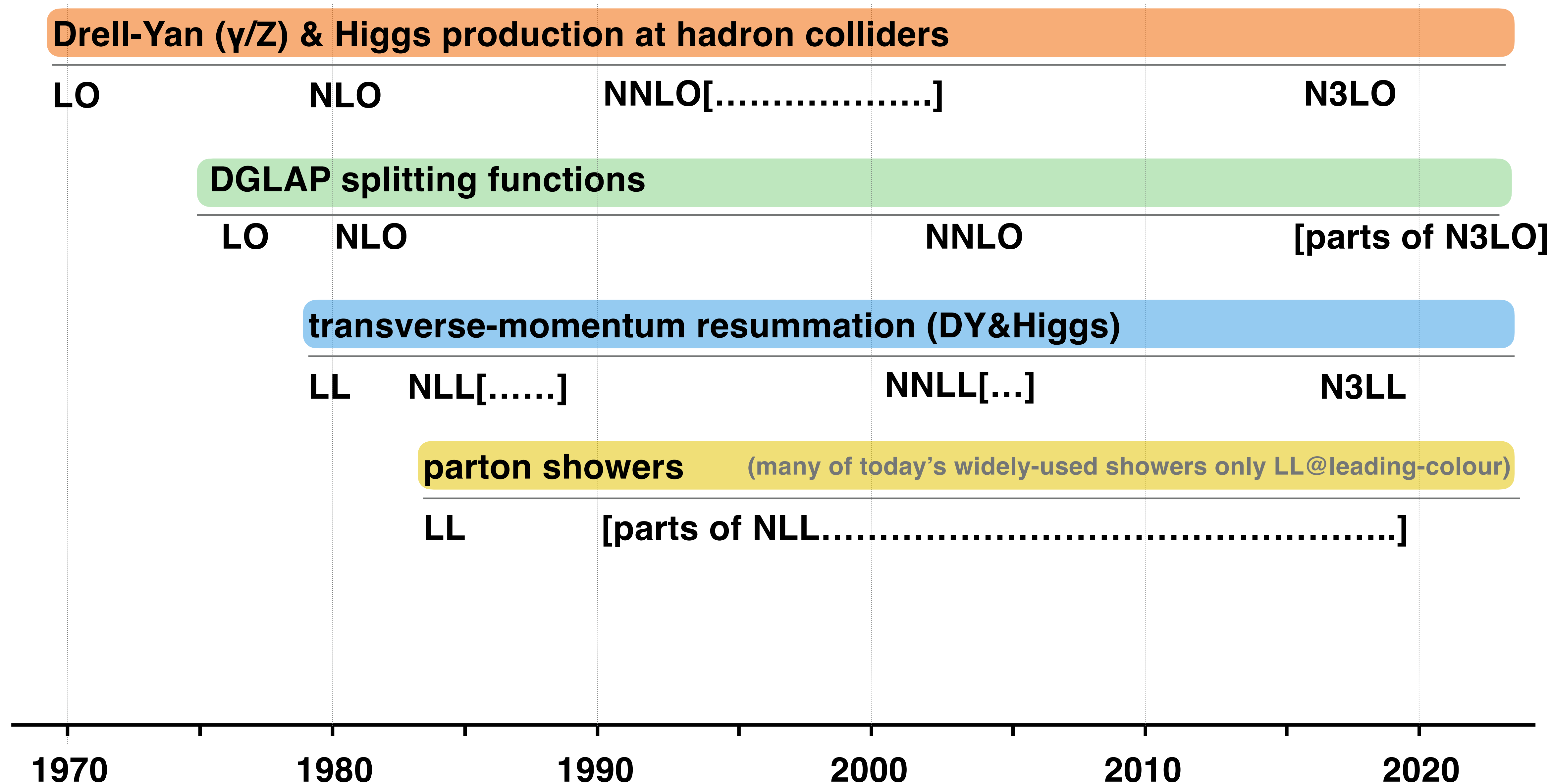


# selected collider-QCD accuracy milestones

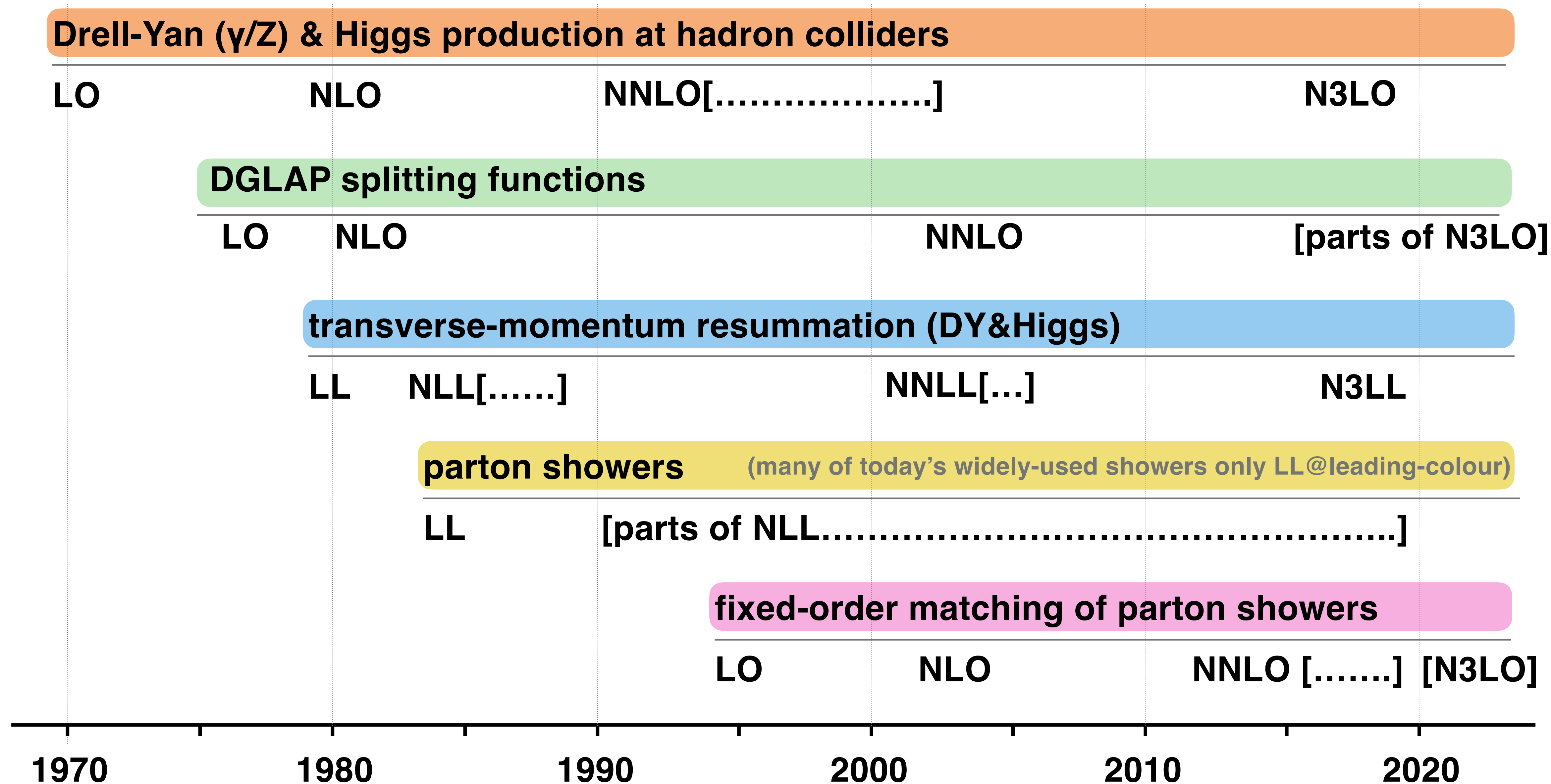




# selected collider-QCD accuracy milestones

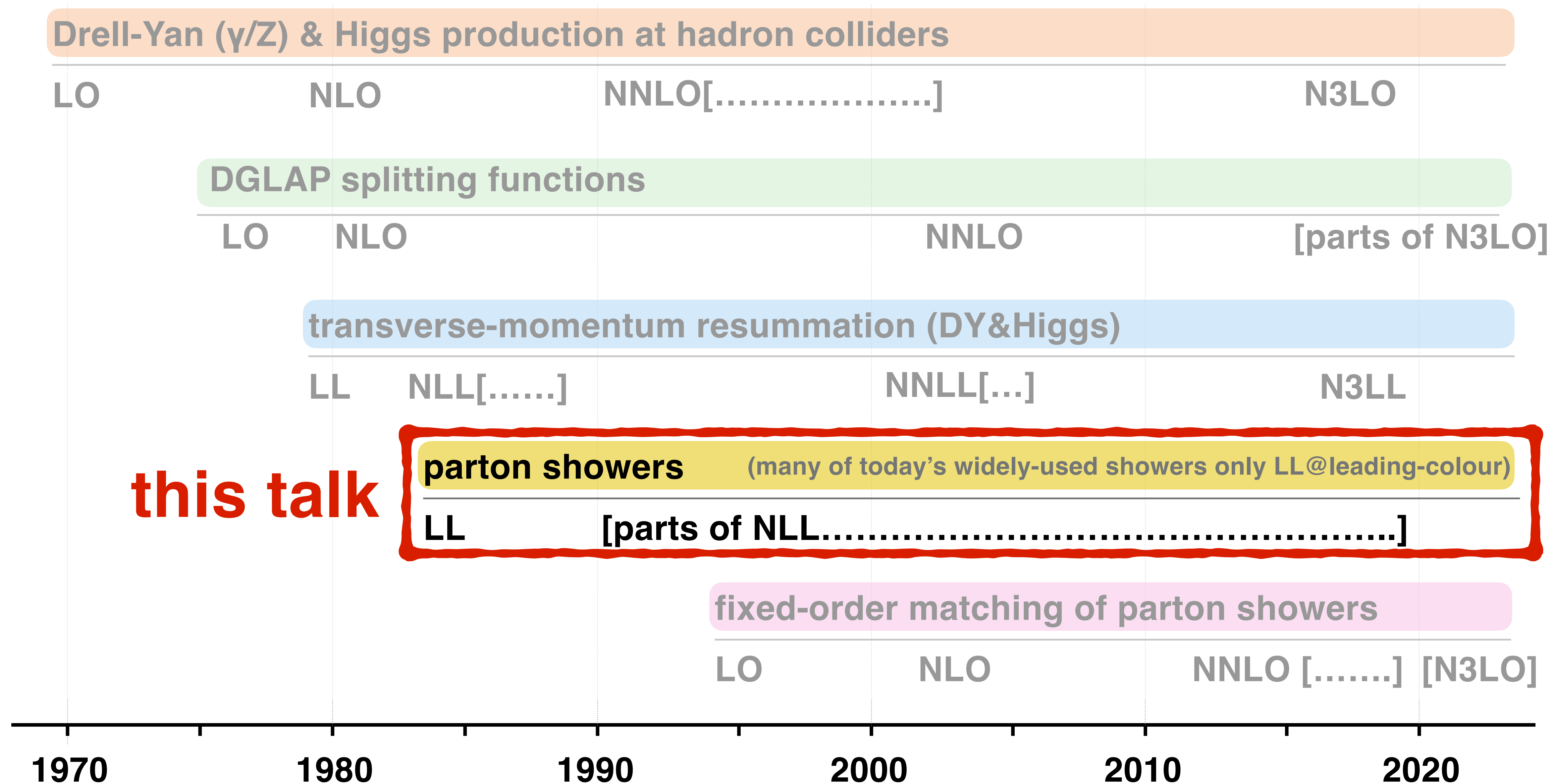


# selected collider-QCD accuracy milestones





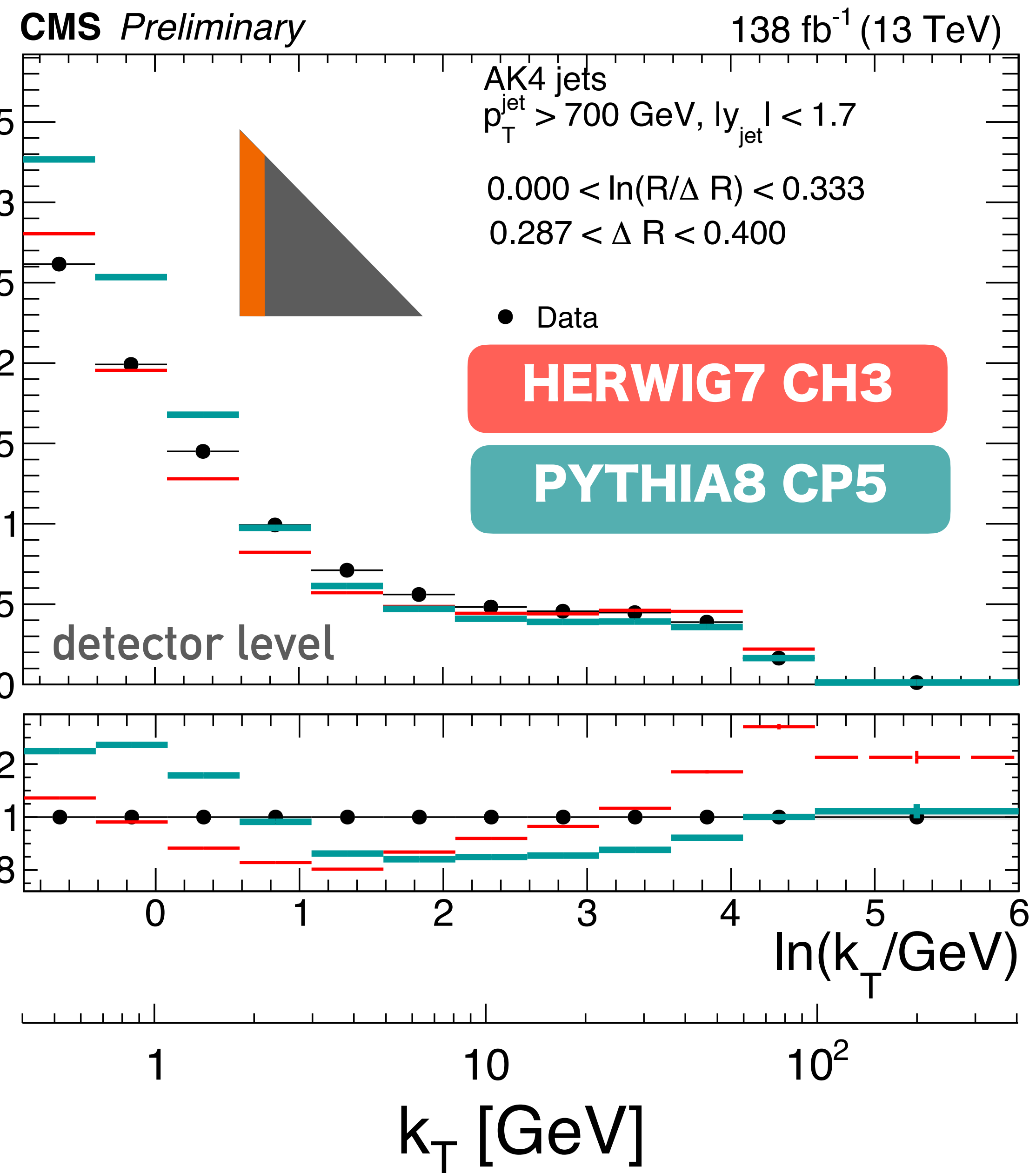
# selected collider-QCD accuracy milestones



# Are showers good enough?

- ▶ showers do an amazing job on many observables
- ▶ but various places see 10–30% discrepancies between showers and data
- ▶ feeds into many analyses (e.g. via jet-energy scale)
- ▶ as machine learning makes use of ever more information in jets & whole event, we want simulations to get it right

## Lund Plane (Negro & Rossini talks; also ATLAS & ALICE)





# We want to design **guaranteed NLL** showers

*Dasgupta, Dreyer, Hamilton, Monni, GPS '18  
ibid + Soyez '20*

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## A Matrix Element condition

- correctly reproduce  $n$ -parton tree-level matrix element for arbitrary configurations, so long as all emissions well separated in the Lund diagram
- supplement with unitarity, 2-loop running coupling & cusp anomalous dimension

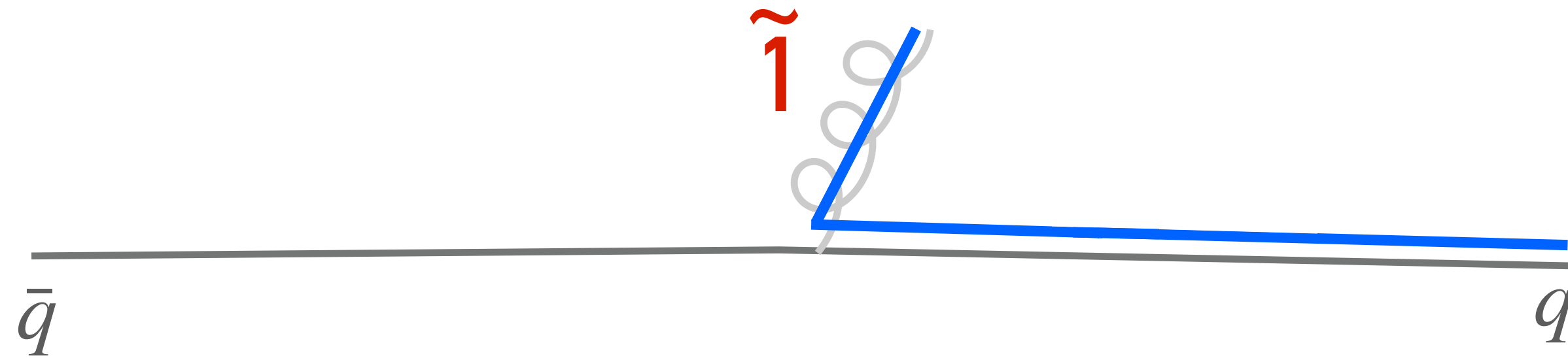
## Resummation condition: reproduce NLL results for all standard resummations

- global event shapes
- non-global observables
- fragmentation functions
- multiplicities
- ...

# 1. Recoil: the core of any shower

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Dipole showers conserve momentum at each step. Traditional dipole-local recoil:



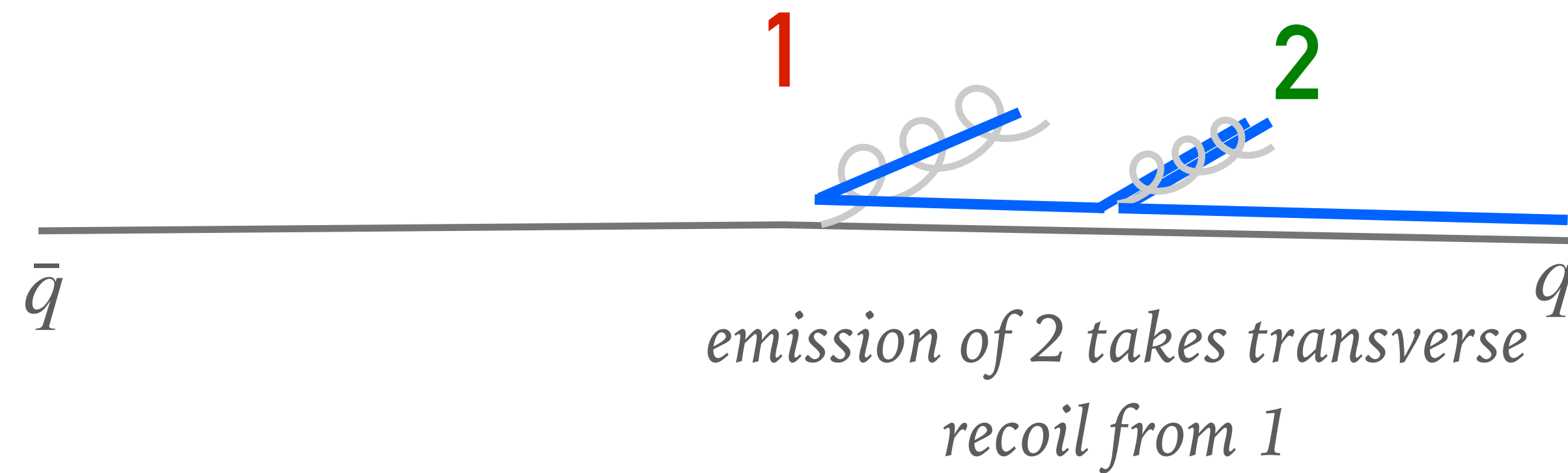
$$d\mathcal{P}_{\tilde{i} \rightarrow ik}^{\text{FS}} = \frac{\alpha_s(k_{\perp}^2)}{2\pi} \frac{dk_{\perp}^2}{k_{\perp}^2} \frac{dz}{z} \frac{d\varphi}{2\pi} N_{ik}^{\text{sym}} [z P_{\tilde{i} \rightarrow ik}(z)]$$



# 1. Recoil: the core of any shower

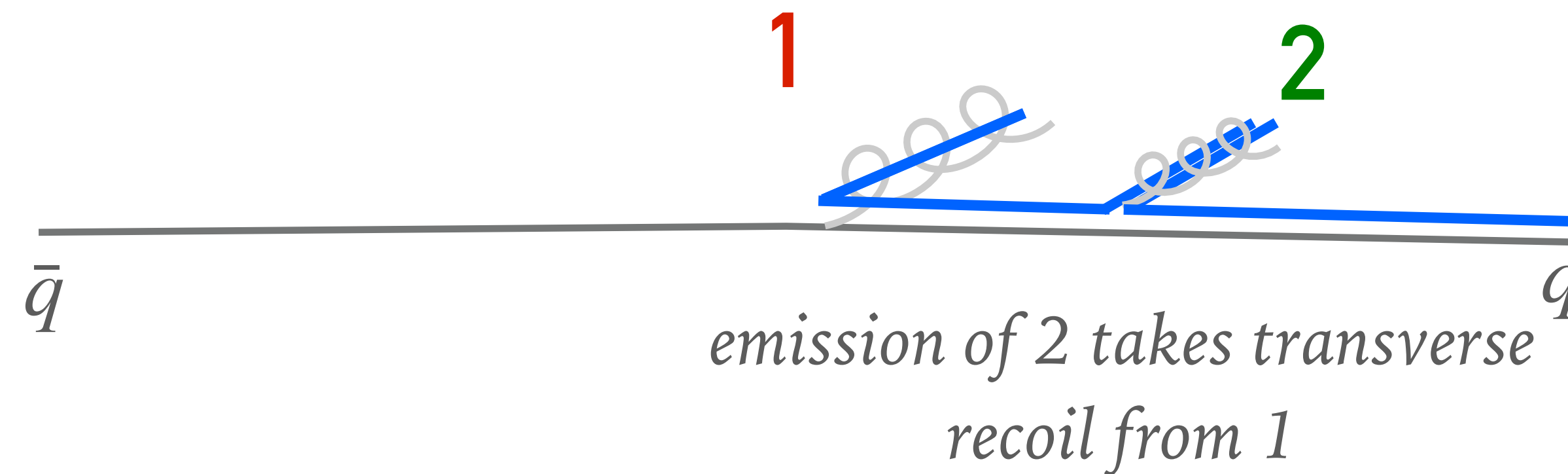
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# 1. Recoil: the core of any shower

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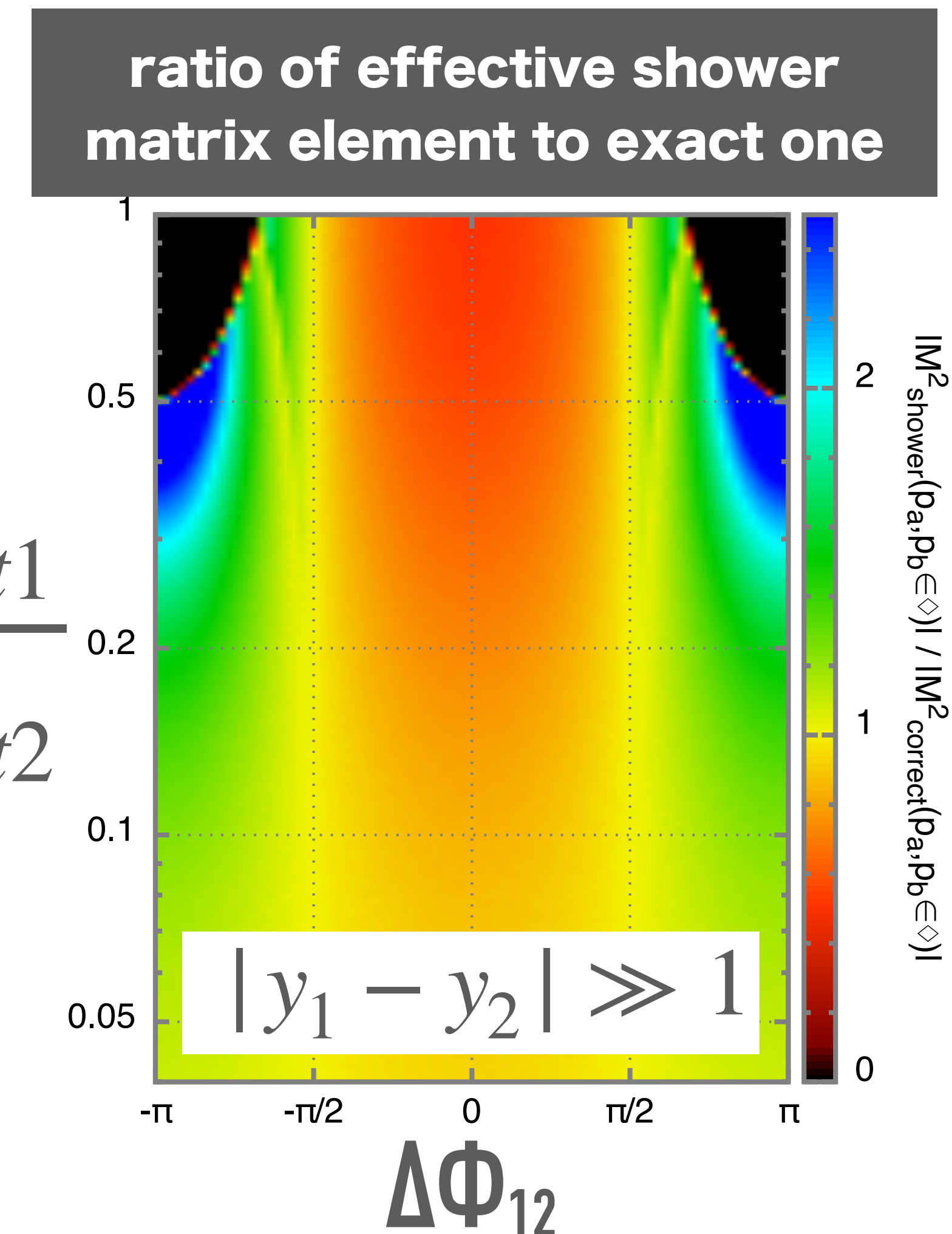
Shower initially generated matrix element for particle  $\tilde{1}$ , whose momentum differs (by  $\sim 50\%$ ) from final particle 1.

**Matrix element is incorrect wrt final momentum 1.**

First observed: Andersson, Gustafson, Sjogren '92

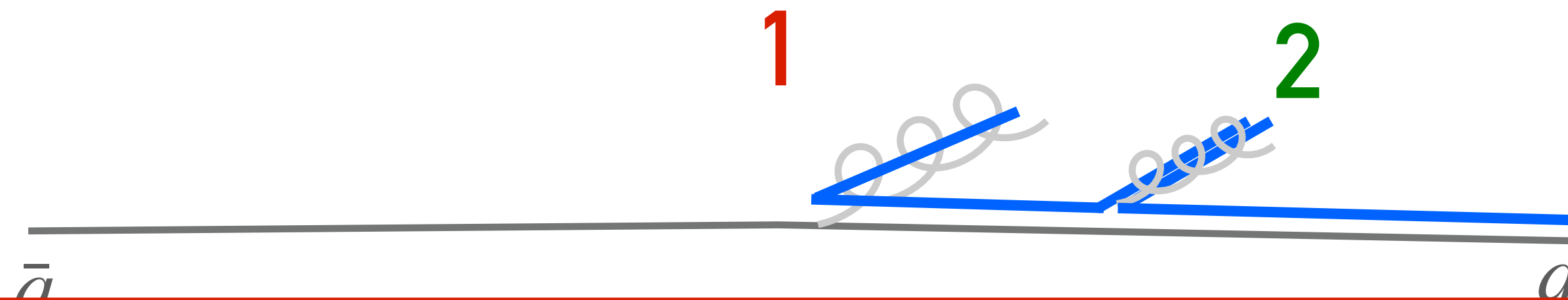
Closely related effect present for Z  $p_t$ : Nagy & Soper [0912.4534](#)

Impact on log accuracy across many observables: Dasgupta, Dreyer, Hamilton, Monni, GPS, [1805.09327](#)



# 1. Recoil: the core of any shower

Dipole showers conserve momentum at each step. Traditional dipole-local recoil:



design principle for new showers:

recoil & other shower design should respect  
absence of cross-talk between disparate scales  
(e.g. angles), i.e. QCD factorisation

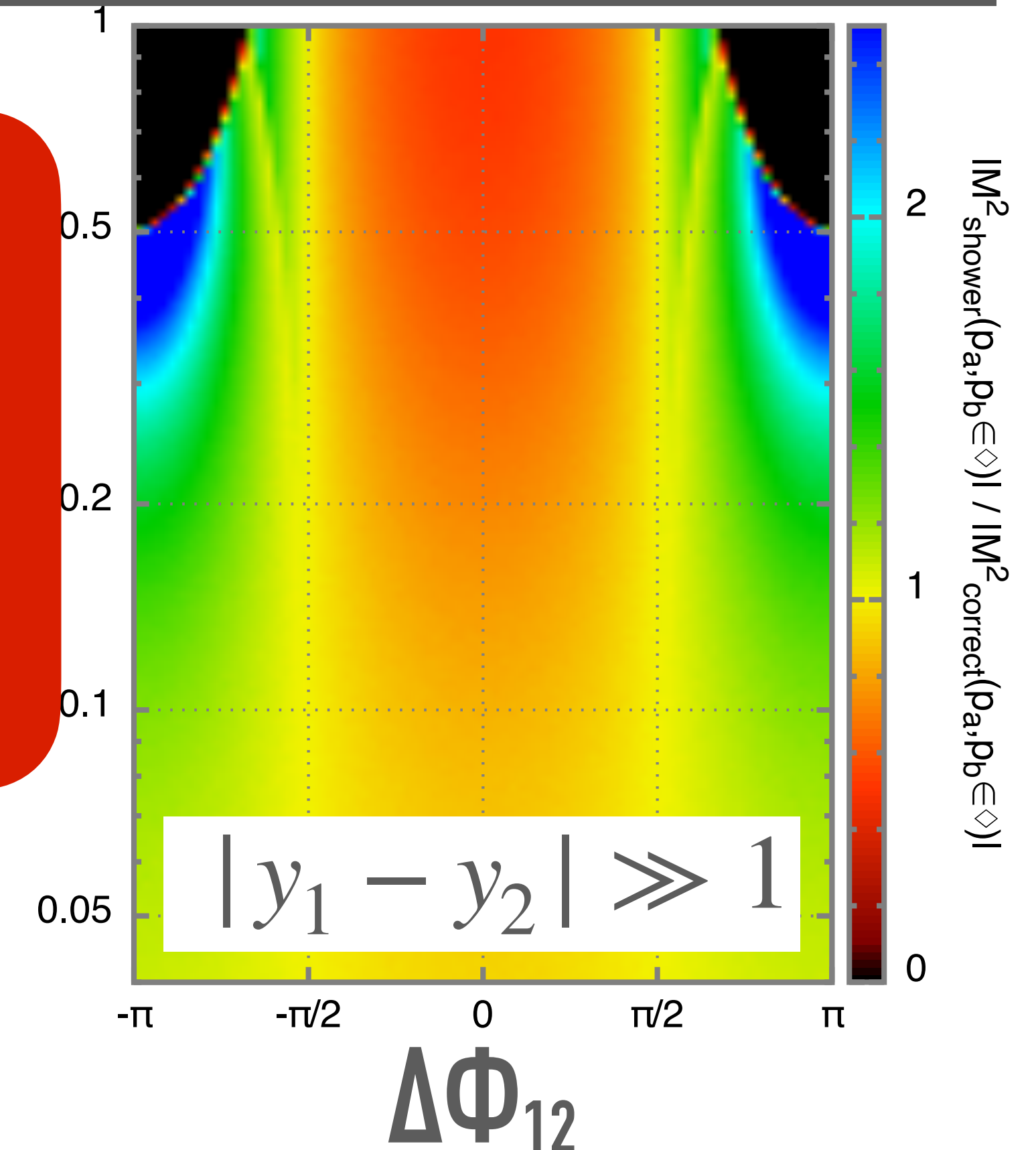
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ratio of effective shower  
matrix element to exact one





## Oxford



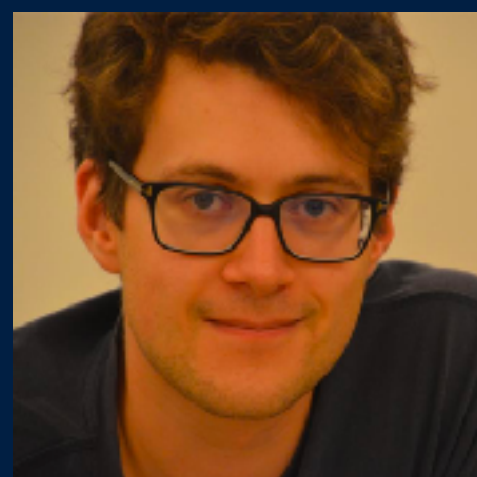
Melissa van Beekveld



Jack Helliwell



Rok Medves



Frederic Dreyer



GPS



Ludo Scyboz

## CERN



Mrinal Dasgupta



Gregory Soyez



Pier Monni



Alexander  
Karlberg



Alba  
Soto Ontoso



Silvia  
Ferrario Ravasio

## UCL



Keith Hamilton



Rob Verheyen

## Manchester



Basem El-Menoufi

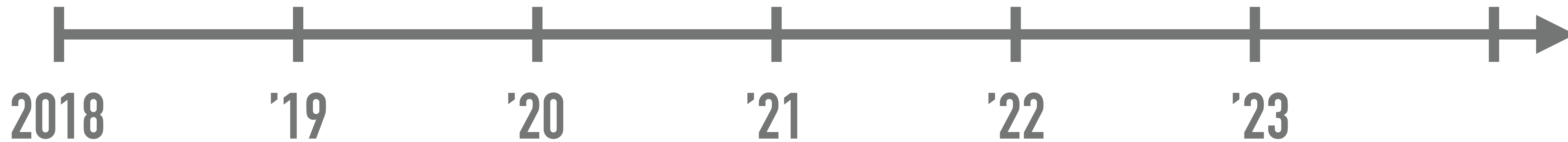
## PanScales

A project to bring logarithmic understanding and accuracy to parton showers

# PanScales timeline

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calculations

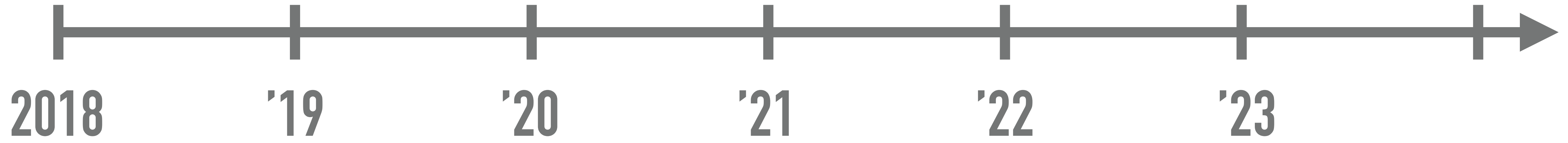


NLL shower

# PanScales timeline

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calculations

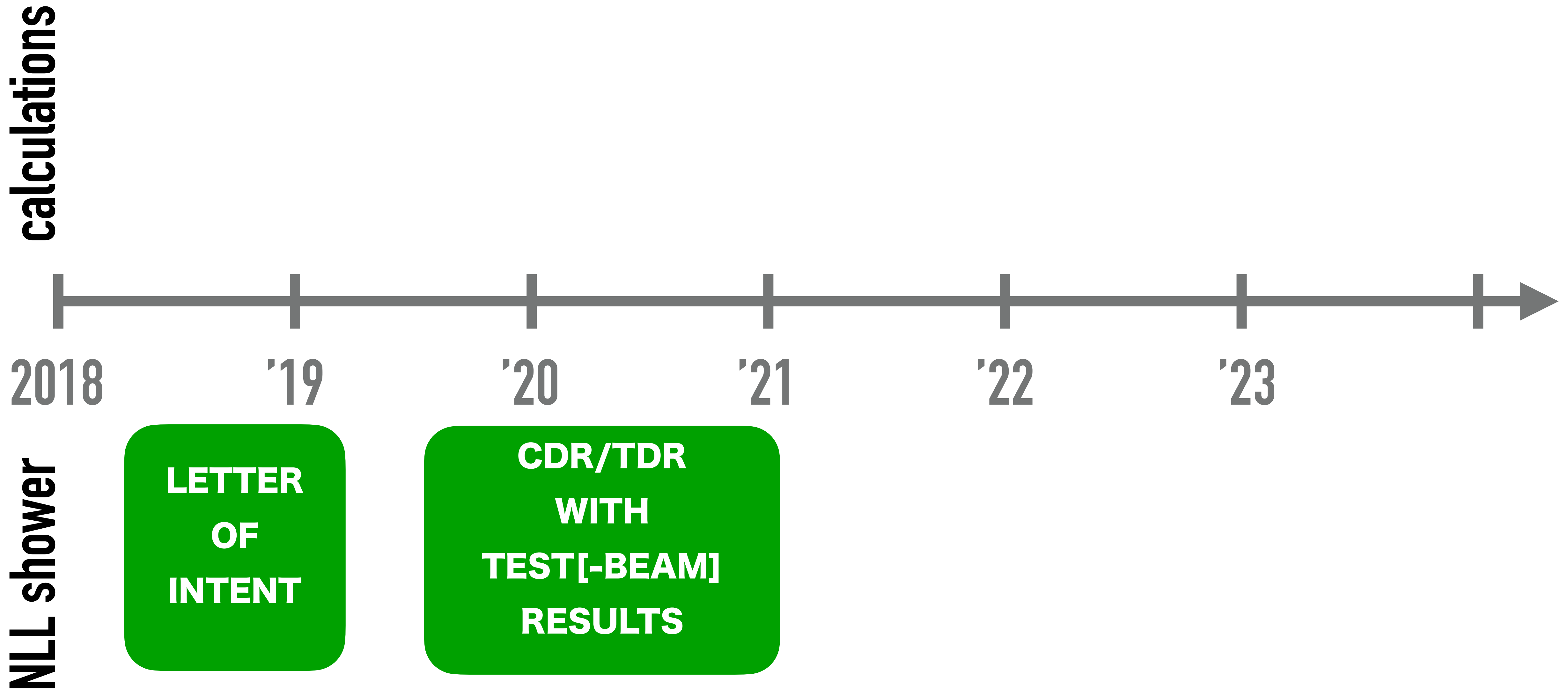


NLL shower

**LETTER  
OF  
INTENT**

# PanScales timeline

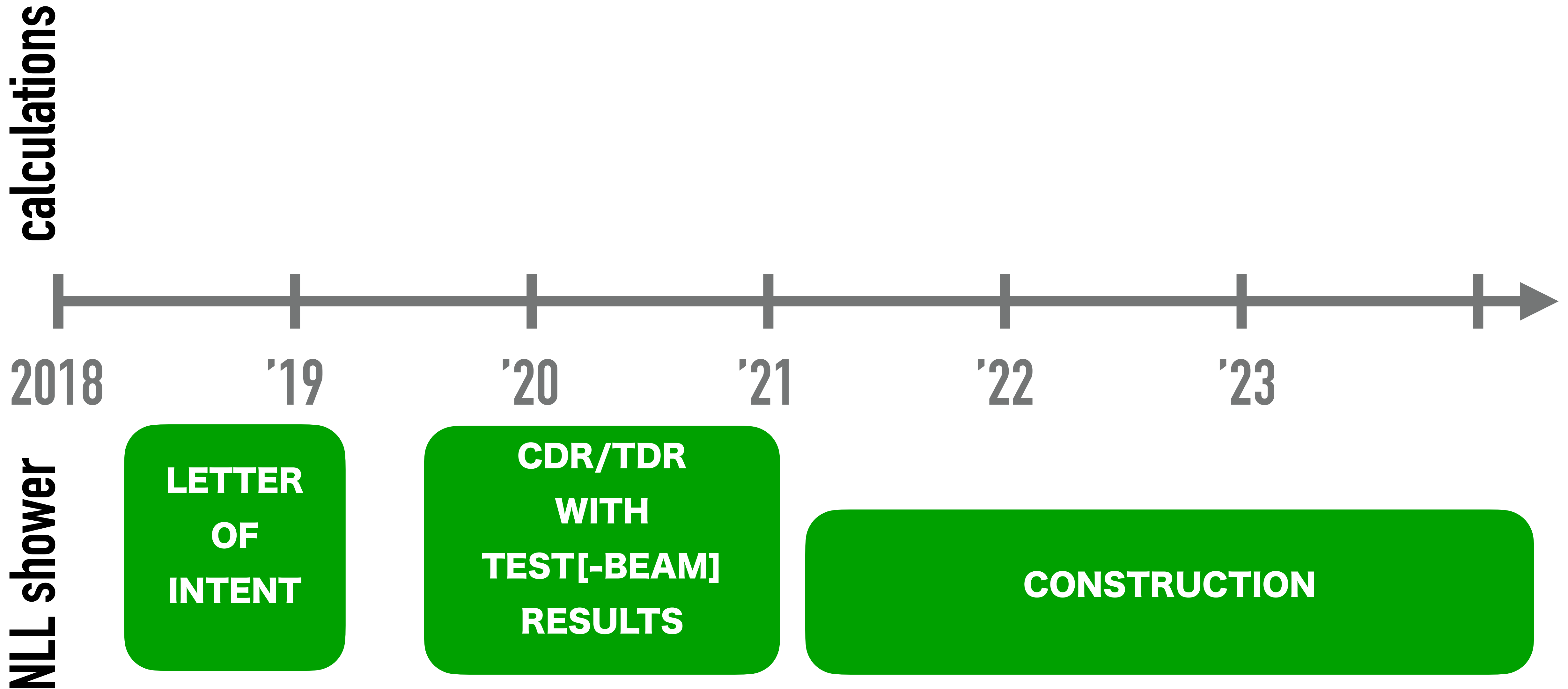
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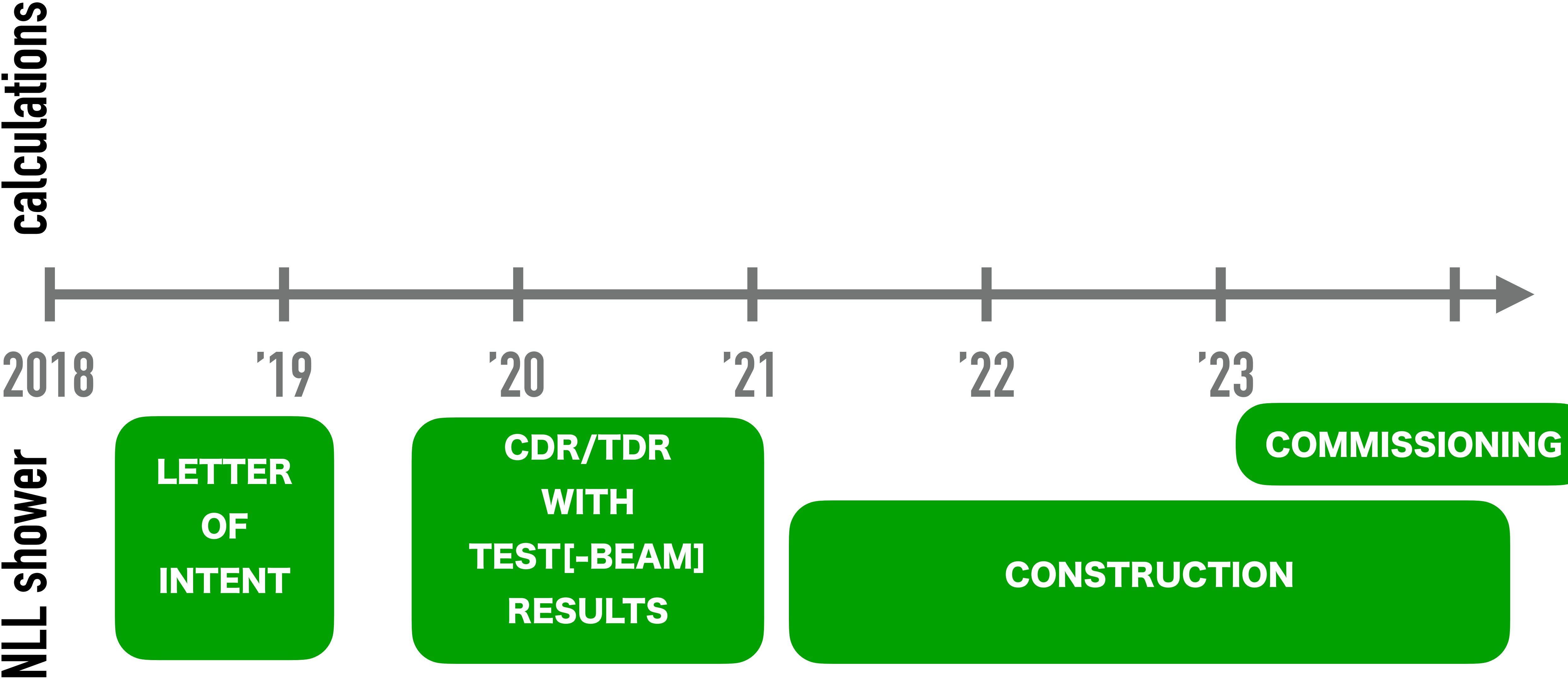


# PanScales timeline

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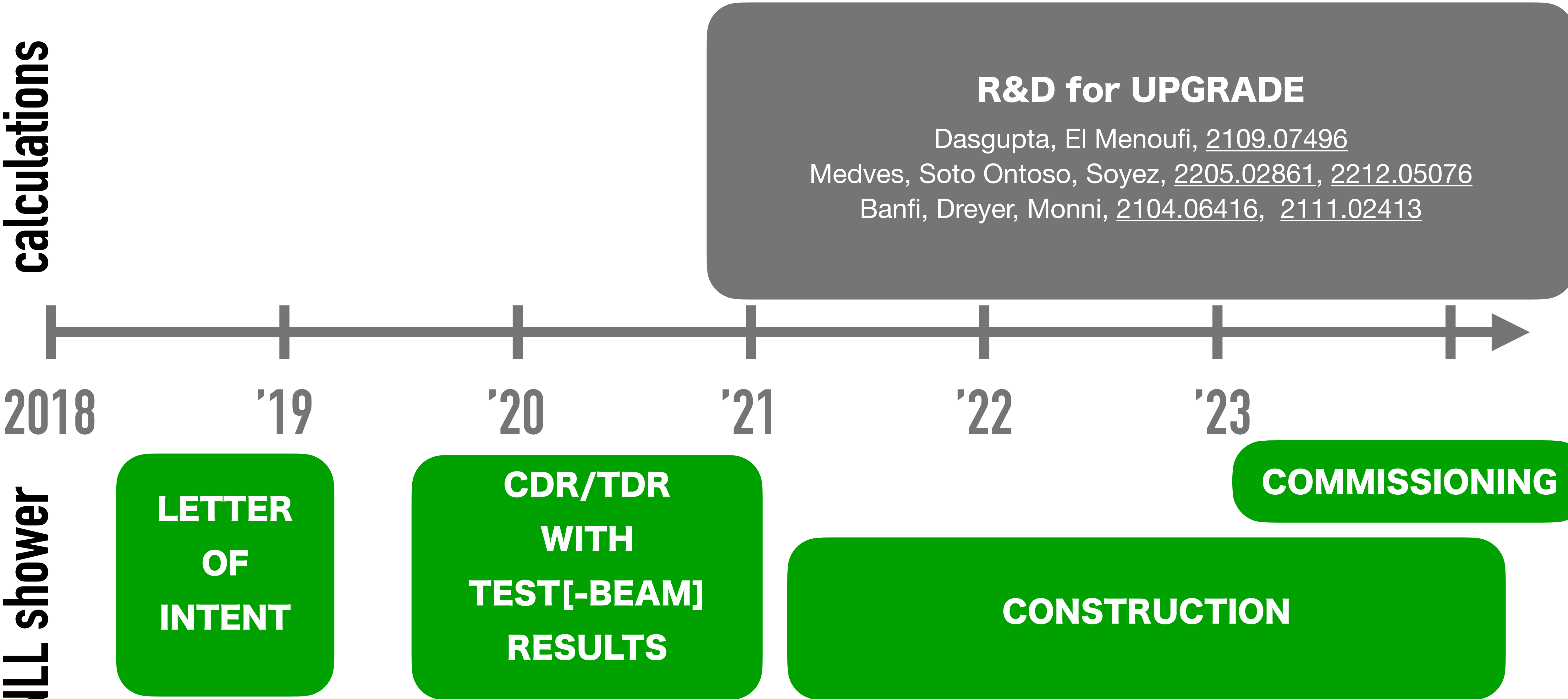
# PanScales timeline



# PanScales timeline

calculations

NLL shower



### PanLocal

$k_t \sqrt{\theta}$  ordered

#### Recoil

$\perp$ : local

$+$ : local

$-$ : local

Dipole partition  
event CoM

### PanGlobal

$k_t$  or  $k_t \sqrt{\theta}$  ordered

#### Recoil

$\perp$ : global

$+$ : local

$-$ : local

Dipole partition  
event CoM

### Colour

nested ordered  
double soft  
(NODS)

Designed to  
ensure LL are  
full colour  
(also gets many  
NLL at full  
colour)

### Spin

for correct  
azimuthal  
structure in  
collinear and  
soft  $\rightarrow$  collinear

[Collins-Knowles  
extended to soft  
sector]

*e<sup>+</sup>e<sup>-</sup>*: Dasgupta, Dreyer, Hamilton, Monni, GPS & Soyez, 2002.11114; *pp*: van Beekveld, Ferrario Ravasio, GPS, Soto Ontoso, Soyez, Verheyen, 2205.02237; & *pp* tests, *ibid* + Hamilton: 2207.09467

Hamilton, Medves, GPS, Scyboz, Soyez, 2011.10054

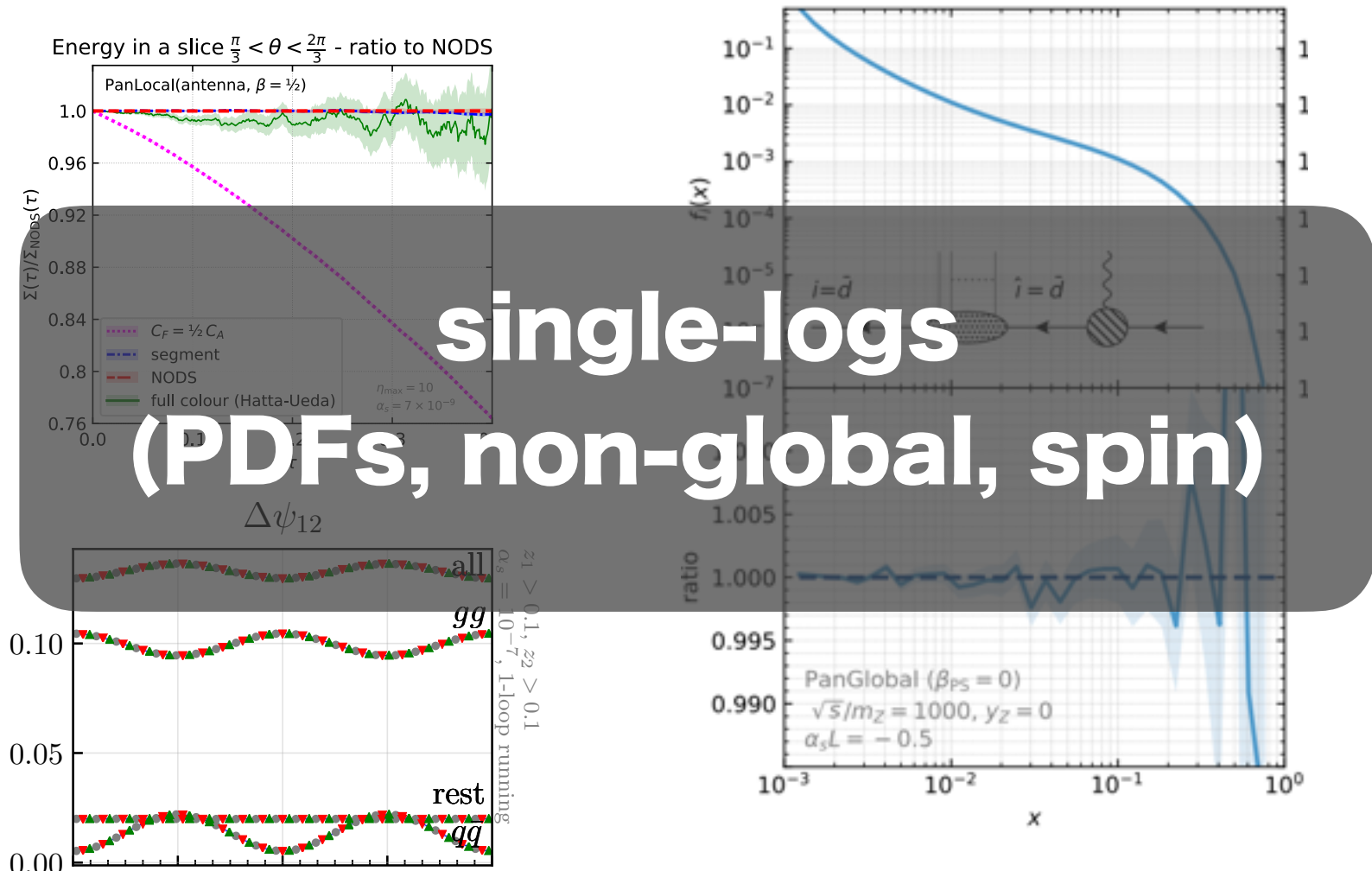
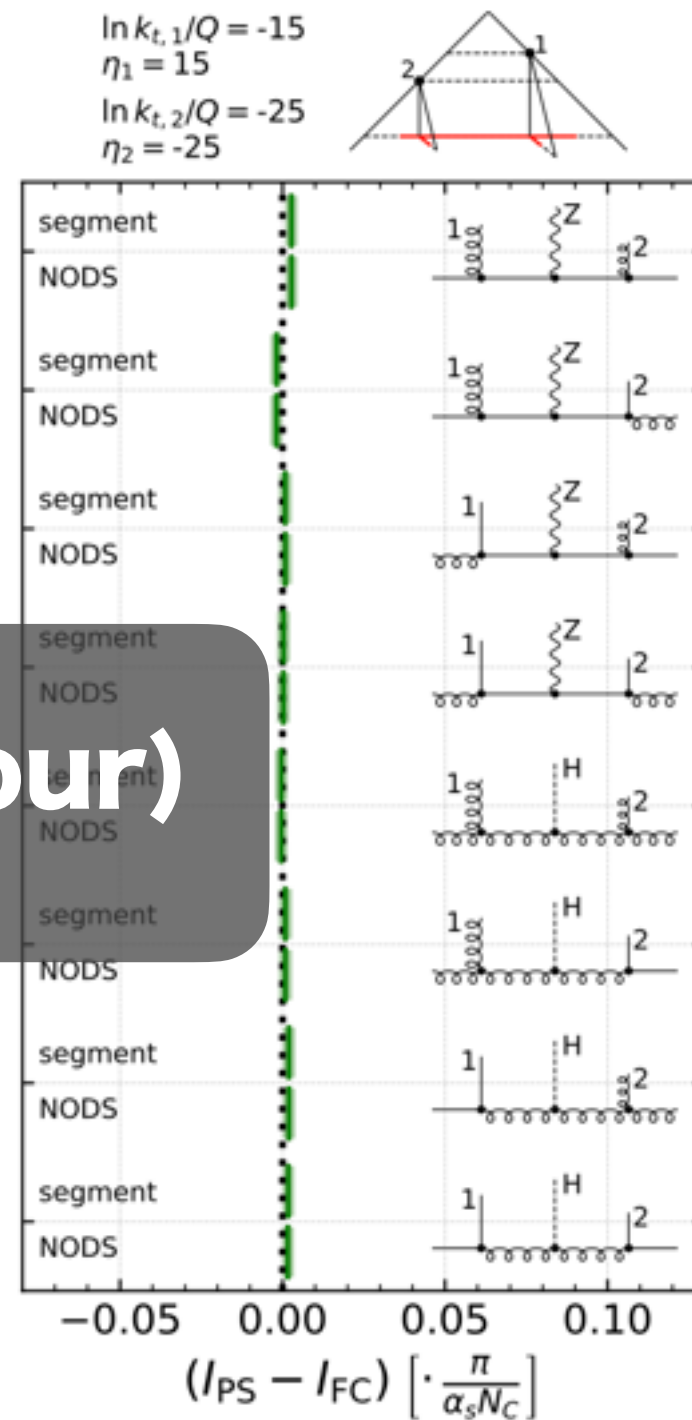
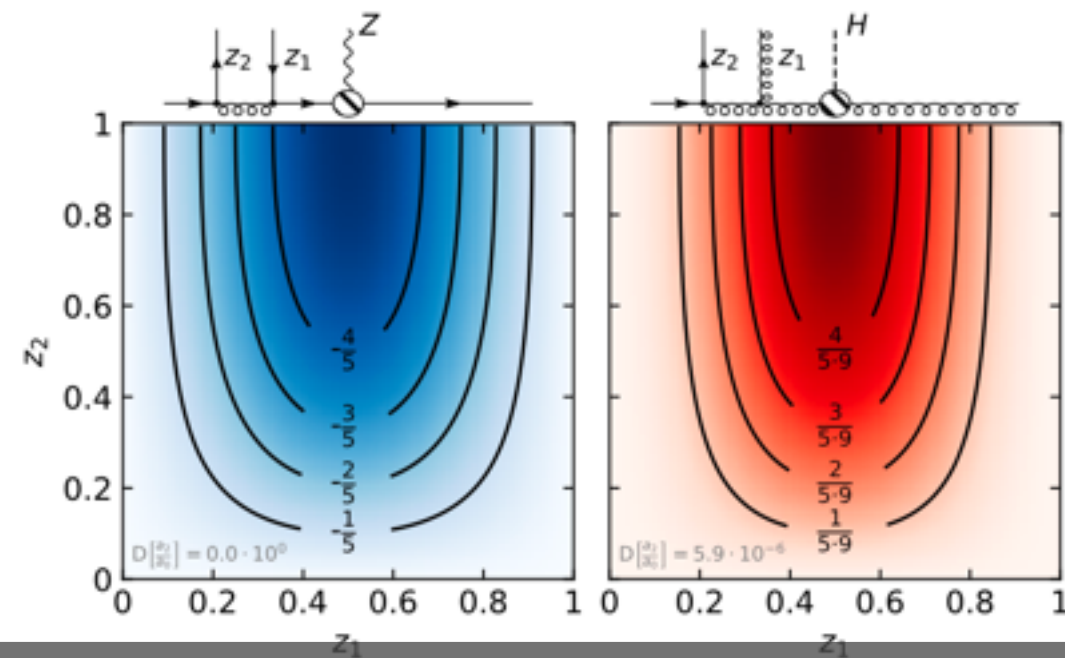
& *pp* extensions: van Beekveld et al, 2205.02237

Karlberg, GPS, Scyboz, Verheyen, 2011.10054; *ibid* + Hamilton, 2111.01161



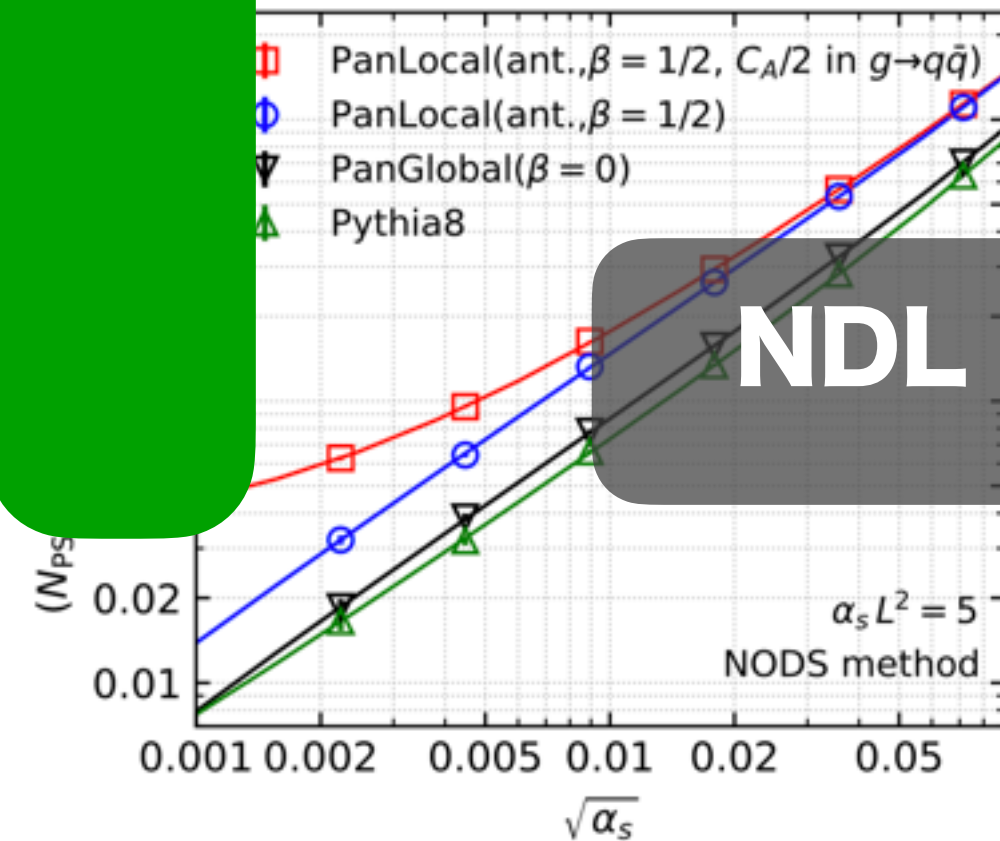
# a selection of the logarithmic accuracy tests

TESTS

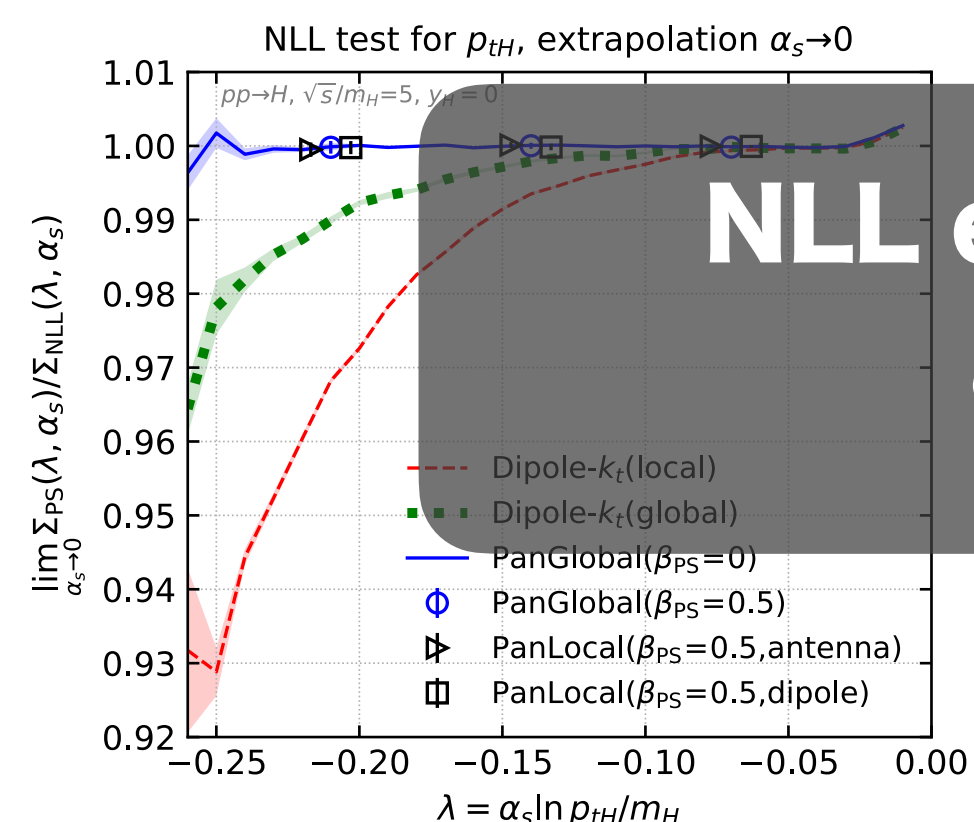
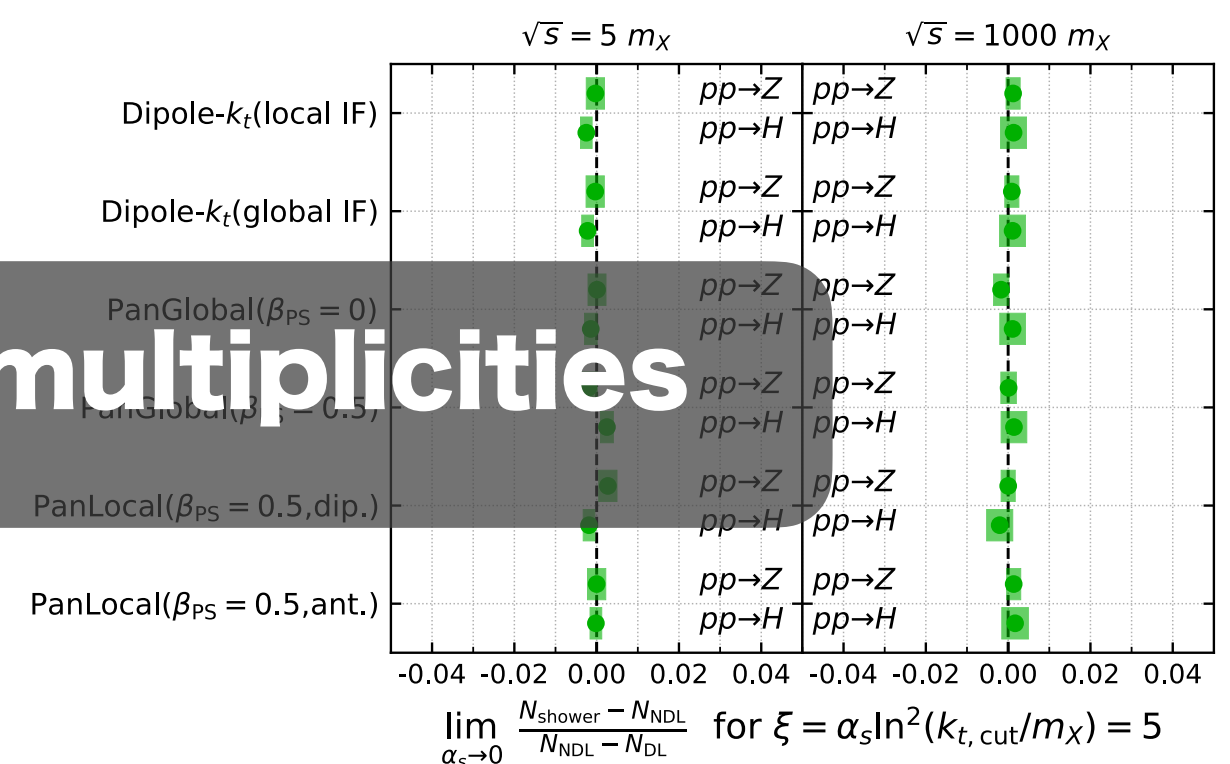


fixed order (kinematics, spin, colour)

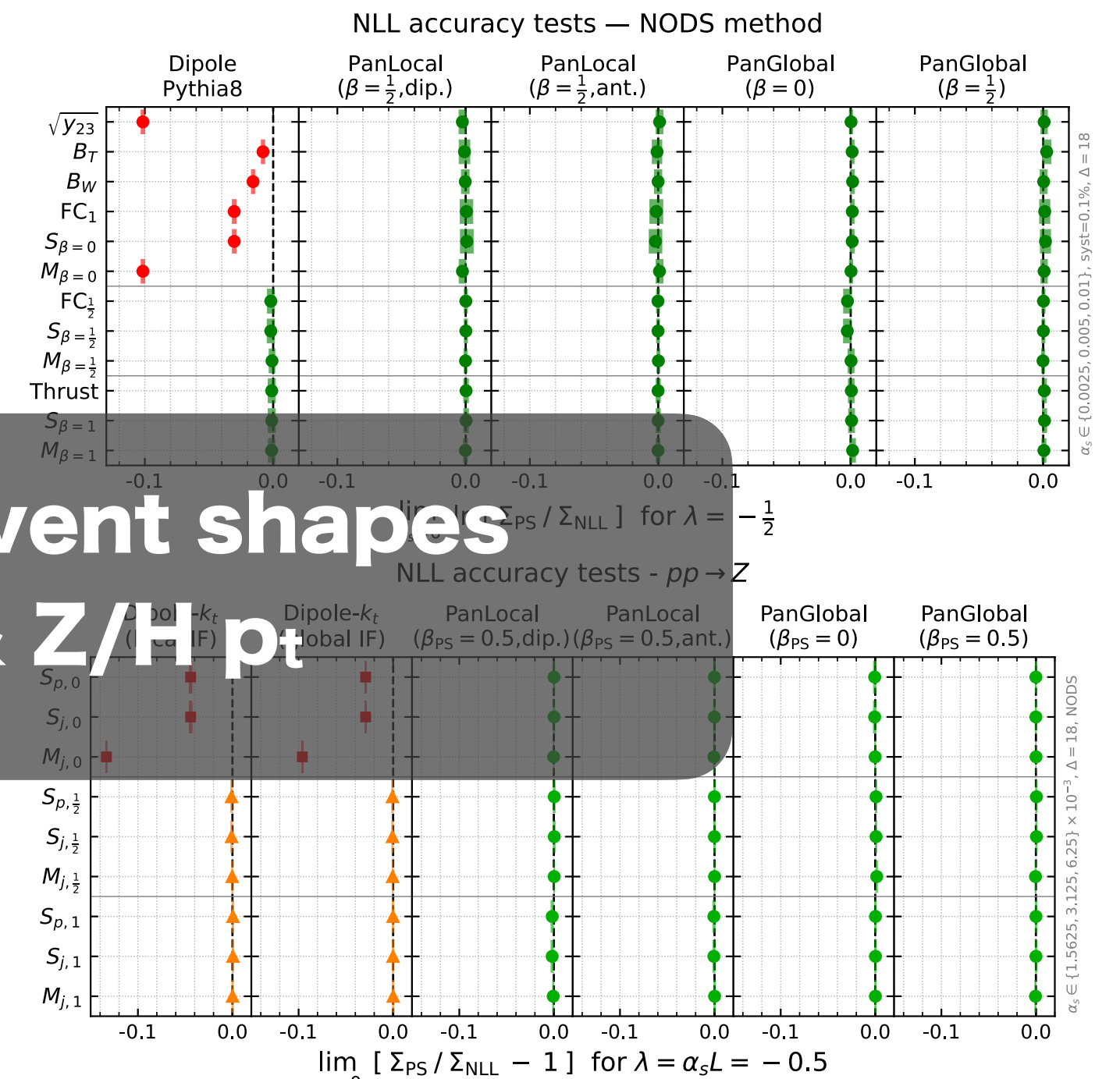
convergence towards NDL multiplicities

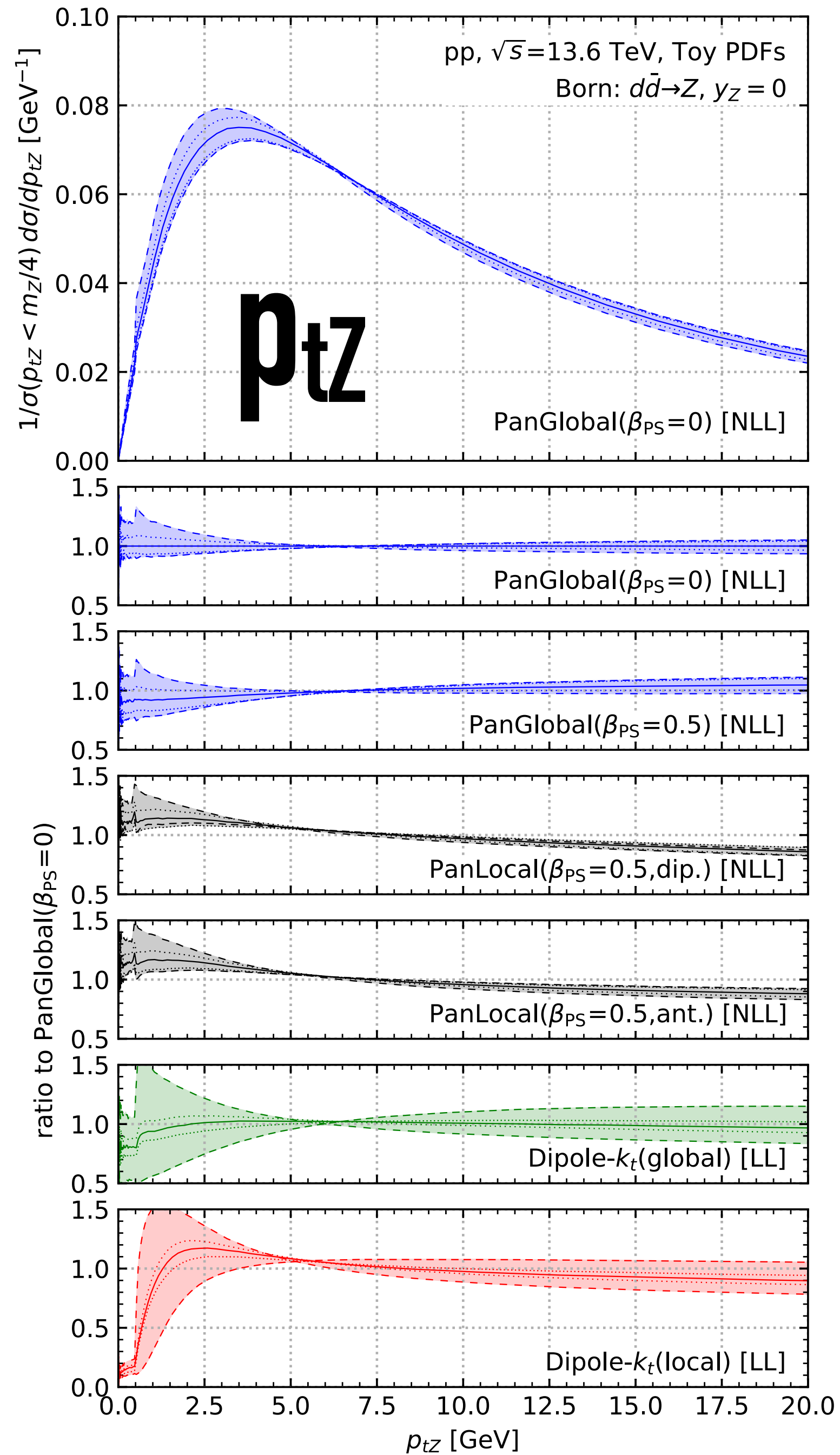


NDL multiplicities



NLL event shapes & Z/H pt





NLL  
showers

LL  
showers

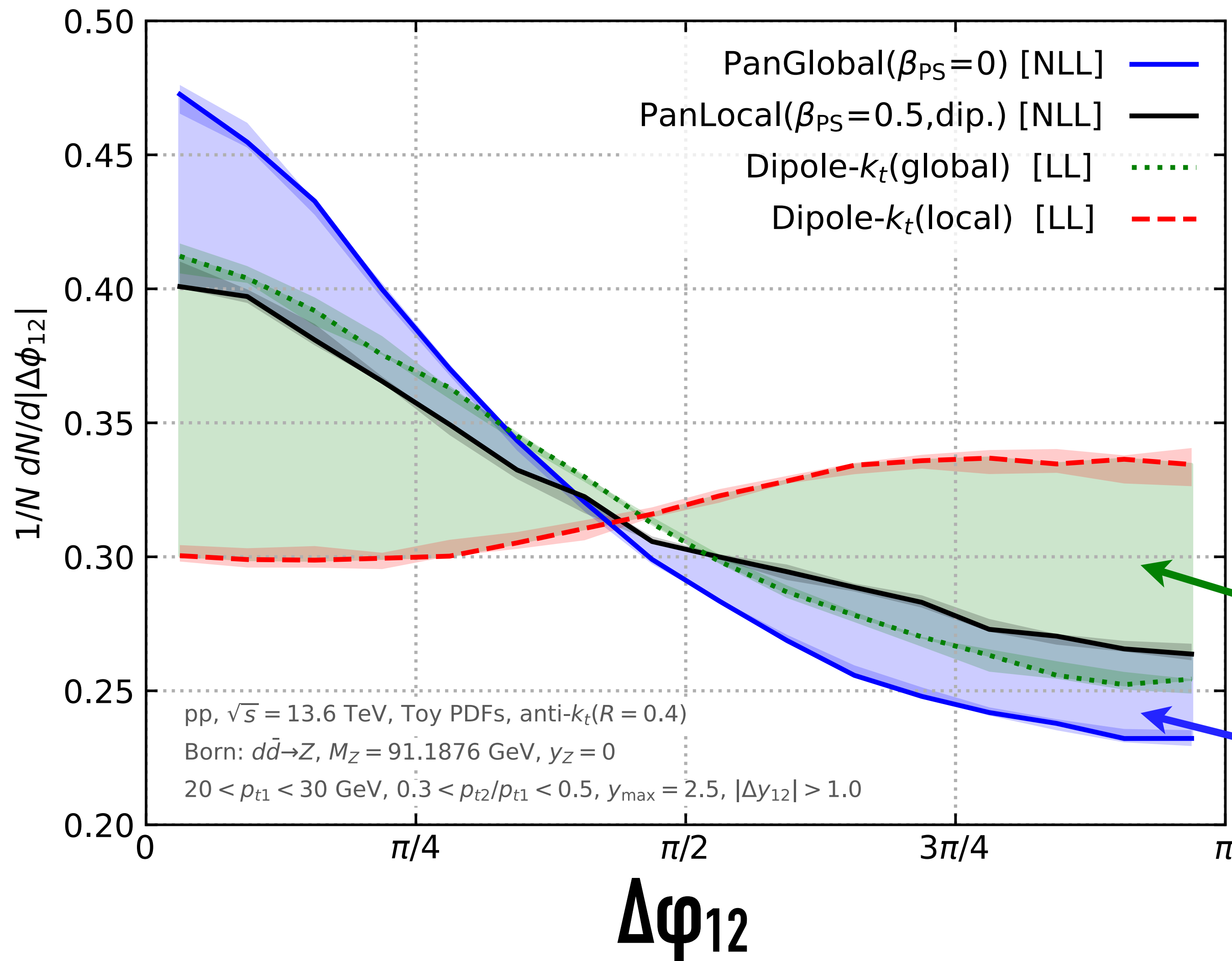
for inclusive quantities like  $p_{tZ}$ , advantage of NLL shower is partly in reduction of uncertainties

van Beekveld, Ferrario Ravasio, GPS,  
Soto Ontoso, Soyez, Verheyen,  
Hamilton: [2207.09467](https://arxiv.org/abs/2207.09467)



$$m_{\ell\ell} = m_Z$$

Azimuthal angle between leading jets (DY)



for more exclusive quantities, also see clear shape differences in going to NLL

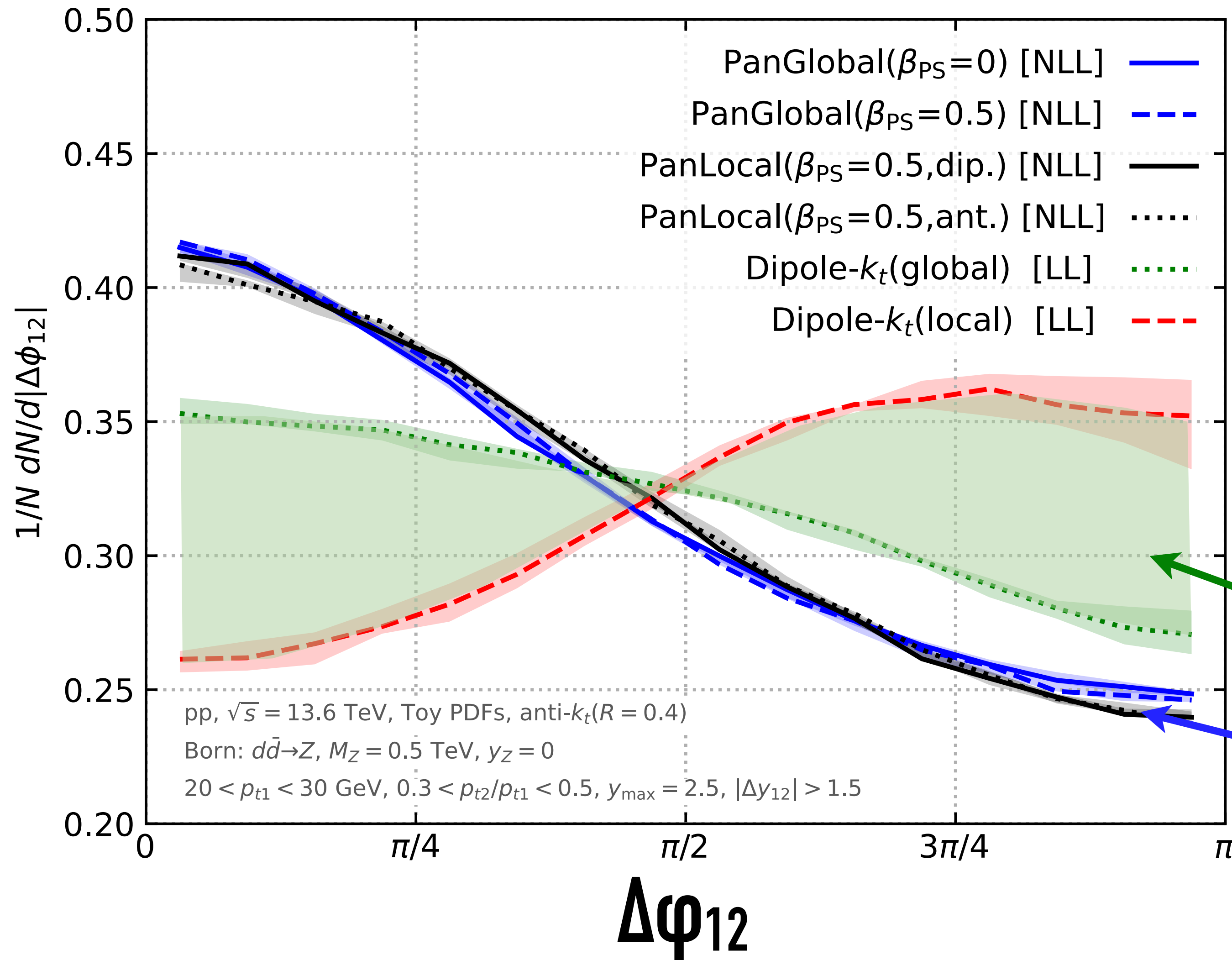
LL showers

NLL showers

van Beekveld, Ferrario Ravasio, GPS,  
 Soto Ontoso, Soyez, Verheyen,  
 Hamilton: [2207.09467](https://arxiv.org/abs/2207.09467)

$$m_{\ell\ell} = 500 \text{ GeV}$$

Azimuthal angle between leading jets (DY)



for more exclusive quantities, also see clear shape differences in going to NLL

especially at larger scales

LL showers

NLL showers

van Beekveld, Ferrario Ravasio, GPS,  
 Soto Ontoso, Soyez, Verheyen,  
 Hamilton: [2207.09467](https://arxiv.org/abs/2207.09467)

COMMISSIONING

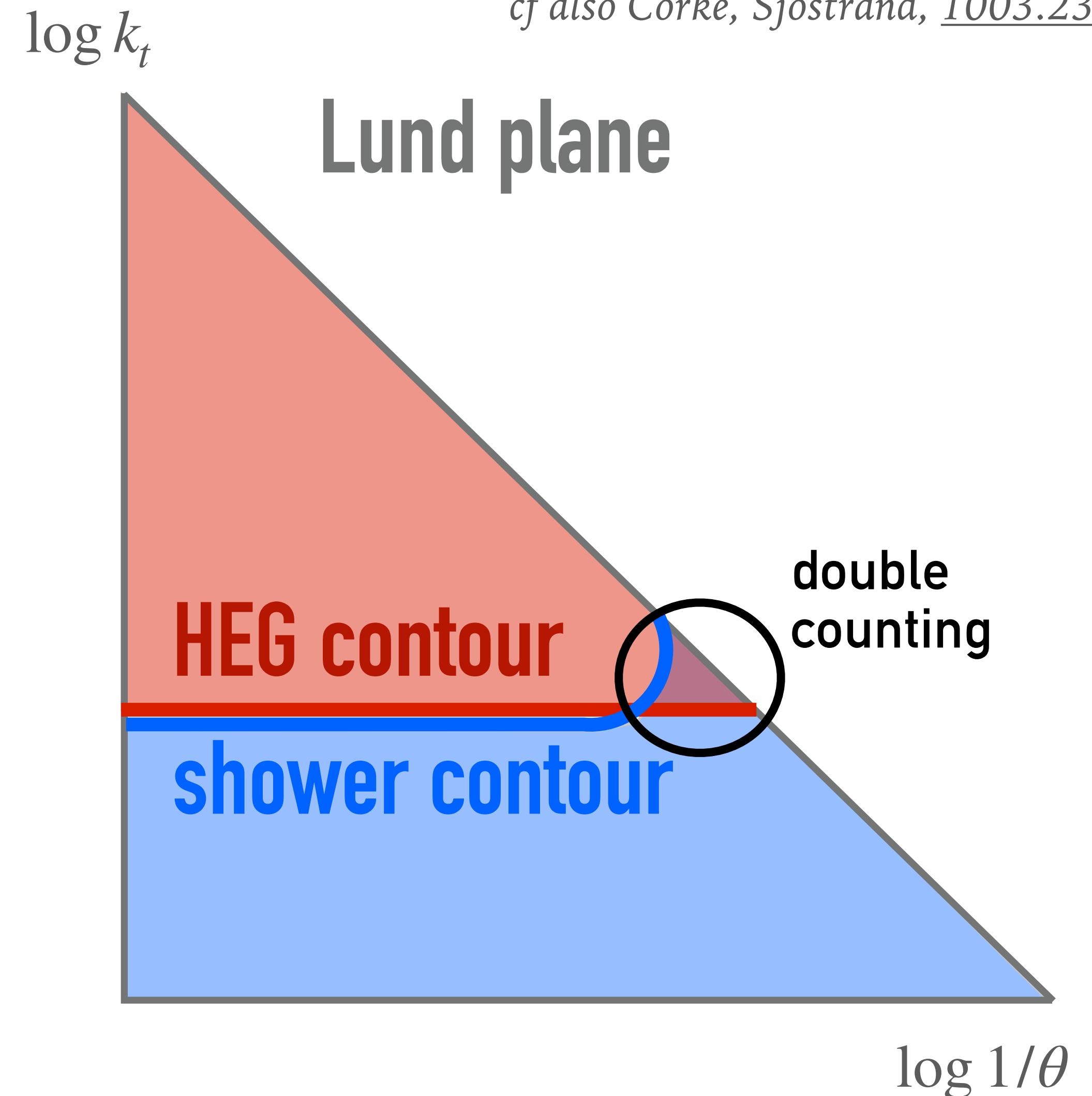


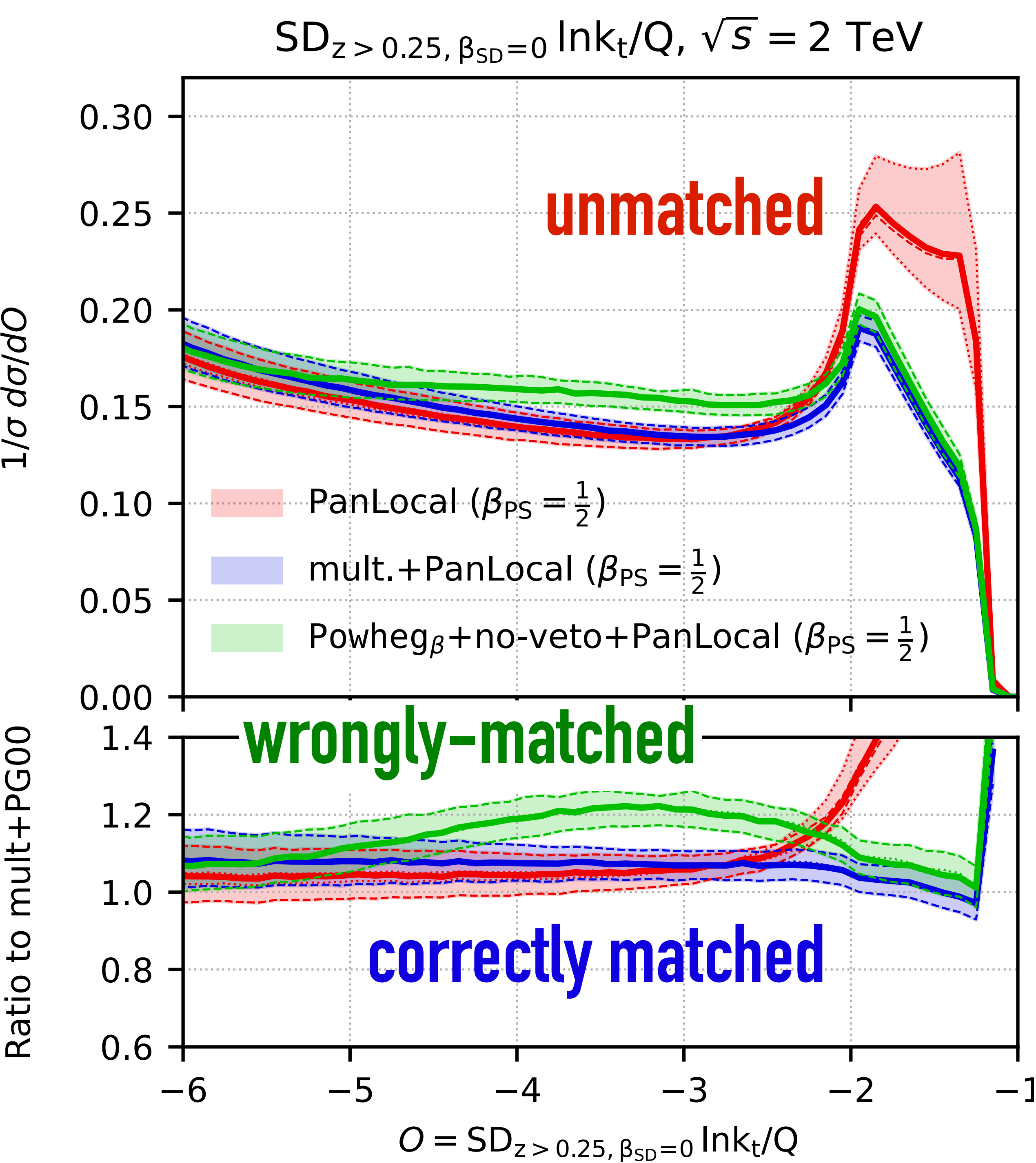
# Logarithmic accuracy and NLO matching

Hamilton, Karlberg, GPS,  
Scyboz, Verheyen, [2301.09645](#)

- Proof of concept explored for  $e^+e^- \rightarrow 2 \text{ jets @ NLO}$
- some matching schemes supplement shower with pure  $\mathcal{O}(\alpha_s)$ , e.g. MC@NLO, KrKNLO, MAcNLOPS:  
**these seem straightforward**
- in other schemes, first emission is generated by an external program (POWHEG, MINNLO, Geneva, etc.):  
**these need more care**

cf also Corke, Sjostrand, [1003.2384](#)





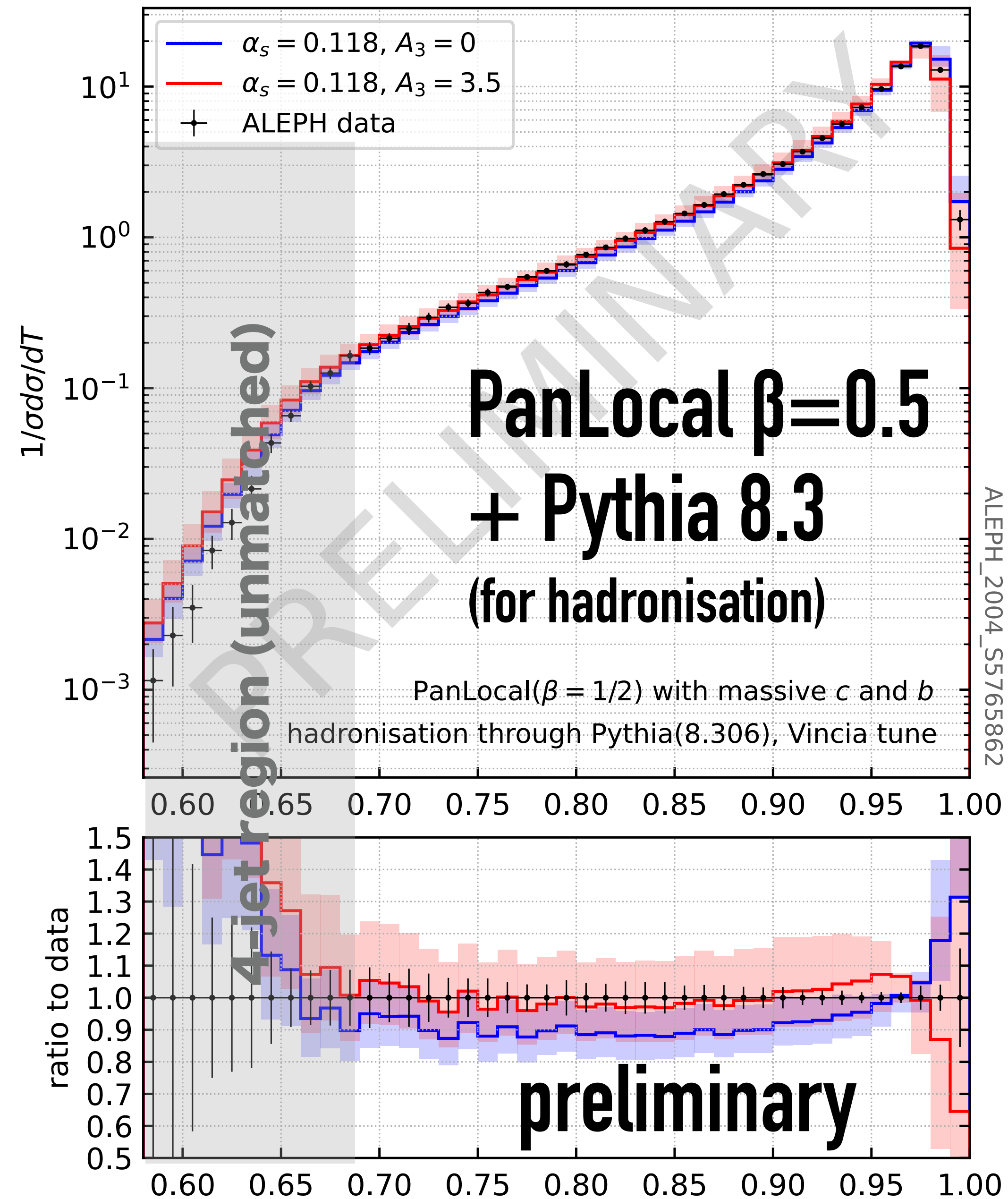
## Matching & log-accuracy

- Done correctly, **matching augments accuracy** of shower from NLL to NLL + NNDL (for event shapes)
- Done wrongly, it breaks exponentiation structure of shower (impact depends on observable)
- example with significant impact is **SoftDrop transverse momentum** (i.e. jet substructure)

$$\partial_L \Sigma_{SD}(L) = \bar{\alpha} c e^{\bar{\alpha} c L - \bar{\alpha} \Delta} - 2\bar{\alpha} L e^{-\bar{\alpha} L^2} (1 - e^{-\bar{\alpha} \Delta})$$

**spurious term from wrong matching**

# $e^+e^-$ thrust



## First comparisons to data

- ▶ we're starting with  $e^+e^-$  data
- ▶ aiming to understand nature of residual perturbative shower uncertainties
- ▶ and interplay with non-perturbative tuning
- ▶ plot includes preliminary treatment of heavy-quark masses

Medium term: making proper use of LEP data for tuning almost certainly requires NLO 3-jet accuracy.

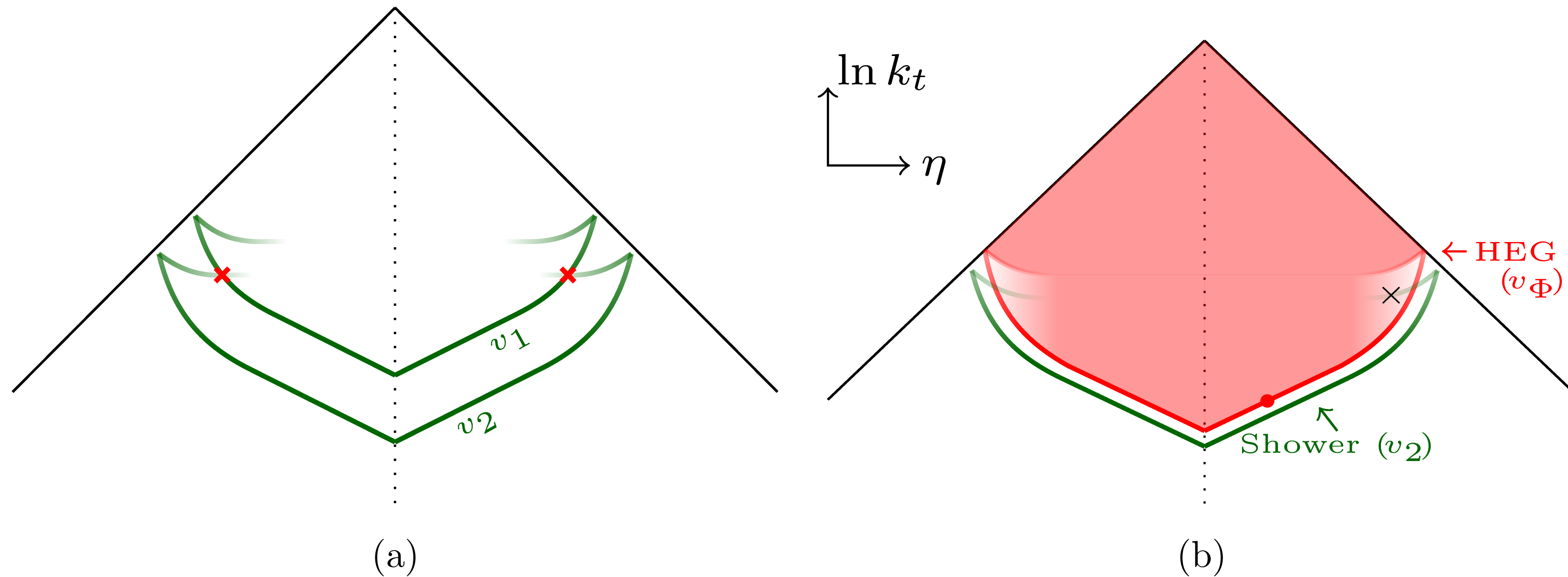
# Conclusions

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- **PanScales is first validated NLL shower (with spin & full-colour@LL/NLL)**
  - benefits of LL → NLL include reduced uncertainties (and ability to reliably estimate uncertainties)
  - multi-differential soft/collinear observables have enhanced sensitivity to NLL
  - NLL is foundation for yet higher accuracies
- **Matching is one of the next frontiers**
  - first results with NLO  $e^+e^- \rightarrow 2$  jets
  - for realistic applications we also need massive quarks and tuning
- **We're on the path towards public code**
  - exact timeline still fuzzy!

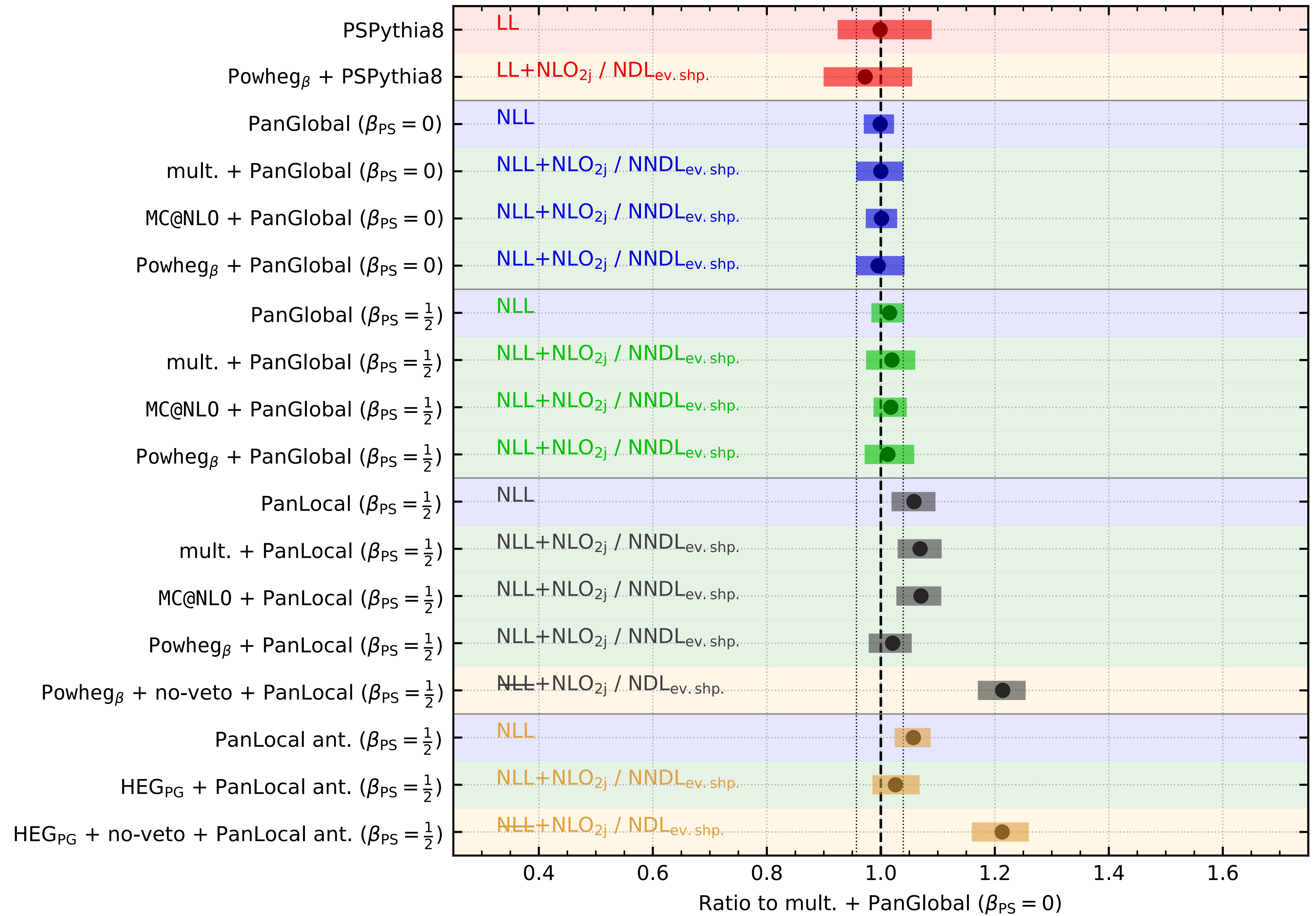


**backup**



**Figure 2:** Schematic illustration of the issue associated with gluon asymmetrisation. (a) Contours on the Lund plane, in the PanLocal family of showers, highlighting the fact that a given physical point  $X$  in the Lund plane (highlighted with a red cross) can come from two different values of  $v$ . The shading of the green curves represents the variation in radiation intensity along the contour. (b) Density plot, at each point in the Lund plane, representing schematically the fraction of the emission intensity at that point that has been excluded once the HEG has reached a given  $v$  value ( $v_\Phi$ ) without emitting, and an illustration that as the shower continues there may still be phase-space points (such as that marked with a cross) where the Sudakov has only been partially accounted for. The implications are discussed in the text.

$\sqrt{s} = 2 \text{ TeV}, SD_{z > 0.25}, \beta_{SD=0} \ln k_t/Q = -3.0$



# Matching — augment from NLL to NLL + NNLL?

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Two ways of counting logarithms

$$\ln \Sigma = \underbrace{\alpha_s^n L^{n+1}}_{\text{LL}} + \underbrace{\alpha_s^n L^n}_{\text{NLL}} + \underbrace{\alpha_s^n L^{n-1}}_{\text{NNLL}} + \dots \quad (\text{relevant when } \alpha_s L \sim 1)$$

$$\Sigma = \underbrace{\alpha_s^n L^{2n}}_{\text{DL}} + \underbrace{\alpha_s^n L^{2n-1}}_{\text{NDL}} + \underbrace{\alpha_s^n L^{2n-2}}_{\text{NNDL}} + \dots \quad (\text{relevant when } \alpha_s L^2 \sim 1)$$